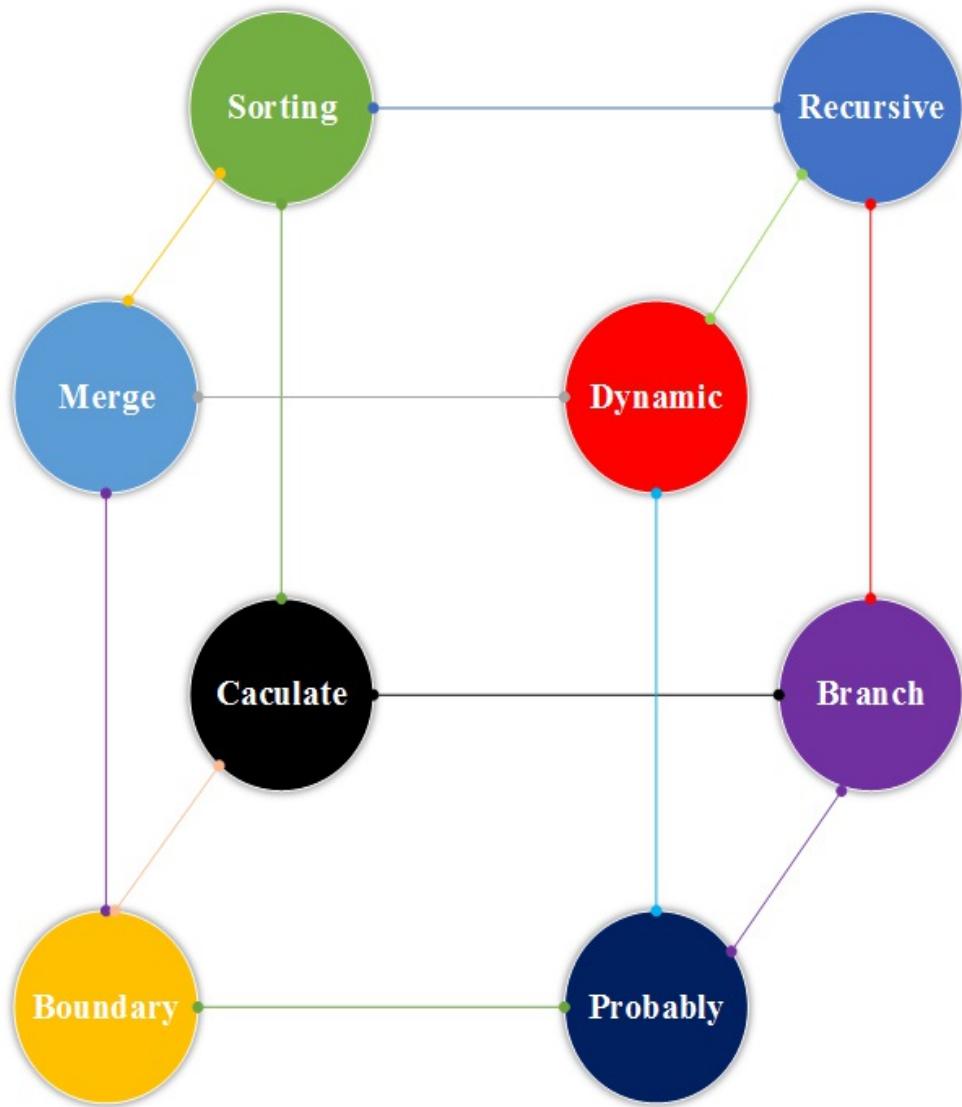
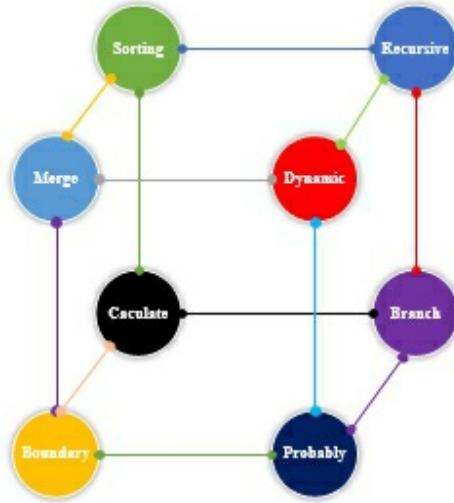


# Algorithms JavaScript



Algorithms Explain With Beautiful Pictures

# Algorithms JavaScript



YANG HU

Simple is the beginning of wisdom. the essence of practice, to briefly explain the concept, and vividly cultivate programming interest, this book deeply analyzes Data Structures Algorithms Javascript and fun of programming.

<http://en.verejava.com>

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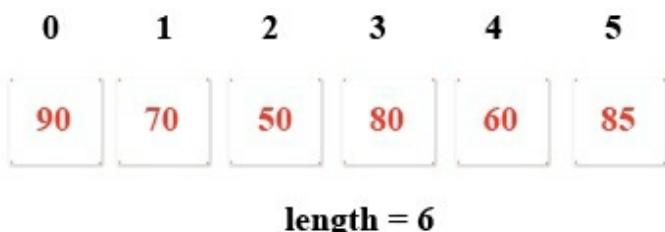
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# Linear Table Definition

## Linear Table:

Sequence of elements, is a one-dimensional array.

### 1. Define a one-dimensional array of student scores

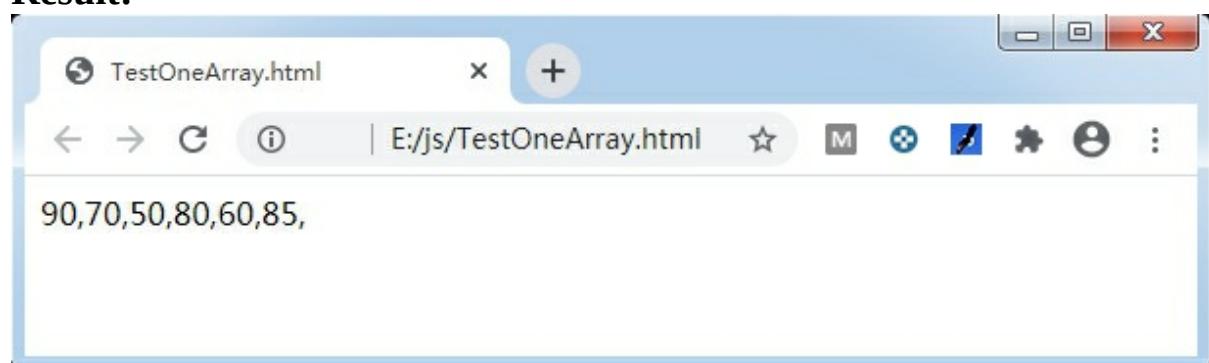


### 1. Create a **TestOneArray.html** with **Notepad** and open it in your browser.

```
<script type="text/javascript">
    var scores = new Array( 90, 70, 50, 80, 60, 85 );

    //print out the score of the array scores
    for (var i = 0; i < scores.length; i++) {
        document.write(scores[i] + ",");
    }
</script>
```

## Result:



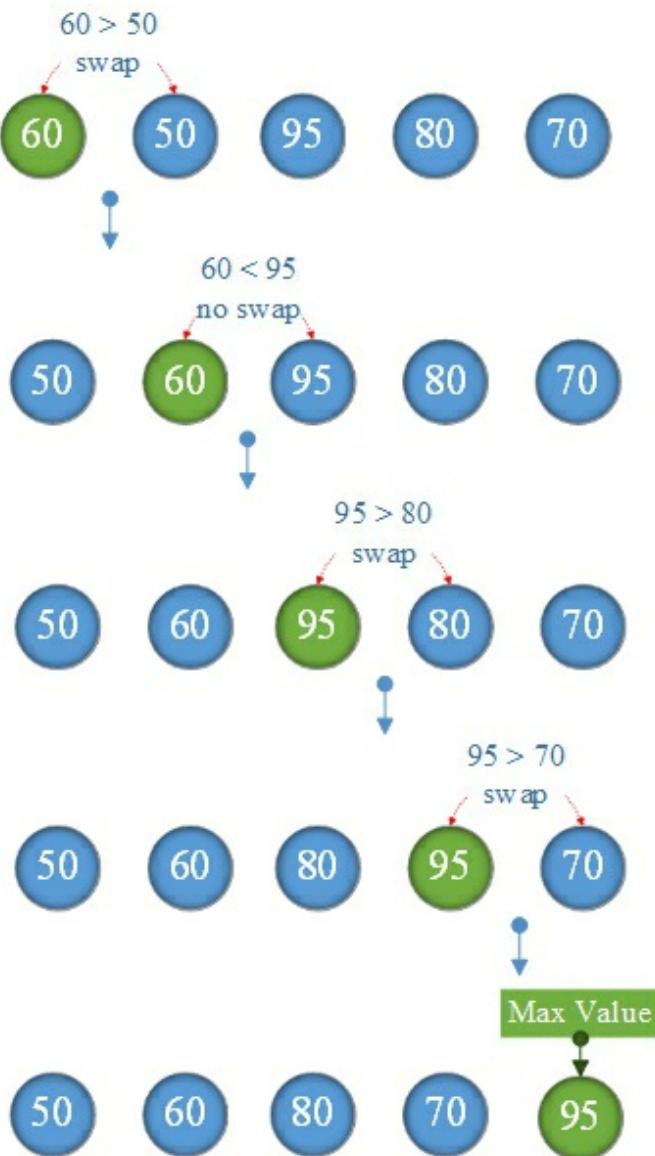
# Maximum Value

## Maximum of Integer Sequences:



### 1. Algorithmic ideas

Compare `arrays[i]` with `arrays[i + 1]`, if `arrays[i] > arrays[i + 1]` are exchanged. So continue until the last number, `arrays[length - 1]` is the maximum.



**1. Create a `Test.MaxValue.html` with **NotePad** and open it in your browser.**

```
<script type="text/javascript">
function max(arrays) {
    // Maximum initialization value is 0
    for (var i = 0; i < arrays.length - 1; i++) {
        if (arrays[i] > arrays[i + 1]) { // swap
            var temp = arrays[i];
            arrays[i] = arrays[i + 1];
            arrays[i + 1] = temp;
        }
    }
    var maxValue = arrays[arrays.length - 1];
    return maxValue;
}

//////////////////testing////////////////

var scores = [ 60, 50, 95, 80, 70];
var maxValue = max(scores);
document.write("maxValue = " + maxValue);

</script>
```

**Result:**



# Bubble Sorting Algorithm

## Bubble Sorting Algorithm:

Compare `arrays[j]` with `arrays[j + 1]`, if `arrays[j] > arrays[j + 1]` are exchanged.

Remaining elements repeat this process, until sorting is completed.

**Sort the following numbers from small to large**



## Explanation:



No sorting,

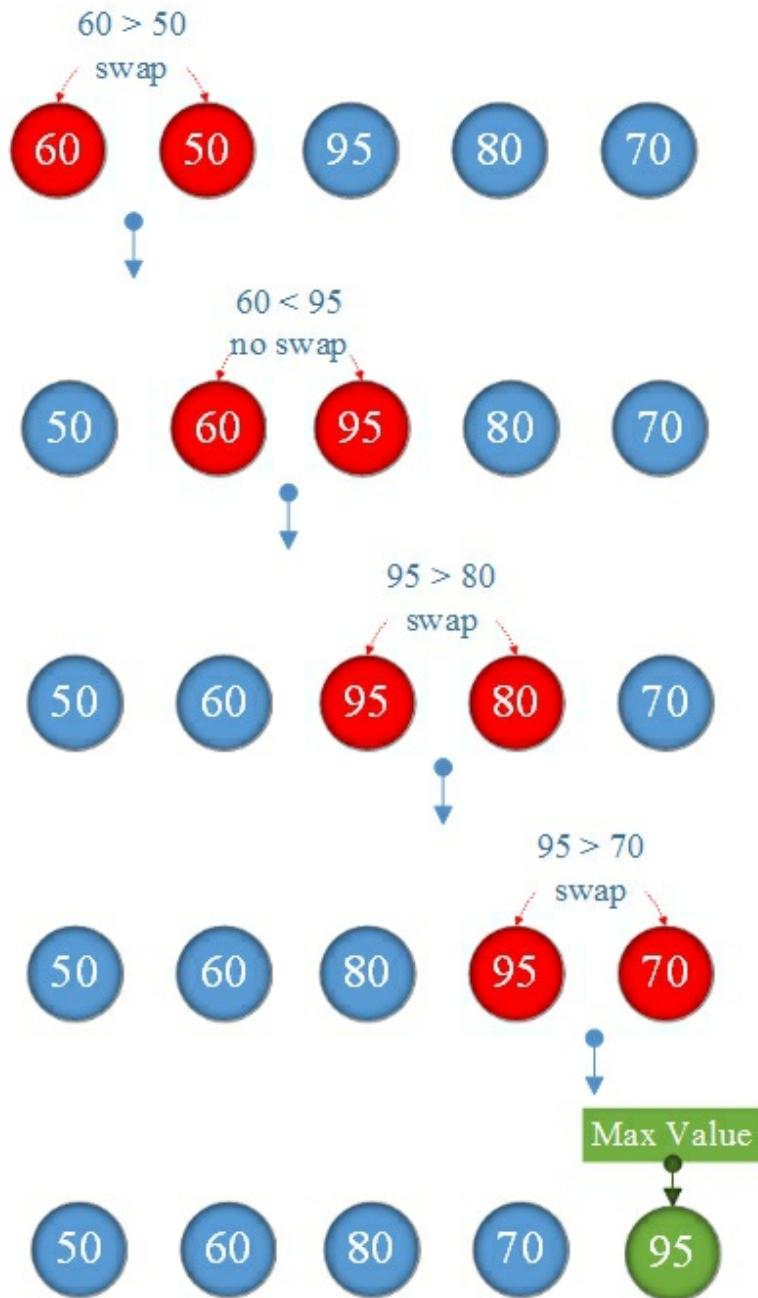


Comparing,

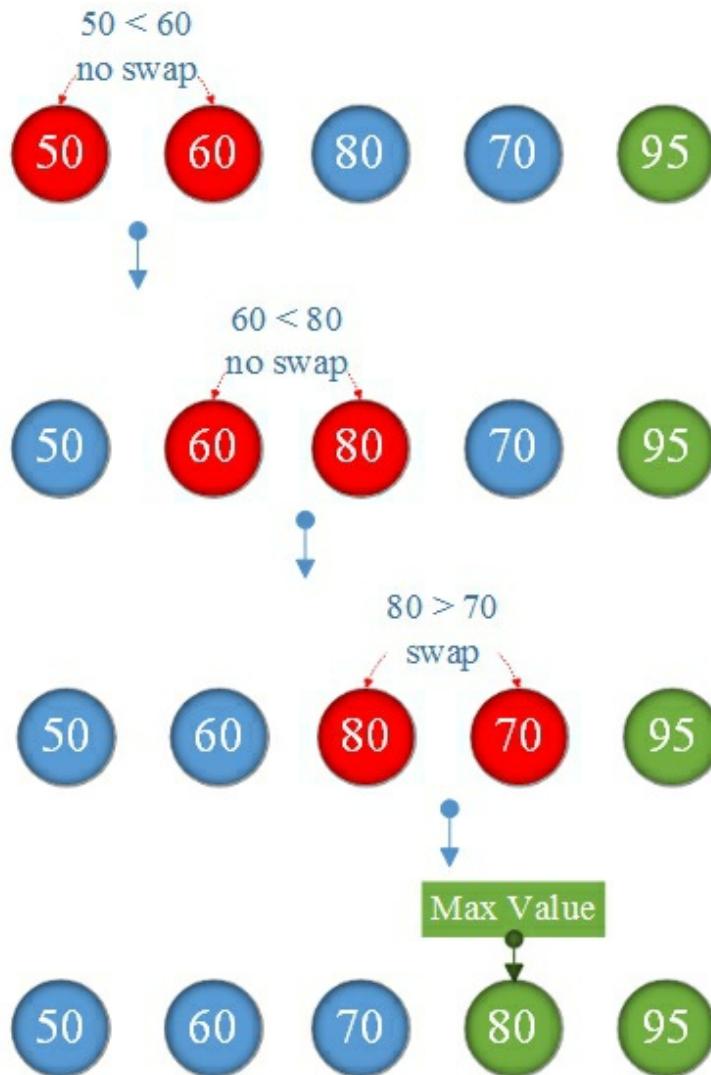


Already sorted

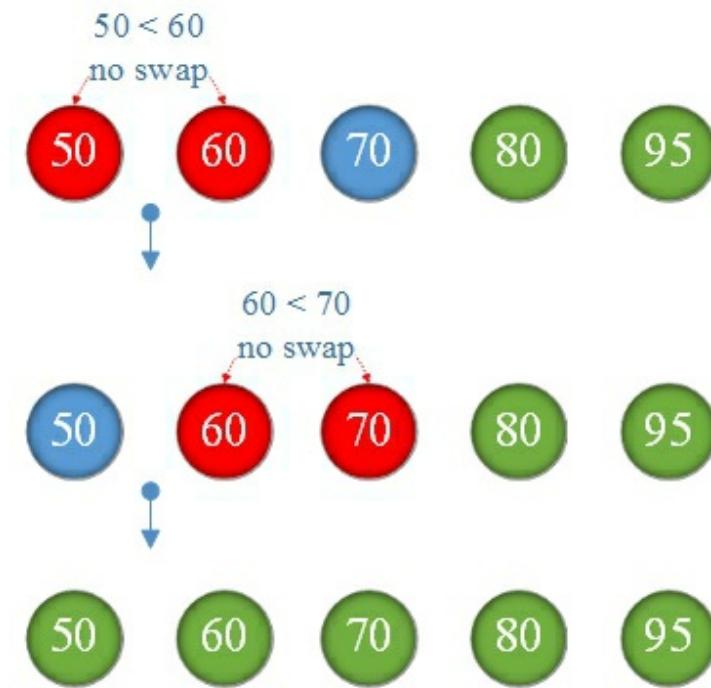
## 1. First sorting:



## 2. Second sorting:



### 3. Third sorting:



**No swap so terminate sorting** : we can get the sorting numbers from small to large



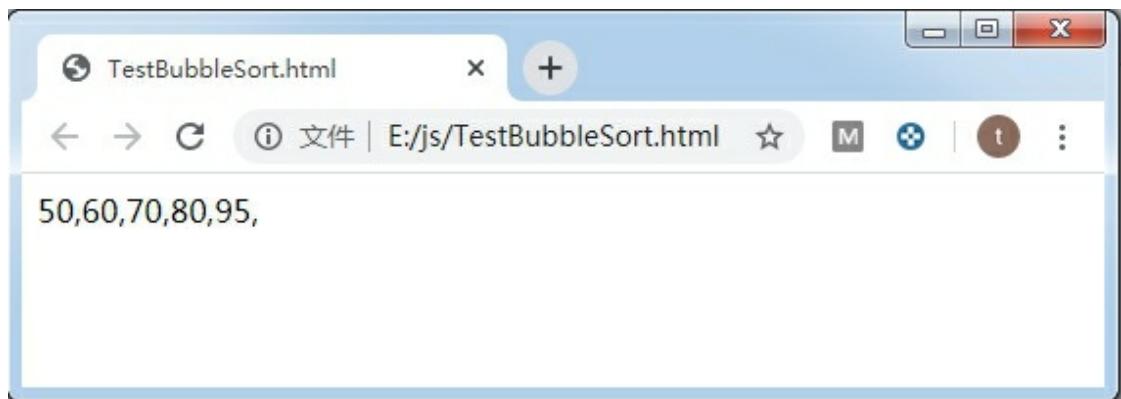
**1. Create a `TestBubbleSort.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
    class BubbleSort{
        static sort(arrays) {
            for (var i = 0; i < arrays.length - 1;
i++) {
                for (var j = 0; j < arrays.length - i -
1; j++) {
                    //swap
                    if (arrays[j] > arrays[j + 1]) {
                        var flag = arrays[j];
                        arrays[j] = arrays[j + 1];
                        arrays[j + 1] = flag;
                    }
                }
            }
        }
    }

//////////////////testing////////////////

var scores = [ 60, 50, 95, 80, 70 ];
BubbleSort.sort(scores);
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ",");
}
</script>
```

**Result:**



# Minimum Value

**Search the Minimum of Integer Sequences:**

60

80

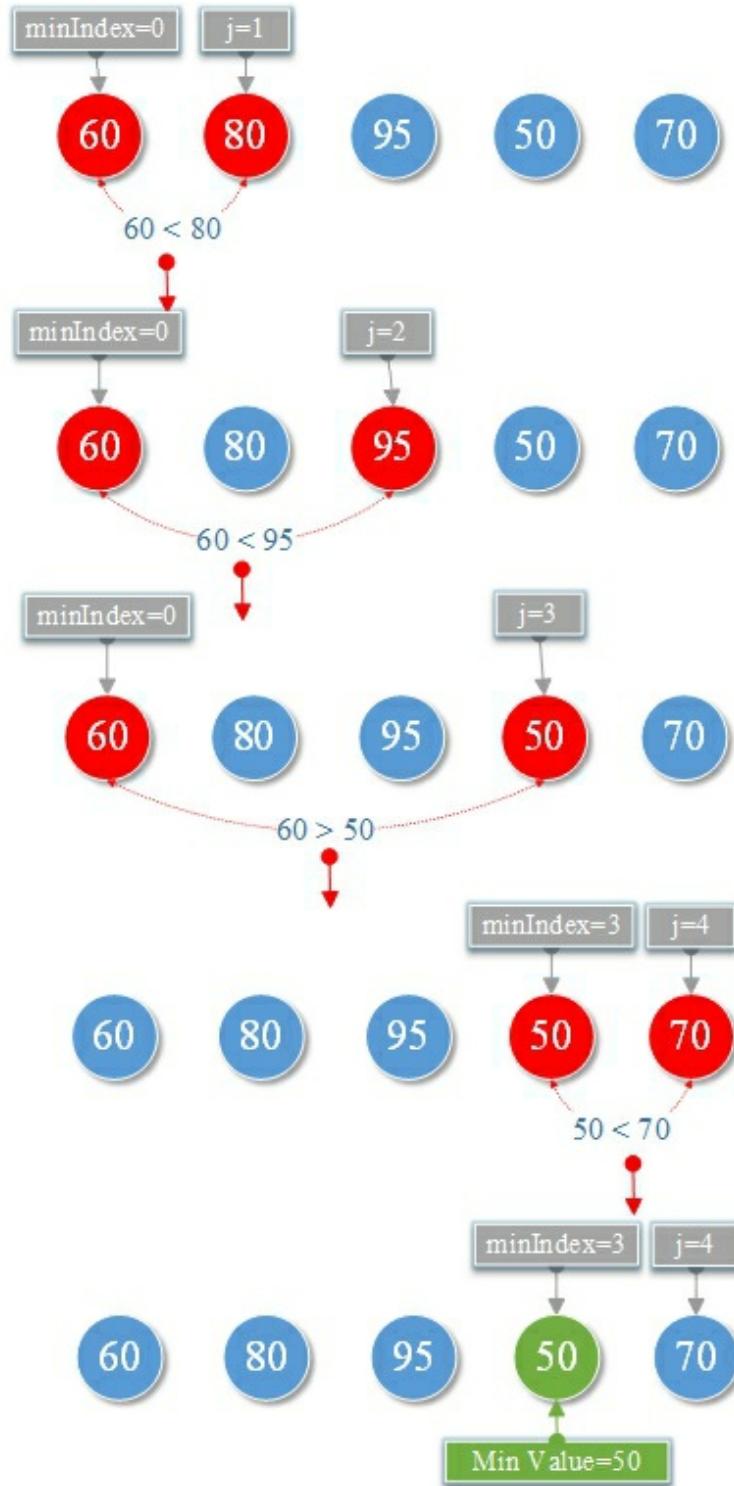
95

50

70

## 1. Algorithmic ideas

Initial value `minIndex=0, j=1` Compare `arrays[minIndex]` with `arrays[j]` if `arrays[minIndex] > arrays[j]` then `minIndex=j, j++` else `j++`. continue until the last number, `arrays[minIndex]` is the Min Value.



**1. Create a `TestMinValue.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
function min(arrays) {
    var minIndex = 0;// the index of the minimum
    for (var j = 1; j < arrays.length; j++) {
        if (arrays[minIndex] > arrays[j]) {
            minIndex = j;
        }
    }
    return arrays[minIndex];
}

//////////////////testing////////////////

var scores = [ 60, 80, 95, 50, 70 ];
var minValue = min(scores);
document.write("Min Value = " + minValue);

</script>
```

**Result:**



# Select Sorting Algorithm

## Select Sorting Algorithm:

Sorts an array by repeatedly finding the minimum element from unsorted part and putting it at the beginning.

Sort the following numbers from small to large

60

80

95

50

70

**Explanation:**



No sorting,

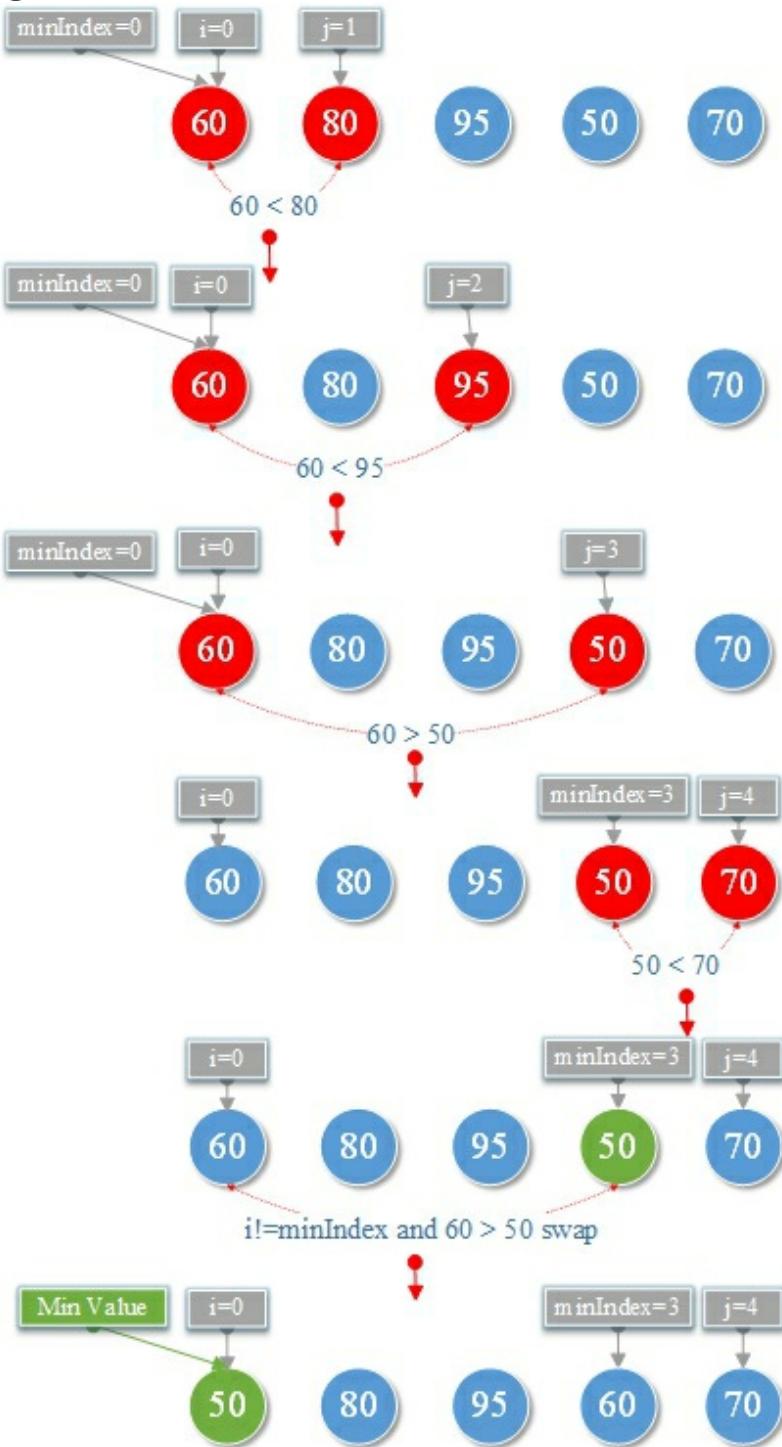


Comparing,

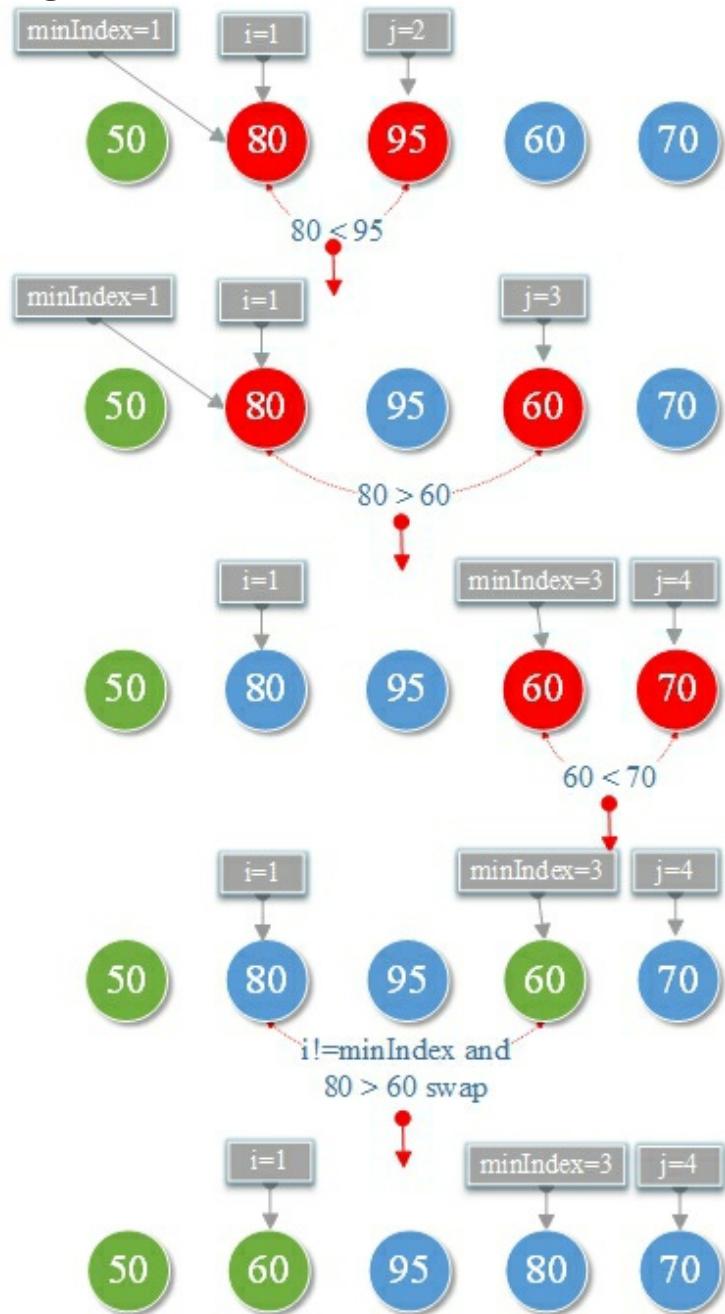


Already sorted.

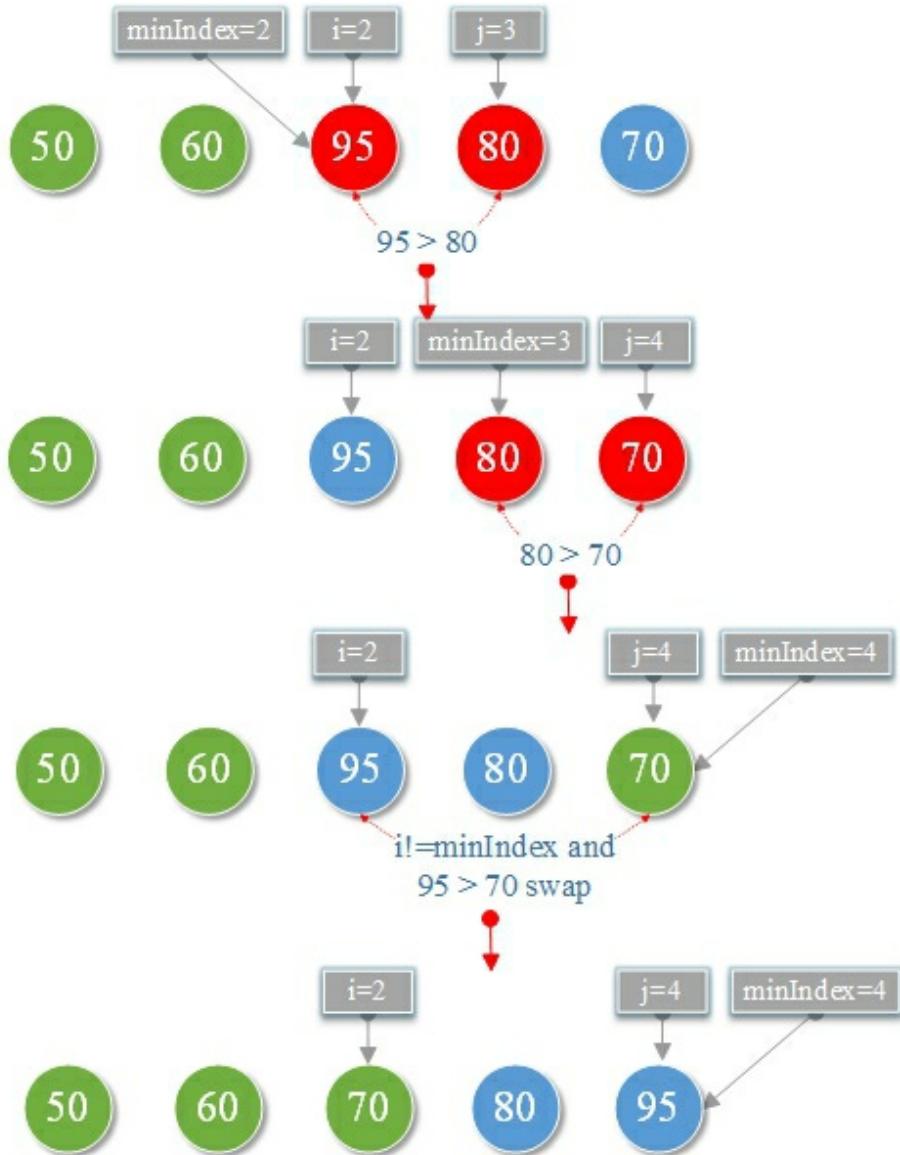
## 1. First sorting:



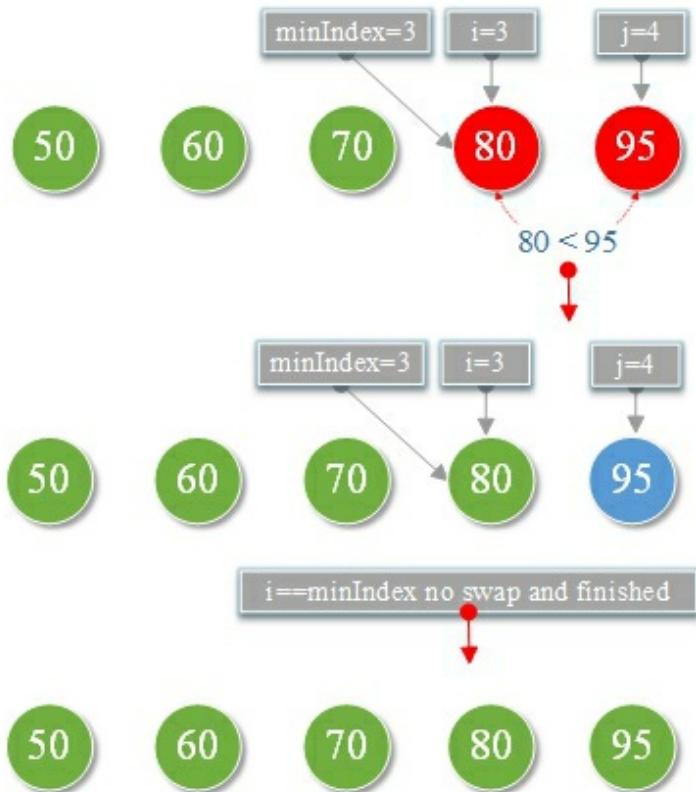
## 2. Second sorting:



### 3. Third sorting:



#### 4. Forth sorting:



we can get the sorting numbers from small to large



**1. Create a `TestSelectSort.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
    class SelectSort{
        static sort(arrays) {
            var len = arrays.length - 1;
            var minIndex;// Save the index of the selected minimum

            for (var i = 0; i < len; i++) {
                minIndex = i;
                //Save the minimum value of each loop as the first element
                var minValue = arrays[minIndex];
                for (var j = i; j < len; j++) {
                    if (minValue > arrays[j + 1]) { // minimum value
                        exchange with the minIndex
                        minValue = arrays[j + 1];
                        minIndex = j + 1;
                    }
                }
            }

            //if minimum index changes, current minimum is exchanged
            with the minIndex
            if (i != minIndex){
                var temp = arrays[i];
                arrays[i] = arrays[minIndex];
                arrays[minIndex] = temp;
            }
        }
    }
}

//////////////////testing///////////
var scores = [ 90, 70, 50, 80, 60, 85 ];
SelectSort.sort(scores);
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ",");
}
```

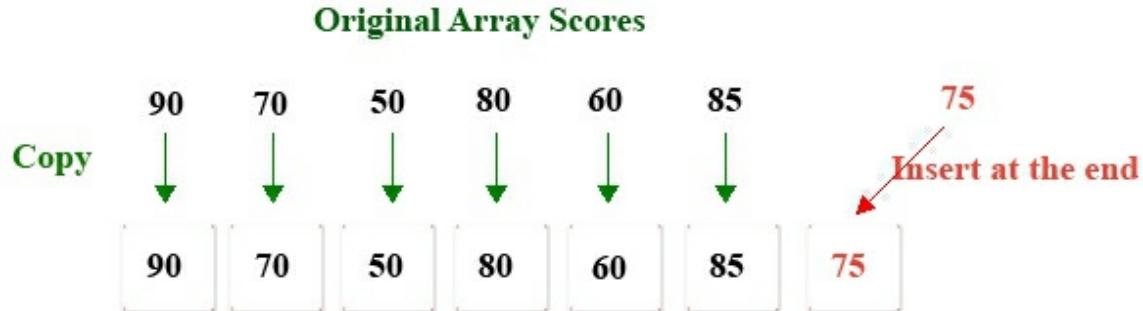
```
</script>
```

**Result:**

50,60,70,80,95,

# Linear Table Append

1. Add a score **75** to the end of the one-dimensional array **scores**.



**Analysis:**

1. First create a temporary array(**tempArray**) larger than the original scores array length
2. Copy each value of the scores to **tempArray**
3. Assign 75 to the last index position of **tempArray**
4. Finally assign the **tempArray** pointer reference to the original scores;

**1. Create a `TestOneArrayAppend.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">

function append(array, value) {
    //create a new array, length = array.length + 1
    var tempArray = new Array(array.length + 1);

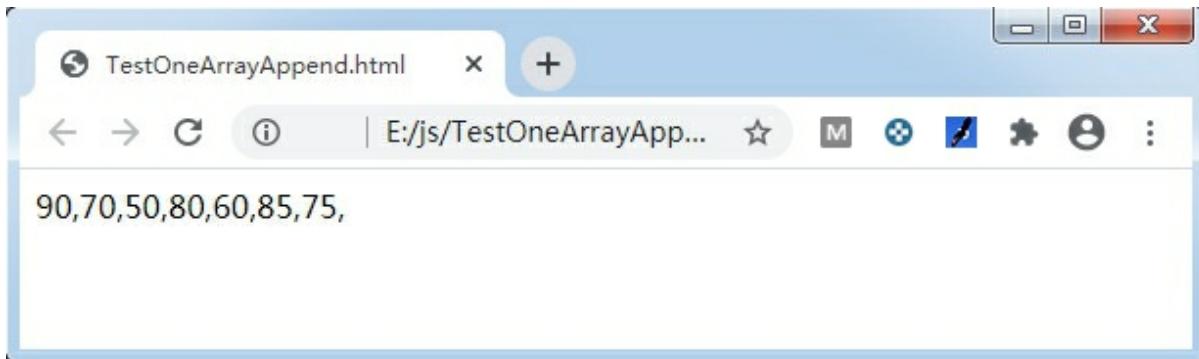
    for (var i = 0; i < array.length; i++) {
        tempArray[i] = array[i];
    }
    tempArray[array.length] = value
    return tempArray;
}

//////////////////testing/////////////////
var scores = new Array( 90, 70, 50, 80, 60, 85 );

scores = append(scores, 75);

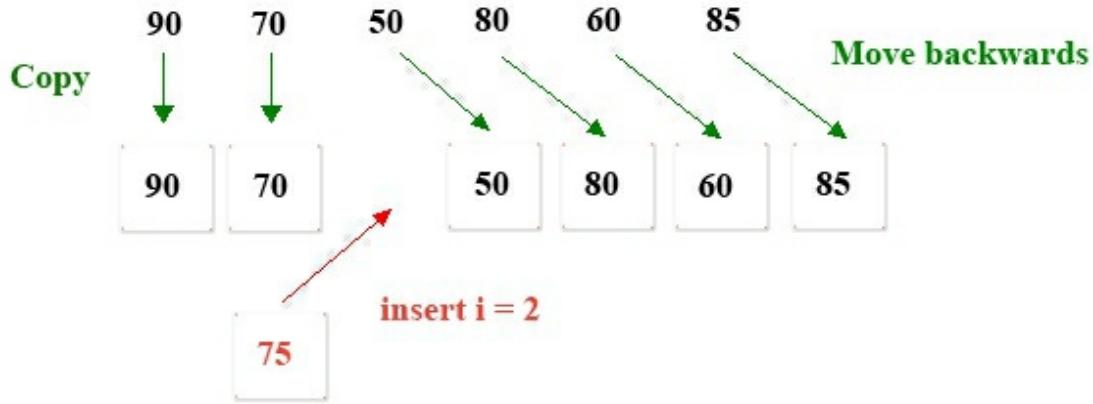
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ",");
}
</script>
```

**Result:**



# Linear Table Insert

1. Insert a student's score anywhere in the one-dimensional array scores.



## Analysis:

1. First create a temporary array **tempArray** larger than the original scores array length
2. Copy each value of the previous value of the scores array from the beginning to the insertion position to **tempArray**
3. Move the scores array from the insertion position to each value of the last element and move it back to **tempArray**
4. Then insert the score **75** to the index of the **tempArray**.
5. Finally assign the **tempArray** pointer reference to the scores;

**1. Create a `TestOneArrayInsert.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">

function insert(array, score, insertIndex) {
    var tempArray = new Array(array.length + 1);
    for (var i = 0; i < array.length; i++) {
        if (i < insertIndex) {
            tempArray[i] = array[i];
        } else {
            tempArray[i + 1] = array[i];
        }
    }
    tempArray[insertIndex] = score;
    return tempArray;
}

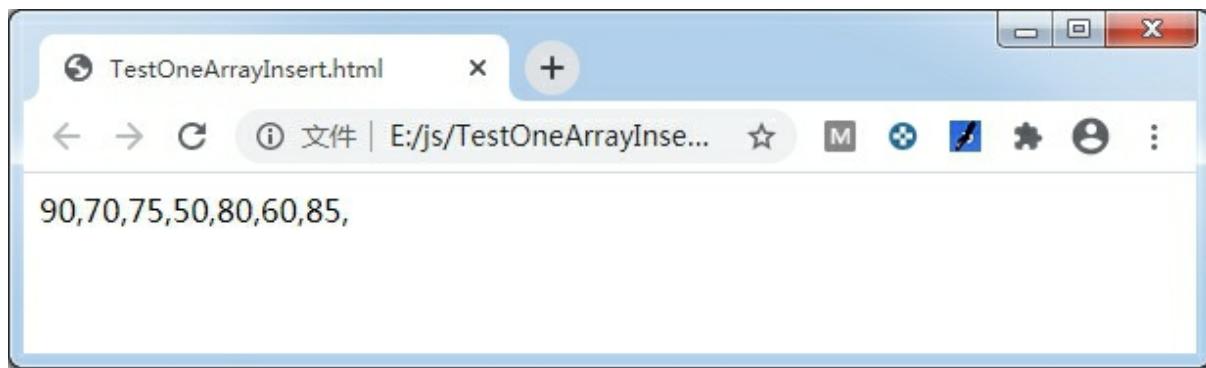
//////////////////testing/////////////////
var scores = new Array( 90, 70, 50, 80, 60, 85 );

//Insert 75 into the position: index = 2
scores = insert(scores, 75, 2);

for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ",");
}

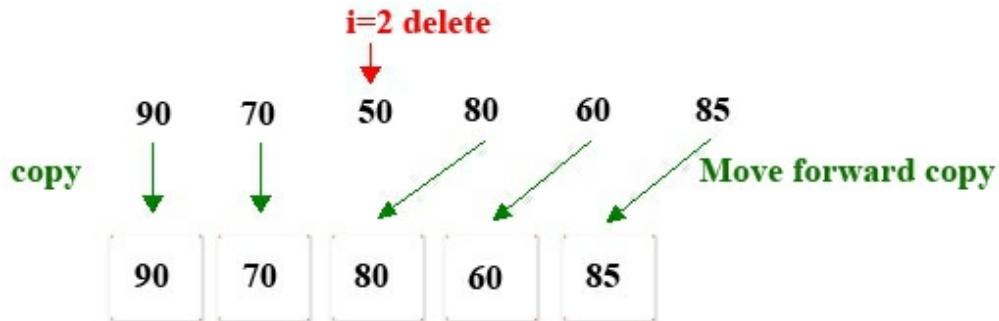
</script>
```

**Result:**



# Linear Table Delete

1. Delete the value of the **index=2** from scores array



## Analysis:

1. Create a temporary array **tempArray** that length smaller than scores by 1.
2. Copy the data in front of **i=2** to the front of **tempArray**
3. Copy the array after **i=2** to the end of **tempArray**
4. Assign the **tempArray** pointer reference to the scores
5. Printout scores

**1. Create a `TestOneArrayDelete.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">

    function remove(array, index){
        // create a new array, length = array.length - 1
        var tempArray = new Array(array.length - 1);

        for (var i = 0; i < array.length; i++) {
            if (i < index) // Copy the data in front of index to the front of
tempArray
                tempArray[i] = array[i];
            if (i > index) // Copy the array after index to the end of
tempArray
                tempArray[i - 1] = array[i];
        }
        return tempArray;
    }

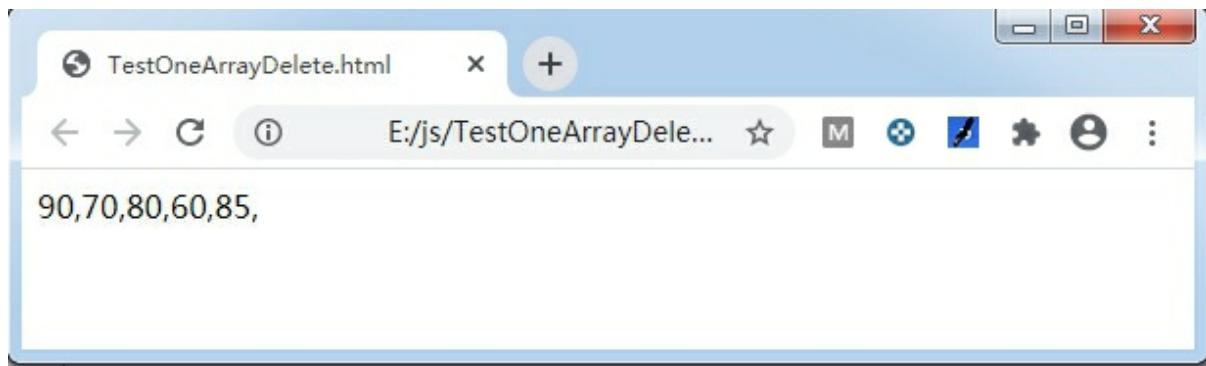
    /////////////////////testing/////////////////
var scores = new Array( 90, 70, 50, 80, 60, 85 );

scores = remove(scores, 2);//delete score that index = 2

    for (var i = 0; i < scores.length; i++) {
        document.write(scores[i] + ",");
    }

</script>
```

**Result:**



# Insert Sorting Algorithm

## Insert Sorting Algorithm:

Take an unsorted new element in the array, compare it with the already sorted element before, if the element is smaller than the sorted element, insert new element to the right position.

**Sort the following numbers from small to large**



## Explanation:



No sorting,

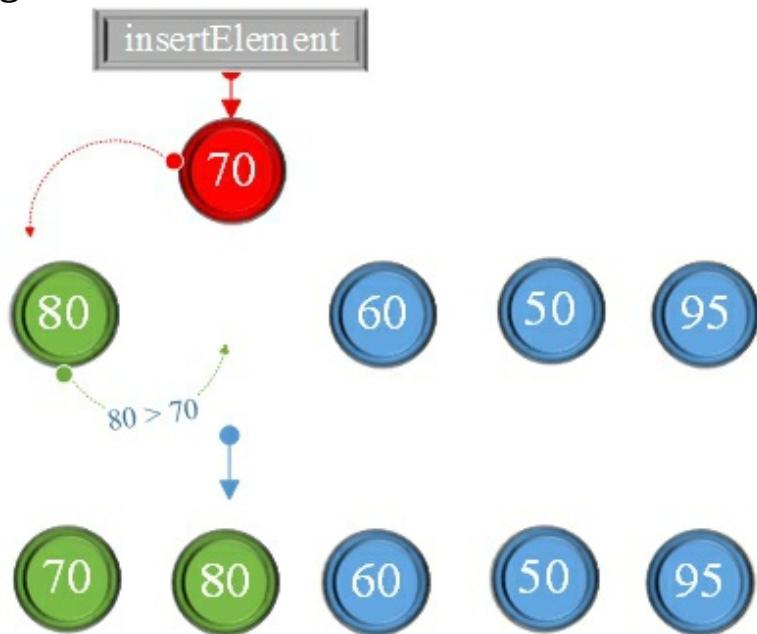


Inserting,

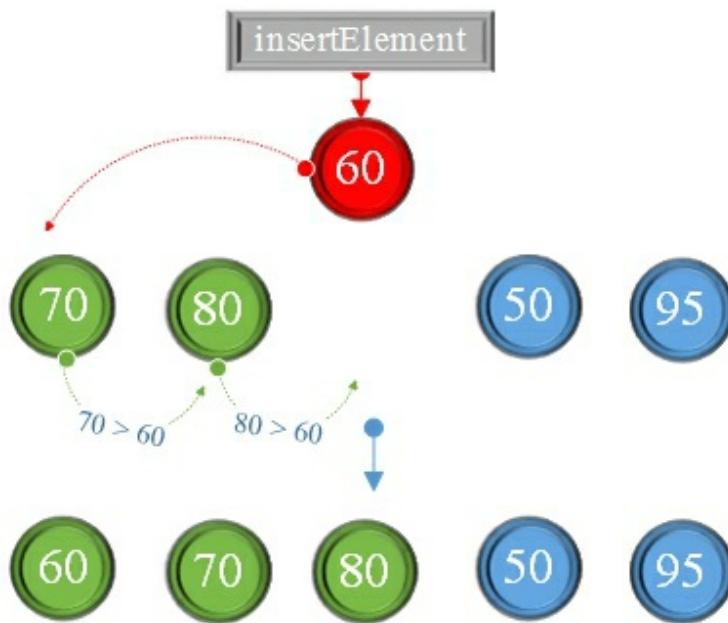


Already sorted

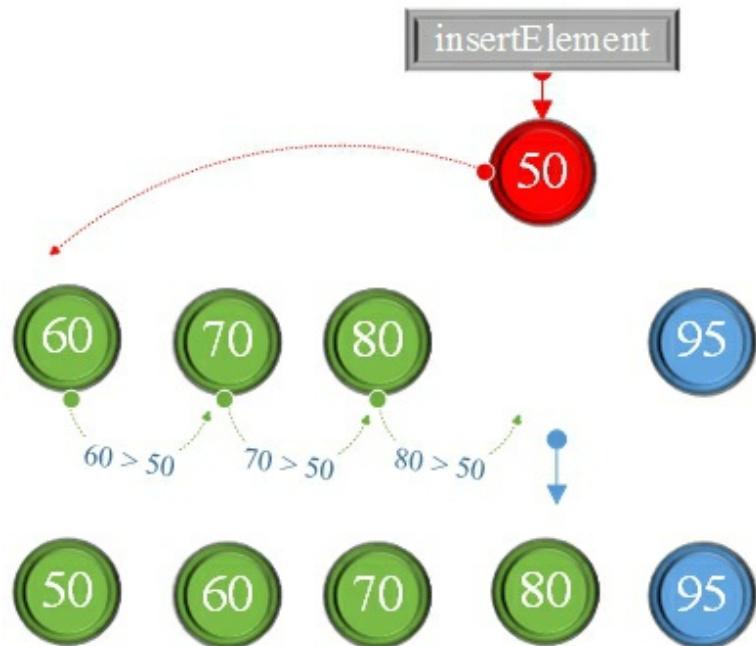
## 1. First sorting:



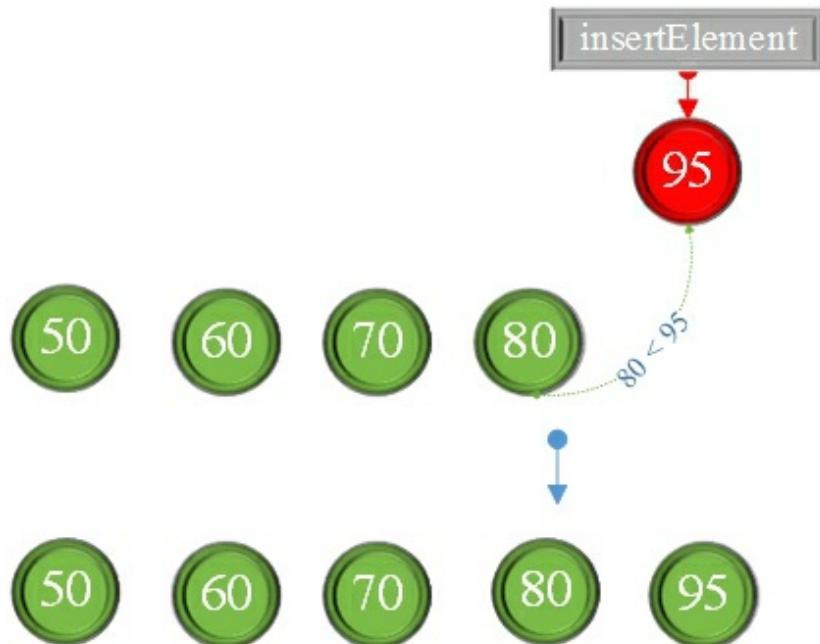
## 2. Second sorting:



### 3. Third sorting:



### 4 Third sorting:



**1. Create a `TestInsertSort.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
    class InsertSort{
        static sort(arrays) {
            for (var i = 0; i < arrays.length; i++) {
                var insertElement = arrays[i];//Take unsorted new elements
                var insertPosition = i; //Inserted position
                for (var j = insertPosition - 1; j >= 0; j--) {
                    //If the new element is smaller than the sorted element,
                    shifted to the right
                    if (insertElement < arrays[j]) {
                        arrays[j + 1] = arrays[j];
                        insertPosition--;
                    }
                }
                arrays[insertPosition] = insertElement;//Insert the new
                element
            }
        }
    }

//////////testing//////////

var scores = [ 90, 70, 50, 80, 60, 85 ];
InsertSort.sort(scores);
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ",");
}
</script>
```

**Result:**

50,60,70,80,95,

# Reverse Array

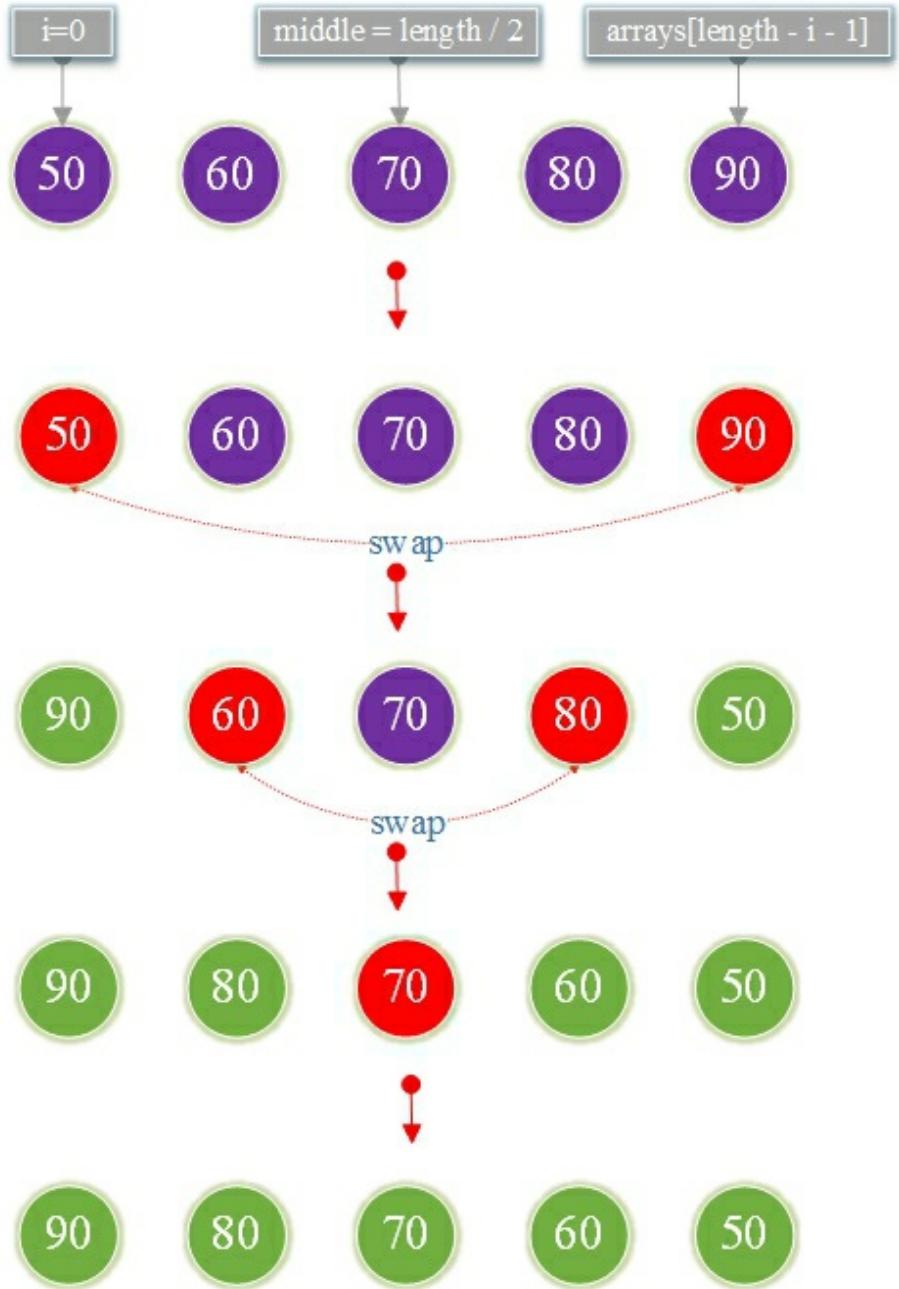
**Inversion of ordered sequences:**



## 1. Algorithmic ideas

Initial  $i = 0$  and then swap the first element `arrays[i]` with last element `arrays[length - i - 1]`

Repeat until index of middle  $i == \text{length} / 2$ .



**1. Create a `TestReverse.html` with **Notepad** and open it in your browser.**

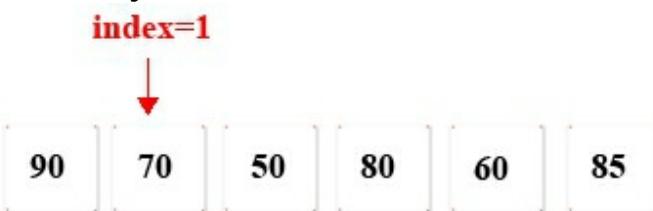
```
<script type="text/javascript">
    function reverse(arrays) {
        var length = arrays.length;
        var middle = length / 2;
        for (var i = 0; i <= middle; i++) {
            var temp = arrays[i];
            arrays[i] = arrays[length - i - 1];
            arrays[length - i - 1] = temp;
        }
    }
    ////////////////testing/////////////
    var scores = [ 50, 60, 70, 80, 90 ];
    reverse(scores);
    for (var i = 0; i < scores.length; i++) {
        document.write(scores[i] + ",");
    }
</script>
```

**Result:**

90,80,70,60,50,

# Linear Table Search

1. Please enter the value you want to search like : **70** return index.

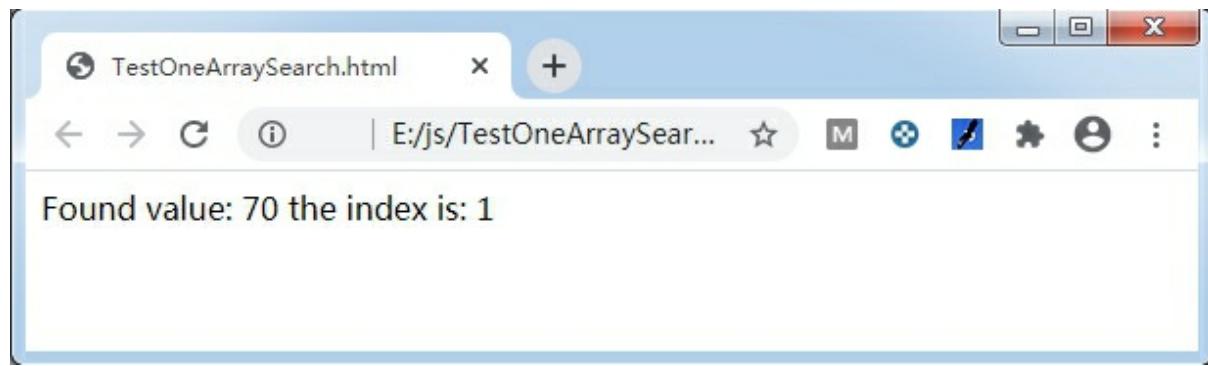


1. Create a **TestOneArraySearch.html** with **Notepad** and open it in your browser.

