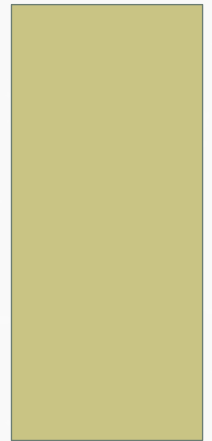


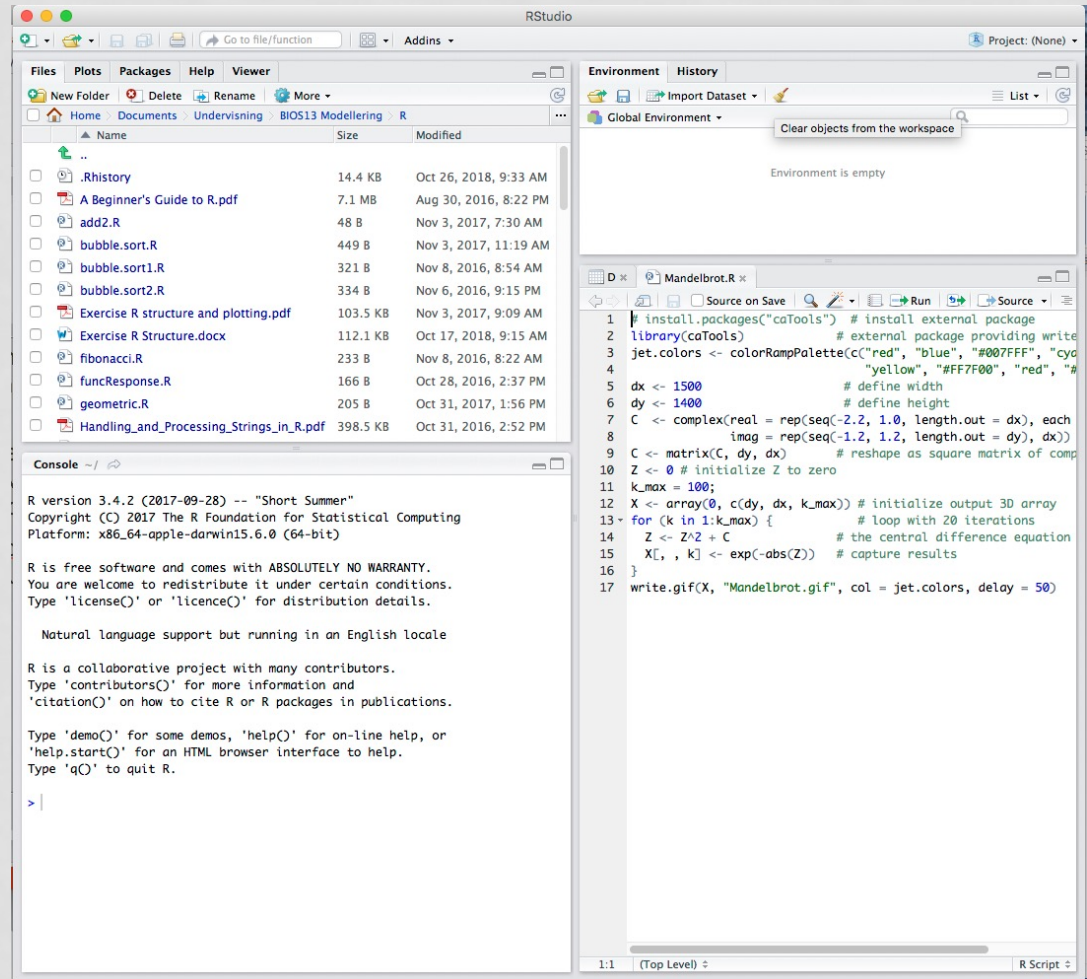
VARIABLES, VECTORS AND FLOW CONTROL IN R

MODELLING BIOLOGICAL SYSTEMS, BIOS13
PEDRO ROSERO



R

- **R** is a programming language
- **RStudio** is a convenient environment for working with R. There are others.
- We will use the RStudio environment throughout this course.



