

0.fit__qinlabrls.Rmd

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20170424. Major bug found. file names and strains names are inconsistent.

20160711-> Fitting RLS dataset merged by strains.

20160706-0711. Finished batch fitting of all individual RLS data sets. The fitting results showed that 'n' are often in the range of [5,7], though it is very noisy.

```
rm(list=ls())
#setwd("~/github/0.network.aging.prj.bmc/0a.rls.fitting")
setwd("~/github/bmc_netwk_aging_manuscript/R1/0.nat.rls.fitting")
library('flexsurv')
```

```
## Loading required package: survival
```

```
source("../lifespan.r")
```

Parse strains from files

```
files = list.files(path="../qinlab_rls/", pattern="rls.tab")
tmp1 = gsub("\\d{6}\\."," ", files)
redundant_strains = gsub(".rls.tab", " ", tmp1)
strains = sort( unique( redundant_strains ) )
strains
```

```
## [1] "101S"          "BY4716"          "BY4741"          "BY4742"
## [5] "BY4743"        "JSBY4741"        "M1-2"            "M13"
## [9] "M14"           "M2-8"            "M22"             "M32"
## [13] "M34"           "M5"              "M8"              "RM112N"
## [17] "S288c"          "SGU57"           "sir2D.4741a"     "sir2D.4742"
## [21] "sir2DSIR2.4742" "SK1"             "W303"            "YPS128"
## [25] "YPS163"
```

Take files from natural isolates

```
my.strains=c("101S", "M1-2", "M13", "M14", "M2-8", "M22", "M32", "M34", "M5", "M8", "RM112N", "S288c", "SGU57", "YPS163")
files2=c();
for( i in 1:length(my.strains)){
  files2 = c( files2, files[grep(my.strains[i], files)]);
}

report = data.frame(cbind(my.strains))
report$samplesize = NA; report$R=NA; report$t0=NA; report$n=NA; report$G=NA; report$longfilename=NA;

files = files2;
strains = my.strains;
```

Explore the fitting outcomes of ‘flexsurv’.

```
i=2
tb = read.table( paste("../qinlab_rls/",files[i],sep=''), sep="\t")
GompFlex = flexsurvreg(formula = Surv(tb[,1]) ~ 1, dist = 'gompertz')
WeibFlex = flexsurvreg(formula = Surv(tb[,1]) ~ 1, dist = 'weibull')
#str(GompFlex)
GompFlex$res

##              est              L95%              U95%              se
## shape 0.1687294394 0.1133678236 0.224091055 0.0282462414
## rate  0.0006950097 0.0001325189 0.003645052 0.0005876487

GompFlex$res.t

##              est              L95%              U95%              se
## shape  0.1687294  0.1133678  0.2240911 0.02824624
## rate -7.2715847 -8.9287849 -5.6143845 0.84552585

GompFlex$opt$hessian

##              shape              rate
## shape 23297.3140 757.0619
## rate   757.0619 26.0000

#str(WeibFlex)
```

Now, fit all RLS data sets by strains

```
for( i in 1:length(report[,1])){
  #for( i in 3:4){
    my.files = files[grep(strains[i], files)]
    report$longfilename[i] = paste(my.files, collapse = "::");
    tb = read.table( paste("../qinlab_rls/",my.files[1],sep=''), sep="\t")
    if( length(my.files)> 1){
      for( fi in 2:length(my.files)) {
        tmp.tb = read.table( paste("../qinlab_rls/",my.files[fi],sep=''), sep="\t")
        tb = rbind( tb, tmp.tb)
      }
    }
    report$samplesize[i] = length(tb[,1])

    GompFlex = flexsurvreg(formula = Surv(tb[,1]) ~ 1, dist = 'gompertz')
    WeibFlex = flexsurvreg(formula = Surv(tb[,1]) ~ 1, dist = 'weibull')

    report$avgLS[i] = mean(tb[,1])
    report$stdLS[i] = sd(tb[,1])
    report$CV[i] = report$stdLS[i] / report$avgLS[i]

    report$GompGFlex[i] = GompFlex$res[1,1]
    report$GompRFlex[i] = GompFlex$res[2,1]
    report$GompLogLikFlex[i] = round(GompFlex$loglik, 1)
    report$GompAICFlex[i] = round(GompFlex$AIC)
```

```

report$WeibShapeFlex[i] = WeibFlex$res[1,1]
report$WeibRateFlex[i] = WeibFlex$res[2,1]
report$WeibLogLikFlex[i] = round(WeibFlex$loglik, 1)
report$WeibAICFlex[i] = round(WeibFlex$AIC)

#set initial values
Rhat = report$GompRFlex[i]; # 'i' was missing. a bug costed HQ a whole afternoon.
Ghat = report$GompGFlex[i];
nhathat = 6;
t0= (nhathat-1)/Ghat;
fitBinom = optim ( c(Rhat, t0, nhathat), llh.binomialMortality.single.run,
                  lifespan=tb[,1],
                  #method='SANN') #SANN needs control
                  method="L-BFGS-B",
                  lower=c(1E-10, 1, 4), upper=c(1,200,20) );
report[i, c("R", "t0", "n")] = fitBinom$par[1:3]
report$G[i] = (report$n[i] - 1)/report$t0[i]
}

