

# Data Representation

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HAiV

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## Disclaimer

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  - Dr. David Ebert (Purdue)

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## Data Models

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- Data models/representations are structured forms suitable for computer-based transformations
- These structures exist in the original data or are derivable from the original data
- Structures retain the information and knowledge content and the related context within the original data
- These structures are transformable into lower-dimensional representations for visualization and analysis

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## Data Models vs. Conceptual Models

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- **Data models are mathematical abstractions**
  - We can perform numerical operations, addition, subtraction, etc.
- **Conceptual models are our mental constructs**
  - These contain semantic structure and support reasoning
  - Think of giving directions to someone using landmarks

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# What Types of Data Models Do We Have?



## • Relational Data Models

- These are data records that you deal with in excel, or typical database records
- Data records are of fixed length and well-defined
- Data is in rows and columns where each column has a domain type

	A	B	C
1	Animal	Brain Weight (kg)	Body Weight (kg)
2	Mountain beaver	1.35	465
3	Cow	465	423
4	Grey wolf	36.33	119.5
5	Goat	27.66	115
6	Guinea pig	1.04	5.5
7	Dipliodocus	11700	50
8	Asian elephant	2547	4603

Codd, E.F. (1970). "A Relational Model of Data for Large Shared Data Banks". Communications of the ACM 13(6): 37-387

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# What Types of Data Models Do We Have?



## • Relational Data Models

- There may be a relationship defined in a schema between tables
- A database is a collection of these relations

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# What Types of Data Models Do We Have?



## • Statistical Data Models

- This consists of variables or measurements (think of things like the census)
- Categories are factors relating to the measurements
- Observations or cases

Patient ID	Date	Chief Complaints	Location
9398	4/16/09	Ear pain	Karachi
10816	4/16/09	Stuffy nose	Lebanon
1491	4/16/09	Fever	Allepo
16237	4/16/09	Head bleed	Yemen

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## Data Types



### • Nominal

- Data whose categories have no implied ordering
- Examples include political affiliations of a population

### • Ordinal

- Data that has a specified order, but no specified distance metric
- Examples include beverage sizes at McDonalds (Small, medium, large)

1- SS Stevens, "On the Theory of Scales of Measurement," *Science*, 103(2684):677-680, 1946.

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## Data Types

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### • Interval

- Data that has measurable distances
- Examples include periods of time (second, minute, etc.) – the zero point is arbitrary

### • Ratio

- Same as interval, but include a zero point
- Example include Celsius scale, height above sea level

1- SS Stevens, "On the Theory of Scales of Measurement," *Science*, 103(2684):677-680, 1946.

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## Mapping Data

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- We need to know how to assign quantitative dimensions of our data to *aesthetic attributes*<sup>1</sup> of the data

Form	Surface	Motion	Sound	Text
Position	Color	Direction	Tone	Label
Size	hue	Speed	Volume	
Shape	brightness	Acceleration	Rhythm	
polygon	saturation		Voice	
glyph	Texture			
image	pattern			
Rotation	granularity			
Resolution	orientation			
	Blur			
	Transparency			

L Wilkinson (2005) *The Grammar of Graphics*

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# Aesthetic Attributes

- An attribute must be capable of representing both continuous and categorical variables
- When representing a continuous variable, an attribute must vary primarily on one psychophysical dimension
- In order to use multidimensional attributes (such as color), we must scale them on a single dimension
- An attribute does not imply a linear perceptual scale
- Much of the skill in graphic design is knowing what combination of attributes should be avoided<sup>1</sup>

<sup>1</sup>-SM Kosslyn (1994), *The Elements of Graph Design*

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## 8 Visual Variables

- **Visualization is concerned primarily with a mapping to visual form**
- **[x,y]**
  - Position
- **[z]**
  - Size (Taille)
  - Value (Valeur)
  - Color (Couleur)
  - Texture (Grain)
  - Orientation
  - Shape (Forme)

LES VARIABLES DE L'IMAGE							12	14
XY 2 DIMENSIONS DU PLAN	POINTS		LIGNES		ZONES			
Z TAILLE								
VALEUR								
LES VARIABLES DE SÉPARATION DES IMAGES							13	
GRAIN								
COULEUR								
ORIENTATION								
FORME								

