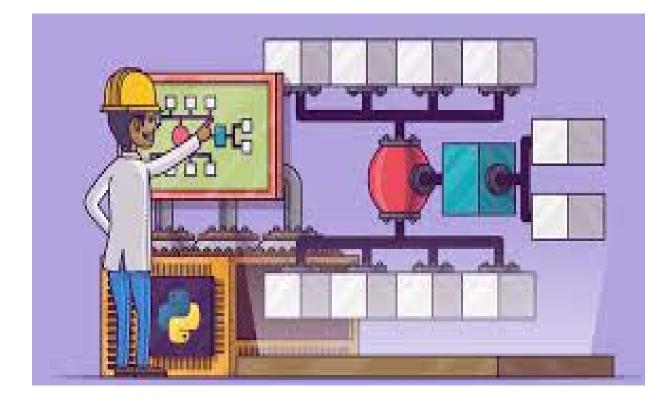


# ساختمان داده ها

مدرس: سمانه حسینی سمنانی

دانشگاه صنعتی اصفهان- دانشکده برق و کامپیوتر





### تابع FastTranspose

	row	col	value
mArray[0]	0	0	15
[1]	0	3	22
[2]	0	5	-15
[3]	1	1	11
[4]	1	2	3
[5]	2	3	-6
[6]	4	0	91
[7]	5	2	28
	(الغ)		



[0][1][2][3][4][5] rowsize = 2 1 2 2 0 1 rowstart = 0 2 3 5 7 7



### تابع FastTranspose

	row	col	value
mArray[0]	0	0	15
[1]	0	3	22
[2]	0	5	-15
[3]	1	1	11
[4]	1	2	3
[5]	2	3	-6
[6]	4	0	91
[7]	5	2	28
	(الف)		

[0][1][2][3][4][5] rowsize = 2 1 2 2 0 1 rowstart = 0 2 3 5 7 7

	row	col	value
smArray[0]	0	0	15
[1]	0	4	91
[2]	1	1	11
[3]	2	1	3
[4]	2	5	28
[5]	3	0	22
[6]	3	2	-6
[7]	5	0	-15
	(ب)		



### تابع FastTranspose

```
SparseMatrix SparseMatrix::FastTranspose()
      {// Return the transpose of *this in O(terms + cols) time.
         SparseMatrix b (cols, rows, terms);
         if (term > 0)
         {// nonzero matrix
             int *rowSize = new int/cols7;
             int *rowStart = new int/cols/;
             // compute rowSize[i] = number of terms in row i of b
             fill(rowSize, rowSize + cols, 0); // initialize
10
             for (i = 0; i < terms; i++) rowSize [smArray[i].col]++;
             // rowStart[i] = starting position of new i in b
11
12
             rowStart/07 = 0;
             for (i = 1; i < cols; i++) rowStart[i] = rowStart[i - 1] + rowSize[i - 1];
13
             for (i = 0 : i < terms : i++)
14
              \{// \text{ copy from *this to } b\}
15
                int j = rowStart[smArray[i].col];
16
                b.smArray[j].row = smArray[i].col;
17
                b.smArray[j].col = smArray[i].row;
18
                b.smArray[i].value = smArray[i].value;
19
                rowStart[smArray[i].col]++;
20
            } // end of for
21
22
            delete [7 rowSize;
            delete [] rowStart;
23
         } // end of if
24
25
         return b;
26
                                           سمانه حسيني سمناني
```



### تحلیل تابع FastTranspose

O(cols + terms)

• برای ماتریس غیر خلوت cols × rows

 $O(cols + terms) \xrightarrow{cols \ll cols \times rows} O(cols \times rows)$  زمان اجرا

• پیچیدگی مکانی FastTranspose بیشتر است.(rowSize , rowStart)





- ذخیره سازی در حافظه:
- در زبان ++3، رشته ها به صورت آرایه های کاراکتری که به کاراکتر تهی، 0،ختم می شوند نگهداری می گردد.

s[0] s[1] s[2] s[3]

d o g \0

char s[] = "dog";



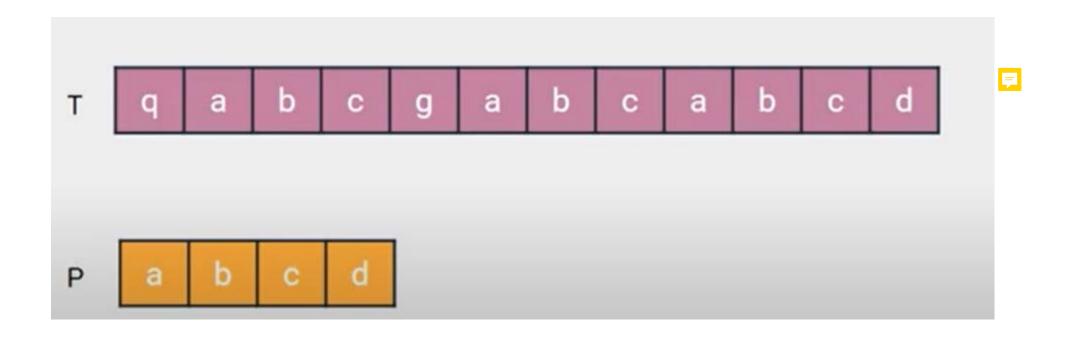
#### • اعمال:

- ایجاد یک رشته تهی جدید
- خواندن یا نوشتن یک رشته
- ضمیمه کردن دو رشته به یکدیگر (concatenation)
  - کپی کردن یک رشته
    - مقایسه رشته ها
  - درج کردن یک زیر رشته به داخل رشته
  - برداشتن یک زیر رشته از یک رشته مشخص
- پیدا کردن یک الگو( pattern )یا عبارت در یک رشته

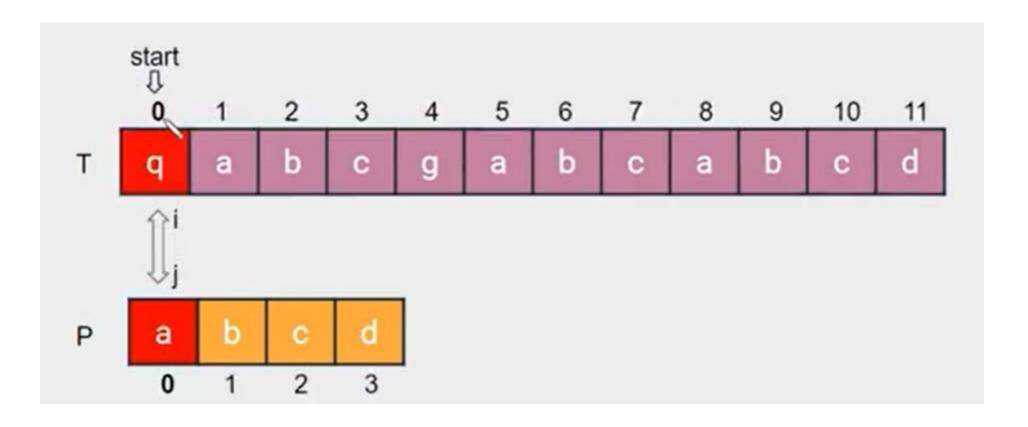


```
class String
public:
  String (char *init, int m);
 // Constructor that initializes *this to string init of length m.
 boll operator = = (string t);
 // If the string represented by *this equals t, return true;
 // else return false.
  bool operator!();
 // If *this is empty then return true; else return false.
 int Length();
 // Return the number of characters in *this.
  String Concat(Stringt);
  // Return a string whose elements are those of *this followed by those of t.
  String Substr(int i, int i);
  // Return a string containing the j characters of *this at positions i, i + 1, ...,
  //i + j - 1 if these are valid positions of *this; otherwise, throw an exception.
  int Find(String pat);
  // Return an index i such that pat matches the substring of *this that begins
  // at position i. Return -1 if pat is either empty or not a substring of *this
```

