Extension: In-Place Placebo for Piauí

```
install.packages("dplyr")
install.packages("ggplot2")
install.packages("Synth")
install.packages("xtable")
install.packages("ggpubr")
# Load Data
load("data/DATA_COMPLETE.RData")
load("data/abbr_code.RData")
# Subsetting data by grade and subject (for all states, including PI):
PRIMARY_M <- as.data.frame(filter(DATA_COMPLETE, grade == "P", subject == "math"))
PRIMARY_P <- as.data.frame(filter(DATA_COMPLETE, grade == "P", subject == "port"))</pre>
LOWERS_M <- as.data.frame(filter(DATA_COMPLETE, grade == "LS", subject == "math"))
LOWERS_P <- as.data.frame(filter(DATA_COMPLETE, grade == "LS", subject == "port"))
UPPERS_M <- as.data.frame(filter(DATA_COMPLETE, grade == "US", subject == "math"))</pre>
UPPERS_P <- as.data.frame(filter(DATA_COMPLETE, grade == "US", subject == "port"))</pre>
                                  # Function: prepare_p_ls_PI()
# Description: prepares data for the synth function - primary and lower secondary school
prepare_p_ls_PI <- function(data){</pre>
 library(Synth)
 predictors <- c("homicides", "TWh", "ln pop", "unemployment", "edu invest pc")</pre>
 DATA_PM <- dataprep(foo = data,</pre>
                      predictors = predictors,
                      dependent = "score",
                      unit.variable = "code_state",
                      time.variable = "year",
                      unit.names.variable = "abbr_state",
                      treatment.identifier = 22, # Piauí Code
                      controls.identifier = c(11:17, 21, 24:29, 31:33, 35, 41:43, 50:53),
                      # Exclude PI (22) and CE (23) from controls
                      time.predictors.prior = seq(1995, 2007, 2),
                      time.optimize.ssr = seq(1995, 2007, 2),
time.plot = seq(1995, 2019, 2))
 return(DATA PM)
};
# Function: prepare_us_PI()
# Description: prepares data for the synth function - upper secondary school
prepare_us_PI <- function(data){</pre>
 library(Synth)
```

```
predictors <- c("homicides", "TWh", "unemployment", "ln_pop", "edu_invest_pc")</pre>
  DATA_PM <- dataprep(foo = data,</pre>
                      predictors = predictors,
                      dependent = "score",
                      unit.variable = "code state",
                      time.variable = "year",
                      unit.names.variable = "abbr state",
                      treatment.identifier = 22, # Piauí Code
                      controls.identifier = c(11:17, 21, 24:26, 28:29, 31:33, 35, 41:43, 50:53),
                      # Exclude PI (22) and CE (23) from controls
                      time.predictors.prior = seq(1995, 2009, 2),
                      time.optimize.ssr = seq(1995, 2009, 2),
                                            = seq(1995, 2019, 2))
                      time.plot
 return (DATA_PM)
};
# Preparing data for Synth for PI
                                -----#
# Prepare data for SCM (specifying PI as the treatment unit):
DATA_PI_PM <- prepare_p_ls_PI(PRIMARY_M)</pre>
DATA_PI_PP <- prepare_p_ls_PI(PRIMARY_P)</pre>
DATA_PI_LSM <- prepare_p_ls_PI(LOWERS_M)</pre>
DATA_PI_LSP <- prepare_p_ls_PI(LOWERS_P)</pre>
DATA_PI_USM <- prepare_us_PI(UPPERS_M)</pre>
DATA_PI_USP <- prepare_us_PI(UPPERS_P)</pre>
# Primary School Mathematics and Portuguese
DATA_PI_PM <- prepare_p_ls_PI(PRIMARY_M)</pre>
DATA_PI_PP <- prepare_p_ls_PI(PRIMARY_P)</pre>
# Lower Secondary School Mathematics and Portuguese
DATA_PI_LSM <- prepare_p_ls_PI(LOWERS_M)</pre>
DATA_PI_LSP <- prepare_p_ls_PI(LOWERS_P)</pre>