J Bertin (1967), *The Semiology of Graphics*

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## Position

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- Position refers to a location in a multi-dimensional space
- **Continuous variables** map to densely distributed locations
- **Categorical variables** map to a lattice
- Positions are ordered, but the ordering may or may not have meaning in terms of what is being measured
- Sometimes, position is just a way to keep things from overlapping

L Wilkinson (2005) *The Grammar of Graphics*

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## Position<sup>1</sup>

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- Cleveland<sup>2</sup> rates position on a common scale as the **best way to represent a quantitative dimension visually**
- This reflects research findings that points or line lengths placed adjacent to a common axis enable judgments with the least bias or error
- However, this recommendation has a caveat, as it depends on how far the graphic primitive (point, line, etc.) is from a reference axis<sup>3</sup>
- If a graphic is far from an axis, the multiple steps needed to store and decode the variation can impair judgment

1 - L Wilkinson (2005) *The Grammar of Graphics*

2 - WS Cleveland, *The Elements of Graphing Data*, 1985

3 - D Simkin and R Hastie (1987). An information processing analysis of graph perception. *Journal of the American Statistical Association*, 82, 454-465

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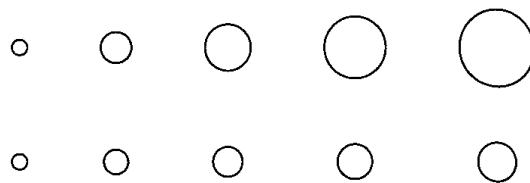




## Size

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- For objects with rotational symmetry, we can map size to the diameter rather than area
- Representing data through area or volume should probably be confined to positively skewed data that can benefit from the perceptual equivalent of the square root transformation



Top row changes diameter from 1-5  
Bottom row changes area from 1-5

L Wilkinson (2005) *The Grammar of Graphics*

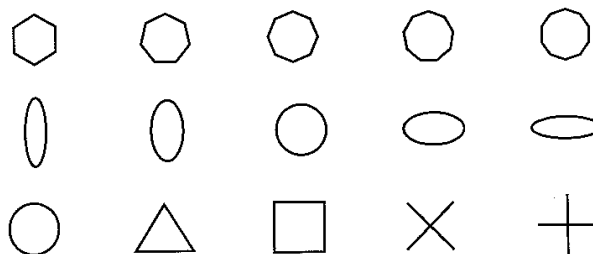
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## Shape

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- Shape refers to the shape or boundary of an object
- Examples would include map symbols
- Shape must vary without affecting size, rotation and other attributes



L Wilkinson (2005) *The Grammar of Graphics*

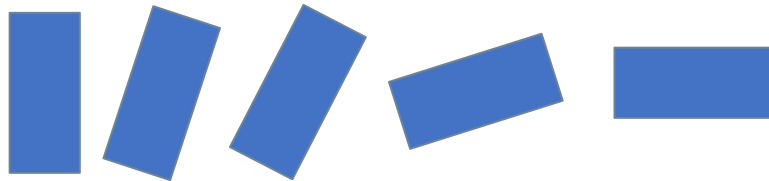
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## Rotation

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- This is the rotational angle of the graphic primitive
- Lines, areas and surfaces can only rotate if they are positionally unconstrained



L Wilkinson (2005) *The Grammar of Graphics*

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## Color

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- Color is really a psychological phenomenon
- The physical stimulus for color is light
- We see color because of the photoreceptors in our retina



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## Color

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- Use of Rainbow?