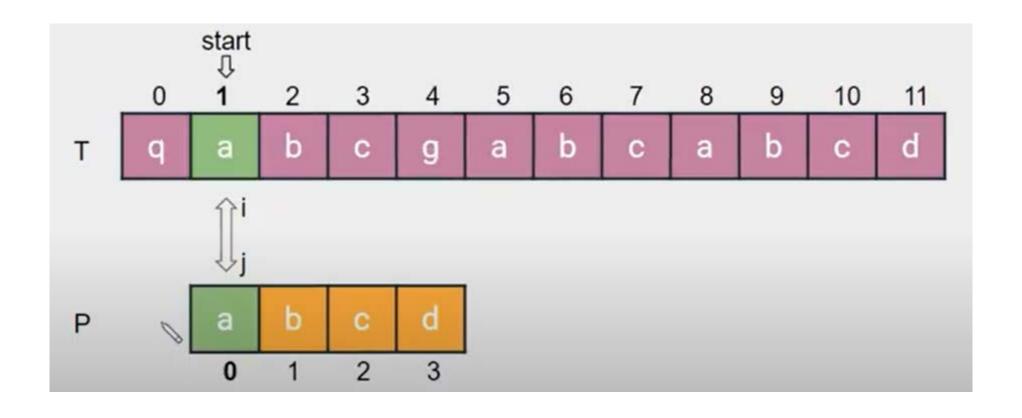




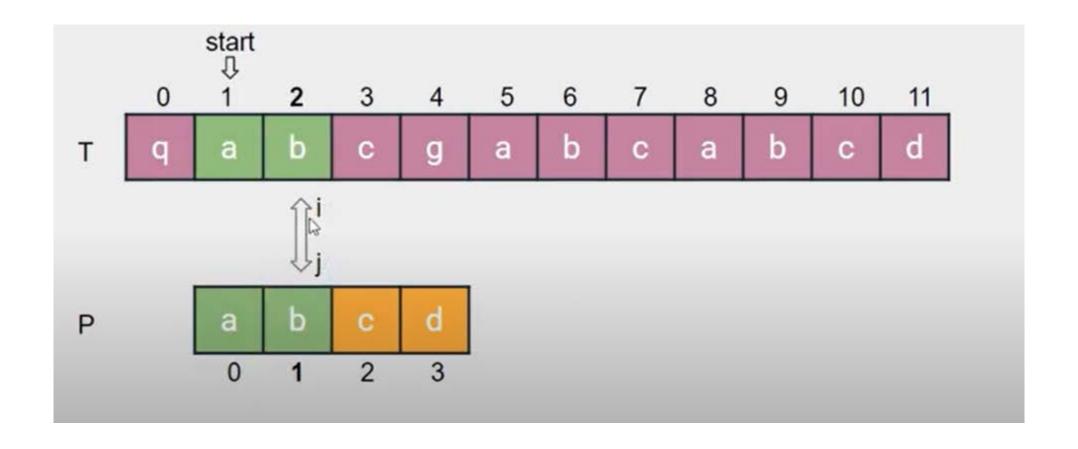




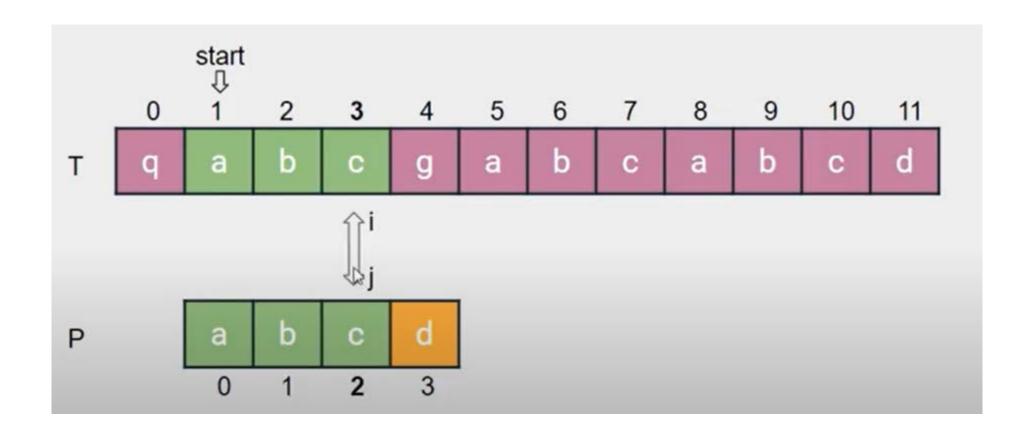




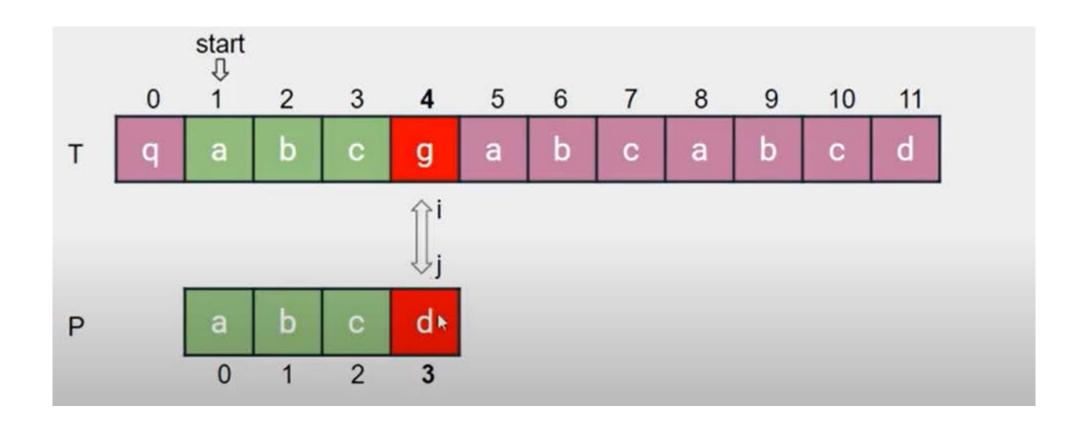




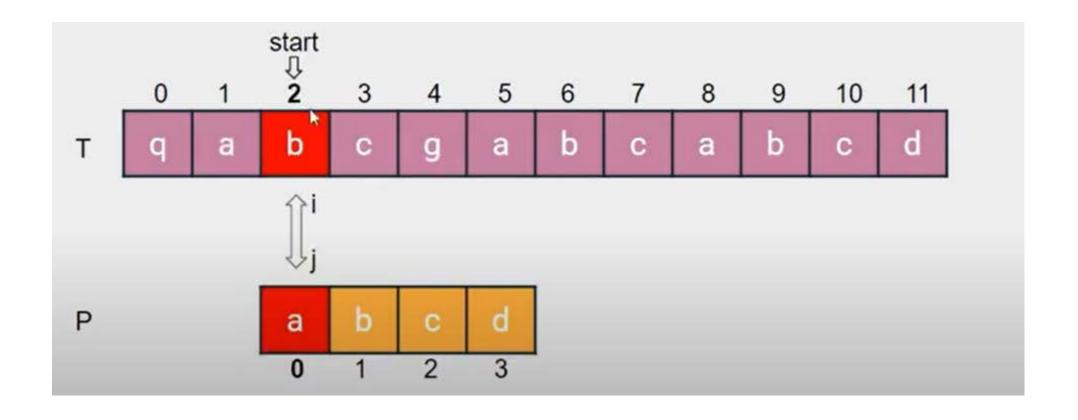




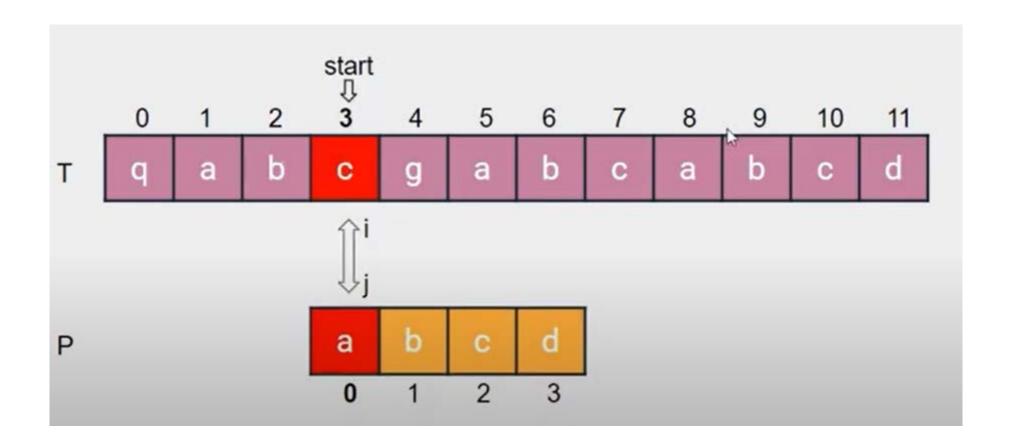




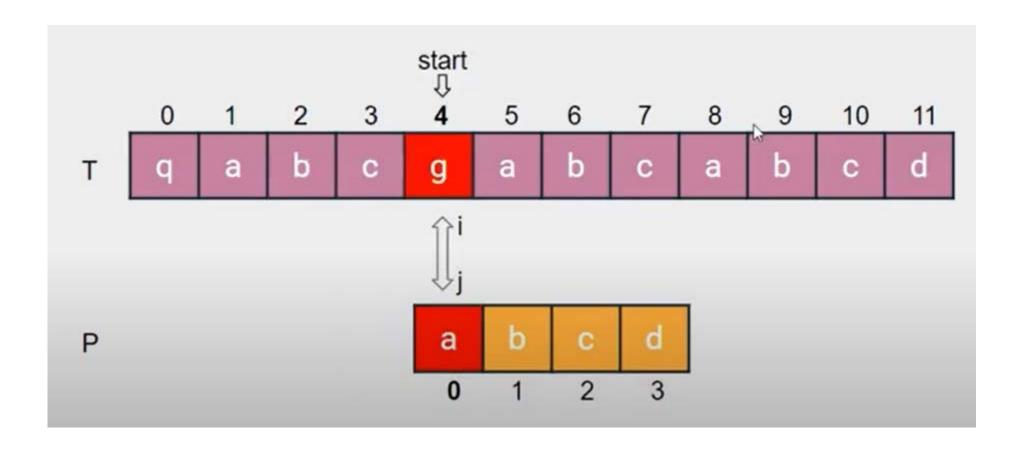




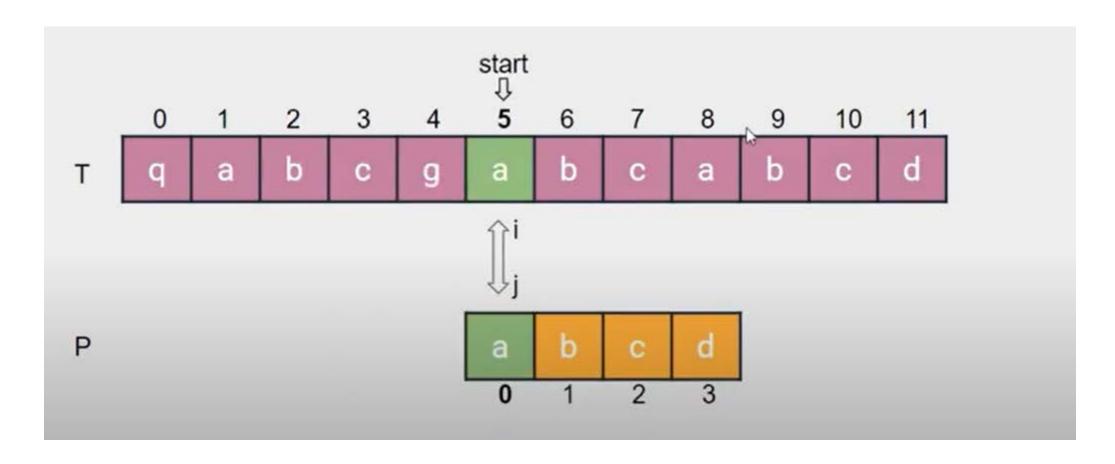




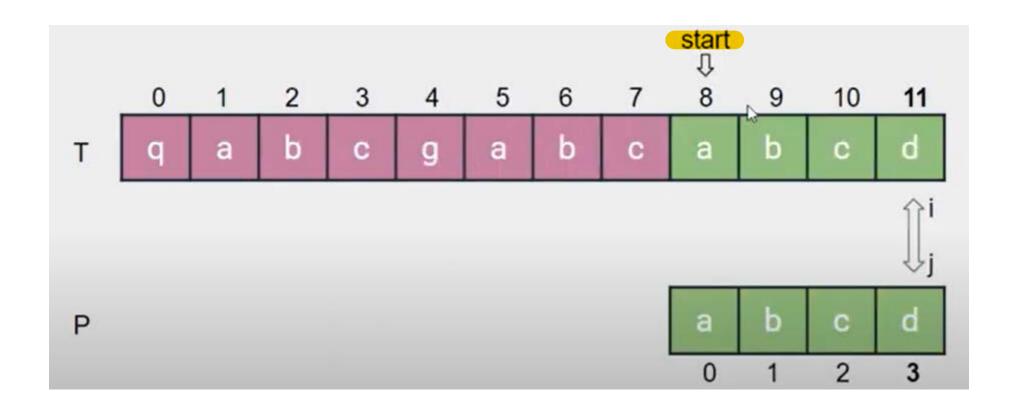




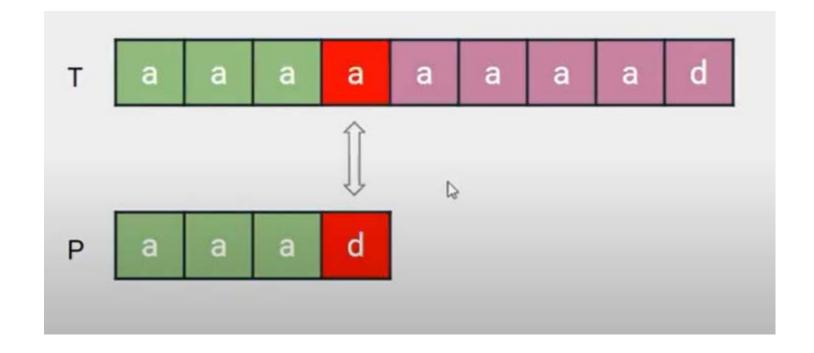




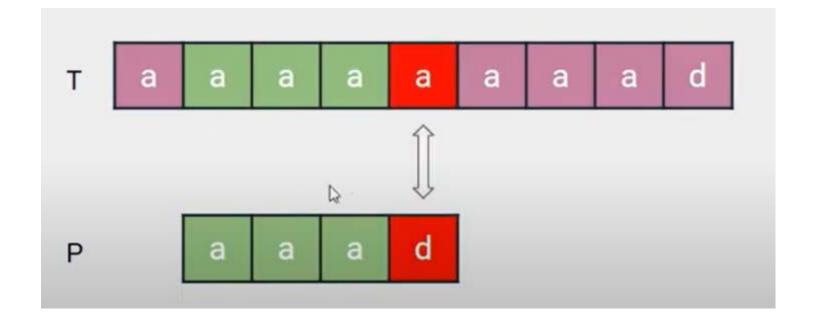




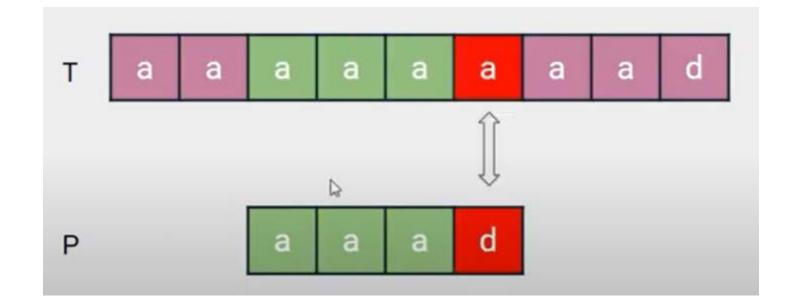




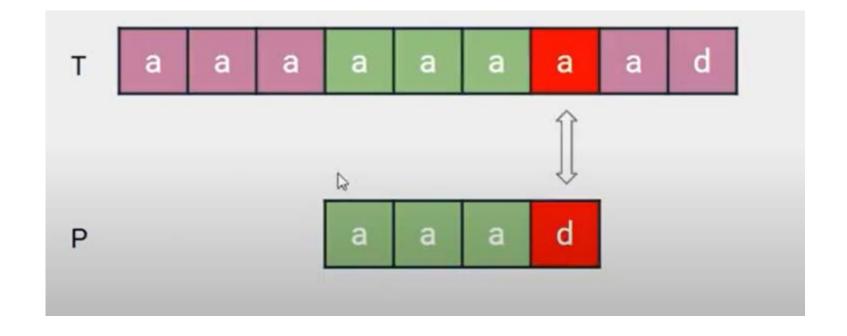




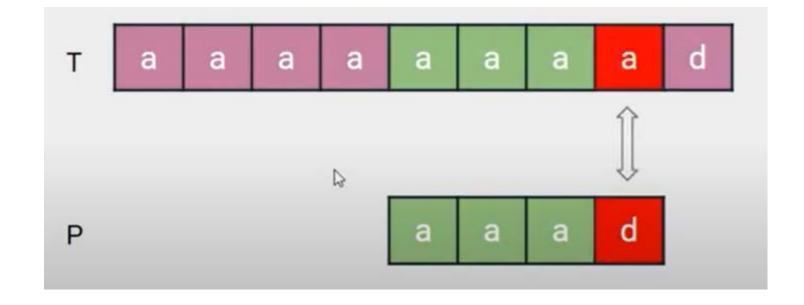




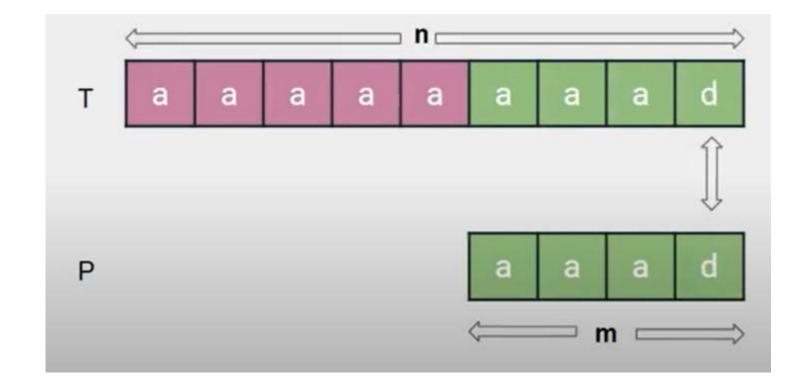






