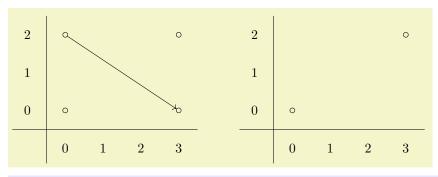
## Contents

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## 1 Introduction

The sseqpages package consists of two main environments – the <u>sseqdata</u> environment, which specifies the data for a named spectral sequence diagram, and the <u>sseqpage</u> environment, which prints a single page of a spectral sequence diagram. The command \printpage is also available as a synonym for a sseqpage environment with an empty body.

Here is a basic example:



```
\begin{sseqdata} [name=ex1, cohomological Serre grading]
\class(0,0)
\class(0,2)
\class(3,0)
\class(3,2)
\d3(0,2)
\end{sseqdata}
\printpage [name=ex1, page=3] \hskip1cm
\printpage [name=ex1, page=4]
```

\begin{sseqdata} [name=ex1, degree= $\{\#1\}\{1-\#1\}\}$  starts the declaration of the data of a spectral sequence named ex1 whose page r differentials go r to the right and down r-1 (this is cohomological Serre grading).

Then we specify four classes and one page 3 differential, and we ask sseqpages to print the third and fourth pages of the spectral sequence. Note that on the fourth page, the source and target of the differential have disappeared.

### 2 The main commands

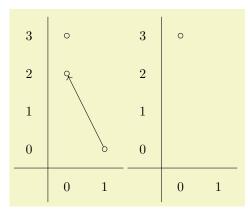
 $\cline{class} [\langle options \rangle] \langle coordinate \rangle$ 

This places a class at  $\langle coordinate \rangle = (\langle xcoord \rangle, \langle ycoord \rangle)$  where  $\langle xcoord \rangle$  and  $\langle ycoord \rangle$  are integers. If multiple classes occur at the same position, sseqpages will automatically arrange them in a pre-specified pattern:

```
\begin{sseqpage} [no axes,ymirror]
\class(0,0)
\class(1,0)\class(1,0)
\class(0,1)\class(0,1)\class(0,1)
\class(1,1)\class(1,1)\class(1,1)\class(1,1)
\class(0,2)\class(0,2)\class(0,2)\class(0,2)\class(0,2)
\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2
```

The effect of the  $\class$  command is to print a  $\class$  node on a range of pages. Any option that would work for a  $\class$  node command will also work in the same way for the  $\class$ ,  $\class$  and  $\class$  options commands.

If a class is the source or the target of a differential on a certain page, then the page of the class is set to that page, and the class is only rendered on pages up to that number:



```
\begin{sseqdata} [name=class example, Adams grading]
\class(1,0)
\class(0,2)
\class(0,3)
\d2(1,0)
\end{sseqdata}
\printpage [name=class example, page=2]
\printpage [name=class example, page=3]
```

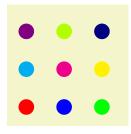
 $\cline{classoptions} [\langle options \rangle] \langle coordinate \rangle$ 

For instance:

#### A TikZ shape

If you give the name of a TikZ shape, the class node will be of that shape. The standard TikZ shapes are circle and rectangle, but there are many more TikZ shapes in the shapes library, which you can load using the command \usetikzlibrary{shapes}

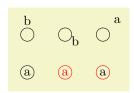
#### A TikZ color



```
\begin{sseqpage} [classes={fill,inner sep=0.4em}, no axes]
\class[red](0,0)
\class[blue](1,0)
\class[green](2,0)
\class[cyan](0,1)
\class[magenta](1,1)
\class[yellow](2,1)
\class[blue!50!red](0,2)
\class[green!30!yellow](1,2)
\class[blue!50!black](2,2)
\end{sseqpage}
```

#### $"\langle text \rangle "\langle options \rangle$

A label. This uses the TikZ quotes syntax, but the behavior specific to sseqpages. By default, the  $\langle text \rangle$  is placed in the position inside the node – in effect, the  $\langle text \rangle$  becomes the label text of the node (so saying \class["label text"](0,0) causes a similar effect to saying \node at (0,0) {label text};). There are other position options such as left, above left, etc which cause the label text to be placed in a separate node positioned appropriately. If the placement is above, left, etc, then any option that you may pass to a TikZ node will also work for the label, including general coordinate transformations. If the placement is "inside", then the only relevant  $\langle options \rangle$  are those that alter the appearance of text, such as opacity and color.



