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# Efficient KV Cache Management for Long-Context LLM Inference: Lazy Pruning, Slack, and Staged Eviction

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## Abstract

1 Long-context LLM inference is bottlenecked by KV-cache growth and per-token  
2 runtime overhead. StreamingLLM [10] bounds KV-cache size by retaining atten-  
3 tion sinks and a recent-token window, but practical decoding can suffer from (i)  
4 non-trivial KV pruning overhead and (ii) quality degradation caused by periodic  
5 hard evictions, especially on long-form generation. We propose three lightweight,  
6 training-free KV-cache management mechanisms on top of StreamingLLM: **Lazy**  
7 **Pruning** (amortize pruning by triggering after  $R$  tokens of overflow), **Slack**  
8 (a hard-cap buffer that enables staged evictions under bounded memory), and  
9 **Max\_Drop** (limit the maximum tokens evicted per prune event). We evaluate  
10 on Pythia-2.8B using WikiText-103 (sanity) and PG19 (long-context), and report  
11 TTFT/TPOT/throughput/memory/perplexity trade-offs. We also document why  
12 FlashAttention, speculative decoding, quantization, and CUDA operator fusion did  
13 not improve batch-1 streaming decode under our setting.

## 14 1 Introduction

15 Long-context LLM inference is challenging because both computation and memory scale with the  
16 context length. During autoregressive decoding, the KV cache grows linearly with the number of  
17 processed tokens, increasing attention cost and memory traffic. StreamingLLM [10] mitigates this  
18 by keeping only (i) the first  $S$  “sink” tokens and (ii) a sliding window of the most recent  $W$  tokens,  
19 thereby bounding the effective KV-cache length.

20 **Motivation.** In our setting (Pythia-2.8B on NVIDIA A800), once attention length is bounded,  
21 decode becomes dominated by MLP and framework/launch overhead. Meanwhile, KV pruning itself  
22 can incur additional overhead due to slicing/copy and rotary-position re-alignment. More importantly,  
23 periodic hard eviction introduces distribution shifts that manifest as token-level NLL spikes and  
24 perplexity (PPL) degradation on long-form datasets. These observations motivate KV-management  
25 mechanisms that (i) reduce amortized pruning overhead and (ii) stage evictions to stabilize quality,  
26 without modifying attention kernels or model weights.

27 **Contributions.** We propose three training-free, modular mechanisms on top of StreamingLLM: (i)  
28 **Lazy Pruning**, which triggers pruning only after the cache overflow reaches  $R$  tokens; (ii) **Slack**,  
29 a hard capacity buffer of  $\sigma$  tokens that supports staged pruning; (iii) **Max\_Drop**, which limits the  
30 maximum tokens evicted per prune event to  $\delta$ . We provide a reproducible evaluation pipeline and  
31 summarize negative results for methods that are effective in other regimes but do not improve batch-1  
32 streaming decode.

## 2 Related Work

**Long-context inference and KV-cache compression.** Test-time KV-cache management is a widely used approach to make long-context inference feasible, including retention/eviction heuristics and cache compression [10, 11, 8, 6]. Our work builds on StreamingLLM’s Start+Recent rule and focuses on *training-free* extensions that target the practical costs of pruning and eviction-induced distribution shifts. **Kernel- and decoding-level accelerations.** Attention kernels such as FlashAttention aim to reduce attention IO cost [3, 2], while speculative decoding accelerates generation by drafting tokens [7, 1]. Post-training quantization reduces compute/memory but its benefits depend on hardware and runtime regime [4, 5]. We empirically find these do not improve batch-1 streaming decode in our setting and analyze the underlying reasons (Sec. 5).

## 3 Method

We first define Start+Recent streaming, then formalize our three mechanisms.