```
<script type="text/javascript">
    function search(array, value){
        for (var i = 0; i < array.length; i++) {
            if (array[i] == value) {
                return i;
            }
        }
        return -1;
    }
    ////////////////////testing/////////////////
    var scores = new Array( 90, 70, 50, 80, 60, 85 );
    var value = 70;
    var index = search(scores, value);

    if (index > 0) {
        document.write("Found value: " + value + " the index is: " + index);
    }else{
        document.write("The value was not found : " + value);
    }
</script>
```

**Result:**



# Dichotomy Binary Search

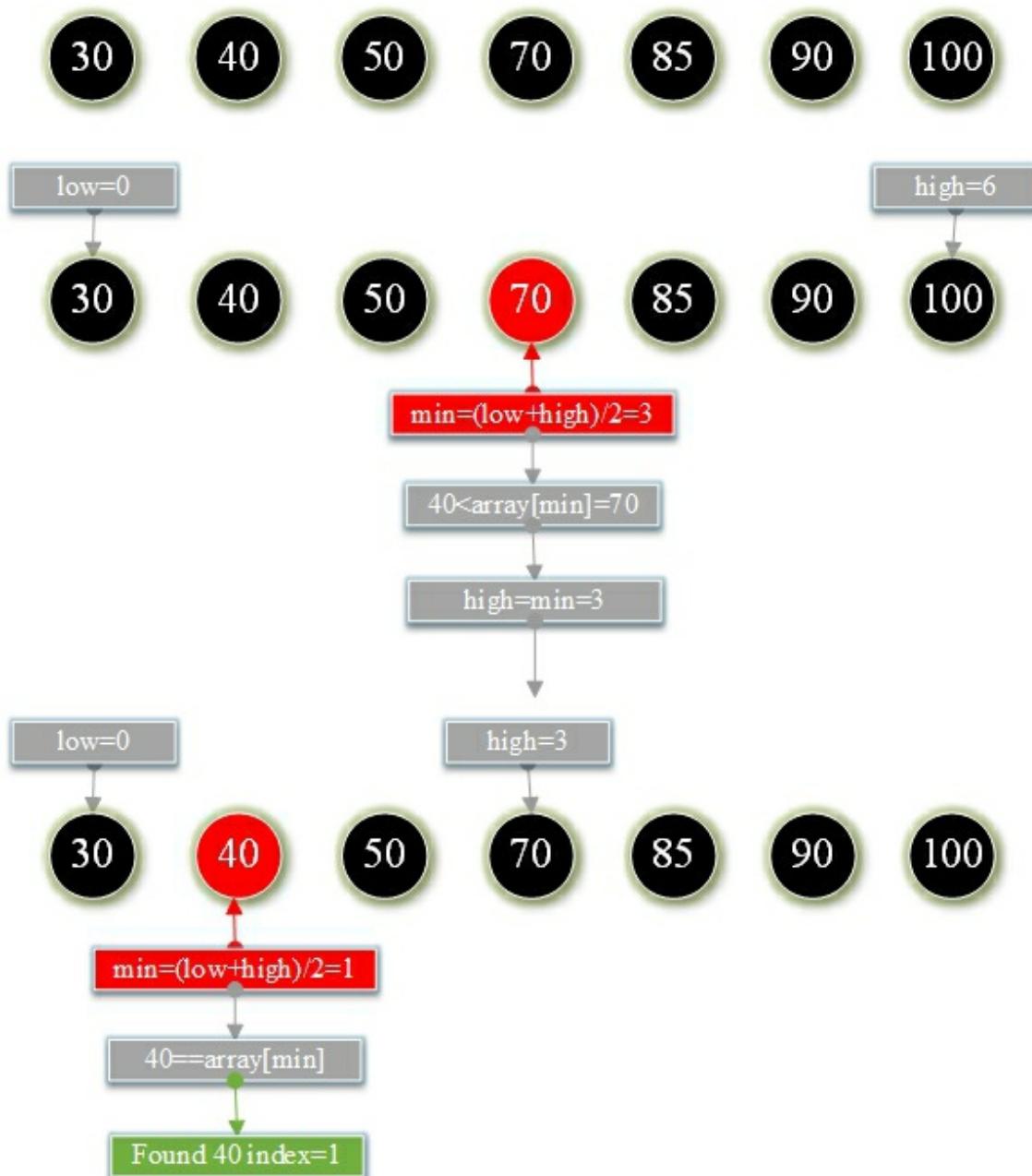
## Dichotomy Binary Search:

Find the index position of a given value from an already ordered array.

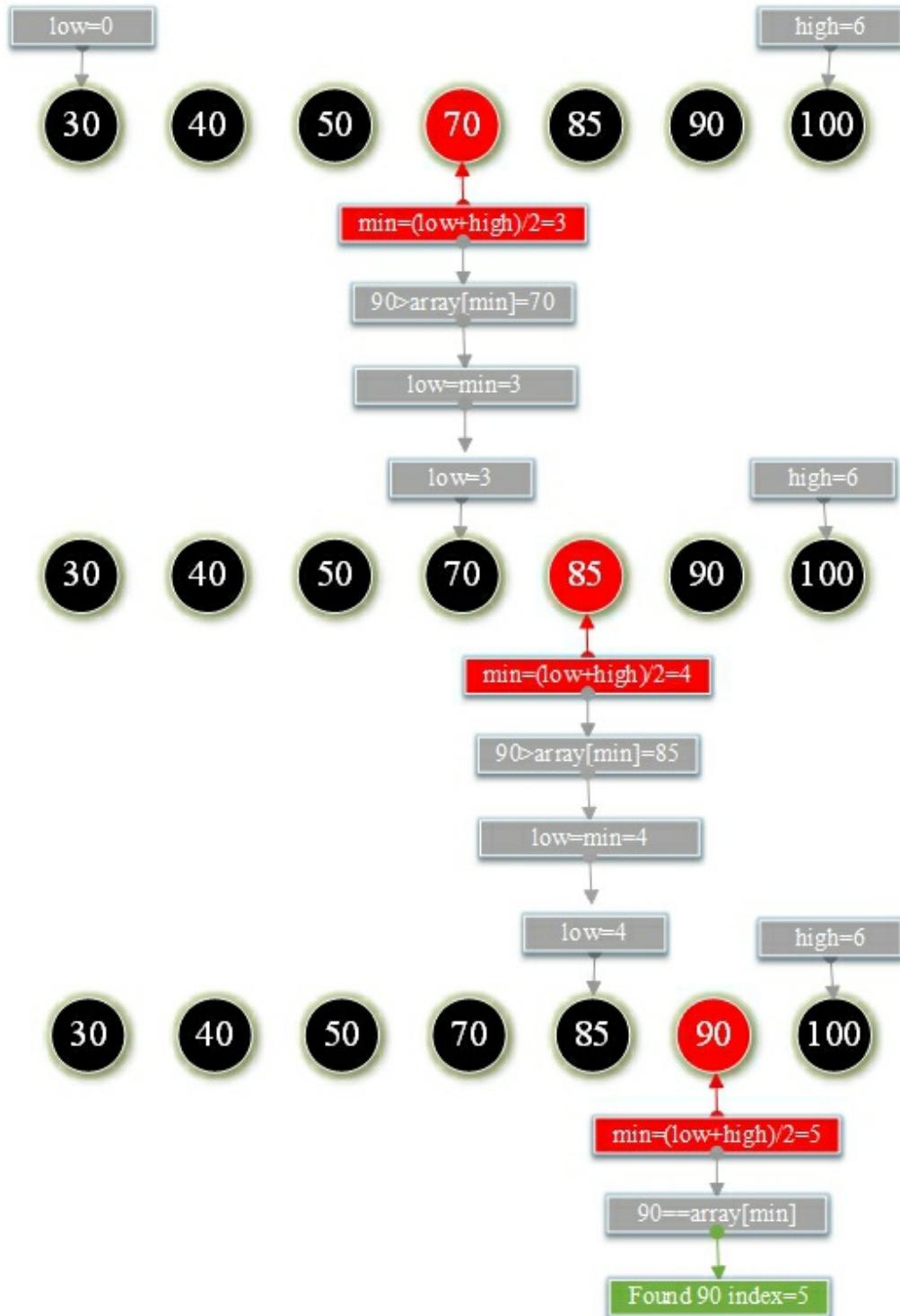


1. Initialize the lowest index `low=0`, the highest index `high=scores.length-1`
2. Find the `searchValue` of the middle index `mid=(low+high)/2` `scores[mid]`
3. Compare the `scores[mid]` with `searchValue`  
If the `scores[mid]==searchValue` print current mid index,  
If `scores[mid]>searchValue` that the `searchValue` will be found between  
`low and mid-1`
4. And so on. Repeat step 3 until you find `searchValue` or `low>=high` to terminate the loop.

**Example 1 : Find the index of `searchValue=40` in the array that has been sorted below.**



**Example 2 : Find the index of `searchValue=90` in the array that has been sorted below.**



**1. Create a `TestBinarySearch.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
    class BinarySearch{
        static search(arrays, searchValue) {
            var low = 0;
            var high = arrays.length - 1;
            var mid = 0;
            while (low <= high) {
                mid = (low + high) / 2;
                if (arrays[mid] == searchValue) {
                    return mid;
                } else if (arrays[mid] < searchValue) {
                    low = mid + 1;
                } else if (arrays[mid] > searchValue) {
                    high = mid - 1;
                }
            }
            return -1;
        }
    }

//////////testing//////////

var scores = [ 30, 40, 50, 70, 85, 90, 100 ];
var searchValue = 40;
var position = BinarySearch.search(scores, searchValue);
document.write(searchValue + " position:" + position);

document.write("<br>-----<br>");

searchValue = 90;
position = BinarySearch.search(scores, searchValue);
document.write(searchValue + " position:" + position);
</script>
```

**Result:**

40 position:1

---

90 position:5

# Shell Sorting

## Shell Sorting:

Shell sort is a highly efficient sorting algorithm and is based on insertion sort algorithm. This algorithm avoids large shifts as in case of insertion sort, if the smaller value is to the far right and has to be moved to the far left.

**Sort the following numbers from small to large by Shell Sorting**

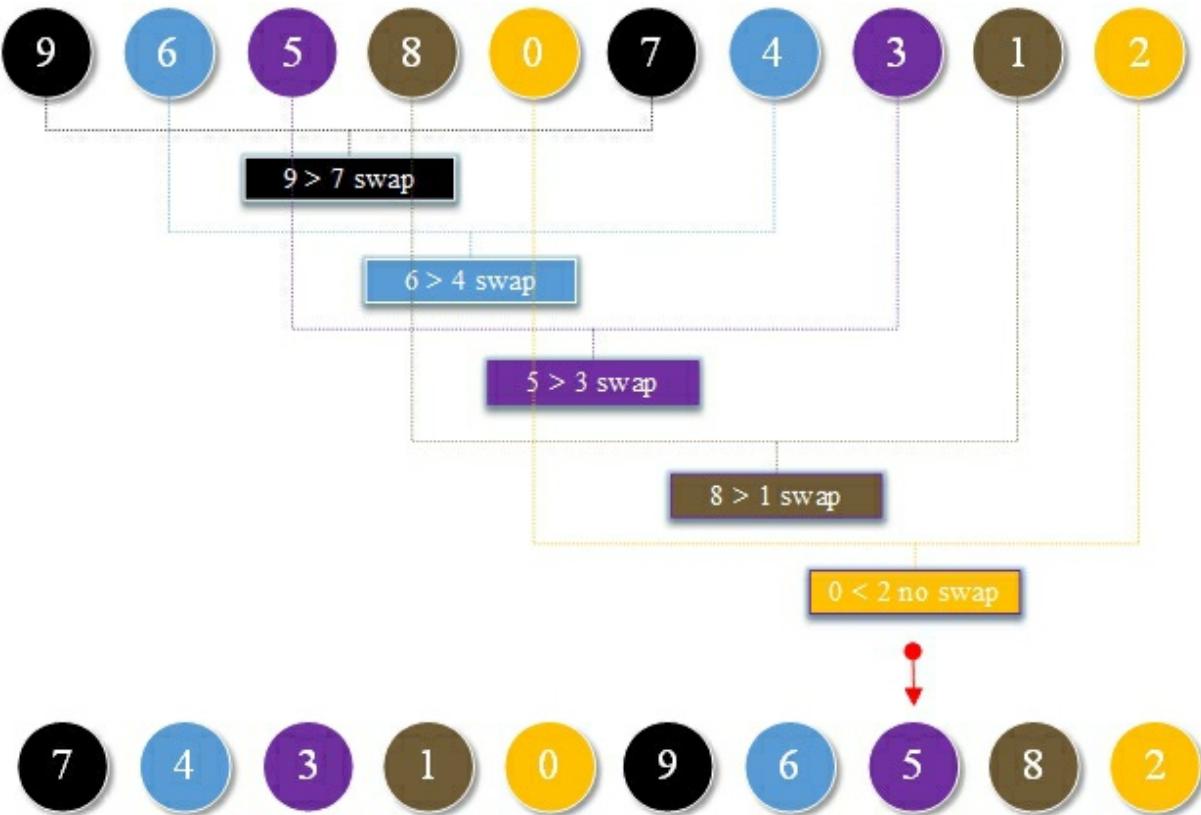


## Algorithmic result:

The array is grouped according to a certain increment of subscripts, and the insertion of each group is sorted. As the increment decreases gradually until the increment is 1, the whole data is grouped and sorted.

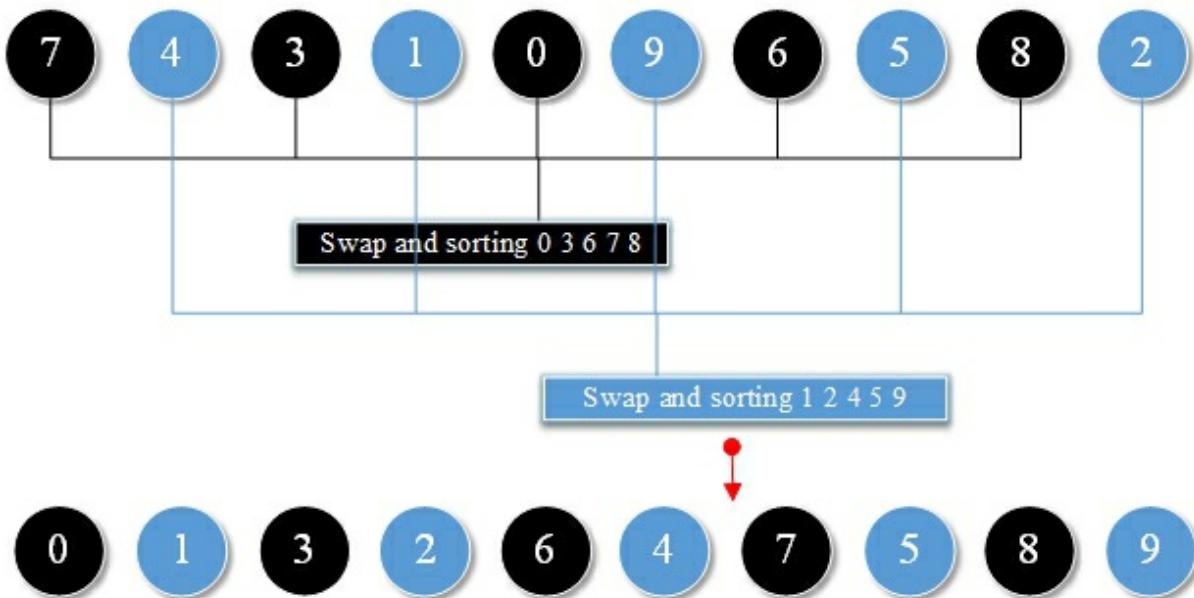
## 1. The first sorting :

gap = array.length / 2 = 5



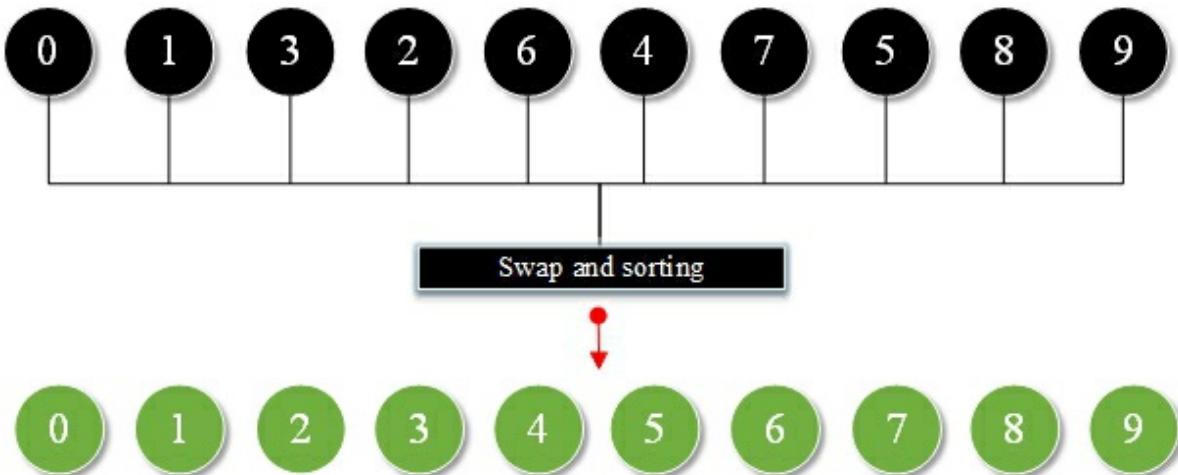
## 2. The second sorting :

$$\text{gap} = 5 / 2 = 2$$



**3. The third sorting :**

$$\text{gap} = 2 / 2 = 1$$



**1. Create a `TestShellSort.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
    function shellSort(array) {
        var middle = parseInt(array.length / 2);
        for (var gap = middle ; gap > 0; gap = parseInt(gap / 2)) {
            for (var i = gap; i < array.length; i++) {
                var j = i;
                while (j - gap >= 0 && array[j] < array[j - gap]) {
                    swap(array, j, j - gap);
                    j = j - gap;
                }
            }
        }
    }

    function swap(array, a, b) {
        array[a] = array[a] + array[b];
        array[b] = array[a] - array[b];
        array[a] = array[a] - array[b];
    }

    ////////////////////testing/////////////////
    var scores = [ 9, 6, 5, 8, 0, 7, 4, 3, 1, 2 ];
    shellSort(scores);
    for (var i = 0; i < scores.length; i++) {
        document.write(scores[i] + ",");
    }

</script>
```

**Result:**

0,1,2,3,4,5,6,7,8,9,

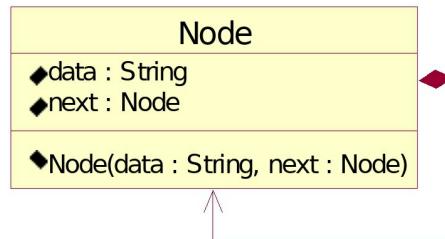
# Unidirectional Linked List

## Unidirectional Linked List Single Link:

Is a chained storage structure of a linear table, which is connected by a node. Each node consists of data and next pointer to the next node.



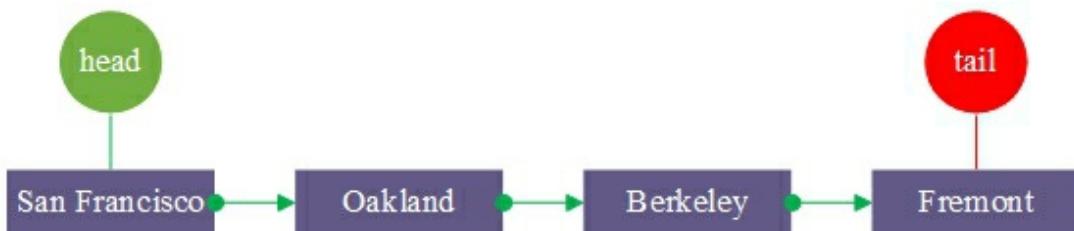
## UML Diagram



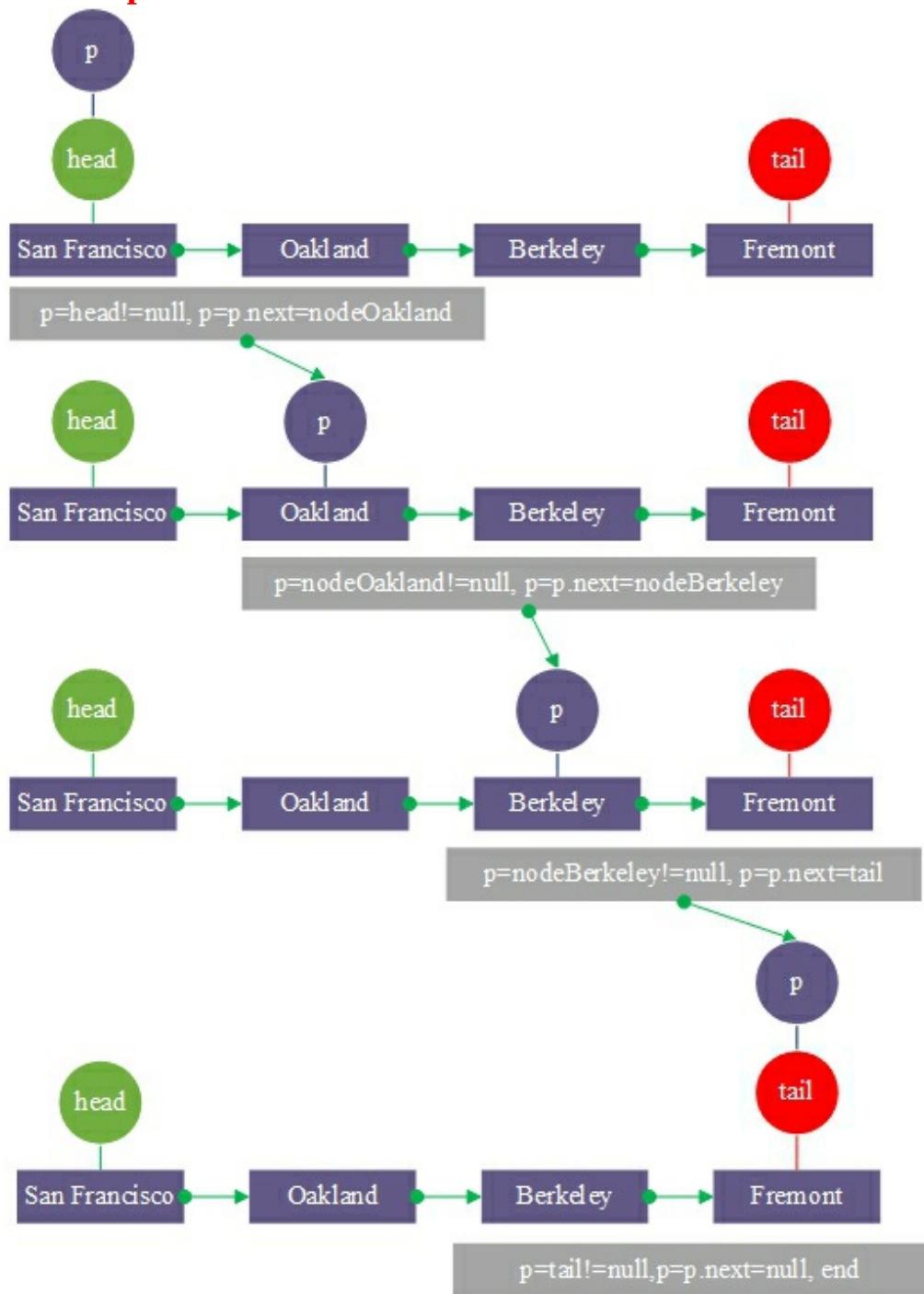
```
class Node{    constructor(data, next){        this.data = data;        this.next = next;    }    getData(){        return this.data;    }}
```

## 1. Unidirectional Linked List initialization.

Example : Construct a San Francisco subway Unidirectional linked list



## 2. traversal output.



**1. Create a [TestUnidirectionalLinkedList.html](#) with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
class Node{
    constructor(data, next){
        this.data = data;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class LinkedList{
    init() {
        // the first node called head node
        this.head = new Node("San Francisco",
null);

        var nodeOakland = new Node("Oakland",
null);
        this.head.next = nodeOakland;

        var nodeBerkeley = new
Node("Berkeley", null);
        nodeOakland.next = nodeBerkeley;

        // the last node called tail node
        this.tail = new Node("Fremont", null);
        nodeBerkeley.next = this.tail;

        return this.head;
    }

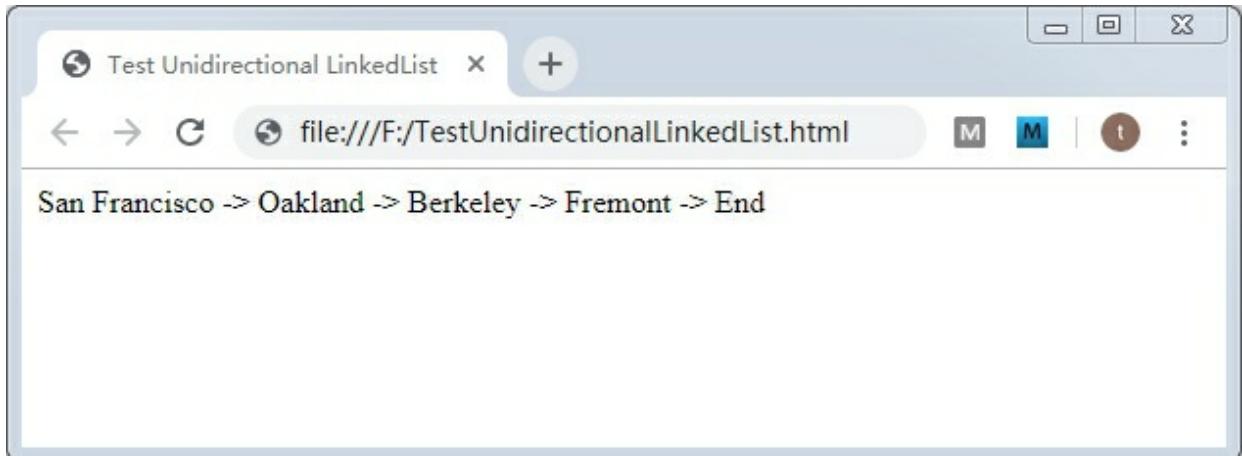
    print(node) {
        var p = node;
        while (p != null) // From the beginning to
```

the end

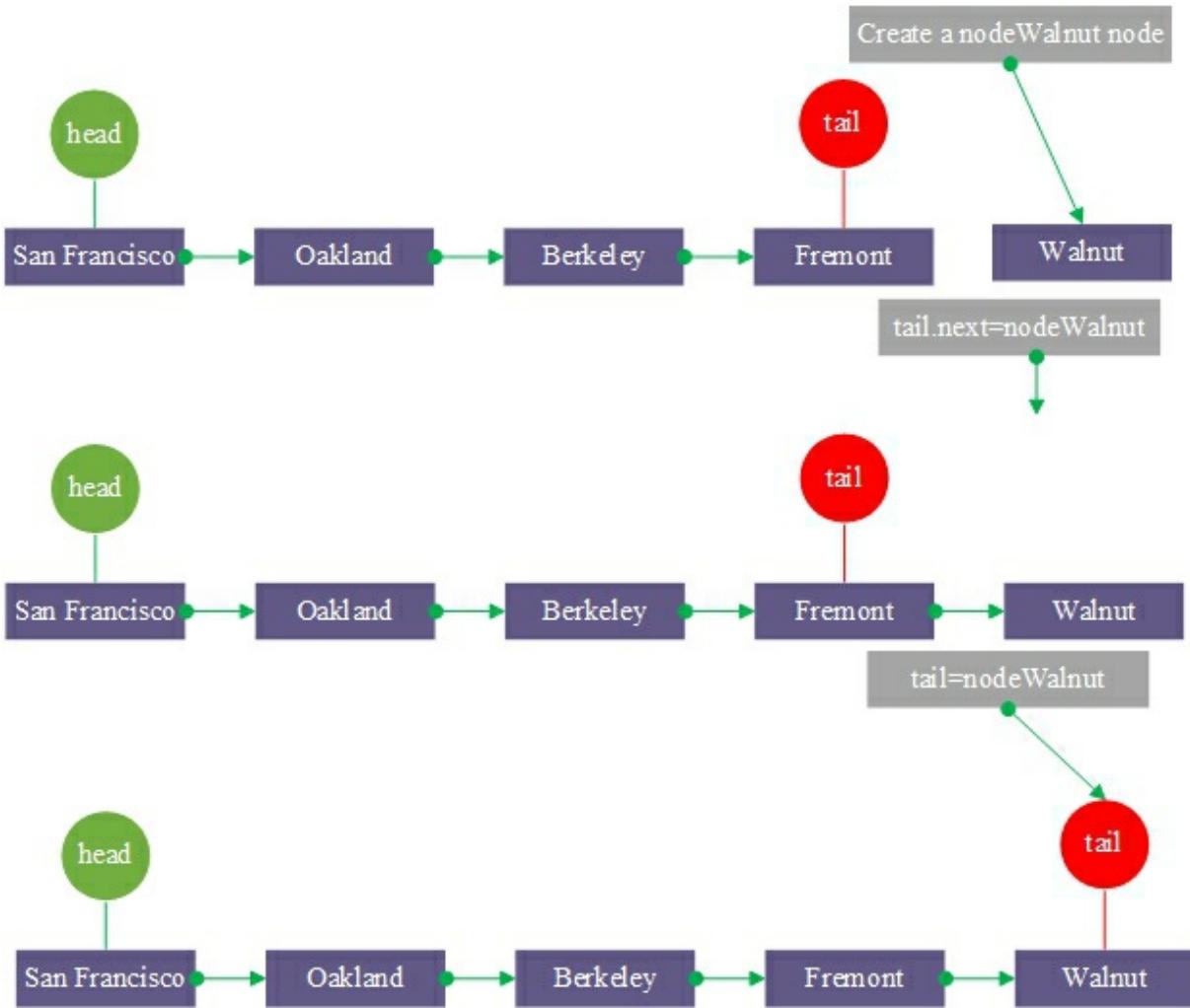
```
{  
    var data = p.getData();  
    document.write(data + " -> ");  
    p = p.next;  
}  
document.write("End<br><br>");  
}  
}  
  
//////////////////testing////////////////
```

```
var linkedList = new LinkedList();  
var head = linkedList.init();  
linkedList.print(head);  
</script>
```

## Result:



### 3. Append a new node name: **Walnut** to the end.



## 1. Create a **TestUnidirectionalLinkedListAppend.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, next){
        this.data = data;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class LinkedList{

    init() {
        // the first node called head node
        this.head = new Node("San Francisco", null);

        var nodeOakland = new Node("Oakland", null);
        this.head.next = nodeOakland;

        var nodeBerkeley = new Node("Berkeley", null);
        nodeOakland.next = nodeBerkeley;

        // the last node called tail node
        this.tail = new Node("Fremont", null);
        nodeBerkeley.next = this.tail;

        return this.head;
    }

    add(newNode) {
        this.tail.next = newNode;
        this.tail = newNode;
    }
}
```

```

print(node) {
    var p = node;
    while (p != null) // From the beginning to the end
    {
        var data = p.getData();
        document.write(data + " -> ");
        p = p.next;
    }
    document.write("End<br><br>");
}
}

//////////////////testing////////////////

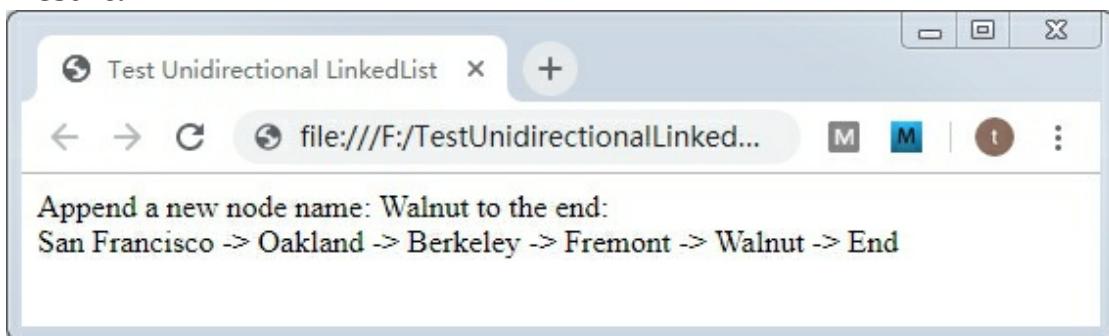
var linkedList = new LinkedList();
var head = linkedList.init();

document.write("Append a new node name: Walnut to the end: <br>");
linkedList.add(new Node("Walnut", null));

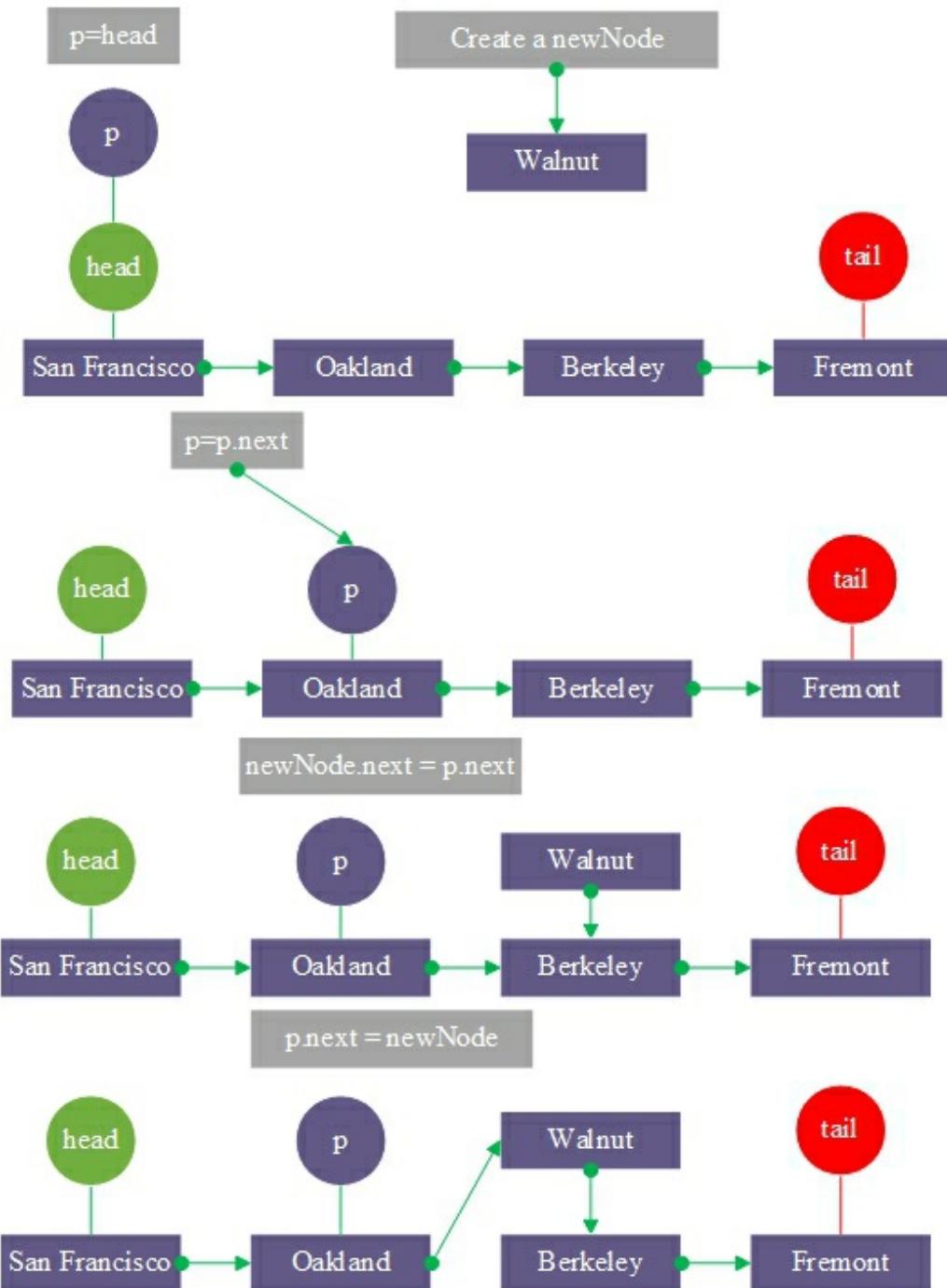
linkedList.print(head);
</script>

```

## Result:



### 3. Insert a node **Walnut** in position 2.



## 1. Create a **TestUnidirectionalLinkedListInsert.html** with **Notepad**

```
<script type="text/javascript">
  class Node{
    constructor(data, next){
      this.data = data;
      this.next = next;
    }

    getData(){
      return this.data;
    }
  }

  class LinkedList{
    init() {
      // the first node called head node
      this.head = new Node("San Francisco", null);

      var nodeOakland = new Node("Oakland", null);
      this.head.next = nodeOakland;

      var nodeBerkeley = new Node("Berkeley", null);
      nodeOakland.next = nodeBerkeley;

      // the last node called tail node
      this.tail = new Node("Fremont", null);
      nodeBerkeley.next = this.tail;

      return this.head;
    }

    insert(insertPosition, newNode) {
      var p = this.head;
      var i = 0;
      // Move the node to the insertion position
      while (p.next != null && i < insertPosition - 1) {
        p = p.next;
        i++;
      }
    }
  }
}
```

```

        }
        newNode.next = p.next; // newNode next point to next
    node
        p.next = newNode; // current next point to newNode
    }

    print(node) {
        var p = node;
        while (p != null) // From the beginning to the end
        {
            var data = p.getData();
            document.write(data + " -> ");
            p = p.next;
        }
        document.write("End<br><br>");
    }
}

//////////////////testing/////////////////

```

```

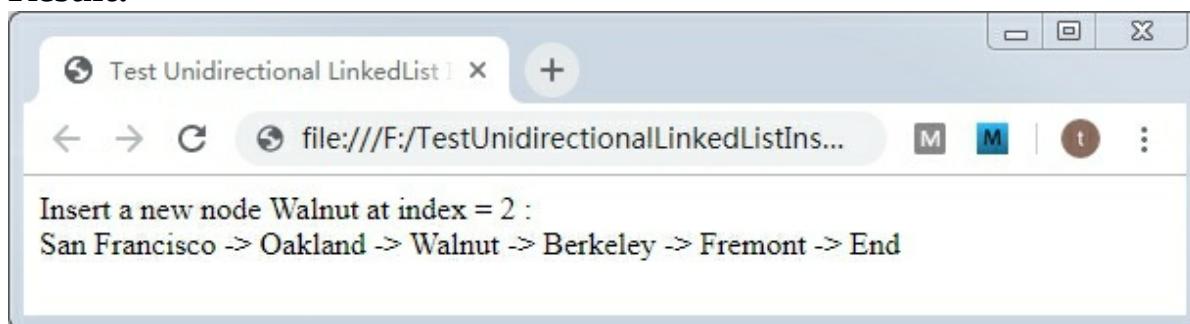
var linkedList = new LinkedList();
var head = linkedList.init();

document.write("Insert a new node Walnut at index = 2 : <br>");
linkedList.insert(2, new Node("Walnut", null));

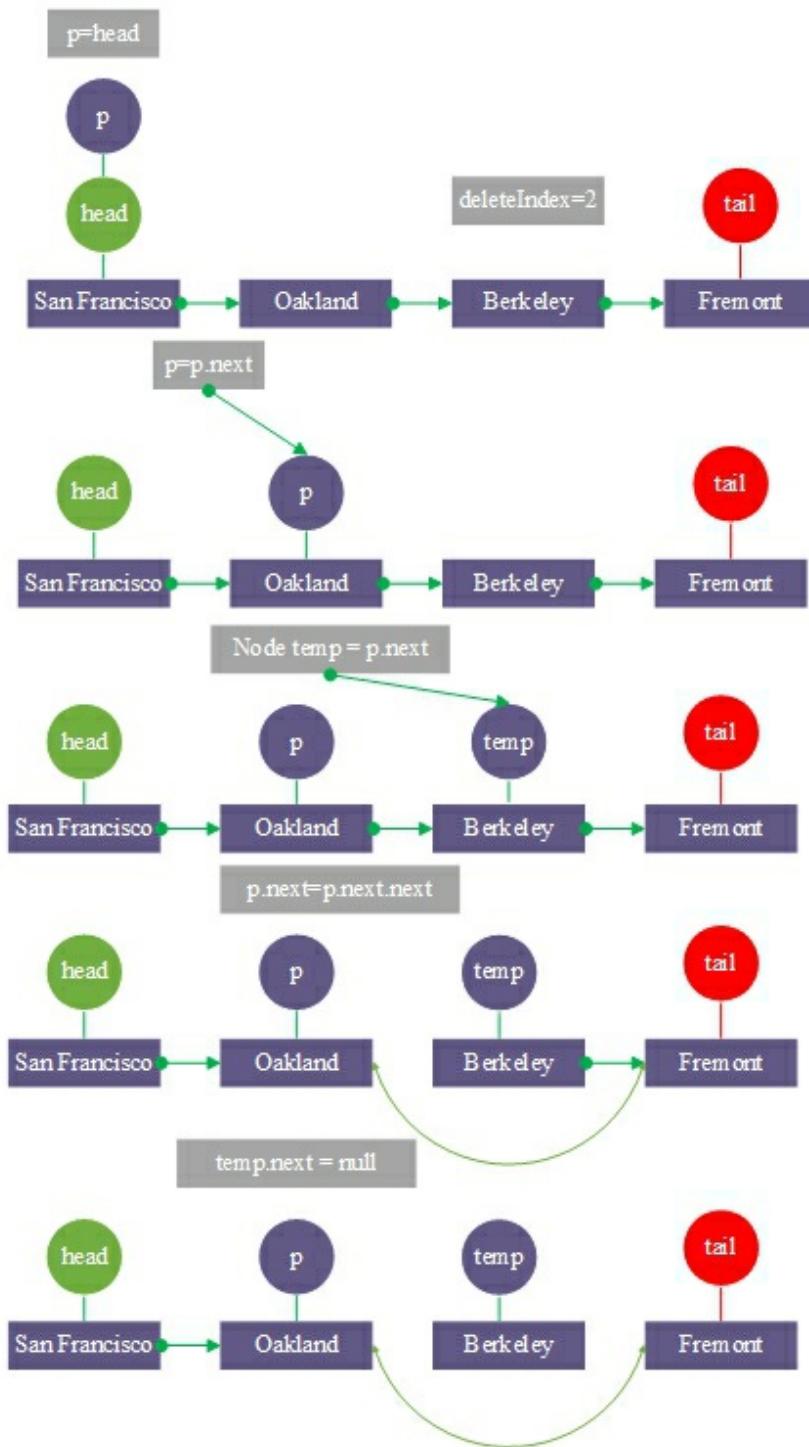
linkedList.print(head);
</script>

```

## Result:



#### 4. Delete the index=2 node.



## 1. Create a **TestUnidirectionalLinkedListDelete.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, next){
        this.data = data;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class LinkedList{
    init() {
        // the first node called head node
        this.head = new Node("San Francisco", null);

        var nodeOakland = new Node("Oakland", null);
        this.head.next = nodeOakland;

        var nodeBerkeley = new Node("Berkeley", null);
        nodeOakland.next = nodeBerkeley;

        // the last node called tail node
        this.tail = new Node("Fremont", null);
        nodeBerkeley.next = this.tail;
        return this.head;
    }

    remove(removePosition) {
        var p = this.head;
        var i = 0;
        // Move the node to the previous node position that was deleted
        while (p.next != null && i < removePosition - 1) {
            p = p.next;
            i++;
        }
    }
}
```

```

var temp = p.next;// Save the node you want to delete
p.next = p.next.next;// Previous node next points to next of
delete the node
    temp.next = null;
}

print(node) {
    var p = node;
    while (p != null) // From the beginning to the end
    {
        var data = p.getData();
        document.write(data + " -> ");
        p = p.next;
    }
    document.write("End<br><br>");
}
}

//////////////////testing////////////////

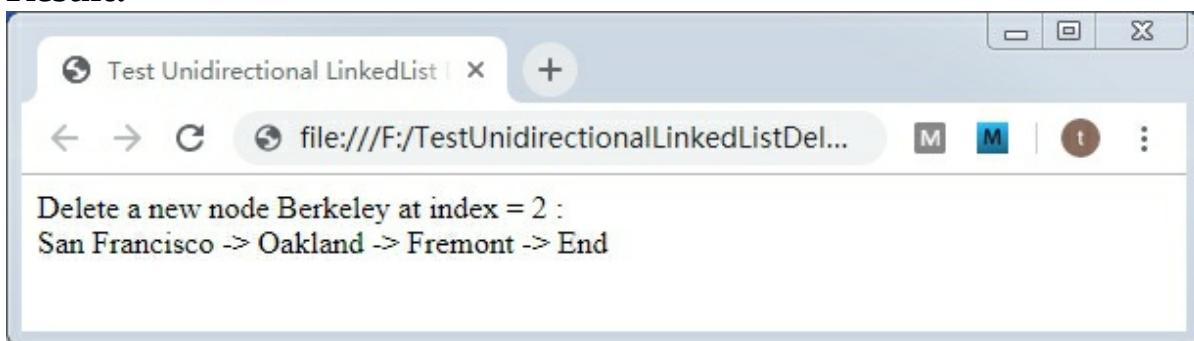
var linkedList = new LinkedList();
var head = linkedList.init();

document.write("Delete a new node Berkeley at index = 2 : <br>");
linkedList.remove(2);

linkedList.print(head);
</script>

```

## Result:



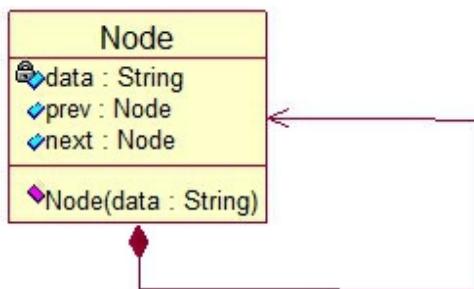
# Doubly Linked List

## Doubly Linked List:

It is a chained storage structure of a linear table. It is connected by nodes in two directions. Each node consists of data, pointing to the previous node and pointing to the next node.



## UML Diagram

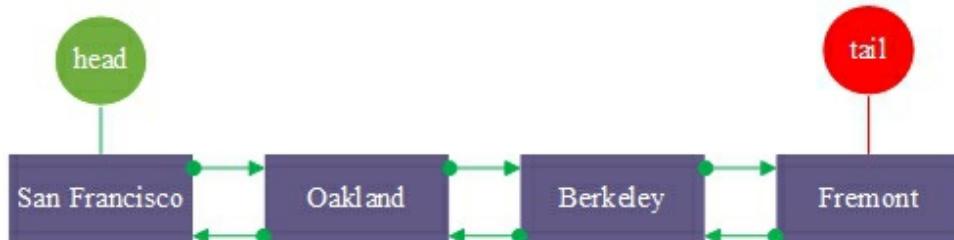


```
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}
```

## 1. Doubly Linked List initialization.

Example : Construct a San Francisco subway Doubly linked list



## 2. Create a **TestDoubleLink.html** with **Notepad**

```
<script type="text/javascript">
  class Node{
    constructor(data, prev, next){
      this.data = data;
      this.prev = prev;
      this.next = next;
    }

    getData(){
      return this.data;
    }
  }

  class DoubleLinkedList{
    init() {
      this.head = new Node("San Francisco");
      this.head.prev = null;
      this.head.next = null;

      var nodeOakland = new
      Node("Oakland");
      nodeOakland.prev = this.head;
      nodeOakland.next = null;
      this.head.next = nodeOakland;

      var nodeBerkeley = new
      Node("Berkeley");
      nodeBerkeley.prev = nodeOakland;
      nodeBerkeley.next = null;
      nodeOakland.next = nodeBerkeley;

      this.tail = new Node("Fremont");
      this.tail.prev = nodeBerkeley;
      this.tail.next = null;
      nodeBerkeley.next = this.tail;
      return this.head;
    }
  }
}
```

```

}

print(node) {
    var p = node;
    var end = null;
    while (p != null)
    {
        var data = p.getData();
        document.write(data + " -> ");
        end = p;
        p = p.next;
    }
    document.write("End <br><br>");

    p = end;
    while (p != null)
    {
        var data = p.getData();
        document.write(data + " -> ");
        p = p.prev;
    }
    document.write("Start<br><br>");
}
}

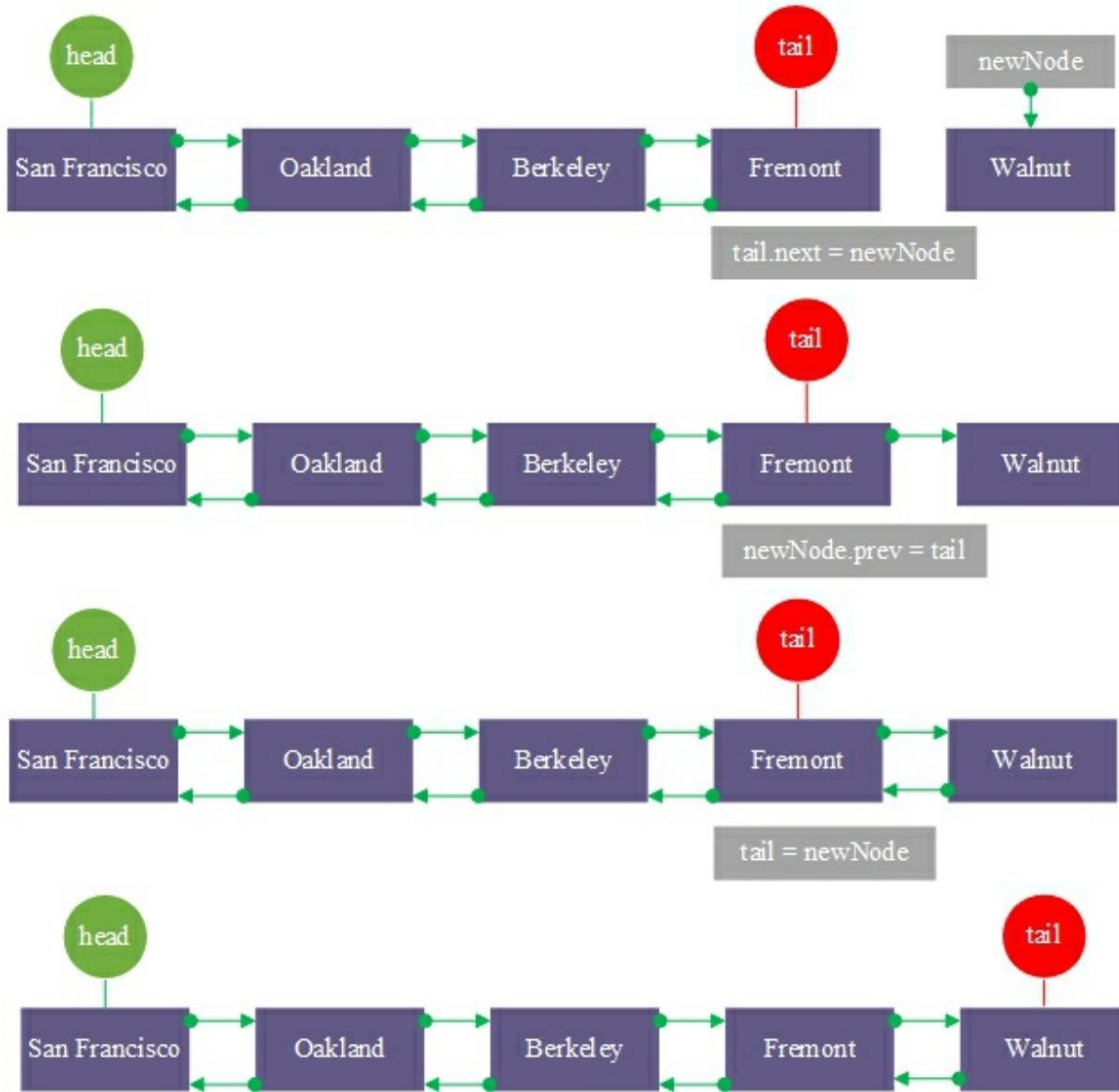
//////////////////testing/////////////////
var doubleLinkList = new DoubleLinkList();
var head = doubleLinkList.init();
doubleLinkList.print(head);
</script>

```

## Result:



### 3. add a node **Walnut** at the end of Fremont.



## Create a **TestDoubleLinkAdd.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class DoubleLinkedList{
    init() {
        this.head = new Node("San Francisco");
        this.head.prev = null;
        this.head.next = null;

        var nodeOakland = new
Node("Oakland");
        nodeOakland.prev = this.head;
        nodeOakland.next = null;
        this.head.next = nodeOakland;

        var nodeBerkeley = new
Node("Berkeley");
        nodeBerkeley.prev = nodeOakland;
        nodeBerkeley.next = null;
        nodeOakland.next = nodeBerkeley;

        this.tail = new Node("Fremont");
        this.tail.prev = nodeBerkeley;
        this.tail.next = null;
        nodeBerkeley.next = this.tail;
        return this.head;
    }
}
```

```

}

add(newNode) {
this.tail.next = newNode;
newNode.prev = this.tail;
this.tail = newNode;
}

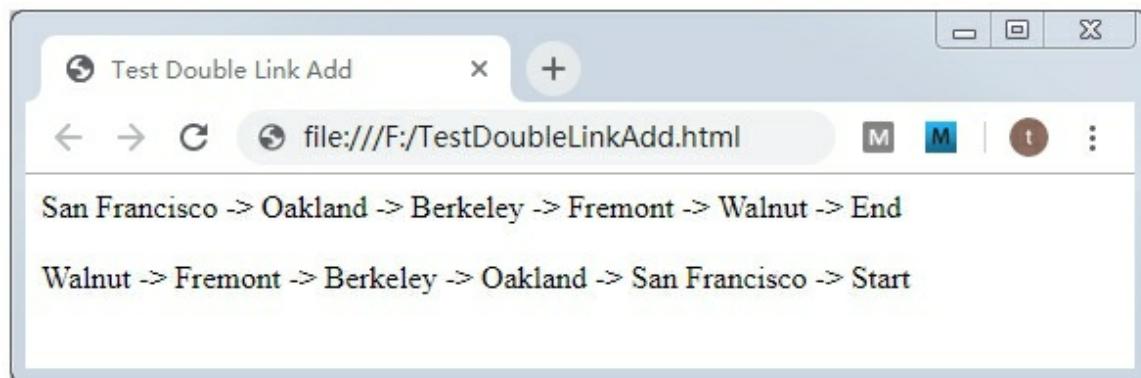
print(node) {
var p = node;
var end = null;
while (p != null)
{
    var data = p.getData();
    document.write(data + " -> ");
    end = p;
    p = p.next;
}
document.write("End <br><br>");

p = end;
while (p != null)
{
    var data = p.getData();
    document.write(data + " -> ");
    p = p.prev;
}
document.write("Start<br><br>");
}