```

Show the results

```

#report[ grep("tBY", report$strains), ]
report

```

##	my.strains	samplesize	R	t0	n	G	
## 1	101S	85	0.001963826	36.96827	7.286027	0.17003846	
## 2	M1-2	54	0.002597778	40.44275	7.581458	0.16273519	
## 3	M13	70	0.002863446	40.56801	7.650792	0.16394178	
## 4	M14	60	0.004156533	54.65063	6.031192	0.09206101	
## 5	M2-8	105	0.003438767	42.75291	8.026908	0.16436094	
## 6	M22	60	0.004669075	46.38267	6.035812	0.10857096	
## 7	M32	60	0.001856854	35.31281	7.690560	0.18946549	
## 8	M34	58	0.002238125	31.64343	7.085632	0.19231896	
## 9	M5	166	0.003348780	74.58364	7.898541	0.09249403	
## 10	M8	60	0.001863662	31.46248	6.021022	0.15958760	
## 11	RM112N	59	0.002702475	55.93484	6.023393	0.08980795	
## 12	S288c	41	0.004995123	57.42117	7.948488	0.12100918	
## 13	SGU57	58	0.006334776	55.69961	7.714361	0.12054593	
## 14	YPS128	69	0.002045751	41.96634	6.960180	0.14202285	
## 15	YPS163	130	0.001820701	36.99506	6.820331	0.15732725	
##							longfilename
## 1			060805.101S.rls.tab::	091904.101S.rls.tab::	122004.101S.rls.tab		
## 2				030905.M1-2.rls.tab::	091904.M1-2.rls.tab		
## 3				030205.M13.rls.tab::	051704.M13.rls.tab		
## 4				030905.M14.rls.tab::	032105.M14.rls.tab		
## 5				011705.M2-8.rls.tab::	020105.M2-8.rls.tab		
## 6				030905.M22.rls.tab::	090104.M22.rls.tab		
## 7				020905.M32.rls.tab::	122004.M32.rls.tab		
## 8				010305.M34.rls.tab::	030105.M34.rls.tab		
## 9	020205.M5.rls.tab::	040805.M5.rls.tab::	041505.M5.rls.tab::	090104.M5.rls.tab::	122004.M5.rls.tab		
## 10				030205.M8.rls.tab::	030905.M8.rls.tab		
## 11				032105.RM112N.rls.tab::	042805.RM112N.rls.tab		
## 12					051704.S288c.rls.tab		
## 13				042805.SGU57.rls.tab::	091904.SGU57.rls.tab		

```
## 14 010305.YPS128.rls.tab::020105.YPS128.rls.tab
## 15 010305.YPS163.rls.tab::020905.YPS163.rls.tab::030105.YPS163.rls.tab::040805.YPS163.rls.tab
##      avgLS      stdLS      CV  GompGFlex  GompRFlex  GompLogLikFlex
## 1  31.34118  7.512772  0.2397093  0.13407292  0.0012654562  -295.0
## 2  27.83333  9.201620  0.3305971  0.12310344  0.0024494207  -193.6
## 3  26.54286  9.142488  0.3444425  0.12284897  0.0029261133  -250.1
## 4  36.55000  12.804164  0.3503191  0.09148573  0.0019510502  -233.7
## 5  24.80952  8.133614  0.3278424  0.11608390  0.0043612883  -373.3
## 6  31.83333  10.271182  0.3226549  0.10778993  0.0021454528  -222.9
## 7  27.96667  6.888868  0.2463242  0.14043277  0.0017384578  -205.6
## 8  27.01724  8.206740  0.3037593  0.15692797  0.0012896468  -198.0
## 9  36.62651  12.938747  0.3532618  0.06684902  0.0041472501  -670.1
## 10 34.93333  6.905823  0.1976858  0.15888831  0.0003653141  -201.9
## 11 44.06780  13.006450  0.2951464  0.08938574  0.0010363304  -232.0
## 12 26.26829  10.254327  0.3903690  0.08686882  0.0064512047  -154.2
## 13 23.86207  10.538898  0.4416590  0.08956763  0.0076748634  -216.5
## 14 35.00000  9.719598  0.2777028  0.11866014  0.0011041546  -252.2
## 15 34.43077  8.591449  0.2495282  0.13387276  0.0007889455  -459.6
##      GompAICFlex  WeibShapeFlex  WeibRateFlex  WeibLogLikFlex  WeibAICFlex
## 1           594           4.778139           34.15561           -291.0           586
## 2           391           3.538533           30.92356           -195.6           395
## 3           504           3.114056           29.26548           -259.1           522
## 4           471           3.361407           40.80155           -236.8           478
## 5           751           3.371375           27.61417           -368.5           741
## 6           450           3.596392           35.37118           -223.9           452
## 7           415           4.419104           30.62828           -201.4           407
## 8           400           3.985745           29.77062           -203.7           411
## 9          1344           3.098392           40.98709           -658.3          1321
## 10           408           5.872213           37.70008           -200.1           404
## 11           468           4.038465           48.63895           -233.7           471
## 12           312           2.792964           29.42942           -153.3           311
## 13           437           2.455703           26.85910           -218.2           440
## 14           508           4.294122           38.52990           -253.0           510
## 15           923           4.825655           37.62671           -460.2           924
```

```
summary(report[, c("avgLS", "t0", "n")])
```

```
##      avgLS      t0      n
## Min. :23.86 Min. :31.46 Min. :6.021
## 1st Qu.:26.78 1st Qu.:36.98 1st Qu.:6.428
## Median :31.34 Median :41.97 Median :7.286
## Mean :31.27 Mean :45.52 Mean :7.118
## 3rd Qu.:34.97 3rd Qu.:55.18 3rd Qu.:7.702
## Max. :44.07 Max. :74.58 Max. :8.027
```

Calculate lambda based on $t_0 = (1-p)/(p \text{ Lambda})$ So, $1/\text{lambda} = t_0 * p / (1-p)$

```
p = 0.7
report$One.over.lambdaP07 = report$t0 * p / (1-p)
report[, c("t0", "One.over.lambdaP07")]
```

```
##      t0 One.over.lambdaP07
## 1  36.96827           86.25929
## 2  40.44275           94.36642
## 3  40.56801           94.65870
## 4  54.65063          127.51813
```

```
## 5 42.75291          99.75678
## 6 46.38267        108.22624
## 7 35.31281         82.39657
## 8 31.64343         73.83468
## 9 74.58364        174.02849
## 10 31.46248        73.41245
## 11 55.93484        130.51462
## 12 57.42117        133.98272
## 13 55.69961        129.96576
## 14 41.96634         97.92146
## 15 36.99506         86.32181
```

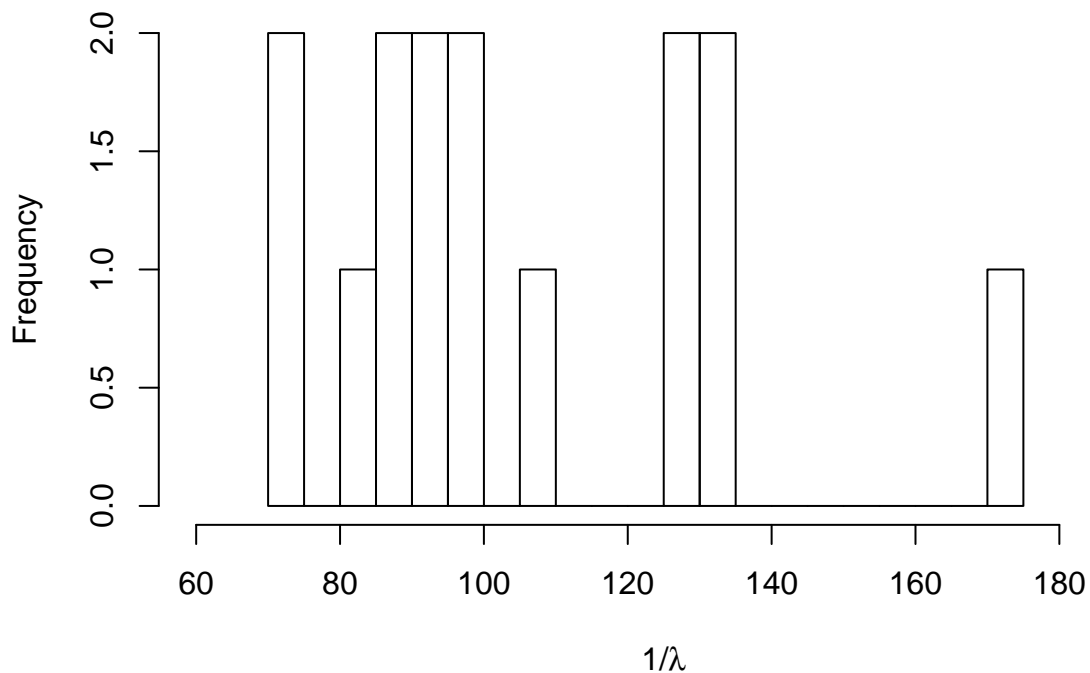
```
summary( report[, c("t0", "One.over.lambdaP07")])
```

```
##           t0           One.over.lambdaP07
##  Min.      :31.46   Min.      : 73.41
## 1st Qu.:36.98   1st Qu.: 86.29
## Median :41.97   Median : 97.92
## Mean   :45.52   Mean   :106.21
## 3rd Qu.:55.18   3rd Qu.:128.74
## Max.    :74.58   Max.    :174.03
```