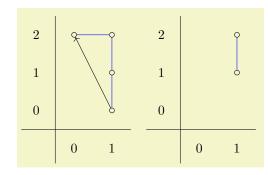
```
\begin{sseqpage} [no axes,classes={minimum width=width("a")+0.5em}]
\class["a"](0,0)
\class["a",red](1,0)
\class["a" black,red](2,0)
\class["b" above](0,1)
\class["b" {below right,yshift=0.1cm}](1,1)
\class["a" {above right={1em}}](2,1)
\end{sseqpage}
```

```
\begin{array}{ll} \operatorname{minimum\ width=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{minimum\ height=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{minimum\ size=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{inner\ sep=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{outer\ sep=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \end{array}
```

These options control the size of a node. This is typically useful to make the size of nodes consistent independent of the size of their label text. For instance:

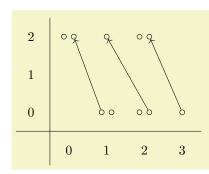
#### $\d[\langle options \rangle] \langle page \rangle \langle source\ coordinate \rangle$

This creates a differential starting at  $\langle source\ coordinate \rangle$  of length determined by the specified page. In order to use the \d command, you must first specify the degree of the differentials as an option to the sseqdata or sseqpage environment. The degree indicates how far to the right and how far up a page r differential will go as a function of r. If there is a page r differential, on page r+1, the source, target, and any \structlines connected to the source and target of the differential disappear.



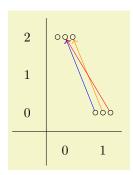
```
\begin{sseqdata} [name=d example, degree={-1}{#1}, struct lines=blue] \class(0,2) \class(1,2) \class(1,2) \class(1,0) \structline(1,2)(0,2) \structline(1,2)(1,1) \structline(1,2)(1,1) \structline(1,1)(1,0) \d2(1,0) \end{sseqdata} \printpage[name=d example, page=2] \hskip0.3cm \printpage[name=d example, page=3]
```

If there are multiple nodes in the source or target coordinate, then there is a funny syntax for indicating which one should be the source and target:  $\d\langle page\rangle (\langle x\rangle, \langle y\rangle, \langle source\ n\rangle, \langle target\ n\rangle)$ 



```
\begin{sseqpage} [Adams grading]
\class(1,0)\class(1,0)
\class(0,2)\class(0,2)
\d2(1,0,1,2)
\class(2,0)\class(2,0)
\class(1,2)
\d2(2,0,2)
\class(3,0)
\class(2,2)\class(2,2)
\d2(3,0,2)
\end{sseqpage}
```

Negative indices will count from the most recent class in the coordinate (so -1 is the most recent, -2 is the second most recent, etc):



```
begin{sseqpage} [Adams grading]

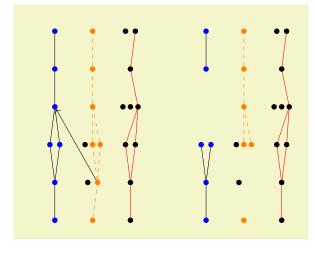
\class(1,0)
\class(0,2)\class(0,2)
\d[blue] 2(1,0,-1,-1)
\class(1,0)
\class(0,2)
\d[orange] 2(1,0,-1,-1)
\class(1,0)
\d[red] 2(1,0,-1,-2)
\end{sseqpage}
```

 $\dot{doptions}[\langle options \rangle] \langle page \rangle \langle source\ coordinate \rangle$ 

#### $\texttt{\sc tructline}[\langle options \rangle] \langle source\ coordinate \rangle \langle target\ coordinate \rangle$

This command creates a structure line from  $\langle source\ coordinate \rangle$  to  $\langle target\ coordinate \rangle$ . The source and target coordinates are of the form  $(\langle x \rangle, \langle y \rangle, \langle n \rangle)$ . If there are multiple classes at (x, y), then  $\langle n \rangle$  specifies which of the classes at (x, y) the structline starts and ends at – if n is positive, then it counts from the first class in that position, if n is negative, it counts backwards from the most recent.

If the source or target of a structure line is hit by a differential, then on subsequent pages, the structure line disappears.