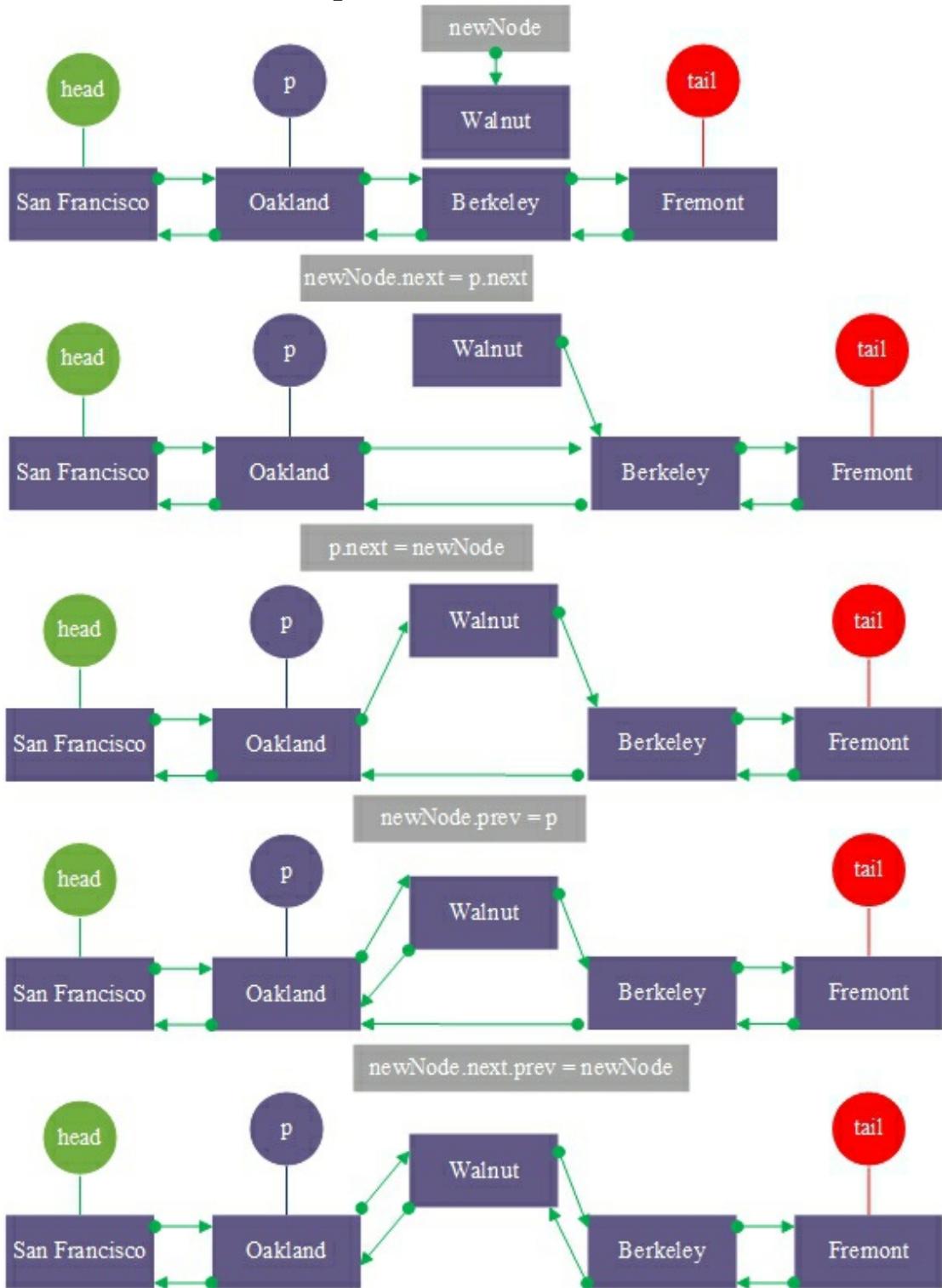
//////////testing/////////
var doubleLinkedList = new DoubleLinkedList();
var head = doubleLinkedList.init();
doubleLinkedList.add(new Node("Walnut"));
doubleLinkedList.print(head);
</script>

```

**Result:**



### 3. Insert a node **Walnut** in position 2.



## Create a **TestDoubleLinkInsert.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class DoubleLinkedList{

    init() {
        this.head = new Node("San Francisco");
        this.head.prev = null;
        this.head.next = null;

        var nodeOakland = new Node("Oakland");
        nodeOakland.prev = this.head;
        nodeOakland.next = null;
        this.head.next = nodeOakland;

        var nodeBerkeley = new Node("Berkeley");
        nodeBerkeley.prev = nodeOakland;
        nodeBerkeley.next = null;
        nodeOakland.next = nodeBerkeley;

        this.tail = new Node("Fremont");
        this.tail.prev = nodeBerkeley;
        this.tail.next = null;
        nodeBerkeley.next = this.tail;
        return this.head;
    }
}
```

```
insert(insertPosition, newNode) {
    var p = this.head;
    var i = 0;
    // Move the node to the insertion position
    while (p.next != null && i < insertPosition-1) {
        p = p.next;
        i++;
    }

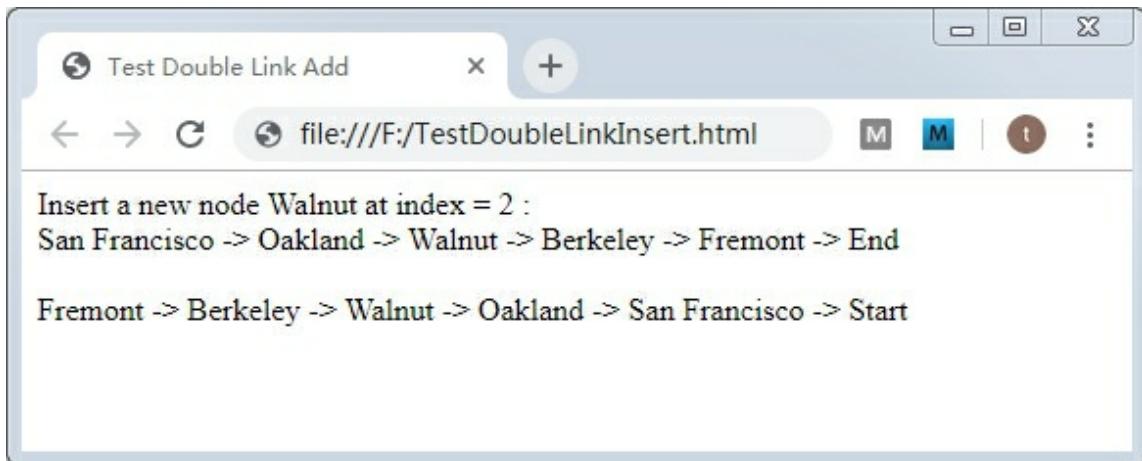
    newNode.next = p.next;
    p.next = newNode;
    newNode.prev = p;
    newNode.next.prev = newNode;
}

print(node) {
    var p = node;
    var end = null;
    while (p != null)
    {
        var data = p.getData();
        document.write(data + " -> ");
        end = p;
        p = p.next;
    }
    document.write("End <br><br>");

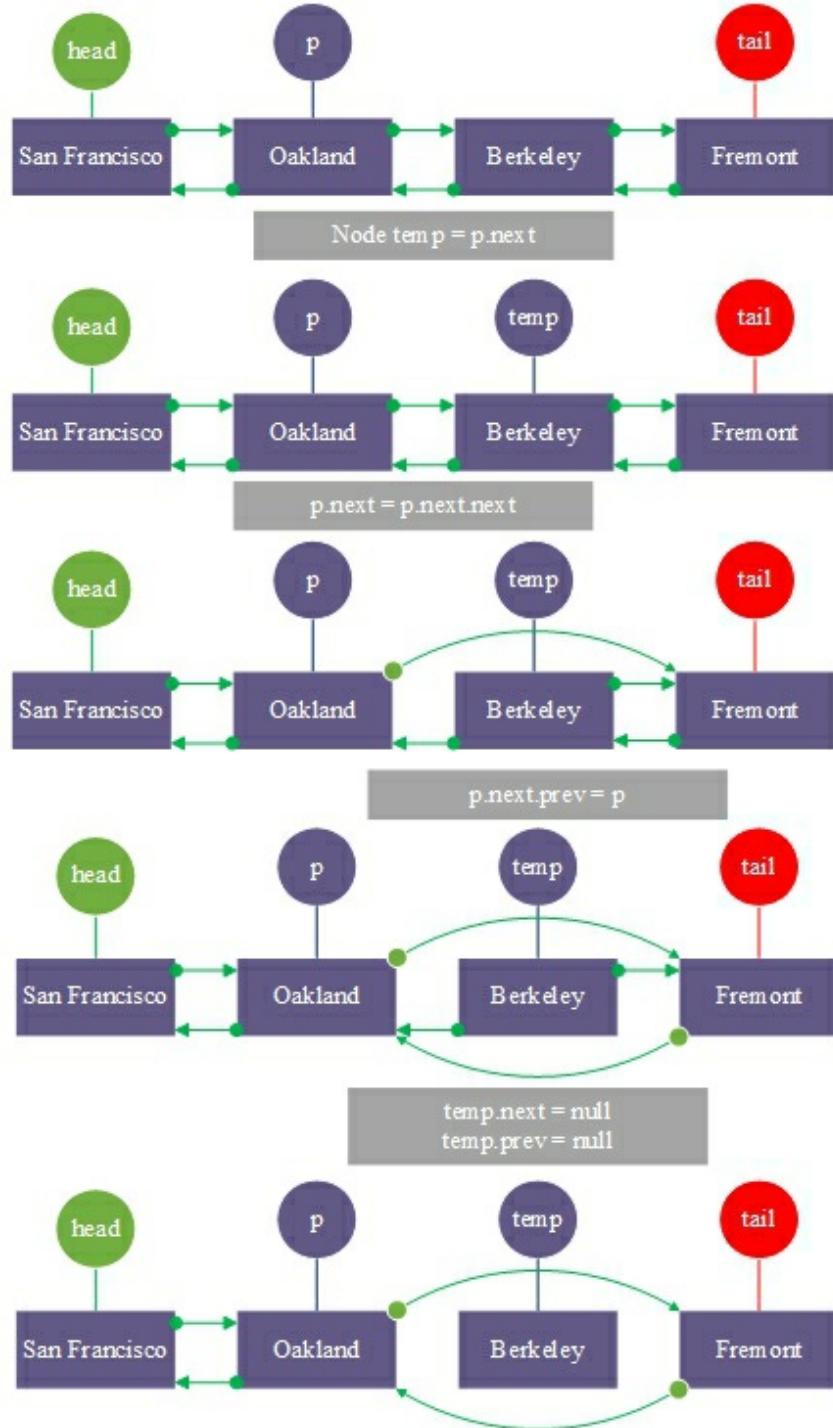
    p = end;
    while (p != null)
    {
        var data = p.getData();
        document.write(data + " -> ");
        p = p.prev;
    }
    document.write("Start<br><br>");
}
}
```

```
//////////////////testing////////////////  
var doubleLinkedList = new DoubleLinkedList();  
var head = doubleLinkedList.init();  
  
document.write("Insert a new node Walnut at index = 2 : <br>");  
doubleLinkedList.insert(2,new Node("Walnut"));  
  
doubleLinkedList.print(head);  
</script>
```

## Result:



#### 4. Delete the index=2 node.



## Create a **TestDoubleLinkDelete.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class DoubleLinkedList{

    init() {
        this.head = new Node("San Francisco");
        this.head.prev = null;
        this.head.next = null;

        var nodeOakland = new Node("Oakland");
        nodeOakland.prev = this.head;
        nodeOakland.next = null;
        this.head.next = nodeOakland;

        var nodeBerkeley = new Node("Berkeley");
        nodeBerkeley.prev = nodeOakland;
        nodeBerkeley.next = null;
        nodeOakland.next = nodeBerkeley;

        this.tail = new Node("Fremont");
        this.tail.prev = nodeBerkeley;
        this.tail.next = null;
        nodeBerkeley.next = this.tail;
        return this.head;
    }
}
```

```

remove(removePosition) {
    var p = this.head;
    var i = 0;
    // Move the node to the previous node that was deleted
    while (p.next != null && i < removePosition - 1) {
        p = p.next;
        i++;
    }

    var temp = p.next;// Save the node you want to delete
    p.next = p.next.next;
    p.next.prev = p;
    temp.next = null;// Set the delete node next to null
    temp.prev = null;// Set the delete node prev to null
}

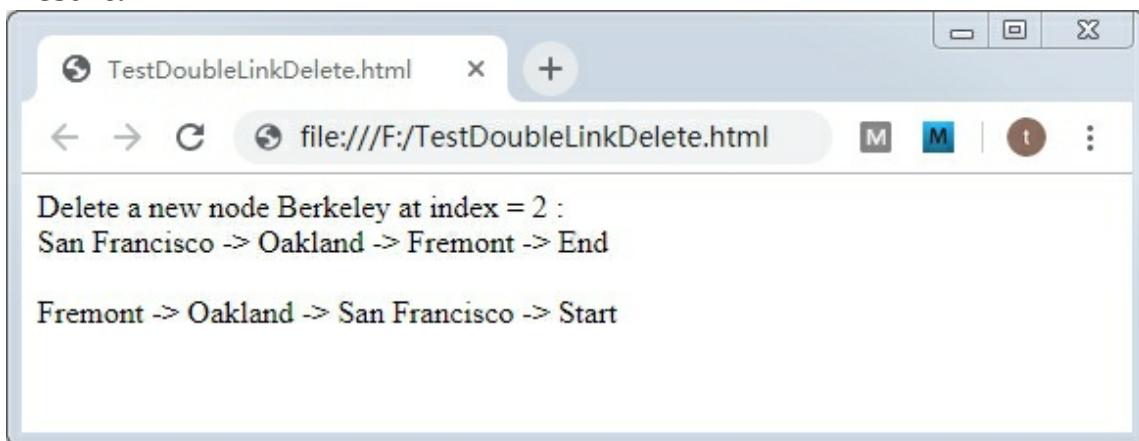
print(node) {
    var p = node;
    var end = null;
    while (p != null)
    {
        var data = p.getData();
        document.write(data + " -> ");
        end = p;
        p = p.next;
    }
    document.write("End<br><br>");

    p = end;
    while (p != null)
    {
        var data = p.getData();
        document.write(data + " -> ");
        p = p.prev;
    }
    document.write("Start<br><br>");
}

```

```
//////////////////testing////////////////  
var doubleLinkedList = new DoubleLinkedList();  
var head = doubleLinkedList.init();  
  
document.write("Delete a new node Berkeley at index = 2 : <br>");  
doubleLinkedList.remove(2);  
  
doubleLinkedList.print(head);  
</script>
```

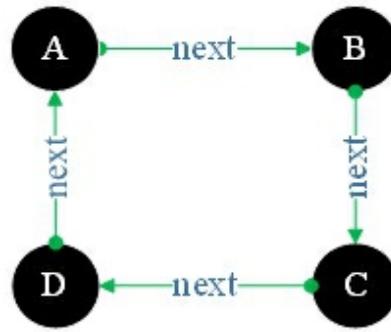
## Result:



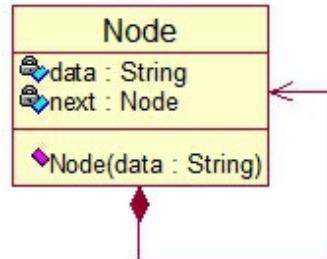
# One-way Circular LinkedList

## One-way Circular List:

It is a chain storage structure of a linear table, which is connected to form a ring, and each node is composed of data and a pointer to next.



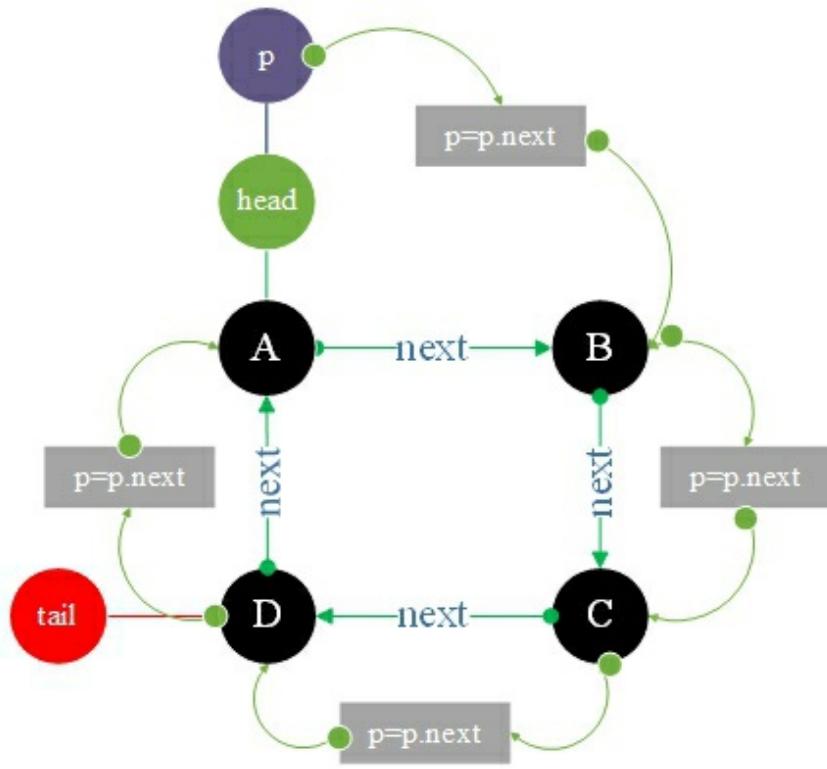
## UML Diagram



```
class Node{
    constructor(data, next){
        this.data = data;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}
```

## 1. One-way Circular Linked List **initialization and traversal output.**



## Create a **TestSingleCircleLink.html** with **Notepad**

```
<script type="text/javascript">
  class Node{
    constructor(data, next){
      this.data = data;
      this.next = next;
    }

    getData(){
      return this.data;
    }
  }

  class SingleCircleLink{
    init() {
      // the first node called head node
      this.head = new Node("A");
      this.head.next = null;

      var nodeB = new Node("B");
      nodeB.next = null;
      this.head.next = nodeB;

      var nodeC = new Node("C");
      nodeC.next = null;
      nodeB.next = nodeC;

      // the last node called tail node
      this.tail = new Node("D");
      this.tail.next = this.head;
      nodeC.next = this.tail;
    }
  }
}
```

```

print() {
    var p = this.head;
    do{
        var data = p.getData();
        document.write(data + " -> ");
        p = p.next;
    }while(p != this.head);

    var data = p.getData();
    document.write(data + "<br><br>");
}
}

//////////////////testing////////////////

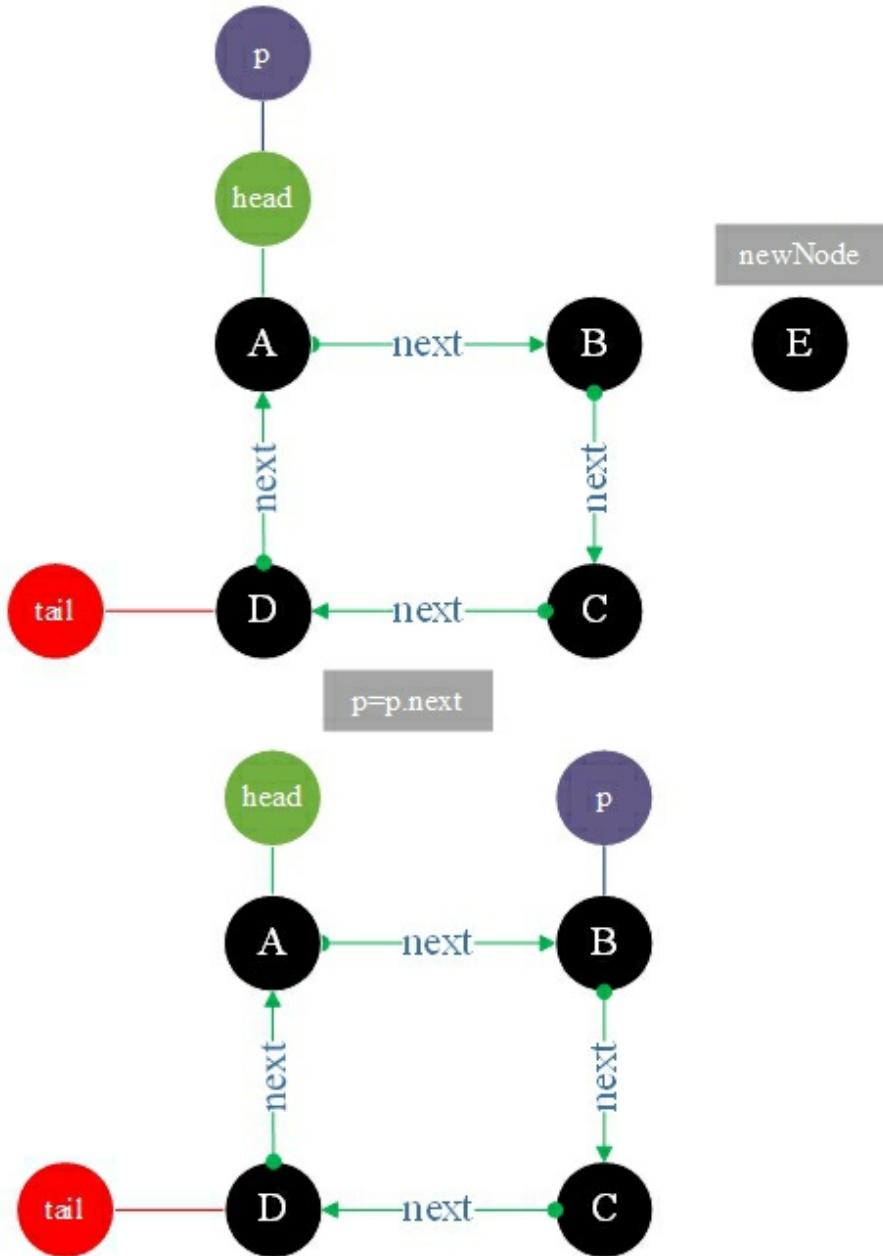
var singleCircleLink = new SingleCircleLink();
var head = singleCircleLink.init();
singleCircleLink.print(head);
</script>

```

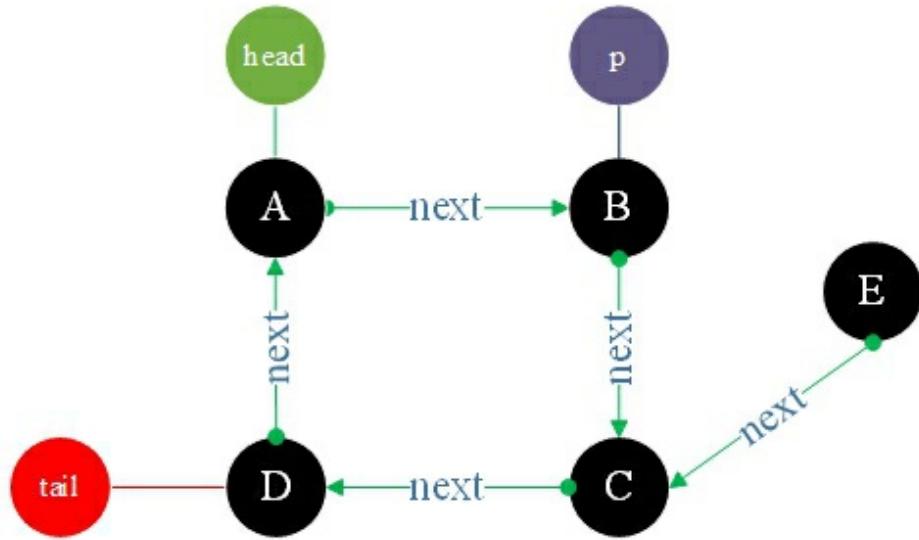
## Result:



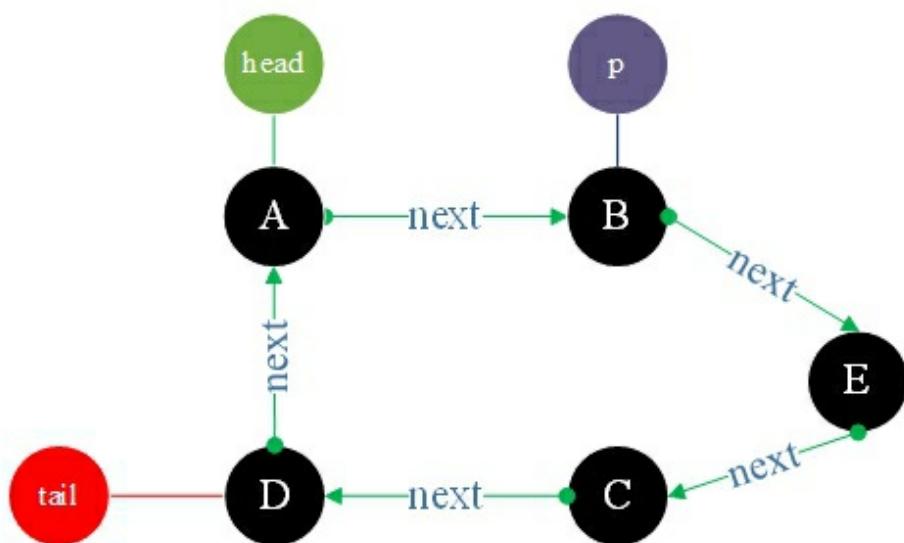
### 3. Insert a node E in position 2.



```
newNode.next = p.next
```



```
p.next = newNode
```



## Create a **TestSingleCircleLinkInsert.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, next){
        this.data = data;
        this.next = next;
    }
    getData(){
        return this.data;
    }
}

class SingleCircleLink{
    init() {
        // the first node called head node
        this.head = new Node("A");
        this.head.next = null;

        var nodeB = new Node("B");
        nodeB.next = null;
        this.head.next = nodeB;

        var nodeC = new Node("C");
        nodeC.next = null;
        nodeB.next = nodeC;

        // the last node called tail node
        this.tail = new Node("D");
        this.tail.next = this.head;
        nodeC.next = this.tail;
    }

    insert(insertPosition, newNode) {
        var p = this.head;
        var i = 0;
        while (p.next != null && i < insertPosition - 1) {
            p = p.next;
        }
        p.next = newNode;
        newNode.next = this.tail;
        if (insertPosition === 1) {
            this.tail = newNode;
        }
    }
}
```

```

        i++;
    }
    newNode.next = p.next;
    p.next = newNode;
}

print() {
    var p = this.head;
    do{
        var data = p.getData();
        document.write(data + " -> ");
        p = p.next;
    }while(p != this.head);

    var data = p.getData();
    document.write(data + "<br><br>");
}
}

//////////////////testing////////////////

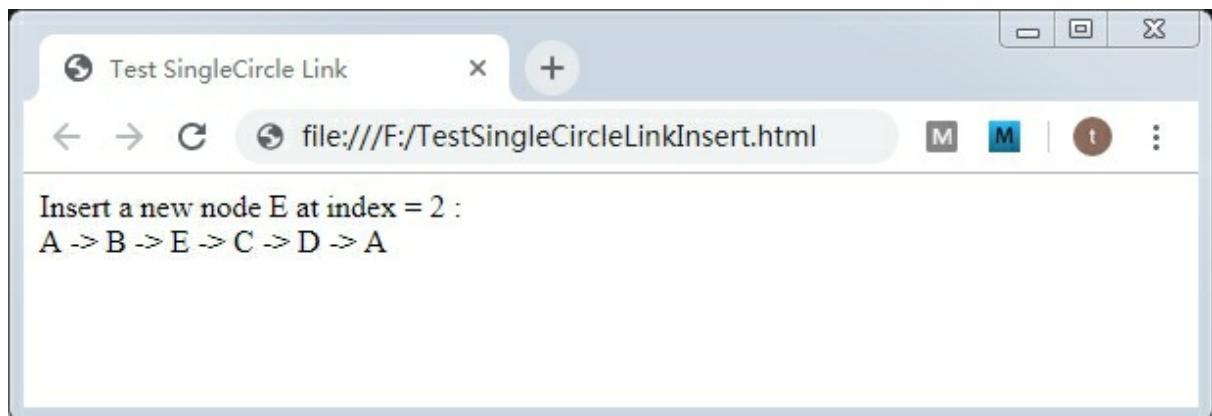
var singleCircleLink = new SingleCircleLink();
var head = singleCircleLink.init();

document.write("Insert a new node E at index = 2 : <br>");
singleCircleLink.insert(2,new Node("E"));

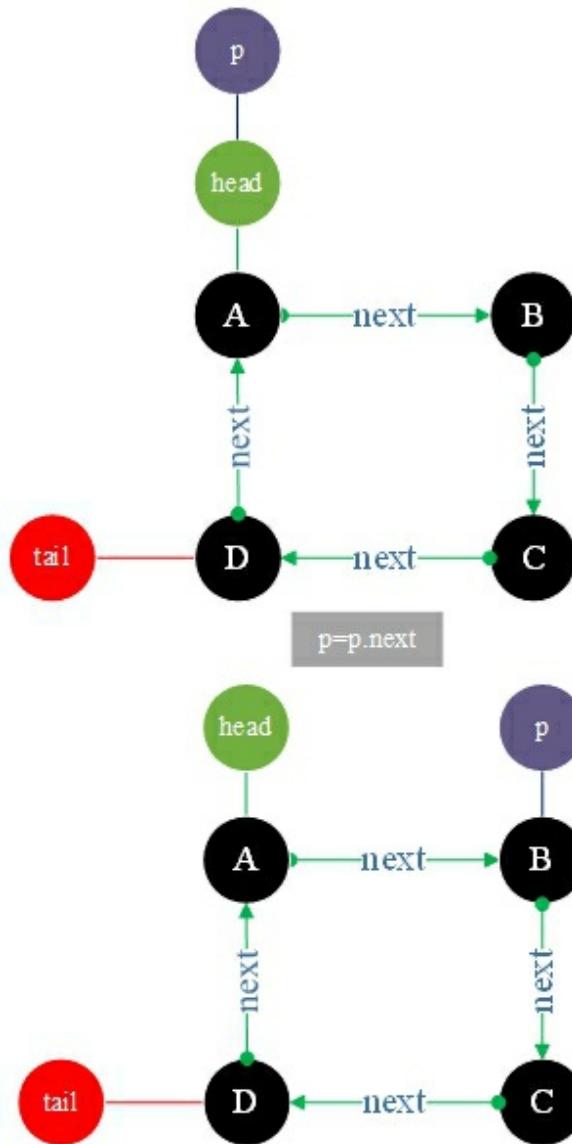
singleCircleLink.print(head);
</script>

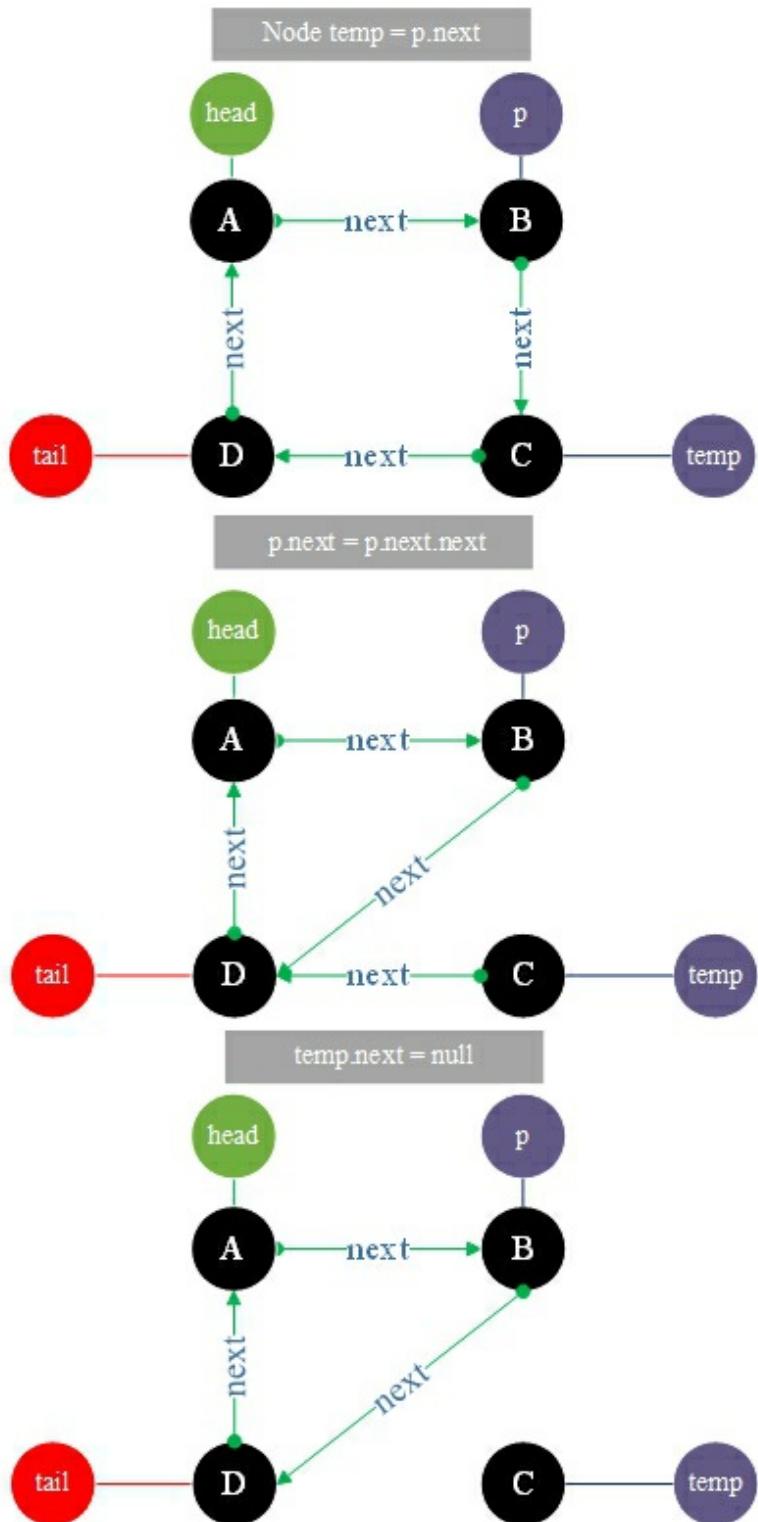
```

**Result:**



#### 4. Delete the **index=2** node.





## Create a **TestSingleCircleLinkDelete.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, next){
        this.data = data;
        this.next = next;
    }
    getData(){
        return this.data;
    }
}

class SingleCircleLink{
    init() {
        this.head = new Node("A");
        this.head.next = null;

        var nodeB = new Node("B");
        nodeB.next = null;
        this.head.next = nodeB;

        var nodeC = new Node("C");
        nodeC.next = null;
        nodeB.next = nodeC;

        this.tail = new Node("D");
        this.tail.next = this.head;
        nodeC.next = this.tail;
    }

    remove(removePosition) {
        var p = this.head;
        var i = 0;
        while (p.next != null && i < removePosition - 1) {
            p = p.next;
            i++;
        }
    }
}
```

```

var temp = p.next;
p.next = p.next.next;
temp.next = null;
}

print() {
    var p = this.head;
    do{
        var data = p.getData();
        document.write(data + " -> ");
        p = p.next;
    }while(p != this.head);

    var data = p.getData();
    document.write(data + "<br><br>");
}
}

//////////testing///////////
var singleCircleLink = new SingleCircleLink();
singleCircleLink.init();

document.write("Delete a new node C at index = 2 : <br>");
singleCircleLink.remove(2);

singleCircleLink.print();
</script>

```

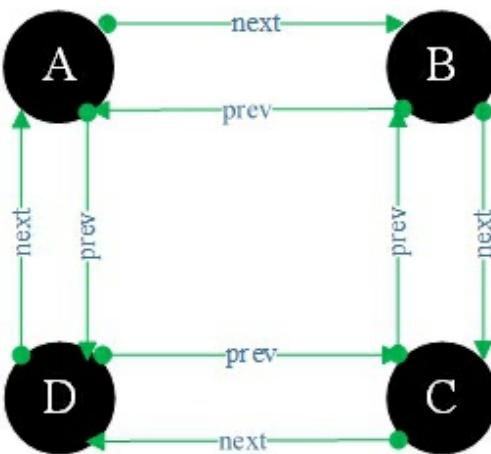
## Result:



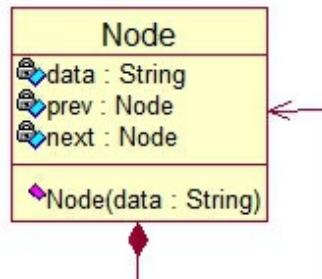
# Two-way Circular LinkedList

## Two-way Circular List:

It is a chain storage structure of a linear table. The nodes are connected in series by two directions, and is connected to form a ring. Each node is composed of **data**, pointing to the previous node **prev** and pointing to the next node **next**.



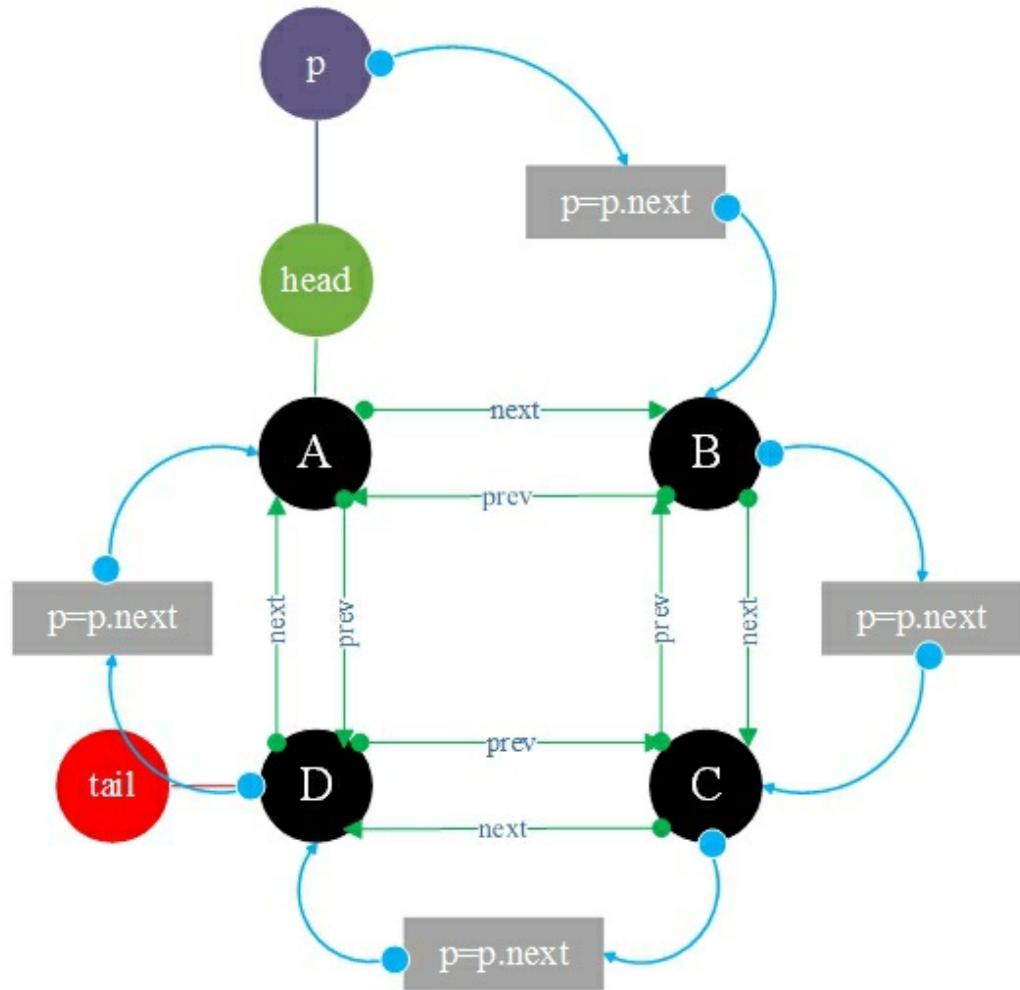
## UML Diagram

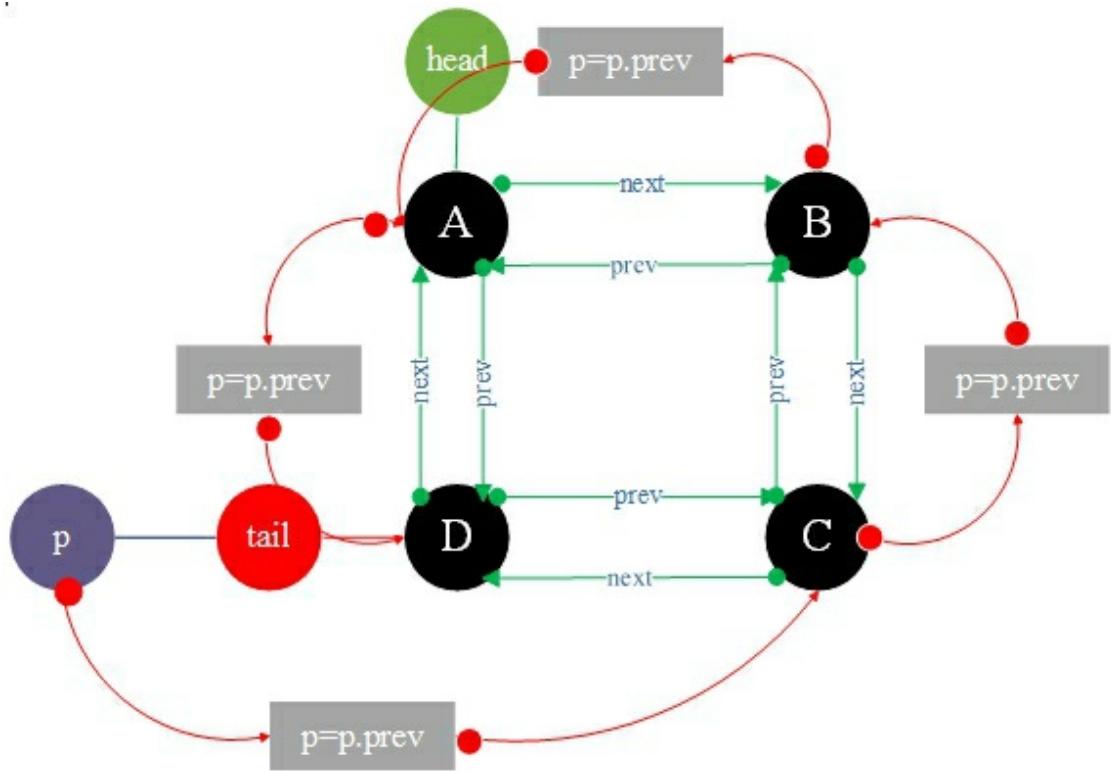


```
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}
```

## 1. Two-way Circular Linked List **initialization** and **traversal output**.





## Create a **TestDoubleCircleLink.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class DoubleCircleLink{
    init() {
        // the first node called head node
        this.head = new Node("A");
        this.head.next = null;
        this.head.prev = null;

        var nodeB = new Node("B");
        nodeB.next = null;
        nodeB.prev = this.head;
        this.head.next = nodeB;

        var nodeC = new Node("C");
        nodeC.next = null;
        nodeC.prev = nodeB;
        nodeB.next = nodeC;

        // the last node called tail node
        this.tail = new Node("D");
        this.tail.next = this.head;
        this.tail.prev = nodeC;
        nodeC.next = this.tail;
        this.head.prev = this.tail;
    }
}
```

```
}
```

```
print() {
    var p = this.head;
    do {
        var data = p.getData();
        document.write(data + " -> ");
        p = p.next;
    } while (p != this.head);

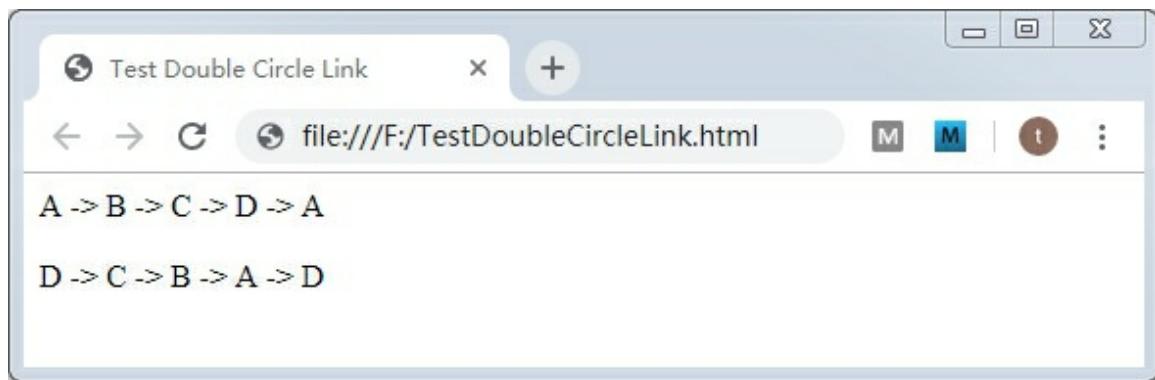
    var data = p.getData();
    document.write(data + "<br><br>");

    p = this.tail;
    do {
        data = p.getData();
        document.write(data + " -> ");
        p = p.prev;
    } while (p != this.tail);

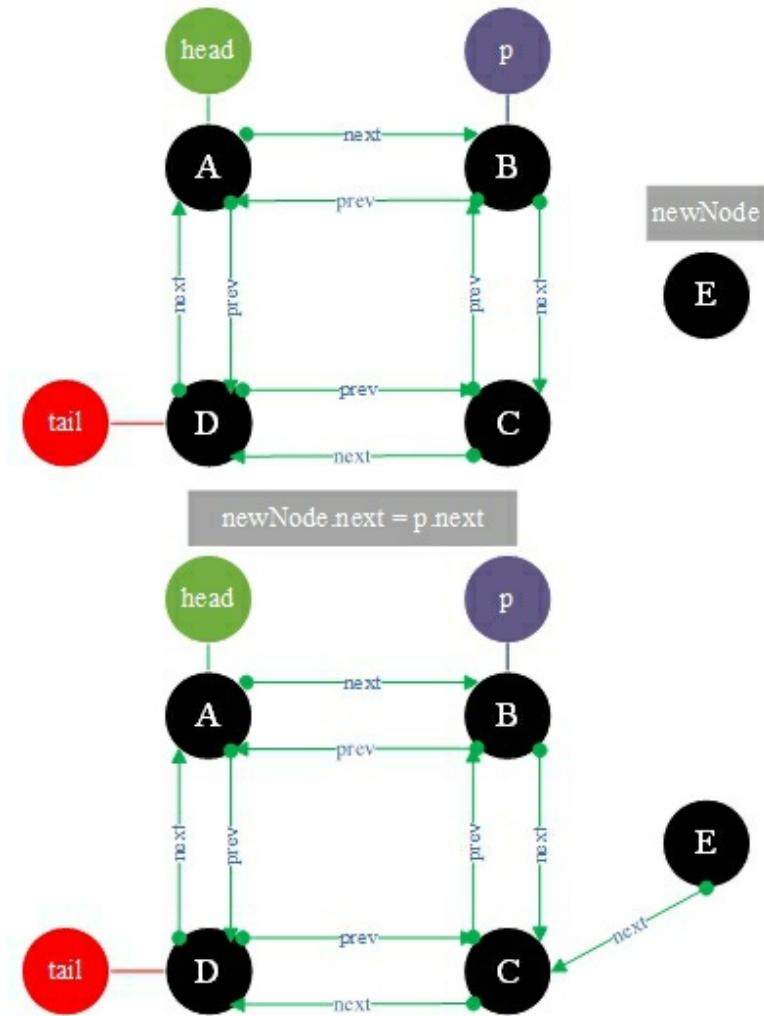
    data = p.getData();
    document.write(data + "<br><br>");
}
}

//////////////////testing/////////////////
var doubleCircleLink = new DoubleCircleLink();
doubleCircleLink.init();
doubleCircleLink.print();
</script>
```

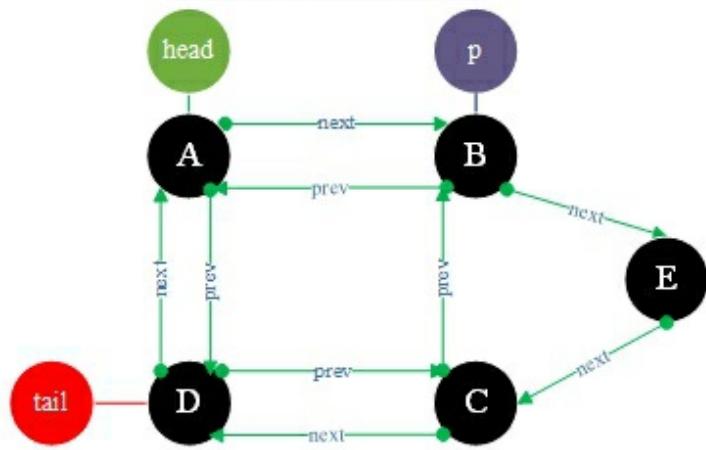
**Result:**



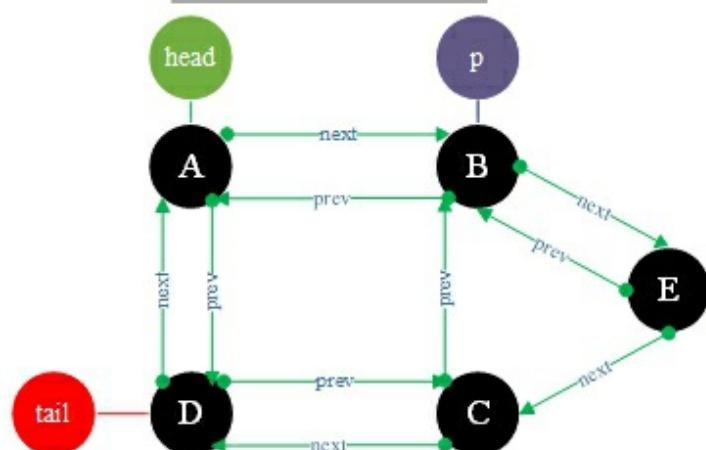
### 3. Insert a node E in position 2.



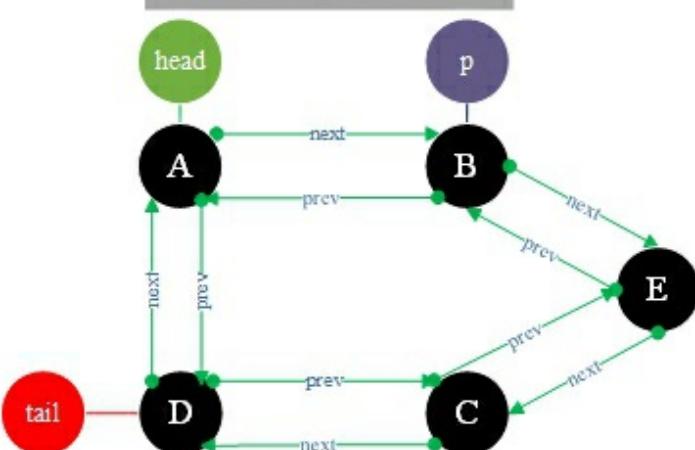
`p.next = newNode`



`newNode.prev = p`



`newNode.next.prev = newNode`



## Create a **TestDoubleCircleLinkInsert.html** with Notepad

```
<script type="text/javascript">
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class DoubleCircleLink{
    init() {
        // the first node called head node
        this.head = new Node("A");
        this.head.next = null;
        this.head.prev = null;

        var nodeB = new Node("B");
        nodeB.next = null;
        nodeB.prev = this.head;
        this.head.next = nodeB;

        var nodeC = new Node("C");
        nodeC.next = null;
        nodeC.prev = nodeB;
        nodeB.next = nodeC;

        // the last node called tail node
        this.tail = new Node("D");
        this.tail.next = this.head;
        this.tail.prev = nodeC;
        nodeC.next = this.tail;
        this.head.prev = this.tail;
    }
}
```

```
}
```

```
insert(insertPosition, newNode) {  
    var p = this.head;  
    var i = 0;  
    //Move the node to the insertion position  
    while (p.next != null && i < insertPosition - 1) {  
        p = p.next;  
        i++;  
    }  
  
    newNode.next = p.next;  
    p.next = newNode;  
    newNode.prev = p;  
    newNode.next.prev = newNode;  
}  
  
print() {  
    var p = this.head;  
    do {  
        var data = p.getData();  
        document.write(data + " -> ");  
        p = p.next;  
    } while (p != this.head);  
  
    var data = p.getData();  
    document.write(data + "<br><br>");  
  
    p = this.tail;  
    do {  
        data = p.getData();  
        document.write(data + " -> ");  
        p = p.prev;  
    } while (p != this.tail);  
  
    data = p.getData();
```

```
        document.write(data + "<br><br>");
    }
}

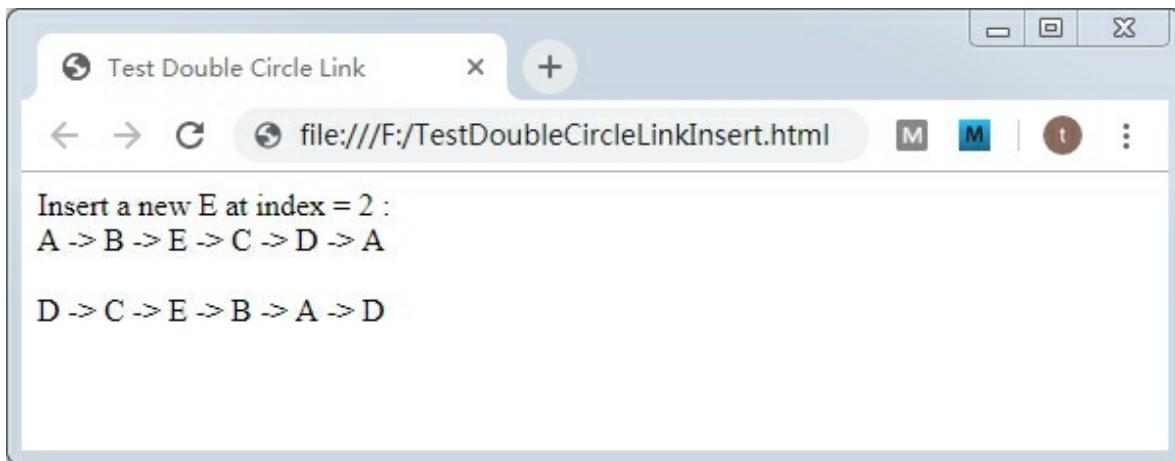
//////////////////testing////////////////

var doubleCircleLink = new DoubleCircleLink();
doubleCircleLink.init();

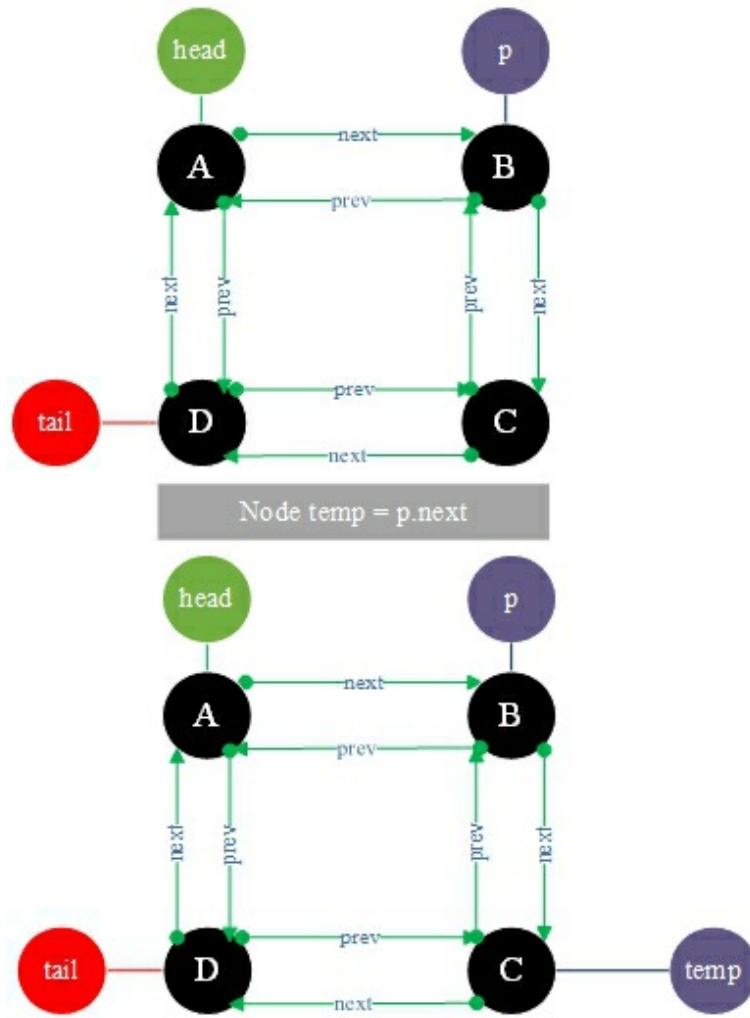
document.write("Insert a new E at index = 2 : <br>");
doubleCircleLink.insert(2,new Node("E"));

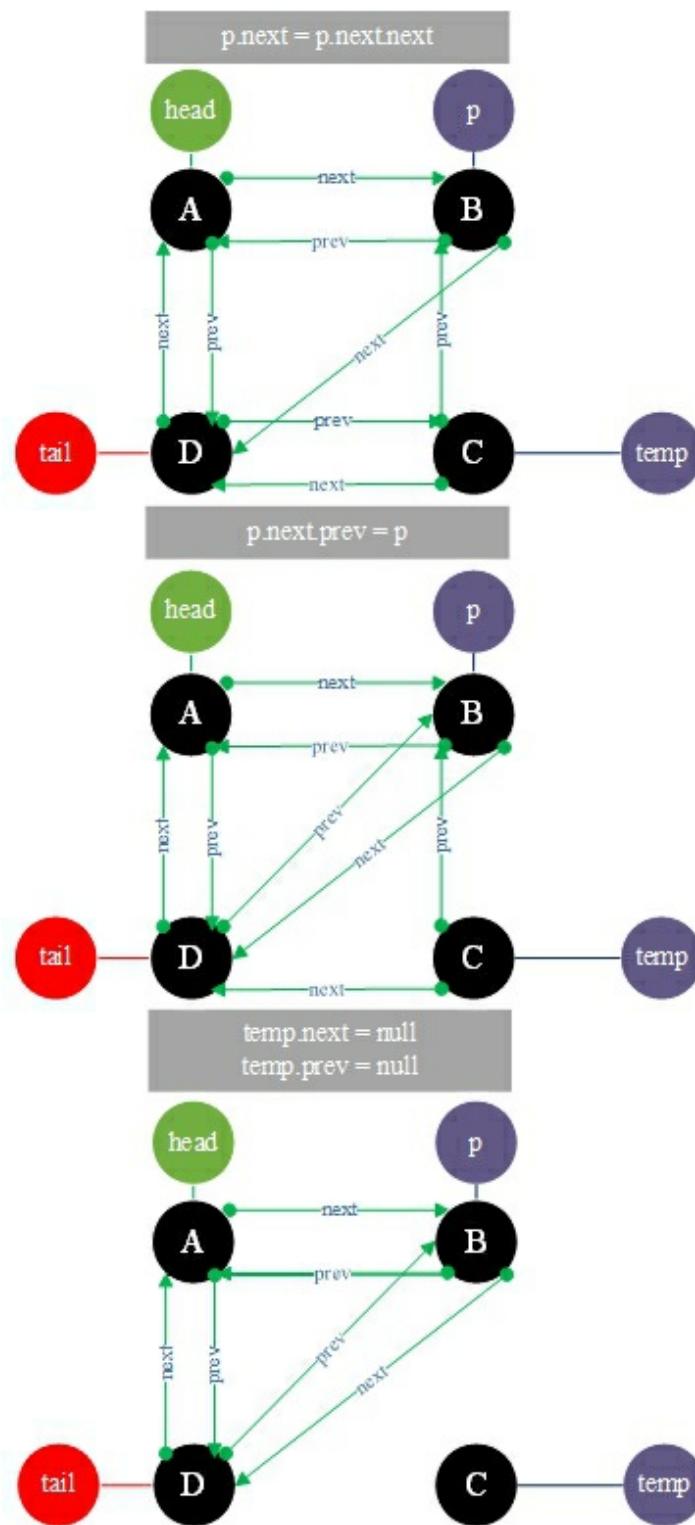
doubleCircleLink.print();
</script>
```