Variables in R

(<-, objects, ls, rm)

- Variables are created by assignment:

```
> x <- 3  
> x  
[1] 3
```

The value 3 is copied!

- Each variable is an object in the current workspace (= a part of computer memory):

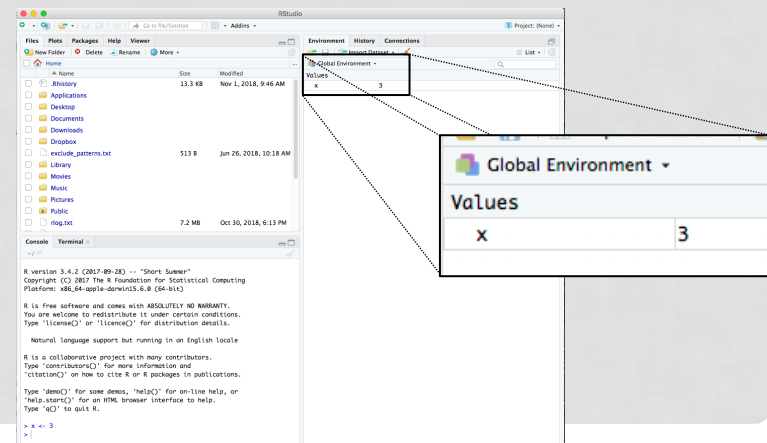
```
> objects()  
[1] "x"
```

Equivalent:

```
> ls()  
[1] "x"
```

- Also check the “Environment” tab:
- Delete (remove) a variable:

```
> rm(x)
```



Mathematical Operators in R

- Mathematical operators: $+$, $-$, $*$, $/$, $^$

- Examples:

```
> 23 + 13
```

```
[1] 36
```

```
> 4*5 + 7
```

```
[1] 27
```

```
> 4*(5+7)
```

```
[1] 48
```

```
> 4*(5+7)^2
```

```
[1] 576
```

- The operations are carried out in order of *precedence*, which is the reverse order of the list above. Precedence can be overridden with parantheses $()$.

Exercise (stolen from this afternoon)

Mathematical operators: +, -, *, /, ^

Calculate (you find the correct answer on the right):

a) 2^8 256

b) $\frac{26}{7}$ 3.714286

c) $\frac{26+2^8}{7}$ 40.28571

d) $26 + 2^{8/7}$ 28.20818

e) $(26 + 2)^{8/7}$ 45.07076

Mathematical Functions in R

- **Basic mathematical functions**

R

`exp(x)`, `log(x)`

`sin(x)`, `cos(x)`, `tan(x)`

`asin(x)`, `acos(x)`, `atan(x)`

`log10(x)`

`sqrt(x)`

`abs(x)`

`pi`

`round(x)`, `floor(x)`, `ceiling(x)`

Standard math

e^x , $\ln(x)$ or $\log(x)$

$\sin(x)$, $\cos(x)$, $\tan(x)$

$\sin^{-1}(x)$, $\cos^{-1}(x)$, $\tan^{-1}(x)$

$\log_{10}(x)$

\sqrt{x}

$|x|$

π (3.1415964 ...)

rounding (nearest, down, up)

- **Other operations**, not commonly used in math:

`%/%` integer division (remove decimals)

`%%` modulo (the remainder, after division)

Special values

NA	Missing Value (Not Available)
NaN	Undefined (Not A Number)
NULL	Empty set (Nothing)
Inf, -Inf	Infinity

```
> a <- NA
> a + 3
[1] NA
> 1/a
[1] NA
> 1/0
[1] Inf
> -1/0
[1] -Inf
> log(0)
[1] -Inf
> 0/0
[1] NaN
```

```
> 4 < 1/0
[1] TRUE
> 4 < -1/0
[1] FALSE
> c <- NULL
> c + 5
numeric(0)
```

A numeric vector with
0 elements

Logical operators in R

Logical operators generate logical values (TRUE or FALSE, T or F)

- Comparisons: <, <=, >, >=, ==, !=
- Operators:

! negation

&, && And

|, || Or

These operators are 'lazy'. The second value is not calculated if the first is FALSE (&&) or TRUE (||). Sometimes useful.

```
> 3 < 7
[1] TRUE
> 3 + 5 < 7
[1] FALSE
> 4 == 0
[1] FALSE
> a <- 6
> b <- 10
> a > 6
[1] FALSE
> a >= 6
[1] TRUE
> a != b
[1] TRUE
> a != a
[1] FALSE
```

```
> a > 8 & b > 1
[1] FALSE
> a > 8 && b > 1
[1] FALSE
> a > 8 | b > 1
[1] TRUE
> a > 8 || b > 1
[1] TRUE
> !(a > 8 || b > 1)
[1] FALSE
> c <- a > b
> c
[1] FALSE
> !c
[1] TRUE
```


Vectors in R

(c, seq, rep)

- Vectors are sequences of objects of the same type, usually numbers
- Vectors can be created with the `c()` (combine or concatenate) command

```
> c(3, 4.5, 6, 78)
[1] 3.0 4.5 6.0 78.0
```

Since the result is not stored in a variable, it is printed and then lost

- Other constructions:

```
> 1:5
[1] 1 2 3 4 5
> 5:1
[1] 5 4 3 2 1

> seq(1,5,by=2)
[1] 1 3 5
> seq(1,5,length=9)
[1] 1.0 1.5 2.0 2.5 3.0 3.5 4.0 4.5 5.0

> rep(3,4)
[1] 3 3 3 3
> rep(3:7,2)
[1] 3 4 5 6 7 3 4 5 6 7
```

Check "R quick guide" for more examples!

Some useful vector functions

<code>length(v)</code>	the number of elements
<code>max(v), min(v)</code>	the largest and smallest value
<code>range(v)</code>	equivalent to <code>c(min(x), max(v))</code>
<code>sort(v)</code>	creates a sorted vector (does not change v!)
<code>sum(v)</code>	the sum of all elements
<code>cumsum(v)</code>	the cumulative sum (a new vector)
<code>prod(v)</code>	the product of all elements
<code>cumprod(v)</code>	cumulative product (a new vector)
<code>mean(v), median(v)</code>	mean and median
<code>var(v), sd(v)</code>	variance and standard deviation
<code>all(v)</code>	logical testing if all elements of <code>v == TRUE</code>
<code>any(v)</code>	logical testing if any element of <code>v == TRUE</code>

Mathematical expressions with vectors

Basic mathematical expressions and functions are carried out element-by-element in a vector.

```
> x <- 2:6
> x
[1] 2 3 4 5 6
> x + 4
[1] 6 7 8 9 10
> y <- 5:9
> y
[1] 5 6 7 8 9
> x + y
[1] 7 9 11 13 15
> x*y
[1] 10 18 28 40 54
> x^y
[1] 32 729 16384 390625 10077696
> exp(x)
[1] 7.389056 20.085537 54.598150 148.413159 403.428793
> sin(y)*cos(x)
[1] 0.3990533 0.2766192 -0.4294351 0.2806435 0.3957039
```

Indexing

([], length)

- Single elements of a vector are obtained through indexing within square brackets:

```
> v1 <- seq(1,3,by=0.5)    # create a vector
> v1                       # print out its values
[1] 1.0 1.5 2.0 2.5 3.0

> length(v1)               # check its size
[1] 5

> v1[3]                    # element number 3
[1] 2

> v1[4] <- 8                # assign a new value to element 4
> v1
[1] 1.0 1.5 2.0 8.0 3.0
```

More indexing ([])

- Extract a part of a vector: (v1 from previous slide)

```
> v1[2:4]
[1] 1.5 2.0 8.0

> v1[c(1,5,2)]
[1] 1.0 3.0 1.5

> v1[-2]   # everything but element 2
[1] 1 2 8 3

> v1[-(2:3)]
[1] 1 8 3
```

- Assigning values to a part of a vector:

```
> v1[4:5] <- -1
> v1
[1] 1.0 1.5 2.0 -1.0 -1.0
```