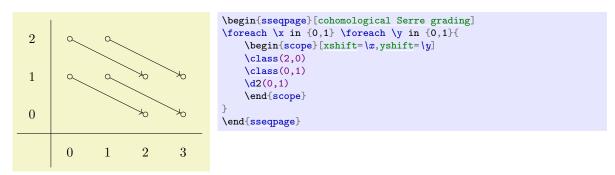
```
\sseqnewgroup\tower{
    \class(0,0)
    \class(0,2)
    \foreach \y in\{1, \ldots, 5\}
        \class(0,\y)
        \structline(0,\y-1,-1)(0,\y,-1)
    \text{structline}(0,1,-1)(0,2,-2)
    \text{structline}(0,2,-2)(0,3,-1)
\begin{sseqdata} [name=structline example,
                  classes={circle,fill},
                  Adams grading, no axes]
\class(1,1)\class(1,2)
\class(2,3)\class(2,3)\class(2,5)
\tower[classes=blue](0,0)
\tower[struct lines=dashed,orange](1,0)
\tower[struct lines=red](2,0)
d2(1,1,2)
\end{sseqdata}
\printpage[name=structline example,page=2]
\hskip1cm
\printpage[name=structline example,page=3]
```

 $\texttt{\sc tructline options}[\langle options \rangle] \langle source\ coordinate \rangle \langle target\ coordinate \rangle$ 

# 2.1 Options

```
xshift=\langle integer \rangle \quad \text{(no default)} \quad \quad \text{(no default)} \quad \quad \text{(no default)} \quad \qu
```

Shifts by integer values are the only local coordinate changes that are allowed to be applied to \class, \d, and \structline. These shift commands help with reusing code. For instance:



A word of warning: the behavior of xshift in sseqpages is incompatible with the normal behavior of xshift in TikZ. For some reason, saying xshift=1 in TikZ does not shift the coordinate (0,0) to the coordinate (1,0) – instead it shifts a tiny fraction of the distance.

#### 2.1.1 for \d and \structline

In general, any option that you could apply to a TikZ "to" command can be applied to both  $\d$  and  $\structline$ . Some such options are as follows:

```
"\langle text \rangle", \langle options \rangle
```

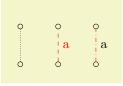
A label "" $\langle text \rangle$ ""  $\langle options \rangle$ . By default, such a label is placed to the right of the edge. The optional prime places it to the left of the edge instead. The options include anything you might pass as an option to a TikZ node, including arbitrary coordinate transforms, colors, opacity options, shapes, fill, draw, etc.

The special option "description," stolen from tikzcd, places the label on top of the edge. In order to make this option work correctly, if the background color is not the default white, you must inform sseqpages about this using the key background color= $\langle color \rangle$ . In this case, the background color is called graphicbackground.

```
a a' b c
```

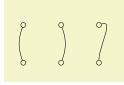
```
\begin{sseqpage} [no axes,background color=graphicbackground]
\foreach\x in {0,1,2} \foreach\y in {0,1}{
    \class(\x,\y)
}
\structline["a" red](0,0)(0,1)
\structline["a"'blue,"b"{yshift=1em}](1,0)(1,1)
\structline["c" description](2,0)(2,1)
\end{sseqpage}
```

Colors and dash patterns:



```
\begin{sseqpage}[no axes]
\foreach\x in {0,1,2} \foreach\y in {0,1}{
    \class(\x,\y)
}
\structline[densely dotted](0,0)(0,1)
\structline[dashed,red, "a"](1,0)(1,1)
\structline[dash dot,red, "a" black](2,0)(2,1)
\end{sseqpage}
```

```
\begin{array}{ll} \textbf{bend left=}\langle angle \rangle & \text{(no default)} \\ \textbf{bend right=}\langle angle \rangle & \text{(no default)} \\ \textbf{in=}\langle anchor \rangle & \text{(no default)} \\ \textbf{out=}\langle anchor \rangle & \text{(no default)} \\ \end{array}
```



```
source anchor=\langle anchor \rangle (no default) target anchor=\langle anchor \rangle (no default)
```



```
\begin{sseqpage}[no axes]
\foreach\x in {0,1} \foreach\y in {0,1}{
      \class(\x,\y)
}
\structline(0,0)(0,1)
\structline[source anchor=north west, target anchor=-30](1,0)(1,1)
\end{sseqpage}
```

