

Communicating Sequential Processes

Syntax

Syntax

- **Destination!port(e1, ..., en);**



Syntax

- **Destination!port(e₁, ..., e_n);**



- **Source?port(x₁, ..., x_n);**



Example: Copy

West

East

Example: Copy

West

East

x=

Example: Copy

West

Copy

East
x=

```
process Copy {
```

Example: Copy

West

Copy
c=

East
x=

```
process Copy {  
    char c;
```

Example: Copy



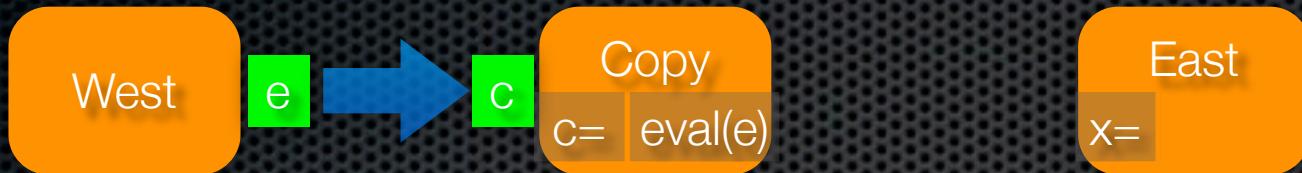
```
process Copy {  
    char c;  
    do true ->  
        West?c; # input char from West
```

Example: Copy



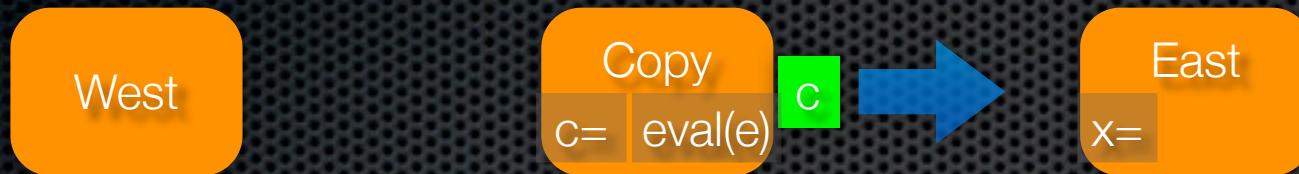
```
process Copy {  
    char c;  
    do true ->  
        West?c; # input char from West
```

Example: Copy



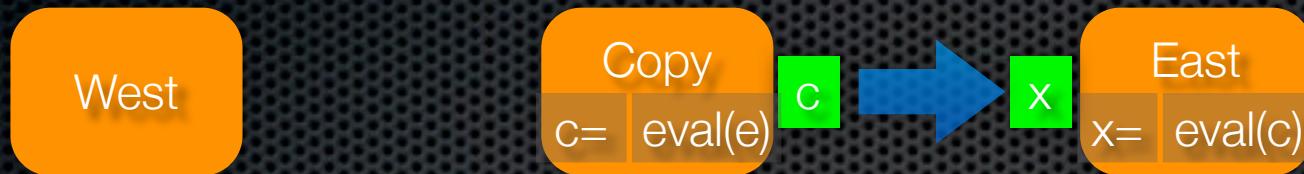
```
process Copy {  
    char c;  
    do true ->  
        West?c; # input char from West
```

Example: Copy



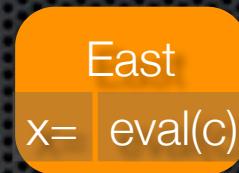
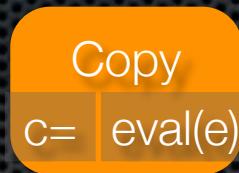
```
process Copy {  
    char c;  
    do true ->  
        West?c; # input char from West  
        East!c; # output char to East
```

Example: Copy



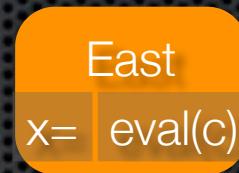
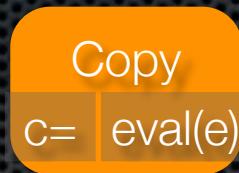
```
process Copy {  
    char c;  
    do true ->  
        West?c; # input char from West  
        East!c; # output char to East
```

Example: Copy



```
process Copy {  
    char c;  
    do true ->  
        West?c; # input char from West  
        East!c; # output char to East  
    od}
```

Example: Copy



```
process Copy {  
    char c;  
    do true ->  
        West?c; # input char from West  
        East!c; # output char to East  
    od  
}
```

