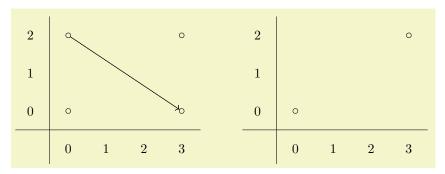
1 Introduction

The sseqpages package consists of two main environments – the <u>sseqdata</u> environment, which specifies the data for a named spectral sequence diagram, and the <u>sseqpage</u> environment, which prints a single page of a spectral sequence diagram. The command \printpage is also available as a synonym for a sseqpage environment with an empty body.

Here is a basic example:



```
\begin{sseqdata} [name=ex1,cohomological Serre grading]
\class(0,0)
\class(0,2)
\class(3,0)
\class(3,2)
\d3(0,2)
\end{sseqdata}
\printpage [name=ex1,page=3] \hskip1cm
\printpage [name=ex1,page=4]
```

\begin{sseqdata} [name=ex1,degree={#1}{1-#1}] starts the declaration of the data of a spectral sequence named ex1 whose page r differentials go r to the right and down r-1 (this is cohomological Serre grading). Then we specify four classes and one page 3 differential, and we ask sseqpages to print the third and fourth pages of the spectral sequence. Note that on the fourth page, the source and target of the differential have disappeared.

2 The main commands

This places a class at $\langle coordinate \rangle = (\langle xcoord \rangle, \langle ycoord \rangle)$ where $\langle xcoord \rangle$ and $\langle ycoord \rangle$ are integers. If multiple classes occur at the same position, **sseqpages** will automatically arrange them in a pre-specified pattern:

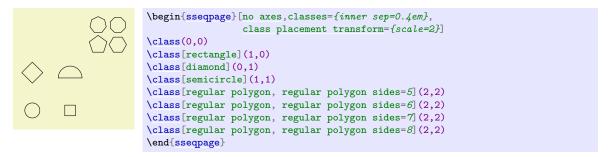
```
\begin{sseqpage} [no axes,ymirror] \\class(0,0) \\class(1,0)\class(0,1) \\class(0,1)\class(0,1)\class(0,1) \\class(1,1)\class(1,1)\class(1,1)\class(1,1)\class(1,1)\class(0,2)\class(0,2)\class(0,2)\class(0,2)\class(0,2)\class(0,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\class(1,2)\c
```

The effect of the \class command is to print a \class node. Any option that would work for a \class node command will also work in the same way for the \class , \class , and \class commands. For instance:

A TikZ shape

If you give the name of a TikZ shape, the class node will be of that shape. The standard TikZ shapes are circle and rectangle, but there are many more TikZ shapes in the shapes library,

which you can load using the command \usetikzlibrary{shapes}



A TikZ color

```
\begin{sseqpage} [classes={fill,inner sep=0.4em}, no axes]
\class[red](0,0)
\class[blue](1,0)
\class[green](2,0)
\class[cyan](0,1)
\class[magenta](1,1)
\class[yellow](2,1)
\class[blue!50!red](0,2)
\class[green!30!yellow](1,2)
\class[blue!50!black](2,2)
\end{sseqpage}
```

$"\langle text \rangle "\langle options \rangle$

A label. This uses the TikZ quotes syntax, but the behavior specific to sseqpages. By default, the $\langle text \rangle$ is placed in the position inside the node – in effect, the $\langle text \rangle$ becomes the label text of the node (so saying \class["label text"](0,0) causes a similar effect to saying \node at (0,0) {label text};). There are other position options such as left, above left, etc which cause the label text to be placed in a separate node positioned appropriately. If the placement is above, left, etc, then any option that you may pass to a TikZ node will also work for the label, including general coordinate transformations. If the placement is "inside", then the only relevant $\langle options \rangle$ are those that alter the appearance of text, such as opacity and color.

```
\begin{array}{ll} \operatorname{minimum\ width=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{minimum\ height=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{minimum\ size=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{inner\ sep=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \operatorname{outer\ sep=}\langle \operatorname{dimension}\rangle & \text{(no\ default)} \\ \end{array}
```

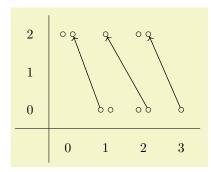
These options control the size of a node. This is typically useful to make the size of nodes consistent independent of the size of their label text. For instance:

For more information, see the pgf manual.