### 3 The Environments

```
\begin{sseqdata}[\langle options \rangle]\\ \langle environment\ contents \rangle\\ \begin{sseqdata}\\ \begin{sseqdata}\\ \end{sseqdata}\\ \end{sseqdata}
```

The sseqdata environment is for storing a spectral sequence to be printed later. This environment is intended for circumstances where you want to print multiple pages of the same spectral sequence. When using the <u>sseqdata</u> environment, you must use the <u>name</u> option to tell <u>sseqpages</u> where to store the spectral sequence so that you can access it later.

```
\begin{sseqpage} [\langle options \rangle] \\ \langle environment\ contents \rangle \\ \begin{sseqpage} \end{sseqpage}
```

This environment is used for printing a page of an existing spectral sequence with some modification, or for printing a stand-alone page. If you use the <u>name</u> option, the name given must match with the name given for some **sseqdata** environment

```
\printpage[\langle options \rangle]
```

This command prints a single page of an existing spectral sequence as-is. This is equivalent to a sseqpage environment with an empty body.

## 4 Commands

#### $\scalebox{sseqset}\{\langle keys \rangle\}$

\sseqset is for adjusting the global options for all spectral sequences in the current scope. For instance, if most of the spectral sequences in the current document are going to be Adams graded, you can say \sseqset{Adams grading} and all future spectal sequences in the current scope will have Adams grading (unless you specify a different grading explicitly). As another example, \sseqset{no\_axes} will suppress axes from spectral sequences in the current scope.

For options that only apply to pages, such as keep changes, you should say instead \sseqset{pages={keep changes}}.

```
\scalebox{$\backslash$sseqnewcmd*$}\langle macro\rangle(\langle x\ variable\ macro\rangle,\langle y\ variable\ macro\rangle)[\langle num\ args\rangle]{\{\langle body\rangle\}}
```

This command makes a new command with syntax similar to  $\class$ . By default it takes three arguments:  $\mbox{mycommand}[\langle options \rangle](\langle x \rangle, \langle y \rangle)$ . To access the  $\langle options \rangle$  argument in the body of the command, use the macro  $\mbox{options}$ . Likewise to access  $\langle x \rangle$ , use  $\mbox{x}$ , and to access  $\langle y \rangle$  use  $\mbox{y}$ :

The unstarred version will throw an error if the command to be defined already exists. The starred variant will quietly overwrite the existing command. Note that the command is always defined globally. Sometimes it's inconvenient to use \x and \y as arguments, for instance if you want to use code that already uses them as iterators. In this case, you can specify other macros to use for the arguments:

```
\sseqnewcmd\test(\a,\b){
                                          \foreach \x in \{0, ..., 2\} \foreach \y in \{0, ..., 1\}
2
                                              \class[\options](\a+\x,\b+\y)
1
       0
                                      \begin{sseqpage}
                                      \test(0,0)
                                     \test[red,fill](1,1)
0
       0
                                     \end{sseqpage}
       0
              1
                      2
                             3
```

The command you create with \sseqnewcmd can take up to six arguments in addition to \options, \x, and \y. These extra arguments are mandatory and are delimited by braces.

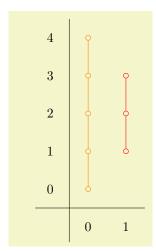
```
\sseqnewcmd*\tower[1]{
   \begin{scope}[\options]
   \class(\x,\y)
   \foreach \n in {1,...,#1}{
        \class(\x,\y+\n)
        \structline(\x,\y+\n-1)(\x,\y+\n)
   }
   \end{scope}
}
\begin{sseqpage}
\tower[orange](0,0){4}
\tower[red](1,1){2}
\end{sseqpage}
\end{sseqpage}
```

```
\space{1mm} \spa
```

This is more or less a shorthand for

```
\label{lem:cope} $$ \operatorname{scope}[xshift=\obscurexname, yshift=\obscurexname, \options] $$ \langle body \rangle$ \end{scope} $$
```

For instance:



```
\sseqnewgroup*\tower[1]{
    \class(0,0)
    \foreach \n in \{1,...,\#1\}{
        \class(0,\n)
        \structline(0,\n-1)(0,\n)
    }
    \end{\scope}
}
\begin{\sseqpage}
\tower[orange](0,0){4}
\tower[red](1,1){2}
\end{\sseqpage}
```

# 5 Global options

```
name = \langle sseq \ name \rangle  (no default)
```

```
page = \langle page \ number \rangle (no default, initially 0)
```

This key is for sseqpage and  $\printpage$ . It specifies which page of the spectral sequence is to be printed. On page r, all  $\classes$  that are not hit by differentials on pages less than r will be printed, as well as all  $\sructlines$  whose source and target classes are both printed on page r, and all differentials of length exactly r. The special value  $\printpage=0$  prints all classes, differentials, and structure lines.