## Result:



#### 4. Delete the index=2 node.





## Create a **TestDoubleCircleLinkDelete.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}

class DoubleCircleLink{
    init() {
        // the first node called head node
        this.head = new Node("A");
        this.head.next = null;
        this.head.prev = null;

        var nodeB = new Node("B");
        nodeB.next = null;
        nodeB.prev = this.head;
        this.head.next = nodeB;

        var nodeC = new Node("C");
        nodeC.next = null;
        nodeC.prev = nodeB;
        nodeB.next = nodeC;

        // the last node called tail node
        this.tail = new Node("D");
        this.tail.next = this.head;
        this.tail.prev = nodeC;
        nodeC.next = this.tail;
        this.head.prev = this.tail;
    }
}
```

```
}
```

```
remove(removePosition) {
    var p = this.head;
    var i = 0;
    while (p.next != null && i < removePosition - 1) {
        p = p.next;
        i++;
    }

    var temp = p.next;
    p.next = p.next.next;
    p.next.prev = p;
    temp.next = null;//Set the delete node next to null
    temp.prev = null;// Set the delete node prev to null
}

print() {
    var p = this.head;
    do {
        var data = p.getData();
        document.write(data + " -> ");
        p = p.next;
    } while (p != this.head);

    var data = p.getData();
    document.write(data + "<br><br>");

    p = this.tail;
    do {
        data = p.getData();
        document.write(data + " -> ");
        p = p.prev;
    } while (p != this.tail);

    data = p.getData();
```

```
        document.write(data + "<br><br>");
    }
}

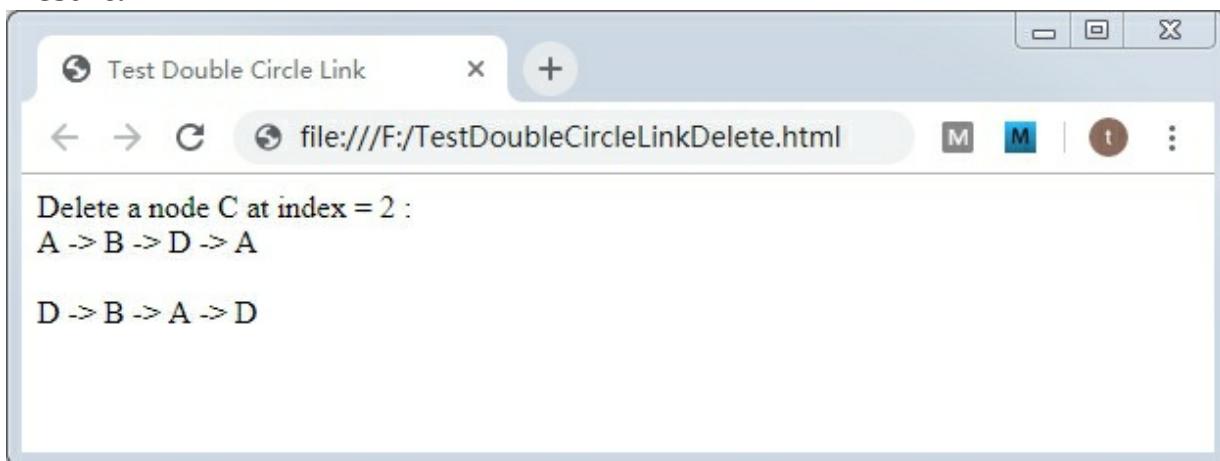
//////////////////testing////////////////

var doubleCircleLink = new DoubleCircleLink();
doubleCircleLink.init();

document.write("Delete a node C at index = 2 : <br>");
doubleCircleLink.remove(2);

doubleCircleLink.print();
</script>
```

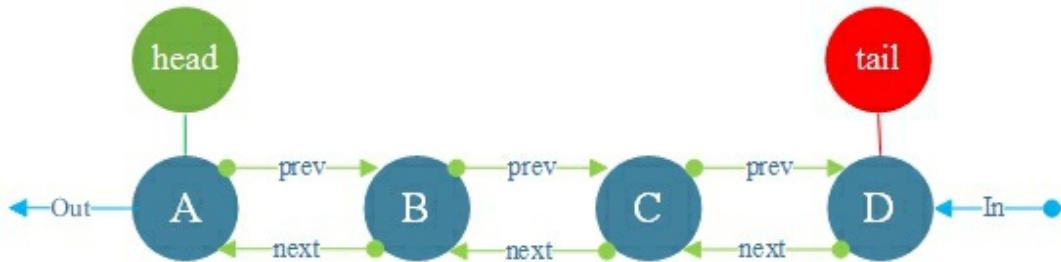
### Result:



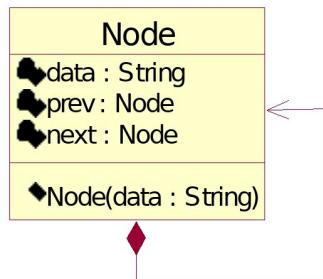
# Queue

## Queue:

FIFO (First In First Out) sequence.



## UML Diagram



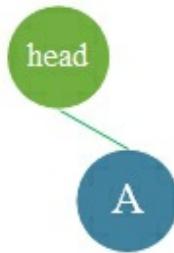
```
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }

    getData(){
        return this.data;
    }
}
```

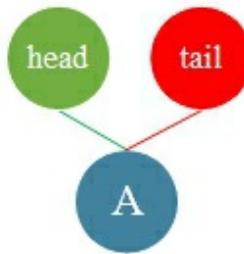
## 1. Queue **initialization** and traversal output.

### Initialization Insert A

```
head = new Node( "A" );
```

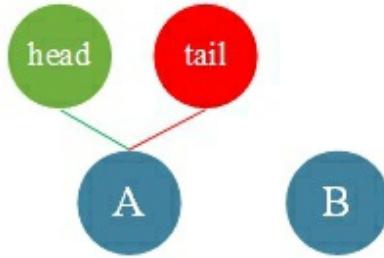


```
tail = head;
```

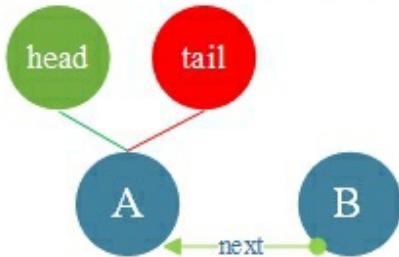


## Initialization Insert B

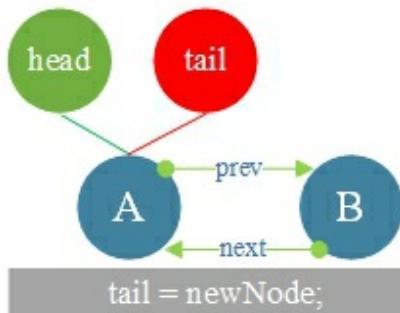
```
newNode = new Node( "B" );
```



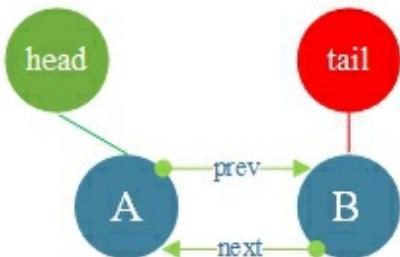
```
newNode.next = tail;
```



```
tail.prev = newNode;
```

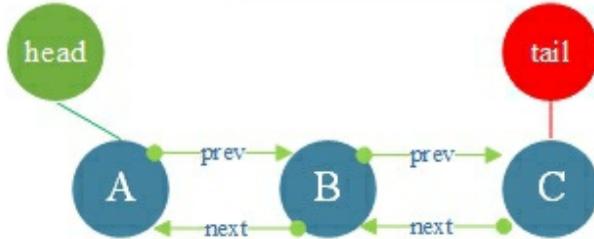
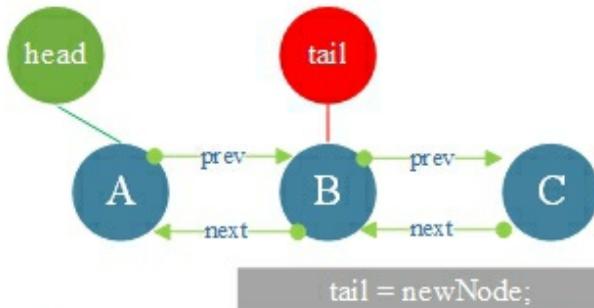
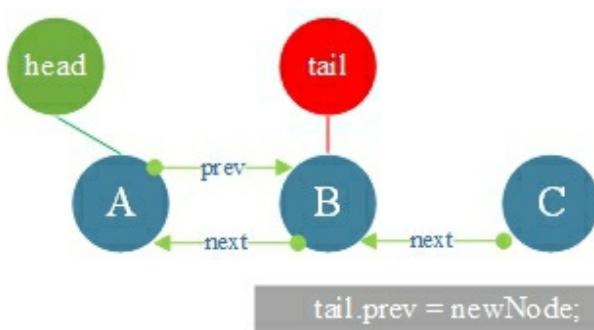
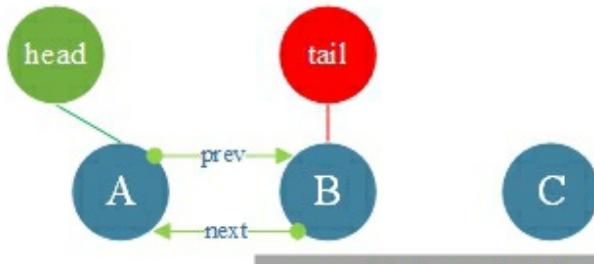


```
tail = newNode;
```



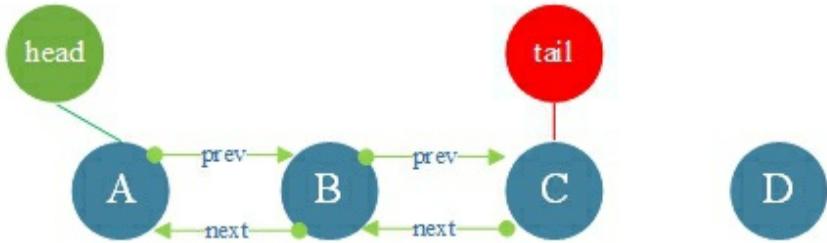
## Initialization Insert C

```
newNode = new Node( "C" );
```

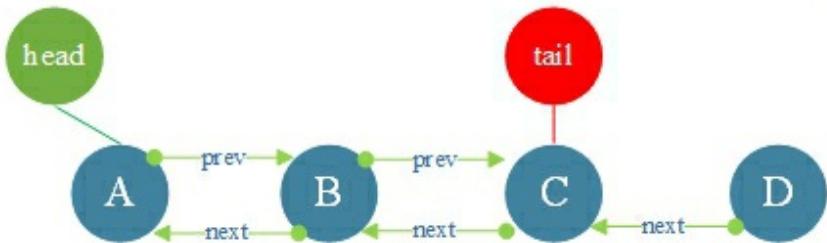


## Initialization Insert D

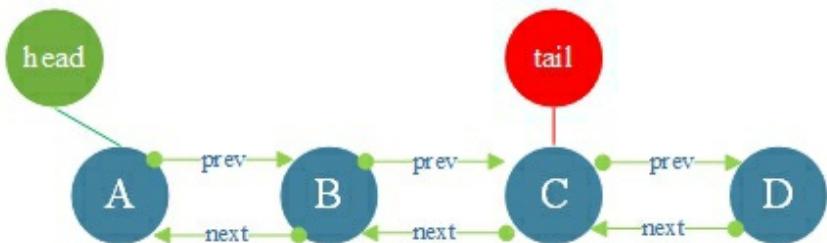
```
newNode = new Node( "D" );
```



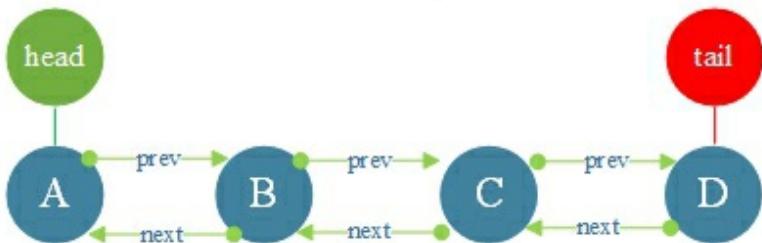
```
newNode.next = tail;
```



```
tail.prev = newNode;
```



```
tail = newNode;
```



## Create a **TestQueue.html** with **Notepad**

```
<script type="text/javascript">
class Node{
    constructor(data, prev, next){
        this.data = data;
        this.prev = prev;
        this.next = next;
    }
    getData(){
        return this.data;
    }
}

class Queue{
    constructor(){
        this.head = null;
        this.tail = null;
        this.size = 0;
    }

    offer(element) {
        if (this.head == null) {
            this.head = new Node(element);
            this.tail = this.head;
        } else {
            var newNode = new
Node(element);
            newNode.next = this.tail;
            this.tail.prev = newNode;
            this.tail = newNode;
        }
        this.size++;
    }

    poll() {
        var p = this.head;
        if (p == null) {
            return null;
        }
        this.head = p.next;
        if (this.head != null)
            this.head.prev = null;
        this.size--;
        return p.data;
    }
}
```

```

    }
    this.head = this.head.prev;
    p.next = null;
    p.prev = null;
    this.size--;
    return p;
}

size() {
return this.size;
}
}

//////////////testing///////////

```

**function** print(queue) {  
 document.write("Head ");  
**var** node = **null**;  
**while** ((node = queue.poll())!=**null**) {  
 document.write(node.getData() + " <-"  
 );  
 }  
 document.write("Tail <br>");  
}  
  
**var** queue = **new** Queue();  
queue.offer("A");  
queue.offer("B");  
queue.offer("C");  
queue.offer("D");  
  
print(queue);  
</script>

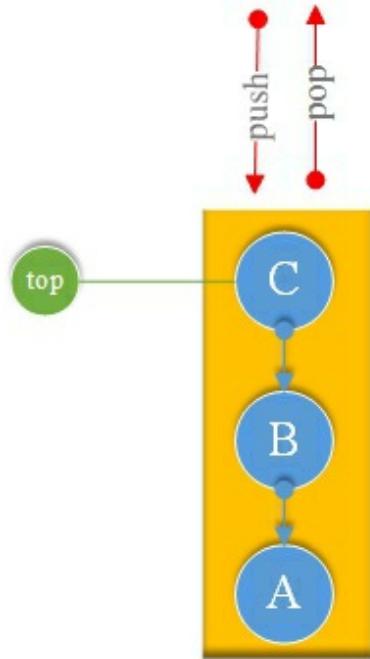
**Result:**



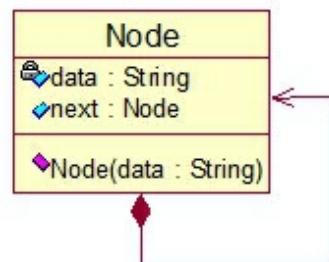
# Stack

## Stack:

FILO (First In Last Out) sequence.



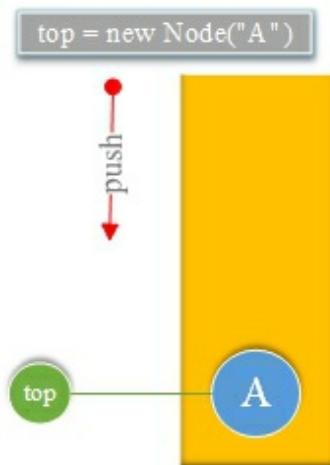
## UML Diagram



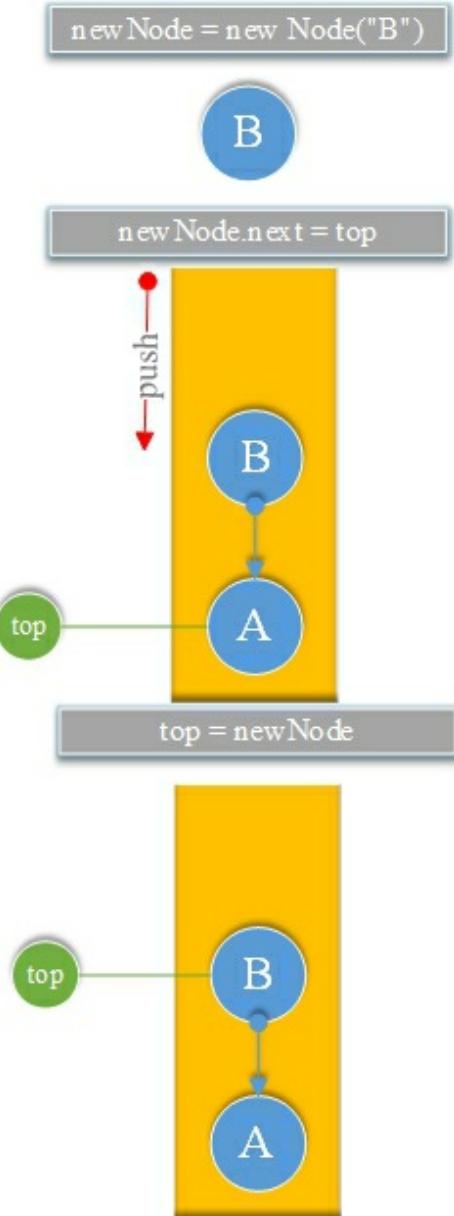
```
class Node{  
    constructor(data, next){  
        this.data = data;  
        this.next = next;  
    }  
  
    getData(){  
        return this.data;  
    }  
}
```

## 1. Stack initialization and traversal output.

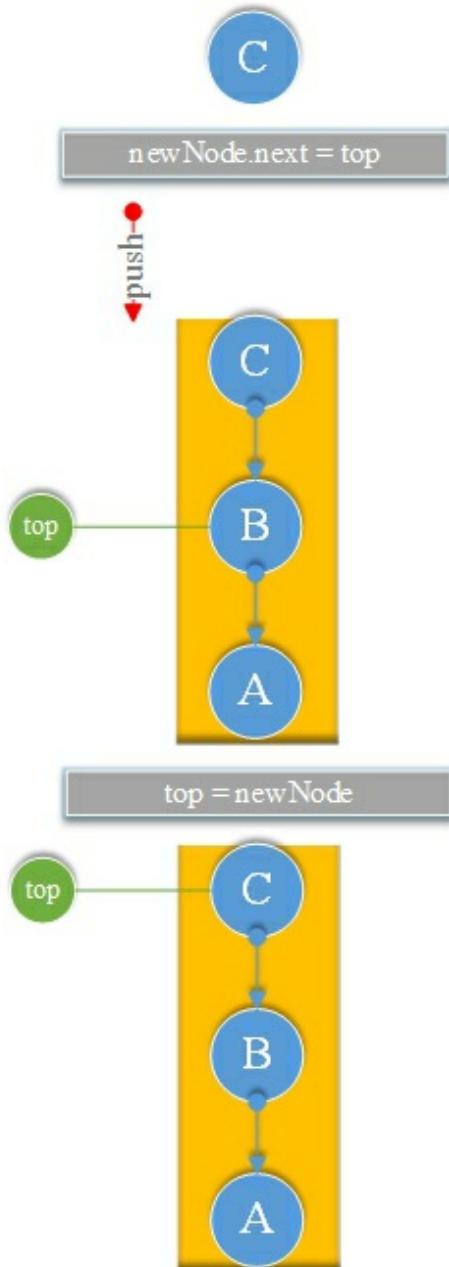
Push A into Stack



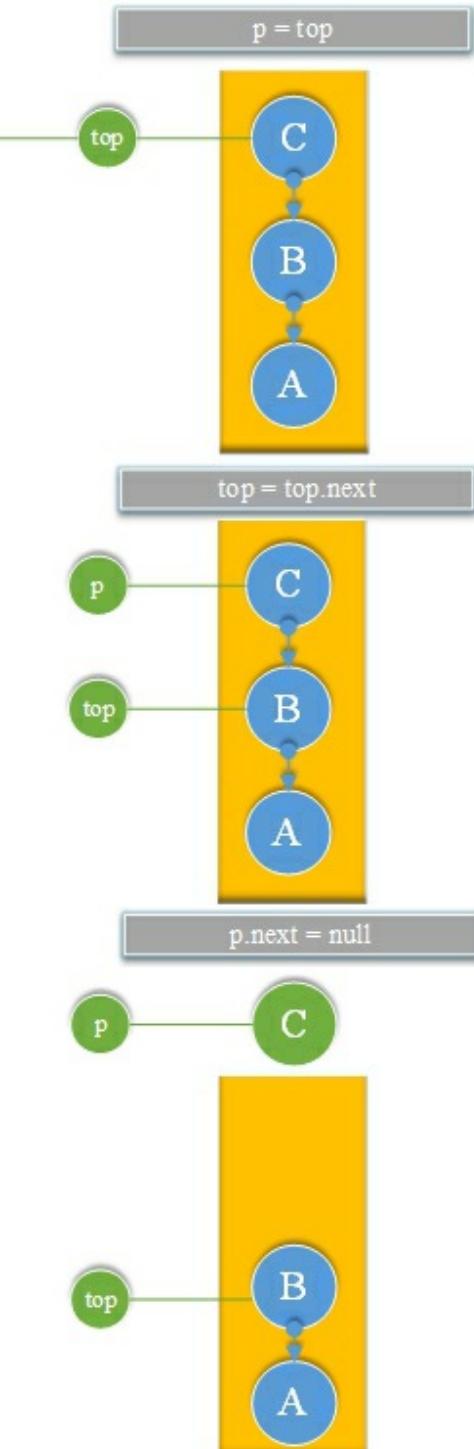
## Push B into Stack



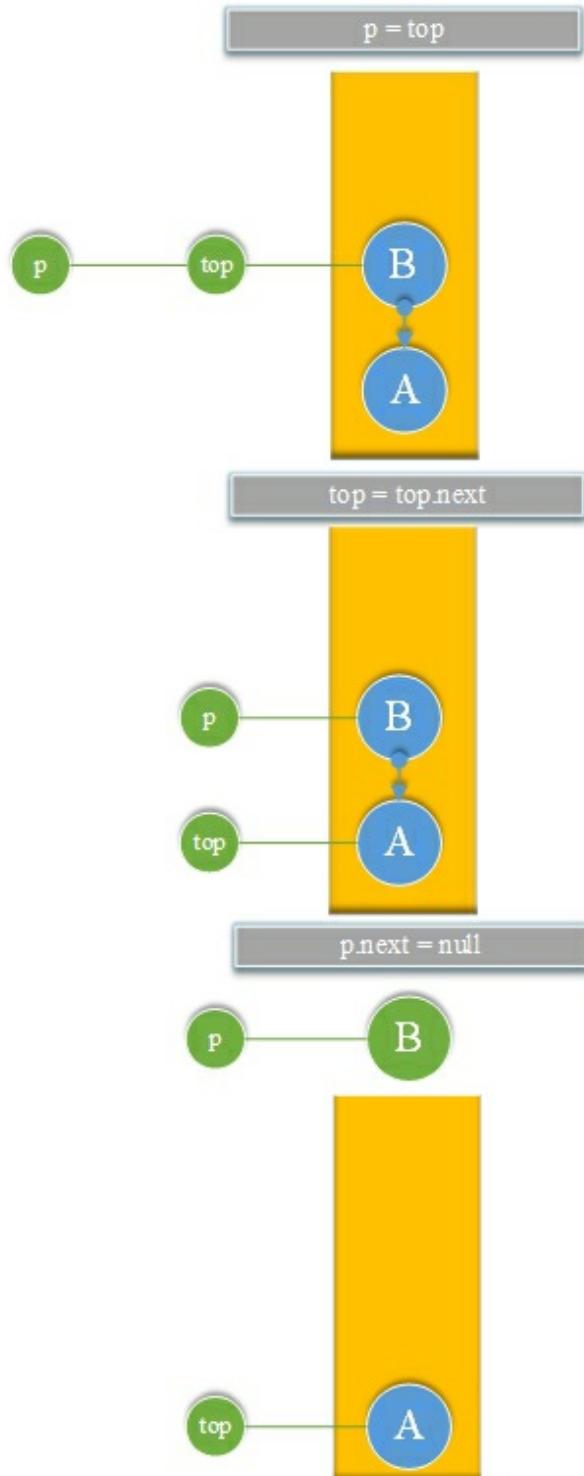
## Push C into Stack



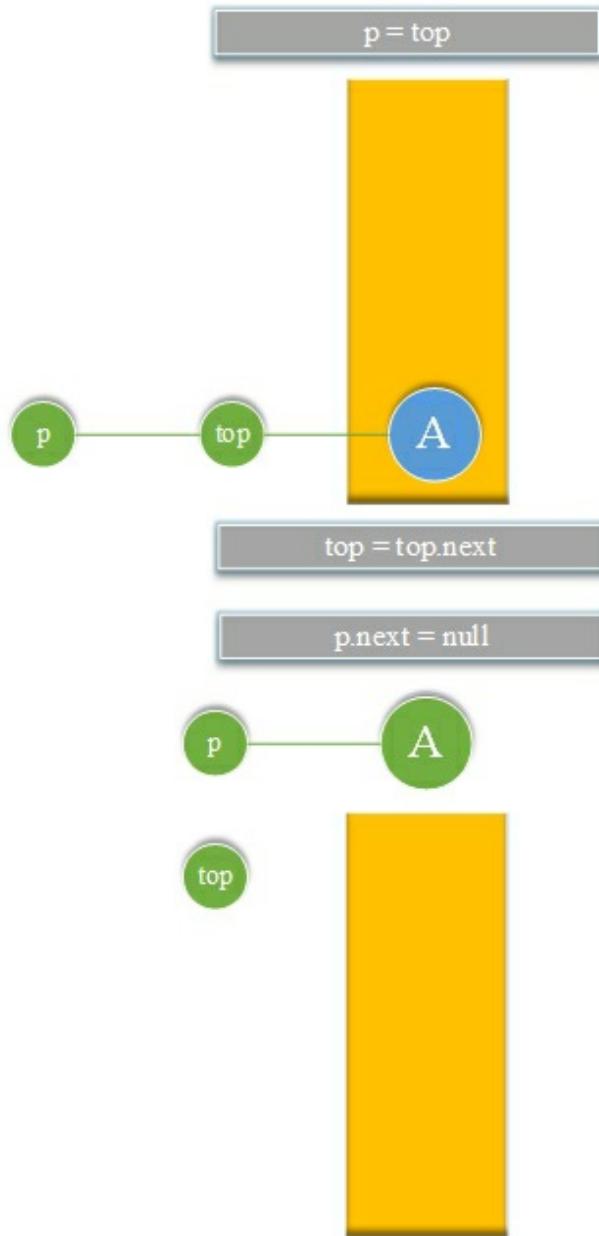
If pop C from Stack:



If pop B from Stack:



If pop A from Stack:



## Create a TestStack.html with Notepad

```
<script type="text/javascript">
class Node{
    constructor(data, next){
        this.data = data;
        this.next = next;
    }
    getData(){
        return this.data;
    }
}

class Stack {
    constructor(){
        this.top = null;
        this.size = 0;
    }

    push(element) {
        if (this.top == null) {
            this.top = new Node(element);
        } else {
            var newNode = new
Node(element);
            newNode.next = this.top;
            this.top = newNode;
        }
        this.size++;
    }

    pop() {
        if(this.top == null){
            return null;
        }
    }

    var p = this.top;
    this.top = this.top.next;// top move
```

```

down
    p.next = null;
    this.size--;
    return p;
}

size() {
    return this.size;
}
}

//////////testing//////////

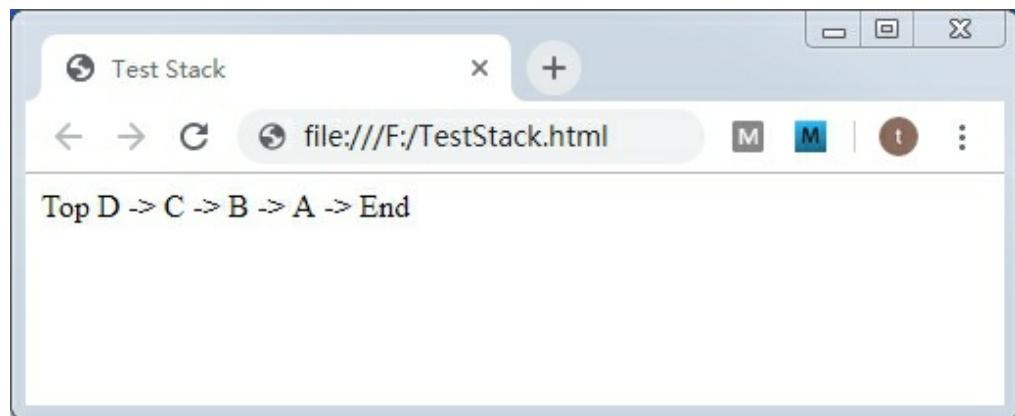
function print(stack) {
    document.write("Top ");
    var node = null;
    while ((node = stack.pop())!=null) {
        document.write(node.getData() + " - "
        > );
    }
    document.write("End <br>");
}

var stack = new Stack();
stack.push("A");
stack.push("B");
stack.push("C");
stack.push("D");
print(stack);

</script>

```

**Result:**



# Recursive Algorithm

## Recursive Algorithm:

The program function itself calls its own layer to progress until it reaches a certain condition and step by step returns to the end..

### 1. Factorial of n : $n * (n-1) * (n-2) \dots * 2 * 1$

Create a **TestRecursive.html** with **Notepad**

```
<script type="text/javascript">
    function factorial(n) {
        if (n == 1) {
            return 1;
        } else {
            //Recursively call yourself until the end of
            the return
            return factorial(n - 1) * n;
        }
    }

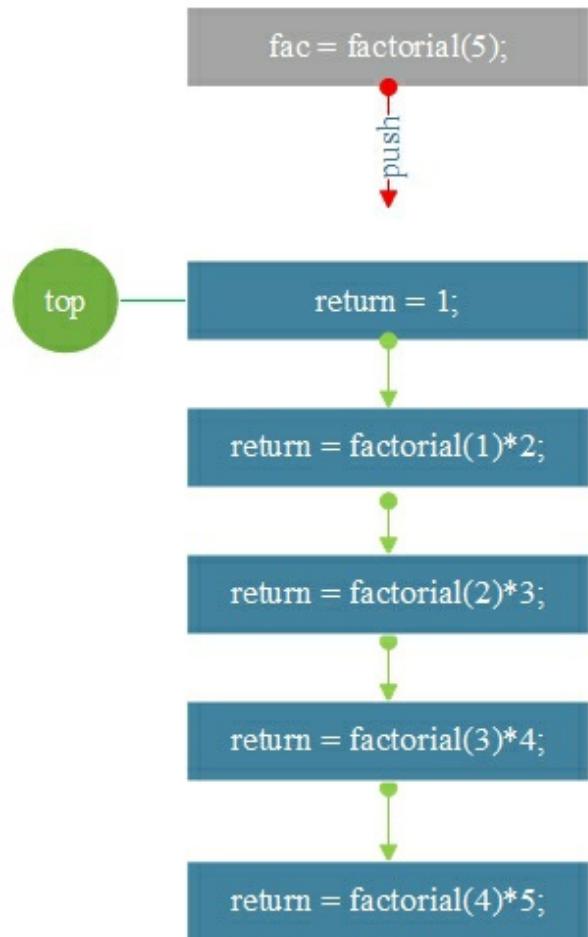
    ////////////////////testing////////////////

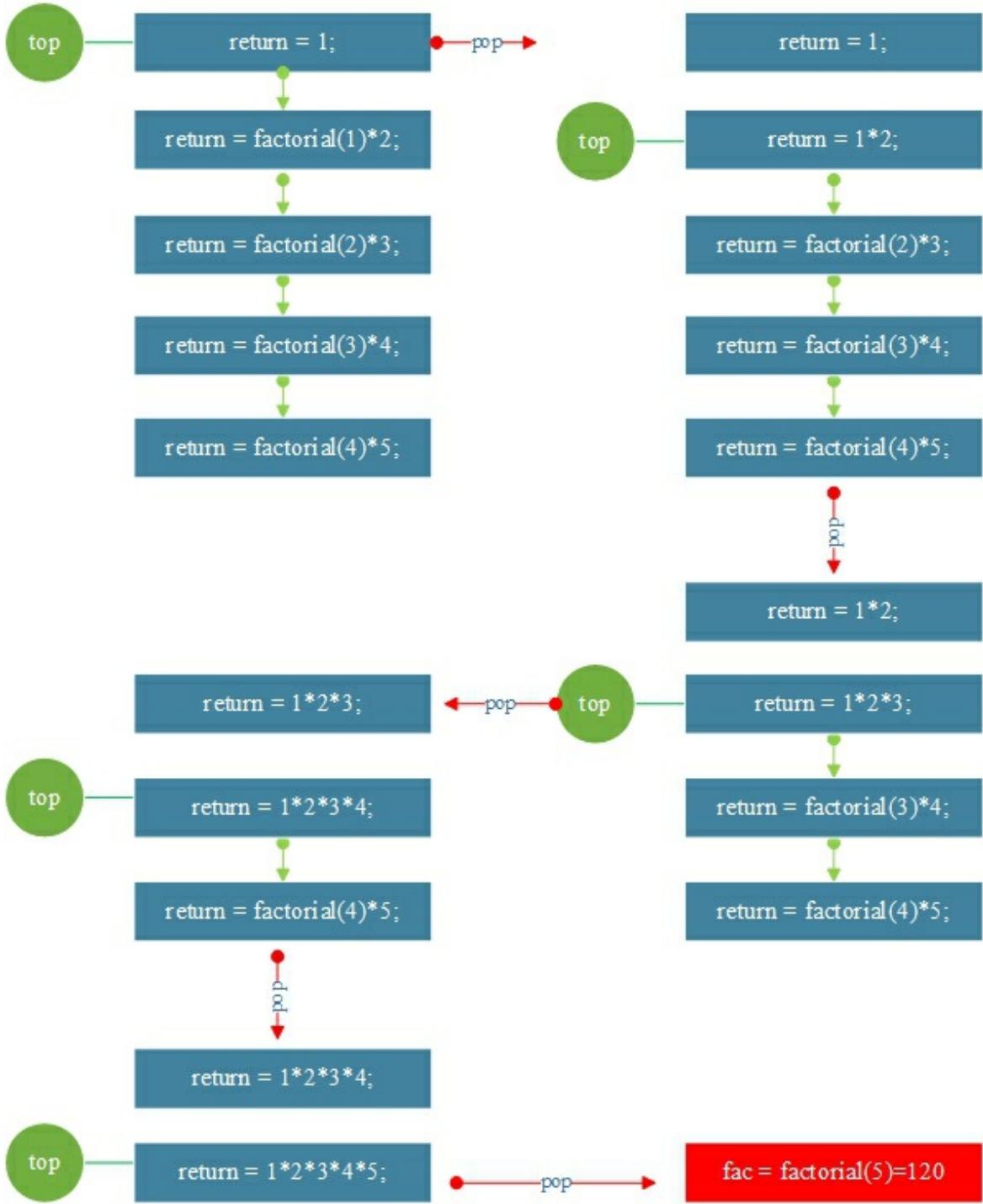
    var n = 5;
    var fac = factorial(n);
    document.write("The factorial of 5 is :" + fac);
```

## Result:



## Graphical analysis:



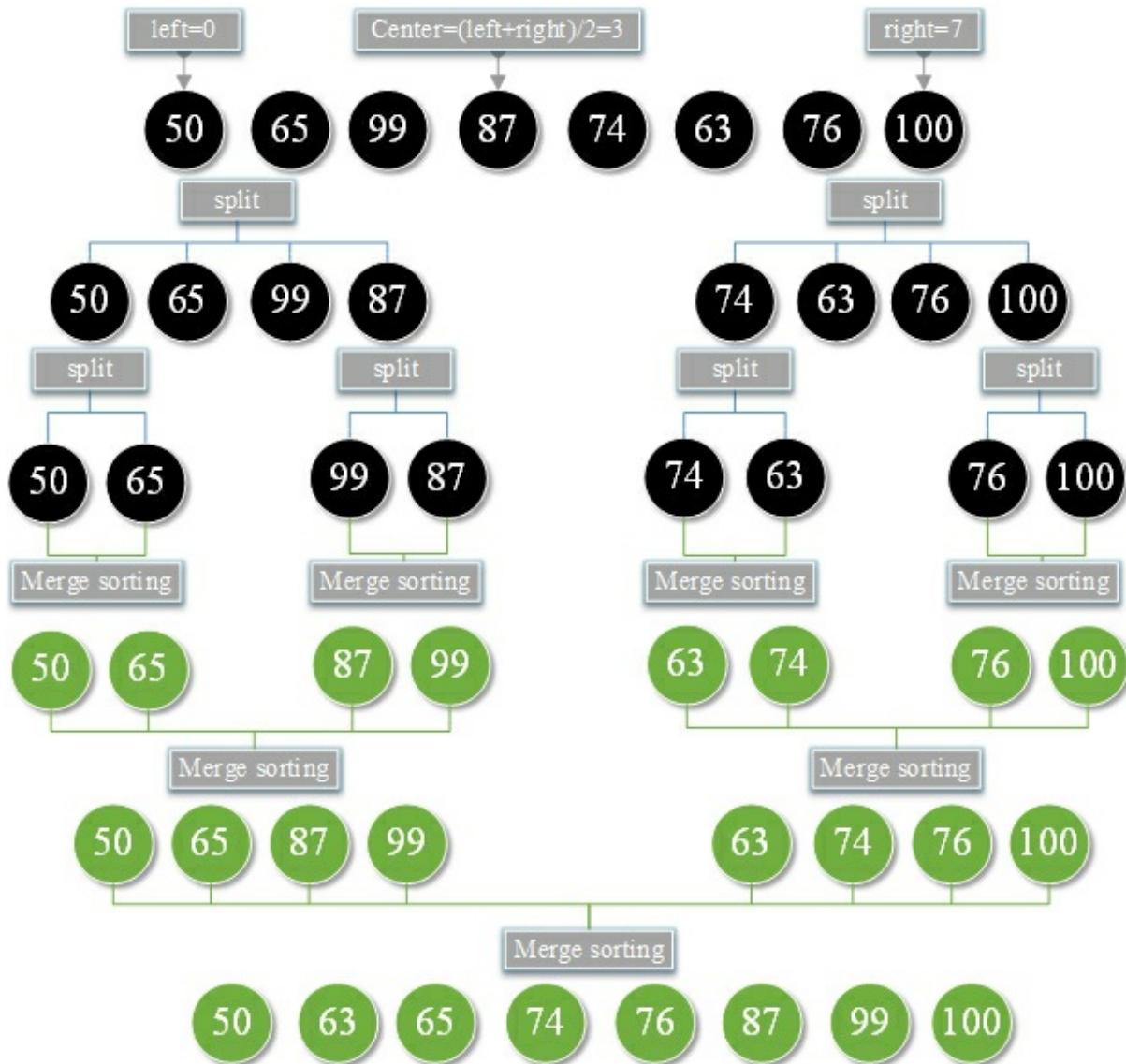


# Two-way Merge Algorithm

## Two-way Merge Algorithm:

The data of the first half and the second half are sorted, and the two ordered sub-list are merged into one ordered list, which continue to recursive to the end.

### 1. The scores {50, 65, 99, 87, 74, 63, 76, 100} by merge sort



## Create a **TestMergeSort.html** with **Notepad**

```
<script type="text/javascript">
  class MergeSort{
    sort(array) {
      var temp = new Array(array.length);
      this.mergeSort(array, temp, 0, array.length - 1);
    }

    mergeSort(array, temp, left, right) {
      if (left < right) {
        var center = parseInt((left + right) / 2);
        this.mergeSort(array, temp, left, center); // Left merge sort
        this.mergeSort(array, temp, center + 1, right); // Right merge
        sort
        this.merge(array, temp, left, center + 1, right); // Merge two
        ordered arrays
      }
    }

    merge(array, temp, left, right, rightEndIndex) {
      var leftEndIndex = right - 1; // End subscript on the left
      var tempIndex = left; // Starting from the left count
      var elementNumber = rightEndIndex - left + 1;

      while (left <= leftEndIndex && right <= rightEndIndex) {
        if (array[left] <= array[right])
          temp[tempIndex++] = array[left++];
        else
          temp[tempIndex++] = array[right++];
      }

      while (left <= leftEndIndex) { // If there is element on the left
        temp[tempIndex++] = array[left++];
      }

      while (right <= rightEndIndex) { // If there is element on the
        right
        temp[tempIndex++] = array[right++];
      }
    }
  }
}
```

```
// Copy temp to array
for (var i = 0; i < elementNumber; i++) {
    array[rightEndIndex] = temp[rightEndIndex];
    rightEndIndex--;
}
}

//////////////////testing////////////////

var scores = [ 50, 65, 99, 87, 74, 63, 76, 100, 92 ];
var mergeSort = new MergeSort();
mergeSort.sort(scores);
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ",");
}

```

### Result:

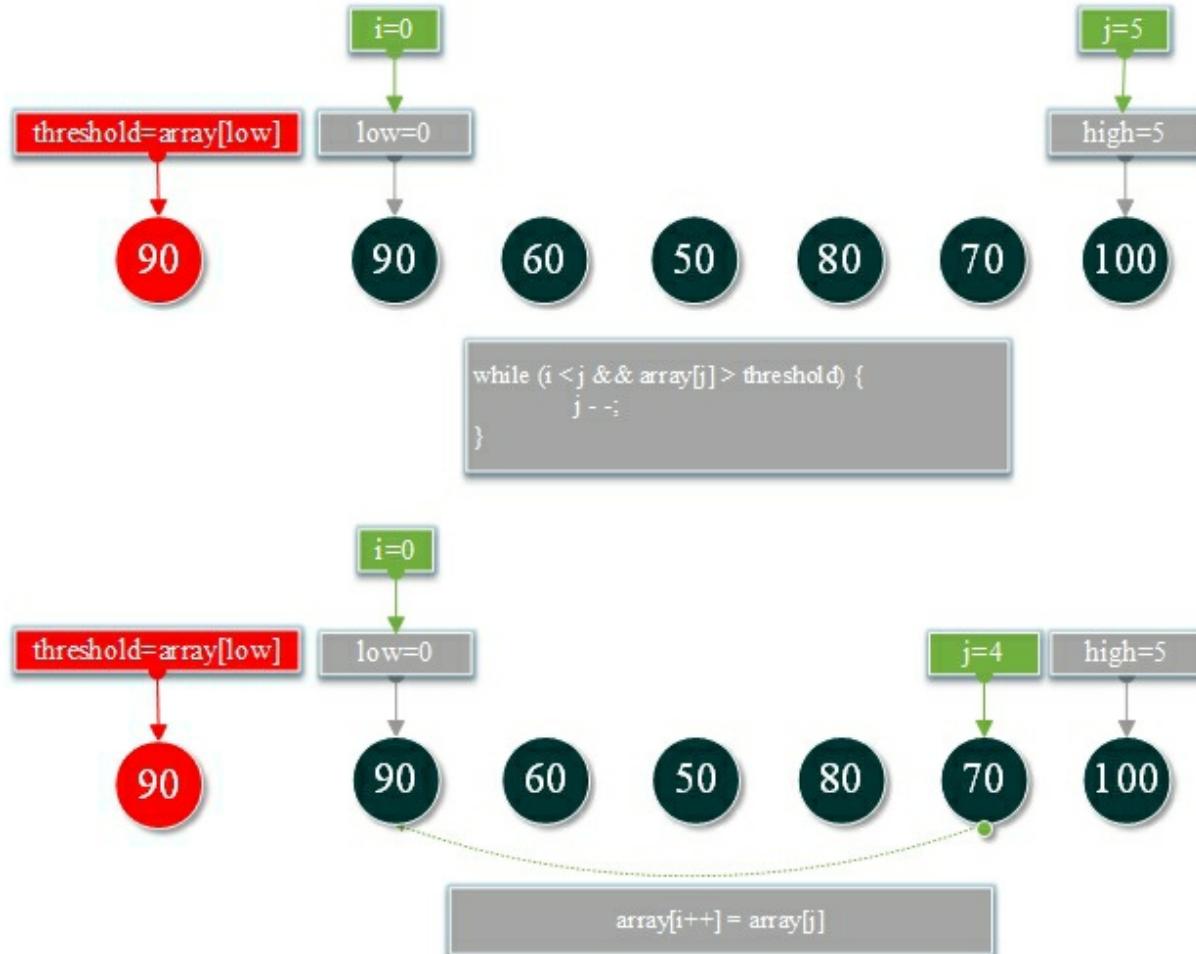


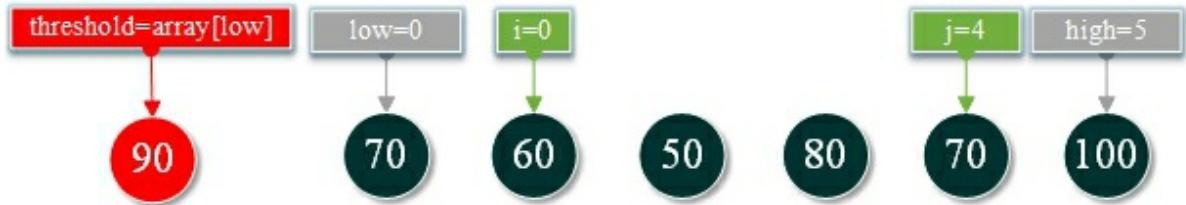
# Quick Sort Algorithm

## Quick Sort Algorithm:

Quicksort is a popular sorting algorithm that is often faster in practice compared to other sorting algorithms. It utilizes a divide-and-conquer strategy to quickly sort data items by dividing a large array into two smaller arrays.

### 1. The scores {90, 60, 50, 80, 70, 100} by quick sort





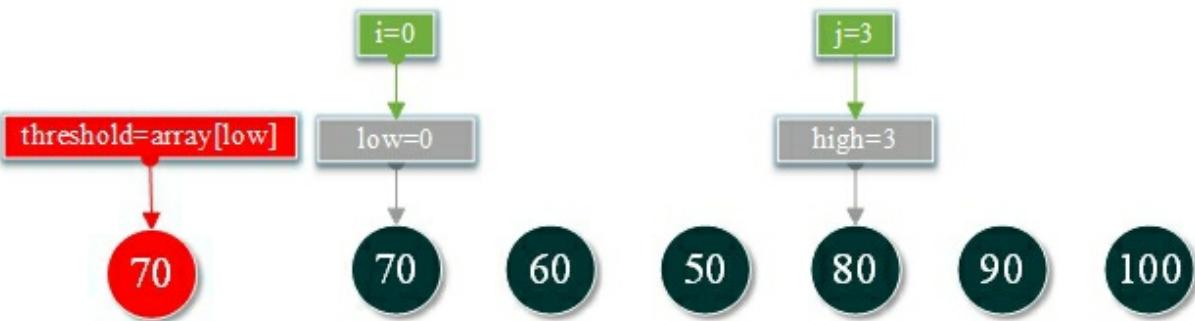
```
while (i < j && array[i] <= threshold) {  
    i++;  
}
```



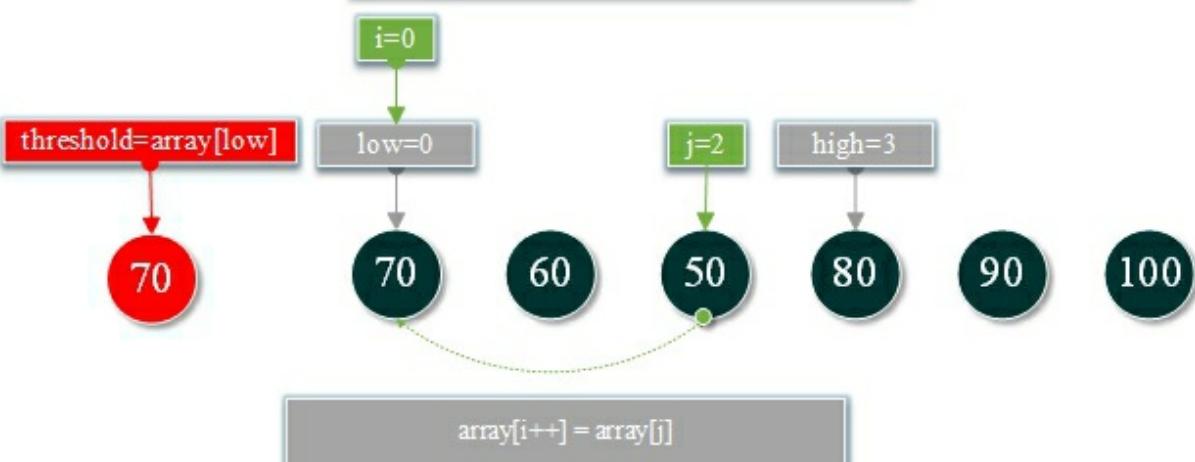
```
array[i] = threshold
```



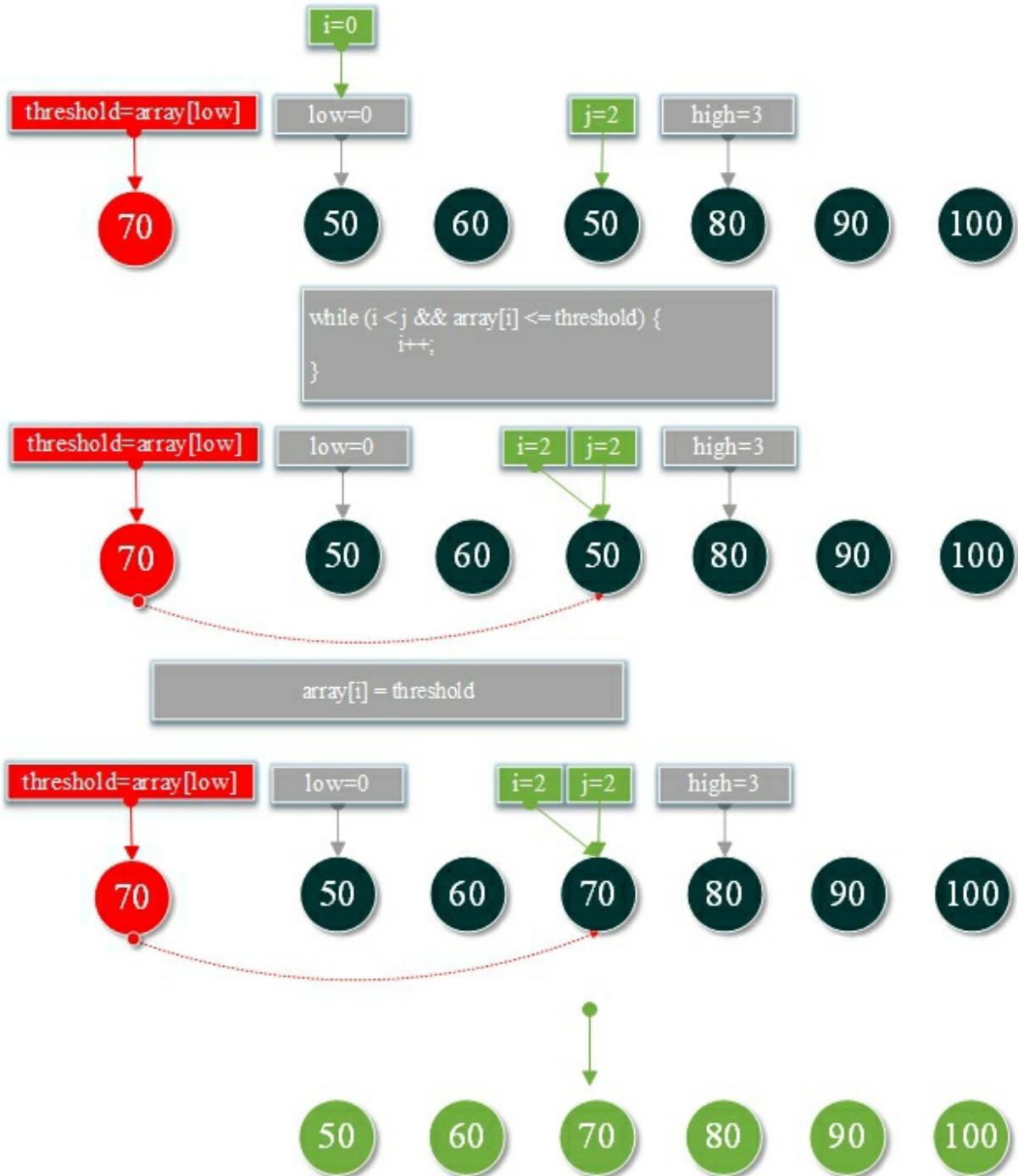
```
quickSort(array, low, i - 1)
```



```
while (i < j && array[j] > threshold) {  
    j -= 1;  
}
```



```
array[i++] = array[j]
```



## Create a **TestQuickSort.html** with **Notepad**

```
<script type="text/javascript">
  class QuickSort{
    sort(array) {
      if (array.length > 0) {
        this.quickSort(array, 0, array.length - 1);
      }
    }

    quickSort(array, low, high) {
      if (low > high) {
        return;
      }
      var i = low;
      var j = high;
      var threshold = array[low];
      // Alternately scanned from both ends of the list
      while (i < j) {
        // Find the first position less than threshold from
        right to left
        while (i < j && array[j] > threshold) {
          j--;
        }
        //Replace the low with a smaller number than the
        threshold
        if (i < j)
          array[i++] = array[j];

        // Find the first position greater than threshold from
        left to right
        while (i < j && array[i] <= threshold) {
          i++;
        }
        //Replace the high with a number larger than the
        threshold
        if (i < j)
```

```

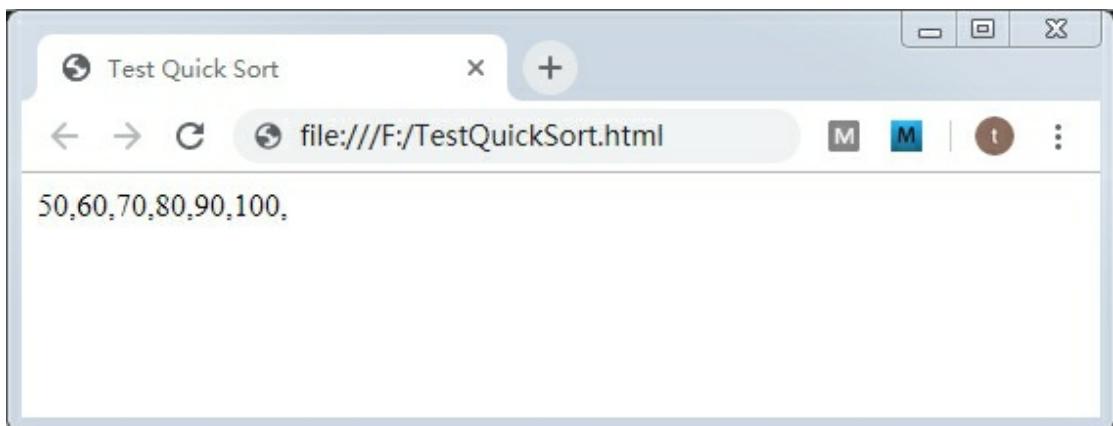
        array[j--] = array[i];
    }
    array[i] = threshold;

    this.quickSort(array, low, i - 1); // left quickSort
    this.quickSort(array, i + 1, high); // right quickSort
}
}

//////////testing/////////
var scores = [ 90, 60, 50, 80, 70, 100 ];
var quickSort = new QuickSort();
quickSort.sort(scores);
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ",");
}
</script>

```

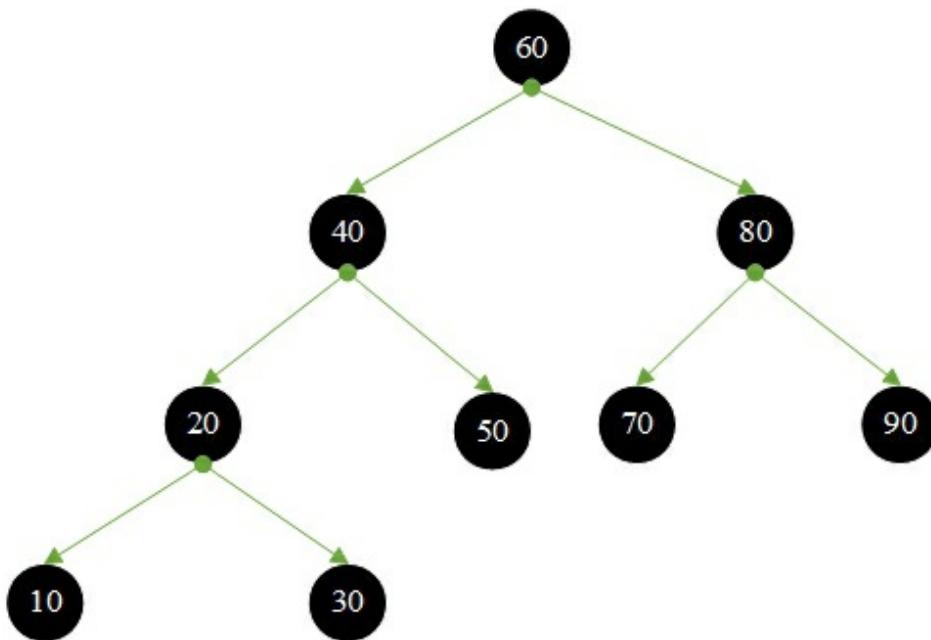
## Result:



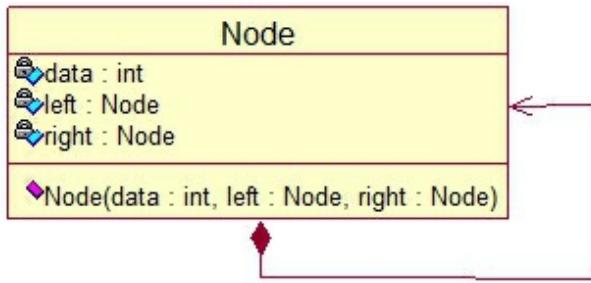
# Binary Search Tree

## Binary Search Tree:

1. If the left subtree of any node is not empty, the value of all nodes on the left subtree is less than the value of its root node;
2. If the right subtree of any node is not empty, the value of all nodes on the right subtree is greater than the value of its root node;
3. The left subtree and the right subtree of any node are also binary search trees.



## Node UML Diagram



