## FROM LOTUS

APPENDIX B - THE FORMULA COMPILER

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## APPENDIX B: The Formula Compiler

This appendix describes the internal workings of the formula compiler. The

compiler transforms an ASCII string of characters representing a formula to

its Reverse Polish code. The basic algorithm utilizes and SR parser (SR =

shift and reduce). The aim of the parser is to apply a set of reduction

rules which embody the syntax of the compiler to an input string. Formula

code is compiled to a temporary buffer.

## Lexicon Analysis

A lexical analyzer breaks up the input string into lexical units called

tokens. A token is a substring of the original input string operand,

operator, or special symbol (such as comma, parentheses, etc.) In addition,

the lexical analyser supplies two special tokens, "beginning of formula"

(boform) and "end of formula" (eoform), to facilitate the compilation

process. The lexical analyzer identifies and processes literals (both

number and string), cell and range references, operators, and function

calls. It assigns a unique code to each distinct operator, function, or type of operand.

A function with no arguments is treated like a number.

Syntax Analysis

The syntactical analysis of a formula is accomplished by processing a list

of tokens in left-to-right order. A stack called the syntax is also used

during the syntactical scan. The basic algorithm is as follows:

Repeat the following steps:

- 1) Get the next token
- 2) If the token is a literal or cell reference:
  - a) Push the number code on the syntax stack
  - b) Push the number code on the syntax stack
- 3) If the token is a range reference:
  - a) Compile code to push the range reference

- b) Push the range code on the syntax stack
- 4) Otherwise push the token code for the token on the syntax stack.

For each syntax rule, if the pattern on the top of the syntax matches the

rule pattern take the action associated with the rule and start scanning

from the beginning for any additional rules which may apply.

When a token code is pushed on the syntax stack, an additional word of

zeros is also pushed on the stack. This is used when compiling function

calls to hold the function's argument count.

### Rule Matching

A relatively small number of rules are used to process formulas of arbitrary

complexity. If a rule matches the top of the syntax stack, then the

compiler takes a specific action and rule scanning starts again with the

first rule. Each rule matches certain patterns on the syntax stack. A

typical rule might be: if the top of the stack is the token for right

parenthesis, and the next-to-top is a number, and the second form the top

is a left parenthesis, then pop the top three items from the syntax stack

and push the number on the syntax stack.

This rule can be more succinctly represented as:

Stack

Before After

Action

)

number

( number

none

The Rules

The following are the syntax rules used to process formulas. Note that the

order of the rules is important. The rules for compilation of operators

used additional tables which assign a precedence number and opcode to each

legal unary and binary operator. Thus, for example, there is a single

token code for minus sign (-), but there are two opcodes one for unary

minus and one for binary minus. In addition, these two operators, while

lexically identical, also have different precedence. In general, operators

of higher precedence will be performed before operators of lower precedence

are performed left-to-right. All special operators (boform, eoform,

parentheses, comma, etc.) are implicitly assigned a precedence of zero.

Rule 1 Termination test

Stack

Before After Action

```
eoform
                                    Output a return code
to compile buffer
        number
                                     Return, indicating
successful compile
        boform
Rule 2 Function argument processing
                Stack
        Before
                        After
                                   Action
                                   Error if range
argument illegal for
        number or range
                                    function.
                        (
                                   Increment argument
count on stack
        function function
Rule 3 Process final function argument
                Stack
        Before
                  After
                                   Action
                                   Error if range
argument illegal for
                                    function.
        number or range
                                    Increment argument
count on stack
        function number
                                   Compile function
opcode
                                    If list function,
compile argument
                                    count; otherwise error
is wrong
                                    argument count.
```

Rule 4 Parenthesis removal

Stack

Before After Action

) Compile parenthesis opcode number ( number operator operator

Rule 5 Binary operators

Stack

Before After Action

op2 If binary op<br/>op,

rule does

number not match. Otherwise,

compile opcode

op1 op2 for operator op1.

Rule 6 Unary operators

Stack

Before After Action

op2 I unary op<br/>binary op,

rule does

number op2 not match. Otherwise,

compile opcode.

op1 number for operator op 1.

Rule 7 Error detection

Stack

Before After Action

eoform Return indicating

unsuccessful compile

Table 9 Operator Precedence Table

Operator	Unary Precedence	Binary
Precedence		
+	6	4
_	6	4
*	na	5
/	na	7
^	na	3
=	na	3
< >	na	3
< =	na	3
> =	na	3
<	na	3
>	na	3
#and#	na	1
#or#	na	1
#not#	2	na

## Example:

Using the above rules, we can now see how a particular formula is

compiled. Let us consider the following formula:

3+5\*6

This is broken up by the lexical analyzer into seven tokens.

boform

3 +

5

..