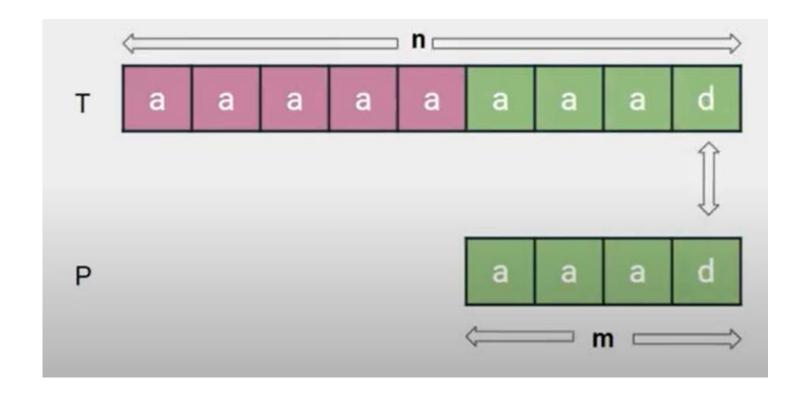






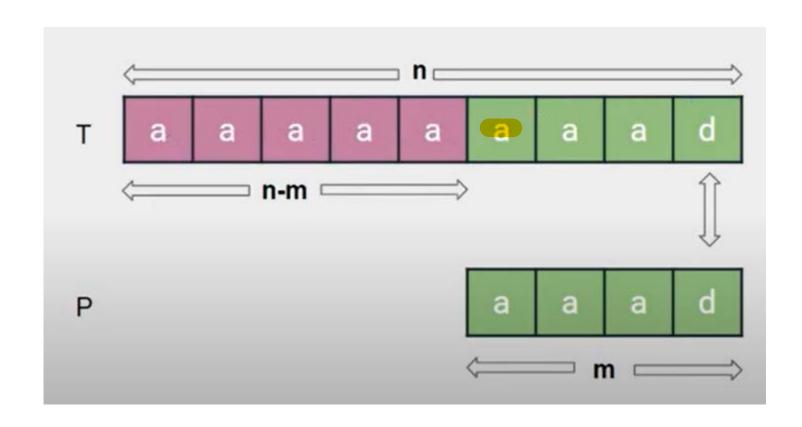


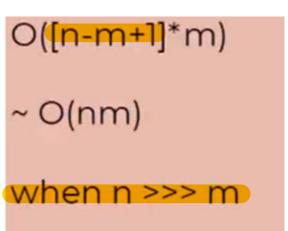
### تحليل پيچيدگي الگوريتم ساده





### تحليل پيچيدگي الگوريتم ساده







```
int String::Find(String pat)
{// Return -1 if pat does not occur in *this;
// otherwise return the first position in *this, where pat begind.
for (int start = 0; start <= Length0 - pat.Length0; start++)
{// check for match beginning at str [start]
    int j;
    for (j = 0; j < pat.length() && str [start + j] == pat.str[j]; j++)
    if (j == pat.length()) return start; // match found
    // no match at position start
}
return -1; // pat is empty or does not occur in s</pre>
```