### 3.1 Preliminaries: Start+Recent StreamingLLM

Let  $x_{1:t}$  be the processed prefix at decode step  $t$ . For each layer  $\ell$ , let  $(\mathbf{K}_t^\ell, \mathbf{V}_t^\ell)$  denote the KV cache with sequence length  $L_t$  along the cache dimension. Start+Recent streaming retains (i) the first  $S$  sink tokens, and (ii) the most recent  $W$  tokens. Define the soft capacity

$$C_0 \triangleq S + W. \quad (1)$$

Our code also supports optional *non-core* retained tokens (e.g., overlap/refresh); we denote their total budget by  $B \geq 0$  and define the effective soft capacity

$$C \triangleq C_0 + B. \quad (2)$$

Unless stated otherwise, we use  $B = 0$  in paper experiments to isolate our three mechanisms. When pruning is performed, the retained index set is

$$\mathcal{I}_t = \{0, 1, \dots, S - 1\} \cup \{L_t - W, \dots, L_t - 1\}, \quad (3)$$

with the recent segment clamped to avoid overlap with the sink segment.

**RoPE consistency.** For rotary-position-embedding models (e.g., Pythia/GPT-NeoX), pruning changes token positions in the cache; therefore, cached keys must be re-aligned to the new positions. Let  $p \in \mathcal{I}_t$  be an old token position and  $p' = f_t(p) \in \{0, \dots, |\mathcal{I}_t| - 1\}$  be its new position after compaction. RoPE encodes position via per-dimension frequencies  $\omega_i$  (from `inv_freq`). Re-alignment is equivalent to applying a *delta-rotation* with  $\Delta p = p' - p$ :

$$\begin{bmatrix} k'_{2i} \\ k'_{2i+1} \end{bmatrix} = \begin{bmatrix} \cos(\omega_i \Delta p) & -\sin(\omega_i \Delta p) \\ \sin(\omega_i \Delta p) & \cos(\omega_i \Delta p) \end{bmatrix} \begin{bmatrix} k_{2i} \\ k_{2i+1} \end{bmatrix}. \quad (4)$$

Our implementation exploits that Start+Recent yields a constant  $\Delta p$  for the contiguous recent block (a constant shift), and falls back to the general per-token re-rotation when tokens are explicitly relocated (e.g., refresh tokens).

### 3.2 Lazy Pruning

Naïve streaming prunes as soon as the cache exceeds  $C$ , which can add overhead due to slicing/copy and KV relocation. We instead amortize pruning by allowing the cache to exceed  $C$  by up to  $R - 1$  tokens before triggering a prune. Define overflow:

$$\text{overflow}_t \triangleq L_t - C. \quad (5)$$

Let  $R$  be the *overflow allowance* hyperparameter (in code: `compress_every`). We allow  $R = 0$  to disable pruning for debugging (unbounded memory), and use  $R \geq 1$  in all bounded-memory settings. Lazy pruning triggers only when overflow reaches  $R$ :

$$\text{PruneTrigger}(t) \triangleq \mathbb{I}[R > 0] \cdot \mathbb{I}[\text{overflow}_t \geq R]. \quad (6)$$

This matches the implementation semantics and avoids the ambiguity that would arise from interpreting  $R = 0$  as “prune immediately”.

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**Algorithm 1** KV pruning with Lazy Pruning, Slack, and Max\_Drop

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**Require:** sink size  $S$ , window size  $W$ , extra budget  $B$  (default 0), overflow allowance  $R$  (0 disables), slack  $\sigma$ , max\_drop  $\delta$

- 1:  $C_0 \leftarrow S + W$ ,  $C \leftarrow C_0 + B$ ,  $H \leftarrow C + \sigma$
- 2: observe cache length  $L_t$
- 3: **if**  $R = 0$  **then**
- 4:   **return**
- 5: **end if**
- 6: **if**  $L_t \leq C$  **then**
- 7:   **return**
- 8: **end if**
- 9: **if**  $L_t - C < R$  **then**
- 10:   **return**
- 11: **end if**
- 12: **if**  $\delta = 0$  **then**
- 13:    $L_t^* \leftarrow C$
- 14: **else**
- 15:    $L_t^* \leftarrow \min(\max(L_t - \delta, C), H)$
- 16: **end if**
- 17: keep first  $S$  tokens and most recent  $(L_t^* - S)$  tokens
- 18: prune KV cache and re-align RoPE positions