$\d[\langle options \rangle] \langle page \rangle \langle source\ coordinate \rangle$

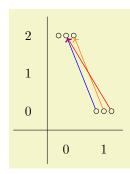
This creates a differential starting at $\langle source\ coordinate \rangle$ of length determined by the specified page. In order to use the \d command, you must first specify the degree of the differentials as an option to the sseqdata or sseqpage environment. The degree indicates how far to the right and how far up a page r differential will go as a function of r. If there is a page r differential, on page r+1, the source, target, and any \structlines connected to the source and target of the differential disappear.

If there are multiple nodes in the source or target coordinate, then there is a funny syntax for indicating which one should be the source and target: $\d\langle page \rangle (\langle x \rangle, \langle y \rangle, \langle source \ n \rangle, \langle target \ n \rangle)$



```
\begin{sseqpage} [Adams grading]
\class(1,0)\class(1,0)
\class(0,2)\class(0,2)
\d2(1,0,1,2)
\class(2,0)\class(2,0)
\class(1,2)
\d2(2,0,2)
\class(3,0)
\class(2,2)\class(2,2)
\d2(3,0,2)
\end{sseqpage}
```

Negative indices will count from the most recent class in the coordinate (so -1 is the most recent, -2 is the second most recent, etc):

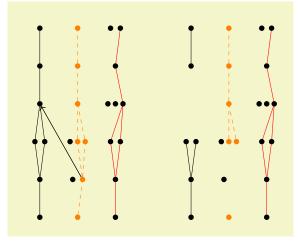


```
\begin{sseqpage} [Adams grading]
\class(1,0)
\class(0,2)\class(0,2)
\d[blue]2(1,0,-1,-1)
\class(1,0)
\class(0,2)
\d[orange]2(1,0,-1,-1)
\class(1,0)
\d[ared]2(1,0,-1,-2)
\end{sseqpage}
```

$\texttt{\sc tructline}[\langle options \rangle] \langle source\ coordinate \rangle \langle target\ coordinate \rangle$

This command creates a structure line from $\langle source\ coordinate \rangle$ to $\langle target\ coordinate \rangle$. The source and target coordinates are of the form $(\langle x \rangle, \langle y \rangle, \langle n \rangle)$. If there are multiple classes at (x, y), then $\langle n \rangle$ specifies which of the classes at (x, y) the structline starts and ends at – if n is positive, then it counts from the first class in that position, if n is negative, it counts backwards from the most recent.

If the source or target of a structure line is hit by a differential, then on subsequent pages, the structure line disappears.



```
\sseqnewgroup\tower{
    \class(0,0)
    \class(0,2)
    \foreach \y in\{1, \ldots, 5\}
        \class(0,\y)
        \structline(0,\y-1,-1)(0,\y,-1)
    \text{\table structline}(0,1,-1)(0,2,-2)
    \text{structline}(0,2,-2)(0,3,-1)
\begin{sseqdata} [name=structline example,
                  classes={circle,fill},
                  Adams grading, no axes]
\class(1,1)\class(1,2)
\class(2,3)\class(2,3)\class(2,5)
\tower[classes=blue](0,0)
\tower[struct lines=dashed,orange](1,0)
\tower[struct lines=red](2,0)
\d2(1,1,2)
\end{sseqdata}
\printpage[name=structline example,page=2]
\hskip1cm
\printpage[name=structline example,page=3]
```

2.1 Options for \d and \structline

In general, any option that you could apply to a TikZ "to" command can be applied to both \d and \structline . Some such options are as follows:

```
"\langle text \rangle", \langle options \rangle
```

A label " $\langle text \rangle$ " ' $\langle options \rangle$. By default, such a label is placed to the right of the edge. The optional prime places it to the left of the edge instead. The options include anything you might pass as an option to a TikZ node, including arbitrary coordinate transforms, colors, opacity options, shapes, fill, draw, etc.