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## Texture

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- Texture includes pattern, granularity and orientation
- Granularity is the repetition of a pattern per unit of area
- Orientation is the angle of the pattern
- Textures can be described in a variety of ways
  - Fourier transform – decomposes a grid of brightness values into sums of trigonometric components
  - This decomposition is orientation dependent
  - Auto-correlogram – characterize the spatial moments of a texture

L Wilkinson (2005) *The Grammar of Graphics*

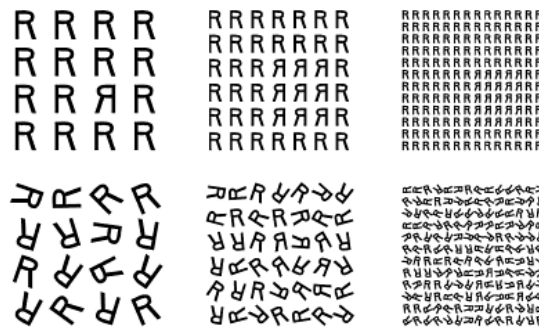
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## Texture

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- Texture alone can be a basis for perception
- Two gray areas that have the same overall level of brightness can be discriminated if their texture is different



L. Wilkinson (2005) *The Grammar of Graphics*

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## Texture

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- Granularity – Changing the size or resolution of patterns in a texture changes the granularity
  - Less grainy patterns (those with low-frequency spatial components) are more difficult to resolve
- Pattern – Patterns make use of increasing degrees of randomness to encode data

L. Wilkinson (2005) *The Grammar of Graphics*

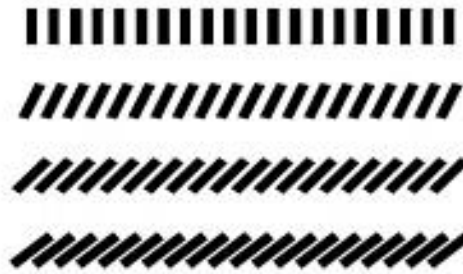
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# Texture

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- Orientation – Variation in texture orientation can introduce visual illusions (making lines not seem parallel) and is typically avoided as an encoding in textures



L Wilkinson (2005) *The Grammar of Graphics*

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	Point	Line	Area	Surface
Form				
Size	• • •	≡ ≡ ≡	□ □ □	▭ ▭ ▭
Shape	• ■ ▲	≡ ≡ ≡	△ ▢ ▣	▭ ▭ ▭
Rotation	◀ ▶ ▶	≡ ≡ ≡	□ □ □	▭ ▭ ▭
Color				
Brightness	• • •	≡ ≡ ≡	□ □ □	▭ ▭ ▭
Hue	• • •	≡ ≡ ≡	□ □ □	▭ ▭ ▭
Saturation	• • •	≡ ≡ ≡	□ □ □	▭ ▭ ▭
Texture				
Granularity	◊ ◊ ◊	≡ ≡ ≡	▭ ▭ ▭	▭ ▭ ▭
Pattern	◊ ◊ ◊	≡ ≡ ≡	▭ ▭ ▭	▭ ▭ ▭
Orientation	◊ ◊ ◊	≡ ≡ ≡	▭ ▭ ▭	▭ ▭ ▭
Optics				
Blur	• • •	≡ ≡ ≡	▭ ▭ ▭	▭ ▭ ▭
Transparency	• • •	≡ ≡ ≡	▭ ▭ ▭	▭ ▭ ▭

L Wilkinson (2005) *The Grammar of Graphics*, p. 317

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## Groups of Representation

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- Bertin describes four groups of representations
- *Diagrams* – correspondences are between a single component (think of things like a bar chart or a line graph)
- *Networks* – correspondences between different components are linked together
- *Maps* – correspondences between components are arranged according to geography
- *Symbols* – correspondences between components is linked to a symbol or a shape

J Bertin (1967), *The Semiology of Graphics*

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## Taxonomy by Data Type<sup>1</sup>

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- 1D (sets and sequences)
- Temporal
- 2D (maps)
- 3D (shapes)
- nD (relational)
- Trees (hierarchies)
- Networks (graphs)
- Text and Documents<sup>2</sup>

<sup>1</sup> – B. Shneiderman. *The Eyes Have It: A Task by Data Type Taxonomy for Information Visualizations*. In the Proceedings of the IEEE Symposium on Visual Languages, pp. 336-343, 1996.


