```
class Node{
    constructor(data, left, right){
        this.data = data;
        this.left = left;
        this.right = right;
    }

    getData(){
        return this.data;
    }
}
```

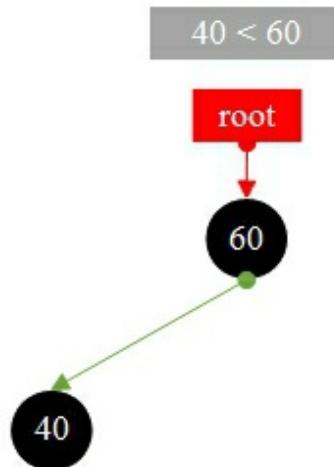
## 1. Construct a binary search tree, insert node

The inserted nodes are compared from the root node, and the smaller than the root node is compared with the left subtree of the root node, otherwise, compared with the right subtree until the left subtree is empty or the right subtree is empty, then is inserted.

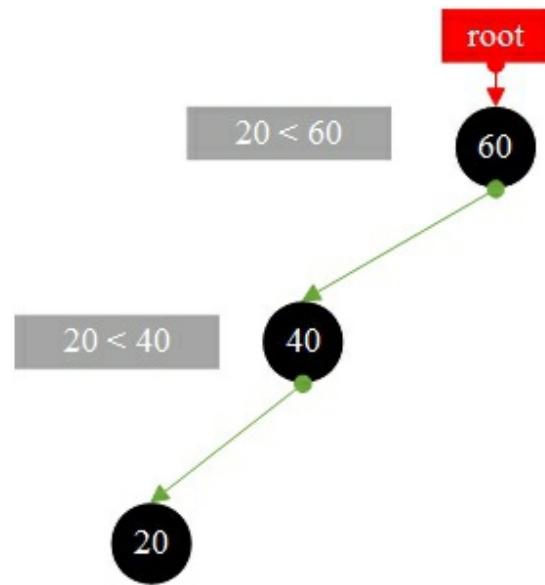
### Insert 60



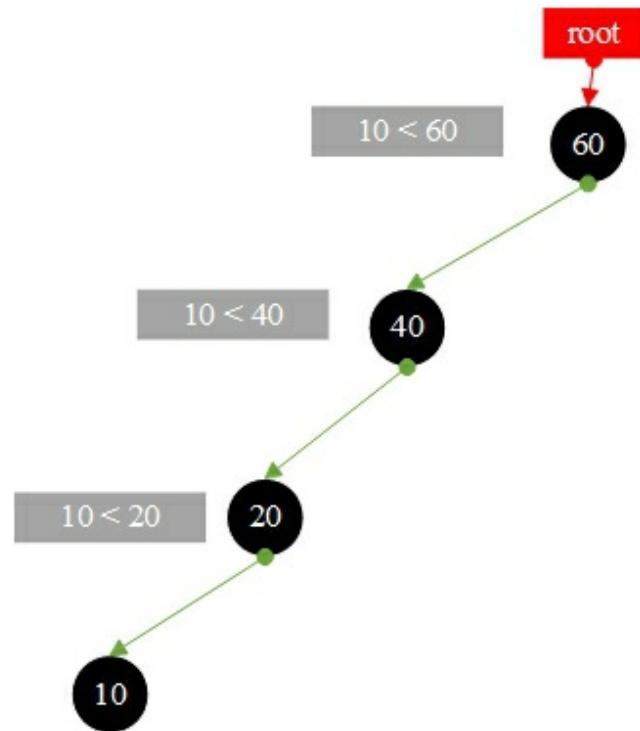
### Insert 40



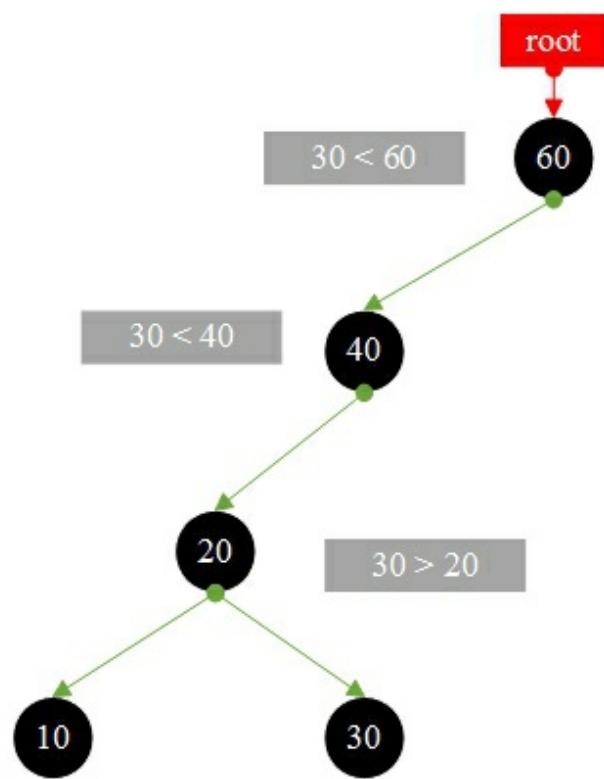
## Insert 20



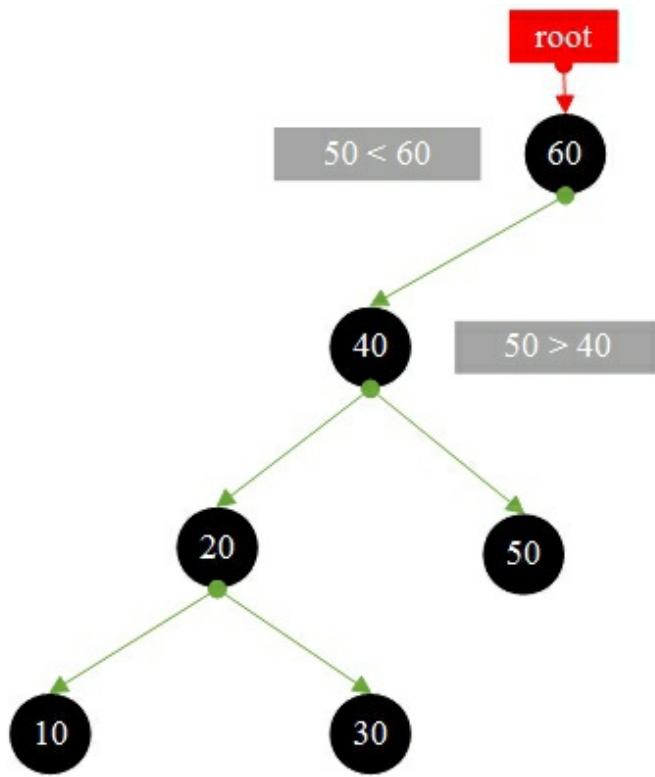
## Insert 10



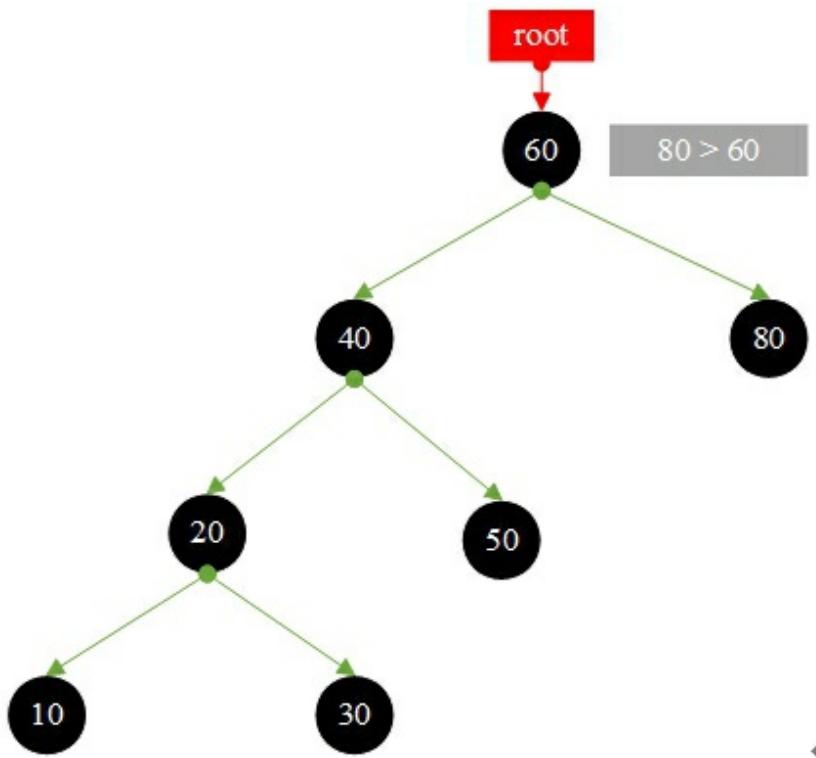
## Insert 30



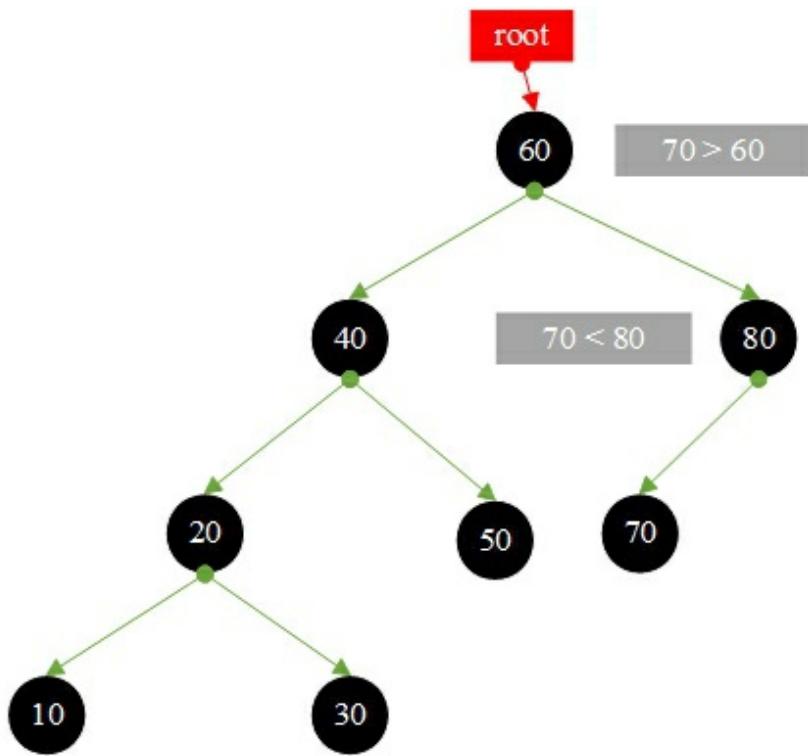
## Insert 50



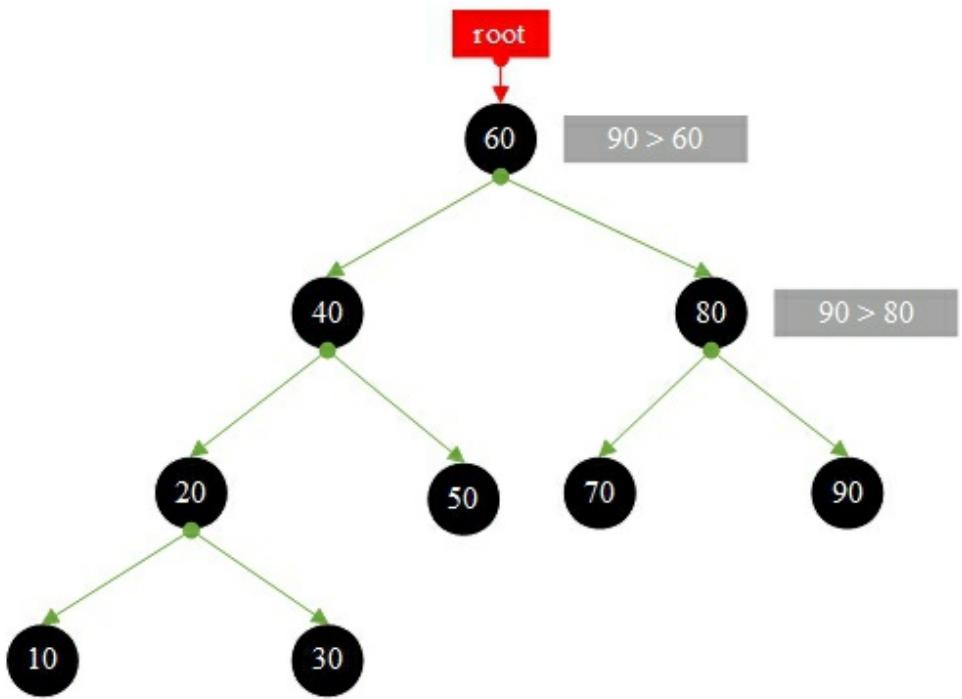
## Insert 80



## Insert 70

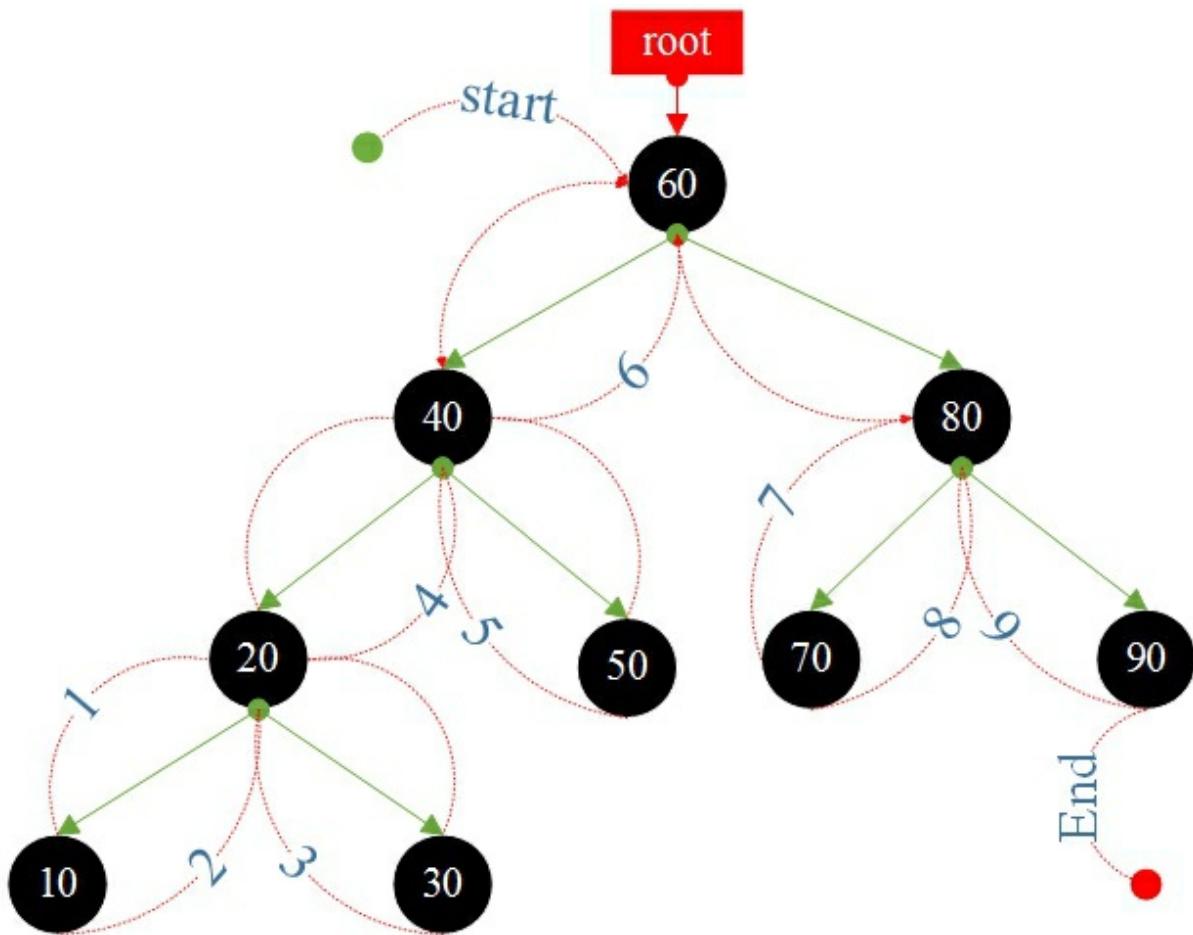


## Insert 90

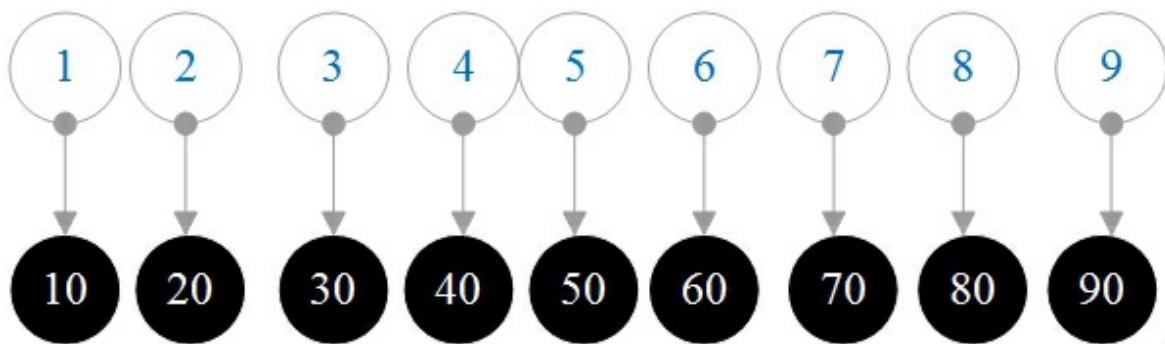


## 2. binary search tree **In-order traversal**

**In-order traversal** : left subtree -> root node -> right subtree



**Result:**



## Create a **TestBinarySearchTreeInOrder.html** with **Notepad**

```
<script type="text/javascript">
class BinaryTree {
    getRoot() {
        return this.root;
    }

    // In-order traversal binary search tree
    inOrder(root) {
        if (root == null) {
            return;
        }
        this.inOrder(root.left); // Traversing the left subtree
        document.write(root.getData() + ", ");
        this.inOrder(root.right); // Traversing the right subtree
    }

    insert(node, newData) {
        if (this.root == null) {
            this.root = new Node(newData, null, null);
            return;
        }

        var compareValue = newData - node.getData();

        //Recursive left subtree, continue to find the insertion position
        if (compareValue < 0) {
            if (node.left == null) {
                node.left = new Node(newData, null, null);
            } else {
                this.insert(node.left, newData);
            }
        } else if (compareValue > 0) {///Recursive right subtree, find the
            insertion position
            if (node.right == null) {
                node.right = new Node(newData, null, null);
            } else {
```

```

        this.insert(node.right, newData);
    }
}
}
}

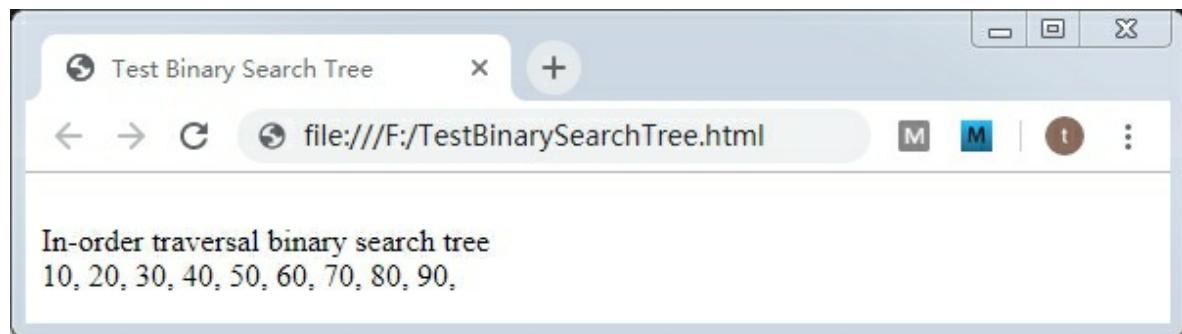
class Node{
    constructor(data, left, right){
        this.data = data;
        this.left = left;
        this.right = right;
    }

    getData(){
        return this.data;
    }
}

//////////////testing///////////
var binaryTree=new BinaryTree();
//Constructing a binary search tree
binaryTree.insert(binaryTree.getRoot(), 60);
binaryTree.insert(binaryTree.getRoot(), 40);
binaryTree.insert(binaryTree.getRoot(), 20);
binaryTree.insert(binaryTree.getRoot(), 10);
binaryTree.insert(binaryTree.getRoot(), 30);
binaryTree.insert(binaryTree.getRoot(), 50);
binaryTree.insert(binaryTree.getRoot(), 80);
binaryTree.insert(binaryTree.getRoot(), 70);
binaryTree.insert(binaryTree.getRoot(), 90);
document.write("<br> In-order traversal binary search tree <br>");
binaryTree.inOrder(binaryTree.getRoot());
</script>

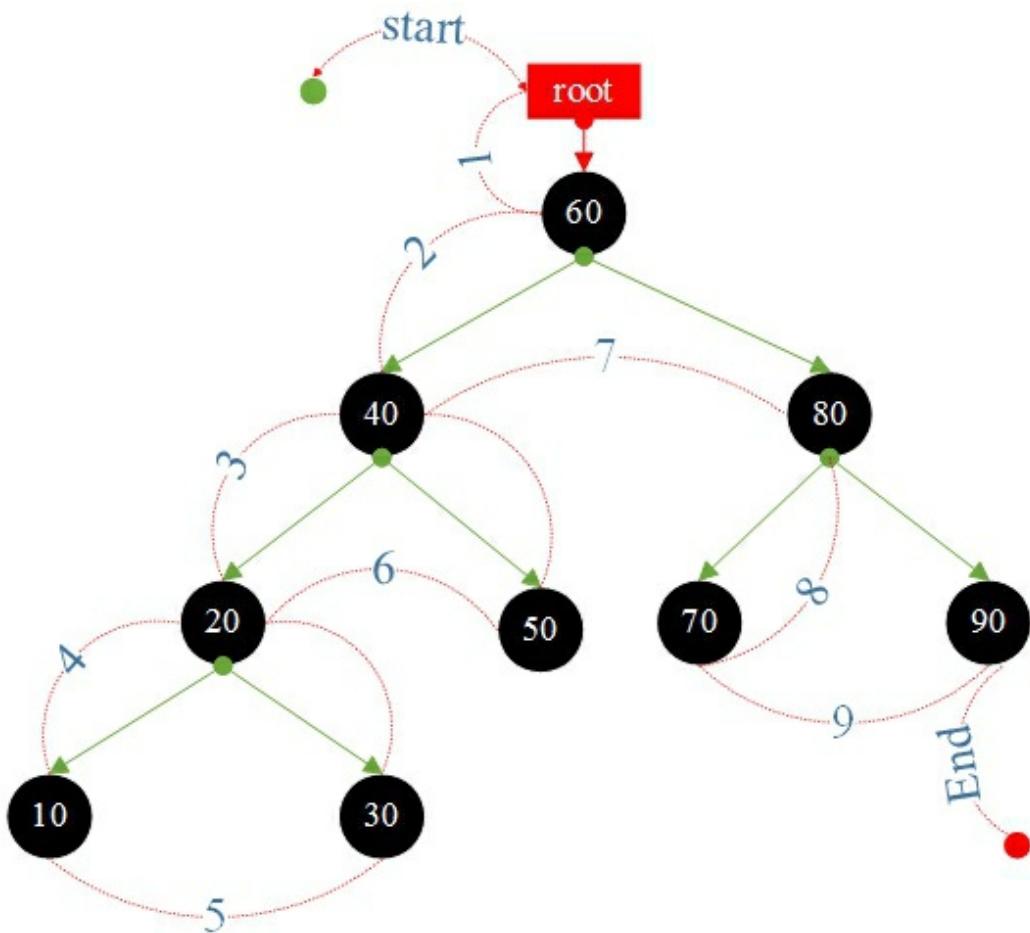
```

**Result:**

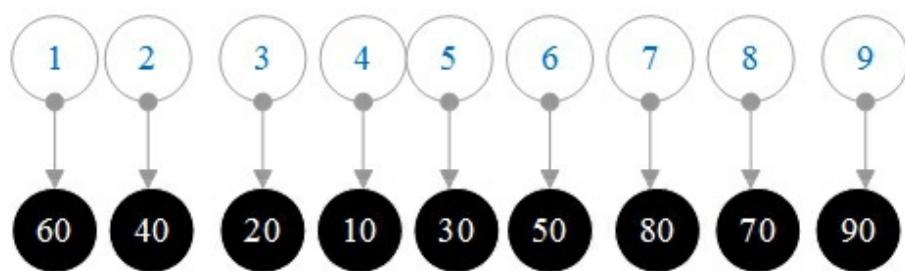


### 3. binary search tree **Pre-order traversal**

**Pre-order traversal** : root node -> left subtree -> right subtree



**Result:**



## Create a **TestBinarySearchTreePreOrder.html** with **Notepad**

```
<script type="text/javascript">
  class BinaryTree {
    getRoot() {
      return this.root;
    }

    //Preorder traversal binary search tree
    preOrder(root) {
      if (root == null) {
        return;
      }
      document.write(root.getData() + ", ");
      this.preOrder(root.left); // Recursive Traversing the left subtree
      this.preOrder(root.right); // Recursive Traversing the right
      subtree
    }

    insert(node, newData) {
      if (this.root == null) {
        this.root = new Node(newData, null, null);
        return;
      }

      var compareValue = newData - node.getData();
      //Recursive left subtree, continue to find the insertion position
      if (compareValue < 0) {
        if (node.left == null) {
          node.left = new Node(newData, null, null);
        } else {
          this.insert(node.left, newData);
        }
      } else if (compareValue > 0) {///Recursive right subtree,
      continue to find the insertion position
        if (node.right == null) {
          node.right = new Node(newData, null, null);
        } else {
```

```

        this.insert(node.right, newData);
    }
}
}
}

class Node{
    constructor(data, left, right){
        this.data = data;
        this.left = left;
        this.right = right;
    }

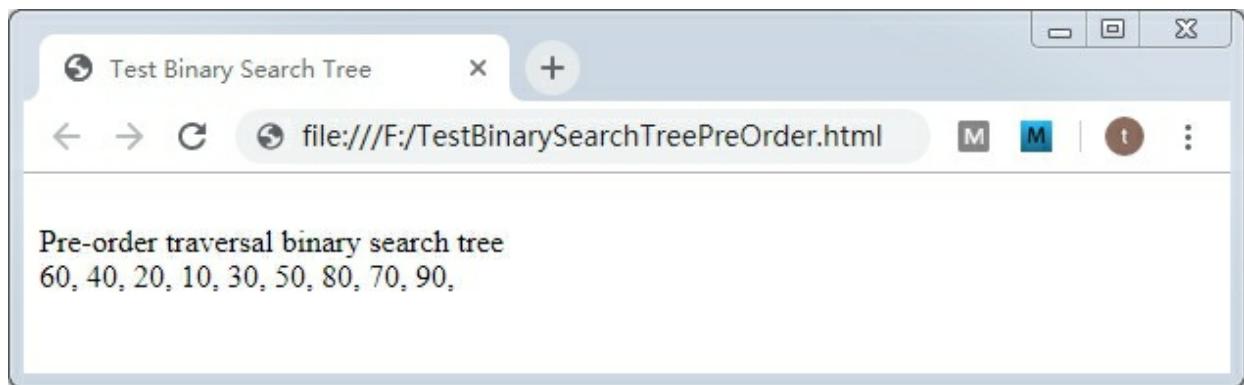
    getData(){
        return this.data;
    }
}

//////////////testing///////////
var binaryTree=new BinaryTree();
//Constructing a binary search tree
binaryTree.insert(binaryTree.getRoot(), 60);
binaryTree.insert(binaryTree.getRoot(), 40);
binaryTree.insert(binaryTree.getRoot(), 20);
binaryTree.insert(binaryTree.getRoot(), 10);
binaryTree.insert(binaryTree.getRoot(), 30);
binaryTree.insert(binaryTree.getRoot(), 50);
binaryTree.insert(binaryTree.getRoot(), 80);
binaryTree.insert(binaryTree.getRoot(), 70);
binaryTree.insert(binaryTree.getRoot(), 90);

document.write("<br> Pre-order traversal binary search tree <br>");
binaryTree.preOrder(binaryTree.getRoot());
</script>

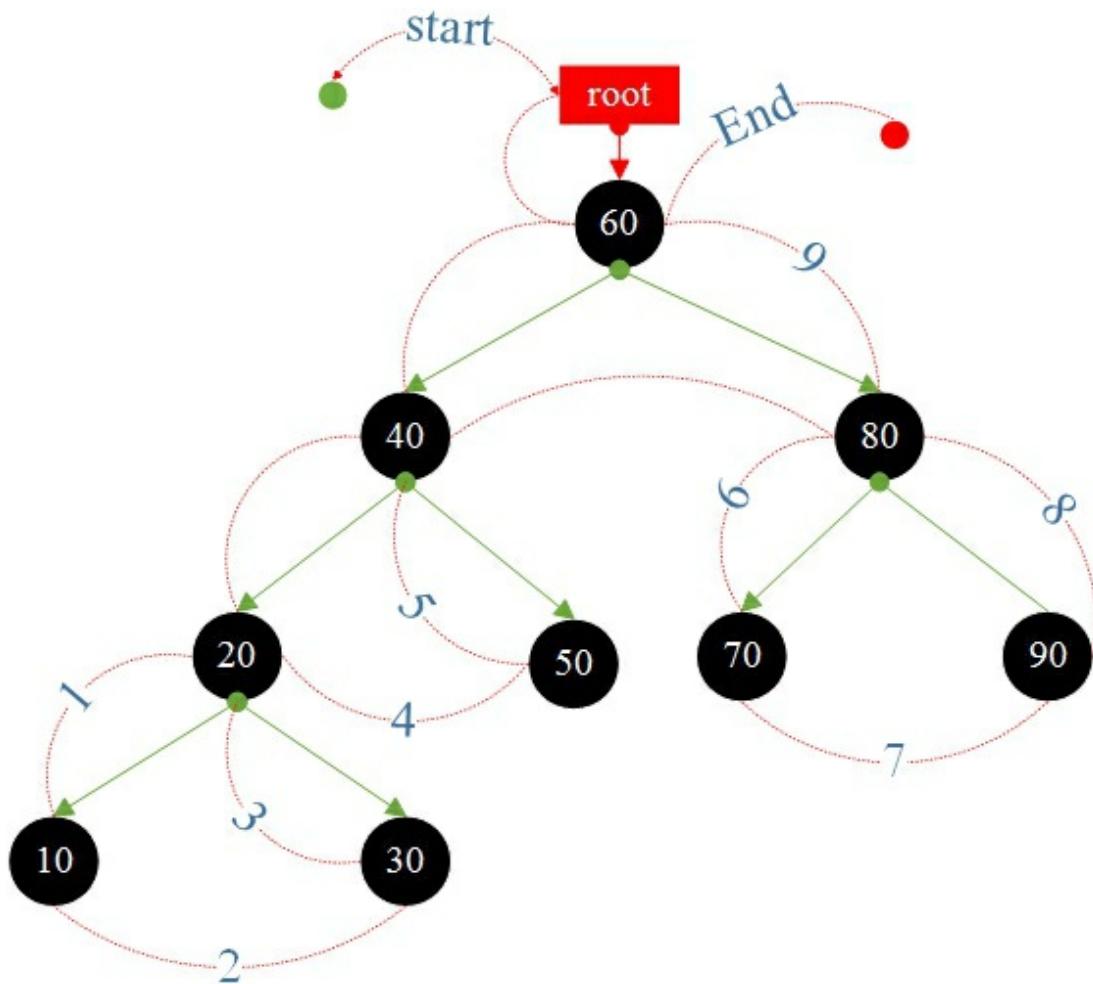
```

**Result:**

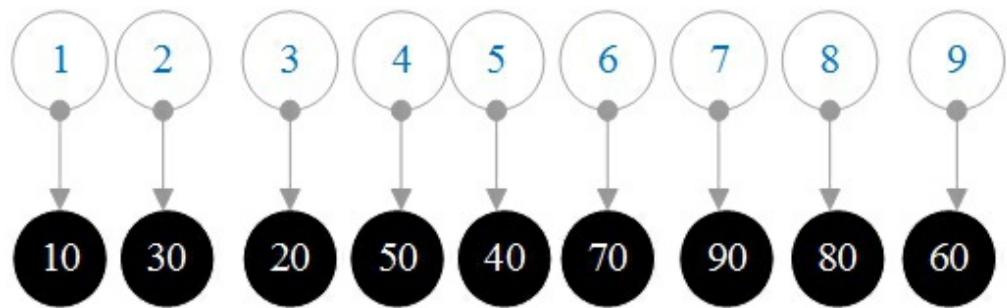


#### 4. binary search tree Post-order traversal

**Post-order traversal** : right subtree -> root node -> left subtree



**Result:**



## Create a **TestBinarySearchTreePostOrder.html** with **Notepad**

```
<script type="text/javascript">
class BinaryTree {
    getRoot() {
        return this.root;
    }

    //Post-order traversal binary search tree
    postOrder(root) {
        if (root == null) {
            return;
        }
        this.postOrder(root.left); // Recursive Traversing the left subtree
        this.postOrder(root.right); // Recursive Traversing the right
        subtree
        document.write(root.getData() + ", ");
    }

    insert(node, newData) {
        if (this.root == null) {
            this.root = new Node(newData, null, null);
            return;
        }

        var compareValue = newData - node.getData();
        //Recursive left subtree, continue to find the insertion position
        if (compareValue < 0) {
            if (node.left == null) {
                node.left = new Node(newData, null, null);
            } else {
                this.insert(node.left, newData);
            }
        } else if (compareValue > 0) {///Recursive right subtree,
        continue to find the insertion position
            if (node.right == null) {
                node.right = new Node(newData, null, null);
            } else {
```

```

        this.insert(node.right, newData);
    }
}
}
}

class Node{
    constructor(data, left, right){
        this.data = data;
        this.left = left;
        this.right = right;
    }

    getData(){
        return this.data;
    }
}

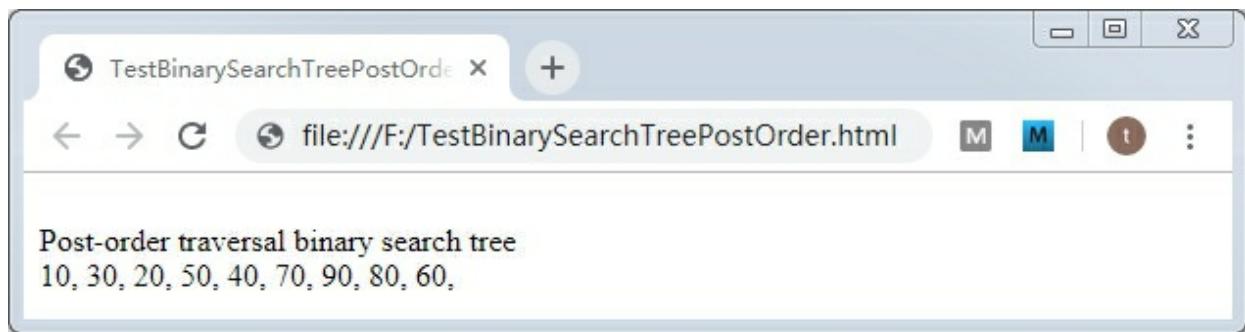
//////////////testing///////////
var binaryTree=new BinaryTree();

//Constructing a binary search tree
binaryTree.insert(binaryTree.getRoot(), 60);
binaryTree.insert(binaryTree.getRoot(), 40);
binaryTree.insert(binaryTree.getRoot(), 20);
binaryTree.insert(binaryTree.getRoot(), 10);
binaryTree.insert(binaryTree.getRoot(), 30);
binaryTree.insert(binaryTree.getRoot(), 50);
binaryTree.insert(binaryTree.getRoot(), 80);
binaryTree.insert(binaryTree.getRoot(), 70);
binaryTree.insert(binaryTree.getRoot(), 90);

document.write("<br> Post-order traversal binary search tree <br>");
binaryTree.postOrder(binaryTree.getRoot());
</script>

```

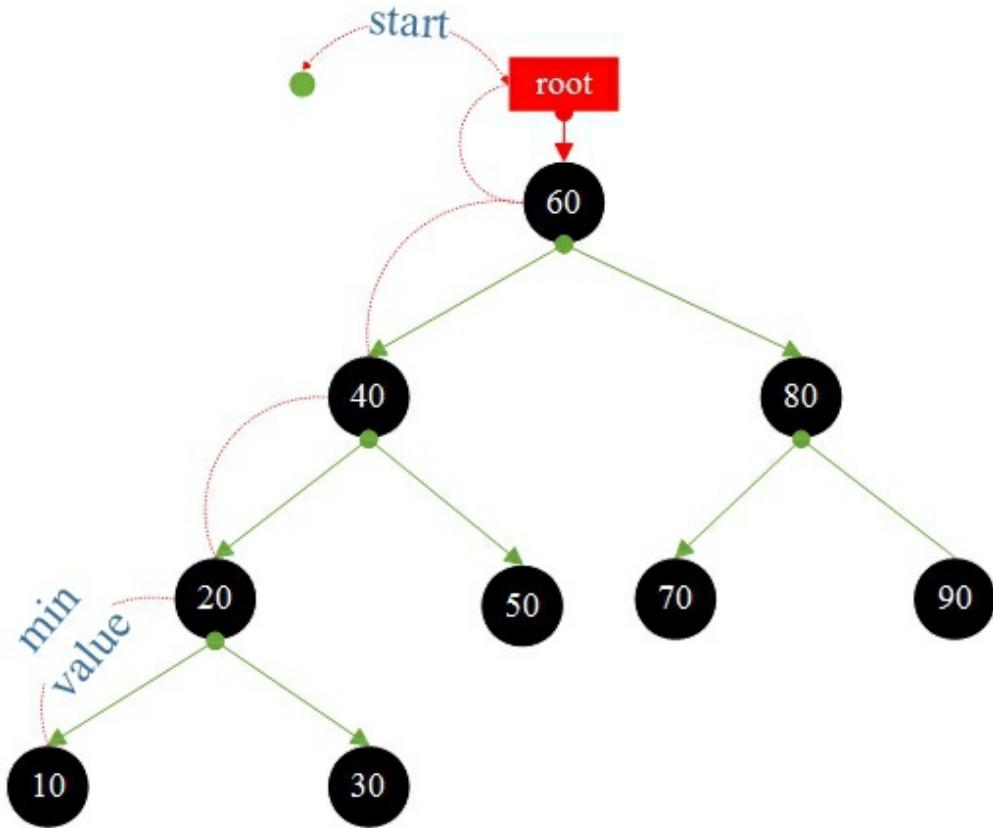
**Result:**

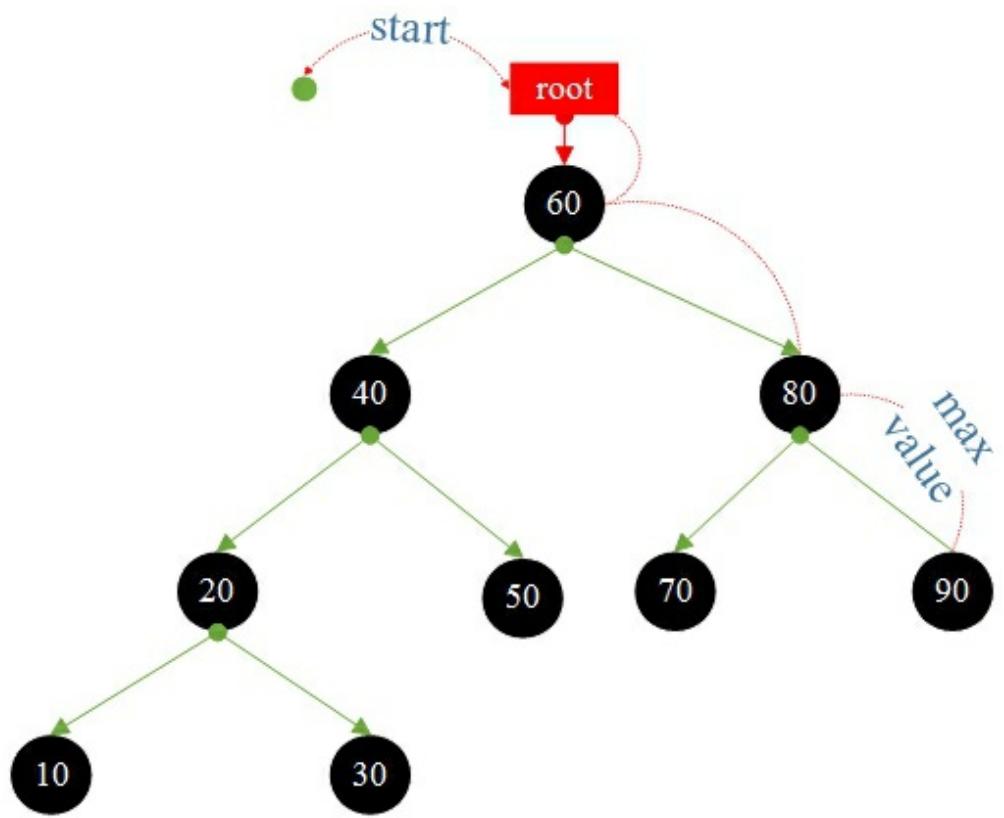


## 5. binary search tree **Maximum and minimum**

**Minimum value:** The small value is on the left child node, as long as the recursion traverses the left child until be empty, the current node is the minimum node.

**Maximum value:** The large value is on the right child node, as long as the recursive traversal is the right child until be empty, the current node is the largest node.





## Create a **TestBinarySearchTreeMaxMinValue.html** with **NotePad**

```
<script type="text/javascript">
  class BinaryTree {
    getRoot() {
      return this.root;
    }

    //Minimum value
    searchMinValue(node) {
      if (node == null || node.getData() == 0)
        return null;
      if (node.left == null) {
        return node;
      }
      //Recursively find the minimum from the left subtree
      return this.searchMinValue(node.left);
    }

    //Maximum value
    searchMaxValue(node) {
      if (node == null || node.getData() == 0)
        return null;
      if (node.right == null) {
        return node;
      }
      //Recursively find the maximum from the right subtree
      return this.searchMaxValue(node.right);
    }
  }
</script>
```

```

insert(node, newData) {
    if (this.root == null) {
        this.root = new Node(newData, null, null);
        return;
    }

    var compareValue = newData - node.getData();
    //Recursive left subtree, continue to find the insertion position
    if (compareValue < 0) {
        if (node.left == null) {
            node.left = new Node(newData, null, null);
        } else {
            this.insert(node.left, newData);
        }
    } else if (compareValue > 0) {///Recursive right subtree,
        continue to find the insertion position
        if (node.right == null) {
            node.right = new Node(newData, null, null);
        } else {
            this.insert(node.right, newData);
        }
    }
}

class Node{
    constructor(data, left, right){
        this.data = data;
        this.left = left;
        this.right = right;
    }

    getData(){
        return this.data;
    }
}

```

```

//////////////////testing////////////////

var binaryTree=new BinaryTree();

//Constructing a binary search tree
binaryTree.insert(binaryTree.getRoot(), 60);
binaryTree.insert(binaryTree.getRoot(), 40);
binaryTree.insert(binaryTree.getRoot(), 20);
binaryTree.insert(binaryTree.getRoot(), 10);
binaryTree.insert(binaryTree.getRoot(), 30);
binaryTree.insert(binaryTree.getRoot(), 50);
binaryTree.insert(binaryTree.getRoot(), 80);
binaryTree.insert(binaryTree.getRoot(), 70);
binaryTree.insert(binaryTree.getRoot(), 90);

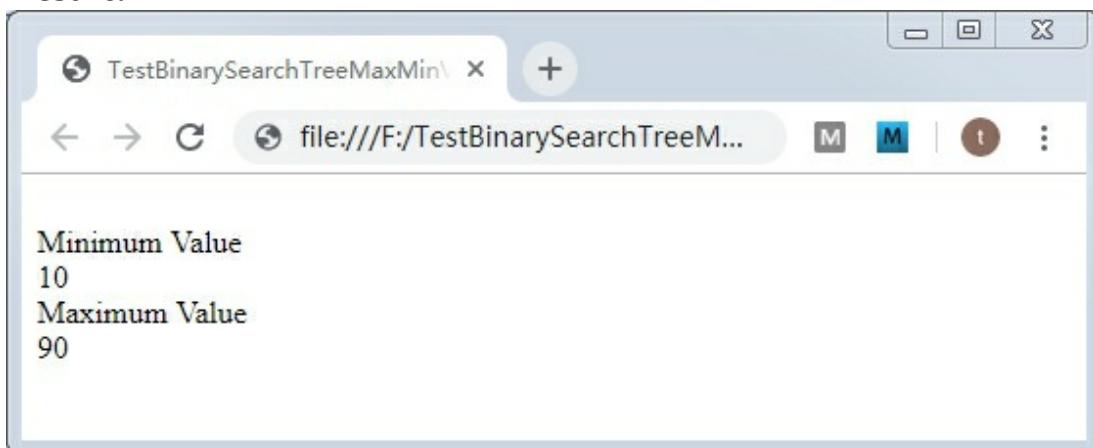
document.write("<br> Minimum Value<br> ");
var minNode = binaryTree.searchMinValue(binaryTree.getRoot());
document.write(minNode.getData());

document.write("<br> Maximum Value<br> ");
var maxNode = binaryTree.searchMaxValue(binaryTree.getRoot());
document.write(maxNode.getData());

</script>

```

## Result:

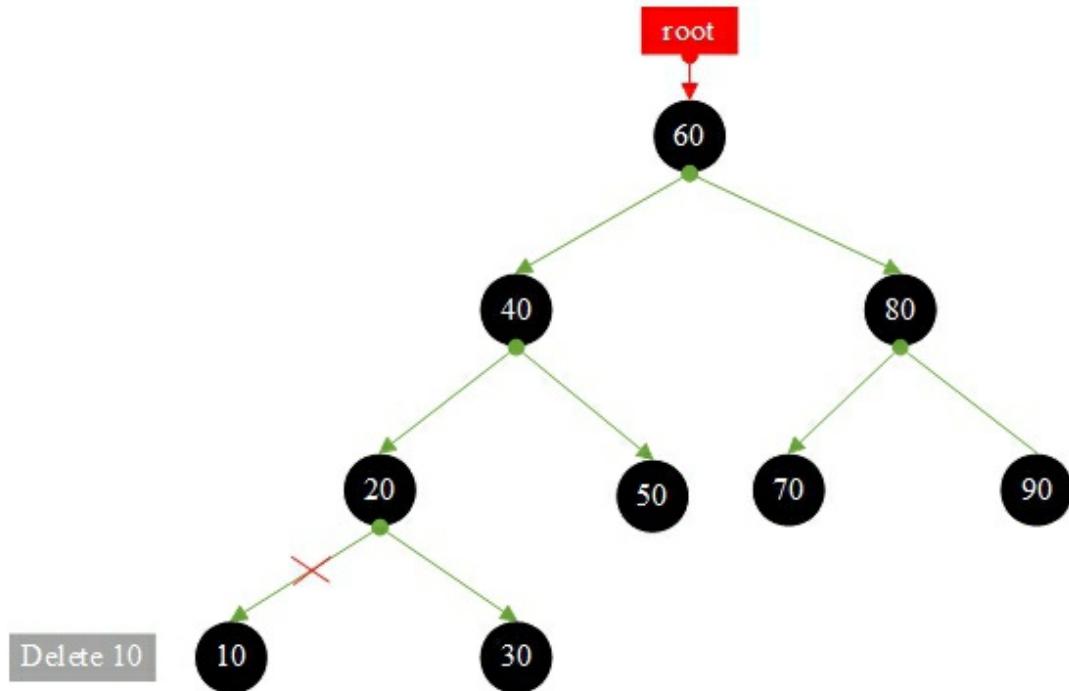


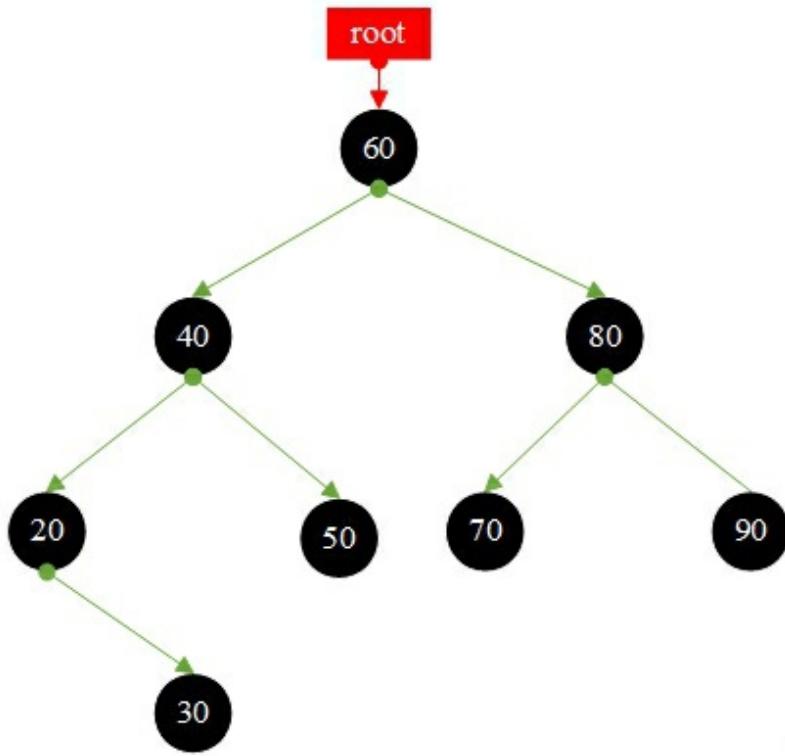
## 6. binary search tree **Delete Node**

Binary search tree delete node 3 cases

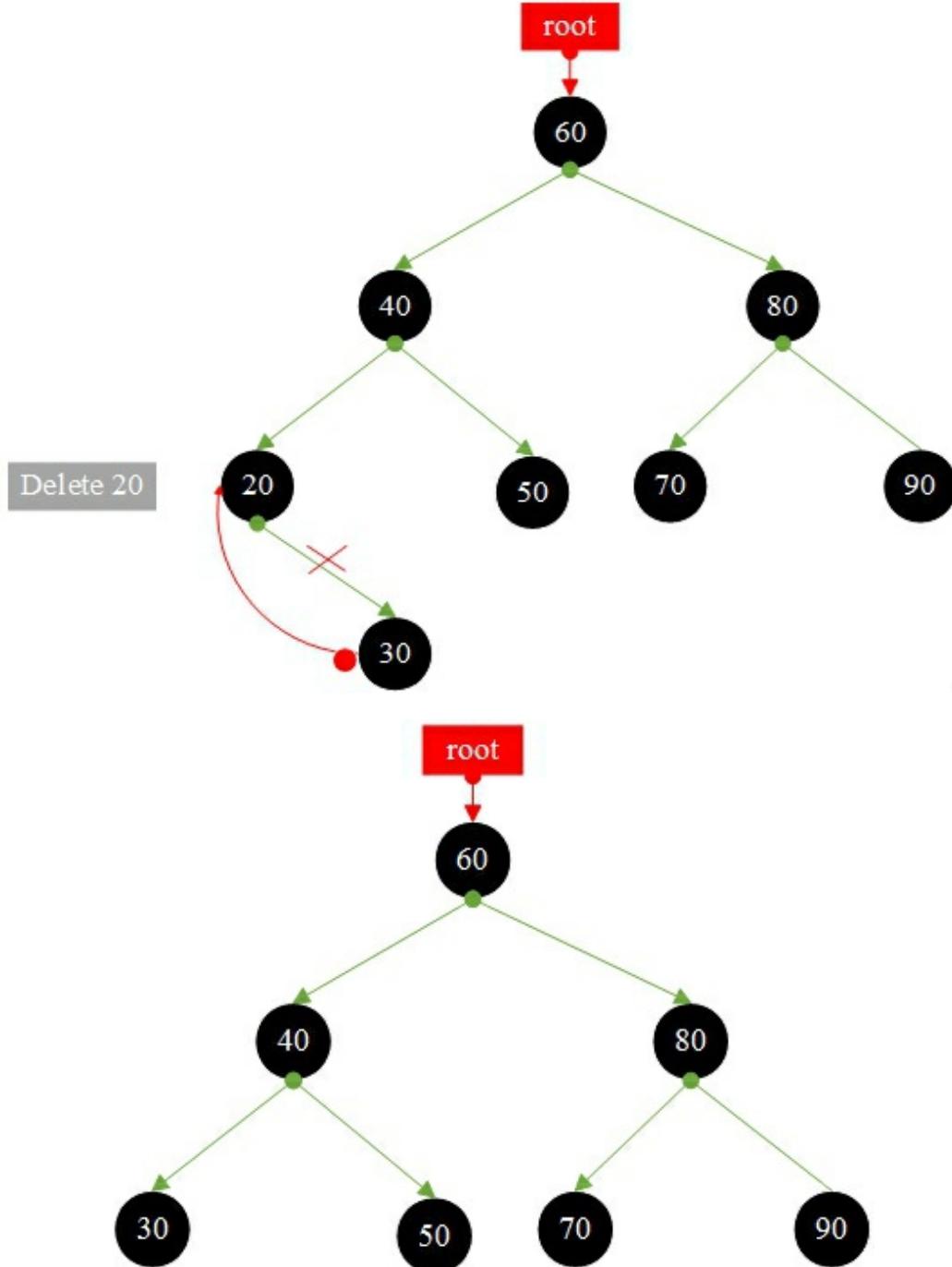
1. If there is no child node, delete it directly
2. If there is only one child node, the child node replaces the current node, and then deletes the current node.
3. If there are two child nodes, replace the current node with the smallest node from the right subtree, because the smallest node on the right is also larger than the value on the left.

### 1. If there is no child node, delete it directly: **delete node 10**

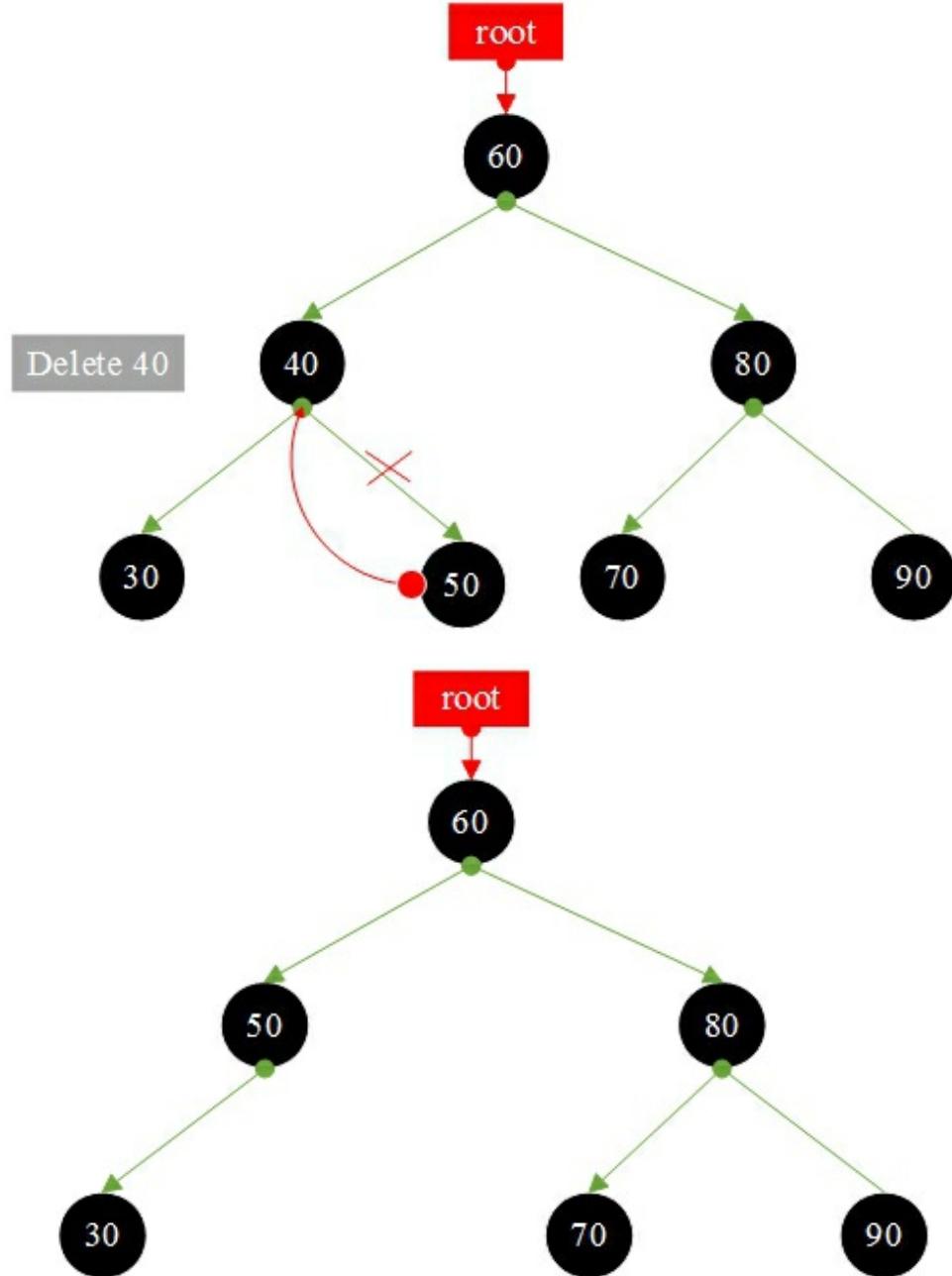




**2. If there is only one child node, the child node replaces the current node, and then deletes the current node. Delete node 20**



**3. If there are two child nodes, replace the current node with the smallest node from the right subtree, Delete node 40**



## Create a **TestBinarySearchTreeDelete.html** with **Notepad**

```
<script type="text/javascript">
class BinaryTree {
    getRoot() {
        return this.root;
    }