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### 71 3.3 Slack (Hard-Cap Buffer)

72 Slack introduces a *hard* capacity that bounds temporary cache growth during staged pruning. Specifi-  
73 cally, we define

$$H \triangleq C + \sigma, \quad (7)$$

74 where  $\sigma \geq 0$  is a fixed slack budget. In our implementation,  $\sigma$  does *not* change the pruning trigger; it  
75 caps the post-prune target length when combined with Max\_Drop (Sec. 3.4).

### 76 3.4 Max\_Drop (Staged Eviction)

77 Periodic pruning can cause “eviction cliffs” when a large block is removed at once, which we observed  
78 as token-level NLL spikes on long-form generation. Max\_Drop limits the maximum number of  
79 tokens evicted in a single prune event.

80 Let  $\delta \geq 0$  be the maximum drop size. When pruning is triggered, we set a target retained length

$$L_t^* = \begin{cases} C, & \delta = 0 \\ \min(\max(L_t - \delta, C), H), & \delta > 0 \end{cases} \quad (8)$$

81 and prune the cache to keep exactly  $L_t^*$  tokens using the Start+Recent rule. This turns a single large  
82 eviction into multiple smaller evictions across steps while remaining within the hard capacity  $H$ .

83 **Hyperparameter interactions and a toy example.** When  $\delta > 0$ , staged eviction can leave  
84  $L_t^* > C$ , so pruning may trigger again soon; this is intentional. A practical rule-of-thumb to avoid  
85 pruning *every* step when the cache saturates at  $H$  is to choose  $\sigma < R$  (so that after pruning to  $H$ ,  
86 the overflow remains  $< R$  until enough new tokens arrive). For example, with  $(S, W, R, \sigma, \delta) =$   
87  $(4, 2044, 32, 16, 32)$  (so  $C = 2048$ ,  $H = 2064$ ), if a step reaches  $L_t = 2090$  (overflow = 42), we  
88 prune to  $L_t^* = \min(\max(2090 - 32, 2048), 2064) = 2058$  and continue staging further evictions as  
89 decoding proceeds.

### 90 3.5 Algorithm Summary

91 Algorithm 1 summarizes the pruning control logic (RoPE re-alignment and buffer management are  
92 omitted for clarity).

Table 1: Main results on PG19 (long-context, *fill values via script output*).

Method	TPOT↓	Speedup↑	PPL↓	Peak Mem (MB)↓
Baseline (Full KV)	100.53	1.00×	19.761	5722
StreamingLLM (MIT)	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]
Ours (Lazy/Slack/Max_Drop)	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]

Table 2: Sanity-check results on WikiText-103 (short-context).

Method	TPOT↓	Speedup↑	PPL↓
Baseline (Full KV)	98.86	1.00×	9.359
StreamingLLM (MIT)	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]
Ours (Lazy/Slack/Max_Drop)	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]

## 4 Experiments

### 4.1 Setup

We evaluate on Pythia-2.8B. We use WikiText-103 as a short-context sanity check and PG19 as the primary long-context benchmark [9]. We report TTFT, TPOT (ms/token), throughput (tok/s), total runtime, peak GPU memory, and perplexity (PPL). **Baselines and fairness.** Our long-context evaluation must respect the model’s maximum position length. Therefore, we compare methods under the same *effective context cap*  $C$  (Sec. 3): the non-streaming baseline uses a sliding window of length  $C$  and recomputes attention each step (no KV cache), while StreamingLLM variants reuse KV cache and apply pruning/re-alignment to stay within the same cap. All methods share the same model, dataset segment, and evaluation protocol implemented in `experiments/eval_streaming_llm.py`.

