

$$\sigma = \exists x. (P(x) \Rightarrow \forall x. P(x))$$

$$\begin{aligned} \neg \sigma &= \neg \exists x. (P(x) \Rightarrow \forall x. P(x)) \\ &= \forall x. (\neg (\neg P(x) \vee \forall x. P(x))) \\ &= \forall x. (P(x) \wedge \neg \forall x. P(x)) \\ &= \forall x. (P(x) \wedge \exists x. \neg P(x)) \\ &= \forall x. (P(x) \wedge \exists y. \neg P(y)) \quad \text{Renombre: } \exists x \rightarrow \exists y \\ &= \forall x. \exists y. (P(x) \wedge \neg P(y)) \\ &= \forall x. (P(x) \wedge \neg P(f(x))) \\ &= \forall x. P(x) \wedge \forall x. \neg P(f(x)) \\ &= \{ \underbrace{\{P(x_1)\}}_1, \underbrace{\{\neg P(f(x_2))\}}_2 \} = C \end{aligned}$$

$$\begin{aligned} 1 \text{ y } 2: \quad \text{mgu} \{P(x_1) \doteq P(f(x_2))\} \\ &= \text{mgu} \{x_1 \doteq f(x_2)\} \\ &= \text{mgu} \{\} \end{aligned}$$

decompose
elim $\{x_1 \doteq f(x_2)\}$

$$\exists = \{\}$$

$$C \vdash \perp \Rightarrow \neg \sigma \vdash \perp \Rightarrow \vdash \sigma$$

$\therefore \sigma$ válida