

daily

August 19, 2025

Dark-Fiber Charakterisierung für entanglement polarisierter QKD

Aufbereitung und Analyse der Messdaten nach Tageszyklen

Autor: Laura Komma

Datensatz: Nordhausen - Sundhausen

1 Aufbereitung der Messdaten

1.1 Ressourcen und Literatur

- Messdaten
- Messgerät
- Plotting-Tool “py_pol”

1.2 Verwendete Libraries / Softwaretools

```
[78]: import pandas as pd
import matplotlib.pyplot as plt
import matplotlib.dates as mdates
import matplotlib.ticker as ticker
import numpy as np
import io
import datetime
from IPython.display import Image

from scipy.stats import norm
from scipy.signal import butter, filtfilt

from py_pol.jones_vector import Jones_vector, degrees
from py_pol.stokes import Stokes
```

1.3 Eigene Hilfsfunktionen

```
[3]: def format_time(x, pos):
    h = int(x) // 3600
    m = (int(x) % 3600) // 60
    return f"{h:02d}:{m:02d}"
```

```
[4]: def lowpass(data, box = 100):
    box = box
    LP_filter = np.full(int(box), 1/box)
    lps = np.convolve(ydata, LP_filter)
    lps = lps[ int((box-1) / 2) :len(lps) - int((box - 1) / 2)]
    return lps

def highpass(data, box = 100):
    lps = lowpass(data, box)
    hps = data - lps[:-1]
    return hps
```

```
[5]: def butter_filter(data, cutoff, fs=18, order=4, btype='low'):
    nyq = 0.5 * fs
    normal_cutoff = cutoff / nyq
    b, a = butter(order, normal_cutoff, btype=btype, analog=False)
    y = filtfilt(b, a, data)
    return y
```

```
[6]: def convert_angel(az, el):
    az = np.array(az) * degrees
    el = np.array(el) * degrees

    x = np.cos(2*el) * np.cos(2*az)
    y = np.cos(2*el) * np.sin(2*az)
    z = np.sin(2*el)
    return x, y, z
```

```
[7]: def calculate_freq(x, y, z):
    bins = 50
    coords = np.vstack((x, y, z)).T
    hist, edges = np.histogramdd(coords, bins=bins)

    # Indices for each coordinate pair (with clipping)
    bin_indices = [
        np.clip(np.digitize(x, edges[0]) - 1, 0, bins - 1),
        np.clip(np.digitize(y, edges[1]) - 1, 0, bins - 1),
        np.clip(np.digitize(z, edges[2]) - 1, 0, bins - 1)
    ]
    freq = hist[bin_indices[0], bin_indices[1], bin_indices[2]]
```

```

    return freq

[8]: def plot_poincare(x, y, z, freq, elev=15, azim=45, title="Not given"):
    fig = plt.figure(figsize=(6, 6))
    ax = fig.add_subplot(111, projection='3d')

    # Poincaré-Sphere
    u = np.linspace(0, 2 * np.pi, 50)
    v = np.linspace(0, np.pi, 50)
    X = np.outer(np.cos(u), np.sin(v))
    Y = np.outer(np.sin(u), np.sin(v))
    Z = np.outer(np.ones(np.size(u)), np.cos(v))

    ax.plot_surface(X, Y, Z, color='lightgray', alpha=0.1, edgecolor='k', ↴
    linewidth=0.5)

    # Axes
    ax.plot([0, 1.6], [0, 0], [0, 0], color='red')      # +S1
    ax.plot([0, -1.6], [0, 0], [0, 0], color='red')     # -S1
    ax.plot([0, 0], [0, 1.6], [0, 0], color='green')    # +S2
    ax.plot([0, 0], [0, -1.6], [0, 0], color='green')   # -S2
    ax.plot([0, 0], [0, 0], [0, 1.4], color='blue')     # +S3
    ax.plot([0, 0], [0, 0], [0, -1.4], color='blue')    # -S3

    # Labeling Axes
    ax.text( 2.0, 0, 0, 'S1', color='red', fontsize=10)
    ax.text(-1.8, 0, 0, '-S1', color='red', fontsize=10)
    ax.text( 0, 1.8, 0, 'S2', color='green', fontsize=10)
    ax.text( 0, -2.0, 0, '-S2', color='green', fontsize=10)
    ax.text( 0, 0, 1.6, 'S3', color='blue', fontsize=10)
    ax.text( 0, 0, -1.6, '-S3', color='blue', fontsize=10)

    # Measurement
    sc = ax.scatter(x, y, z, c=freq, cmap='hot', s=15)
    plt.colorbar(sc, label='density')

    # Scaling
    ax.set_box_aspect([1, 1, 1])
    ax.set_xticks([]); ax.set_yticks([]); ax.set_zticks([])

    # Aligning Poincaré-Sphere
    ax.view_init(elev=elev, azim=azim)

    ax.set_title(title)

plt.show()