Histogram of $1/\lambda$ for $p=0.7$

```
hist(report$One.over.lambdaP07, br=20, xlim=c(60,190), xlab=expression(paste("1/",lambda) ), main=expression(paste("1/",lambda)))
```

Histogram of $1/\lambda$ when $p=0.7$



```
p = 0.9
report$One.over.lambdaP09 = report$t0 * p/ (1-p)
report[, c("t0", "One.over.lambdaP09")]
```

```
##           t0 One.over.lambdaP09
## 1 36.96827    332.7144
```

```
## 2 40.44275      363.9847
## 3 40.56801      365.1121
## 4 54.65063      491.8556
## 5 42.75291      384.7762
## 6 46.38267      417.4441
## 7 35.31281      317.8153
## 8 31.64343      284.7909
## 9 74.58364      671.2527
## 10 31.46248      283.1623
## 11 55.93484      503.4135
## 12 57.42117      516.7905
## 13 55.69961      501.2965
## 14 41.96634      377.6971
## 15 36.99506      332.9555
```

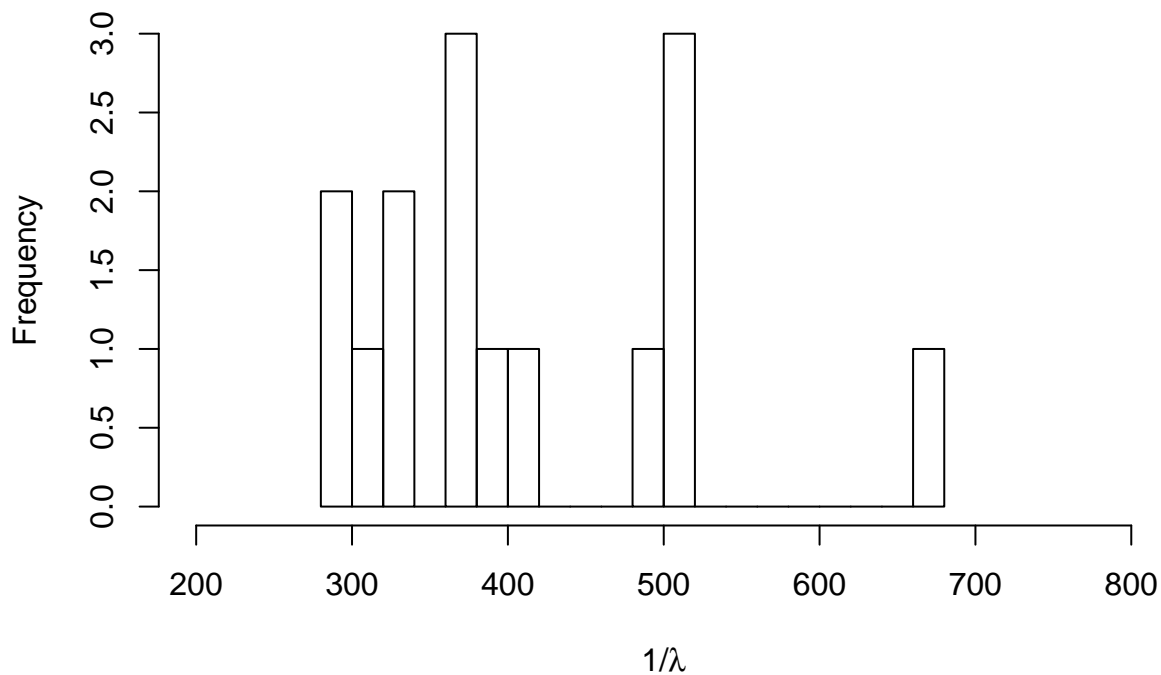
```
summary( report[, c("t0", "One.over.lambdaP09")] )
```

```
##          t0          One.over.lambdaP09
##  Min.   :31.46   Min.   :283.2
## 1st Qu.:36.98   1st Qu.:332.8
## Median :41.97   Median :377.7
## Mean   :45.52   Mean   :409.7
## 3rd Qu.:55.18   3rd Qu.:496.6
## Max.   :74.58   Max.   :671.3
```

Histogram $1/\lambda$, $p=0.9$

```
hist(report$One.over.lambdaP09, br=20, xlim=c(200,800), xlab=expression(paste("1/",lambda) ), main=expression(paste("Histogram of 1/",lambda)))
```

Histogram of $1/\lambda$ when $p=0.9$



Explorative analysis

```
# my.strains=c("101S", "BY4743", "M1-2", "M13", "M14", "M2-8", "M22", "M32", "M34", "M5", "M8", "RM112N", "S288c",  
#my.strains=c("101S", "M1-2", "M13", "M14", "M2-8", "M22", "M32", "M34", "M5", "M8", "RM112N", "S288c", "SGU57", "  
report2 = report  
summary(lm(log10(report2$GompRFlex) ~ report2$GompGFlex))
```

```
##  
## Call:  
## lm(formula = log10(report2$GompRFlex) ~ report2$GompGFlex)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -0.50796 -0.22010 -0.03155  0.20504  0.36320   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept)    -1.6976     0.3278  -5.179 0.000177 ***  
## report2$GompGFlex -8.7148     2.7614  -3.156 0.007585 **  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 0.2789 on 13 degrees of freedom  
## Multiple R-squared:  0.4338, Adjusted R-squared:  0.3902   
## F-statistic:  9.96 on 1 and 13 DF,  p-value: 0.007585
```

```
summary(lm(log10(report2$R) ~ report2$GompGFlex))
```

```
##  
## Call:  
## lm(formula = log10(report2$R) ~ report2$GompGFlex)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -0.16896 -0.09699  0.01555  0.08156  0.21625   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept)    -1.9873     0.1451 -13.699 4.21e-09 ***  
## report2$GompGFlex -4.7701     1.2223  -3.903 0.00182 **  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 0.1234 on 13 degrees of freedom  
## Multiple R-squared:  0.5395, Adjusted R-squared:  0.5041   
## F-statistic: 15.23 on 1 and 13 DF,  p-value: 0.001817
```

```
summary(lm(log10(report2$R) ~ report2$G)) #G from t0 and n
```

```
##  
## Call:  
## lm(formula = log10(report2$R) ~ report2$G)  
##  
## Residuals:
```

```

##           Min           1Q       Median           3Q           Max
## -0.191584 -0.112059  0.002454  0.085419  0.274808
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -2.0949      0.1574 -13.313 5.96e-09 ***
## report2$G    -3.1369      1.0797  -2.905  0.0123 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1417 on 13 degrees of freedom
## Multiple R-squared:  0.3937, Adjusted R-squared:  0.3471
## F-statistic: 8.441 on 1 and 13 DF,  p-value: 0.01228
summary(lm(report2$GompGFlex ~ report2$G)) #good agreement bwteen GFlex and G from binomial modeling

##
## Call:
## lm(formula = report2$GompGFlex ~ report2$G)
##
## Residuals:
##           Min           1Q       Median           3Q           Max
## -0.0158806 -0.0099107 -0.0007003  0.0080448  0.0311292
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.02065      0.01524   1.355   0.199
## report2$G    0.67115      0.10459   6.417 2.28e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.01372 on 13 degrees of freedom
## Multiple R-squared:  0.7601, Adjusted R-squared:  0.7416
## F-statistic: 41.18 on 1 and 13 DF,  p-value: 2.281e-05
summary(lm(log10(report2$R) ~ report2$t0)) #G from t0 and n

##
## Call:
## lm(formula = log10(report2$R) ~ report2$t0)
##
## Residuals:
##           Min           1Q       Median           3Q           Max
## -0.218092 -0.103701  0.003555  0.086222  0.242351
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.982154      0.143440 -20.790 2.33e-11 ***
## report2$t0   0.009722      0.003055   3.183  0.0072 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1364 on 13 degrees of freedom
## Multiple R-squared:  0.4379, Adjusted R-squared:  0.3947
## F-statistic: 10.13 on 1 and 13 DF,  p-value: 0.007204