6

eoform

The syntax scans proceed as follows until a matching rule is found:

#### Stack

boform number + number

boform number +

boform number

boform

Compile buffer

push 3 push 3 push 3

push 5

At this point, rule 5 is invoked, but since the precedence of boform is  $\ensuremath{\mathsf{I}}$ 

zero, no action is taken.

### Stack

\* number

number \*

+ number

number +

boform number

boform

## Compile buffer

push 3
push 5
push 5

push 6

At this point, since the binary precedence of + is lower than the binary

precedence of \*, rule 5 does apply, and the opcode for \*
is compiled. The

stack is reduced by replacing number \* number by number and scan is made,

but no further rule applies.

#### Stack

number eoform
+ number
number +
boform number
boform

## Compile buffer

push	3	push	3
push	5	push	5
push	6	push	6

Rule 5 applies again, and the opcode for + is compiled, reducing the stack

to boform, number, eoform. Rescanning finds a match on rule 1 which

compiles a return opcode and terminates. The final compiled code is thus:

push 3
push 5
push 6

\* + return

A Note on the Decompiler

The algorithm for the formula decompiler was taken verbatim from:

Writing Interactive Compilers and Interpreters, P.J. Brown, John Wiley and Sons, 1979. See chapter 6.2. The algorithm itself is described on pages 216 and 217.

This algorithm is also described in the following article.

More on the Re-creation of Source Code from Reverse Polish, P.J. Brown,

Software Practice and Experience, Vol 7, 545-551 (1977).

#### WORKSHEET COLUMN DESIGNATORS

Most records within the 1-2-3 Condensed Worksheet format are specified

with column/row designators (for example, column 0, row 0 equals A1). When

determining the column designator, the table below will help make  $% \left( 1\right) =\left( 1\right) +\left( 1\right) +$ 

conversion easier.

			Dec	Column	Нех	Dec	Column
Hex A		0	1	ВА	34	52	DA
68 B	104		1	ВВ	35	53	DB
69 C	105	2	2	вс	36	54	DC
6A D			3	BD	37	55	DD
6B	107						
E 6C	108	_	4	BE	38	56	DE
F 6D	109	5	5	BF	39	57	DF
G 6E	110	6	6	BG	3A	58	DG
Н			7	ВН	3B	59	DH
6F I			8	BI	3C	60	DI
70 Ј	112	9	9	ВЈ	3D	61	DJ
71 K	113		10	ВК	3E	62	DK
72	114						
1 73			11	$_{ m BL}$	3F	63	${ m DL}$
M 74	116		12	BM	40	64	DM
N 75	117		13	BN	41	65	DN
0 76			14	ВО	42	66	DO
P			15	BP	43	67	DP
77 Q	119		16	BQ	44	68	DQ
78 R	120		17	BR	45	69	DR
79 S			18	BS		70	DS
7A	122						
Т		13	19	BT	47	71	DT

7B	123						
Մ 7C	124		20	BU	48	72	DU
V	121		21	BV	49	73	DV
7D W	125		22	BW	4A	74	DW
7E			22	DW	411	/ =	DW
X 7F	127		23	BX	4B	75	DX
	127		24	BY	4C	76	DY
80 Z	128		25	BZ	4D	77	DZ
81			23	52	40		DΔ
AA	120		26	CA	4 E	78	EA
82 AB	130		27	СВ	4 F	79	EB
83			20	CC	E O	0.0	EC
AC 84			28	CC	50	80	EC
	122		29	CD	51	81	ED
85 AE	133		30	CE	52	82	EE
86							
AF 87	135		31	CF	53	83	EF
AG		20	32	CG	54	84	EG
88 AH			33	СН	55	85	EH
89	137						
AI 8A			34	CI	56	86	ΕI
AJ		23	35	CJ	57	87	EJ
8B AK	139		36	СК	58	88	EK
8C	140						
AL 8D			37	CL	59	89	EL
AM		26	38	CM	5A	90	EM
8E AN			39	CN	5B	91	EN
8F				<b></b> .	02		1

AO		28	40	CO	5C	92	EO
90	144						
AP			41	CP	5D	93	EP
91							
~			42	CQ	5E	94	EQ
92			4.2	an.	<b>-</b>	0.5	- ED
AR 93	1 / 7		43	CR	5F	95	ER
AS	14/		44	CS	60	96	ES
94			11	CD	00	30	ЦО
AT			45	СТ	61	97	ET
95	149						
AU		2E	46	CU	62	98	EU
96	150						
AV			47	CV	63	99	EV
97							
	150		48	CW	64	100	EW
98			4.0	αv	65	1.0.1	T137
AX 99	152		49	CX	65	101	EX
AY	133		50	CY	66	102	ΕY
9A			30	O1	00	102	
	-5-		51	CZ	67	103	ΕZ
9В							