Example: GCD

```
process GCD {  
    int id, x, y;  
  
    do true ->  
        Client[*] ? args(id, x, y); # input a "call"  
  
        # repeat the following until x == y  
        do x > y -> x = x - y;  
        [ ] x < y -> y = y - x;  
        od  
  
        Client[id] ! result(x); # return the result  
    od  
}
```

Example: GCD

```
process GCD {  
    int id, x, y;  
    do true -> Any Source  
        Client[*] ? args(id, x, y); # input a "call"  
        # repeat the following until x == y  
        do x > y -> x = x - y;  
        [ ] x < y -> y = y - x;  
    od  
    Client[id] ! result(x); # return the result  
od  
}
```

Example: GCD

```
process GCD {  
    int id, x, y;  
  
    do true ->  
        Client[*] ? args(id, x, y); # input a "call"  
  
        # repeat the following until x == y  
        do x > y -> x = x - y;  
        [ ] x < y -> y = y - x;  
        od  
  
        Client[id] ! result(x); # return the result  
    od  
}
```

Nondeterministic
Choice

Example: GCD

```
process GCD {  
    int id, x, y;  
  
    do true ->  
        Client[*] ? args(id, x, y);    # input a "call"  
  
        # repeat the following until x == y  
        do x > y -> x = x - y;  
        [ ] x < y -> y = y - x;  
        od  
        Client[id] ! result(x); # return the result  
    od  
}
```

Destination

Client[id] ! result(x); # return the result

Guarded Communication

Guarded Communication

- Syntax: $B; C \rightarrow S;$

Guarded Communication

- Syntax: $B; C \rightarrow S;$
- Example:

```
process Copy {  
    char c;  
    do West?c -> East!c; od  
}
```

Buffering I

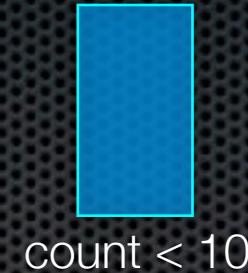
```
process Copy {  
    char c1, c2;  
  
    West ? c1;  
  
    do West ? c2 -> East ! c1; c1 = c2;  
    [ ] East ! c1 -> West ? c1;  
    od  
}
```

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```



West ? buffer [rear]

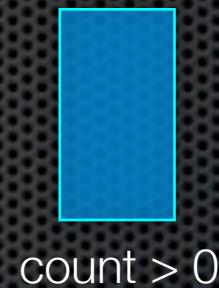
...

East ! buffer [front]

...

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {
```

```
    char buffer[10];
```

```
    int front = 0, rear = 0, count = 0;
```

```
    do count < 10; West ? buffer[rear] ->
```

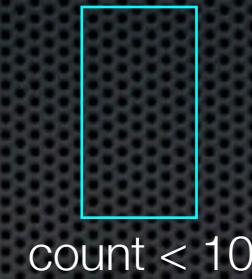
```
        count = count+1; rear = (rear + 1) mod 10;
```

```
        [ ] count > 0; East ! buffer[front] ->
```

```
            count = count - 1; front = (front + 1) mod 10;
```

```
    od
```

```
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {
```

```
    char buffer[10];
```

```
    int front = 0, rear = 0, count = 0;
```

```
    do count < 10; West ? buffer[rear] ->
```

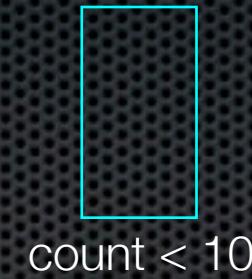
```
        count = count+1; rear = (rear + 1) mod 10;
```

```
        [ ] count > 0; East ! buffer[front] ->
```

```
            count = count - 1; front = (front + 1) mod 10;
```

```
    od
```

```
}
```



West ? buffer [rear]

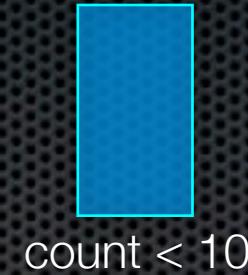
...

East ! buffer [front]

...

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```



West ? buffer [rear]

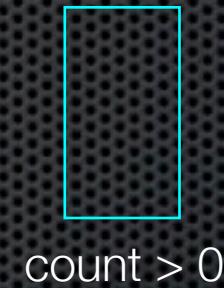
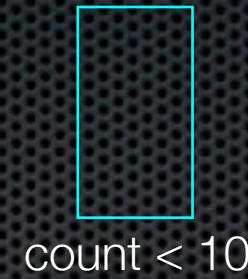
...

East ! buffer [front]

...

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {
```

```
    char buffer[10];
```

```
    int front = 0, rear = 0, count = 0;
```

```
    do count < 10; West ? buffer[rear] ->
```

```
        count = count+1; rear = (rear + 1) mod 10;
```

```
        [ ] count > 0; East ! buffer[front] ->
```

```
            count = count - 1; front = (front + 1) mod 10;
```

```
    od
```

```
}
```



West ? buffer [rear]

...