### **KMP algorithm**

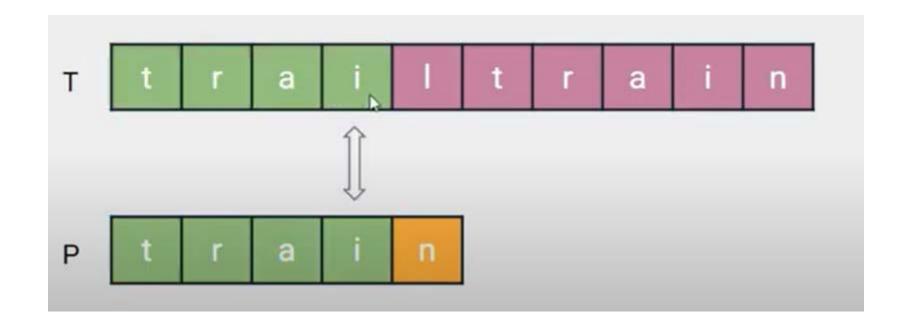




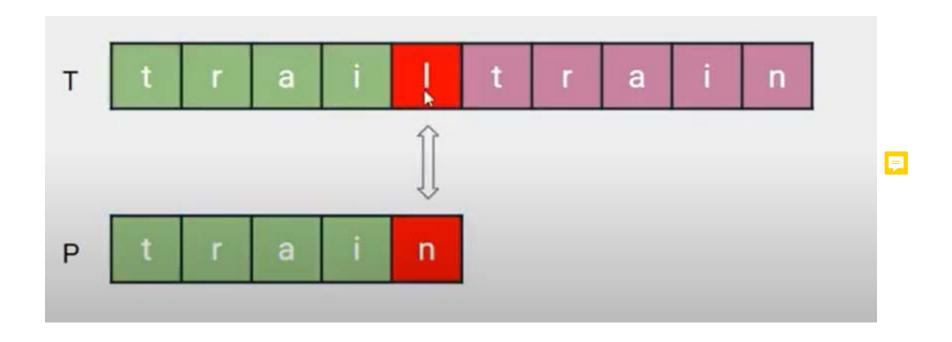
B

p t r a i n

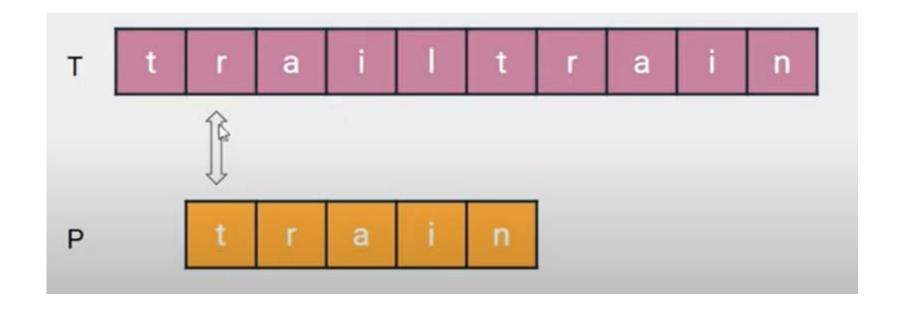




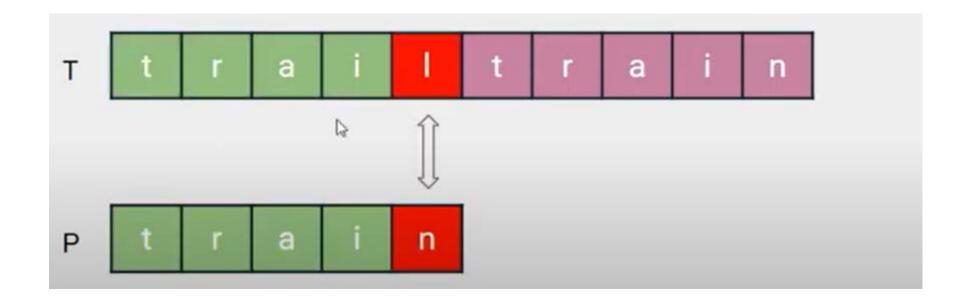




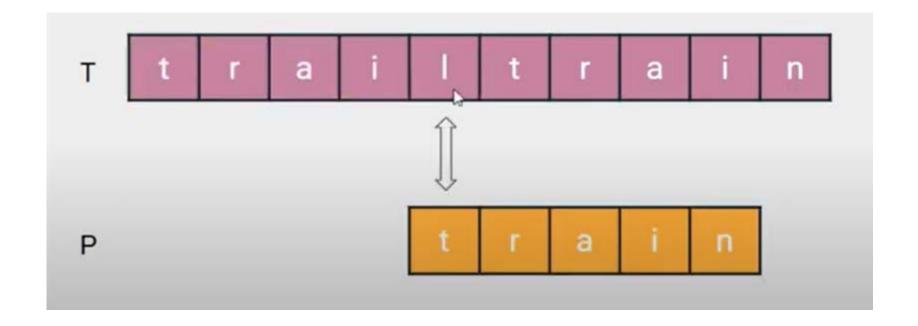




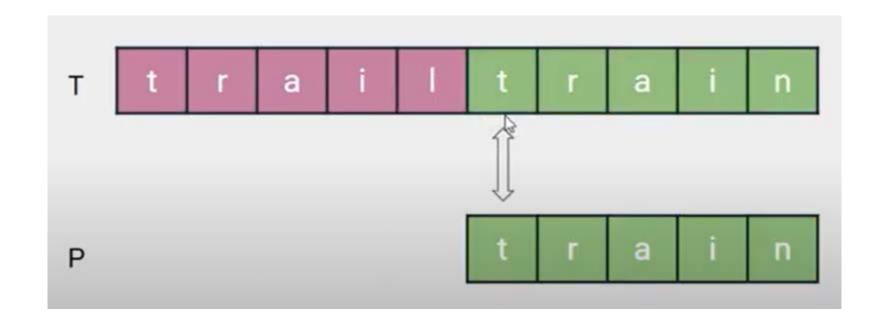




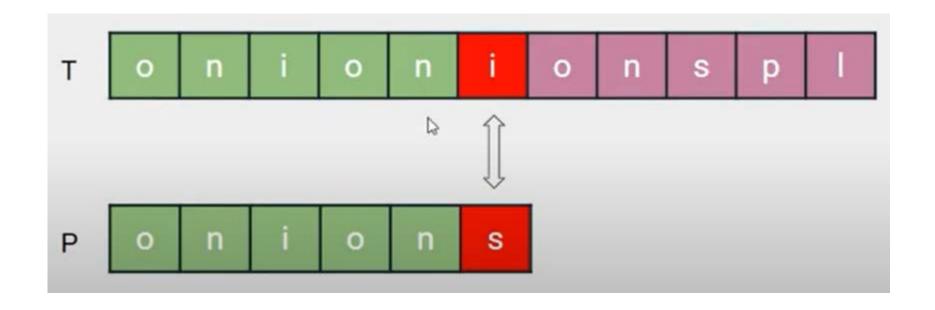




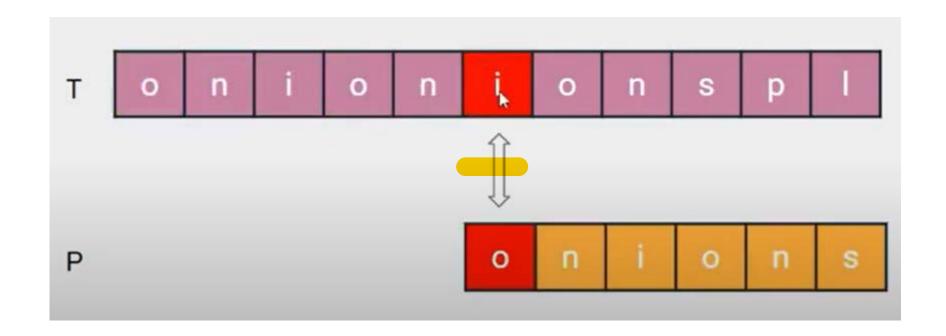




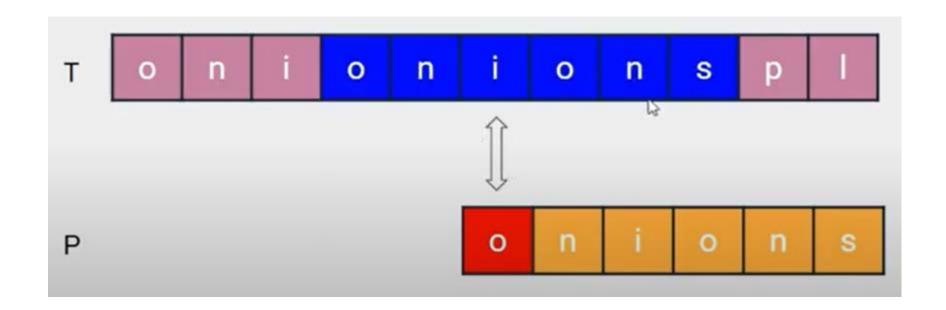




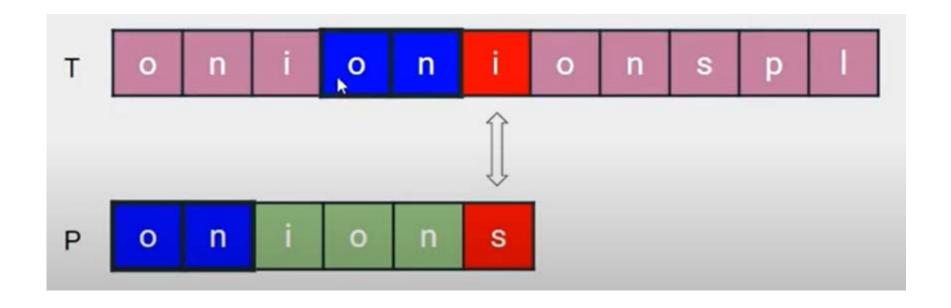




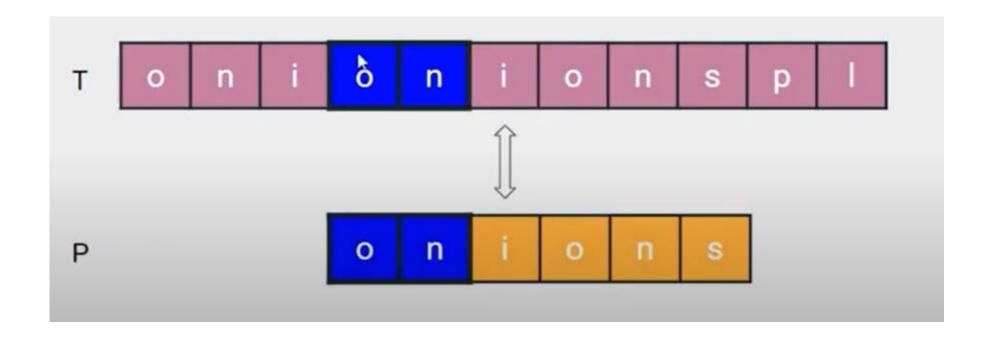




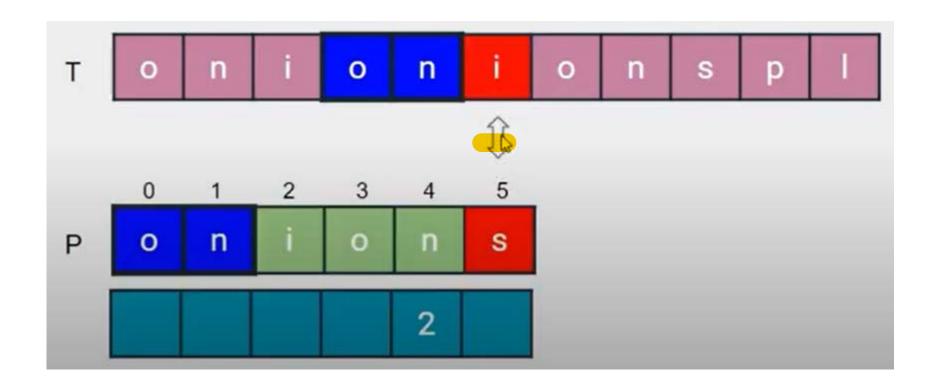




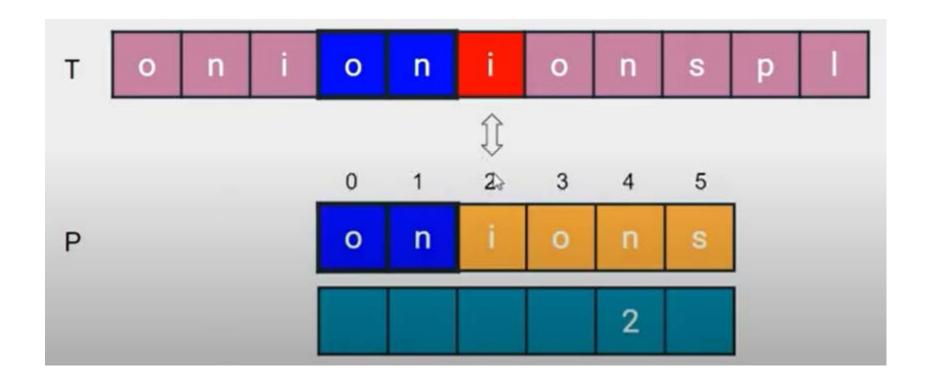




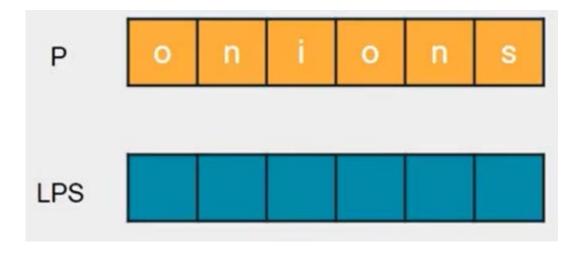




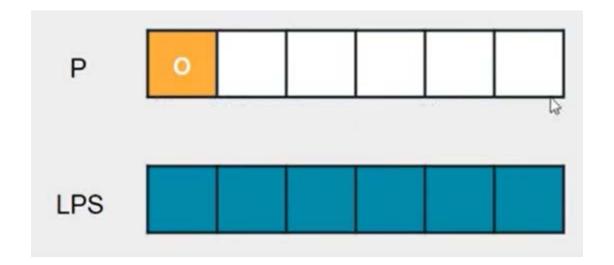




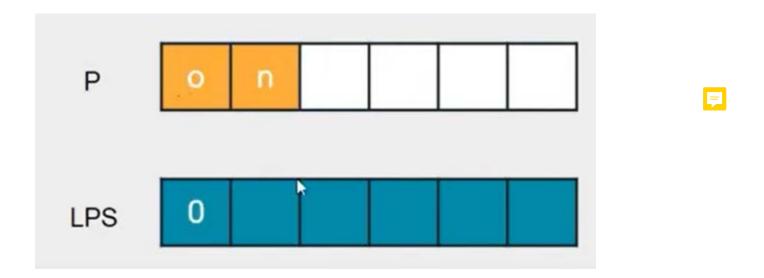




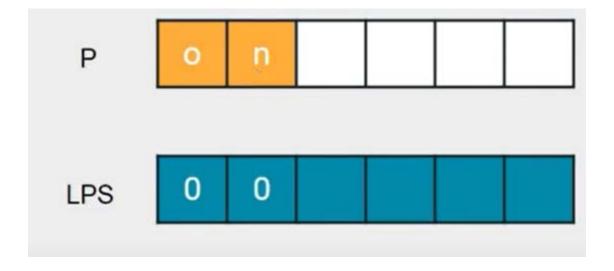




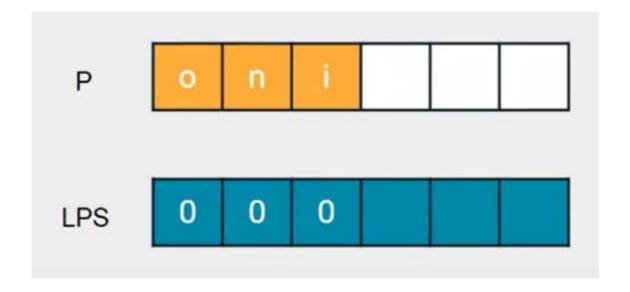




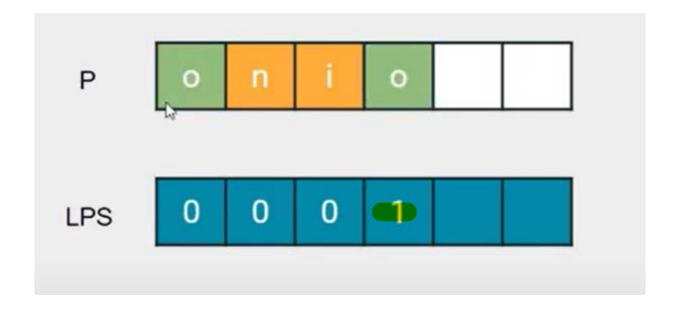




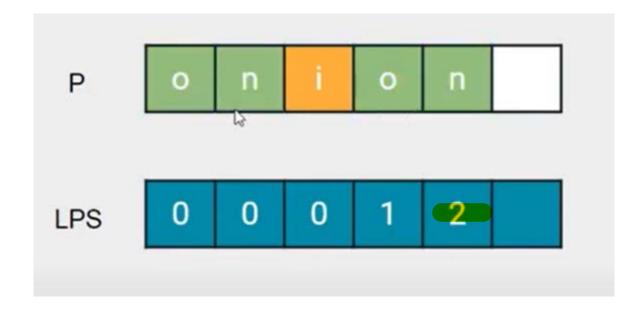




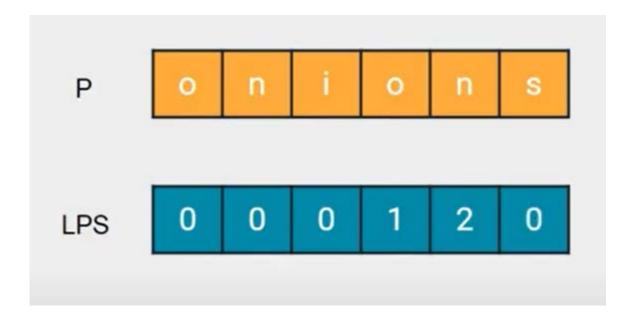






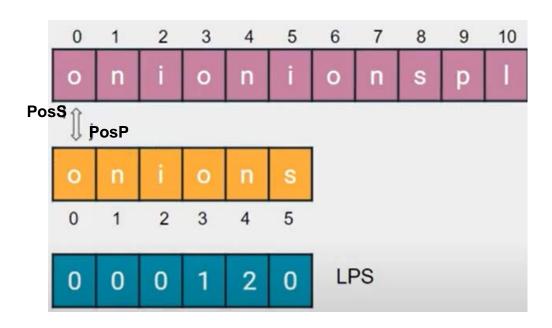






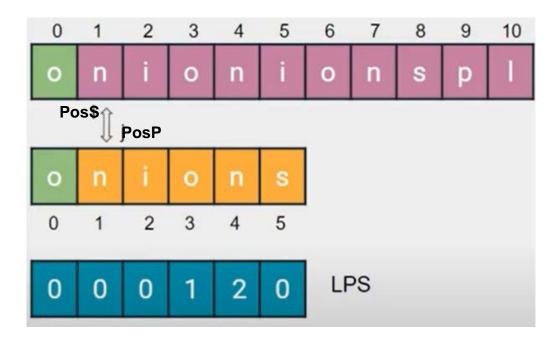


```
1 int string::FastFind (String pat)
2 {
3 //Determine if pat is a substring of s
  int PosP=0, PosS=0;
  int lengthP= pat.length(), lengthS= length();
  while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {
8
              PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
             else PosP = pat.f [ PosP -1 ] ;
12
   if (PosP<lengthP) return -1;
14 else return PosS- lengthp;
15 } // end of FastFind
```





```
1 int string::FastFind (String pat)
2 {
  //Determine if pat is a substring of s
   int PosP=0, PosS=0;
   int lengthP= pat.length(), lengthS= length();
   while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {
8
               PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
12
             else PosP = pat.f [ PosP -1 ];
    if ( PosP<lengthP) return -1;</pre>
14 else return PosS- lengthp;
15 } // end of FastFind
```





```
1 int string::FastFind (String pat)
2 {
3 //Determine if pat is a substring of s
   int PosP=0, PosS=0;
   int lengthP= pat.length(), lengthS= length();
   while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {
8
               PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
