

Topology Seminar

Sune Precht Reeh

of MIT will be speaking on

Dimension functions, homotopy
sphere actions, and fusion systems

on March 20 at 3:00 in
MIT Room 2-131

Given a representation V of a finite group G we can associate a dimension function that to each subgroup H of G assigns the dimension of the fixed point space V^H . The dimension functions are “super class functions” that are constant on the conjugacy classes of subgroups in G . For a p -group the list of Borel-Smith conditions characterizes the super class functions that come from real representations.

In a joint paper with Ergün Yalcin we show that though we cannot lift Borel-Smith functions to real representations for a general group G , we can lift a multiple of any Borel-smith function to an action of G on a finite homotopy sphere (which would be the unit sphere if we had a representation).

To solve the problem we localize at each prime p , and solve it in general for saturated fusion systems. That is, we give a list of Borel-Smith conditions for a fusion system that characterize the dimension functions of the fusion stable real representations. The proof for fusion systems involves biset functors and characteristic bisets for saturated fusion systems.