OFM 3 - Performance Assessment Task 2: Dimensionality Reduction Methods

Part I: Research Question

A1.

For this analysis, we will be attempting to utilize a principal component analysis (PCA) in order to determine the principal components within the 'Churn' dataset that impact customer churn.

A2.

The goal of the analysis is to successfully implement PCA on a set of continuous feature variables within our dataset in order to specifically identify any principal components that may impact customer churn.

Part II: Method Justification

B1.

PCA works by reducing the dimensionality (the variables/number of features within the dataset) of different variables that are correlated with each other, heavily or lightly, while retaining the variance already present in the dataset. PCA transforms the existing variables into a new set of variables, the principal components, that are orthogonal and ordered so that they retain the variance of the original variables. These principal components are ordered from most variance to least variance, with the first principal component retaining the maximum variation present in the original components of the dataset (Principal Component Analysis Tutorial, 2016).

We expect that our PCA will identify the principal components within our dataset, along with the explained variance for each component.

B2.

One assumption of principal component analysis is that PCA makes the assumption that components with large variance correspond to interesting dynamics, whereas lower variance components correspond to noise and are deemed uninteresting (CSE 564 - Visualization, n.d.).

Part III: Data Preparation

C1.

In preparing our dataset for PCA, we first want to determine the continuous variables we will use to determine the principal components that impact customer churn. We can utilize Pandas .info() function to return the list of features in our dataset, along with their data types and counts:

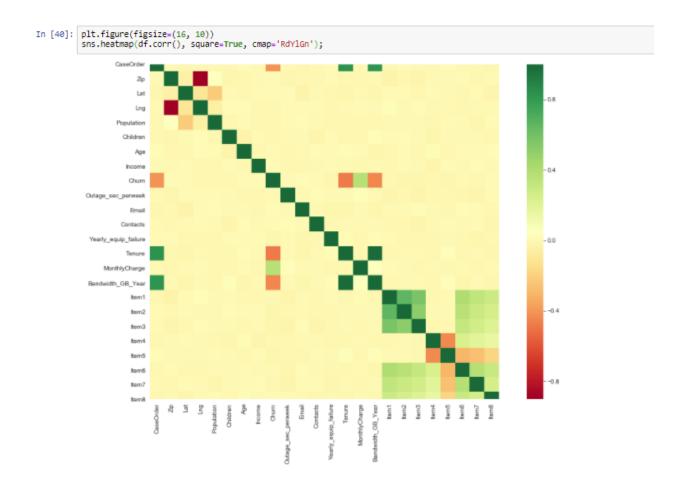
```
In [26]: #gets the data type and count of all variables in the data set
df.info()
          <class 'pandas.core.frame.DataFrame'>
          RangeIndex: 10000 entries, 0 to 9999
         Data columns (total 50 columns):
                                  10000 non-null int64
         CaseOrder
          Customer_id
                                  10000 non-null object
          Interaction
                                  10000 non-null object
                                  10000 non-null object
         city
                                 10000 non-null object
          state
                                  10000 non-null object
         County
                                 10000 non-null object
          Zip
                                  10000 non-null int64
         Lat
                                 10000 non-null float64
                                  10000 non-null float64
          Lng
         Population
                                  10000 non-null int64
                                  10000 non-null object
          Area
          TimeZone
                                  10000 non-null object
                                  10000 non-null object
          Job
          Children
                                  10000 non-null int64
         Age
Income
                                 10000 non-null int64
                                  10000 non-null float64
         Marital
                                 10000 non-null object
         Gender
                                 10000 non-null object
         Churn
                                 10000 non-null object
                                 10000 non-null float64
         Outage_sec_perweek
          Email
                                  10000 non-null int64
         Contacts
                                  10000 non-null int64
          Yearly_equip_failure 10000 non-null int64
          Techie
                                  10000 non-null object
                                  10000 non-null object
          Port modem
                                  10000 non-null object
                                  10000 non-null object
          InternetService
                                 10000 non-null object
          Phone
                                 10000 non-null object
         Multiple
                                 10000 non-null object
                                 10000 non-null object
         OnlineSecurity
         OnlineBackup
DeviceProtection
                                  10000 non-null object
                                 10000 non-null object
          TechSupport
                                  10000 non-null object
                                  10000 non-null object
         StreamingTV
          StreamingMovies
                                  10000 non-null object
         PaperlessBilling
                                 10000 non-null object
          PaymentMethod
                                  10000 non-null object
         Tenure
                                  10000 non-null float64
         MonthlyCharge
                                  10000 non-null float64
         Bandwidth_GB_Year
                                  10000 non-null float64
                                  10000 non-null int64
         Item1
          Ttem2
                                  10000 non-null int64
                                  10000 non-null int64
          Item3
          Item4
                                  10000 non-null int64
                                  10000 non-null int64
          Item5
                                  10000 non-null int64
          Item7
                                  10000 non-null int64
                                  10000 non-null int64
          Item8
          dtypes: float64(7), int64(16), object(27)
          memory usage: 3.8+ MB
```