```

1.4 Datenaufbereitungsschritte

```
[9]: filename = '29.11.2024_10d.csv'
skip = 8
sep = ";"
```

```
[10]: columns = ['Time[date hh:mm:ss] ', ' Elapsed Time [hh:mm:ss:ms]', ' Normalized s 1', ' Normalized s 2', ' Normalized s 3', ' S 0 [mW]', ' S 1 [mW]', ' S 2 [mW]', ' S 3 [mW]', ' Azimuth[°]', ' Ellipticity[°]', ' DOP[%]', ' DOCP[%]', ' DOLP[%]', ' Power[mW]', ' Pol Power[mW]', ' Unpol Power[mW]', ' Power[dBm]', ' Pol Power[dBm]', ' Unpol Power[dBm]', ' Power-Split-Ratio', ' Phase Difference[°]', ' Warning']
for c in range(len(columns)):
    print(c, ':', columns[c])

colors = ["tab:blue", "tab:orange", "tab:green", "tab:red", "tab:purple"]
```

```
0 : Time[date hh:mm:ss]
1 : Elapsed Time [hh:mm:ss:ms]
2 : Normalized s 1
3 : Normalized s 2
4 : Normalized s 3
5 : S 0 [mW]
6 : S 1 [mW]
7 : S 2 [mW]
8 : S 3 [mW]
9 : Azimuth[°]
10 : Ellipticity[°]
11 : DOP[%]
12 : DOCP[%]
13 : DOLP[%]
14 : Power[mW]
15 : Pol Power[mW]
16 : Unpol Power[mW]
17 : Power[dBm]
18 : Pol Power[dBm]
19 : Unpol Power[dBm]
20 : Power-Split-Ratio
21 : Phase Difference[°]
22 : Warning
```

2 Polarisationsgrad (DOP [%])

```
[11]: degree = pd.read_csv(filename, skiprows=skip, sep=sep, usecols=[columns[0], columns[11]])
```

```
[12]: degree[columns[0]] = pd.to_datetime(degree[columns[0]])
degree.set_index(columns[0], inplace=True)
```

2.1 Tägliche Aufteilung der Messdaten

```
[13]: degree_daily = degree.groupby(degree.index.date)
degree_daily_list = list(degree_daily)
```

```
[14]: for date, df_day in degree_daily_list:
    print(date, '\n')
    print(df_day.describe())
    print('')
```

2024-11-29

```
DOP [%]
count 1.676194e+06
mean 9.956919e+01
std 7.112112e+00
min -3.703300e+03
25% 9.688000e+01
50% 9.967000e+01
75% 1.024400e+02
max 2.895590e+03
```

2024-11-30

```
DOP [%]
count 1.500099e+06
mean 9.981857e+01
std 3.211169e+00
min 8.088000e+01
25% 9.752000e+01
50% 9.969000e+01
75% 1.022700e+02
max 1.242400e+02
```

2024-12-01

```
DOP [%]
count 1.429572e+06
mean 9.977245e+01
std 3.271031e+00
min 7.374000e+01
25% 9.734000e+01
50% 9.938000e+01
75% 1.022900e+02
max 1.350300e+02
```

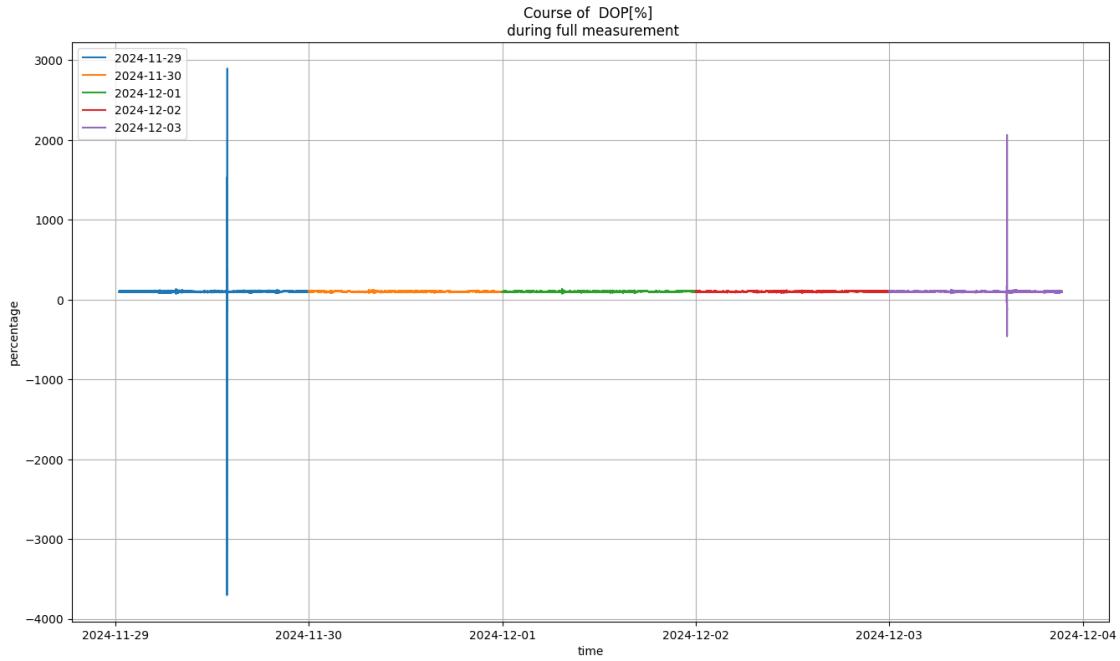
2024-12-02

```
DOP [%]
count   1.368538e+06
mean    1.001463e+02
std     3.223490e+00
min     8.404000e+01
25%    9.781000e+01
50%    9.985000e+01
75%    1.025800e+02
max     1.164700e+02
```