```



```
summary(lm(log10(report2$R) ~ report2$n)) #G from t0 and n

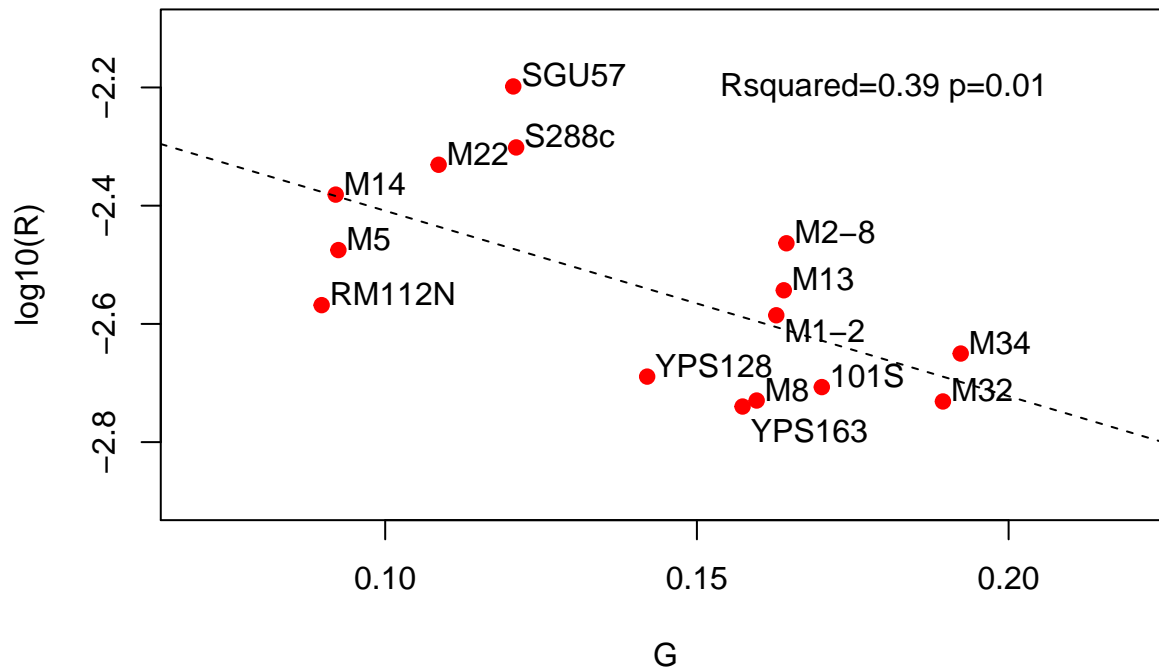
##
## Call:
## lm(formula = log10(report2$R) ~ report2$n)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.21173 -0.14773 -0.02223  0.12030  0.32038
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.78978    0.44916  -6.211 3.16e-05 ***
## report2$n    0.03515    0.06276   0.560  0.585
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1798 on 13 degrees of freedom
## Multiple R-squared:  0.02355,    Adjusted R-squared:  -0.05156
## F-statistic: 0.3136 on 1 and 13 DF,  p-value: 0.585
```

Strehler-Mildvan correlation in natural isolates

```
plot( log10(report2$R) ~ report2$G, pch=19, col='red', xlab='G', ylab='log10(R)',
      xlim=c(0.07, 0.22), ylim=c(-2.9, -2.1),
      main="Strehler-Mildvan correlation in yeast wild isolates")
m = lm(log10(report2$R) ~ report2$G)
abline (m, col='black', lty=2);
text(0.18, -2.2, "Rsquared=0.39 p=0.01")

my.x = report2$G +0.0013 ; my.y = log10(report2$R) ;
names(my.x) = report2$my.strains; names(my.y) = report2$my.strains;
my.y[c("YPS163", "M1-2" )]=c(-2.8, -2.63)
text(my.x,my.y, report2$my.strains, adj=c(0,0) )
```

Strehler–Mildvan correlation in yeast wild isolates



```
summary(lm(log10(report2$R) ~ report2$G)) #G from t0 and n
```

```
##
## Call:
## lm(formula = log10(report2$R) ~ report2$G)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.191584 -0.112059  0.002454  0.085419  0.274808
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -2.0949     0.1574 -13.313 5.96e-09 ***
## report2$G    -3.1369     1.0797  -2.905  0.0123 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1417 on 13 degrees of freedom
## Multiple R-squared:  0.3937, Adjusted R-squared:  0.3471
## F-statistic: 8.441 on 1 and 13 DF, p-value: 0.01228
```