The special option "description," stolen from tikzcd, places the label on top of the edge. In order to make this option work correctly, if the background color is not the default white, you must inform sseqpages about this using the key background color= $\langle color \rangle$. In this case, the background color is called graphicbackground.

```
a a' b c
```

```
\begin{sseqpage}[background color=graphicbackground, no axes]
\foreach\x in {0,1,2} \foreach\y in {0,1}{
    \class(\x,\y)
}
\structline["a" red](0,0)(0,1)
\structline["a""blue,"b"{yshift=1em}](1,0)(1,1)
\structline["c" description](2,0)(2,1)
\end{sseqpage}
```

Colors and dash patterns:

```
a la
```

```
\begin{array}{ll} \mathbf{bend} \ \ \mathbf{left=} \langle angle \rangle & \text{(no default)} \\ \mathbf{bend} \ \ \mathbf{right=} \langle angle \rangle & \text{(no default)} \end{array}
```

```
in=\langle anchor \rangle (no default)

out=\langle anchor \rangle (no default)
```



```
\begin{sseqpage}[background color=graphicbackground, no axes]
\foreach\x in {0,1,2} \foreach\y in {0,1}{
    \class(\x,\y)
}
\structline[bend left=20](0,0)(0,1)
\structline[bend right=20](1,0)(1,1)
\structline[in=20,out=north](2,0)(2,1)
\end{sseqpage}
```

```
\begin{array}{ll} \text{source anchor=}\langle anchor\rangle & \text{(no default)} \\ \text{target anchor=}\langle anchor\rangle & \text{(no default)} \end{array}
```



```
\begin{sseqpage}[background color=graphicbackground, no axes]
\foreach\x in {0,1} \foreach\y in {0,1}{
      \class(\x,\y)
}
\structline(0,0)(0,1)
\structline[source anchor=north west, target anchor=-30](1,0)(1,1)
\end{sseqpage}
```

3 The Environments

```
\begin{sseqdata}[\langle options \rangle]\\ \langle environment\ contents \rangle\\ \begin{sseqdata}\\
```

The <u>sseqdata</u> environment is for storing a spectral sequence to be printed later. This environment is intended for circumstances where you want to print multiple pages of the same spectral sequence. When using the <u>sseqdata</u> environment, you must use the <u>name</u> option to tell <u>sseqpages</u> where to store the spectral sequence so that you can access it later.

```
update existing (no value)
```

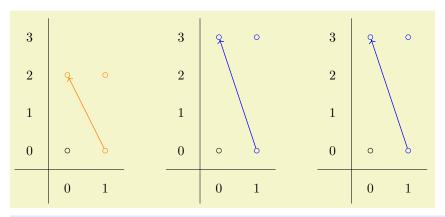
This key specifies that the current **sseqdata** environment is adding data to an already existing spectral sequence. If you don't pass this key, then giving a **sseqdata** environment the same **name** as a different **sseqdata** environment will cause an error.

```
\begin{sseqpage} [\langle options \rangle] \\ \langle environment\ contents \rangle \\ \begin{sseqpage} \end{sseqpage}
```

This environment is used for printing a page of an existing spectral sequence with some modification, or for printing a stand-alone page. If you use the <u>name</u> option, the name given must match with the name given for some **sseqdata** environment

```
keep changes=\langle boolean \rangle (default true) (initially false)
```

This option is only for the <u>sseqpage</u> environment. If true, it specifies that all of the options and commands in the <u>sseqpage</u> environment should be preserved for future drawings of the spectral sequence. For example:



```
\begin{sseqdata} [name=keep changes example, Adams grading, y range={0}{3}]
\class(0,0)
\class(1.0)
\end{sseqdata}
\begin{sseqpage} [name=keep changes example,paths=orange]
\class(0,2)
\class(1,2)
\classoptions[orange](1,0)
d2(1,0)
\end{sseqpage}
\hskip1cm
\begin{sseqpage} [name=keep changes example, paths=blue, keep changes]
\class(0,3)
\class(1,3)
\classoptions[blue](1,0)
\d3(1,0)
\end{sseqpage}
\hskip1cm
\printpage[name=keep changes example,page=3]
```