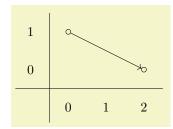
```
\begin{array}{ll} \operatorname{degree} = \{\langle x \; degree \rangle\} \{\langle y \; degree \rangle\} & \text{(no default)} \\ \operatorname{cohomological Serre \; grading} & \text{(no value)} \\ \operatorname{homological Serre \; grading} & \text{(no value)} \end{array}
```

Adams grading (no value)

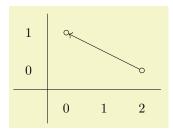
Specifies the degree of differentials. The  $\langle x \ degree \rangle$  and  $\langle y \ degree \rangle$  should both be mathematical expressions in one variable #1 that evaluate to integers on any input. They specify the x and y displacement of a page #1 differential. In practice, they will usually be linear expressions with #1 coefficient 1, -1, or 0.

The degree option must be given before placing any differentials. It can be specified at the beginning of the sseqdata environment, at the beginning of the sseqpage environment if it is being used as a standalone page, or as a default by saying  $\seqset{degree={\langle x \ degree \rangle}}{\langle y \ degree \rangle}}$  or  $\seqset{Adams \ grading}$  outside of the sseqdata and sseqpages environments.

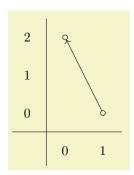
You can make a named grading convention by saying \sseqset{my grading/.sseq grading={ $\langle x \ degree \rangle$ }{ $\langle y \ degree \rangle$ }. Then later passing my grading to a spectral sequence is equivalent to saying degree={ $\langle x \ degree \rangle$ }{ $\langle y \ degree \rangle$ }. The following grading conventions exist by default:



```
\begin{sseqpage}[cohomological Serre grading]{\cite{cohomological Serre grading}}{\cite{cohomological Serre grading}}{\cite{cohomologica
```



```
\begin{sseqpage}[homological Serre grading]{\cite{class(0,1)}} & equivalent to degree={-#1}{#1-1} \\ & class(2,0) \\ & d2(2,0) \\ & end{sseqpage} \end{sseqpage}
```



```
\begin{sseqpage} [Adams grading] % equivalent to degree={-1}{#1-1}
\class(0,2)
\class(1,0)
\d2(1,0)
\end{sseqpage}
```

```
x range=\langle x \min \rangle \langle x \max \rangle (no default)
y range=\langle y \min \rangle \langle y \max \rangle (no default)
```

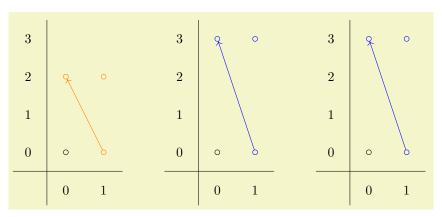
These options force the x and y range to be a specific interval. By default, if no range is specified then the range is chosen to fit all the classes. If an x range is specified but no y range, then the y range is chosen to fit all the classes that lie inside the specified x range, and vice versa.

update existing (no value)

This key is only for the **sseqdata** environment. It specifies that the current **sseqdata** environment is adding data to an existing spectral sequence. If you don't pass this key, then giving a **sseqdata** environment the same **name** as a different **sseqdata** environment will cause an error. This is intended to help you avoid accidentally reusing the same name.