    // In-order traversal binary search tree
    inOrder(root) {
        if (root == null) {
            return;
        }
        this.inOrder(root.left); // Traversing the left subtree
        document.write(root.getData() + ", ");
        this.inOrder(root.right); // Traversing the right subtree
    }

    remove(node, newData) {
        if (node == null)
            return node;
        var compareValue = newData - node.getData();
        if (compareValue > 0) {
            node.right = this.remove(node.right, newData);
        } else if (compareValue < 0) {
            node.left = this.remove(node.left, newData);
        } else if (node.left != null && node.right != null) {
            //Find the minimum node of the right subtree to replace the
            current node
            node.setData(this.searchMinValue(node.right).getData());
            node.right = this.remove(node.right, node.getData());
        } else {
            node = (node.left != null) ? node.left : node.right;
        }
        return node;
    }
}
```

```

//Search minimum
searchMinValue(node) {
    if (node == null || node.getData() == 0)
        return null;
    if (node.left == null) {
        return node;
    }
    //Recursively find the minimum from the left subtree
    return this.searchMinValue(node.left);
}

insert(node, newData) {
    if (this.root == null) {
        this.root = new Node(newData, null, null);
        return;
    }
    var compareValue = newData - node.getData();
    //Recursive left subtree, continue to find the insertion position
    if (compareValue < 0) {
        if (node.left == null) {
            node.left = new Node(newData, null, null);
        } else {
            this.insert(node.left, newData);
        }
    } else if (compareValue > 0) {///Recursive right subtree,
        continue to find the insertion position
        if (node.right == null) {
            node.right = new Node(newData, null, null);
        } else {
            this.insert(node.right, newData);
        }
    }
}

```

```

class Node{
    constructor(data, left, right){
        this.data = data;
        this.left = left;
        this.right = right;
    }

    getData(){
        return this.data;
    }
    setData(data){
        this.data = data;
    }
}

//////////testing//////////
var binaryTree=new BinaryTree();

//Constructing a binary search tree
binaryTree.insert(binaryTree.getRoot(), 60);
binaryTree.insert(binaryTree.getRoot(), 40);
binaryTree.insert(binaryTree.getRoot(), 20);
binaryTree.insert(binaryTree.getRoot(), 10);
binaryTree.insert(binaryTree.getRoot(), 30);
binaryTree.insert(binaryTree.getRoot(), 50);
binaryTree.insert(binaryTree.getRoot(), 80);
binaryTree.insert(binaryTree.getRoot(), 70);
binaryTree.insert(binaryTree.getRoot(), 90);

document.write("<br>delete node is: 10 <br>");
binaryTree.remove(binaryTree.getRoot(), 10);

document.write("<br>In-order traversal binary tree <br>");
binaryTree.inOrder(binaryTree.getRoot());

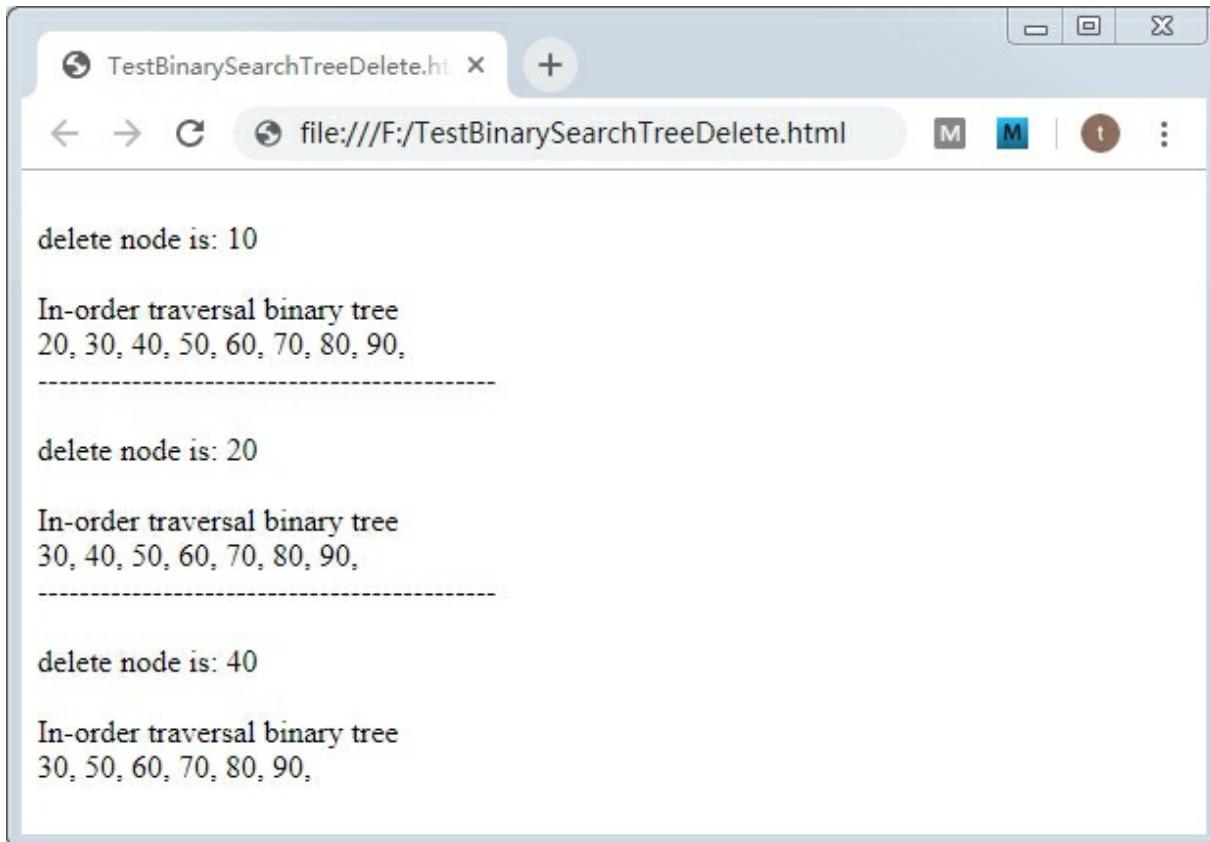
document.write("<br>-----<br>");

document.write("<br>delete node is: 20<br>");
binaryTree.remove(binaryTree.getRoot(), 20);

```

```
document.write("<br>In-order traversal binary tree<br>");  
binaryTree.inOrder(binaryTree.getRoot());  
  
document.write("<br>-----<br>");  
  
document.write("<br>delete node is: 40<br>");  
binaryTree.remove(binaryTree.getRoot(), 40);  
  
document.write("<br>In-order traversal binary tree<br>");  
binaryTree.inOrder(binaryTree.getRoot());  
</script>
```

## Result:



# Binary Heap Sorting

## Binary Heap Sorting:

The value of the non-terminal node in the binary tree is not greater than the value of its left and right child nodes.

Small top heap :  $k_i \leq k_{2i}$  and  $k_i \leq k_{2i+1}$

Big top heap :  $k_i \geq k_{2i}$  and  $k_i \geq k_{2i+1}$

Parent node subscript =  $(i-1)/2$

Left subnode subscript =  $2*i+1$

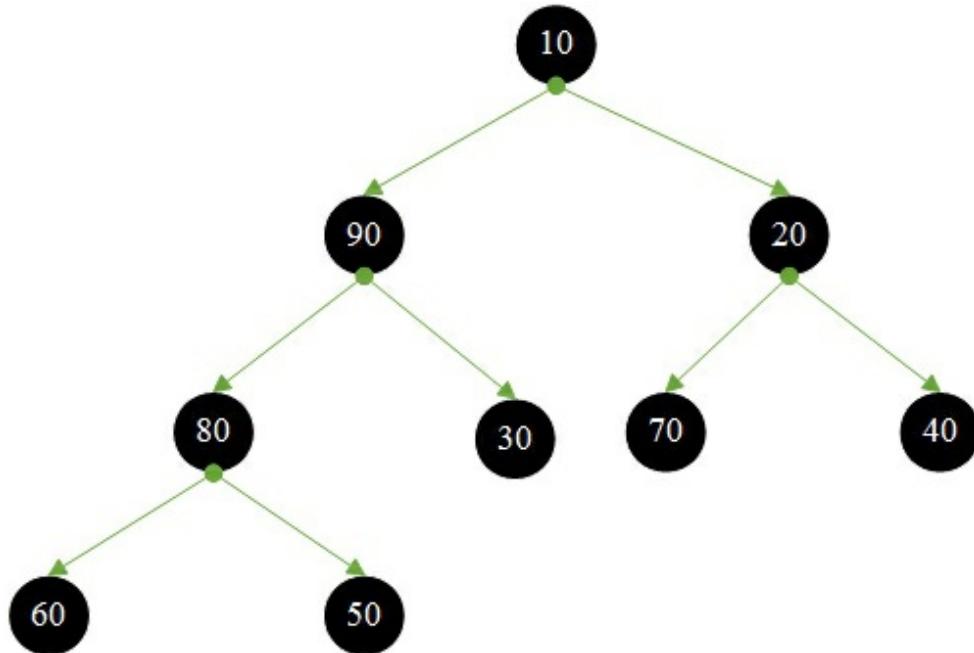
Right subnode subscript =  $2*i+2$

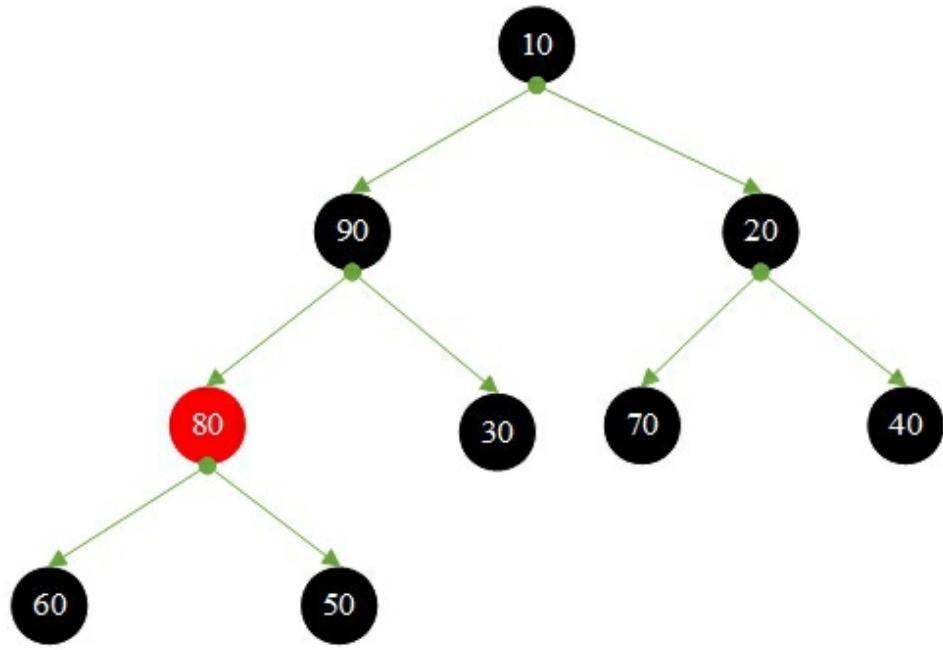
## Heap sorting process:

1. Build a heap
2. After outputting the top element of the heap, adjust from top to bottom, compare the top element with the root node of its left and right subtrees, and swap the smallest element to the top of the heap; then adjust continuously until the leaf nodes to get new heap.

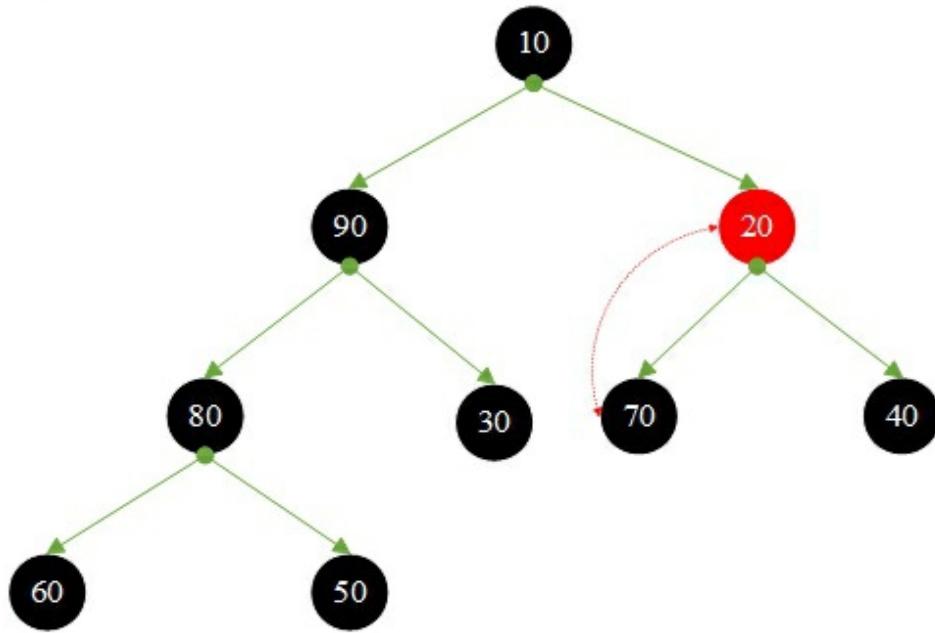
**1. {10, 90, 20, 80, 30, 70, 40, 60, 50} build heap and then heap sort output.**

**Initialize the heap and build the heap**

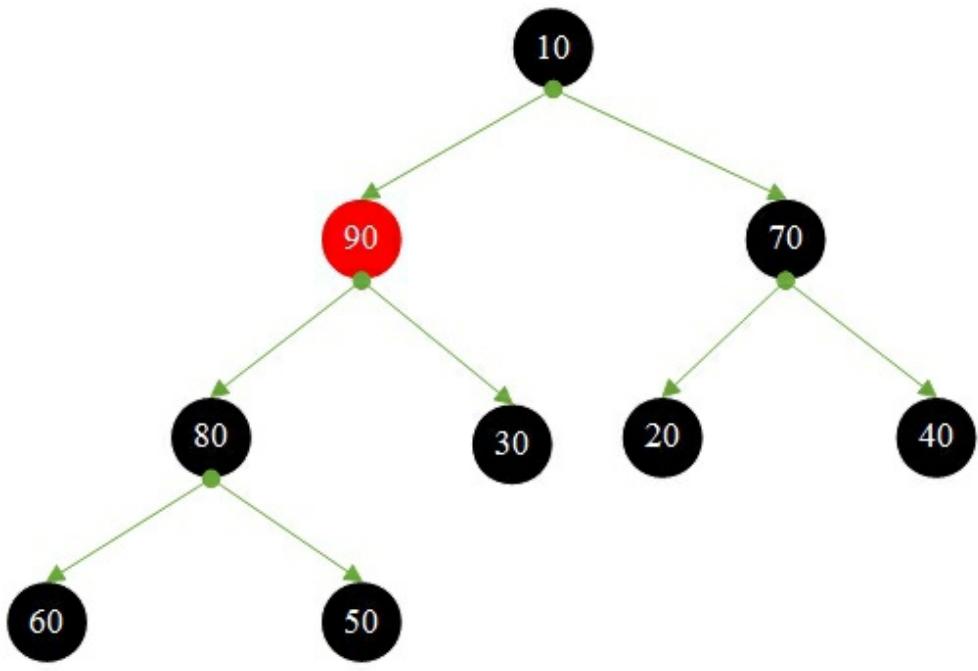




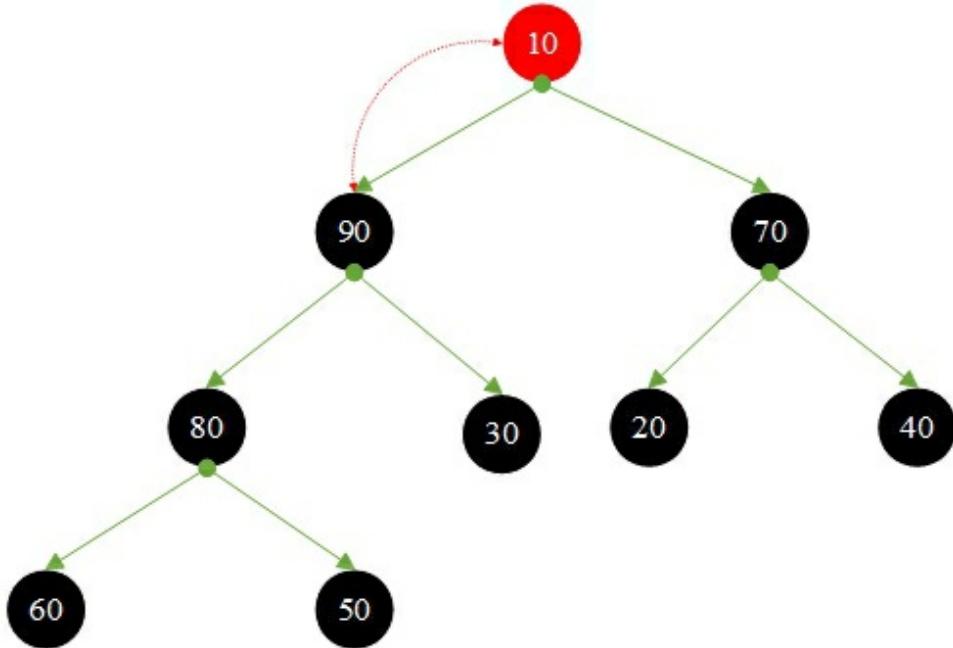
Not Leaf Node = 80 > left = 60 , 80 > right = 50 No need to move



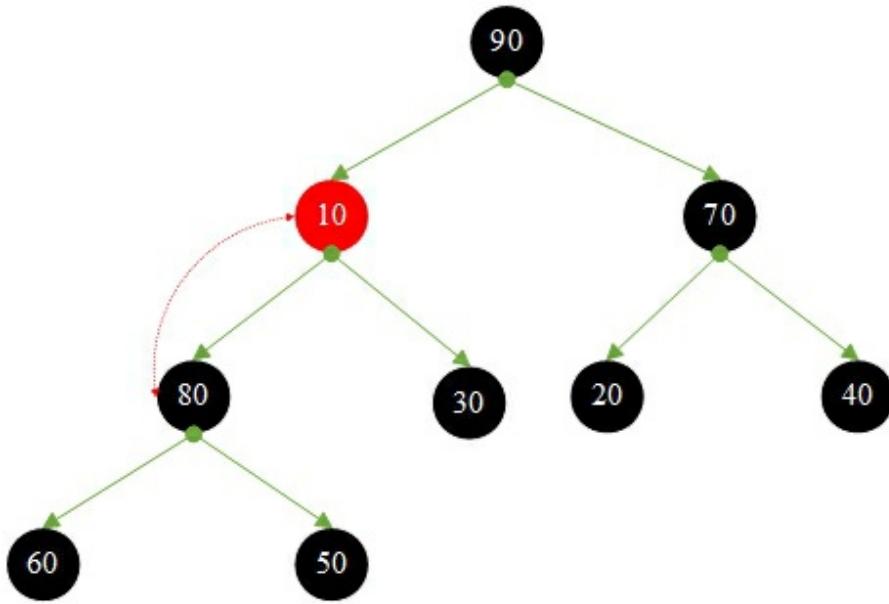
Not Leaf Node = 20 < left = 70 , 70 > right = 40 , 20 swap with 70



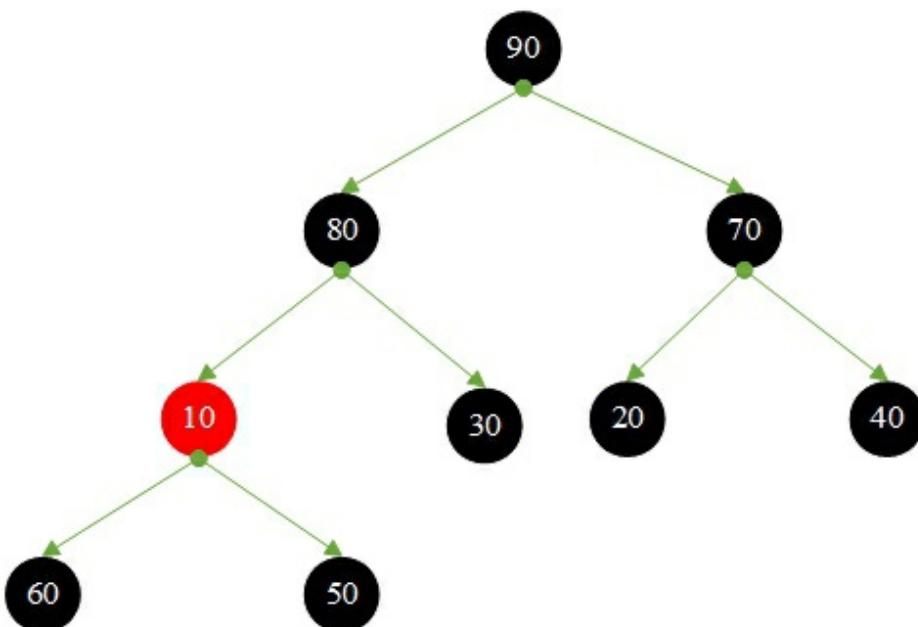
Not Leaf Node = 90 > left = 80 , 80 > right = 30 No need to move



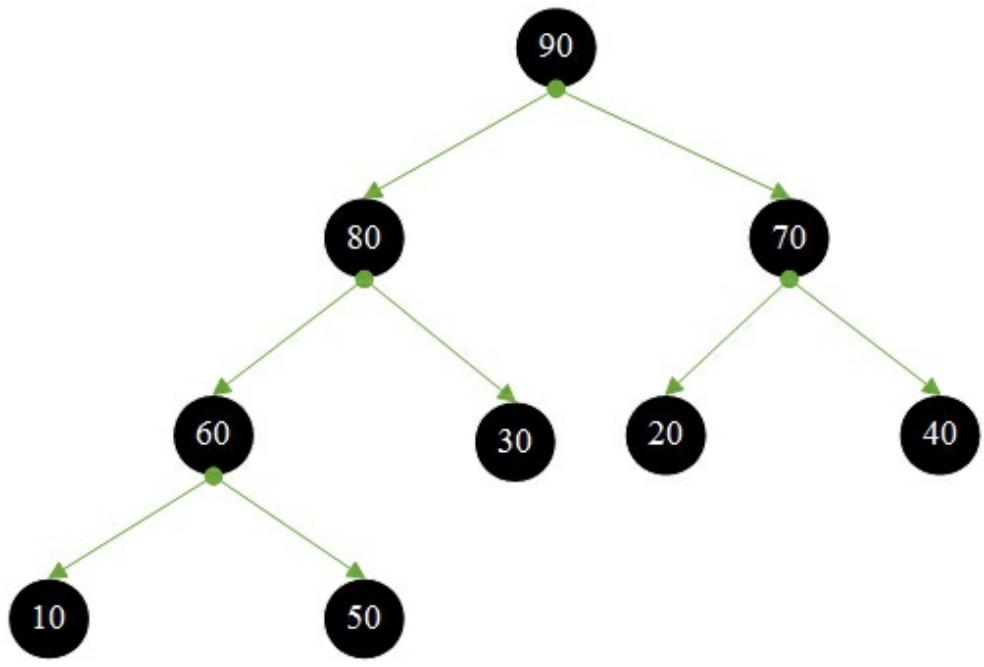
Not Leaf Node = 10 < left = 90 , 90 > right = 70 , 10 swap with 90



Still Not Leaf Node = 10 < left = 80 , 80 > right =30 , 10 swap with 80

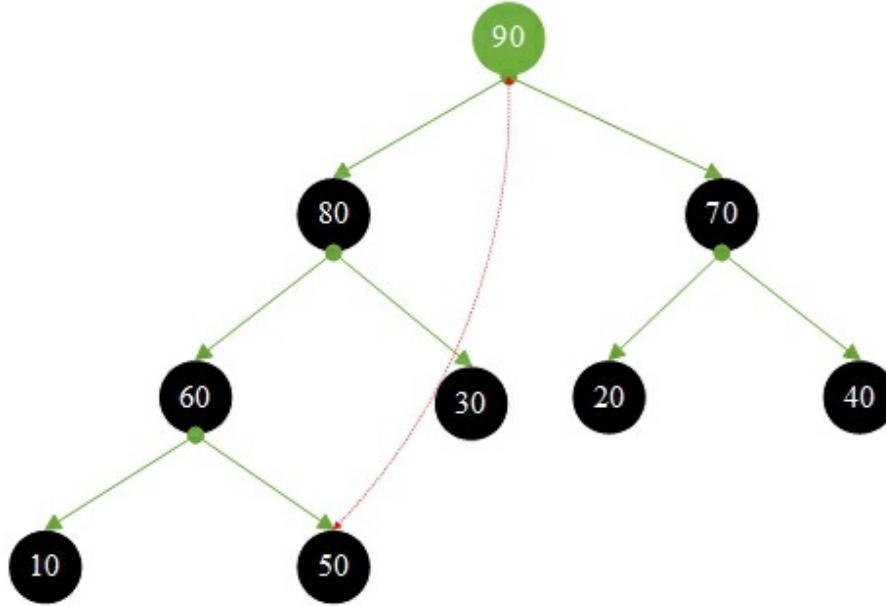


Still Not Leaf Node = 10 < left = 60 , 60 > right =50 , 10 swap with 60

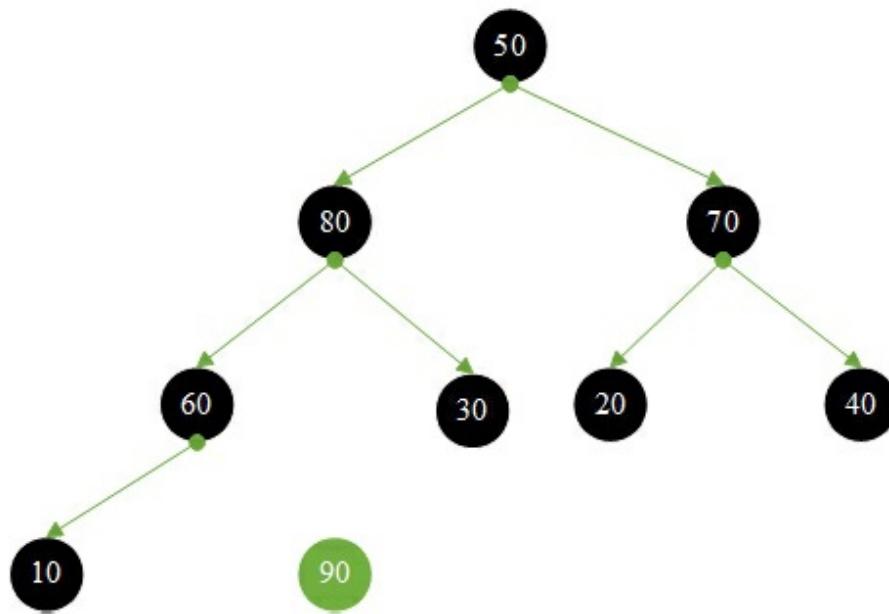


**Create the heap finished**

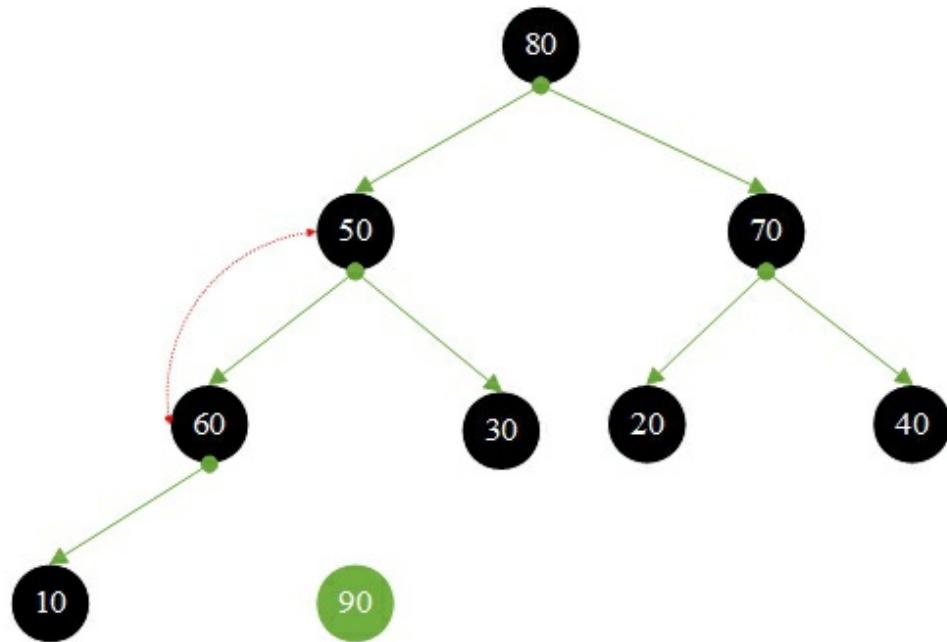
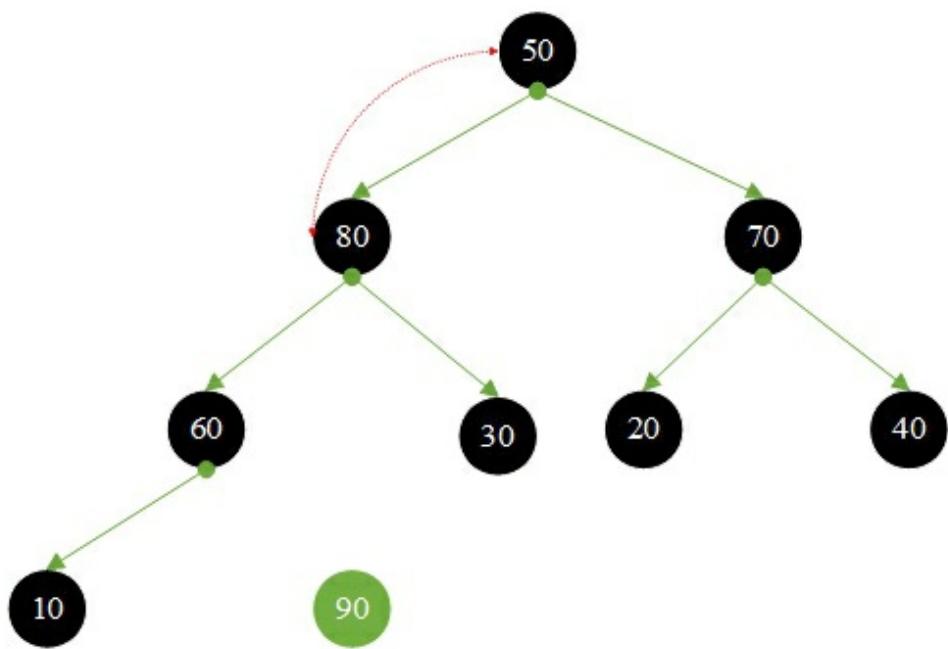
## 2. Start heap sorting

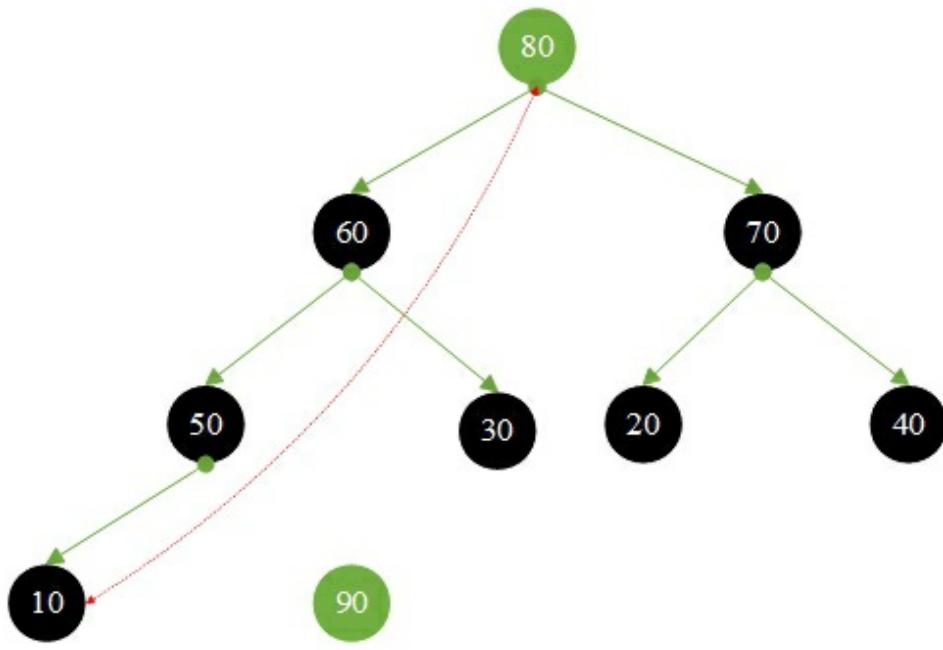


root = 90 and tail = 50 are exchanged

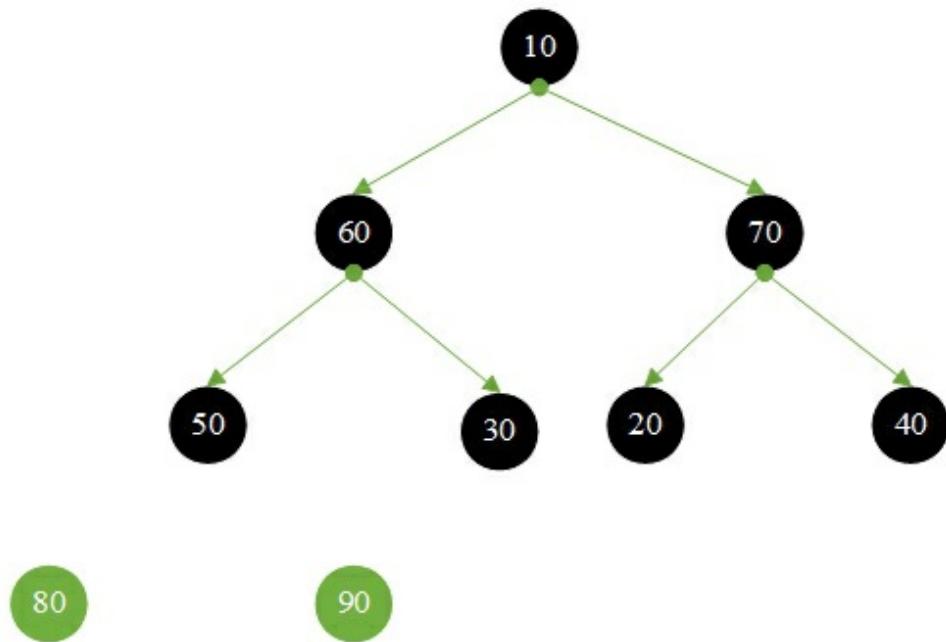


adjust the heap

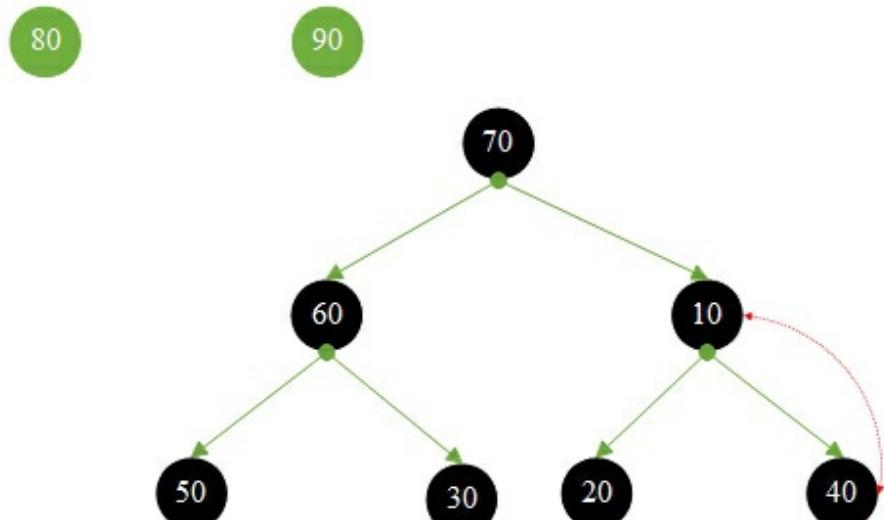
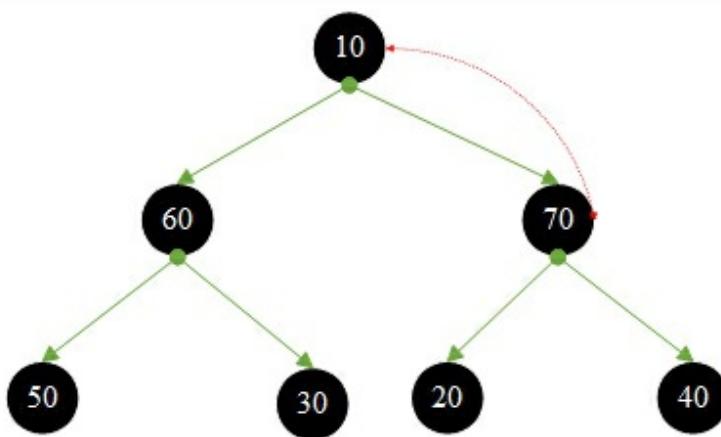


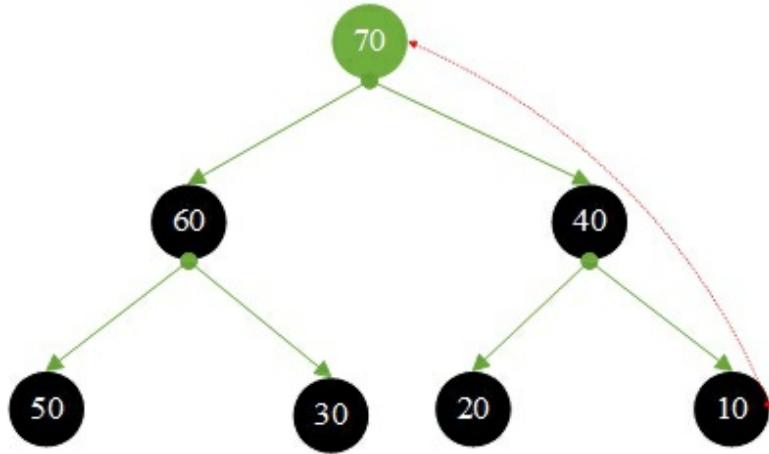


root = 80 and tail = 10 are exchanged

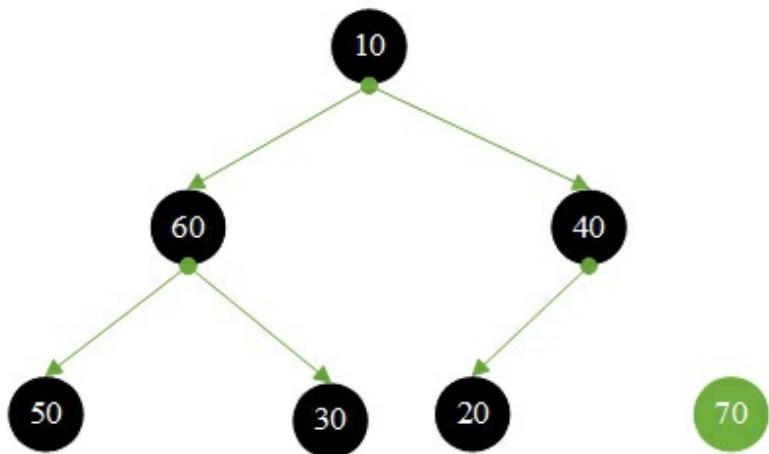


adjust the heap

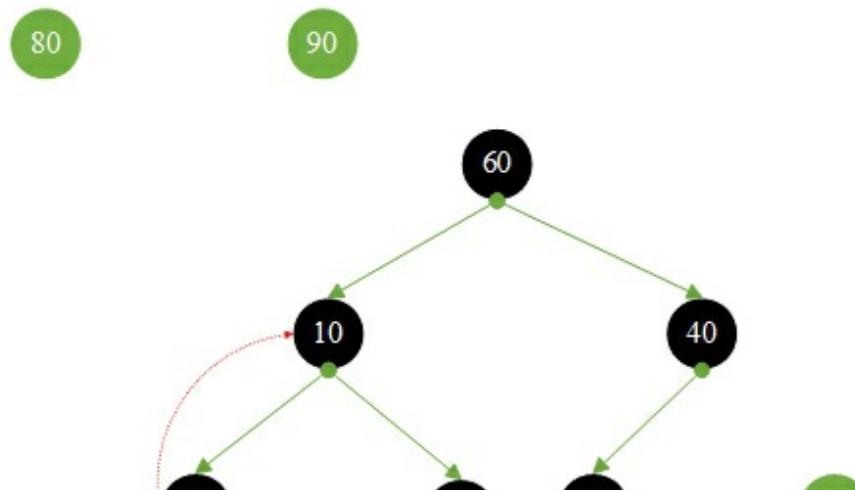
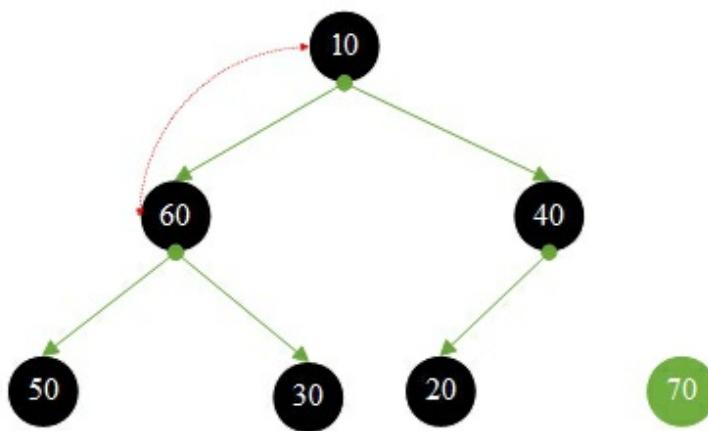


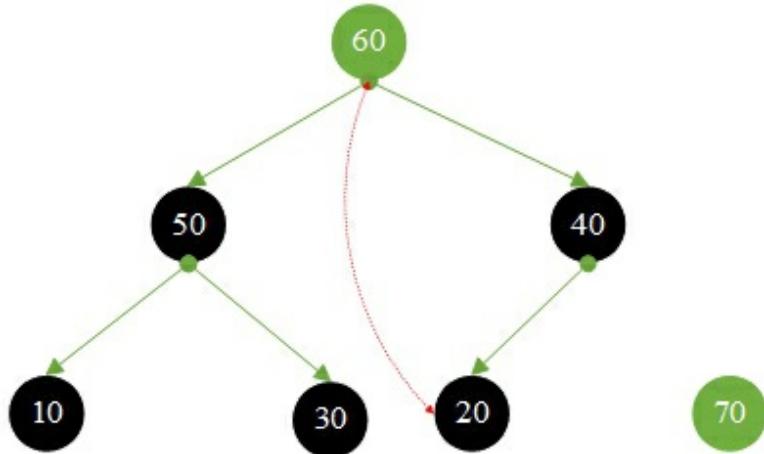


root = 70 and tail = 10 are exchanged

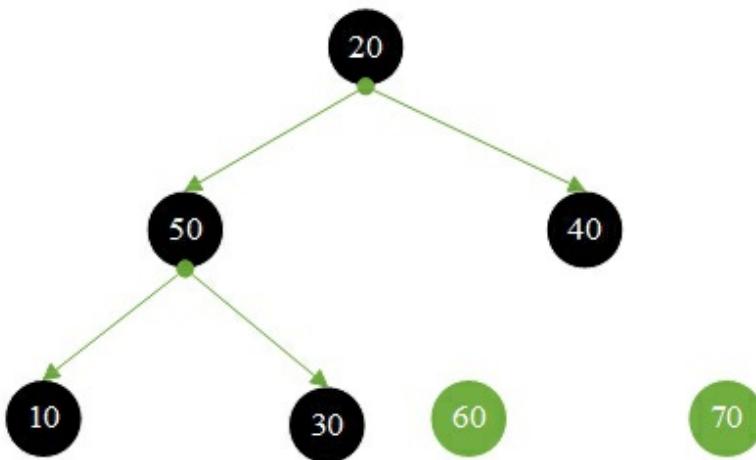


adjust the heap





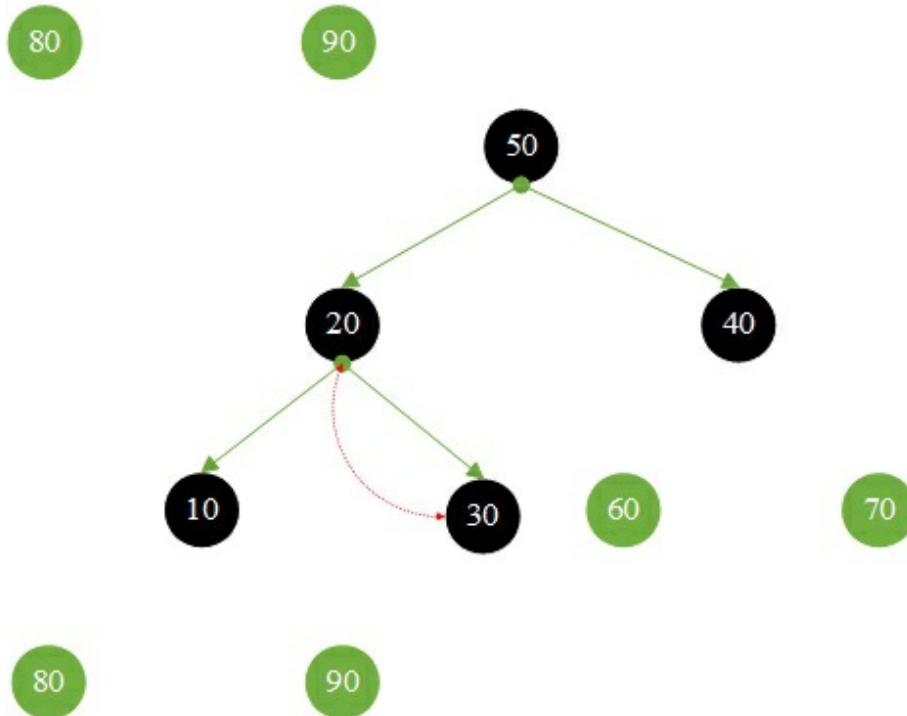
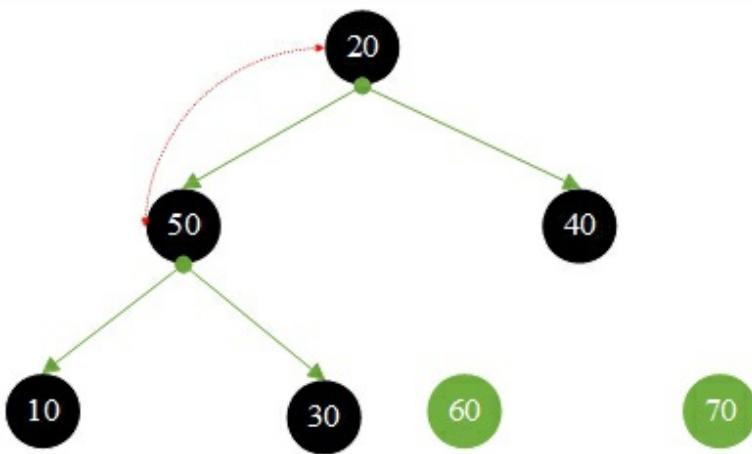
root = 60 and tail = 20 are exchanged

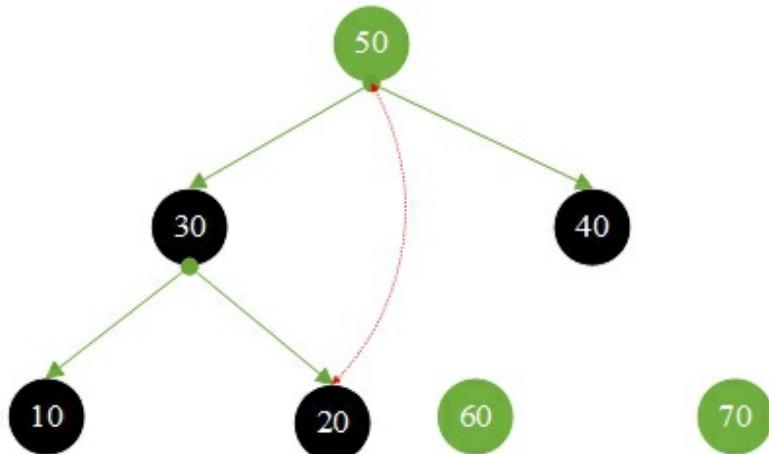


80  
90

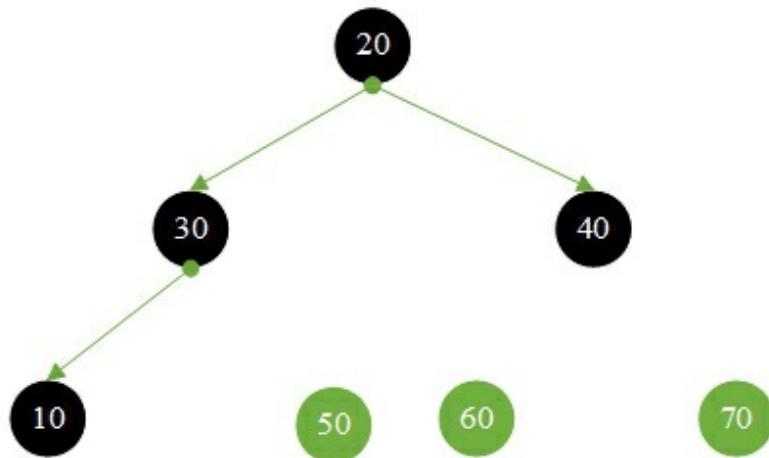
60  
70

adjust the heap



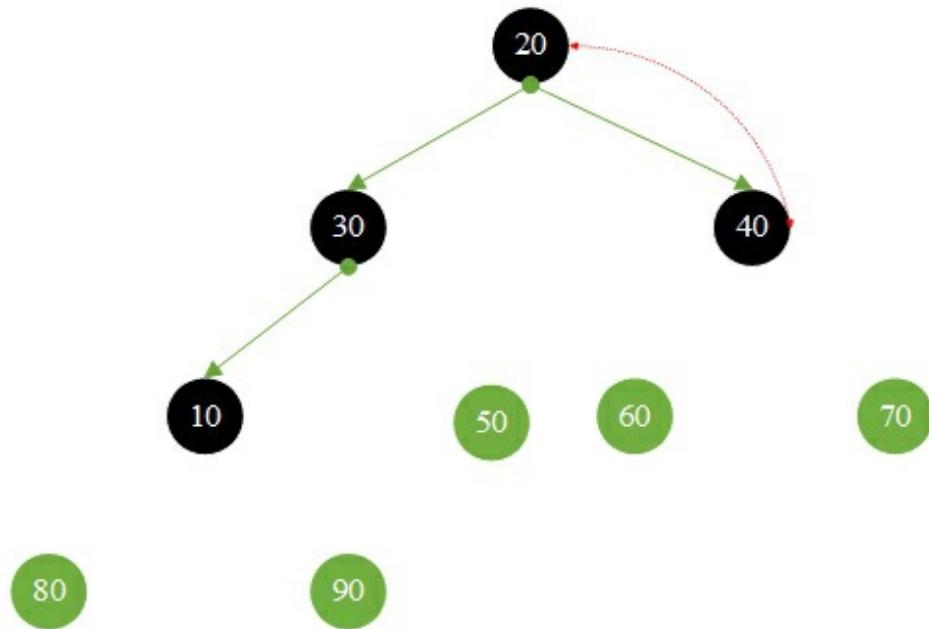


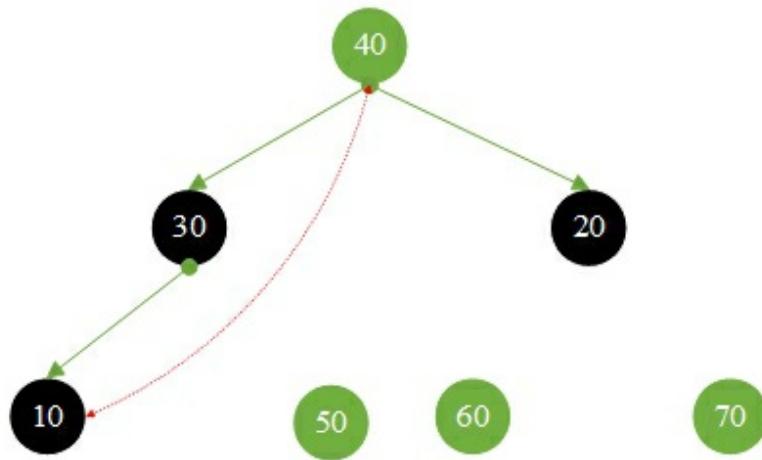
root = 50 and tail = 20 are exchanged



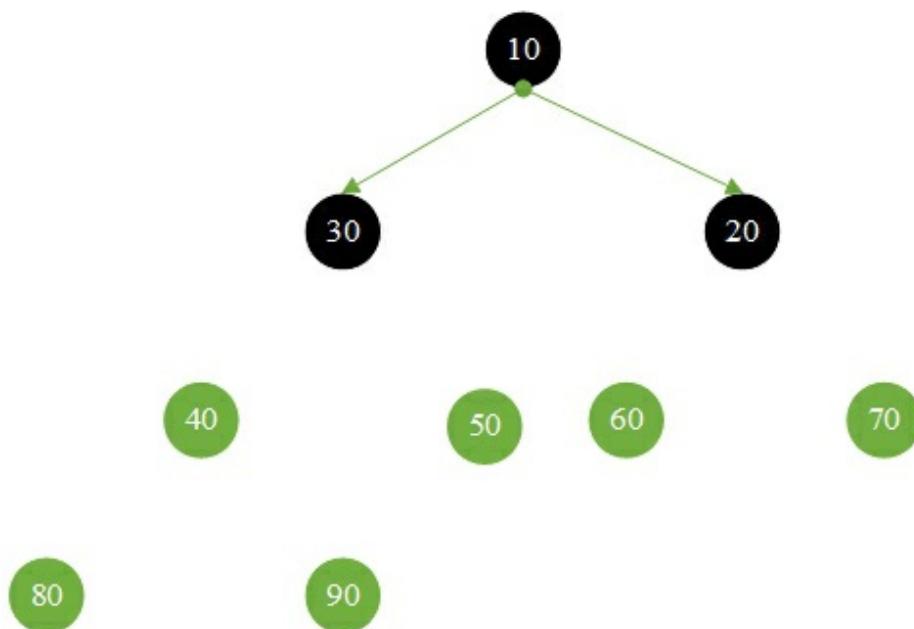
80  
90

adjust the heap

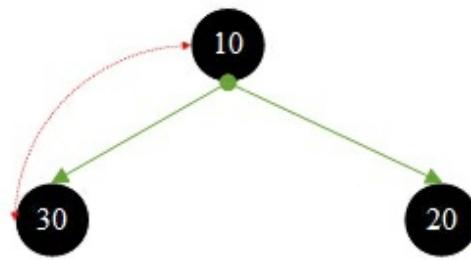




root = 40 and tail = 10 are exchanged



adjust the heap



40

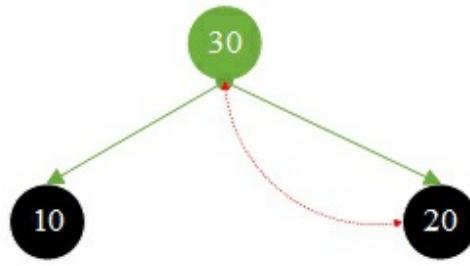
50

60

70

80

90

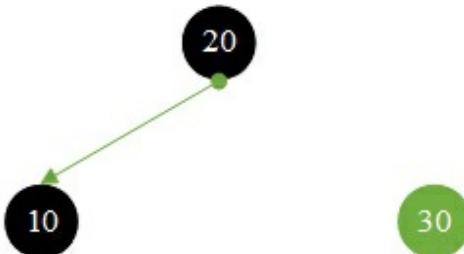


40                  50                  60                  70

80

90

root = 30 and tail = 20 are exchanged

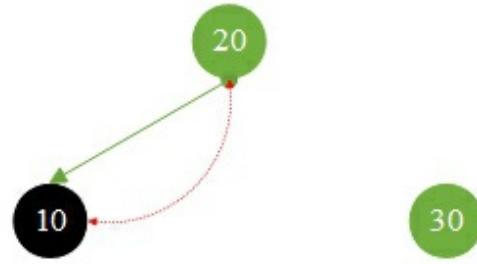


40                  50                  60                  70

80

90

no need adjust the heap



root = 20 and tail = 10 are exchanged



## Heap sort result



Create a **TestBinaryHeapSorting.html** with **Notepad**

```
<script type="text/javascript">
class HeapSort {
    constructor(){
        this.array = [];
    }

    //Initialize the heap
    createHeap(array) {
        this.array = array;
        // Build a heap, (array.length - 1) / 2 scan half of the nodes with
        child nodes
        for (var i = (array.length - 1) / 2; i >= 0; i--) {
            this.adjustHeap(i, array.length - 1);
        }
    }

    //Adjustment heap
    adjustHeap(currentIndex, maxLength) {
        var noLeafValue = this.array[currentIndex]; // Current non-leaf
node

        //2 * currentIndex + 1 Current left subtree subscript
        for (var j = 2 * currentIndex + 1; j <= maxLength; j =
currentIndex * 2 + 1) {
            if (j < maxLength && this.array[j] < this.array[j + 1]) {
                j++; // j Large subscript
            }
            if (noLeafValue >= this.array[j]) {
                break;
            }
            this.array[currentIndex] = this.array[j]; // Move up to the
```

```
parent node
    currentIndex = j;
}
this.array[currentIndex] = noLeafValue; // To put in the position
}
```

```
heapSort() {
    for (var i = this.array.length - 1; i > 0; i--) {
        var temp = this.array[0];
        this.array[0] = this.array[i];
        this.array[i] = temp;
        this.adjustHeap(0, i - 1);
    }
}
```

```
//////////testing//////////
```

```
var heapSort = new HeapSort();
var scores = [ 10, 90, 20, 80, 30, 70, 40, 60, 50 ];
```

```
document.write("Before building a heap : <br>");
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ", ");
}
document.write("<br><br>");