Indexing with logical vectors

- A logical vectors has elements that are either TRUE (T) or FALSE (F) (**DON'T** use T or F as variable names!)

```
> v2 <- c(T,T,T,F)
> v2
[1] TRUE TRUE TRUE FALSE
```

- It can be the result of a logical expression:

```
> x <- c(4,34,88,9)
> x < 10 # the comparison is done element-by-element
[1] TRUE FALSE FALSE TRUE
```

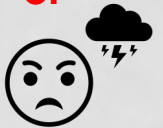
- Logical vectors can be used for indexing:

```
> x[c(T,T,F,T)] # pick out the elements corresponding to TRUE values
[1] 4 34 9
> x[x<10] <- 0 # assign value zero to the chosen elements
> x
[1] 0 34 88 0
```

Using scripts

(source)

- Scripts are a handy way of saving your commands, for later reference. It also simplifies using complicated commands tremendously.
- Workflow:
 - Edit the script, save
 - Run it (use `source` command in console window, or use keyboard shortcut (SHIFT+⌘+S on mac or SHIFT+CTRL+S on windows). **Avoid “run” or copy+paste in the console!**
 - Check results, edit again, a.s.o.
- Running a script is (almost) equivalent to typing the same sequence of commands in the console.



Why does “run” or copy+paste in the console is not appropriate if programming?

- It messes up output with code, making it difficult to track what has been done. What were the parameter values?
- The next day, do you know how you solved the problem?
- “Run the current selection” is using R as an advanced calculator, it is not programming.

Programs are sequences of commands that together perform some well defined task.

You will never learn programming unless you start writing programs.

- From now on: 1 task \Leftrightarrow 1 script (or more)

EXERCISE

(cat)

- Write a script that:
 - Creates a vector `v1` with the values 1, 1.5, 2, 2.5, ...,7
 - Creates another vector `v2` with the 3rd, 4th and 11th elements of `v1`
 - Assigns zero to all elements of `v2` larger than 2.
 - Prints out `v2` in the console (use `'cat (v2)'`)
- Run the script using `'source'` in the console

- If the output is *not*

2 0 0

, correct the script, save and run (source!!!) it again.

More on vectors

(+, -, *, /, ^, NA)

- Assigning can extend a vector (NA = missing value)

```
> x <- 1:3
> x
[1] 1 2 3
> x[6] <- 99
> x
[1] 1 2 3 NA NA 99
```

- Vector arithmetics (element-by-element)

```
> x + c(3,5,1,1,0,1)
[1] 4 7 4 NA NA 100
> x * c(3,5,1,1,0,1)
[1] 3 10 3 NA NA 99
```

- Vectors are *recycled* when necessary!

```
> x + c(1,2)
[1] 2 4 4 NA NA 101
```

Strings = character objects

("", "'", mode, paste, substr)

```
> s1 <- "Hi there" # or 'Hi there'
> s1
[1] "Hi there"

> mode(s1)
[1] "character"

> s1[2] <- "students" # adding an element will increase the length of s1
> s1
[1] "Hi there" "students" # s1 is now a character vector with two elements

> paste('Hi there', ', ', 'students', sep = ' ')
[1] "Hi there, students"
> # use paste to merge strings (in many, many, different ways)

> substr(s1[1],1,4) # use substr to access parts of a string
[1] "Hi t"
> substr(s1[1],1,4) <- 'Dude'
> s1
[1] "Dudehere" "students"

> nchar(s1[1]) # returns the number of characters in s1[1]
[1] 8
```

Lists

(list, \$, [[]])

- Lists are like vectors, an indexed set of objects, *components*, but the components need not be of the same type.
- The components of lists are often named. It is easier to recall a name rather than an index. Names also makes the code easier to interpret.
- Use the '\$' operator to access named components, or [[double brackets]] for indexing.

```
> mylist <- list(car="volvo", weight=9,
"unnamed")
> mylist
$car
[1] "volvo"

$weight
[1] 9

[[3]]
[1] "unnamed"

> mylist$car
[1] "volvo"
> mylist[[1]]
[1] "volvo"
> mylist[[3]]
[1] "unnamed"

> y <- list(1:5)
> y
[[1]]
[1] 1 2 3 4 5

> y[[1]]
[1] 1 2 3 4 5
```