We now have a list of features and their data types from our dataset. We can identify the following continuous variables that we will use as predictor variables for our PCA:

- Age
- Bandwidth_GB_Year
- Children
- Contacts
- Email
- Income
- MonthlyCharge
- Outage_sec_perweek
- Tenure
- Yearly_equip_failure
- Zip

Because we are trying to determine which principal components impact customer churn, our dependent variable will be 'Churn'.

As an additional step to look for multicollinearity within our variables, we will utilize a correlation heatmap to look at the positive and negative correlations within our data:



As we see in the above heatmap, it appears that the only variables that have any correlation with 'Churn' are 'Tenure', 'Bandwidth_GB_Year', and 'MonthlyCharge'. These correlations are not particularly strong, but they do exist. Luckily, it does not appear we have a strong multicollinearity issue with our selected variables.

C2.

PCA requires standardized variables in order to be accurate. Before we can standardize our variables, we need to perform some steps.

First, since 'Churn' is currently a string variable with 'Yes' and 'No' as observations, we need to change these values to be binary values with a 1 = Yes and 0 = No so that the PCA model can read the data. We can do this quickly utilizing Pandas .replace() function:

df.Churn.replace(('Yes', 'No'), (1, 0), inplace=True)

Next, we split the selected continuous variables into their own data frame:

df2 = df[['Age', 'Bandwidth_GB_Year', 'Children', 'Contacts', 'Churn', 'Email', 'Income', 'MonthlyCharge', 'Outage_sec_perweek', 'Tenure', 'Yearly_equip_failure', 'Zip']]

We then check the top rows of our new data frame:

```
df2.head()
```

We then need to define our features and our target variables:

```
x = df2[['Age;'Bandwidth_GB_Year;'Children;'Contacts;'Email', 'Income', 'MonthlyCharge',
'Outage_sec_perweek', 'Tenure', 'Yearly_equip_failure', 'Zip']]
y = df2['Churn']
```

Now we are ready to create our pipeline and standardize our data:

```
from sklearn.decomposition import PCA
from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
pca = PCA()
pipeline = make_pipeline(scaler, pca)
X = pipeline.fit_transform(x)
```

C2.

Please see the attached 'D212_Task2_Dataset.csv'.

Part IV: Analysis

D1.