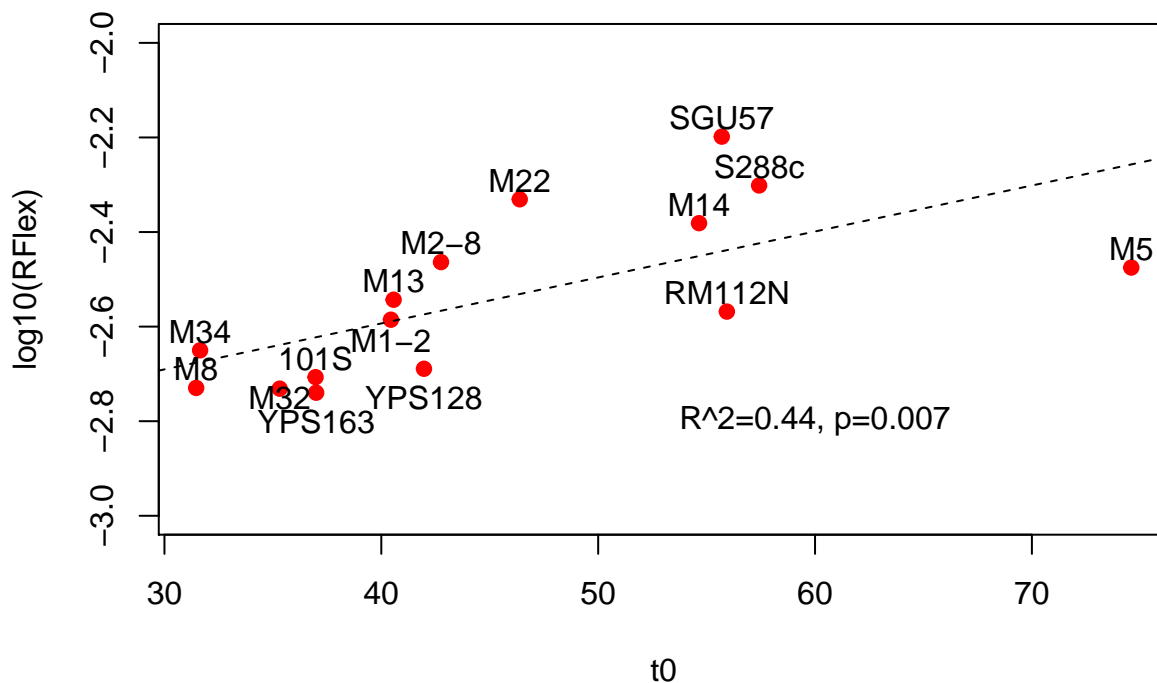
```
summary(lm(log10(report2$GompRFlex) ~ report2$GompGFlex)) #G from t0 and n
```

```
##
## Call:
## lm(formula = log10(report2$GompRFlex) ~ report2$GompGFlex)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.50796 -0.22010 -0.03155  0.20504  0.36320
##
```

```
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -1.6976    0.3278  -5.179 0.000177 ***
## report2$GompGFlex -8.7148    2.7614  -3.156 0.007585 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2789 on 13 degrees of freedom
## Multiple R-squared:  0.4338, Adjusted R-squared:  0.3902
## F-statistic:  9.96 on 1 and 13 DF,  p-value: 0.007585
```

plot $\log_{10}(R) \sim t_0$

```
plot( log10(report2$R) ~ report2$t0, col='red', pch=19, xlab='t0', ylab='log10(RFlex)', ylim=c(-3,-2))
my.x = report2$t0; my.y = log10(report2$R) + 0.04;
names(my.x) = report2$my.strains; names(my.y) = report2$my.strains;
my.y[c("M32", "YPS163", "YPS128", "M1-2" )]=c(-2.75, -2.8, -2.75, -2.63)
text(my.x,my.y, report2$my.strains )
m = lm( log10(report2$R) ~ report2$t0 )
abline (m, col='black', lty=2);
text( 60, -2.8, "R^2=0.44, p=0.007")
```



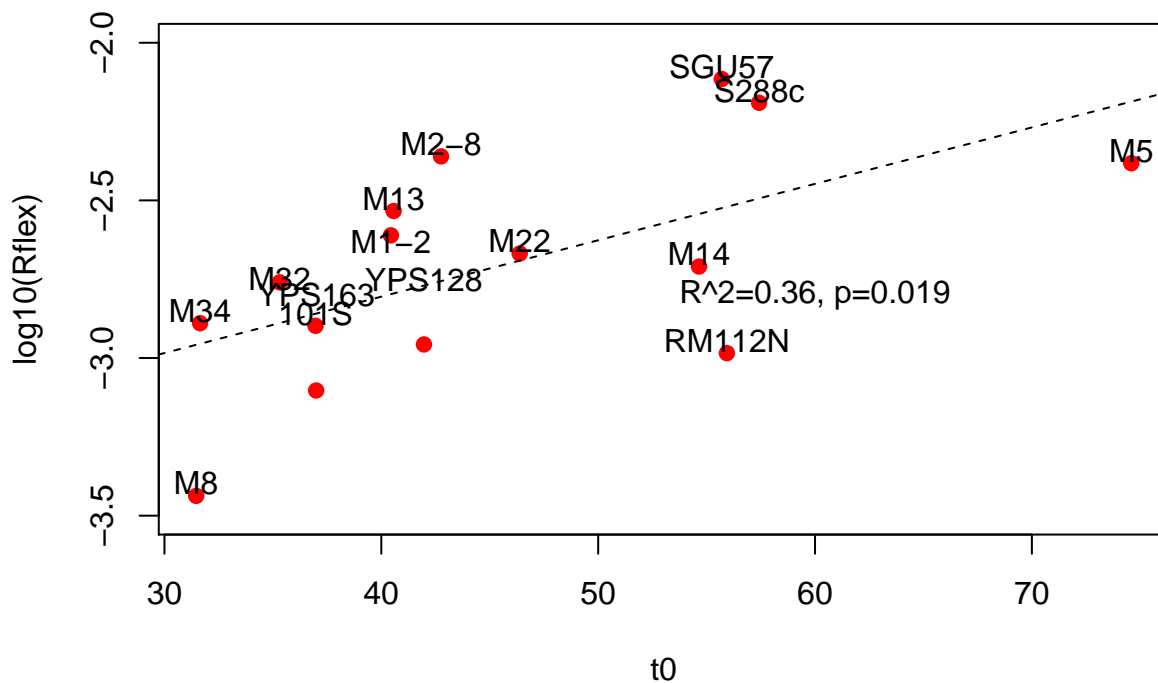
```
summary(m)

##
## Call:
## lm(formula = log10(report2$R) ~ report2$t0)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.218092 -0.103701  0.003555  0.086222  0.242351
```

```
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.982154   0.143440 -20.790 2.33e-11 ***
## report2$t0   0.009722   0.003055   3.183  0.0072 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1364 on 13 degrees of freedom
## Multiple R-squared:  0.4379, Adjusted R-squared:  0.3947
## F-statistic: 10.13 on 1 and 13 DF,  p-value: 0.007204
```

plot log10(GompRFlex) ~ t0

```
plot( log10(report2$GompRFlex) ~ report2$t0, col='red', pch=19, xlab='t0', ylab='log10(Rflex)', ylim=c(
my.x = report2$t0; my.y = log10(report2$GompRFlex) + 0.04;
names(my.x) = report2$my.strains; names(my.y) = report2$my.strains;
my.y[c("M32", "YPS163", "YPS128", "M1-2" )]=c(-2.75, -2.8, -2.75, -2.63)
text(my.x,my.y, report2$my.strains )
m = lm( log10(report2$GompRFlex) ~ report2$t0 )
abline (m, col='black', lty=2);
text( 60, -2.8, "R^2=0.36, p=0.019")
```



```
summary(m)

##
## Call:
## lm(formula = log10(report2$GompRFlex) ~ report2$t0)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```

```
## -0.47921 -0.19118 0.02271 0.22402 0.40957
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.521012  0.312535 -11.266 4.44e-08 ***
## report2$t0  0.017891  0.006656  2.688  0.0186 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2972 on 13 degrees of freedom
## Multiple R-squared:  0.3572, Adjusted R-squared:  0.3078
## F-statistic: 7.225 on 1 and 13 DF, p-value: 0.01862
```

Could t0 be the cause of logR-G correlation?

Partial regression on $G \sim \log(R) + t_0$.