12
             else PosP = pat.f [ PosP -1 ] ;
    if ( PosP<lengthP) return -1;</pre>
14 else return PosS- lengthp;
15 } // end of FastFind
```

```
0 1 2 3 4 5 6 7 8 9 10

O n i O n i O n s p I

Pos$

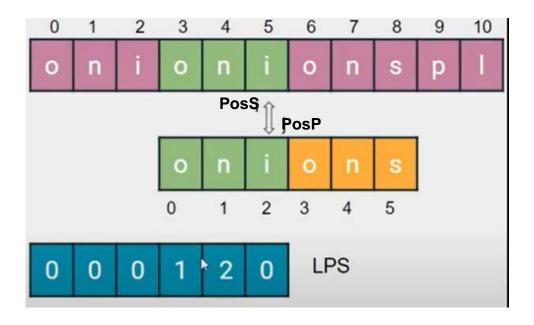
O n i O n s

O n 2 3 4 5

LPS
```

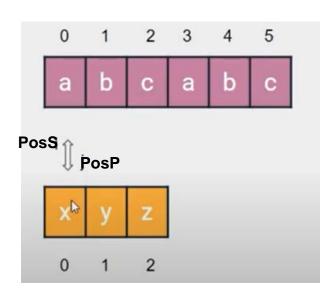


```
1 int string::FastFind (String pat)
2 {
  //Determine if pat is a substring of s
   int PosP=0, PosS=0;
   int lengthP= pat.length(), lengthS= length();
   while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {
8
               PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
12
             else PosP = pat.f [ PosP -1 ] ;
    if ( PosP<lengthP) return -1;</pre>
14 else return PosS- lengthp;
15 } // end of FastFind
```



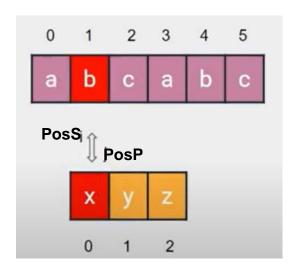


```
1 int string::FastFind (String pat)
2 {
  //Determine if pat is a substring of s
   int PosP=0, PosS=0;
   int lengthP= pat.length(), lengthS= length();
  while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {  //character match
8
              PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
12
             else PosP = pat.f [ PosP -1 ] ;
    if (PosP<lengthP) return -1;
14 else return PosS- lengthp;
15 } // end of FastFind
```



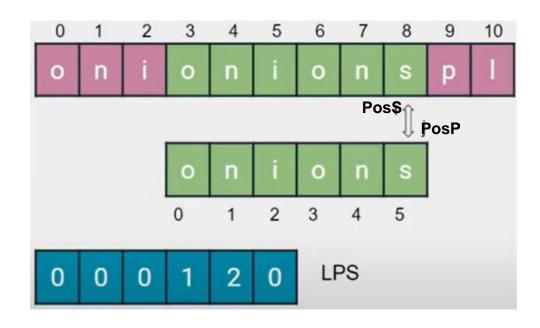


```
1 int string::FastFind (String pat)
2 {
3 //Determine if pat is a substring of s
  int PosP=0, PosS=0;
   int lengthP= pat.length(), lengthS= length();
  while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {  //character match
8
              PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
12
             else PosP = pat.f [ PosP -1 ] ;
    if (PosP<lengthP) return -1;
14 else return PosS- lengthp;
15 } // end of FastFind
```





```
1 int string::FastFind (String pat)
2 {
  //Determine if pat is a substring of s
   int PosP=0, PosS=0;
   int lengthP= pat.length(), lengthS= length();
   while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {
8
               PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
12
             else PosP = pat.f [ PosP -1 ] ;
    if ( PosP<lengthP) return -1;</pre>
14 else return PosS- lengthp;
15 } // end of FastFind
```