Note that the orange classes and differential do not persist because the keep changes option is not set in the first sseqpage environment, but the blue classes and differential do, since the keep changes option is set in the second sseqpage environment.

```
no differentials (no value)
draw differentials (no value)
no structlines (no value)
draw structlines (no value)
```

3.1 \printpage

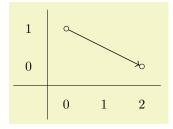
3.2 Global options

Specifies the degree of differentials. The $\langle x \ degree \rangle$ and $\langle y \ degree \rangle$ should both be mathematical expressions in one variable #1 that evaluate to integers on any input. They specify the x and y displacement

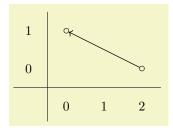
of a page #1 differential. In practice, they will usually be linear expressions with #1 coefficient 1, -1, or 0.

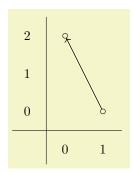
The <u>degree</u> option must be given before placing any differentials. It can be specified at the beginning of the <u>sseqdata</u> environment, at the beginning of the <u>sseqdata</u> environment if it is being used as a standalone page, or as a default by saying $sseqset{degree}{\langle x \ degree \rangle}{\langle y \ degree \rangle}}$ or $seqset{Adams \ grading}$ outside of the <u>sseqdata</u> and <u>sseqdata</u> environments.

You can make a named grading convention by saying \sseqset{my grading/.sseq grading={ $\langle x \ degree \rangle$ }{ $\langle y \ degree \rangle$ }. Then later passing my grading to a spectral sequence is equivalent to saying degree={ $\langle x \ degree \rangle$ }{ $\langle y \ degree \rangle$ }. The following grading conventions exist by default:



```
\begin{sseqpage}[cohomological Serre grading]{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{\center{grading}}{
```





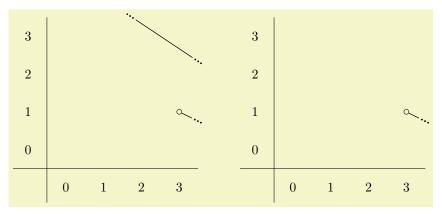
```
\begin{sseqpage}[Adams grading]% equivalent to degree={-1}{#1-1}
\class(0,2)
\class(1,0)
\d2(1,0)
\end{sseqpage}
```

```
x range=\langle x \ min \rangle \langle x \ max \rangle (no default)
y range=\langle y \ min \rangle \langle y \ max \rangle (no default)
```

These options force the x and y range to be a specific interval. By default, if no range is specified then the range is chosen to fit all the classes. If an x range is specified but no y range, then the y range is chosen to fit all the classes that lie inside the specified x range, and vice versa.

```
no orphan edges (no value) draw orphan edges=\langle boolean \rangle (default true) (initially true)
```

An edge is an "orphan" if both its source and target lie off the page. By default these are drawn, but with the option no orphan edges they are not. If the option no orphan edges has been set, draw orphan edges undoes it.



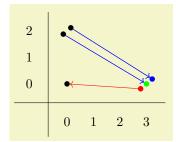
```
\begin{sseqdata} [name=orphan edges example, cohomological Serre grading, x range={0}{3}, y range={0}{3}]
\class(1,4)
\class(4,2)
\d3(1,4)
\class(5,0)
\d2(3,1)
\end{sseqdata}
\printpage[name=orphan edges example]
\hskip1cm
\printpage[name=orphan edges example, no orphan edges]
```

```
class placement transform=\{\langle transform \ keys \rangle\}
```

(no default)

The sseqpages option class placement transform allows the user to specify a Tikz coordinate transform to adjust the relative position of multiple nodes in the same (x,y) position. This coordinate transform can only involve rotation and scaling, no translation. Specifying a scaling factor helps if the nodes are too large and overlap. In some cases a rotation makes it easier to see which class is the target of a differential.