```
summary(lm( log10(report2$GompRFlex) ~ report2$t0 + report2$GompGFlex )) #poor
```

```
##
## Call:
## lm(formula = log10(report2$GompRFlex) ~ report2$t0 + report2$GompGFlex)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.52342 -0.24509  0.04331  0.22083  0.34492
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -0.002954   2.387477  -0.001    0.999
## report2$t0     -0.017838   0.024884  -0.717    0.487
## report2$GompGFlex -16.337520  10.999937  -1.485    0.163
##
## Residual standard error: 0.2843 on 12 degrees of freedom
## Multiple R-squared:  0.457, Adjusted R-squared:  0.3666
## F-statistic: 5.051 on 2 and 12 DF, p-value: 0.02562
```

```
summary(lm( log10(report2$GompGFlex) ~ report2$t0 + report2$GompRFlex )) #good
```

```
##
## Call:
## lm(formula = log10(report2$GompGFlex) ~ report2$t0 + report2$GompRFlex)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.014137 -0.009475 -0.003030  0.002393  0.027857
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -0.5486398  0.0159799 -34.33 2.37e-13 ***
## report2$t0     -0.0086467  0.0003984 -21.70 5.36e-11 ***
## report2$GompRFlex -2.2235872  2.2233354  -1.00  0.337
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.01458 on 12 degrees of freedom
## Multiple R-squared: 0.984, Adjusted R-squared: 0.9814
## F-statistic: 370 on 2 and 12 DF, p-value: 1.652e-11

#summary(lm( report2$G ~ log10(report2$R) + report2$t0 ))
#summary(lm( report2$G ~ report2$t0 + log10(report2$R) ))
summary(lm( report2$GompGFlex ~ report2$t0 + log10(report2$R) ))

##
## Call:
## lm(formula = report2$GompGFlex ~ report2$t0 + log10(report2$R))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.007884 -0.003343 -0.002527  0.001311  0.011427
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    0.1379103  0.0399225   3.454  0.00477 **
## report2$t0     -0.0019345  0.0001938  -9.983 3.65e-07 ***
## log10(report2$R) -0.0259630  0.0131902  -1.968  0.07257 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.006486 on 12 degrees of freedom
## Multiple R-squared: 0.9505, Adjusted R-squared: 0.9423
## F-statistic: 115.2 on 2 and 12 DF, p-value: 1.469e-08

summary(lm( report2$GompGFlex ~ report2$t0 + log10(report2$GompRFlex) ))

##
## Call:
## lm(formula = report2$GompGFlex ~ report2$t0 + log10(report2$GompRFlex))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.008037 -0.004385 -0.001282  0.001773  0.012763
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    0.1818701  0.0236582   7.687 5.64e-06 ***
## report2$t0     -0.0020169  0.0001916 -10.529 2.05e-07 ***
## log10(report2$GompRFlex) -0.0095046  0.0063994  -1.485  0.163
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.006857 on 12 degrees of freedom
## Multiple R-squared: 0.9447, Adjusted R-squared: 0.9355
## F-statistic: 102.5 on 2 and 12 DF, p-value: 2.861e-08
```

Mediation test on Gflex \leftarrow t0 \leftarrow RFlex

Hong thinks this gives positive result.

```

library(mediation)

## Loading required package: MASS
## Loading required package: Matrix
## Loading required package: mvtnorm
## Loading required package: sandwich
## mediation: Causal Mediation Analysis
## Version: 4.4.5

set.seed(20170801)
report2$log10GompRFlex = log10(report2$GompRFlex)
med.fit = lm(t0 ~ log10GompRFlex, data=report2)
summary(med.fit)

##
## Call:
## lm(formula = t0 ~ log10GompRFlex, data = report2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.2238  -7.6956  -0.6106   1.5195  22.5871
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    99.564     20.269   4.912 0.000284 ***
## log10GompRFlex  19.967       7.429   2.688 0.018617 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.928 on 13 degrees of freedom
## Multiple R-squared:  0.3572, Adjusted R-squared:  0.3078
## F-statistic: 7.225 on 1 and 13 DF,  p-value: 0.01862

out.fit = lm(GompGFlex ~ t0 + log10GompRFlex, data=report2)
summary(out.fit)

##
## Call:
## lm(formula = GompGFlex ~ t0 + log10GompRFlex, data = report2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.008037 -0.004385 -0.001282  0.001773  0.012763
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    0.1818701  0.0236582   7.687 5.64e-06 ***
## t0             -0.0020169  0.0001916 -10.529 2.05e-07 ***
## log10GompRFlex -0.0095046  0.0063994  -1.485   0.163
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.006857 on 12 degrees of freedom

```

```
## Multiple R-squared:  0.9447, Adjusted R-squared:  0.9355
## F-statistic: 102.5 on 2 and 12 DF,  p-value: 2.861e-08

med.out <- mediate(med.fit, out.fit, treat = "log10GompRFlex", mediator = "t0", robustSE = TRUE, sims =
summary(med.out))

##
## Causal Mediation Analysis
##
## Quasi-Bayesian Confidence Intervals
##
##           Estimate 95% CI Lower 95% CI Upper p-value
## ACME           -0.04383    -0.08096    -0.01  <2e-16 ***
## ADE            -0.00718    -0.02469     0.01   0.46
## Total Effect   -0.05101    -0.08276    -0.02  <2e-16 ***
## Prop. Mediated  0.86767     0.46191     1.23  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Sample Size Used: 15
##
##
## Simulations: 100
```

Mediation test 2 on Rflex \leftarrow t0 \leftarrow GFlex

Hong thinks this is negative result.

```
med.fit = lm(t0 ~ GompGFlex, data=report2)
summary(med.fit)

##
## Call:
## lm(formula = t0 ~ GompGFlex, data = report2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.6401 -1.9424 -0.8670 -0.0658  8.1513
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   94.999      3.723   25.52 1.72e-12 ***
## GompGFlex    -427.325     31.369  -13.62 4.50e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.168 on 13 degrees of freedom
## Multiple R-squared:  0.9345, Adjusted R-squared:  0.9295
## F-statistic: 185.6 on 1 and 13 DF,  p-value: 4.503e-09

out.fit = lm(log10GompRFlex ~ t0 + GompGFlex, data=report2)
summary(out.fit)