**Protocol and repeatability.** To reduce measurement noise, our reproduction script runs a warmup pass followed by  $N$  repeated trials for each configuration and reports mean and standard deviation (saved in JSON). Each JSON record includes environment fingerprints (GPU, driver, torch/CUDA) to prevent reusing baselines across incompatible environments.

### 4.2 Main Results and Ablations

We provide a one-click script (`run_paper_experiments.sh`) that runs all configurations and generates LaTeX tables automatically. If the tables are not generated yet, we show placeholders.

**Implementation-path fairness check.** To ensure that improvements are not caused by divergent code paths, we also report an *Ours-framework-only* configuration that uses our wrapper implementation but matches Start+Recent semantics (MIT-style cache backend) with all proposed mechanisms disabled.

### Ablations.

## 5 Discussion

**Why do popular inference accelerations fail in batch-1 streaming?** In our setting, streaming bounds attention length, shifting the bottleneck toward MLP and framework/launch overhead. Therefore, further optimizing attention kernels can have limited impact. Moreover, methods that assume static shapes or stable cache semantics may be incompatible with pruning and RoPE re-alignment in streaming decode.

**Attempts and analysis of ineffective methods.** We tested several common acceleration routes (see our project log in `docs/`): (i) FlashAttention integration was non-trivial under RoPE re-alignment and did not improve batch-1 TPOT in our environment; (ii) speculative decoding was unreliable on long-form generation and incompatible with streaming cache management; (iii) quantization via TorchAO exhibited numerical issues (INT8 v1) and remained slower even when stabilized

Table 3: Ablation study for Slack and Max\_Drop (PG19).

Setting	TPOT↓	Speedup↑	PPL↓
w/o Slack ( $\sigma = 0$ )	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]
w/o Max_Drop ( $\delta = 0$ )	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]
Full (Lazy+Slack+Max_Drop)	[INSERT DATA]	[INSERT DATA]	[INSERT DATA]

Table 4: Summary of investigated but ineffective optimization routes in our batch-1 streaming setting.

Method	Outcome	Notes (see project logs)
FlashAttention / FlashDecoding	No gain / hard to integrate	Streaming already bounds attention length; remaining bottlenecks are MLP and launch/framework overhead; RoPE re-alignment complicates clean integration.
Speculative decoding	No gain / unreliable	Long-form generation yields low acceptance; cache consistency with pruning is fragile.
Quantization (TorchAO INT8/INT4)	Slower / unstable	INT8 WO v1 produced NaNs; v2 is stable but slower for batch-1 decode in our stack; INT4 backend dependencies were problematic.
<code>torch.compile</code> / CUDA Graphs	Unstable	Repeated-run CUDA graph overwrite errors observed in rotary-embedding path; shape/cache semantics hinder capture.
HF StaticCache	Incompatible	StaticCache assumes fixed cache updates; pruning can trigger device-side asserts (index out of bounds).
CUDA fusion (residual/LN)	No gain	Amdahl’s law: residual/LN is a small fraction; custom kernel launch overhead dominated, leading to slowdown.

126 (INT8 v2) in batch-1 streaming decode; (iv) `torch.compile` with CUDA Graphs was unstable  
 127 due to overwritten outputs in rotary-embedding paths; (v) HuggingFace StaticCache conflicted with  
 128 pruning updates and triggered device-side asserts. These results highlight that strong batch-inference  
 129 accelerations do not directly transfer to batch-1 streaming decode.

## 130 6 Conclusion

131 We presented three modular KV-cache management mechanisms for StreamingLLM: Lazy Pruning,  
 132 Slack, and Max\_Drop. Our method is training-free and targets long-context decoding where pruning  
 133 overhead and eviction-induced quality loss become important. We provide a reproducible pipeline  
 134 and report negative results to clarify which acceleration techniques do or do not apply in this regime.

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