# Upper Secondary School Mathematics and Portuguese
DATA_PI_USM <- prepare_us_PI(UPPERS_M)</pre>
DATA_PI_USP <- prepare_us_PI(UPPERS_P)</pre>
# Function: plot scm PI()
# Description: prepares data from the synthetic control output to be plotted with qqplot
plot_scm_PI <- function(original_data, synth.tables){</pre>
 library(tidyverse)
  W <- as.data.frame(synth.tables[["tab.w"]])</pre>
  str(W)
  W <- W %>%
   filter(w.weights > 0.01) %>%
```

```
mutate(w.weights = round(w.weights, digits = 3)) %>%
   rename(abbr_state = unit.names)
 str(original_data)
 str(W)
 SC <- left_join(original_data, select(W, -unit.numbers), by = "abbr_state") %>%
   na.omit() %>%
   group_by(year) %>%
   summarise(sc = weighted.mean(score, w.weights))
 PI <- original_data %>%
   filter(abbr_state == "PI") %>%
   select(year, score)
 GAP <- left_join(PI, SC, by = "year") %>%
   mutate(gap = score - sc)
 GAP$grade <- unique(original_data$grade)</pre>
 GAP$subject <- unique(original_data$subject)</pre>
 GG_DATA <- left_join(PI, SC, by = "year") %>%
   pivot_longer(!year, names_to = "unit", values_to = "score")
 GG_DATA$unit[GG_DATA$unit == "score"] <- "Piauí"</pre>
 GG_DATA$unit[GG_DATA$unit == "sc"] <- "Synthetic Control"</pre>
 GG_DATA$grade <- unique(original_data$grade)</pre>
 GG_DATA$subject <- unique(original_data$subject)</pre>
 return(list(GG_DATA, GAP))
}
                           -----#
# Data Preparation for Plotting
# Run SCM for Primary School Mathematics (PI)
SCM_PI_PM <- synth(DATA_PI_PM)</pre>
##
## X1, X0, Z1, Z0 all come directly from dataprep object.
##
## ********
## searching for synthetic control unit
##
##
## *********
## *********
## ********
##
## MSPE (LOSS V): 3.721776
## solution.v:
## 0.2217879 1.9274e-06 0.05259182 1.4035e-06 0.7256169
##
## solution.w:
```

```
## 2.826e-07 4.5732e-06 1.2587e-06 8.076e-07 8.55e-08 6.889e-07 0.2006367 0.7843464 8.30438e-05 2.789e
TABLES_PI_PM <- synth.tab(dataprep.res = DATA_PI_PM, synth.res = SCM_PI_PM)
# Run SCM for Primary School Portuguese (PI)
SCM_PI_PP <- synth(DATA_PI_PP)</pre>
##
## X1, X0, Z1, Z0 all come directly from dataprep object.
##
## ********
       searching for synthetic control unit
##
##
## *********
## ********
## *********
## MSPE (LOSS V): 2.328019
##
## solution.v:
## 0.2679382 0.2692525 0.3424016 0.01790257 0.1025051
##
## solution.w:
 \texttt{\#\#} \quad 3.906 \texttt{e} - 07 \ 5.719 \texttt{e} - 07 \ 3.559 \texttt{e} - 07 \ 3.107 \texttt{e} - 07 \ 2.231 \texttt{e} - 07 \ 2.397 \texttt{e} - 07 \ 0.3178909 \ 0.3319879 \ 0.22772 \ 4.4972 \texttt{e} - 06 \ 0.3178999 \ 0.3319879 \ 0.22772 \ 0.3178999 \ 0.3319879 \ 0.22772 \ 0.3178999 \ 0.3319879 \ 0.22772 \ 0.3178999 \ 0.3319879 \ 0.22772 \ 0.3178999 \ 0.3319879 \ 0.22772 \ 0.3178999 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 0.3319879 \ 
TABLES_PI_PP <- synth.tab(dataprep.res = DATA_PI_PP, synth.res = SCM_PI_PP)
# Run SCM for Lower Secondary School Mathematics (PI)
SCM_PI_LSM <- synth(DATA_PI_LSM)</pre>
## X1, X0, Z1, Z0 all come directly from dataprep object.
##
##
## *********
##
       searching for synthetic control unit
##
##
## ********
## *********
## ********
##
## MSPE (LOSS V): 3.474292
##
## solution.v:
## 0.1356106 0.2475876 0.5476153 0.00824473 0.06094185
##
## 2.2678e-06 2.1181e-06 1.2029e-06 1.5922e-06 1.0822e-06 1.2055e-06 0.2051833 0.1434177 0.4222922 0.1
TABLES_PI_LSM <- synth.tab(dataprep.res = DATA_PI_LSM, synth.res = SCM_PI_LSM)
# Run SCM for Lower Secondary School Portuguese (PI)
SCM_PI_LSP <- synth(DATA_PI_LSP)</pre>
```