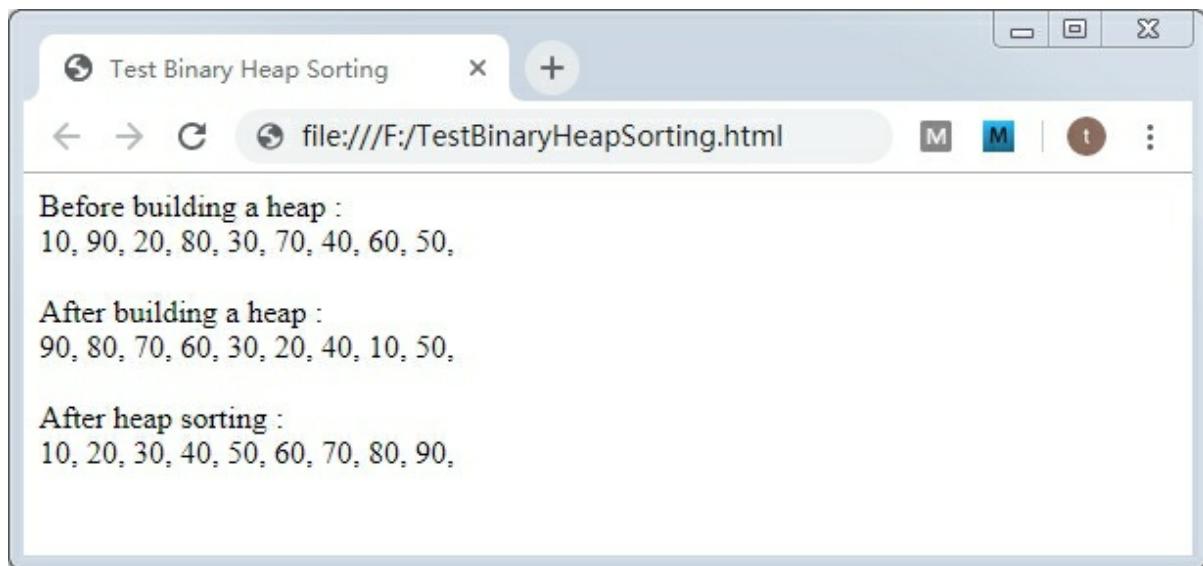
//////////
```

```
document.write("After building a heap : <br>");
heapSort.createHeap(scores);
for (var i = 0; i < scores.length; i++) {
    document.write(scores[i] + ", ");
}
document.write("<br><br>");

//////////
```

```
document.write("After heap sorting : <br>");  
heapSort.heapSort();  
for (var i = 0; i < scores.length; i++) {  
    document.write(scores[i] + ", ");  
}  
</script>
```

## Result:

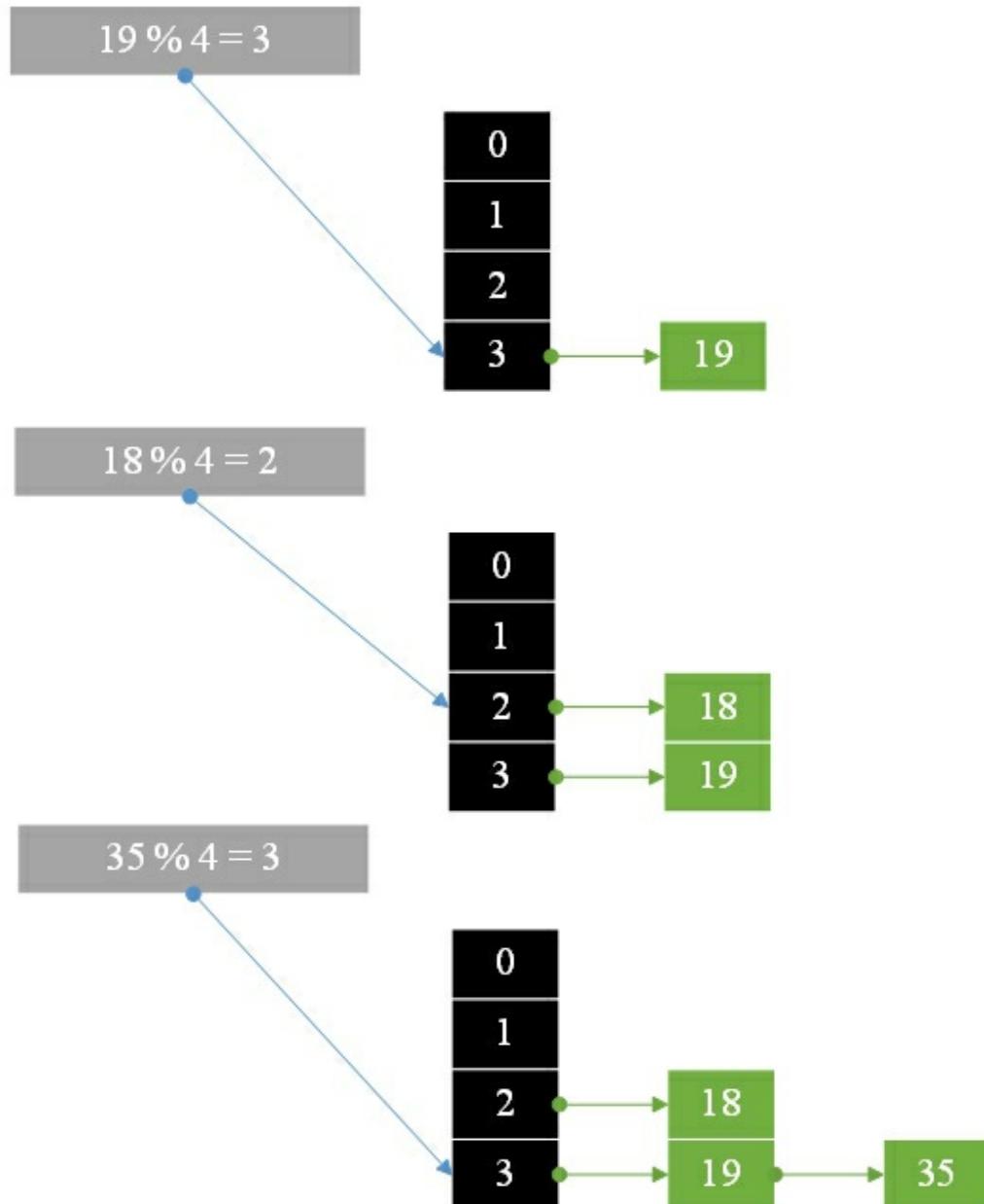


# Hash Table

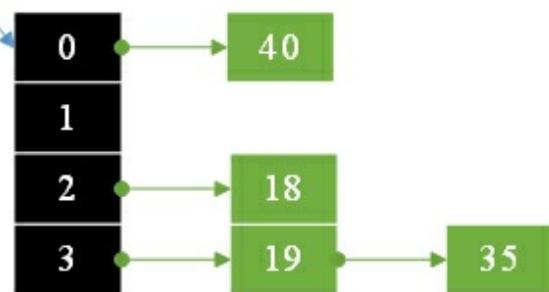
## Hash Table:

Access by mapping key => values in the table.

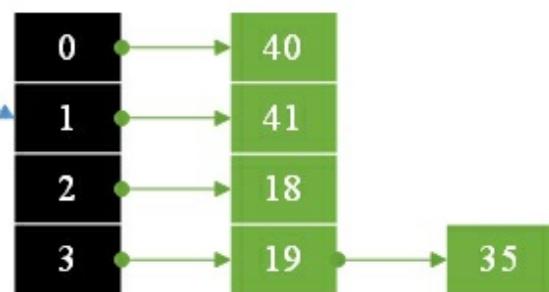
### 1. Map {19, 18, 35, 40, 41, 42} to the HashTable mapping rule $\text{key \% 4}$



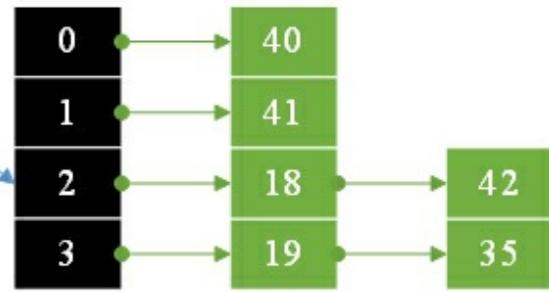
$$40 \% 4 = 0$$



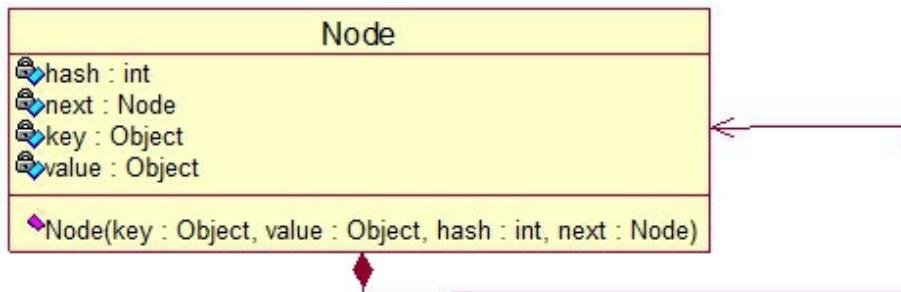
$$41 \% 4 = 1$$



$$42 \% 4 = 2$$



## 2. Implement a Hashtable



Create a **TestHashtable.html** with **Notepad**

```
<script type="text/javascript">
class Node {
    constructor(key, value, hash, next){
        this.key = key;
        this.value = value;
        this.hash = hash;
        this.next = next;
    }

    getKey() {
        return this.key;
    }
    setKey(key) {
        this.key = key;
    }

    getValue() {
        return this.value;
    }
    setValue(value) {
        this.value = value;
    }

    getHash() {
        return this.hash;
    }
    setHash(hash) {
        this.hash = hash;
    }
}
```

```
        }
    }

class Hashtable {
    constructor(){
        this.capacity = 16;
        this.table = new Array(this.capacity);
        this.size = 0;
    }

    size() {
        return this.size;
    }

    isEmpty() {
        return this.size == 0 ? true : false;
    }

    hash(key) {
        var hash = 0;
        for (var i = 0; i < key.length; i++) {
            hash += key.charCodeAt(i);
        }
        return hash % 37;
    }

    //Calculate the hash value according to the key hash algorithm
    hashCode(key) {
        var avg = this.hash(key) * (Math.pow(5, 0.5) - 1) / 2 //hash
        policy for middle-square method
        var numeric = avg - Math.floor(avg)
        return parseInt(Math.floor(numeric * this.table.length))
    }
}
```

```
put(key, value) {
    if (key == null) {
        throw new IllegalArgumentException();
    }

    var hash = this.hashCode(key);
    var newNode = new Node(key, value, hash, null);
    var node = table[hash];
    while (node != null) {
        if (node.getKey().equals(key)) {
            node.setValue(value);
            return;
        }
        node = node.next;
    }
    newNode.next = this.table[hash];
    this.table[hash] = newNode;
    this.size++;
}

get(key) {
    if (key == null) {
        return null;
    }

    var hash = this.hashCode(key);
    var node = this.table[hash];
    while (node != null) {//Get value according to key
        if (node.getKey() == key) {
            return node.getValue();
        }
        node = node.next;
    }
    return null;
}
}
```

```
//////////////////testing////////////////  
var table = new Hashtable();  
  
table.put("david", "Good Boy Keep Going");  
table.put("grace", "Cute Girl Keep Going");  
  
document.write("david => " + table.get("david") + "<br>");  
document.write("grace => " + table.get("grace") + "<br>");  
  
</script>
```

### Result:

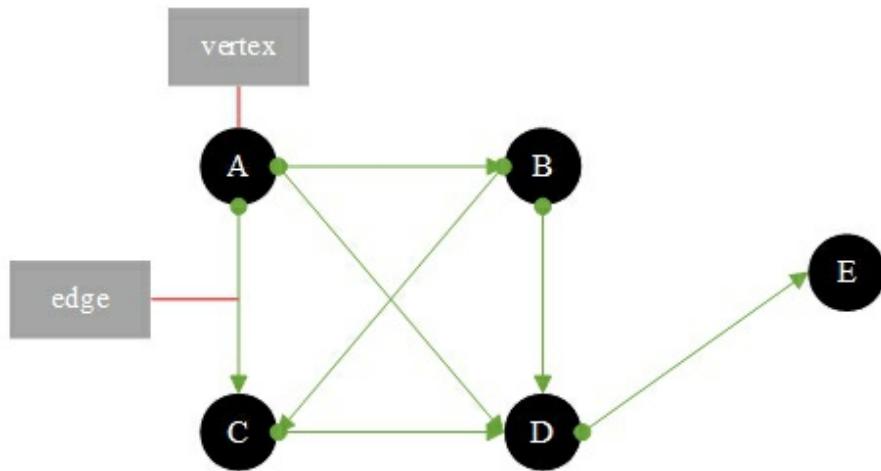


# Directed Graph and Depth-First Search

## Directed Graph:

The data structure is represented by an adjacency matrix (that is, a two-dimensional array) and an adjacency list. Each node is called a vertex, and two adjacent nodes are called edges.

**Directed Graph** has direction : A -> B and B -> A are different



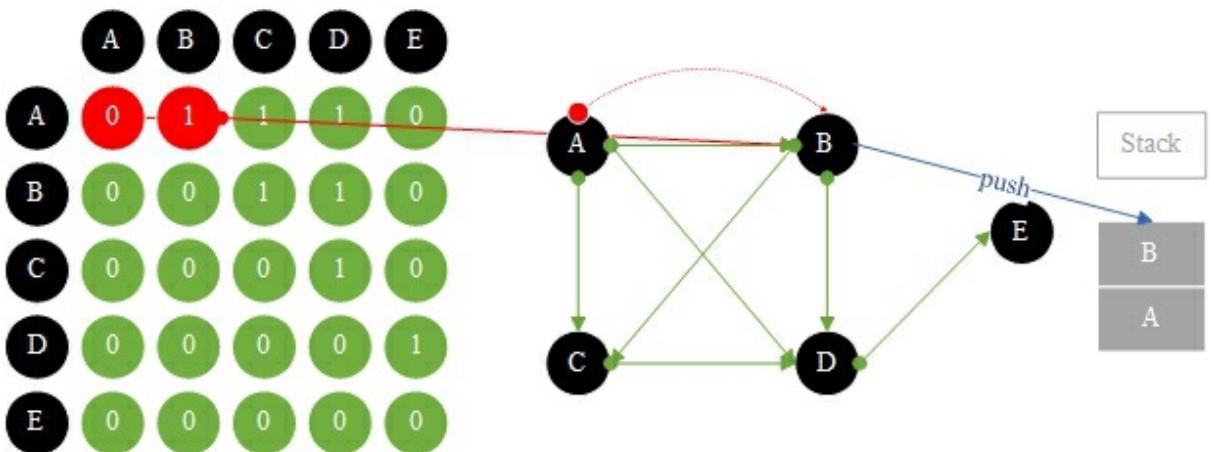
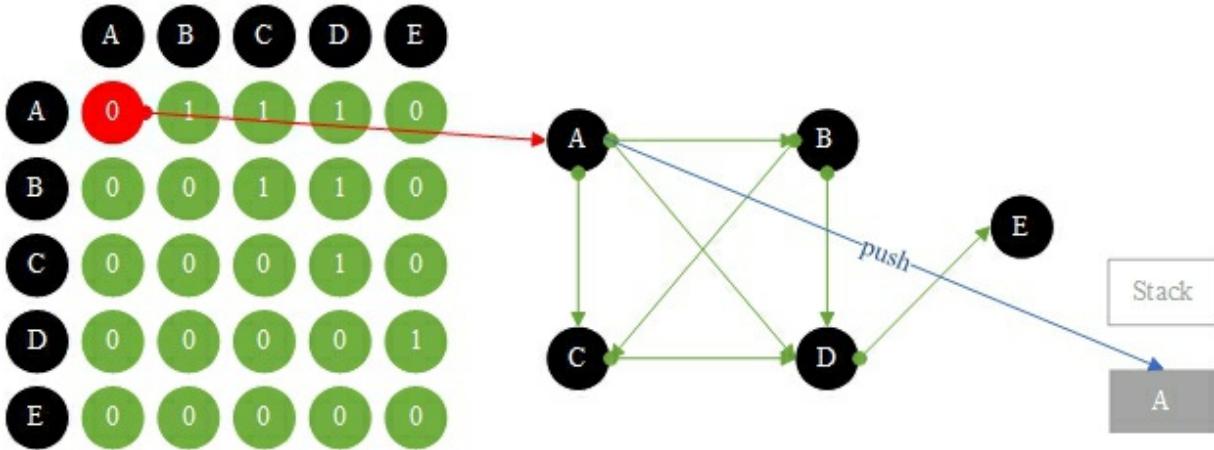
## 1. The adjacency matrix is described above:

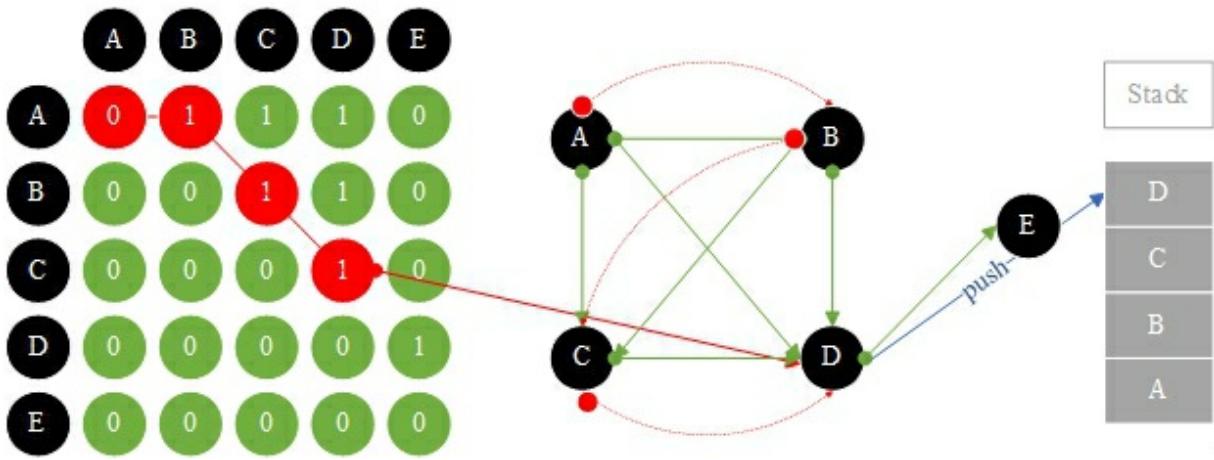
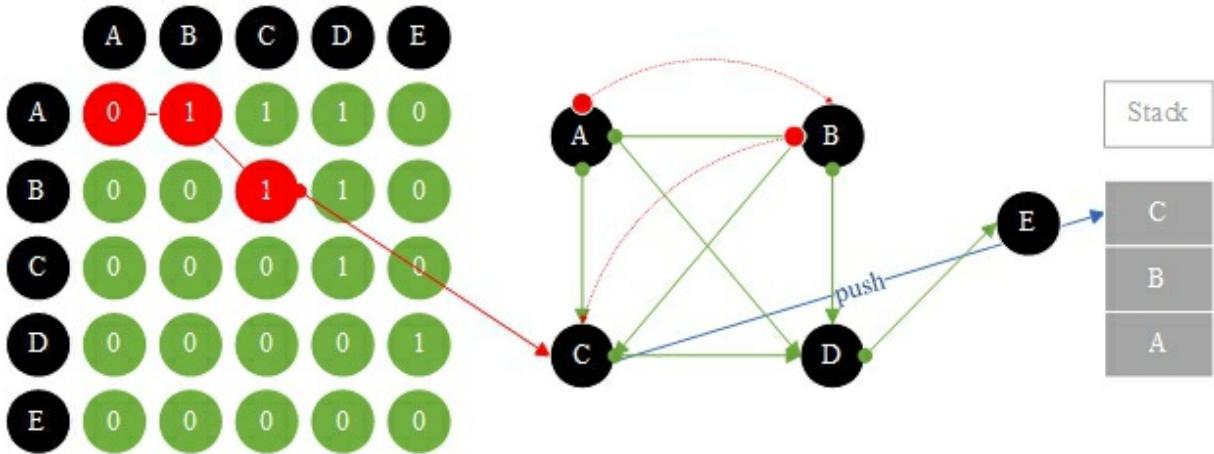
The total number of vertices is a two-dimensional array size, if have value of the edge is 1, otherwise no value of the edge is 0.

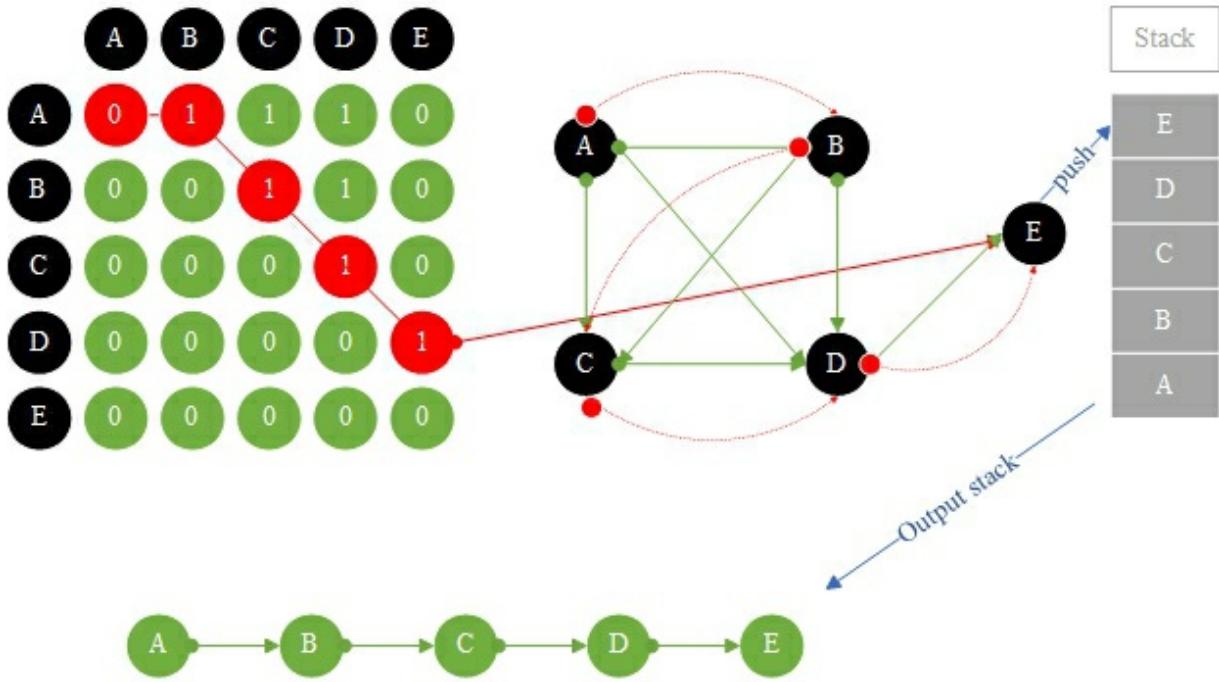
	A	B	C	D	E
A	0	1	1	1	0
B	0	0	1	1	0
C	0	0	0	1	0
D	0	0	0	0	1
E	0	0	0	0	0

## 2. Depth-First Search:

Look for the neighboring edge node B from A and then find the neighboring node C from B and so on until all nodes are found  $A \rightarrow B \rightarrow C \rightarrow D \rightarrow E$ .







## Create a TestDirectedGraphDepthFrstSearch.html with Notepad

```
<script type="text/javascript">
class Vertex {
    constructor(data, visited){
        this.data = data;
        this.visited = visited; // Have you visited
    }

    getData() {
        return this.data;
    }
    setData(data) {
        this.data = data;
    }

    isVisited() {
        return this.visited;
    }
    setVisited(visited) {
        this.visited = visited;
    }
}
```

```
class Stack {  
    constructor(){  
        this.stacks = new Array();  
        this.top = -1;  
    }  
  
    push(element) {  
        this.top++;  
        this.stacks[this.top] = element;  
    }  
  
    pop() {  
        if(this.top == -1){  
            return -1;  
        }  
  
        var data = this.stacks[this.top];  
        this.top--;  
        return data;  
    }  
  
    peek() {  
        if(this.top == -1){  
            return -1;  
        }  
  
        var data = this.stacks[this.top];  
        return data;  
    }  
  
    isEmpty() {  
        if(this.top <= -1){  
            return true;  
        }  
        return false;  
    }  
}
```

```

class Graph {
    constructor(maxVertexSize){
        this.maxVertexSize = maxVertexSize;// Two-dimensional array
        size
        this.vertexs = new Array(maxVertexSize);
        this.size = 0; // Current vertex size
        this.adjacencyMatrix = new Array(maxVertexSize);
        for (var i = 0; i < maxVertexSize; i++) {
            this.adjacencyMatrix[i] = new Array();
            for (var j = 0; j < maxVertexSize; j++) {
                this.adjacencyMatrix[i][j] = 0;
            }
        }
        this.stack = new Stack();// Stack saves current vertices
    }

    addVertex(data) {
        var vertex = new Vertex(data, false);
        this.vertexs[this.size++] = vertex;
    }

    addEdge(from, to) {
        this.adjacencyMatrix[from][to] = 1; // A -> B and B -> A are
        different
    }

    depthFirstSearch() {
        var firstVertex = this.vertexs[0]; // Start searching from the first
        vertex
        firstVertex.setVisited(true);
        document.write(firstVertex.getData());
        this.stack.push(0);
        while (!this.stack.isEmpty()) {
            var row = this.stack.peek();
            // Get adjacent vertex positions that have not been visited
            var col = this.findAdjacencyUnVisitedVertex(row);
            if (col == -1) {
                this.stack.pop();
            }
        }
    }
}

```

```

} else {
    this.vertexs[col].setVisited(true);
    document.write(" -> " + this.vertexs[col].getData());
    this.stack.push(col);
}
}

this.clear();
}

// Get adjacent vertex positions that have not been visited
findAdjacencyUnVisitedVertex(row) {
    for (var col = 0; col < this.size; col++) {
        if (this.adjacencyMatrix[row][col] == 1 &&
!this.vertexs[col].isVisited()) {
            return col;
        }
    }
    return -1;
}

clear() {
    for (var i = 0; i < this.size; i++) {
        this.vertexs[i].setVisited(false);
    }
}

getAdjacencyMatrix() {
    return this.adjacencyMatrix;
}

getVertexs() {
    return this.vertexs;
}

}

function printGraph(graph) {
    document.write("Two-dimensional array traversal output vertex
edge and adjacent array : <br>");
    document.write(" &nbsp;&nbsp;");
}

```

```

for (var i = 0; i < graph.getVertices().length; i++) {
    document.write(graph.getVertices()[i].getData() +
"&nbsnbsp;&nbsnbsp;&nbsnbsp;" );
}
document.write("<br>");

for (var i = 0; i < graph.getAdjacencyMatrix().length; i++) {
    document.write(graph.getVertices()[i].getData() + " ");
    for (var j = 0; j < graph.getAdjacencyMatrix().length; j++) {
        document.write(graph.getAdjacencyMatrix()[i][j] +
"&nbsnbsp;&nbsnbsp;&nbsnbsp;" );
    }
    document.write("<br>");
}
}

var graph = new Graph(5);
graph.addVertex("A");
graph.addVertex("B");
graph.addVertex("C");
graph.addVertex("D");
graph.addVertex("E");

graph.addEdge(0, 1);
graph.addEdge(0, 2);
graph.addEdge(0, 3);
graph.addEdge(1, 2);
graph.addEdge(1, 3);
graph.addEdge(2, 3);
graph.addEdge(3, 4);

// Two-dimensional array traversal output vertex edge and adjacent
array
printGraph(graph);
document.write("<br>Depth-first search traversal output : <br>");
graph.depthFirstSearch();
</script>

```

## Result:

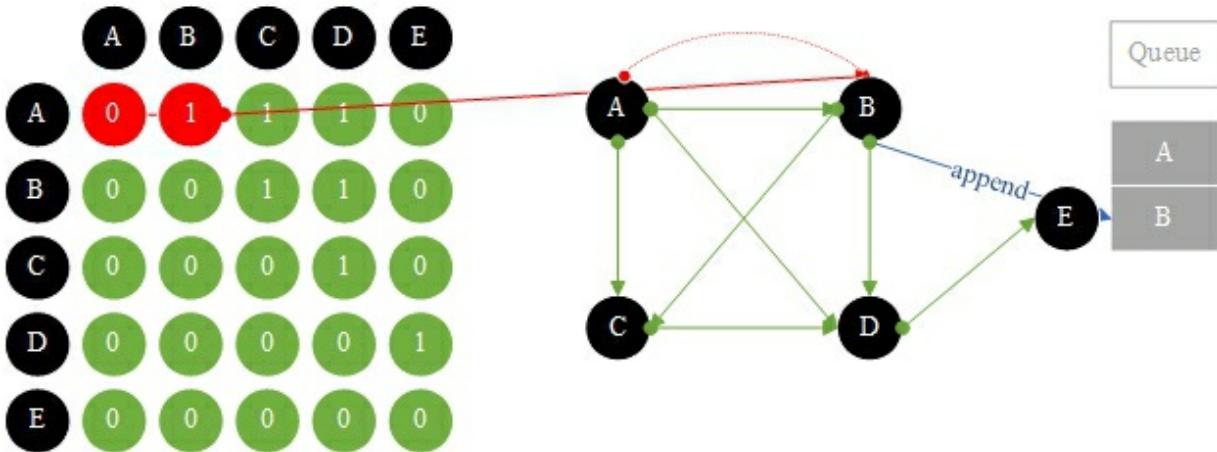
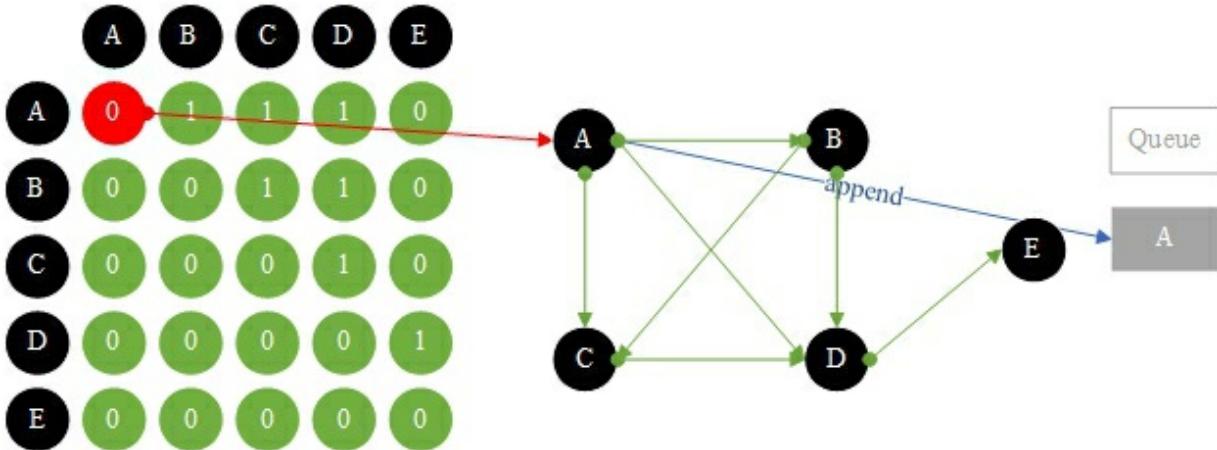
The screenshot shows a Java application window titled "TestDirectedGraphDepthFrstS...". The code output is displayed in the main pane:

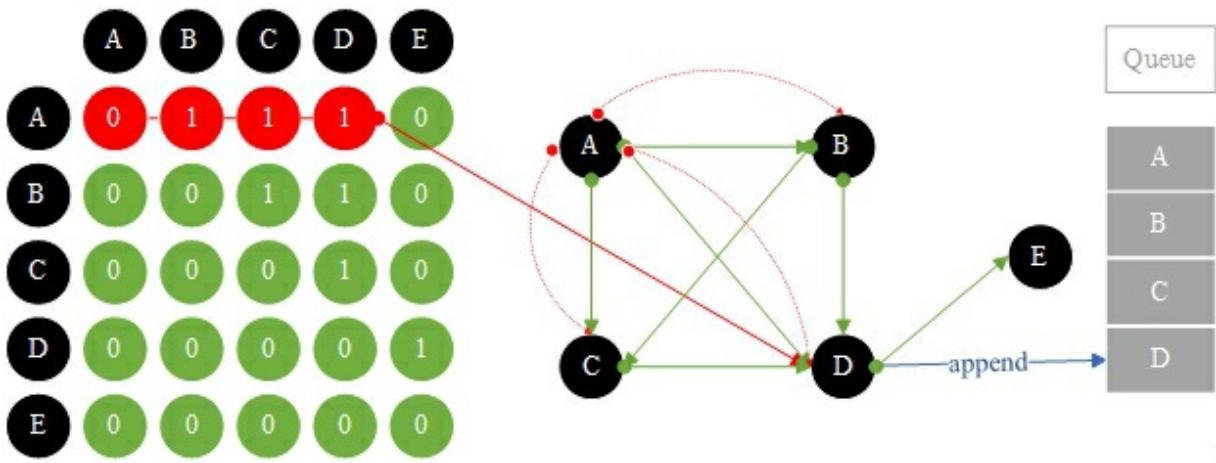
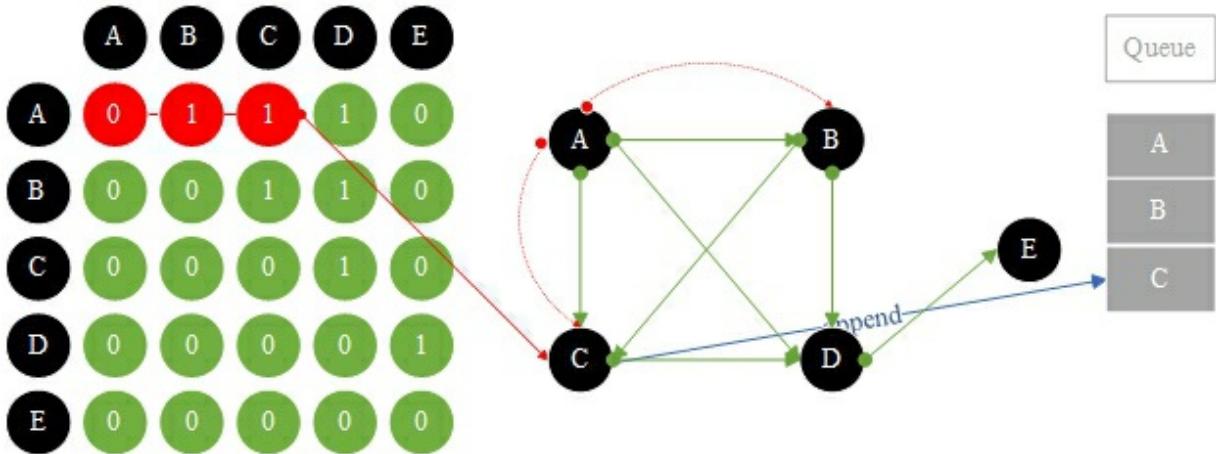
```
Two-dimensional array traversal output vertex edge and adjacent array :  
A B C D E  
A 0 1 1 1 0  
B 0 0 1 1 0  
C 0 0 0 1 0  
D 0 0 0 0 1  
E 0 0 0 0 0  
  
Depth-first search traversal output :  
A -> B -> C -> D -> E
```

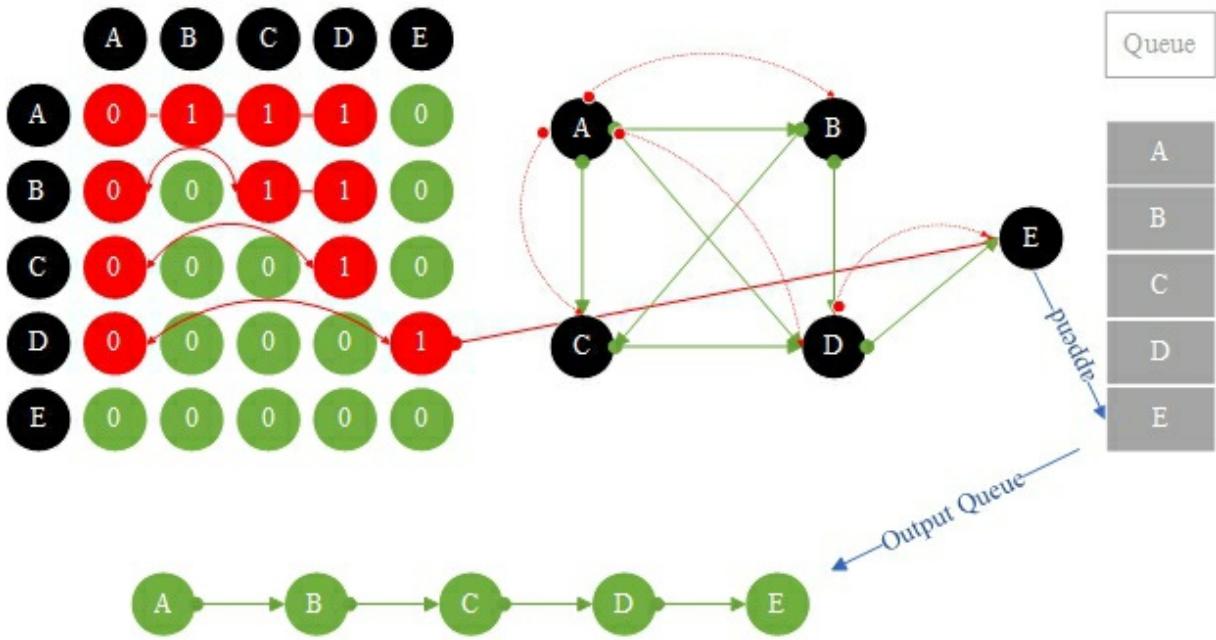
# Directed Graph and Breadth-First Search

## Breadth-First Search:

Find all neighboring edge nodes B, C, D from A and then find all neighboring nodes A, C, D from B and so on until all nodes are found  $A \rightarrow B \rightarrow C \rightarrow D \rightarrow E$ .







## Create a **TestDirectedGraphBreadthFrstSearch.html** with **Notepad**

```
<script type="text/javascript">
class Vertex {
    constructor(data, visited){
        this.data = data;
        this.visited = visited; // Have you visited
    }

    getData() {
        return this.data;
    }
    setData(data) {
        this.data = data;
    }

    isVisited() {
        return this.visited;
    }
    setVisited(visited) {
        this.visited = visited;
    }
}
```

```
class Queue {  
    constructor(){  
        this.queues = new Array();  
    }  
  
    add(element) {  
        this.queues[this.queues.length] = element;  
    }  
  
    remove() {  
        if(this.queues.length <= 0){  
            return -1;  
        }  
        return this.queues.shift();  
    }  
  
    isEmpty() {  
        if(this.queues.length <= 0){  
            return true;  
        }  
        return false;  
    }  
}
```

```
class Graph {
```

```
constructor(maxVertexSize){  
    this.maxVertexSize = maxVertexSize;// Two-dimensional array  
    size  
    this.vertexs = new Array(maxVertexSize);  
    this.size = 0; // Current vertex size  
    this.adjacencyMatrix = new Array(maxVertexSize);  
    for (var i = 0; i < maxVertexSize; i++) {  
        this.adjacencyMatrix[i] = new Array();  
        for (var j = 0; j < maxVertexSize; j++) {  
            this.adjacencyMatrix[i][j] = 0;  
        }  
    }  
    this.queue = new Queue();// Queue saves current vertices  
}  
  
addVertex(data) {  
    var vertex = new Vertex(data, false);  
    this.vertexs[this.size] = vertex;  
    this.size++;  
}  
  
// Add adjacent edges  
addEdge(from, to) {  
    // A -> B and B -> A are different  
    this.adjacencyMatrix[from][to] = 1;  
}
```

```

breadthFirstSearch() {
    // Start searching from the first vertex
    var firstVertex = this.vertices[0];
    firstVertex.setVisited(true);
    document.write(firstVertex.getData());
    this.queue.add(0);

    var col = 0;
    while (!this.queue.isEmpty()) {
        var head = this.queue.remove();
        // Get adjacent vertex positions that have not been visited
        col = this.findAdjacencyUnVisitedVertex(head);

        //Loop through all vertices connected to the current vertex
        while (col != -1)
        {
            this.vertices[col].setVisited(true);
            document.write(" -> " + this.vertices[col].getData());
            this.queue.add(col);
            col = this.findAdjacencyUnVisitedVertex(head);
        }
    }
    this.clear();
}

// Get adjacent vertex positions that have not been visited
findAdjacencyUnVisitedVertex(row) {
    for (var col = 0; col < this.size; col++) {
        if (this.adjacencyMatrix[row][col] == 1 &&
!this.vertices[col].isVisited()) {
            return col;
        }
    }
    return -1;
}

// Clear reset
clear() {

```

```

for (var i = 0; i < this.size; i++) {
    this.vertexs[i].setVisited(false);
}
}

getAdjacencyMatrix() {
    return this.adjacencyMatrix;
}

getVertexts() {
    return this.vertexs;
}
}

function printGraph(graph) {
    document.write("Two-dimensional array traversal output vertex
edge and adjacent array : <br>");
    document.write("&nbsp;&nbsp;&nbsp;");
    for (var i = 0; i < graph.getVertexts().length; i++) {
        document.write(graph.getVertexts()[i].getData() +
"&nbsp;&nbsp;&nbsp;&nbsp;");
    }
    document.write("<br>");

    for (var i = 0; i < graph.getAdjacencyMatrix().length; i++) {
        document.write(graph.getVertexts()[i].getData() + " ");
        for (var j = 0; j < graph.getAdjacencyMatrix().length; j++) {
            document.write(graph.getAdjacencyMatrix()[i][j] +
"&nbsp;&nbsp;&nbsp;&nbsp;");
        }
        document.write("<br>");
    }
}

var graph = new Graph(5);
graph.addVertex("A");
graph.addVertex("B");

```

```

graph.addVertex("C");
graph.addVertex("D");
graph.addVertex("E");

graph.addEdge(0, 1);
graph.addEdge(0, 2);
graph.addEdge(0, 3);
graph.addEdge(1, 2);
graph.addEdge(1, 3);
graph.addEdge(2, 3);
graph.addEdge(3, 4);

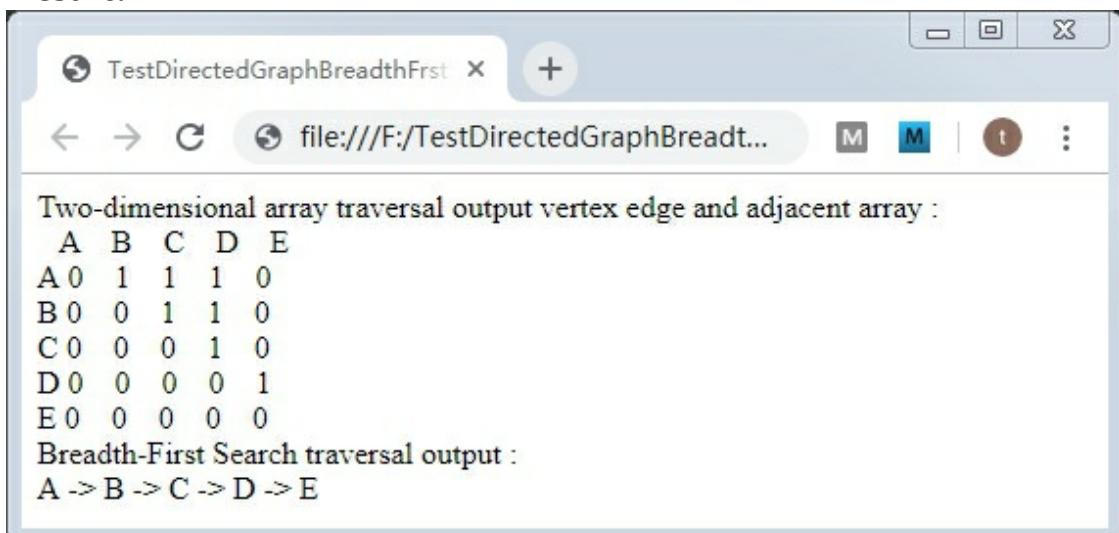
// Two-dimensional array traversal output vertex edge and adjacent
array
printGraph(graph);

document.write("\nBreadth-First Search traversal output : <br>");
graph.breadthFirstSearch();

</script>

```

## Result:

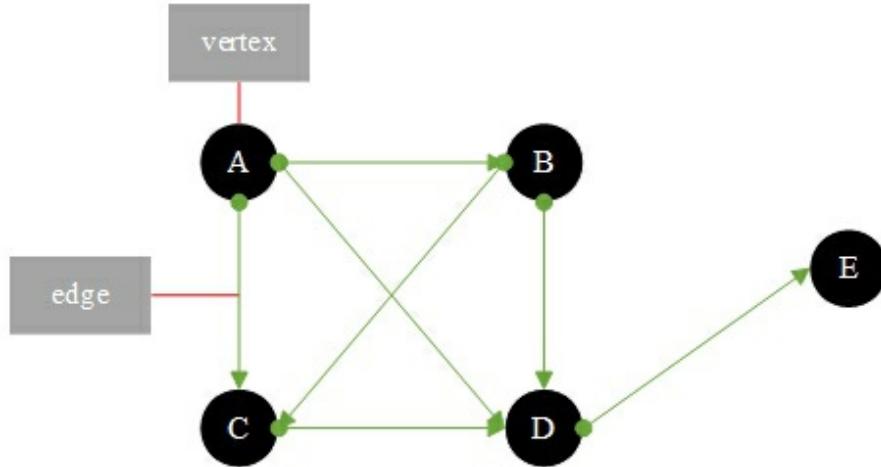


# Directed Graph Topological Sorting

**Directed Graph Topological Sorting:**

Sort the vertices in the directed graph with order of direction

Directed Graph has direction : A -> B and B -> A are different



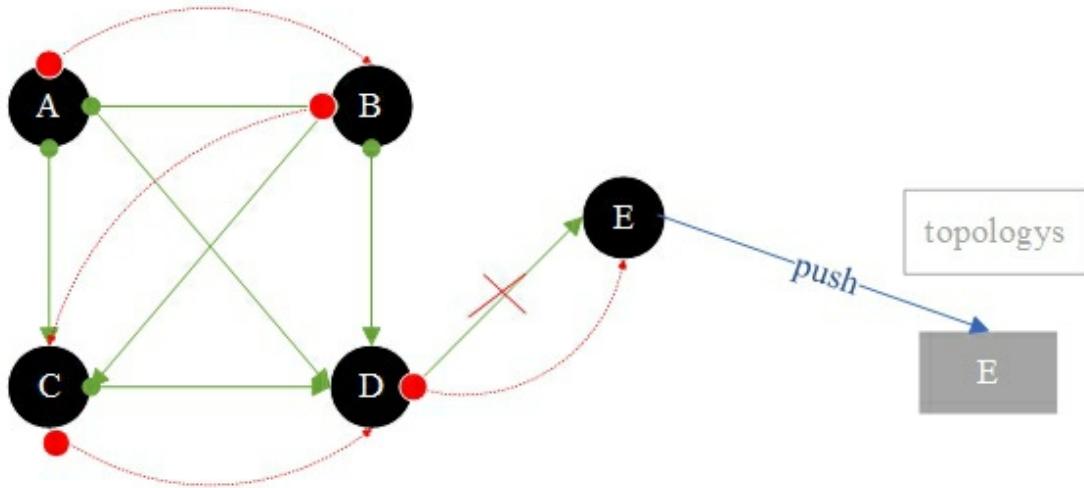
**1. The adjacency matrix is described above:**

The total number of vertices is a two-dimensional array size, if have value of the edge is 1, otherwise no value of the edge is 0.

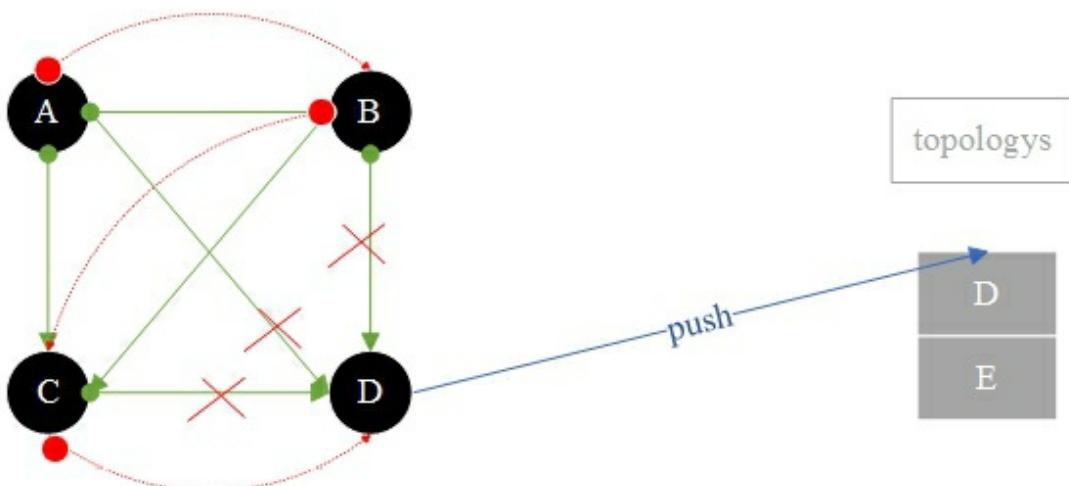
	A	B	C	D	E
A	0	1	1	1	0
B	0	0	1	1	0
C	0	0	0	1	0
D	0	0	0	0	1
E	0	0	0	0	0

## Topological sorting from vertex A : A -> B -> C -> D -> E

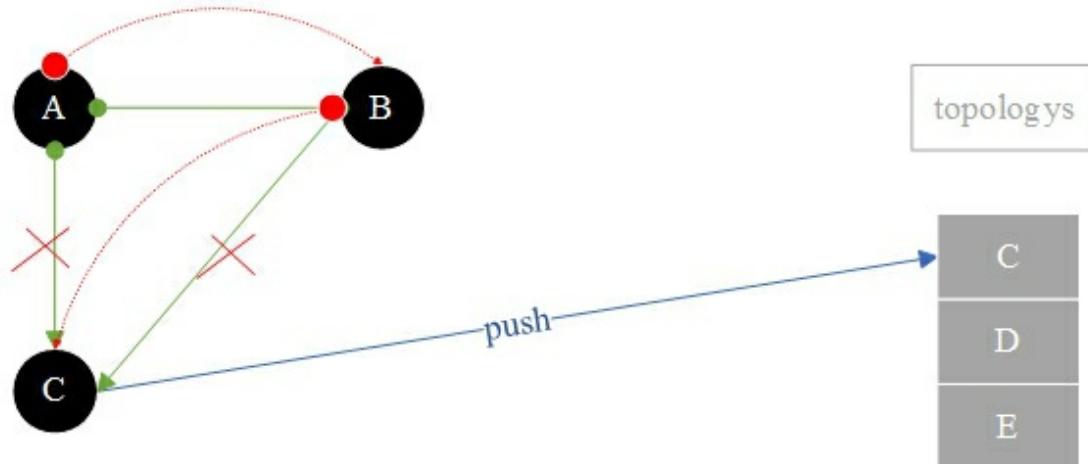
Find no successor vertices E then save to topologys, last E remove from the graph



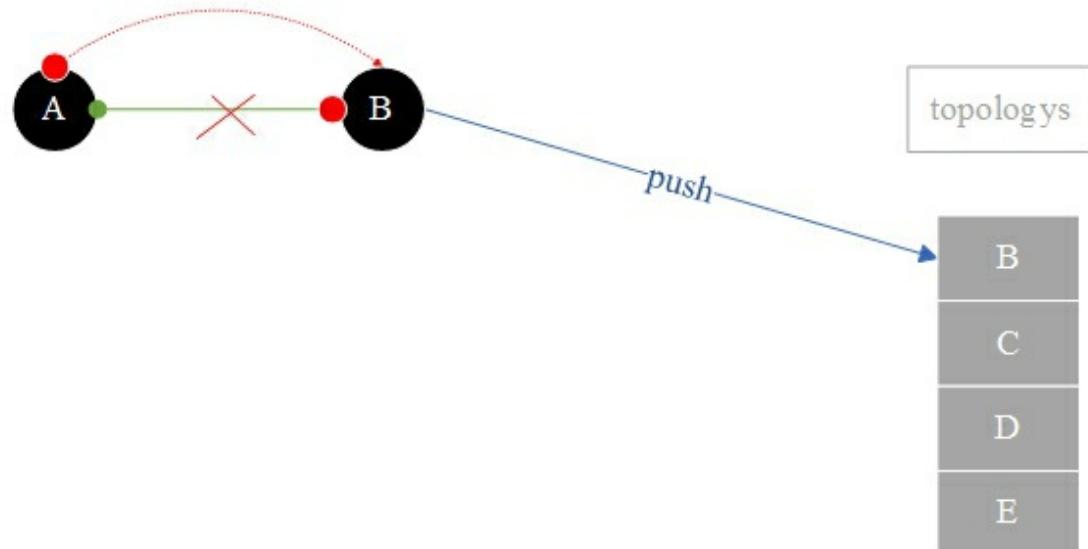
Find no successor vertices D then save to topologys, last D remove from the graph



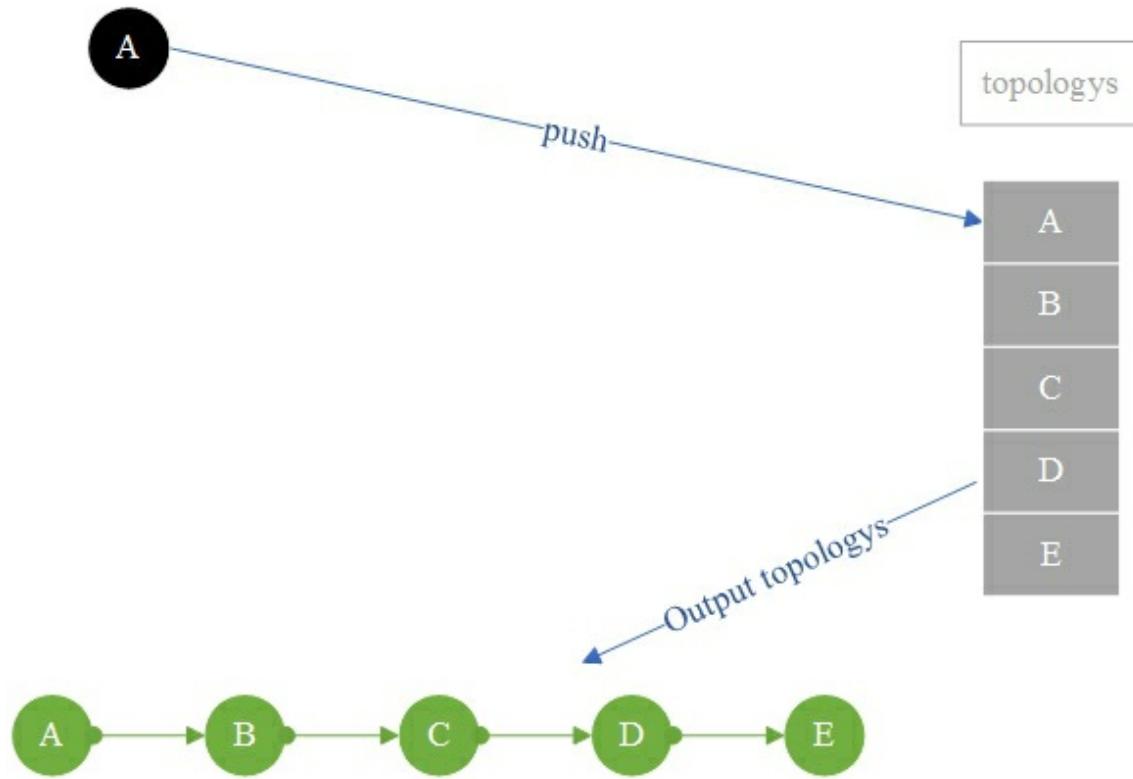
Find no successor vertices C then save to topologys, last C remove from the graph



Find no successor vertices C then save to topologys, last C remove from the graph



Find no successor vertices C then save to topologys, last C remove from the graph



## Create a **TestTopologicalSorting.html** with **NotePad**

```
<script type="text/javascript">
class Vertex {
    constructor(data, visited){
        this.data = data;
        this.visited = visited; // Have you visited
    }

    getData() {
        return this.data;
    }
    setData(data) {
        this.data = data;
    }

    isVisited() {
        return this.visited;
    }
    setVisited(visited) {
        this.visited = visited;
    }
}
```

```

class Graph {
    constructor(maxVertexSize){
        this.maxVertexSize = maxVertexSize;// Two-dimensional array
        size
        this.vertexs = new Array(maxVertexSize);
        this.topologys = new Array();
        this.adjacencyMatrix = new Array(maxVertexSize);
        for (var i = 0; i < maxVertexSize; i++) {
            this.adjacencyMatrix[i] = new Array();
            for (var j = 0; j < maxVertexSize; j++) {
                this.adjacencyMatrix[i][j] = 0;
            }
        }
        this.size = 0;
    }

    addVertex(data) {
        var vertex = new Vertex(data, false);
        this.vertexs[this.size] = vertex;
        this.size++;
    }

// Add adjacent edges
    addEdge(from, to) {
        // A -> B and B -> A are different
        this.adjacencyMatrix[from][to] = 1;
    }

    topologySort() {
        while (this.size > 0) {
            var noSuccessorVertex = this.getNoSuccessorVertex();// Get
            a no successor node
            if (noSuccessorVertex == -1) {
                document.write("There is ring in Graph ");
                return;
            }
            // Copy the deleted node to the sorted array
            this.topologys[this.size - 1] =
        }
    }
}

```

```

this.vertices[noSuccessorVertex];
    this.removeVertex(noSuccessorVertex); // Delete no
successor node
}
}

getNoSuccessorVertex() {
    var existSuccessor = false;
    for (var row = 0; row < this.size; row++) { // For each vertex
        existSuccessor = false;
        // If the node has a fixed row, each column has a 1, indicating
        that the node has a successor, terminating the loop
        for (var col = 0; col < this.size; col++) {
            if (this.adjacencyMatrix[row][col] == 1) {
                existSuccessor = true;
                break;
            }
        }
        if (!existSuccessor) { // If the node has no successor, return its
subscript
            return row;
        }
    }
    return -1;
}

removeVertex(vertex) {
    if (vertex != this.size - 1) { // If the vertex is the last element, the
end
        for (var i = vertex; i < this.size - 1; i++) { // The vertices are
removed from the vertex array
            this.vertices[i] = this.vertices[i + 1];
        }
        for (var row = vertex; row < this.size - 1; row++) { // move

```

up a row

```
    for (var col = 0; col < this.size - 1; col++) {
        this.adjacencyMatrix[row][col] =
this.adjacencyMatrix[row + 1][col];
    }
}

for (var col = vertex; col < this.size - 1; col++) { // move left
a row
    for (var row = 0; row < this.size - 1; row++) {
        this.adjacencyMatrix[row][col] =
this.adjacencyMatrix[row][col + 1];
    }
}
this.size--;// Decrease the number of vertices
}
```

// Clear reset

```
clear() {
    for (var i = 0; i < this.size; i++) {
        this.vertices[i].setVisited(false);
    }
}
```