##
## Call:
```

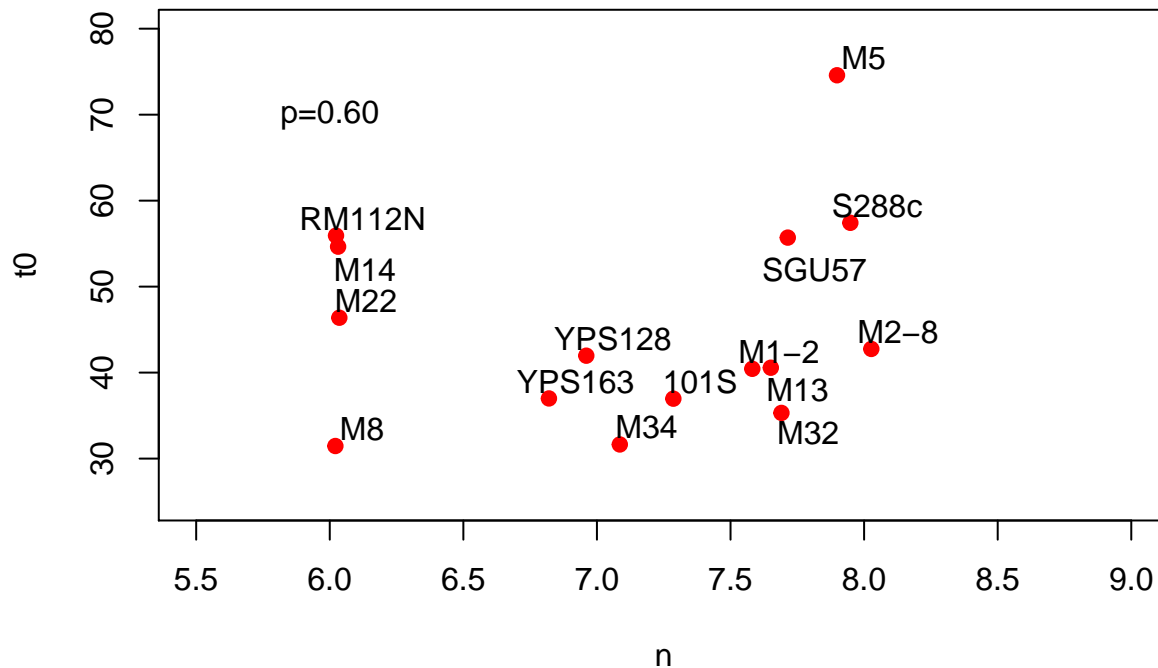


```
## lm(formula = log10GompRFlex ~ t0 + GompGFlex, data = report2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.52342 -0.24509  0.04331  0.22083  0.34492
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.002954    2.387477  -0.001    0.999
## t0            -0.017838    0.024884  -0.717    0.487
## GompGFlex     -16.337520   10.999937  -1.485    0.163
##
## Residual standard error: 0.2843 on 12 degrees of freedom
## Multiple R-squared:  0.457, Adjusted R-squared:  0.3666
## F-statistic: 5.051 on 2 and 12 DF,  p-value: 0.02562
med.out <- mediate(med.fit, out.fit, treat = "GompGFlex", mediator = "t0", robustSE = TRUE, sims = 100)
summary(med.out)

##
## Causal Mediation Analysis
##
## Quasi-Bayesian Confidence Intervals
##
##              Estimate 95% CI Lower 95% CI Upper p-value
## ACME                6.454    -14.468     31.46   0.74
## ADE               -15.052    -45.810      8.83   0.18
## Total Effect       -8.598    -18.553     -1.06   0.04 *
## Prop. Mediated     -0.526     -9.794      3.54   0.74
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Sample Size Used: 15
##
##
## Simulations: 100
```

Plot initial virtula life ~ n (average interactions)

```
plot( report2$t0 ~ report2$n, col='red', xlim=c(5.5, 9), ylim=c(25, 80), pch=19, xlab='n', ylab='t0')
my.x = report2$n + 0.1; my.y = report2$t0 + 2;
names(my.x) = report2$my.strains; names(my.y) = report2$my.strains;
my.y[c("M14", "SGU57", "M32", "M13" )]=c(52, 52, 33, 38)
text(my.x,my.y, report2$my.strains )
text(6, 70, "p=0.60")
```



```
summary(lm(log10(report2$t0) ~ report2$n)) #G from t0 and n
```

```
##
## Call:
## lm(formula = log10(report2$t0) ~ report2$n)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.14438 -0.07600 -0.03324  0.09232  0.21110
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  1.49752    0.27584   5.429 0.000115 ***
## report2$n    0.02077    0.03854   0.539 0.599159
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1104 on 13 degrees of freedom
## Multiple R-squared:  0.02184,    Adjusted R-squared:  -0.0534
## F-statistic: 0.2903 on 1 and 13 DF,  p-value: 0.5992
```

Gompert versus Weibull? AIC: smaller is better (for information loss)

```
report$BestModel = ifelse(report$GompAICFlex < report$WeibAICFlex, "Gomp", "Weib")
report$BestModel = ifelse(abs(report$GompAICFlex - report$WeibAICFlex)<2, "<2", report$BestModel)
```

CV ~ Gomp and Weibull? How does noises influence likelihood of Gompertz and Weibull fitting?

```
summary(lm(report$CV ~ report$BestModel ))
```

```
##
## Call:
## lm(formula = report$CV ~ report$BestModel)
##
## Residuals:
```

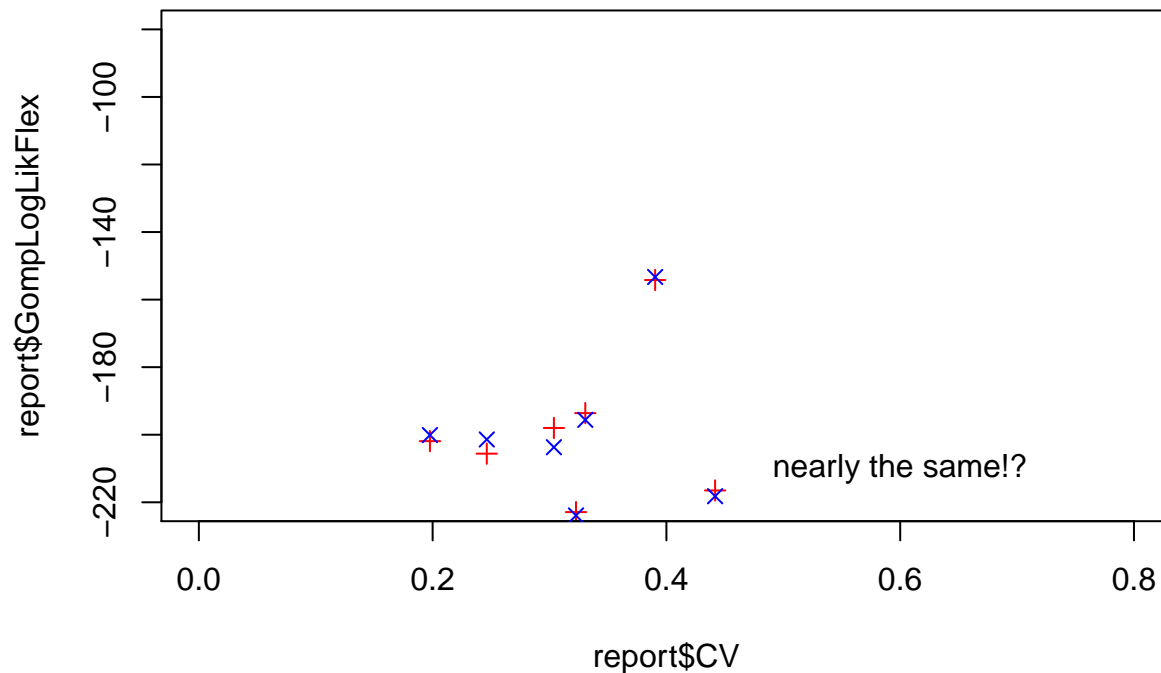
```
##      Min      1Q   Median      3Q      Max
## -0.07528 -0.03570 -0.01063  0.03596  0.10837
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      0.31995    0.04309   7.426 7.99e-06 ***
## report$BestModelGomp  0.01334    0.04817   0.277   0.787
## report$BestModelWeib -0.04698    0.05098  -0.922   0.375
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06093 on 12 degrees of freedom
## Multiple R-squared:  0.2032, Adjusted R-squared:  0.07043
## F-statistic:  1.53 on 2 and 12 DF,  p-value: 0.2559
summary(lm(report$CV ~ report$WeibLogLikFlex ))
```