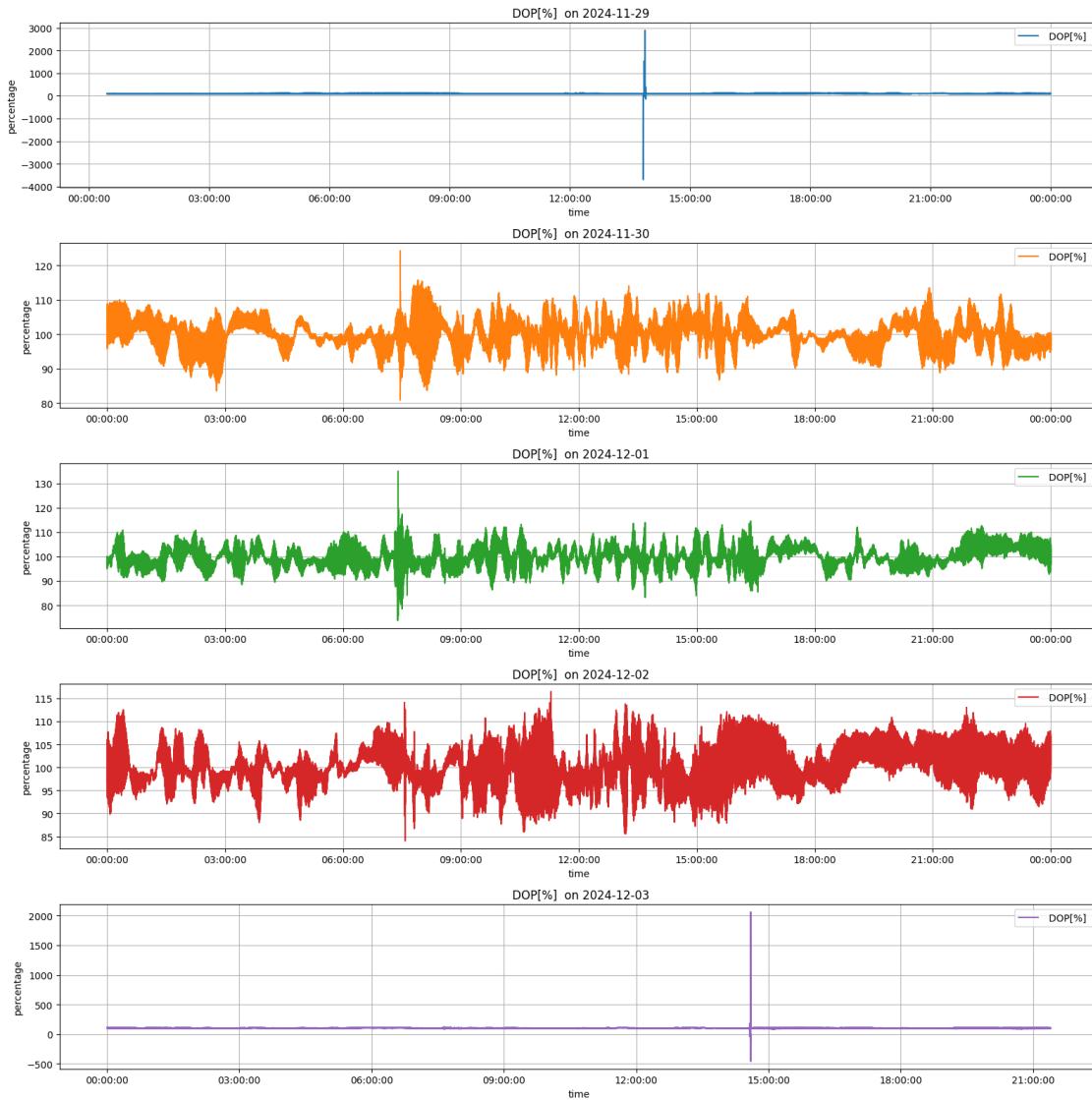
2024-12-03

```
DOP [%]
count   1.117895e+06
mean    9.903248e+01
std     4.732648e+00
min    -4.618900e+02
25%    9.733000e+01
50%    9.897000e+01
75%    1.007900e+02
max     2.062070e+03
```

```
[15]: plt.figure(figsize = (16,9))
for date, df_day in degree_daily_list:
    values = df_day
    plt.plot(values, label=str(date))
plt.grid()
plt.legend(loc = 'best')
plt.title(f'Course of {columns[11]}\n during full measurement')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