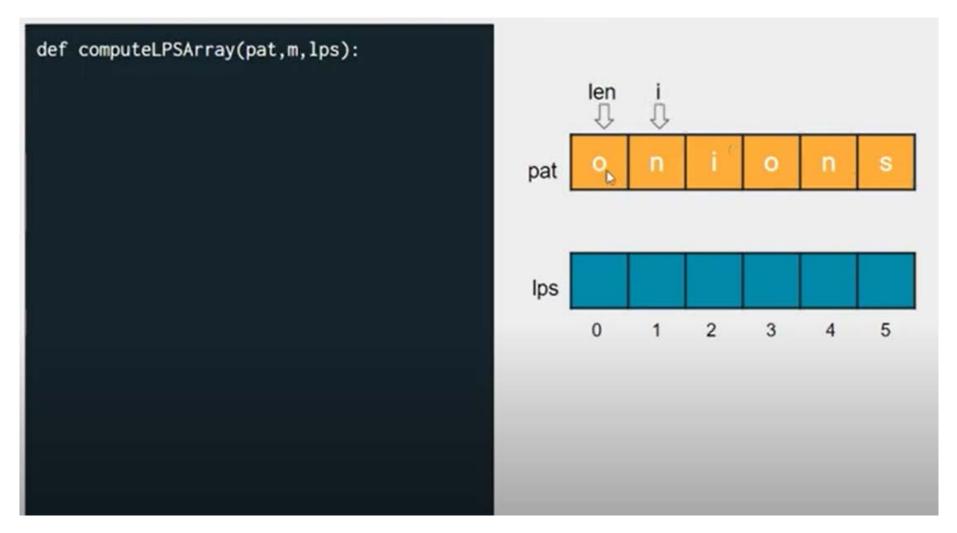


$$f(j) = egin{cases} \int & \sum_{i=1}^{k} k < j \end{cases}$$
 مقدار بزرگترین

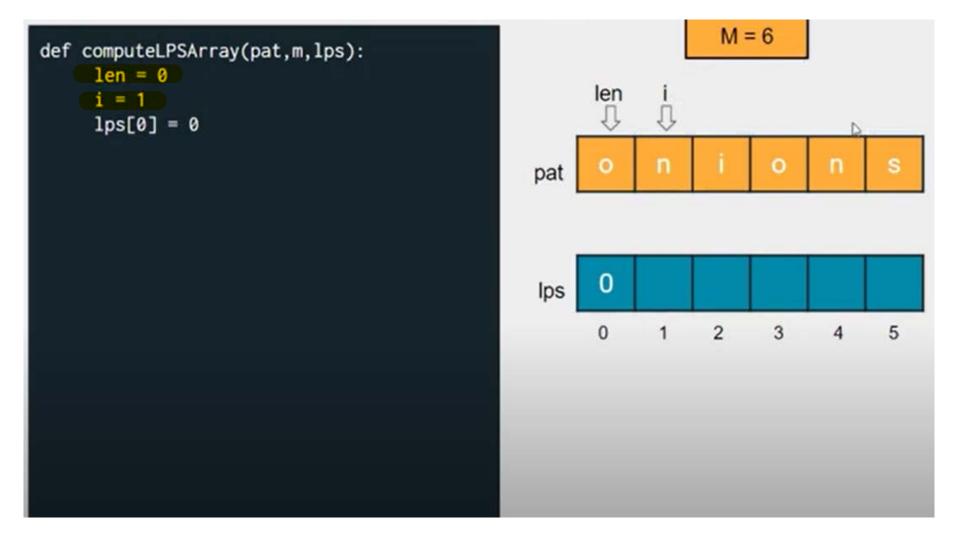
$$p_0 \cdots p_k = p_{j-k} \cdots p_j$$

در غیر این صورت





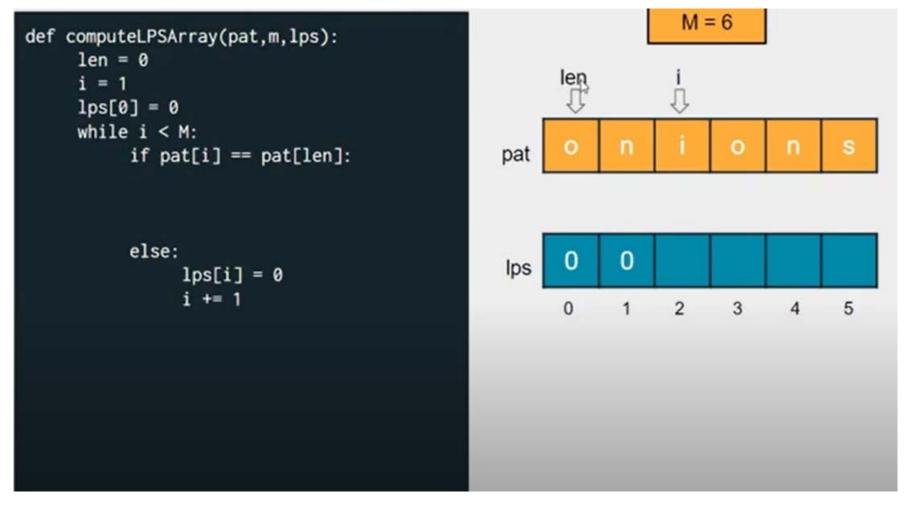




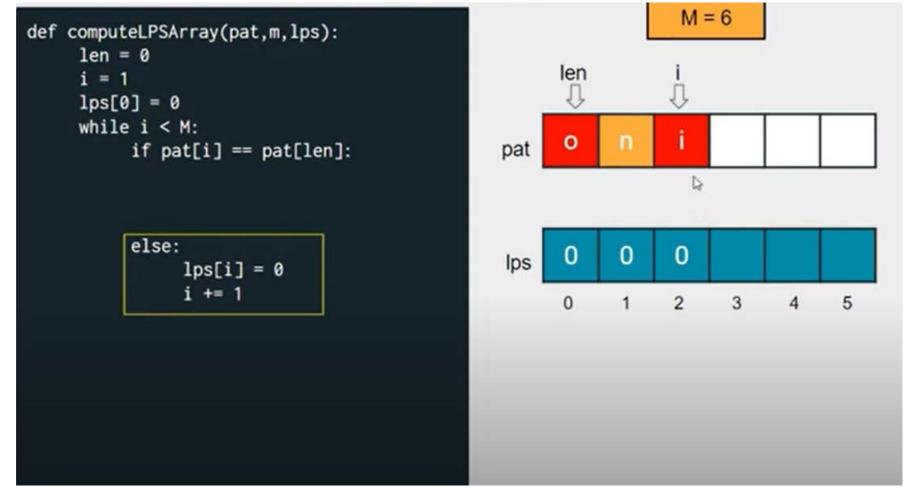


```
M = 6
def computeLPSArray(pat,m,lps):
     len = 0
                                                     len
     i = 1
     lps[0] = 0
     while i < M:
                                                      0
                                                           n
          if pat[i] == pat[len]:
                                                pat
          else:
                                                lps
                                                                 2
                                                      0
```

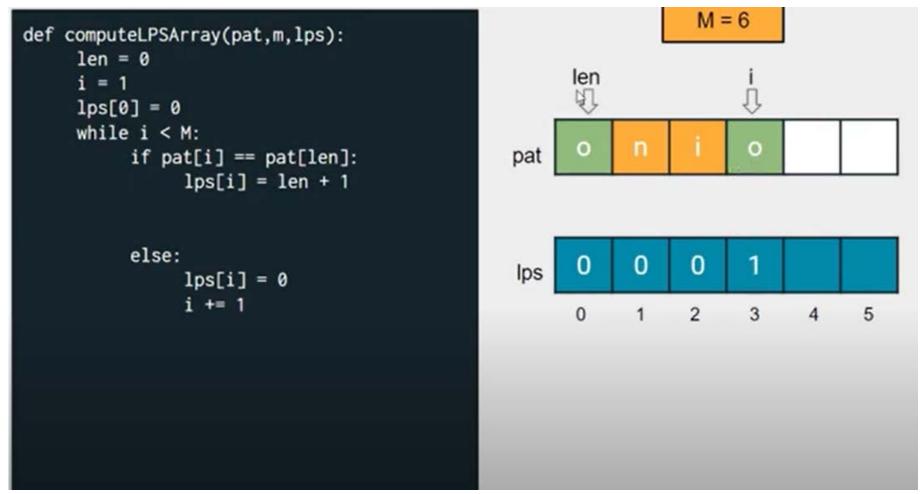








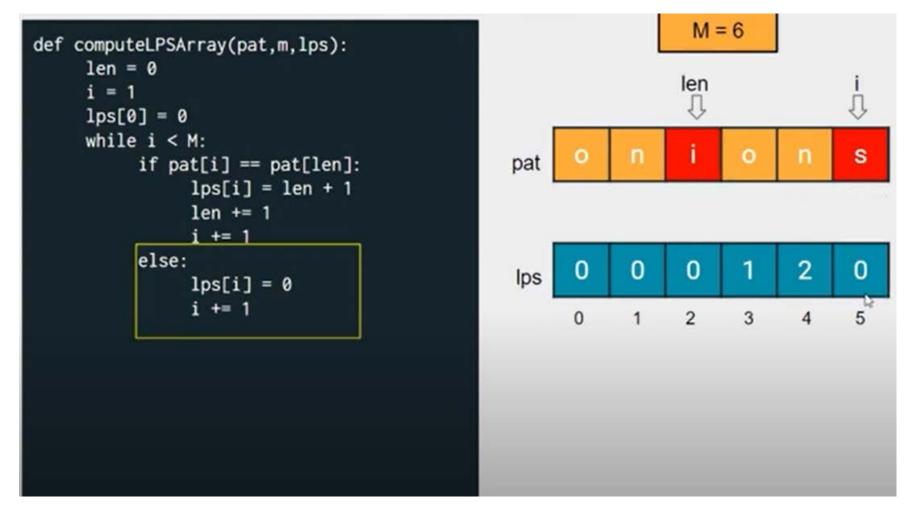






```
M = 6
def computeLPSArray(pat,m,lps):
     len = 0
                                                           len
     i = 1
     lps[0] = 0
     while i < M:
          if pat[i] == pat[len]:
                                                pat
               lps[i] = len + 1
               len += 1
               i += 1
          else:
                                                lps
               lps[i] = 0
               i += 1
                                                                       3
```

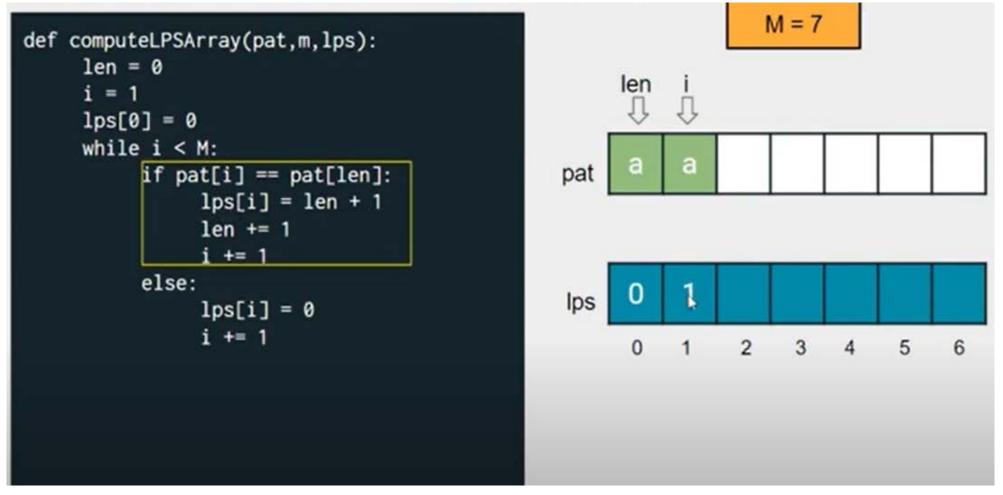




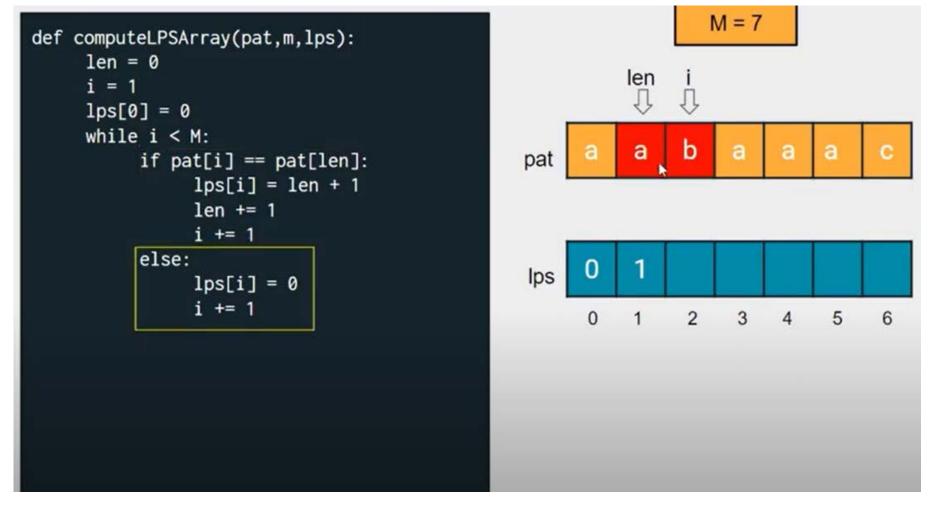


```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                   len i
     i = 1
    lps[0] = 0
     while i < M:
                                              pat
          if pat[i] == pat[len]:
               lps[i] = len + 1
               len += 1
               i += 1
         else:
                                              lps
               lps[i] = 0
               i += 1
                                                                  3 4 5
```