<sup>2</sup> – Borrowed from Pat Hanrahan's "From Data to Image" lecture: <http://graphics.stanford.edu/courses/cs448b-04-winter/lectures/encoding/>

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# Types of Graphic Representation

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GROUPS OF IMPOSITION	TYPES OF IMPOSITION				
	ARRANGEMENT	RECTILINEAR	CIRCULAR	ORTHOGONAL	POLAR
DIAGRAMS		 	 	 	 
NETWORKS		 	 	 	
MAPS					
SYMBOLS					

J Bertin (1967), *The Semiology of Graphics*, p. 52

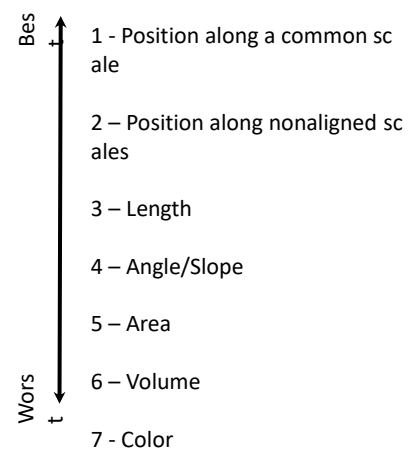
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## Cleveland's Hierarchy<sup>1</sup>

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- Cleveland evaluated elements when isolated
- Tasks were restricted to magnitude and ratio comparisons
- Research indicates this hierarchy may be best in pre-attentive stages or when focusing only on portions of a graphic<sup>2,3,4</sup>



1 - WS Cleveland, *The Elements of Graphing Data*, 1985

2 - Spence, I., and Lewandowsky, S. (1991). Displaying proportions and percentages. *Applied Cognitive Psychology* 5, 61-77

3 - Simkin, D., and Hastie, R. (1987). An information processing analysis of graph perception. *Journal of the American Statistical Association*, 82, 454-465

4 - Carswell, C. M. (1992). Choosing specifiers: An evaluation of the basic tasks model of graphical perception. *Human Factors*, 4, 535-554

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## What if I Combine Encodings?

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- So, what happens when we combine several scales in a single display?
- Can we represent one quantitative dimension with color and another with orientation and expect a perceiver to respond to both dimensions?
- Do these things make psychological sense?

L Wilkinson (2005) *The Grammar of Graphics*

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## Integral Versus Separable Dimensions

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- “A configuration has properties that have to be expressed as some form of interaction or interrelation between the components, be they features or dimensions.”<sup>1</sup>
- *Integral dimensions* are not as easily decomposable by perceivers as *separable dimensions*
- Separating hue from brightness in a color (integral dimensions) are harder to decompose than say size and texture (separable dimensions)

<sup>1</sup> – Garner, W. R. (1981). The analysis of unanalyzed perceptions. In M. Kubovy and J. R. Pomerantz (Eds.), *Perceptual Organization* (pp. 119-139). Hillsdale, NJ: Lawrence Erlbaum.

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## Integral Versus Separable Dimensions

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- Discriminations between classes defined by **multiple integral stimuli** are more **difficult** than those between classes defined by **separable stimuli**
- Selective attention to only one dimension is more difficult with integral stimuli
- Redundant cues in classification improve performance for integral stimuli and degrade performance for separable

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## Combinatorics of Encodings

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- **Principle of Consistency:** The properties of the image should match the properties of the data
- **Principle of Importance Ordering:** Encode the most important information in the most effective way

1 – This slide is borrowed from Pat Hanrahan's "From Data to Image" lecture: <http://graphics.stanford.edu/courses/cs-448b-04-winter/lectures/encoding/>

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## The Expressiveness & Effectiveness Criteria