 $keep changes = \langle boolean \rangle$  (default true) (initially false)

This option is only for the <u>sseqpage</u> environment, and only works when a <u>name</u> is provided. This option specifies that all of the commands in the current <u>sseqpage</u> environment should be carried forward to future pages of the same named spectral sequence. For example:



```
\begin{sseqdata} [name=keep changes example, Adams grading, y range={0}{3}]
\class(1,0)
\end{sseqdata}
\begin{sseqpage} [name=keep changes example,paths=orange]
\class(0,2)
\class(1,2)
\classoptions[orange](1,0)
d2(1,0)
\end{sseqpage}
\hskip1cm
\begin{sseqpage} [name=keep changes example,paths=blue,keep changes]
\class(0,3)
\class(1.3)
\classoptions[blue](1,0)
\d3(1,0)
\end{sseqpage}
\hskip1cm
\printpage[name=keep changes example,page=3]
```

Note that the orange classes and differential do not persist because the keep changes option is not set in the first sseqpage environment, but the blue classes and differential do, since the keep changes option is set in the second sseqpage environment.

```
no differentials (no value) draw differentials (no value)
```

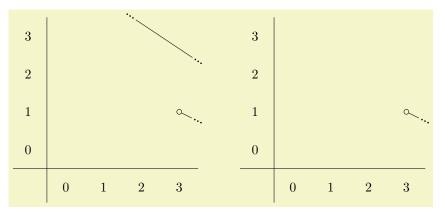
The option no differentials suppresses all of the differentials on the current page, whereas draw differentials causes the page appropriate differentials to be drawn. This is useful for explaining how the computation of the spectral sequence goes:

```
no struct lines (no value)
draw struct lines (no value)
```

The option no struct lines suppresses all of the differentials on the current page, whereas the option draw struct lines causes the page appropriate differentials to be drawn.

```
no orphan edges (no value) draw orphan edges=\langle boolean \rangle (default true)(initially true)
```

An edge is an "orphan" if both its source and target lie off the page. By default these are drawn, but with the option no orphan edges they are not. If the option no orphan edges has been set, draw orphan edges undoes it.



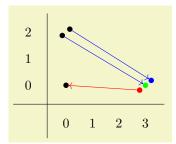
```
class placement transform=\{\langle transform \ keys \rangle\}
```

(no default)

The sseqpages option class placement transform allows the user to specify a Tikz coordinate transform to adjust the relative position of multiple nodes in the same (x,y) position. This coordinate transform can only involve rotation and scaling, no translation. Specifying a scaling factor helps if the nodes are too large and overlap. In some cases a rotation makes it easier to see which class is the target of a differential.

1		$\mathbb{Z}/2 \ \mathbb{Z}/3$
0	$\mathbb{Z}$	
	0	1

```
\label{lem:class} $$ \left[ classes = \{draw = none\}, class \ placement \ transform = \{xscale = 3\}, \ xscale = 2, \ x \ axis \ extend \ end = 0.7cm \right] $$ \class["$\mathbb{Z}$"] (0,0) $$ \class["$\mathbb{Z}$"] (1,1) $$ \class["$\mathbb{Z}$/2$"] (1,1) $$ \class["$\mathbb{Z}$/3$"] (1,1) $$ \end{sseqpage}
```



```
\label{lem:composition} $$ \left[ classes = fill, class \ placement \ transform = \{rotate = 40\}, \\  cohomological \ Serre \ grading, differentials = blue, scale = 0.7] $$ \left[ class(0,0) \\ class(0,2) \\ class[color](3,0) \\ class[green](3,0) \\ class[blue](3,0) \\ d3(0,2,1,2) \\ d3(0,2,1,-1) \\ draw[->,red](3,0,1) --(0,0); \\ end\{sseqpage\} $$
```

#### 5.1 Styles

The sseqpages package has a large number of "styles" which control the appearance of specific components (classes, differentials, or structlines) of a spectral sequence. These are named so that each command has a plural variant (e.g., classes) and a "style" variant (e.g., class style). The difference between these is always that classes=\marg{keys} adds the keys to the list of options used to style every class, whereas class style=\marg{keys} overwrites the list of options. It's important to be aware when using

the style variants that some of the styles are not empty when sseqpages is loaded, so for instance saying class style={} will change the appearance of the diagram. Generally, the plural versions are more useful, but in very large diagrams it can be noticeably faster to use the style variants.

In cases where the same drawing feature is affected by multiple of these styles, the more specific style takes precedence.

Throughout, "class" and "cycle" are synonyms.