```
[16]: fig, axs = plt.subplots(len(degree_daily_list), 1, figsize=(16, 16),  
                           sharex=False)  
  
for i in range(len(degree_daily_list)):  
    ax = axs[i] if len(degree_daily_list) > 1 else axs  
    df_day = degree_daily_list[i][1]  
  
    ax.plot(df_day.index, df_day, label=columns[11], color=colors[i])  
    ax.grid()  
    ax.legend(loc='best')  
    ax.set_title(f'{columns[11]} on {degree_daily_list[i][0]}')  
    ax.set_xlabel('time')  
    ax.set_ylabel('percentage')  
  
    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S'))  
  
plt.tight_layout()  
plt.show()
```



```
[17]: fig, ax = plt.subplots(figsize = (16,9))

for date, df_day in degree_daily_list:
    times = (df_day.index - df_day.index.normalize()).total_seconds()
    values = df_day
    plt.plot(times, values, label=str(date))

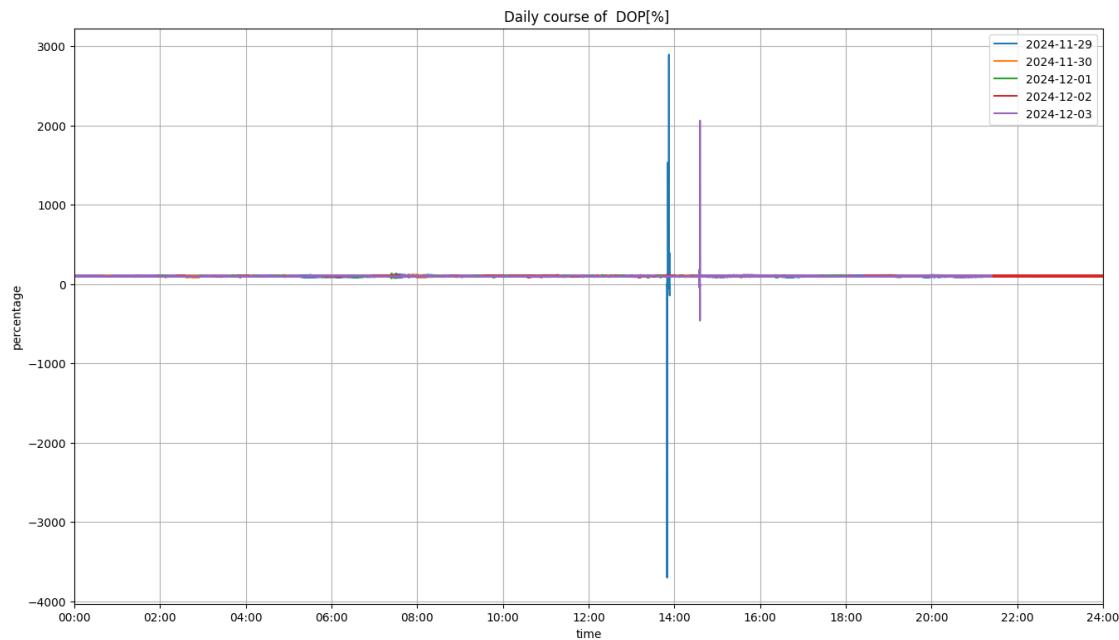
ax.xaxis.set_major_locator(ticker.MultipleLocator(3600 * 2))
ax.xaxis.set_major_formatter(ticker.FuncFormatter(format_time))
ax.set_xlim(0, 24 * 3600)

plt.grid()
```

```

plt.legend(loc = 'best')
plt.title(f'Daily course of {columns[11]}')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()

```



2.2 Stundenweise Aufteilung (Beispiel: erster Tag)

[18]: # exemplary day
day = 0 #first day

[19]: degree_one_day = degree_daily_list[day][1]
hourly = degree_one_day.groupby(degree_one_day.index.hour)
degree_hourly = list(hourly)

[20]: for hour, df_hour in degree_hourly:
 print(f'{hour}:00\n')
 print(df_hour.describe())
 print('')

0:00

	DOP [%]
count	41275.000000
mean	98.782586
std	2.762127

```
min      92.610000
25%     96.120000
50%     99.190000
75%    101.250000
max    106.270000
```

1:00

```
DOP [%]
count 74616.000000
mean   98.671192
std     2.760749
min    92.290000
25%    96.050000
50%    98.895000
75%    101.180000
max    106.340000
```

2:00

```
DOP [%]
count 74706.000000
mean   99.697654
std     2.657860
min    93.690000
25%    97.170000
50%    99.890000
75%    102.180000
max    106.550000
```

3:00

```
DOP [%]
count 74791.000000
mean   100.668886
std     2.529215
min    94.970000
25%    98.290000
50%    100.970000
75%    102.970000
max    107.430000
```

4:00

```
DOP [%]
count 74793.000000
mean   101.770583
std     2.758068
```

```
min      89.800000
25%     99.520000
50%    101.790000
75%    103.920000
max    113.100000
```

5:00

```
DOP [%]
count 74747.000000
mean   98.515741
std     3.715355
min    82.720000
25%    95.980000
50%    98.600000
75%    101.040000
max    117.820000
```

6:00