OR

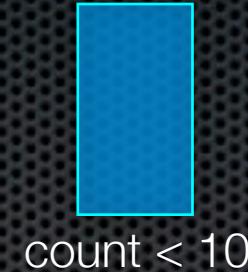


East ! buffer [front]

...

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {
```

```
    char buffer[10];
```

```
    int front = 0, rear = 0, count = 0;
```

```
    do count < 10; West ? buffer[rear] ->
```

```
        count = count+1; rear = (rear + 1) mod 10;
```

```
        [ ] count > 0; East ! buffer[front] ->
```

```
            count = count - 1; front = (front + 1) mod 10;
```

```
    od
```

```
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {
```

```
    char buffer[10];
```

```
    int front = 0, rear = 0, count = 0;
```

```
    do count < 10; West ? buffer[rear] ->
```

```
        count = count+1; rear = (rear + 1) mod 10;
```

```
        [ ] count > 0; East ! buffer[front] ->
```

```
            count = count - 1; front = (front + 1) mod 10;
```

```
    od
```

```
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {
```

```
    char buffer[10];
```

```
    int front = 0, rear = 0, count = 0;
```

```
    do count < 10; West ? buffer[rear] ->
```

```
        count = count+1; rear = (rear + 1) mod 10;
```

```
        [ ] count > 0; East ! buffer[front] ->
```

```
            count = count - 1; front = (front + 1) mod 10;
```

```
    od
```

```
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Buffering II

```
process Copy {  
    char buffer[10];  
    int front = 0, rear = 0, count = 0;  
    do count < 10; West ? buffer[rear] ->  
        count = count+1; rear = (rear + 1) mod 10;  
    [ ] count > 0; East ! buffer[front] ->  
        count = count - 1; front = (front + 1) mod 10;  
    od  
}
```



West ? buffer [rear]

...

East ! buffer [front]

...

Resource Allocator

```
process Allocator {  
    int avail = MAXUNITS;  
    set units = initial values;  
    int index, unitid;  
    do avail > 0; Client[*] ? acquire (index) ->  
        avail--; remove (units, unitid);  
        Client [index] ! reply (unitid);  
    [ ] Client[*] ? release (index, unitid) ->  
        avail++; insert (units, unitid);  
    od  
}
```

Sieve of Erastosthenes

Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]!i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->       # receive next candidate
        if (next mod p) != 0 -> # if it might be prime,
            Sieve[i+1]!next;    #     pass it on
        fi
    od
}
```

Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
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    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```

2

Sieve of Erastosthenes

3

2

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]!i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;          # p is a prime
    do Sieve[i-1]?next ->  # receive next candidate
        if (next mod p) != 0 -> # if it might be prime,
            Sieve[i+1]!next;    #     pass it on
        fi
    od
}
```

Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->       # receive next candidate
        if (next mod p) != 0 -> # if it might be prime,
            Sieve[i+1]!next;    #     pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```

4

2

3

Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->       # receive next candidate
        if (next mod p) != 0 -> # if it might be prime,
            Sieve[i+1]?next;    #     pass it on
        fi
    od
}
```

4 2
3

Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```

5

4

2

3



Sieve of Erastosthenes

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process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```



Sieve of Erastosthenes

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process Sieve[1] {
    int p = 2;
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process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```

6

4

3

5



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->       # receive next candidate
        if (next mod p) != 0 -> # if it might be prime,
            Sieve[i+1]!next;    #     pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->       # receive next candidate
        if (next mod p) != 0 -> # if it might be prime,
            Sieve[i+1]!next;    #     pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```

10

6 4 8 2

9 3

5

7



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->        # receive next candidate
        if (next mod p) != 0 ->  # if it might be prime,
            Sieve[i+1]!next;     #   pass it on
        fi
    od
}
```



Sieve of Erastosthenes

```
process Sieve[1] {
    int p = 2;
    for [i = 3 to n by 2]
        Sieve[2]?i;    # pass odd numbers to Sieve[2]
}

process Sieve[i = 2 to L] {
    int p, next;
    Sieve[i-1]?p;                # p is a prime
    do Sieve[i-1]?next ->       # receive next candidate
        if (next mod p) != 0 -> # if it might be prime,
            Sieve[i+1]!next;    #     pass it on
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