This passes global options to all future spectral sequences in the current scope. It is only useful to use this command with \sseqset. This is only really important for TikZ options, because for most options from sseqpages you can set a default directly by saying \sseqset{key={ $\langle value \rangle}}$ }.

```
\sseqset{sseqs={scale=0.5}}% Applies to both of the two following sseqs
\begin{sseqpage}
\foreach \x in {0,1} \foreach \y in {0,1,2}{
    \class(\x,\y)
}
\end{sseqpage}
\hskip1cm
\begin{sseqpage} [Adams grading,classes={fill,blue}]
\foreach \x in {0,1,2} \foreach \y in {0,1,2}{
    \class(\x,\y)
}
\d2(1,0)
\d2(2,0)
\end{sseqpage}
\end{sseqpage}
```

```
 \begin{array}{c} {\sf classes=\{\langle keys\rangle\}} & \text{(no default)} \\ {\sf cycles=\{\langle keys\rangle\}} & \text{(no default)} \\ {\sf class \ style=\{\langle keys\rangle\}} & \text{(no default)} \\ {\sf cycle \ style=\{\langle keys\rangle\}} & \text{(no default)} \\ \end{array}
```

The keys classes and cycles are synonyms as are class style and cycle style. These options change the appearance of all classes. The options classes and cycles append whatever keys you give to the list of class style options, whereas class style and cycle style overwrite the list of styles.

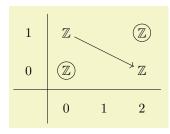
```
2 • 1 0 • 0 1 2
```

```
\begin{sseqpage}[classes={blue,fill,minimum width=0.5em}]
\class(0,0)
\class(2,2)
\end{sseqpage}
```

```
permanent classes=\{\langle keys \rangle\} (no default)
```

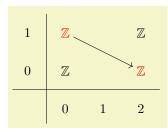
```
 \begin{array}{lll} & & & & & & \\ \text{permanent cycles=}\{\langle keys \rangle\} & & & & & \\ \text{permanent class style=}\{\langle keys \rangle\} & & & & \\ \text{permanent cycle style=}\{\langle keys \rangle\} & & & & \\ \text{(no default)} & & & \\ \text{(no default)} & & & \\ \end{array}
```

These options change the appearance of all permanent cycles (e.g., those classes which never support or are hit by a differential). For instance, we can circle the permanent cycles automatically. Note that because permanent cycles is more specific than classes, the permanent cycles={draw} command wins out over the class={draw=none} command to insure that the permanent cycle nodes are drawn.



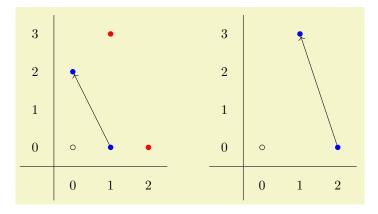
```
\begin{array}{ll} \text{transient classes=}\{\langle keys\rangle\} & \text{(no default)} \\ \text{transient cycles=}\{\langle keys\rangle\} & \text{(no default)} \\ \text{transient class style=}\{\langle keys\rangle\} & \text{(no default)} \\ \text{transient cycle style=}\{\langle keys\rangle\} & \text{(no default)} \\ \end{array}
```

These options change the appearance of all transient cycles (e.g., those classes which eventually support or are hit by a differential). Again, this takes precedence over the classes option.



```
this page classes=\{\langle keys \rangle\} (no default) this page class style=\{\langle keys \rangle\} (no default) this page class style=\{\langle keys \rangle\} (no default) this page cycle style=\{\langle keys \rangle\} (no default)
```