```
DOP [%]
count 74828.000000
mean   98.409908
std     4.205050
min    84.190000
25%    95.090000
50%    98.430000
75%    101.590000
max    112.910000
```

7:00

```
DOP [%]
count 74694.000000
mean   100.838734
std     3.681271
min    73.140000
25%    98.550000
50%    100.890000
75%    103.250000
max    131.350000
```

8:00

```
DOP [%]
count 74628.000000
mean   101.480403
std     3.417497
```

```
min      87.190000
25%     99.240000
50%    101.590000
75%    103.882500
max    115.510000
```

9:00

```
DOP [%]
count 74538.000000
mean   98.771017
std     3.083574
min    88.420000
25%    96.300000
50%    98.600000
75%    101.070000
max    110.460000
```

10:00

```
DOP [%]
count 74219.000000
mean   96.175932
std     1.902132
min    88.210000
25%    94.670000
50%    95.980000
75%    97.630000
max    105.260000
```

11:00

```
DOP [%]
count 74138.000000
mean   97.215173
std     2.521470
min    86.640000
25%    95.080000
50%    97.190000
75%    99.170000
max    112.180000
```

12:00

```
DOP [%]
count 72813.000000
mean   99.000588
std     3.209165
```

```
min      88.910000
25%     96.530000
50%     98.770000
75%    101.270000
max    117.370000
```

13:00

```
DOP [%]
count 73844.000000
mean   93.298756
std    28.597326
min   -3703.300000
25%    94.810000
50%    96.520000
75%    98.550000
max    2895.590000
```

14:00

```
DOP [%]
count 70606.000000
mean   96.375985
std    2.143110
min    88.650000
25%    94.870000
50%    96.080000
75%    97.690000
max    105.030000
```

15:00

```
DOP [%]
count 73448.000000
mean   100.860022
std    3.351608
min    89.790000
25%    98.330000
50%    101.020000
75%    103.250000
max    115.080000
```

16:00

```
DOP [%]
count 70765.000000
mean   100.038458
std    3.674802
```

```
min      84.490000
25%     97.970000
50%    100.380000
75%    102.480000
max    113.170000
```

17:00

```
DOP [%]
count  62936.000000
mean   102.334199
std    3.289435
min    89.740000
25%   100.020000
50%   102.380000
75%   104.670000
max   113.440000
```

18:00

```
DOP [%]
count  67232.000000
mean   104.355162
std    2.338354
min    95.440000
25%   102.650000
50%   104.210000
75%   106.010000
max   112.740000
```

19:00

```
DOP [%]
count  70870.000000
mean   101.068998
std    3.861459
min    84.220000
25%   98.390000
50%   101.080000
75%   103.790000
max   113.610000
```

20:00

```
DOP [%]
count  63528.000000
mean   99.768936
std    2.936399
```

```
min      85.690000
25%     98.100000
50%     99.510000
75%    101.820000
max    115.660000
```

21:00

```
DOP [%]
count  62861.000000
mean    101.711952
std     3.132026
min     90.220000
25%    99.770000
50%    102.450000
75%    103.930000
max    108.160000
```

22:00

```
DOP [%]
count  62481.000000
mean    99.940909
std     3.276664
min     90.690000
25%    97.320000
50%    99.830000
75%    102.300000
max    111.310000
```

23:00