Create a list
from a vector

y has only one
component

Conversions ('coercions') between types (modes)

```
> s <- "12"
> as.numeric(s)
[1] 12

> as.character(43)
[1] "43"

> as.character(pi)
[1] "3.14159265358979"

> as.integer(3.9)
[1] 3

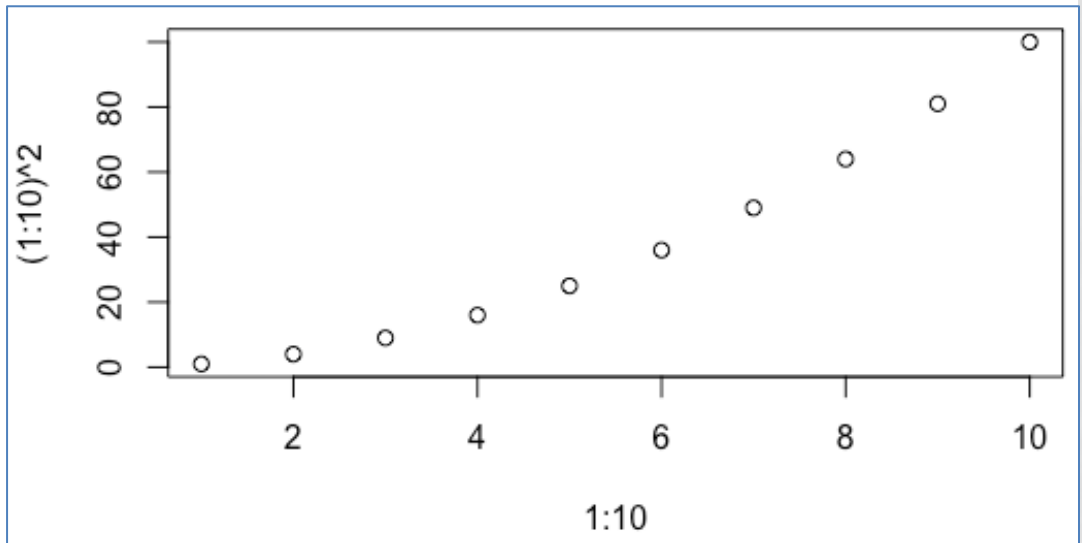
> round(3.9)
[1] 4

> as.integer("549ppp")
[1] NA
Warning message:
NAs introduced by coercion
```

Simple input and output

(readline, scan, cat, plot, line, points)

- `x <- readline("Type x:")` # For input of strings.
Convert to numbers if necessary.
'scan()' is also useful for input.
- `cat(x)` # Outputs x in console window
- `plot(x,y)` # Plots y vs. x in plot window
- `> plot(1:10, (1:10)^2)`
- line and points will add to an existing graph



Flow control

- If-statements
- While, repeat (and break)
- For-loops

The `if` statement

(`if`, `else`)

- The `if` statement is used for conditional expressions or commands

```
if ( condition ) expression
```

or

```
if ( condition ) expression1 else expression2
```

```
> x <- rnorm(1)
> if (x < 0) x <- -x
> x
[1] 0.3441755

> x <- runif(1)
> x
[1] 0.846157
> y <- runif(1)
> y
[1] 0.6319267
> if (x > y) z <- x else z <- y
> z
[1] 0.846157
```

The `if` statement, cont'd

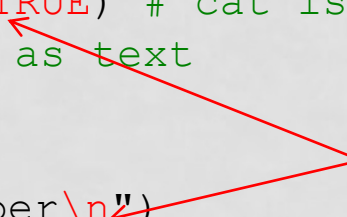
(`{}`)