After creating our pipeline to standardize our data, we print the covariance matrix of our principal components:

```
print('Eigenvectors \n%s' %pca.get_covariance())
print('\nEigenvalues \n%s' %pca.explained_variance_)
```

```
Eigenvectors
[[ 1.00010001 -0.01472512 -0.02973451 0.01506913 0.00158808 -0.00409101 0.01072958 -0.00804752 0.01698097 0.00857821 -0.0081361]
[-0.01472512 1.00010001 0.02558738 0.00329905 -0.01458061 0.00367392 0.06041247 0.00417608 0.99159435 0.0120349 -0.00252745]
[-0.02973451 0.02558738 1.00010001 -0.02077811 0.00447925 0.00994335 -0.00978238 0.00188944 -0.00509183 0.00732132 -0.01720677]
[0.01506913 0.00329905 -0.02077811 1.00010001 0.00304067 0.00123332 0.00425907 0.01509319 0.00282037 -0.00603285 -0.00471999]
[0.00158808 -0.01458061 0.00447925 0.00304067 1.00010001 -0.00926842 0.00199675 0.00399413 -0.01446932 -0.01635598 -0.0078608]
```

```
[-0.00409101 0.00367392 0.00994335 0.00123332 -0.00926842 1.00010001 -0.00301427 -0.01001155 0.00211458 0.00542382 0.00294682]
[0.01072958 0.06041247 -0.00978238 0.00425907 0.00199675 -0.00301427 1.00010001 0.02049812 -0.00333714 -0.00717299 -0.00871765]
[-0.00804752 0.00417608 0.00188944 0.01509319 0.00399413 -0.01001155 0.02049812 1.00010001 0.00293225 0.00290902 -0.01152155]
[0.01698097 0.99159435 -0.00509183 0.00282037 -0.01446932 0.00211458 -0.00333714 0.00293225 1.00010001 0.01243615 -0.00322746]
[0.00857821 0.0120349 0.00732132 -0.00603285 -0.01635598 0.00542382 -0.00717299 0.00290902 0.01243615 1.00010001 0.01104802]
[-0.0081361 -0.00252745 -0.01720677 -0.00471999 -0.0078608 0.00294682 -0.00871765 -0.01152155 -0.00322746 0.01104802 1.00010001]]

Eigenvalues
[1.99435251 1.05401359 1.03762842 1.0126684 1.00302824 0.99851856]
```

D2.

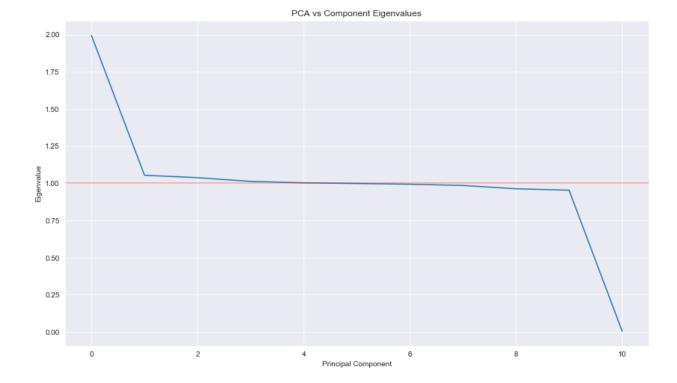
After retrieving the covariance matrix of all of our principal components, we create a scree plot to plot our principal components compared to their eigenvalues:

```
def scree_plot():
    from matplotlib.pyplot import figure, show
    from matplotlib.ticker import MaxNLocator

ax = figure(figsize=(14,8)).gca()
    ax.plot(explained_variance)
    ax.xaxis.set_major_locator(MaxNLocator(integer=True))
    plt.xlabel('Principal Component')
    plt.ylabel('Eigenvalue')
    plt.axhline(y=1, linewidth=2, color='r', alpha=0.25)
    plt.title('PCA vs Component Eigenvalues')
    show()

scree_plot()
```

0.99369936 0.98525965 0.96305395 0.95341089 0.00546654]



We can see from this scree plot that there is a large difference in variance between component 0 and 1, but then the differences in variance slowly decrease until component 9-10. The Kaiser criterion generally states that a component should not be retained unless its eigenvalue is greater than or equal to one (Kaiser Rule - Displayr, n.d.). Based on this rule and our scree plot, we can determine that components 0, 1, 2, 3, and 4 are significant, while components 5-10 are not.

D3.