```
DOP [%]
count  62837.000000
mean    100.938768
std     3.197490
min     90.440000
25%    98.670000
50%    100.990000
75%    103.430000
max    113.040000
```

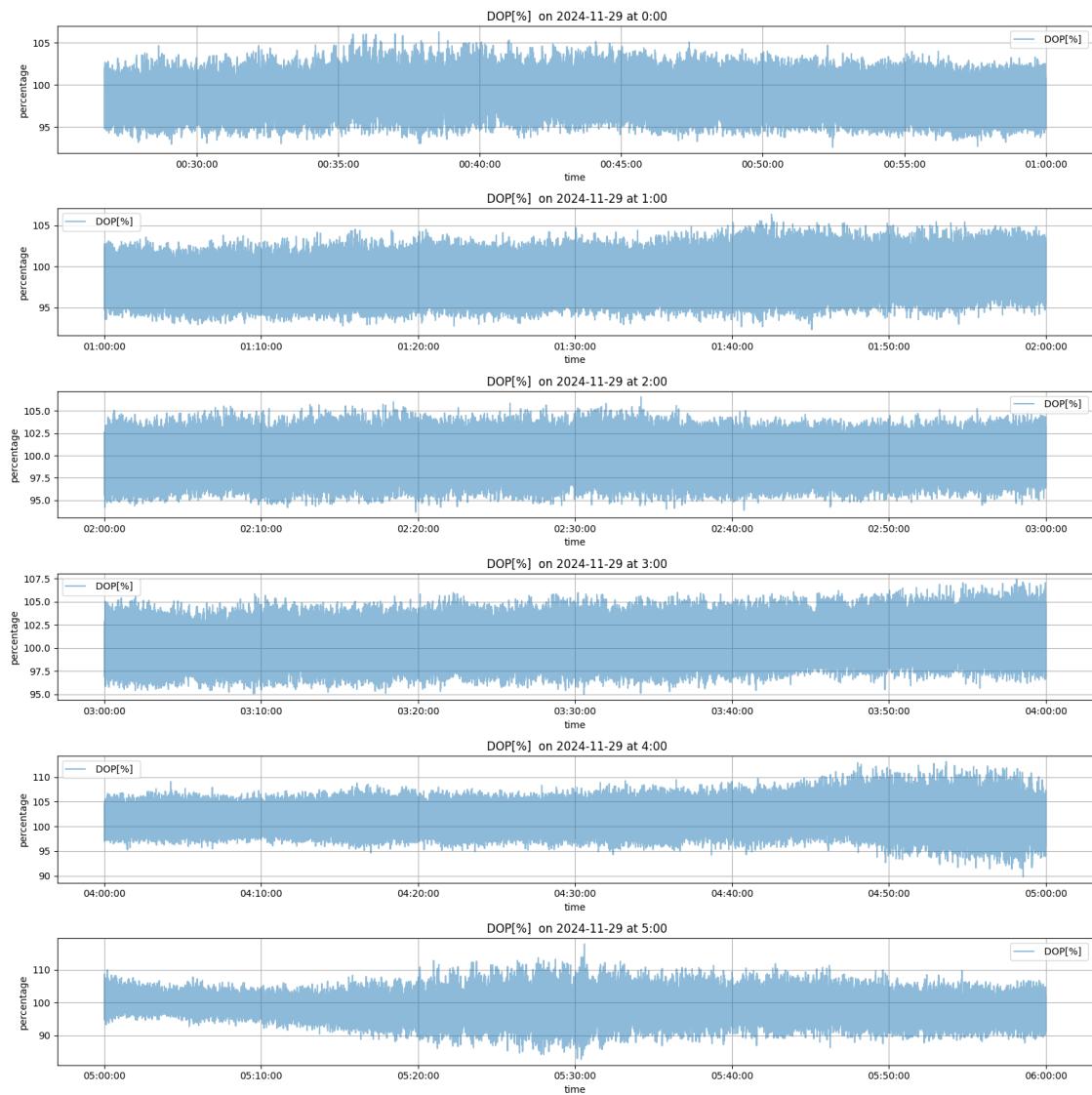
```
[21]: daily_quaters = [degree_hourly[:6], degree_hourly[6:12], degree_hourly[12:18],  
                     degree_hourly[18:]]  
for quater in daily_quaters:  
    fig, axs = plt.subplots(len(quater), 1, figsize=(16, 16), sharex=False)
```

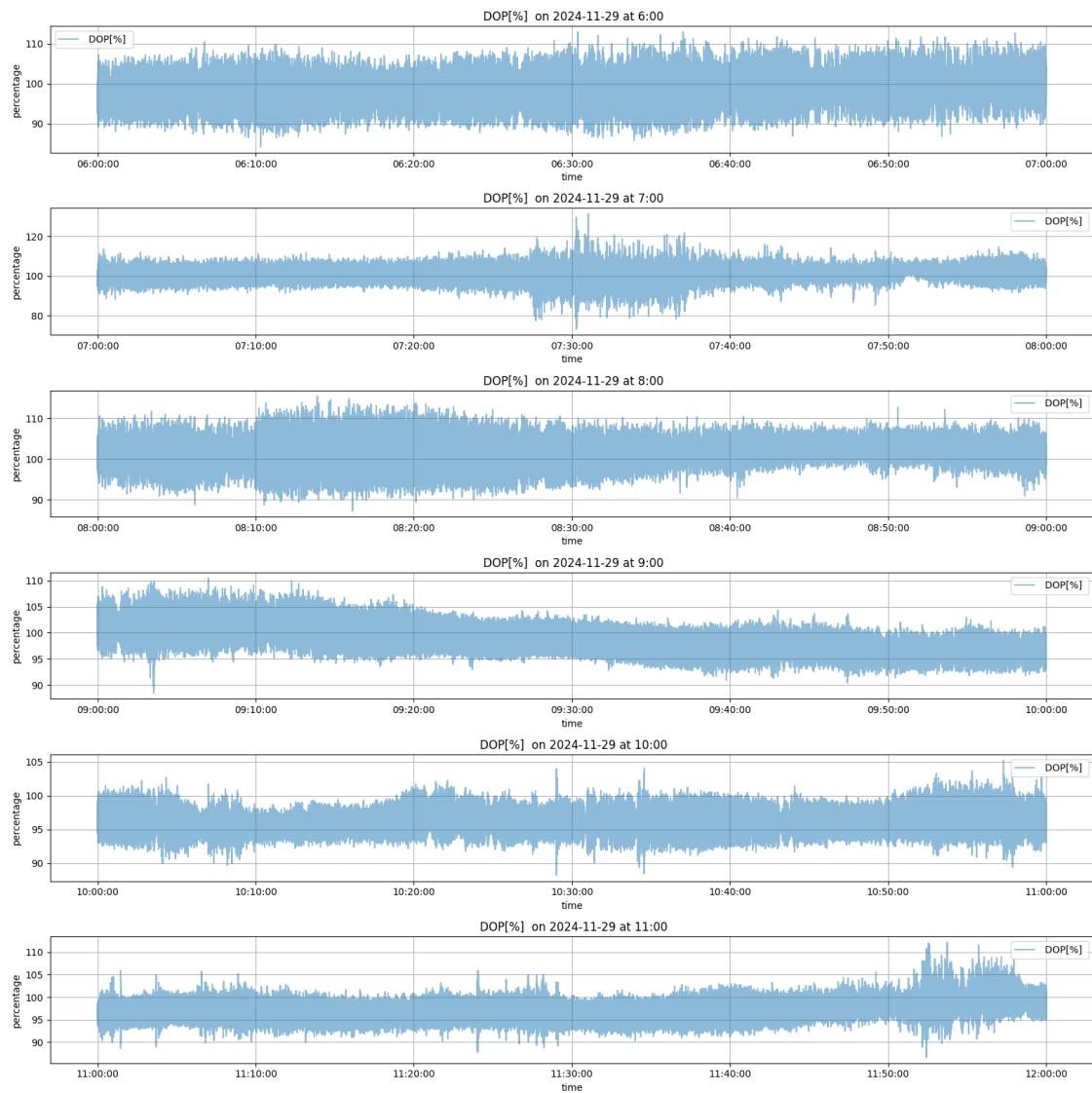
```
for i in range(len(quater)):
    ax = axs[i] if len(quater) > 1 else axs
    df_day = quater[i][1]