```
##
## Call:
## lm(formula = report$CV ~ report$WeibLogLikFlex)
##
## Residuals:
##      Min      1Q   Median      3Q      Max
## -0.11400 -0.04749  0.01106  0.03587  0.13004
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.124e-01  4.099e-02   7.623 3.78e-06 ***
## report$WeibLogLikFlex 3.708e-06  1.347e-04   0.028   0.978
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06558 on 13 degrees of freedom
## Multiple R-squared:  5.83e-05, Adjusted R-squared:  -0.07686
## F-statistic: 0.000758 on 1 and 13 DF,  p-value: 0.9785
summary(lm(report$CV ~ report$GompLogLikFlex ))
```

```
##
## Call:
## lm(formula = report$CV ~ report$GompLogLikFlex)
##
## Residuals:
##      Min      1Q   Median      3Q      Max
## -0.11419 -0.04729  0.01091  0.03576  0.12988
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.131e-01  4.023e-02   7.785 3.01e-06 ***
## report$GompLogLikFlex 6.258e-06  1.316e-04   0.048   0.963
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06558 on 13 degrees of freedom
## Multiple R-squared:  0.0001739, Adjusted R-squared:  -0.07674
```

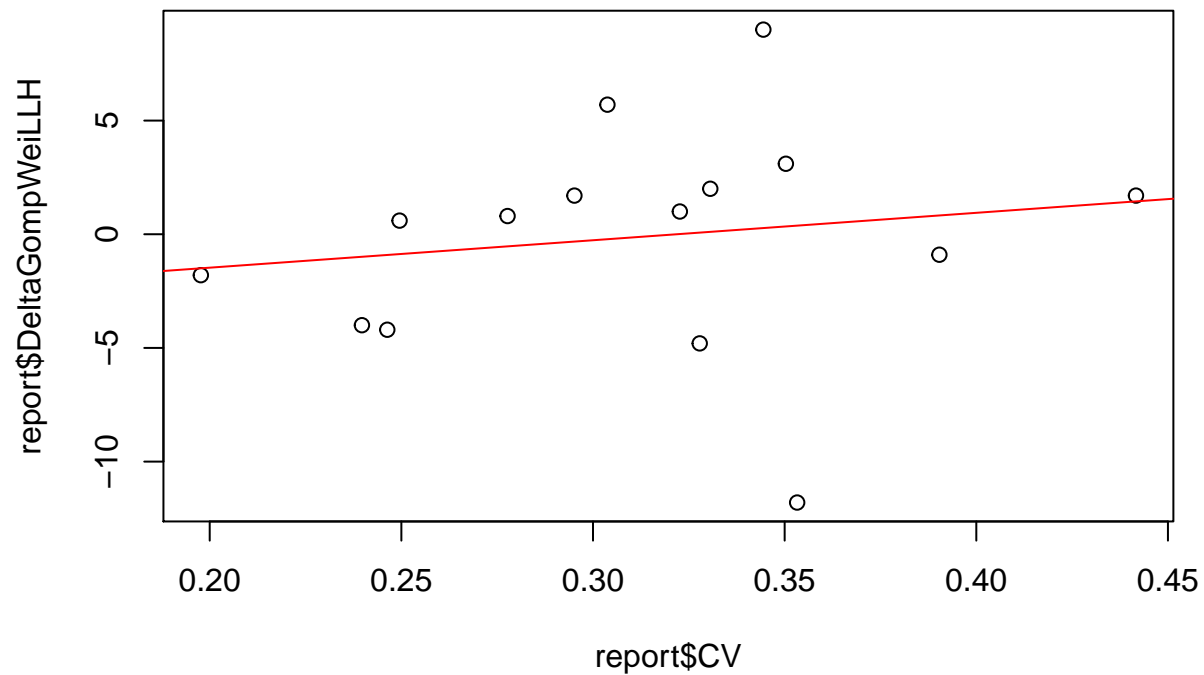
```
## F-statistic: 0.002261 on 1 and 13 DF, p-value: 0.9628
summary(lm(report$CV ~ (report$GompLogLikFlex - report$WeibLogLikFlex)))

##
## Call:
## lm(formula = report$CV ~ (report$GompLogLikFlex - report$WeibLogLikFlex))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.11419 -0.04729  0.01091  0.03576  0.12988
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.131e-01  4.023e-02   7.785 3.01e-06 ***
## report$GompLogLikFlex 6.258e-06  1.316e-04   0.048   0.963
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06558 on 13 degrees of freedom
## Multiple R-squared:  0.0001739, Adjusted R-squared:  -0.07674
## F-statistic: 0.002261 on 1 and 13 DF, p-value: 0.9628
plot( report$GompLogLikFlex ~ report$CV, col="red", pch=3, xlim=c(0, 0.8), ylim=c(-220, -80))
points( report$CV, report$WeibLogLikFlex, col="blue", pch=4)
m1 = lm( report$GompLogLikFlex ~ report$CV)
m2 = lm( report$WeibLogLikFlex ~ report$CV)
abline( m1, col="red", lty=2)
abline( m2, col='blue', lty=1)
text(0.6, -210, "nearly the same!?")
```



The QIN-RLS data suggested that noisy system signal prefer Gompertz model, based on GG01 theory. Notice that CV measures distribution of system signals and are different from white noises (residues)

```
report$DeltaGompWeiLLH = report$GompLogLikFlex - report$WeibLogLikFlex
plot( report$DeltaGompWeiLLH ~ report$CV )
m3 = lm( report$DeltaGompWeiLLH ~ report$CV)
abline(m3, col='red')
```



TODO: Calculate the white noises (fitting errors) using the fitting residues for Gompertz and Weibull models.

```
# report$residues ??
```

Output

```
#write.csv(report2, file = 'sandbox/_report_qinlab_natural_isolates_rls.csv', row.names = FALSE)
```