```
##
## X1, X0, Z1, Z0 all come directly from dataprep object.
##
##
## ********
##
  searching for synthetic control unit
##
##
## ********
## *********
## *********
## MSPE (LOSS V): 13.90849
##
## solution.v:
## 0.09991008 0.8858695 0.005624223 0.002671255 0.005924897
##
## solution.w:
## 3.276e-07 2.258e-07 2.016e-07 1.964e-07 2.108e-06 1.409e-07 0.38369 4.78991e-05 0.6160384 4.045e-06
TABLES_PI_LSP <- synth.tab(dataprep.res = DATA_PI_LSP, synth.res = SCM_PI_LSP)
# Run SCM for Upper Secondary School Mathematics (PI)
SCM_PI_USM <- synth(DATA_PI_USM)</pre>
##
## X1, X0, Z1, Z0 all come directly from dataprep object.
##
##
## ********
  searching for synthetic control unit
##
##
##
## ********
## ********
## ********
##
## MSPE (LOSS V): 14.74899
##
## solution.v:
## 0.0876074 0.1164132 0.01563386 0.6786735 0.1016721
## solution.w:
## 1.9562e-06 5.323e-07 1.2371e-06 5.026e-07 3.827e-07 4.595e-07 0.4235325 0.5760261 2.4744e-05 0.0003
TABLES_PI_USM <- synth.tab(dataprep.res = DATA_PI_USM, synth.res = SCM_PI_USM)</pre>
# Run SCM for Upper Secondary School Portuguese (PI)
SCM_PI_USP <- synth(DATA_PI_USP)</pre>
##
## X1, X0, Z1, Z0 all come directly from dataprep object.
##
## ********
```

```
## searching for synthetic control unit
##
##
## ********
## ********
## ********
## MSPE (LOSS V): 20.3554
##
## solution.v:
## 0.0492984 0.1164686 0.04759728 0.5881315 0.1985042
##
## solution.w:
## 6.427e-07 1.385e-07 8.41e-08 1.073e-07 6.55e-08 6.06e-08 0.3966485 0.6033413 1.387e-07 1.6328e-06 1
TABLES_PI_USP <- synth.tab(dataprep.res = DATA_PI_USP, synth.res = SCM_PI_USP)
# Graphs in applot for Piauí
PM_PI <- plot_scm_PI(PRIMARY_M, TABLES_PI_PM)</pre>
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v forcats 1.0.0 v stringr 1.5.1
## v lubridate 1.9.3 v tibble
                                 3.2.1
## v purrr 1.0.2
                                 1.3.0
                      v tidyr
            2.1.4
## v readr
## -- Conflicts ----- tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
## 'data.frame': 25 obs. of 3 variables:
## $ w.weights : num 0 0 0 0 0 0.201 0.784 0 0 ...
## $ unit.names : chr "RO" "AC" "AM" "RR" ...
## $ unit.numbers: num 11 12 13 14 15 16 17 21 24 25 ...
## 'data.frame': 351 obs. of 14 variables:
## $ abbr_state : chr "AC" "AC" "AC" "AC" ...
## $ code_state : num 12 12 12 12 12 27 27 27 27 27 ...
## $ year
               : num 1995 1997 1999 2001 2003 ...
                : chr "P" "P" "P" "P" ...
## $ grade
## $ subject
                : chr "math" "math" "math" ...
## $ score
                : num 168 166 162 152 159 ...
## $ TWh
                : num 0.0139 0.0132 0.0137 0.0198 0.0227 ...
## $ homicides : num 22.62 19.99 9.66 21.24 22.04 ...
               : num 455242 500185 527937 574355 600595 ...
## $ pop
## $ ln_pop : num 13 13.1 13.2 13.3 13.3 ...
## $ unemployment : num 9.8 8.89 12.2 8.56 7.45 ...
## $ gini : num 0.582 0.574 0.621 0.623 0.578 ...
## $ edu_invest : num 3.69e+08 4.34e+08 4.54e+08 6.19e+08 6.26e+08 ...
## $ edu_invest_pc: num 811 868 860 1077 1042 ...
## 'data.frame': 3 obs. of 3 variables:
## $ w.weights : num 0.201 0.784 0.015
## $ unit.numbers: num 17 21 42
```

```
PM_PI_SC <- PM_PI[[1]]</pre>
PM_PI_GAP <- PM_PI[[2]]</pre>
PP_PI <- plot_scm_PI(PRIMARY_P, TABLES_PI_PP)
## 'data.frame':
                   25 obs. of 3 variables:
## $ w.weights : num 0 0 0 0 0 0.318 0.332 0.228 0 ...
## $ unit.names : chr "RO" "AC" "AM" "RR" ...
## $ unit.numbers: num 11 12 13 14 15 16 17 21 24 25 ...
## 'data.frame': 351 obs. of 14 variables:
## $ abbr_state : chr "AC" "AC" "AC" "AC" ...
## $ code state : num 12 12 12 12 12 27 27 27 27 27 ...
                 : num 1995 1997 1999 2001 2003 ...
## $ year
                         "P" "P" "P" "P" ...
## $ grade
                  : chr
## $ subject
                : chr "port" "port" "port" "port" ...
## $ score
                 : num 166 160 154 148 158 ...
## $ TWh
                  : num 0.0139 0.0132 0.0137 0.0198 0.0227 ...
## $ homicides : num 22.62 19.99 9.66 21.24 22.04 ...
## $ pop
                 : num 455242 500185 527937 574355 600595 ...
## $ ln_pop
               : num 13 13.1 13.2 13.3 13.3 ...
## $ unemployment : num 9.8 8.89 12.2 8.56 7.45 ...
## $ gini
             : num 0.582 0.574 0.621 0.623 0.578 ...
## $ edu_invest : num 3.69e+08 4.34e+08 4.54e+08 6.19e+08 6.26e+08 ...
## $ edu_invest_pc: num 811 868 860 1077 1042 ...
## 'data.frame':
                 4 obs. of 3 variables:
## $ w.weights : num 0.318 0.332 0.228 0.122
## $ abbr state : chr "TO" "MA" "RN" "SC"
## $ unit.numbers: num 17 21 24 42
PP_PI_SC <- PP_PI[[1]]</pre>
PP_PI_GAP <- PP_PI[[2]]</pre>
LSM_PI <- plot_scm_PI(LOWERS_M, TABLES_PI_LSM)
## 'data.frame':
                   25 obs. of 3 variables:
## $ w.weights : num 0 0 0 0 0 0.205 0.143 0.422 0.105 ...
## $ unit.names : chr "RO" "AC" "AM" "RR" ...
## $ unit.numbers: num 11 12 13 14 15 16 17 21 24 25 ...
## 'data.frame': 351 obs. of 14 variables:
## $ abbr_state : chr "AC" "AC" "AC" "AC" ...
## $ code state : num 12 12 12 12 12 27 27 27 27 27 ...
## $ year
                 : num 1995 1997 1999 2001 2003 ...
## $ grade
                  : chr
                         "LS" "LS" "LS" "LS" ...
## $ subject
                : chr "math" "math" "math" "math" ...
## $ score
                 : num 223 220 223 219 225 ...
## $ TWh
                  : num 0.0139 0.0132 0.0137 0.0198 0.0227 ...
                : num 22.62 19.99 9.66 21.24 22.04 ...
## $ homicides
                 : num 455242 500185 527937 574355 600595 ...
## $ pop
## $ ln_pop
                  : num 13 13.1 13.2 13.3 13.3 ...
## $ unemployment : num 9.8 8.89 12.2 8.56 7.45 ...
## $ gini
                  : num 0.582 0.574 0.621 0.623 0.578 ...
## $ edu_invest
                : num 3.69e+08 4.34e+08 4.54e+08 6.19e+08 6.26e+08 ...
## $ edu_invest_pc: num 811 868 860 1077 1042 ...
## 'data.frame':
                5 obs. of 3 variables:
```

```
## $ w.weights : num 0.205 0.143 0.422 0.105 0.124
## $ abbr_state : chr "TO" "MA" "RN" "PB" ...
## $ unit.numbers: num 17 21 24 25 42
LSM_PI_SC <- LSM_PI[[1]]
LSM_PI_GAP <- LSM_PI[[2]]
LSP_PI <- plot_scm_PI(LOWERS_P, TABLES_PI_LSP)
## 'data.frame': 25 obs. of 3 variables:
## $ w.weights : num 0 0 0 0 0 0.384 0 0.616 0 ...
## $ unit.names : chr "RO" "AC" "AM" "RR" ...
## $ unit.numbers: num 11 12 13 14 15 16 17 21 24 25 ...
## 'data.frame': 351 obs. of 14 variables:
## $ abbr_state : chr "AC" "AC" "AC" "AC" ...
## $ code_state : num 12 12 12 12 12 27 27 27 27 27 ...
## $ year : num 1995 1997 1999 2001 2003 ...
## $ grade
## $ grade : chr "LS" "LS" "LS" "LS" ...
## $ subject : chr "port" "port" "port" "port" ...
## $ score
                 : chr "LS" "LS" "LS" "LS" ...