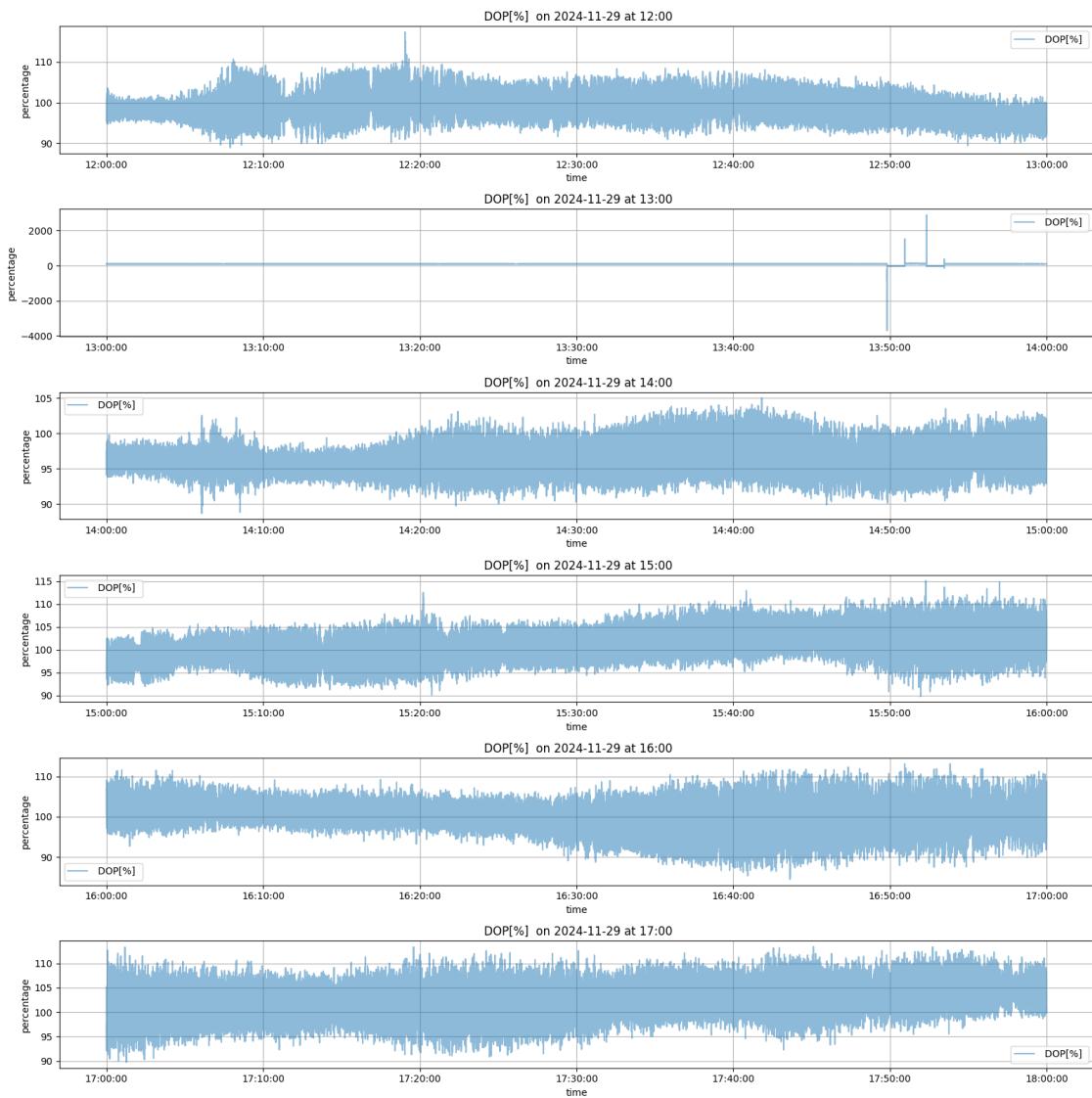
    ax.plot(df_day.index, df_day, label=columns[11], color=colors[day], alpha=0.5)
    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'{columns[11]} on {degree_daily_list[day][0]} at {quater[i][0]}:00')
    ax.set_xlabel('time')
    ax.set_ylabel('percentage')