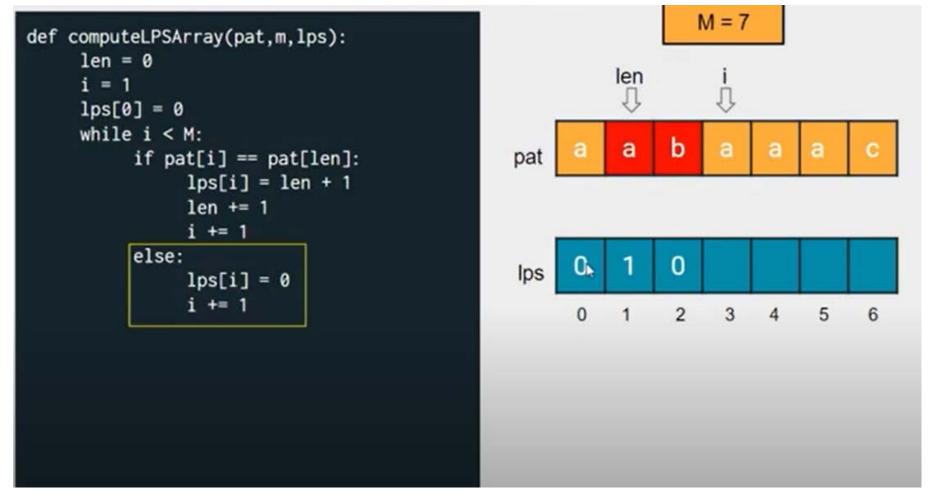




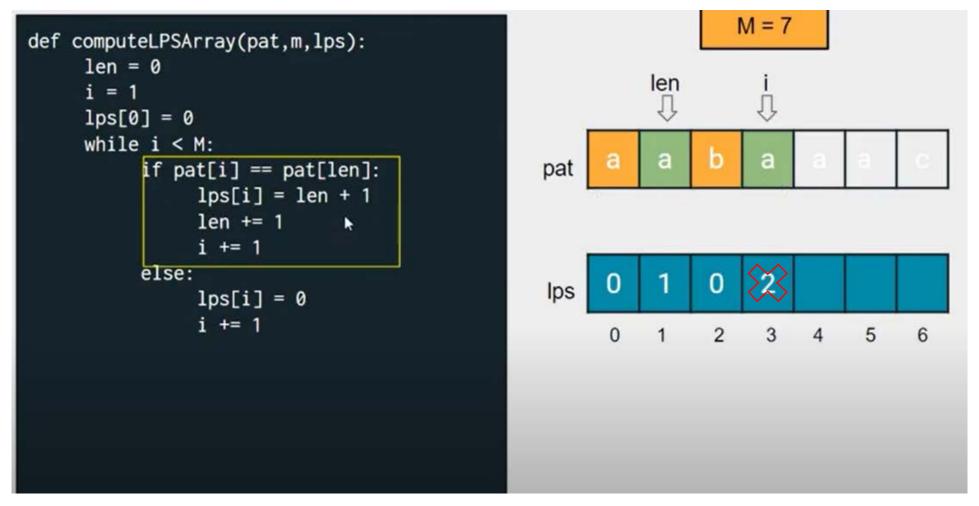




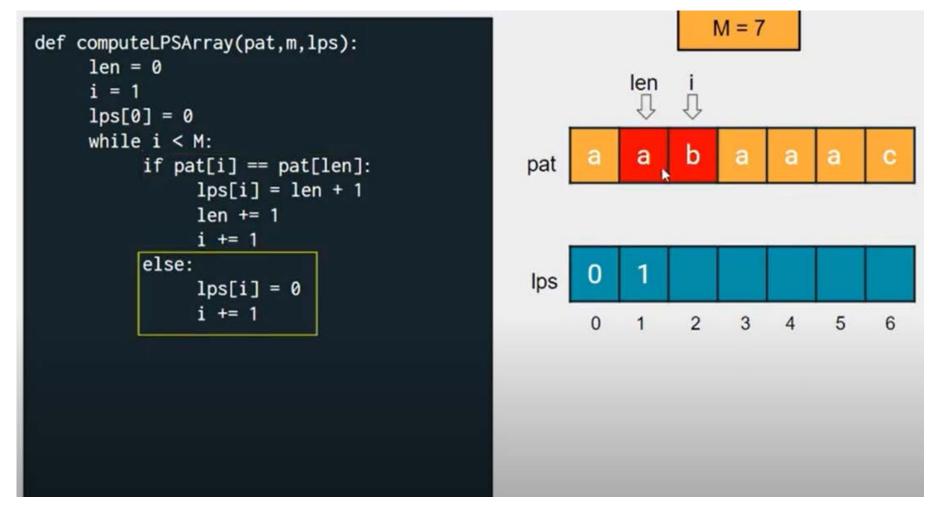












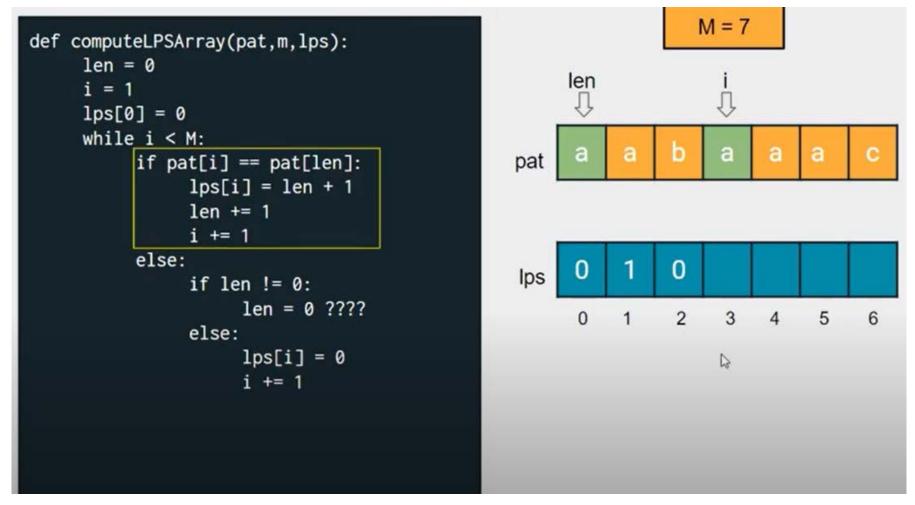


```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                         len
     i = 1
     lps[0] = 0
     while i < M:
          if pat[i] == pat[len]:
                                               pat
               lps[i] = len + 1
               len += 1
               i += 1
          else:
                                                lps
               if len != 0:
                                                                   3
                                                                        4
                                                                            5
                                                                                 6
               else:
                    lps[i] = 0
                    i += 1
```



```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                     len
     i = 1
     lps[0] = 0
     while i < M:
          if pat[i] == pat[len]:
                                                pat
               lps[i] = len + 1
               len += 1
               i += 1
          else:
               if len != 0:
                    len = 0 ????
               else:
                    lps[i] = 0
                    i += 1
```

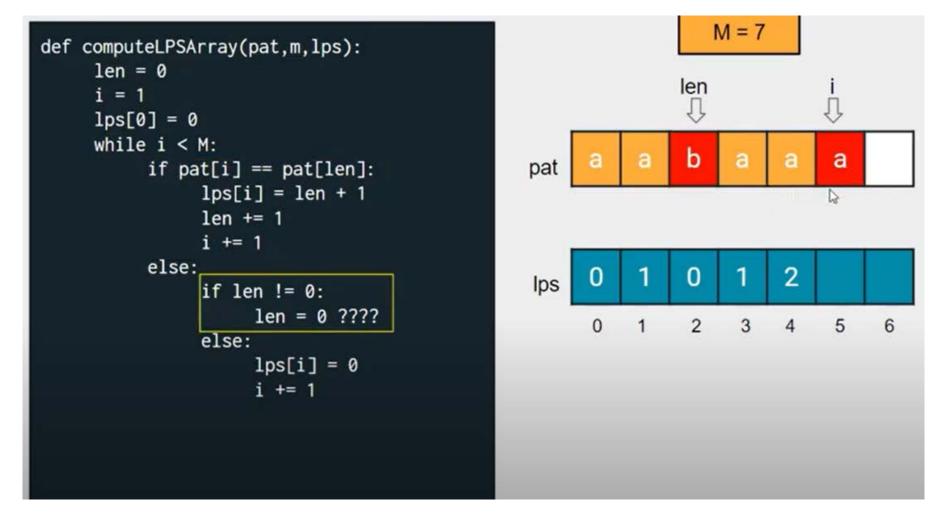




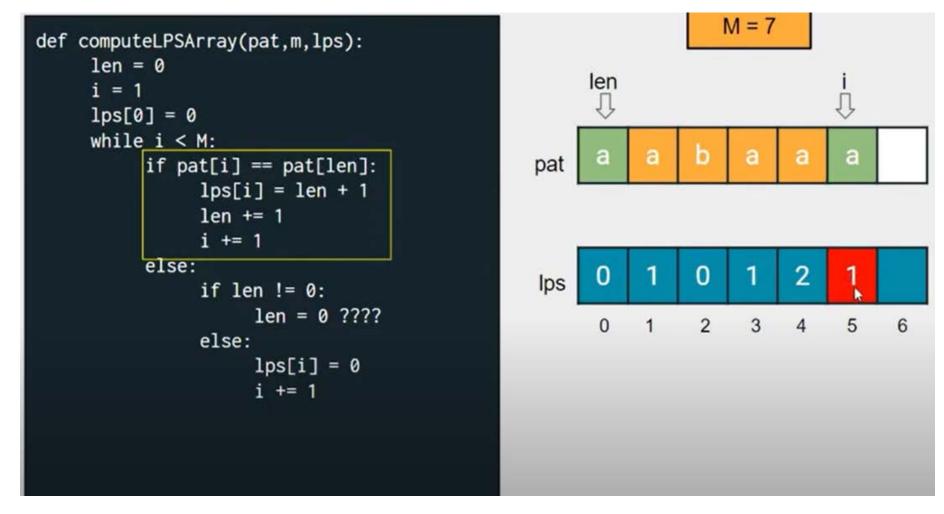


```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                          len
     i = 1
     lps[0] = 0
     while i < M:
                                                pat
          if pat[i] == pat[len]:
               lps[i] = len + 1
               len += 1
               i += 1
          else:
                                                lps
               if len != 0:
                    len = 0 ????
                                                                2
                                                                    3
                                                                             5
                                                                                  6
               else:
                    lps[i] = 0
                    i += 1
```