1		$\mathbb{Z}/2$ $\mathbb{Z}/3$
0	\mathbb{Z}	
	0	1



```
\label{lem:cohomological} $$ \begin{array}{l} [{\it classes=fill,class placement transform=\{rotate=40\}, \\ {\it cohomological Serre grading,differentials=blue,scale=0.7]} \\ {\it class(0,0)} \\ {\it class(0,2),class(0,2)} \\ {\it class[red](3,0),class[green](3,0),class[blue](3,0)} \\ \\ {\it dd}(0,2,1,2) \\ {\it dd}(0,2,1,-1) \\ {\it draw[->,red](3,0,1)--(0,0); } \\ {\it end\{sseqpage\}} \\ $$ \end{array} $$
```

3.3 Global Coordinate Transformations

Of the normal TikZ coordinate transformations, only the following are allowed to be applied to a sseq diagram:

 $xscale = \langle factor \rangle$ (no default)

```
yscale=\langle factor \rangle
                                                                                                            (no default)
                                                                                                              (no value)
xmirror
ymirror
                                                                                                              (no value)
rotate = \langle angle \rangle
                                                                                                            (no default)
       Layout
3.4
custom clip=
                                                                                                            (no default)
clip=\langle boolean \rangle
                                                                                    (default true) (initially true)
                                                                                          (no default, initially 0.5cm)
x axis gap=\langle dimension \rangle
y axis gap=\langle dimension \rangle
                                                                                          (no default, initially 0.5cm)
axes gap = \langle dimension \rangle
                                                                                          (no default, initially 0.5cm)
x label gap=\langle dimension \rangle
                                                                                          (no default, initially 0.5cm)
y label gap=\langle dimension \rangle
                                                                                          (no default, initially 0.5cm)
x axis start extend=\langle dimension \rangle
                                                                                          (no default, initially 0.5cm)
y axis start extend=\langle dimension \rangle
                                                                                          (no default, initially 0.5cm)
x axis end extend=\langle dimension \rangle
                                                                                          (no default, initially 0.9cm)
y axis end extend=\langle dimension \rangle
                                                                                          (no default, initially 0.9cm)
x clip axis padding=\langle dimension \rangle
                                                                                          (no default, initially 0.1cm)
y clip axis padding=\langle dimension \rangle
                                                                                          (no default, initially 0.1cm)
right clip padding=\langle dimension \rangle
                                                                                          (no default, initially 0.1cm)
left clip padding=\langle dimension \rangle
                                                                                          (no default, initially 0.4cm)
top clip padding=\langle dimension \rangle
                                                                                          (no default, initially 0.1cm)
bottom clip padding=\langle dimension \rangle
                                                                                          (no default, initially 0.4cm)
        Axes Style
3.5
x axis style=a
                                                                                         (no default, initially border)
y axis style=a
                                                                                         (no default, initially border)
                                                                                         (no default, initially border)
axes style=
                                                                                                (no default, initially 0)
x axis origin=
y axis origin=
                                                                                                (no default, initially 0)
no x axis
                                                                                                              (no value)
                                                                                                              (no value)
no y axis
no axes
                                                                                                              (no value)
draw x axis
                                                                                                              (no value)
draw y axis
                                                                                                              (no value)
draw axes
                                                                                                              (no value)
                                                                                                              (no value)
no x axis labels
                                                                                                              (no value)
no y axis labels
```

```
(no value)
no axes labels
draw x axis labels
                                                                                                   (no value)
draw y axis labels
                                                                                                   (no value)
draw axes labels
                                                                                                   (no value)
x label step=
                                                                                      (no default, initially 1)
y label step=
                                                                                      (no default, initially 1)
label step=
                                                                                      (no default, initially 1)
\verb"rotate labels="\\ \langle boolean \rangle
                                                                         (default true) (initially false)
```