After determining our number of components, we can utilize the .explained_variance_function of SciKit-Learn's PCA model to obtain the explained variance for all of our identified components:

```
explained_variance = pca.explained_variance_
explained_variance
```

array([1.99435251, 1.05401359, 1.03762842, 1.0126684, 1.00302824, 0.99851856, 0.99369936, 0.98525965, 0.96305395, 0.95341089, 0.00546654])

- Principal component 0 has a cumulative explained variance of 1.99435251
- Principal component 1 has a cumulative explained variance of 1.05401359
- Principal component 2 has a cumulative explained variance of 1.03762842
- Principal component 3 has a cumulative explained variance of 1.0126684
- Principal component 4 has a cumulative explained variance of 1.00302824
- Principal component 5 has a cumulative explained variance of 0.99851856
- Principal component 6 has a cumulative explained variance of 0.99369936
- Principal component 7 has a cumulative explained variance of 0.98525965

- Principal component 8 has a cumulative explained variance of 0.96305395
- Principal component 9 has a cumulative explained variance of 0.95341089
- Principal component 10 has a cumulative explained variance of 0.00546654

If we just want to obtain the explained variance of *only* our five principal components that have a eigenvalue greater than or equal to 1, we can obtain those with the following code that gives us just the first five principal components' explained variances:

```
explained_variance_pca = pca.explained_variance_[:5]
explained_variance_pca
```

[1.99435251 1.05401359 1.03762842 1.0126684 1.00302824]

- Principal component 0 has a cumulative explained variance of 1.99435251
- Principal component 1 has a cumulative explained variance of 1.05401359
- Principal component 2 has a cumulative explained variance of 1.03762842
- Principal component 3 has a cumulative explained variance of 1.0126684
- Principal component 4 has a cumulative explained variance of 1.00302824

D4.

To determine the total variance for our PCA, with all 10 of our identified principal components, we can simply sum the explained variance:

```
sum(explained_variance)
```

11.001100110010995

To determine the total variance of only our principal components with eigenvalues greater than or equal to 1, we can sum those by summing explained_variance_pca that we defined in the step above:

```
sum(explained_variance_pca)
```

6.101691171613005

As we can see, the total explained variance for all 10 principal components is 11.0, while the total explained variance for only our five principal components with eigenvalues greater than or equal to 1 is 6.10.

D5.

Our PCA has determined that there are five principal components with eigenvalues greater than or equal to 1 and are responsible for a large amount of variance within our dataset.

We can utilize a covariance matrix to sum the cumulative explained variance ratio that will inform us of how much variance each principal component accounts for:

```
covar_matrix = PCA(n_components = 5)
```

```
covar_matrix.fit(x)
variance = covar_matrix.explained_variance_ratio_ #calculate variance ratios

total_var = np.cumsum(covar_matrix.explained_variance_ratio_)
print(total_var)
```

[0.5104989 0.99693305 0.99999852 0.99999997 0.99999998]

As we can see above, the first feature explains 51% of the variance, the first two features explain 99.6% of the variance, the first three features explain 99% of the variance, and this continues with the first four and first five features increasingly explaining closer to 100% of the variance. This means that our first two principal components explain most, if not all of the variance. This means we likely could have selected only two principal components earlier, despite having five with an eigenvalue of greater than 1. As a result of our covariance matrix showing that nearly all the variance in the data can be explained with these principal components, we could likely trace back our principal components and explore them further in order to determine the exact causes of the variance, which will allow us to get a more insightful look at what leads to customer churn.

The recommendation to stakeholders within the business would be to explore these primary components in order to determine the differences between them and explore this difference in variance. By exploring these components, the business can gain valuable insight into common factors that cause customers to leave the service.

References

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- Principal Component Analysis Tutorial. (2016, March 2). ProjectPro.Io. Retrieved October 25, 2021, from https://www.projectpro.io/data-science-in-python-tutorial/principal-component-analysis-tutorial
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- Tavares, E. (2017, February 10). *Principle Component Analysis (PCA) with Scikit-Learn Python*. GitHub. Retrieved October 25, 2021, from https://etav.github.io/python/scikit_pca.html