- The expressions of an `if` statement are often *compound*, or *grouped*, i.e. a sequence of commands within `{curly brackets}`

```
print("Enter a number")
x <- scan(nmax=1)    # scan can be used for keyboard input of
                     # numbers, but also input from files

cat("You entered:", x , fill=TRUE) # cat is useful for
                                   # combining and printing output as text

if (x >= 0) {
  cat("It is a positive number\n")
  cat("Its double value is", 2*x, "\n")
} else {
  cat("It is a negative number", fill=T)
  cat("Half its value is", x/2, fill=T)
}
```



Use one of these to
get a new line

while and repeat

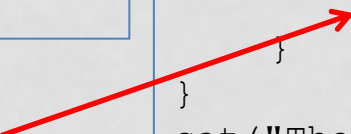
(while, repeat, break)

- while and repeat are used to repeat a command, or a sequence of commands, several times

Exercise: Generate a random number from a geometric distribution
It can be interpreted as the number of times you have to roll a die *before* you get a certain result, e.g. before you get a 6.

```
n <- 0           # starting value
x <- runif(1)     # roll the die!
while (x < 5/6) { # while failure...
  n <- n+1        # increase the count
  x <- runif(1)   # roll again!
}
cat("The number is", n, fill=F)
```

```
n <- 0 # starting value
repeat {
  x <- runif(1) # roll the die
  if (x < 5/6) { # if failure
    n <- n+1    # increase the count
  } else {     # else
    break      # exit repeat
  }
}
cat("The number is", n, fill=F)
```



This is necessary to break the loop!

for-loops: if you know how many times something will be repeated

```
for ( name in expression1 ) expression2
```

If *expression1* is a vector, the loop-variable *name* is given its values, one at a time

```
> for (i in 1:3) print(1:i)
[1] 1
[1] 1 2
[1] 1 2 3
```

```
> str <- c('a','vector','of','strings')
> str
[1] "a"          "vector"    "of"        "strings"
> for (s in str) cat(substr(s,1,3),' ')
a  vec  of  str
```

for-loops, cont'd

(rnorm)

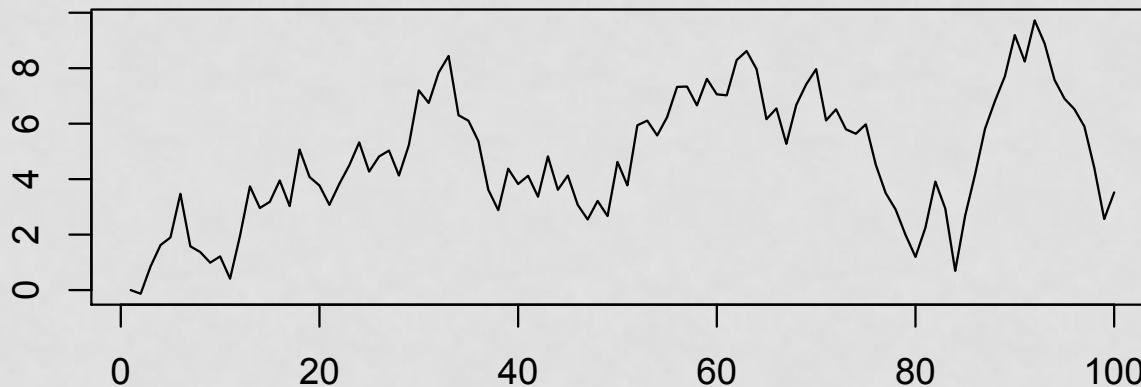
```
# a sample script to generate random numbers and plot local optima

x <- rnorm(20)           # generate 20 random numbers
plot(1:20, x, type='b')  # 'b' stands for 'both', i.e. line + points
for (i in 2:19) {
  if (x[i-1] < x[i] && x[i+1]<x[i]) { # is x[i] a local max?
    cat('Found maximum at', i, fill=T)
    points(i, x[i], col='red') # mark the maximum
  }
}
```

Exercise: Generate a random walk and plot it

- Definition of a random walk:

- $x[1] = 0$
- $x[i+1] = x[i] + \text{rnorm}(1)$



- *Task:* Write a script that inputs the length of the walk, generates a sample time series, and plots it as a solid line (`plot(x, type='l')`)
- *Extra:* generate 10 sample time series and plot them all in the same graph