# (CONTINUED)

Dec	Column	Нех	Dec	Column	Нех
	FA	9C	156	НА	DO

200					
208	FB	9D	157	НВ	D1
209	FC	9E	158	НС	D2
210	FD	9F	159	HD	D3
211	FE	AO	160	HE	D4
212	FF			HF	D5
213		A1	161		
214	FG	A2	162	HG	D6
215	FH	A3	163	НН	D7
216	FI	A4	164	HI	D8
217	FJ	A5	165	HJ	D9
	FK	<b>A</b> 6	166	HK	DA
218	${ t FL}$	Α7	167	HL	DB
219	FM	A8	168	НМ	DC
220	FN	A9	169	HN	DD
221	FO	AA	170	НО	DE
222	FP	AB	171	HP	DF
223	FQ	AC	172	НQ	EO
224					
225	FR	AD	173	HR	E1
226	FS	AE	174	HS	E2
227	FT	AF	175	HT	E3
228	FU	во	176	HU	E4

	FV	В1	177	HV	E5
229	FW	В2	178	HW	E6
230	FX	В3	179	НХ	E7
231	FY	В4	180	НҮ	E8
232					
233	FZ	B5	181	HZ	E9
234	GA	В6	182	IA	EA
235	GB	В7	183	IB	EB
236	GC	В8	184	IC	EC
237	GD	В9	185	ID	ED
	GE	BA	186	IE	EE
238	GF	BB	187	IF	EF
239	GG	вс	188	IG	FO
240	GH	BD	189	IH	F1
241	GI	BE	190	II	F2
242	GJ	BF	191	IJ	F3
243	GK	CO	192	IK	F4
244					
245	GL	C1	193	IL	F5
246	GM	C2	195	IM	F6
247	GN	C3	195	IN	F7
248	GO	C4	196	IO	F8
	GP	C5	197	IP	F9

249					
	GQ	C6	198	IQ	FA
250					
251	GR	С7	199	IR	FB
231	GS	C8	200	IS	FC
252					
	GT	C9	201	IT	FD
253	<b></b>	<b>~</b> -	0.00		
254	GU	CA	202	IU	FE
234	GV	СВ	203	IV	FF
255					
	GW	CC	204		
	GX	CD	205		
	GY	CE	206		
	GZ	CF	207		

## ANALYSIS OF 1-2-3 WORKSHEET FILE

The worksheet shown below was created in 1-2-3 and saved to disk.

Key:
A2A5 Named
A2: Label
A3:
A4:
A5:
(code

The example shown below is a partial hex dump of this worksheet file. By

reading each record header, you can determine the type of record you are

encountering. The record header will also tell you the length of that

follows the header. By analyzing the record header, you can read the

records you want and skip unrelated records.

	362B:0100							06	00	08	00	00	00
00	00 00 00												
	362B:0110	04	00	2F	00	01	00	01	02	00	01	00	FF
03	00 01 00												
	362B:0120	00	04	00	01	00	00	05	00	01	00	FF	07
00	1F 00 00												
	362B:0130	00	01	00	71	00	09	00	80	00	14	00	00
00	00 00 00												
	362B:0140	00	00	00	00	00	00	00	04	00	04	00	48
00	00 0B 00												
	362B:0150	18	00	54	45	53	54	00	00	00	00	00	00
00	00 00 00												
	362B:0160	00	00	00	00	01	00	00	00	04	00	18	00
19	00 00 FF												
	362B:0170	FF	00	00	FF	FF	00	00	FF	FF	00	00	FF
FF	00 00 FF												
	362B:0180												
	362B:05C0												
	362B:05D0	00	00	00	00	00	00	00	00	00	00	00	00
00	00 00 00												
	362B:05E0	00	00	00	00	00	00	00	00	00	00	00	00
00	00 00 00												
	362B:05F0	00	00	00	00	71	71	01	00	0F	00	0E	00
FF	00 00 01												
	362B:0600	00	27	45	58	41	4 D	50	4C	45	00	0 D	00

07	00 FF 00												
	362B:0610	00	02	00	64	00							
	362B:0620							10	00	1B	00	FF	00
00	04 00 00												
	362B:0630	00	00	00	00	ΕO	55	40	0C	00	01	00	80
FE	BF 01 00												
	362B:0640	80	FF	BF	0A	03							