These options change the appearance of all cycles which support or are hit by a differential on this page. Any class that is hit on the current page is also a transient cycle, and so this page classes takes precedence over transient cycles



```
\begin{sseqdata} [name=this page cycles example, Adams grading,
                      transient cycles={red,fill},this page cycles={blue}]
     \class(0,0)
     \class(0,2)\class(1,0)
     \class(1,3)\class(2,0)
     d2(1,0)d3(2,0)
     \end{sseqdata}
     \printpage[name=this page cycles example,page=2]
    \printpage[name=this page cycles example,page=3]
edges=\{\langle keys \rangle\}
                                                                                                      (no default)
edge style=\{\langle keys \rangle\}
                                                                                                      (no default)
    This style applies to both differentials and structure lines. The differentials and struct lines keys
    both take precedence over edges.
differentials = \{\langle keys \rangle\}
                                                                                                      (no default)
differential style=\{\langle keys \rangle\}
                                                                                                      (no default)
struct lines=\{\langle keys \rangle\}
                                                                                                      (no default)
                                                                                                      (no default)
struct line style=\{\langle keys \rangle\}
this page struct lines=\{\langle keys \rangle\}
                                                                                                      (no default)
this page struct line style=\{\langle keys \rangle\}
                                                                                                      (no default)
    This style applies to structure lines whose source or target is hit on the current page. It takes precedence
    over struct lines.
labels
                                                                                                        (no value)
label style
                                                                                                        (no value)
                                                                                                        (no value)
class labels
class label style
                                                                                                        (no value)
inner class labels
                                                                                                        (no value)
inner class label style
                                                                                                        (no value)
outer class labels
                                                                                                        (no value)
                                                                                                        (no value)
outer class label style
edge labels
                                                                                                        (no value)
                                                                                                        (no value)
edge label style
                                                                                                        (no value)
differential labels
differential label style
                                                                                                        (no value)
struct line labels
                                                                                                        (no value)
                                                                                                        (no value)
struct line label style
```

#### 5.2 Global Coordinate Transformations

Of the normal TikZ coordinate transformations, only the following can be applied to a sseq diagram:

Scale the diagram by  $\langle factor \rangle$ . Under normal circumstances, you can tell TikZ to mirror a diagram by saying, for instance, xscale=-1, but sseqpages needs to be aware that the diagram has been mirrored in order to draw the axes correctly. Thus, if you want to mirror a spectral sequence, use the xmirror and ymirror options as appropriate.

```
rotate=\langle angle \rangle (no default)
```

It probably won't look great if you pick an angle that isn't a multiple of 90 degrees.

## 5.3 Layout

no y axis

```
custom clip=\langle clip path\rangle
                                                                                                               (no default)
                                                                                      (default true) (initially true)
clip=\langle boolean \rangle
                                                                                             (no default, initially 0.5cm)
x axis gap=\langle dimension \rangle
y axis gap=\langle dimension \rangle
                                                                                             (no default, initially 0.5cm)
axes gap = \langle dimension \rangle
                                                                                             (no default, initially 0.5cm)
x label gap=\langle dimension \rangle
                                                                                             (no default, initially 0.5cm)
y label gap=\langle dimension \rangle
                                                                                             (no default, initially 0.5cm)
x axis start extend=\langle dimension \rangle
                                                                                             (no default, initially 0.5cm)
y axis start extend=\langle dimension \rangle
                                                                                             (no default, initially 0.5cm)
x axis end extend=\langle dimension \rangle
                                                                                             (no default, initially 0.9cm)
y axis end extend=\langle dimension \rangle
                                                                                             (no default, initially 0.9cm)
x clip axis padding=\langle dimension \rangle
                                                                                             (no default, initially 0.1cm)
y clip axis padding=\langle dimension \rangle
                                                                                             (no default, initially 0.1cm)
right clip padding=\langle dimension \rangle
                                                                                             (no default, initially 0.1cm)
left clip padding=\langle dimension \rangle
                                                                                             (no default, initially 0.4cm)
top clip padding=\langle dimension \rangle
                                                                                             (no default, initially 0.1cm)
bottom clip padding=\langle dimension \rangle
                                                                                             (no default, initially 0.4cm)
        Axes Style
5.4
x axis style=a
                                                                                           (no default, initially border)
y axis style=a
                                                                                           (no default, initially border)
axes style=
                                                                                           (no default, initially border)
x axis origin=
                                                                                                  (no default, initially 0)
                                                                                                  (no default, initially 0)
y axis origin=
no x axis
                                                                                                                 (no value)
```

(no value)

```
(no value)
no axes
draw x axis
                                                                                              (no value)
draw y axis
                                                                                              (no value)
                                                                                              (no value)
draw axes
                                                                                              (no value)
no x axis labels
no y axis labels
                                                                                              (no value)
no axes labels
                                                                                              (no value)
draw x axis labels
                                                                                             (no value)
draw y axis labels
                                                                                             (no value)
draw axes labels
                                                                                              (no value)
x label step=
                                                                                 (no default, initially 1)
                                                                                 (no default, initially 1)
y label step=
                                                                                 (no default, initially 1)
label step=
rotate labels=\langle boolean \rangle
                                                                      (default true)(initially false)
```