```
getAdjacencyMatrix() {
    return this.adjacencyMatrix;
}
```

```
getVertices() {
    return this.vertices;
}
```

```
getTopologys() {
    return this.topologys;
}
}
```

```
///////////testing//////////
```

```
function printGraph(graph) {  
    document.write("Two-dimensional array traversal output vertex  
edge and adjacent array : <br>");  
    document.write("&nbsp;&nbsp;&nbsp;");  
    for (var i = 0; i < graph.getVertexts().length; i++) {  
        document.write(graph.getVertexts()[i].getData() +  
"&nbsp;&nbsp;&nbsp;");  
    }  
    document.write("<br>");  
  
    for (var i = 0; i < graph.getAdjacencyMatrix().length; i++) {  
        document.write(graph.getVertexts()[i].getData() + " ");  
        for (var j = 0; j < graph.getAdjacencyMatrix().length; j++) {  
            document.write(graph.getAdjacencyMatrix()[i][j] +  
"&nbsp;&nbsp;&nbsp;");  
        }  
        document.write("<br>");  
    }  
}
```

```
var graph = new Graph(5);
```

```
graph.addVertex("A");  
graph.addVertex("B");  
graph.addVertex("C");  
graph.addVertex("D");  
graph.addVertex("E");  
  
graph.addEdge(0, 1);  
graph.addEdge(0, 2);  
graph.addEdge(0, 3);  
graph.addEdge(1, 2);  
graph.addEdge(1, 3);  
graph.addEdge(2, 3);  
graph.addEdge(3, 4);
```

```
printGraph(graph);

document.write("<br>Depth-First Search traversal output : <br>");
document.write("Directed Graph Topological Sorting:<br>");

graph.topologySort();

for(var i=0;i< graph.getTopologys().length ; i++){
    document.write(graph.getTopologys()[i].getData()+" -> ");
}

</script>
```

## Result:

The screenshot shows a web browser window titled "TestTopologicalSorting.html". The address bar displays "file:///F:/TestTopologicalSorting.html". The content area of the browser shows the following text and data:

Two-dimensional array traversal output vertex edge and adjacent array :

	A	B	C	D	E
A	0	1	1	1	0
B	0	0	1	1	0
C	0	0	0	1	0
D	0	0	0	0	1
E	0	0	0	0	0

Depth-First Search traversal output :

Directed Graph Topological Sorting:

A -> B -> C -> D -> E ->

# Towers of Hanoi

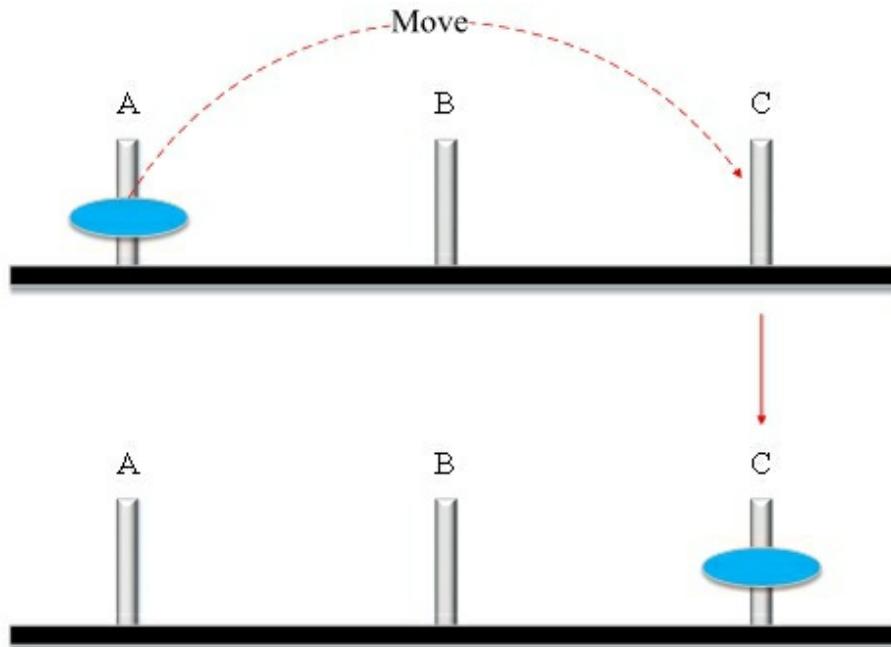
The Hanoi Tower that a Frenchman M. Claus (Lucas) from Thailand to France in 1883. Hanoi Tower which is supported by three diamond Pillars. At the beginning, God placed 64 gold discs from top to bottom on the first Pillar. God ordered the monks to move all gold discs from the first Pillar to the third Pillar. The principle of large plates under small plates during the handling process. If only one plate is moved daily, the tower will be destroyed. when all the discs are moved that is the end of the world.

**Let's turn this story into an algorithm:**

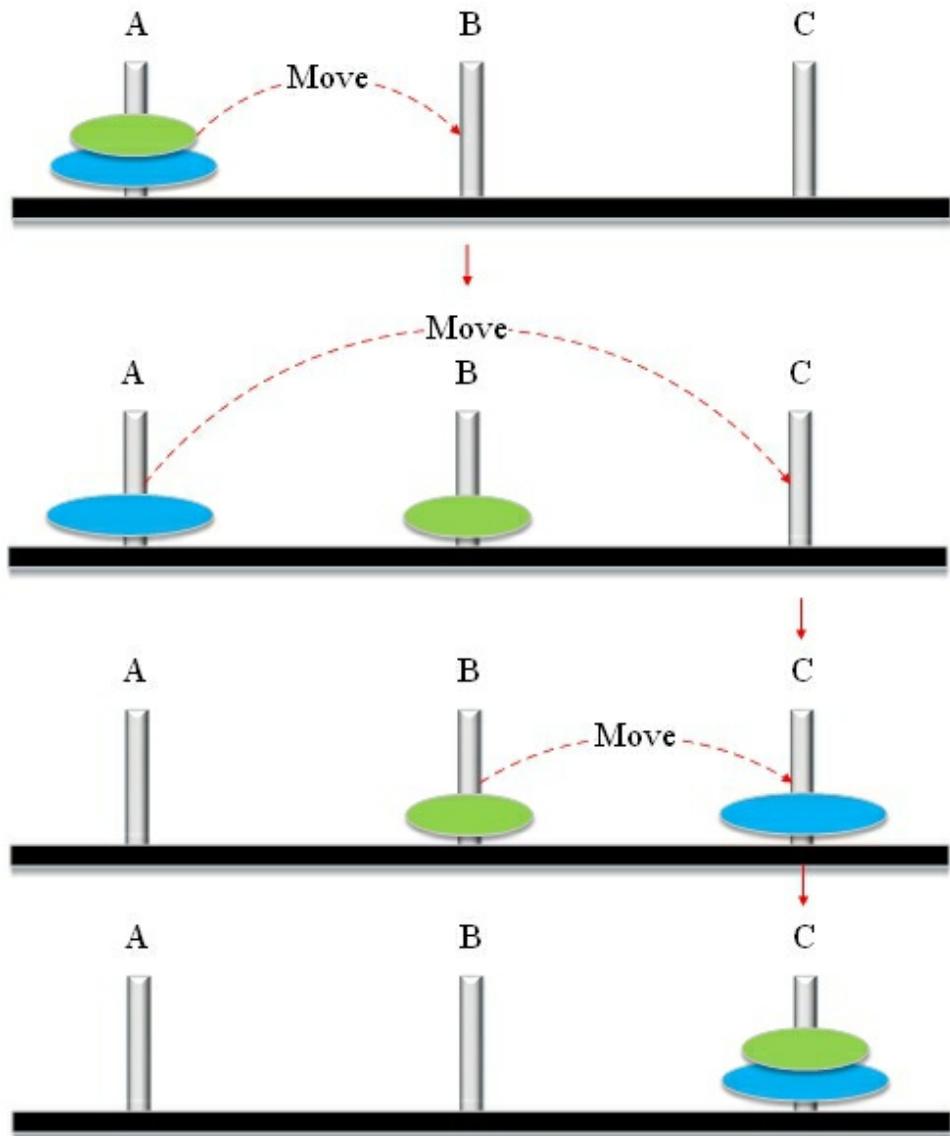
Mark the three columns as ABC.

1. If there is only one disc, move it directly to C ( $A \rightarrow C$ ).
2. When there are two discs, use B as an auxiliary ( $A \rightarrow B$ ,  $A \rightarrow C$ ,  $B \rightarrow C$ ).
3. If there are more than two discs, use B as an auxiliary( $A \rightarrow B$ ,  $A \rightarrow C$ ,  $B \rightarrow C$ ), and continue to recursive process.

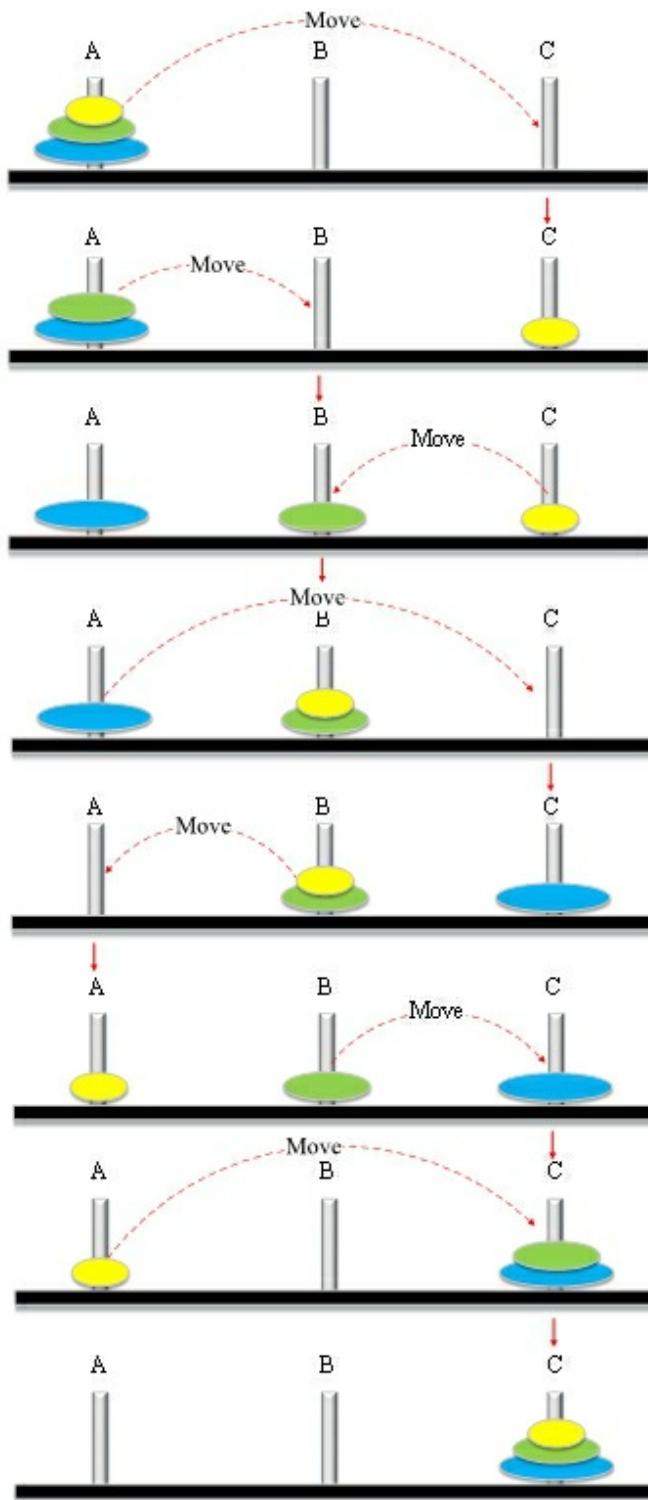
**1. If there is only one disc, move it directly to C ( $A \rightarrow C$ ).**



2. When there are two discs, use B as an auxiliary (**A->B, A->C, B->C**).



**3. If more than two discs, use B as an auxiliary, and continue to recursive process.**



**1. Create a `TowersofHanoi.html` with `Notepad` and open it in your browser.**

```
<script type="text/javascript">
    function hanoi(n, A, B, C) {
        if (n == 1) {
            document.write("Move " + n + " " + A + " to " + C + "
<br>");
        } else {
            hanoi(n - 1, A, C, B); // Move the n-1th disc on the
            A through C to B
            document.write("Move " + n + " from " + A + " to " + C + "
<br>");
            hanoi(n - 1, B, A, C); //Move the n-1th disc on the
            B through A to C
        }
    }

//////////////////testing/////////////////
document.write("Please enter the number of discs 1 <br>");

var n = 1;
hanoi(n, 'A', 'B', 'C');

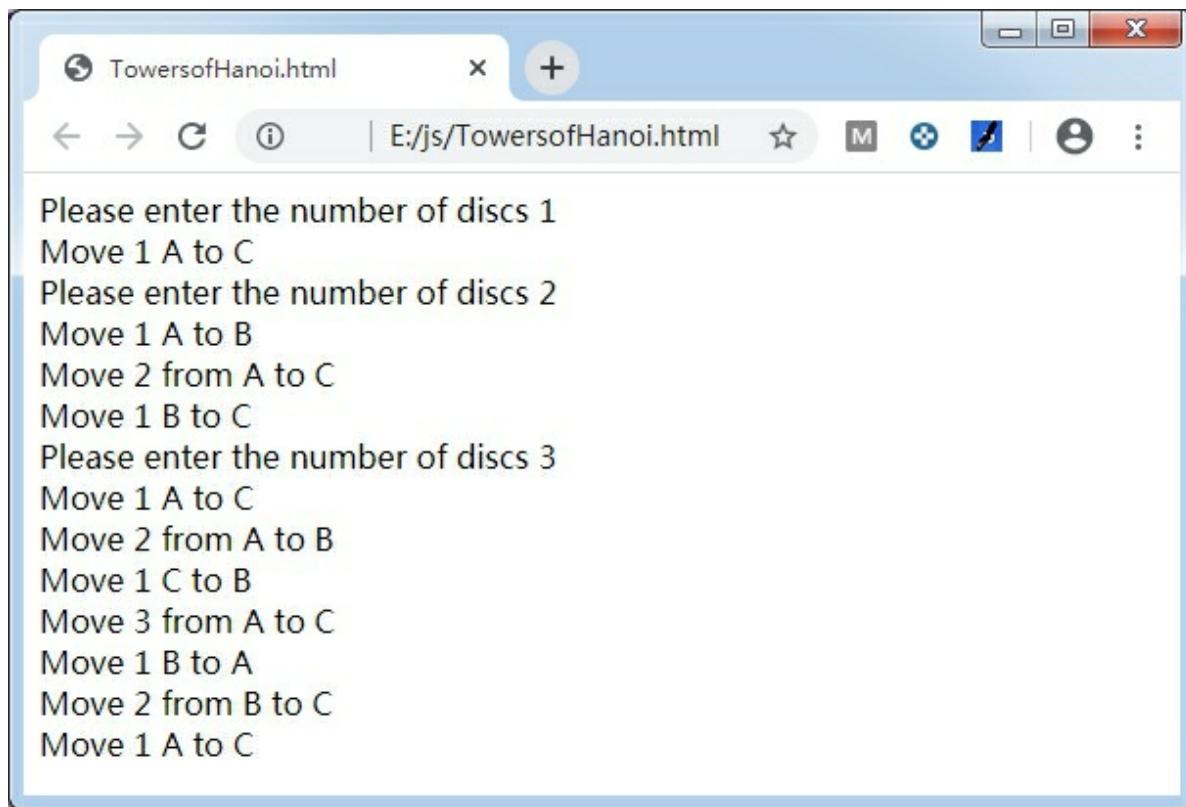
document.write("Please enter the number of discs 2 <br>");

var n = 2;
hanoi(n, 'A', 'B', 'C');

document.write("Please enter the number of discs 3 <br>");

var n = 3;
hanoi(n, 'A', 'B', 'C');
</script>
```

## Result:



# Fibonacci

**Fibonacci** : a European mathematician in the 1200s, in his writings: "If there is a rabbit

After a month can birth to a newborn rabbit. At first there was only 1 rabbit, after one month still 1 rabbit. after two month 2 rabbit, and after three months there are 3 rabbit .....

for example: 1, 1, 2, 3, 5, 8, 13 ...

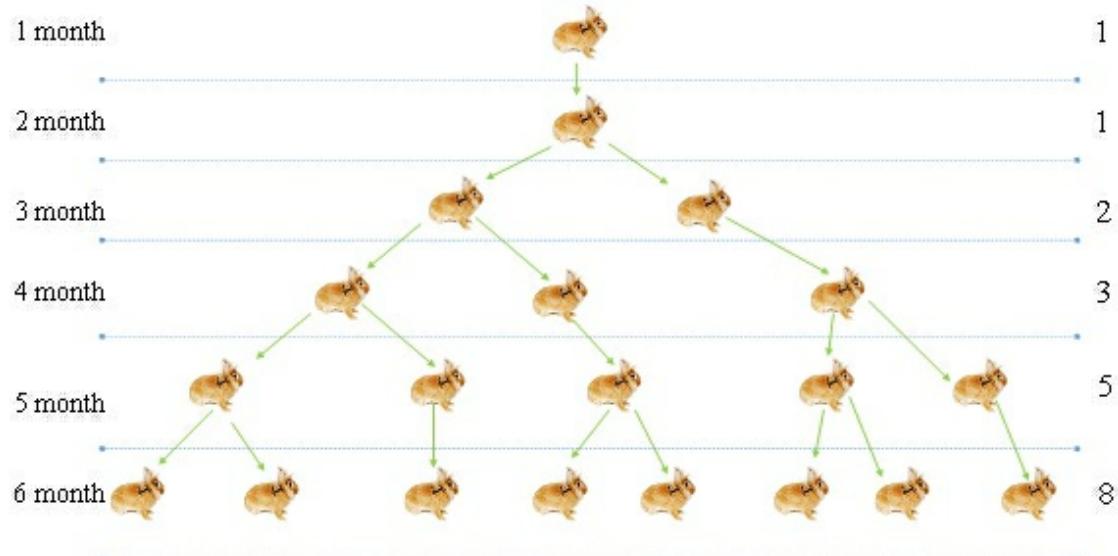
**Fibonacci definition:**

if  $n = 0, 1$

$$f_n = n$$

if  $n > 1$

$$f_n = f_{n-1} + f_{n-2}$$



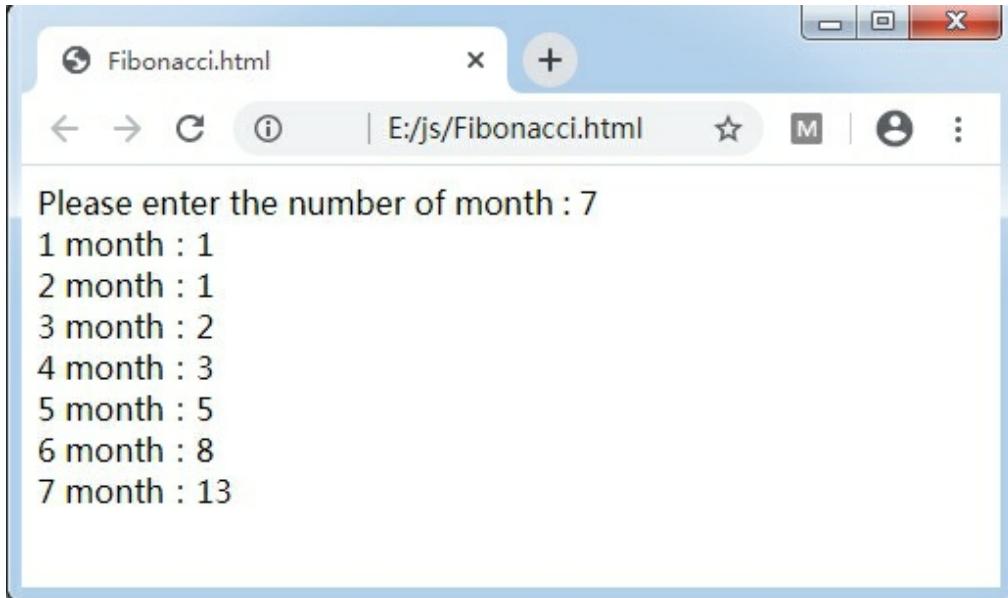
## 1. Create a **Fibonacci.html** with **Notepad** and open it in your browser.

```
<script type="text/javascript">
    function fibonacci(n) {
        if (n == 1 || n == 2) {
            return 1;
        } else {
            return fibonacci(n - 1) + fibonacci(n - 2);
        }
    }

//////////////////testing/////////////////
document.write("Please enter the number of month : 7 <br>");
var number = 7;

for (var i = 1; i <= number; i++) {
    document.write(i + " month:" + fibonacci(i) + "<br>");
}
</script>
```

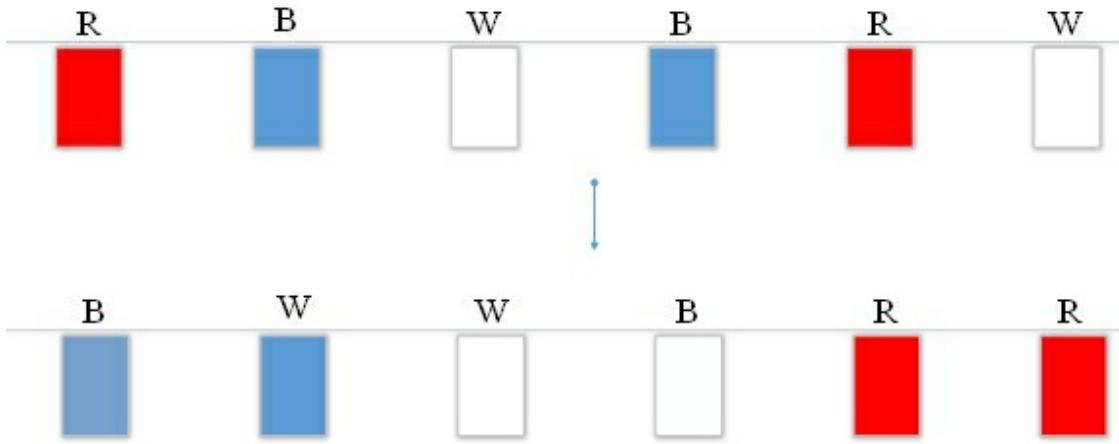
### Result:



# Dijkstra

The tricolor flag was originally raised by E.W. Dijkstra, who used the Dutch national flag (Dijkstra is Dutch).

Suppose there is a rope with red, white, and blue flags. At first all the flags on the rope are not in order. You need to arrange them in the order of **blue -> white -> red**. How to move them with the least times. you just only do this on the rope, and only swap two flags at a time.



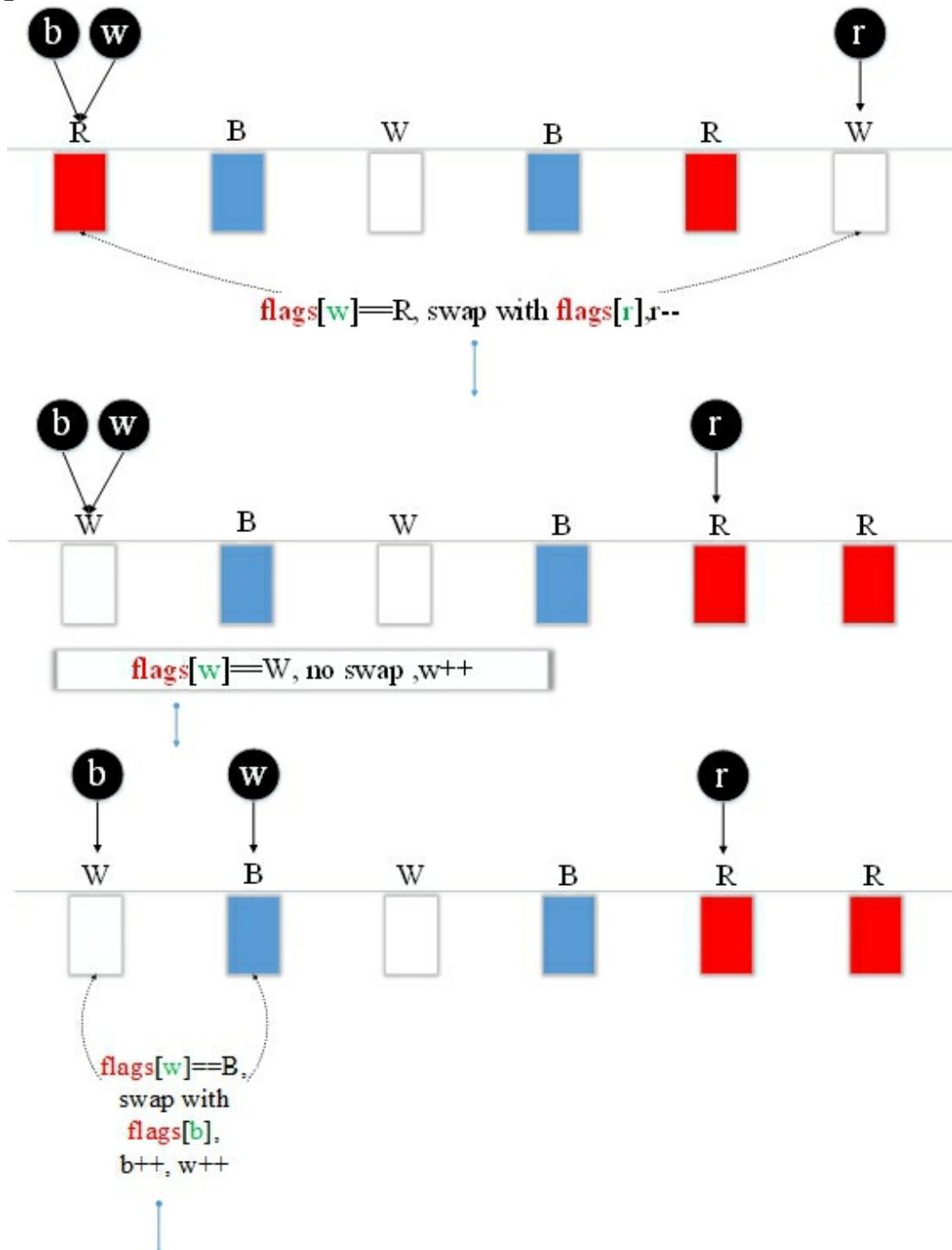
## Solution:

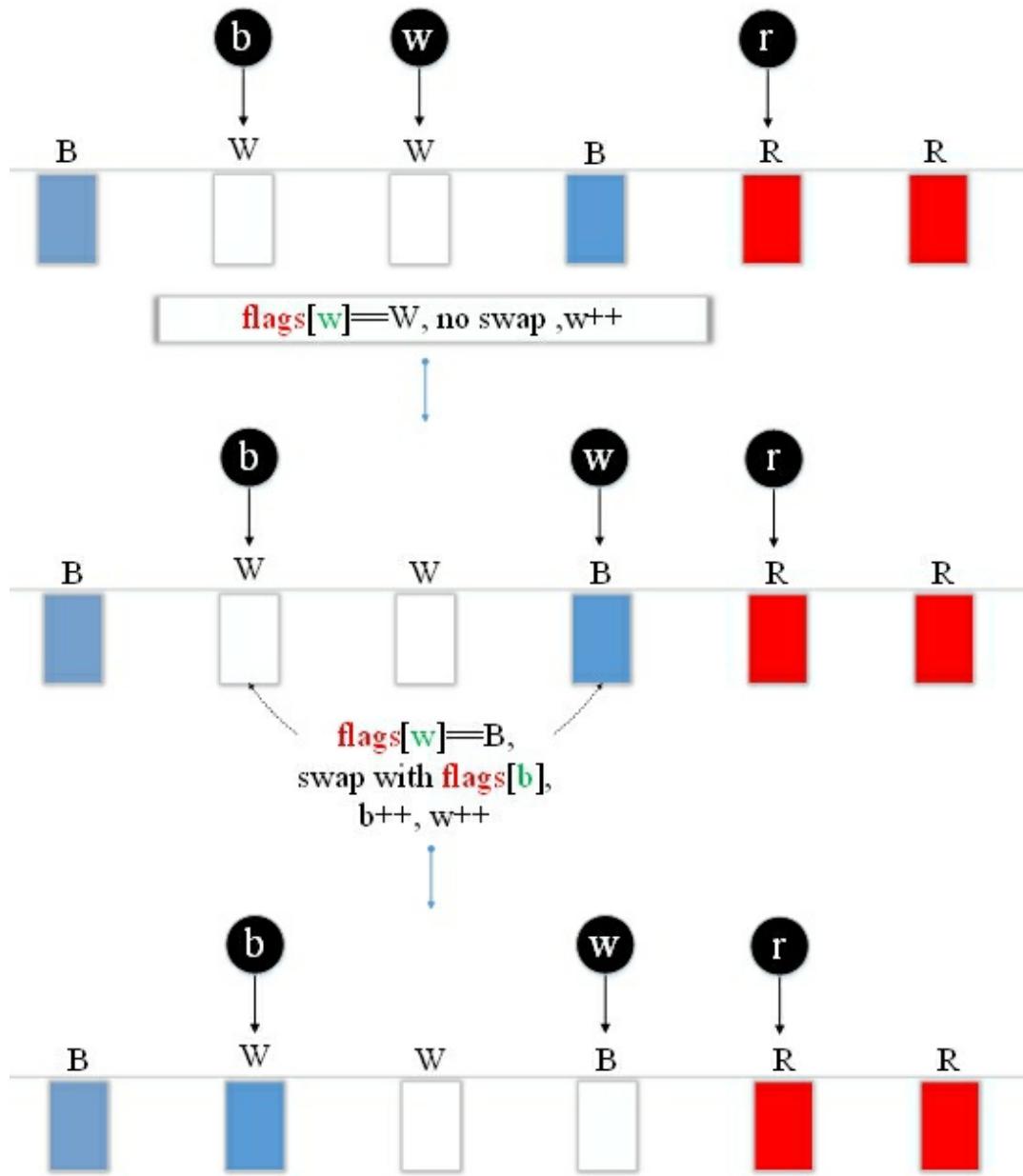
Use the **char arrays** to store the **flags**. For example, **b**, **w**, and **r** indicate the position of **blue**, **white** and **red** flags. The beginning of **b** and **w** is 0 of the array, and **r** is at the end of the array.

- (1) If the position of **w** is a blue flag, **flags[w]** exchange with **flags[b]**. And **whiteIndex** and **b** is moved backward by 1.
- (2) If the position of **w** is a white flag, **w** moves backward by 1.
- (3) If the position of **w** is a red flag, **flags[w]** exchange with **flags[r]**. **r** moves forward by 1.

In the end, the flags in front of **b** are all blue, and the flags behind **r** are all red.

## Graphic Solution





**1. Create a `Dijkstra.html` with **Notepad** and open it in your browser.**

```
<script type="text/javascript">
function dijkstra(flags) {
    var b = 0, w = 0, r = flags.length - 1;
    var count = 0;
    while (w <= r) {
        if (flags[w] == 'W') {
            w++;
        } else if (flags[w] == 'B') {
            var temp = flags[w];
            flags[w] = flags[b];
            flags[b] = temp;
            w++;
            b++;
            count++;
        } else if (flags[w] == 'R') {
            var m = flags[w];
            flags[w] = flags[r];
            flags[r] = m;
            r--;
            count++;
        }
    }
}

var flags = [ 'R', 'B', 'W', 'B', 'R', 'W' ];
dijkstra(flags);
for (var i = 0; i < flags.length; i++) {
    document.write(flags[i]);
}
</script>
```

**Result:**



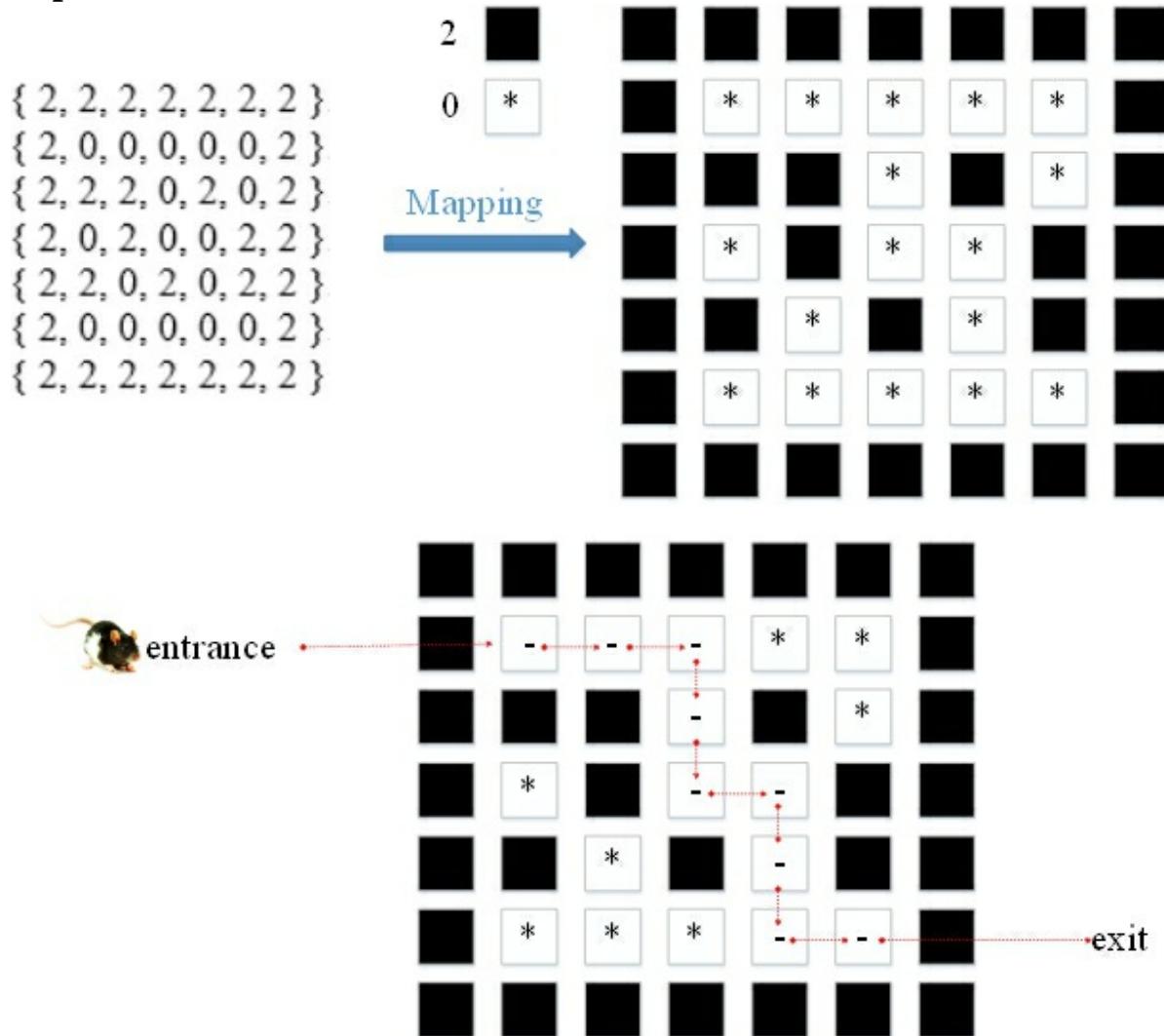
# Mouse Walking Maze

Mouse Walking Maze is a basic type of recursive solution. We use **2** to represent the **wall** in a **two-dimensional array**, and use **1** to represent the **path** of the mouse, and try to find the path from the entrance to the exit.

## Solution:

The mouse moves in four directions: **up, left, down, and right**. If hit the **wall** go back and select the next forward direction, so test the four directions in the array until mouse reach the exit.

## Graphic Solution



**1. Create a [MouseWalkingMaze.html](#) with [Notepad](#) and open it in your browser.**

```
<script type="text/javascript">
var maze = [
    [ 2, 2, 2, 2, 2, 2, 2 ],
    [ 2, 0, 0, 0, 0, 0, 2 ],
    [ 2, 2, 2, 0, 2, 0, 2 ],
    [ 2, 0, 2, 0, 0, 2, 2 ],
    [ 2, 2, 0, 2, 0, 2, 2 ],
    [ 2, 0, 0, 0, 0, 0, 2 ],
    [ 2, 2, 2, 2, 2, 2, 2 ]
];

var startI = 1;
var startJ = 1;
var endI = 5;
var endJ = 5;
var success = 0;

//The mouse moves in four directions: up, left, down, and right. if hit
the wall go back and select the next forward direction
function visit(i, j) {
    maze[i][j] = 1;
    if (i == endI && j == endJ) {
        success = 1;
    }
    if (success != 1 && maze[i][j + 1] == 0)
        visit(i, j + 1);
    if (success != 1 && maze[i + 1][j] == 0)
        visit(i + 1, j);
    if (success != 1 && maze[i][j - 1] == 0)
        visit(i, j - 1);
    if (success != 1 && maze[i - 1][j] == 0)
        visit(i - 1, j);
    if (success != 1)
        maze[i][j] = 0;
```

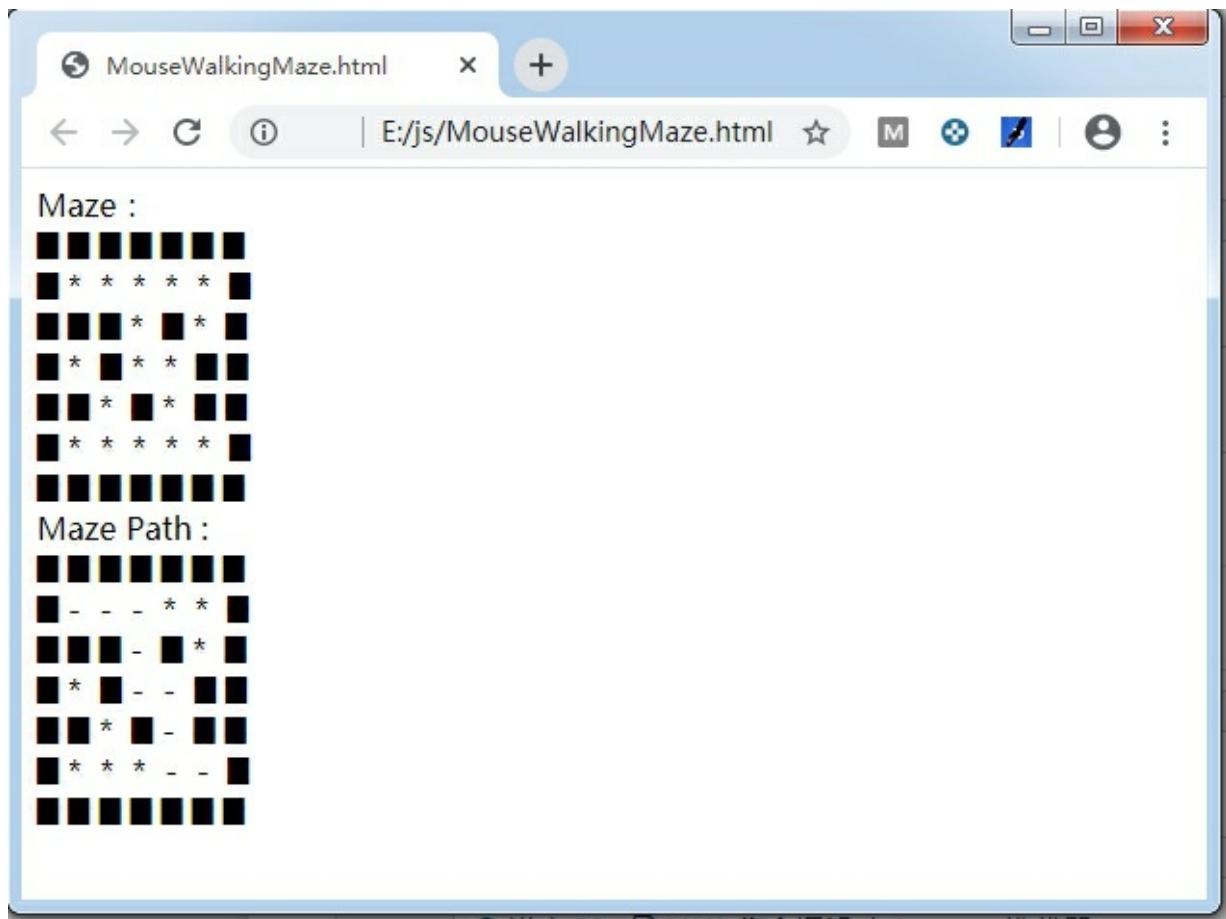
```
        return success;
    }

//////////////////testing/////////////////
document.write("Maze : <br>");
for (var i = 0; i < 7; i++) {
    for (var j = 0; j < 7; j++) {
        if (maze[i][j] == 2) {
            document.write("█&nbsp;");
        } else {
            document.write("*&nbsp;&nbsp;");
        }
    }
    document.write("<br>");
}

if (visit(startI, startJ) == 0) {
    document.write("No exit found <br>");
} else {
    document.write("Maze Path : <br>");
    for (var i = 0; i < 7; i++) {
        for (var j = 0; j < 7; j++) {
            if (maze[i][j] == 2) {
                document.write("█&nbsp;");
            } else if (maze[i][j] == 1) {
                document.write("-&nbsp;&nbsp;");
            } else {
                document.write("*&nbsp;&nbsp;");
            }
        }
        document.write("<br>");
    }
}
</script>
```



## Result:



# Eight Coins

There are eight coins with the same appearance, one is a counterfeit coin, and the weight of counterfeit coin is different from the real coin, but it is unknown whether the counterfeit coin is lighter or heavier than the real coin. Please design an efficient algorithm to detect this counterfeit coin.

## Solution:

Take six  $a, b, c, d, e, f$  from eight coins, and put three to the balance for comparison. Suppose  $a, b, c$  are placed on one side, and  $d, e, f$  are placed on the other side.

$$1. a + b + c > d + e + f$$

$$2. a + b + c = d + e + f$$

$$3. a + b + c < d + e + f$$

If  $a + b + c > d + e + f$ , there is a counterfeit coin in one of the six coins, and  $g, h$  are real coins. At this time, one coin can be removed from both sides.

Suppose that  $c$  and  $f$  are removed. At the same time, one coin at each side is replaced. Suppose the coins  $b$  and  $e$  are interchanged, and then the second comparison. There are also three possibilities:

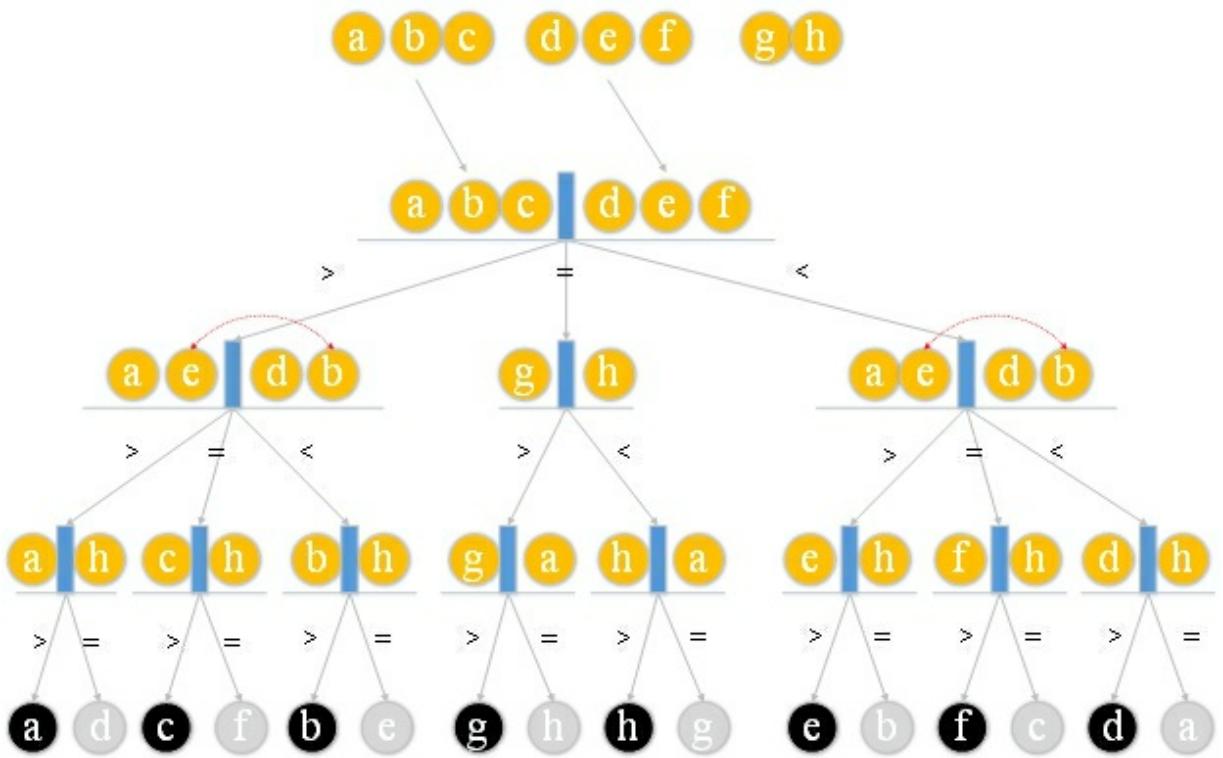
1.  $a + e > d + b$ : the counterfeit currency must be one of  $a, d$ . as long as we compare a real currency  $h$  with  $a$ , we can find the counterfeit currency. If  $a > h$ ,  $a$  is a heavier counterfeit currency; if  $a = h$ ,  $d$  is a lighter counterfeit currency.

2.  $a + e = d + b$ : the counterfeit currency must be one of  $c, f$ , and the real coin  $h$  is compared with  $c$ . If  $c > h$ ,  $c$  is a heavier counterfeit currency; if  $c = h$ , then  $f$  is a lighter counterfeit currency.

3.  $a + e < d + b$ : one of  $b$  or  $e$  is a counterfeit coin , Also use the real coin  $h$  to compare with  $b$ , if  $b > h$ , then  $b$  is a heavier counterfeit currency; if  $b = h$ , then  $e$  is a lighter counterfeit currency;

## Graphic Solution





# 1. Create a EightCoins.html with Notepad and open it in your browser.

```
<script type="text/javascript">
    function compare(coins, i, j, k) { //coin[k] true, coin[i]>coin[j]
        if (coins[i] > coins[k]) //coin[i]>coin[j]&&coin[i]>coin[k] -----
        >coin[i] is a heavy counterfeit coin
            document.write("\nCounterfeit currency " + (i + 1) + " is heavier
<br>"); 
        else //coin[j] is a light counterfeit coin
            document.write("\nCounterfeit currency " + (j + 1) + " is lighter
<br>"); 
    }

    function eightcoins(coins) {
        if (coins[0] + coins[1] + coins[2] == coins[3] + coins[4] + coins[5]){
        // (a+b+c)==(d+e+f)
            if (coins[6] > coins[7]) //g>h?(g>a?g:a):(h>a?h:a)
                compare(coins, 6, 7, 0);
            else //h>g?(h>a?h:a):(g>a?g:a)
                compare(coins, 7, 6, 0);
        } else if (coins[0] + coins[1] + coins[2] > coins[3] + coins[4] +
        coins[5]){
        // (a+b+c)>(d+e+f)
            if (coins[0] + coins[3] == coins[1] + coins[4]) // (a+e)==(d+b)
                compare(coins, 2, 5, 0);
            else if (coins[0] + coins[3] > coins[1] + coins[4]) // (a+e)>(d+b)
                compare(coins, 0, 4, 1);
            if (coins[0] + coins[3] < coins[1] + coins[4]) // (a+e)<(d+b)
                compare(coins, 1, 3, 0);
        } else if (coins[0] + coins[1] + coins[2] < coins[3] + coins[4] +
        coins[5]) { // (a+b+c)<(d+e+f)
            if (coins[0] + coins[3] == coins[1] + coins[4]) // (a+e)>(d+b)
                compare(coins, 5, 2, 0);
            else if (coins[0] + coins[3] > coins[1] + coins[4]) // (a+e)>(d+b)
                compare(coins, 3, 1, 0);
            if (coins[0] + coins[3] < coins[1] + coins[4]) // (a+e)<(d+b)
                compare(coins, 4, 0, 1);
        }
    }
}
```

```
}
```

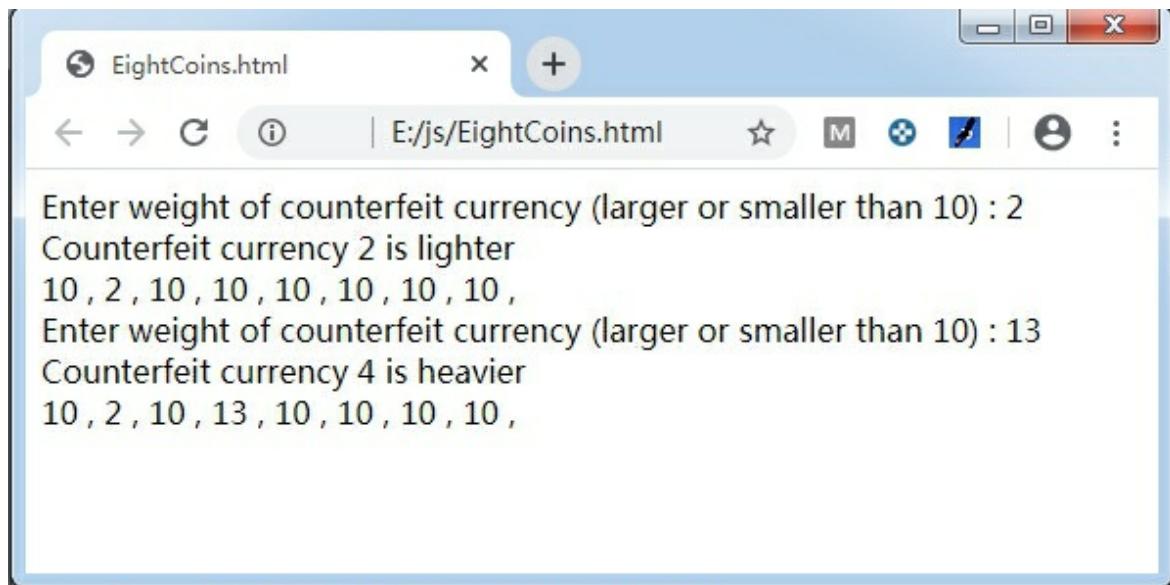
```
//////////testing/////////
var coins = new Array();
// Initial coin weight is 10
for (var i = 0; i < 8; i++)
    coins[i] = 10;

document.write("Enter weight of counterfeit currency (larger or
smaller than 10) : 2<br>");
coins[1] = 2;
eightcoins(coins);
for (var i = 0; i < 8; i++)
    document.write(coins[i]+", ");

document.write("<br>");

document.write("Enter weight of counterfeit currency (larger or
smaller than 10) : 13<br>");
coins[3] = 13;
eightcoins(coins);
for (var i = 0; i < 8; i++)
    document.write(coins[i]+", ");
</script>
```

## Result:



# Josephus Problem

There are 9 Jewish hid in a hole with Josephus and his friends . The 9 Jews decided to die rather than be caught by the enemy, so they decided In a suicide method, 11 people are arranged in a circle, and the first person reports the number. After each number is reported to the third person, the person must commit suicide. Then count again from the next one until everyone commits suicide. But Josephus and his friends did not want to obey. Josephus asked his friends to pretend to obey, and he arranged the friends with himself. In the 2th and 7st positions, they escaped this death game.

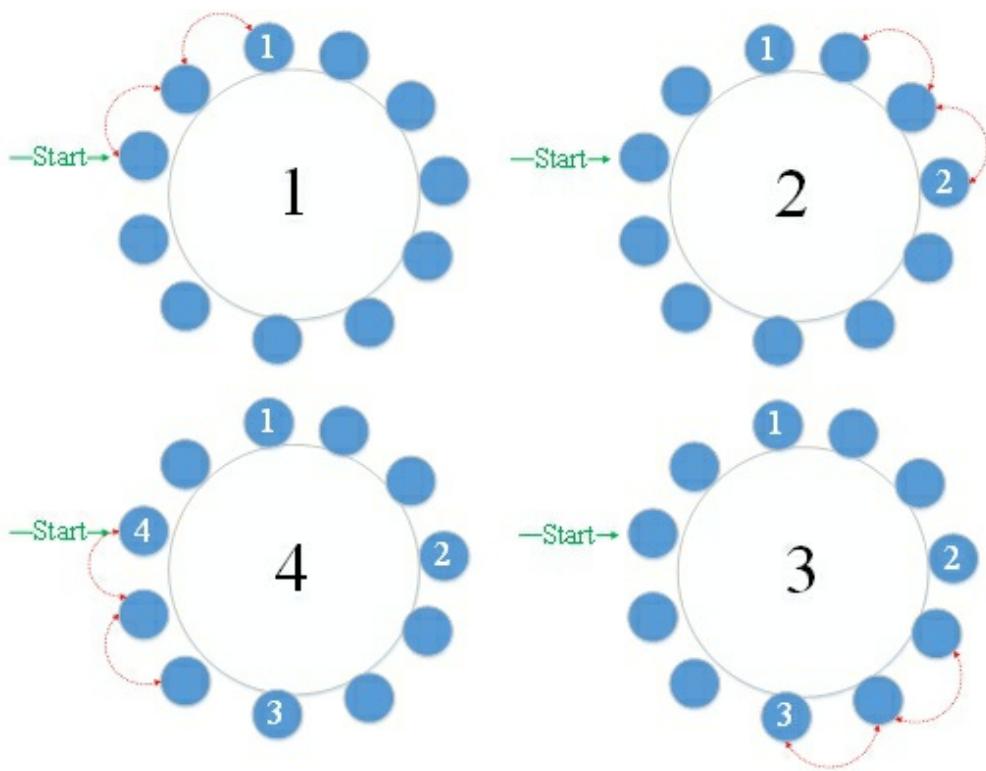
## Solution:

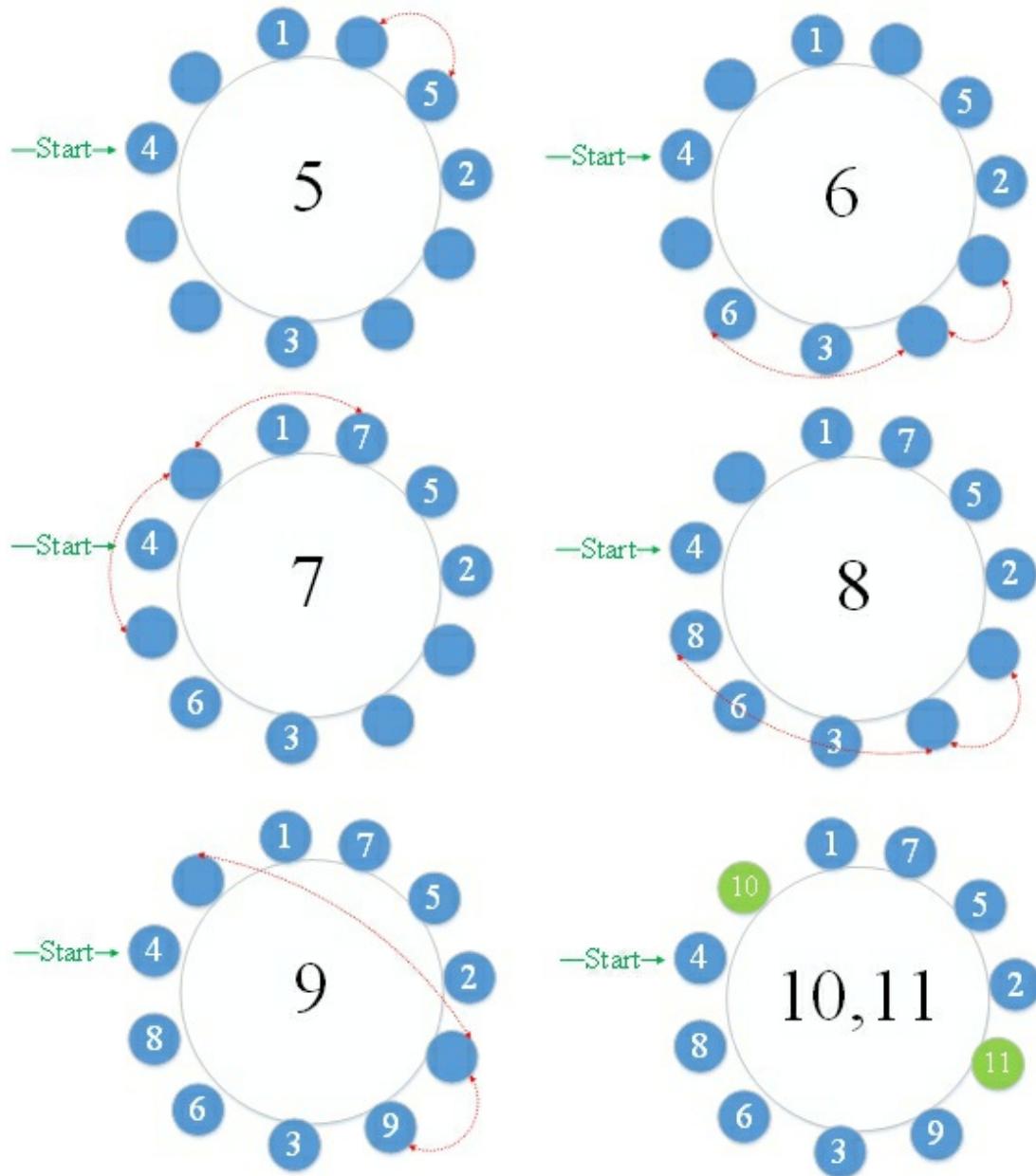
As long as the array is treated as a ring. Fill in a count for each dataless area, until the count reaches 11, and then list the array from index 1, you can know that each suicide order in this position is the Joseph's position. The 11-person position is as follows:

4 10 1 7 5 2 11 9 3 6 8

From the above, the last two suicide was in the 31st and 16th position. The previous one

Everyone died, so they didn't know that Joseph and his friends didn't follow the rules of the game.





## 1. Create a **Josephus.html** with **Notepad** and open it in your browser.

```
<script type="text/javascript">
    var N = 11;
    var M = 3;

    function joseph(man) {
        var count = 1;
        var i = 0, pos = -1;
        var alive = 0;
        while (count <= N) {
            do {
                pos = (pos + 1) % N; // Ring
                if (man[pos] == 0)
                    i++;
                if (i == M) {
                    i = 0;
                    break;
                }
            } while (true);
            man[pos] = count;
            count++;
        }
    }

    ////////////////////testing/////////////////
    var man = new Array();
    for (var i = 0; i < N; i++)
        man[i] = 0;

    joseph(man);

    document.write("\nJoseph sequence:<br>");
    for (var i = 0; i < N; i++)
        document.write(man[i] + " , ");
</script>
```

**Result:**

Joseph sequence :

4 , 10 , 1 , 7 , 5 , 2 , 11 , 9 , 3 , 6 , 8 ,

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**I wish you all the best in your future success!**