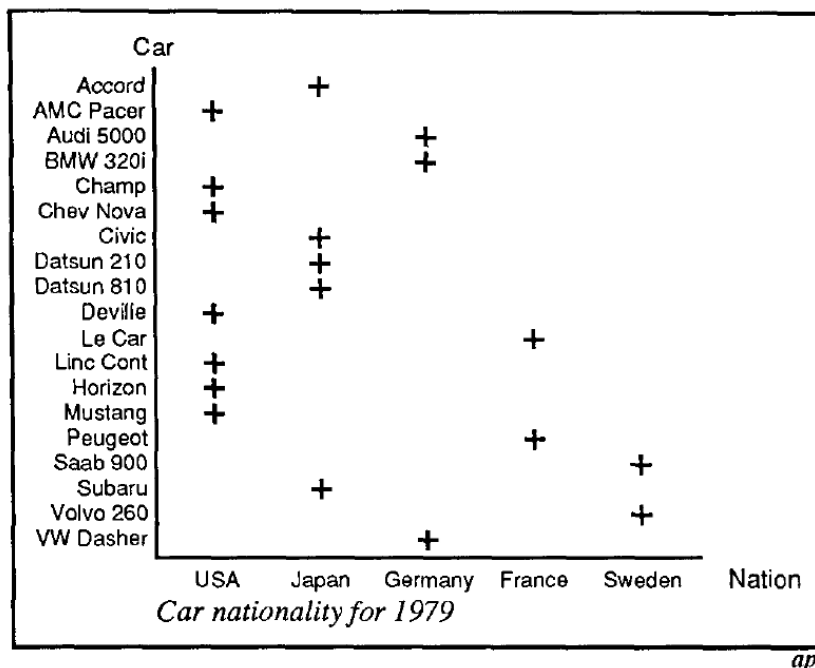
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- **Expressiveness:** A set of facts is expressible in a visual language if the visualizations express all the facts in the set of data, and only the facts in the data
- **Effectiveness:** A visualization is more effective than another visualization if the information conveyed by one visualization is **more readily perceived** than the information in the other visualization

1 – J. Mackinlay, Automating the Design of Graphical Presentations of Relational Information, ACM Transactions on Graphics, 5(2): 110-141, 1986.

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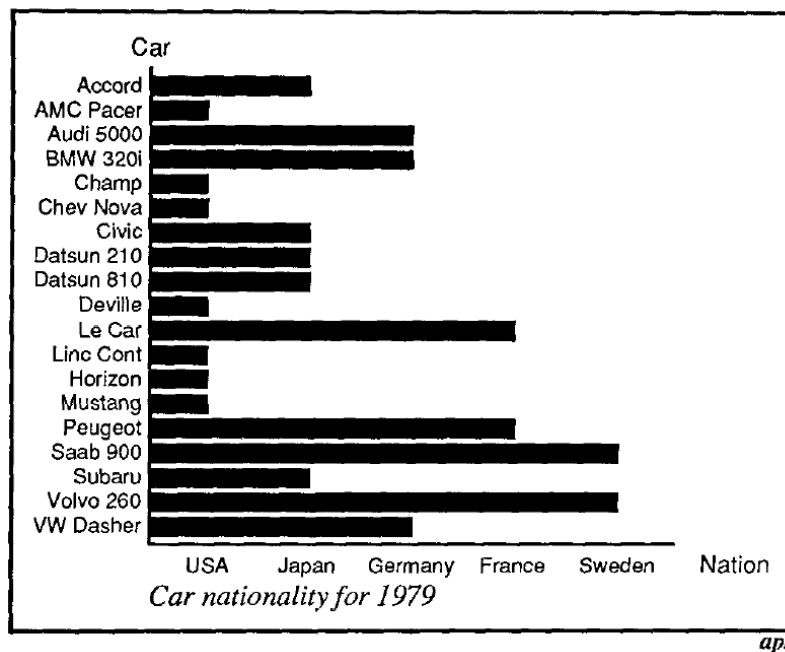
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1 – J. Mackinlay, Automating the Design of Graphical Presentations of Relational Information, ACM Transactions on Graphics, 5(2): 110-141, 1986.

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1 – J. Mackinlay, Automating the Design of Graphical Presentations of Relational Information, ACM Transactions on Graphics, 5(2): 110-141, 1986.

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## Potentially Expressive/Effective

- Extensions to the expressive/effectiveness criteria are necessary under interaction
- Potential Expressiveness: A visualization is potentially expressive if it has the potential, **under user control**, to display all its assigned information over time
- Potential Effectiveness: A visualization is potentially effective if over time it can present the information sufficiently clearly

1 – C. Beshers and S. Feiner, Auto Visual: Rule-Based Design of Interactive Multivariate Visualizations, IEEE Computer Graphics & Applications, 13(4): 41-49, 1993.

2 – H. Senay and E. Ignatius, A Knowledge-Based System for Visualization Design, IEEE Computer Graphics & Applications, 14(6): 36-47, 1994.

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