## $ score
                 : num 227 223 217 218 223 ...
            : num 0.0139 0.0132 0.0137 0.0198 0.0227 ...
## $ TWh
## $ homicides : num 22.62 19.99 9.66 21.24 22.04 ...
## $ pop : num 455242 500185 527937 574355 600595 ...
## $ ln_pop : num 13 13.1 13.2 13.3 13.3 ...
## $ unemployment : num 9.8 8.89 12.2 8.56 7.45 ...
## $ gini
            : num 0.582 0.574 0.621 0.623 0.578 ...
## $ edu_invest : num 3.69e+08 4.34e+08 4.54e+08 6.19e+08 6.26e+08 ...
## $ edu_invest_pc: num 811 868 860 1077 1042 ...
## 'data.frame': 2 obs. of 3 variables:
## $ w.weights : num 0.384 0.616
## $ unit.numbers: num 17 24
LSP_PI_SC <- LSP_PI[[1]]
LSP_PI_GAP <- LSP_PI[[2]]
# Combining Graph Data for Piauí
DATA_GRAPH_PI <- rbind(PM_PI_SC, PP_PI_SC, LSM_PI_SC, LSP_PI_SC)
# Adjusting Labels for Piauí data
DATA_GRAPH_PI$grade[DATA_GRAPH_PI$grade=="P"] <- "Primary Education"
DATA_GRAPH_PI$grade[DATA_GRAPH_PI$grade=="LS"] <- "Lower Secondary Education"
DATA_GRAPH_PI$grade <- factor(DATA_GRAPH_PI$grade, levels = c("Primary Education", "Lower Secondary Edu
DATA_GRAPH_PI$subject[DATA_GRAPH_PI$subject=="math"] <- "Mathematics"
DATA_GRAPH_PI$subject[DATA_GRAPH_PI$subject=="port"] <- "Portuguese"
# Plotting
# Figure for Primary Education in PI
a_06_PI <- ggplot(data = filter(DATA_GRAPH_PI, grade == "Primary Education"), aes(x = year, y = score,
 geom_vline(xintercept = 2008, color = "#636363", linetype = "dashed", size = 0.9) +
 geom_vline(xintercept = 2011, color = "#636363", linetype = "dashed", size = 0.9) +
```

```
geom_line(size = 0.9) +
  scale_color_manual(values = c("#42B1BD", "#D26B5F"), labels = c("Piauí", "Synthetic Piauí"), name = "
  ylab("Score") +
  xlab("") +
  annotate("text", x = 2007, y = 220, label = "TI", color = "#636363", size = 4) +
  annotate("text", x = 2013, y = 152, label = "TI + TA", color = "#636363", size = 4) +
 theme_bw() +
 theme(panel.grid.major = element blank(), panel.grid.minor = element blank(), legend.position = "bott
 facet_grid(vars(grade), vars(subject))
## Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use `linewidth` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
# Figure for Lower Secondary Education in PI
b_06_PI <- ggplot(data = filter(DATA_GRAPH_PI, grade == "Lower Secondary Education"), aes(x = year, y =
  geom_vline(xintercept = 2008, color = "#636363", linetype = "dashed", size = 0.9) +
  geom_vline(xintercept = 2015, color = "#636363", linetype = "dashed", size = 0.9) +
  geom_line(size = 0.9) +
  scale_color_manual(values = c("#42B1BD", "#D26B5F"), labels = c("Piauí", "Synthetic Piauí"), name = "
 ylab("Score") +
  xlab("Year") +
  annotate("text", x = 2007, y = 250, label = "TI", color = "#636363", size = 4) +
  annotate("text", x = 2017, y = 190, label = "TI + TA", color = "#636363", size = 4) +
 theme_bw() +
  theme(panel.grid.major = element_blank(), panel.grid.minor = element_blank(), legend.position = "bott
 facet_grid(vars(grade), vars(subject))
# Arrange and Save the Plots
ggarrange(a_06_PI, b_06_PI, ncol = 1, nrow = 2, common.legend = TRUE, legend = "bottom")
```