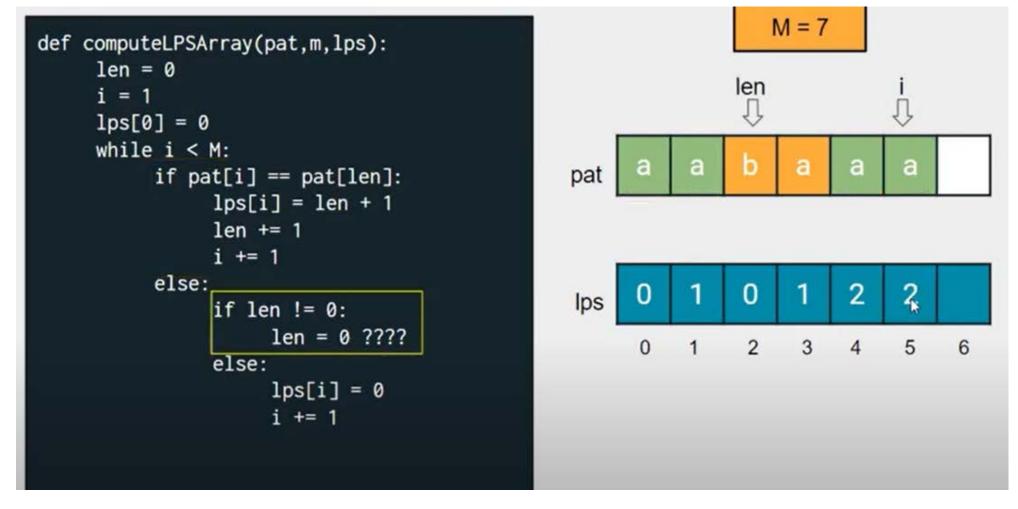




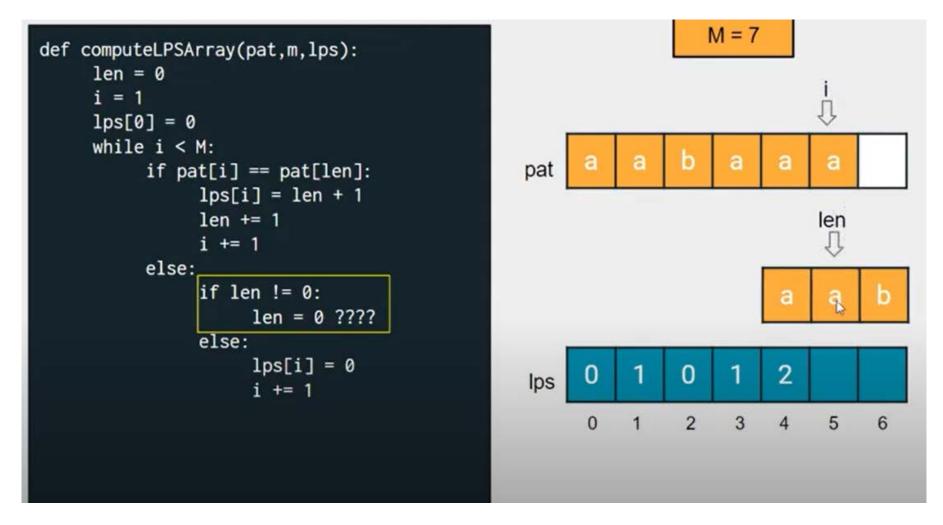














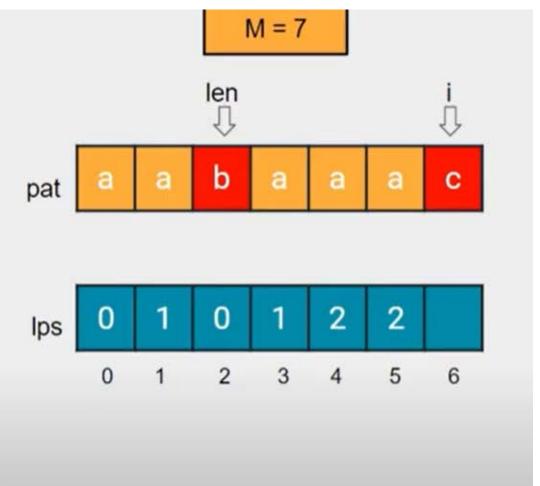
```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                         len
     i = 1
     lps[0] = 0
     while i < M:
          if pat[i] == pat[len]:
                                               pat
               lps[i] = len + 1
               len += 1
               i += 1
          else:
                                               lps
               if len != 0:
                    len = lps[len-1]
                                                               2
                                                                   3
               else:
                    lps[i] = 0
                    i += 1
```



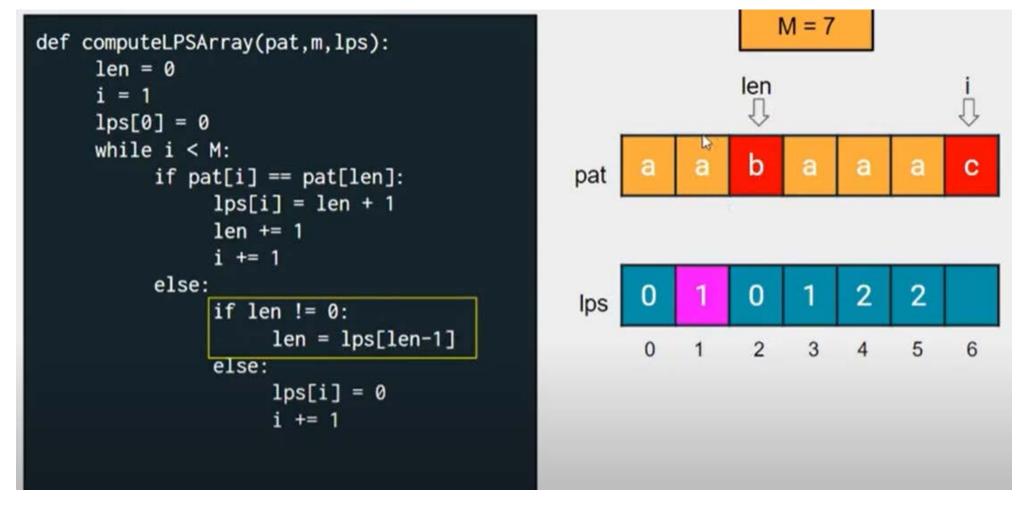
```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                               len
     i = 1
     lps[0] = 0
     while i < M:
                                                pat
          if pat[i] == pat[len]:
               lps[i] = len + 1
               len += 1
               i += 1
          else:
                                                lps
               if len != 0:
                     len = lps[len-1]
               else:
                    lps[i] = 0
                    i += 1
```



```
def computeLPSArray(pat,m,lps):
     len = 0
     i = 1
     lps[0] = 0
     while i < M:
          if pat[i] == pat[len]:
                                                pat
               lps[i] = len + 1
               len += 1
               i += 1
          else:
                                                 lps
               if len != 0:
                     len = lps[len-1]
               else:
                     lps[i] = 0
                     i += 1
```





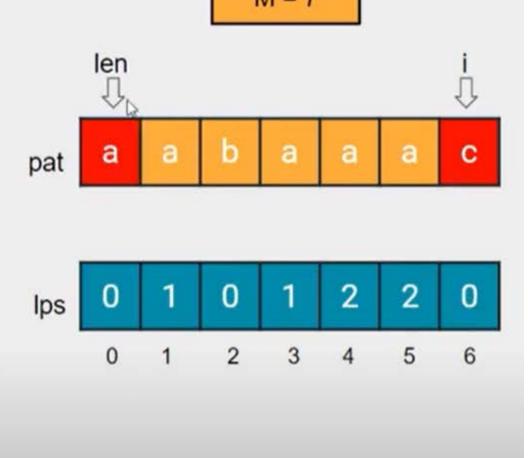




```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                          len
     i = 1
     lps[0] = 0
     while i < M:
          if pat[i] == pat[len]:
                                                pat
               lps[i] = len + 1
               len += 1
               i += 1
          else:
                                                lps
               if len != 0:
                     len = lps[len-1]
                                                                    3 4
                                                                              5
               else:
                     lps[i] = 0
                     i += 1
```



```
M = 7
def computeLPSArray(pat,m,lps):
     len = 0
                                                      len
     i = 1
     lps[0] = 0
     while i < M:
          if pat[i] == pat[len]:
                                                 pat
               lps[i] = len + 1
                len += 1
                i += 1
          else:
                                                 lps
                if len != 0:
                     len = lps[len-1]
                                                                      3
                else:
                     lps[i] = 0
                     i += 1
```



```
1 int string::FastFind (String pat)
                                                               O(length5)

اگر تابع شکست محاسبه شده باشد
2 {
  //Determine if pat is a substring of s
   int PosP=0, PosS=0;
   int lengthP= pat.length(), lengthS= length();
   while ((PosP< lengthP) && (PosS < lengthS))
        if (pat.str [PosP] == str [PosS] ) {    //character match
8
               PosP++; PosS++;
9
10
        else
11
             if (PosP == 0) PosS++;
12
             else PosP = pat.f [ PosP -1 ];
    if (PosP<lengthP) return -1;
14 else return PosS- lengthp;
15 } // end of FastFind
```



#### تحلیل پیچیدگی تابع شکست

```
def computeLPSArray(pat,m,lps):
     len = 0
                                                   → O( length )
     i = 1
     lps[0] = 0
     while i < M:
           if pat[i] == pat[len]:
                lps[i] = len + 1
                len += 1
                i += 1
          else:
                if len != 0:
                     len = lps[len-1]
                else:
                     lps[i] = 0
                     i += 1
```

# تحليل پيچيدگي الگوريتم كنوث-موريس-پرات KMP

```
1 int string::FastFind (String pat)
2 {
                                                                  O(lengthS + LengthP)
  //Determine if pat is a substring of s
4 int PosP=0, PosS=0;
  int lengthP= pat.length(), lengthS= length();
  while ((PosP< lengthP) && (PosS < lengthS))
                                                                  If lengthS \gg LengthP:
        if (pat.str [PosP] == str [PosS]) { //character match
                                                                  O(length5)
8
              PosP++; PosS++;
9
10
        else
             if (PosP == 0) PosS++;
11
12
             else PosP = pat.f [ PosP -1 ];
   if (PosP<lengthP) return -1;
14 else return PosS- lengthp;
15 } // end of FastFind
```