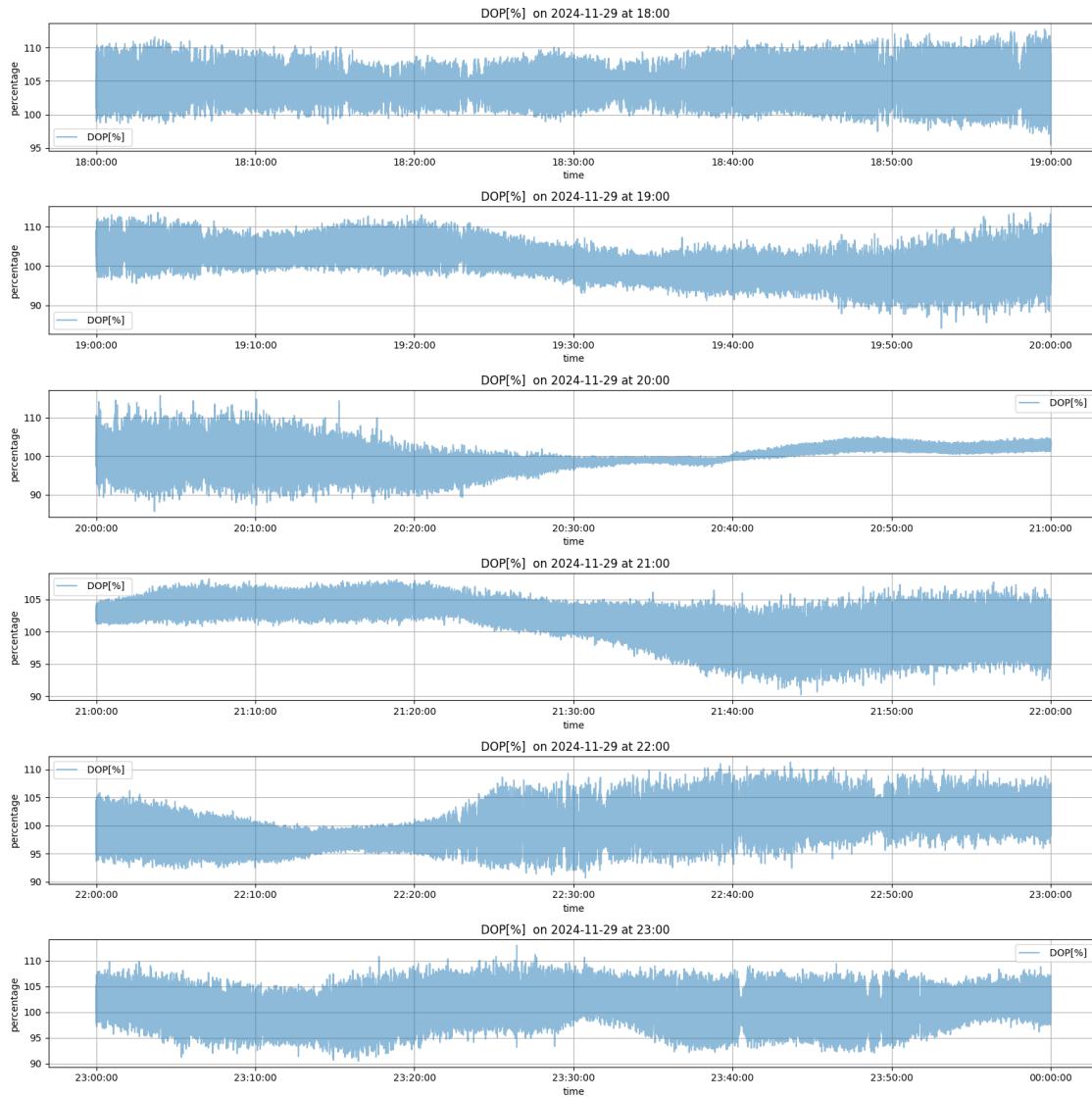
    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S'))

plt.tight_layout()
plt.show()
```









2.3 Ausreißerbereinigung

```
[22]: new_degree = degree.columns[11]
new_degree = new_degree.drop(new_degree[(new_degree > 140) | (new_degree < 0)].index)
new_degree.describe()
```

```
[22]: count    7.088521e+06
mean      9.974852e+01
std       3.296249e+00
min       7.314000e+01
25%      9.738000e+01
```

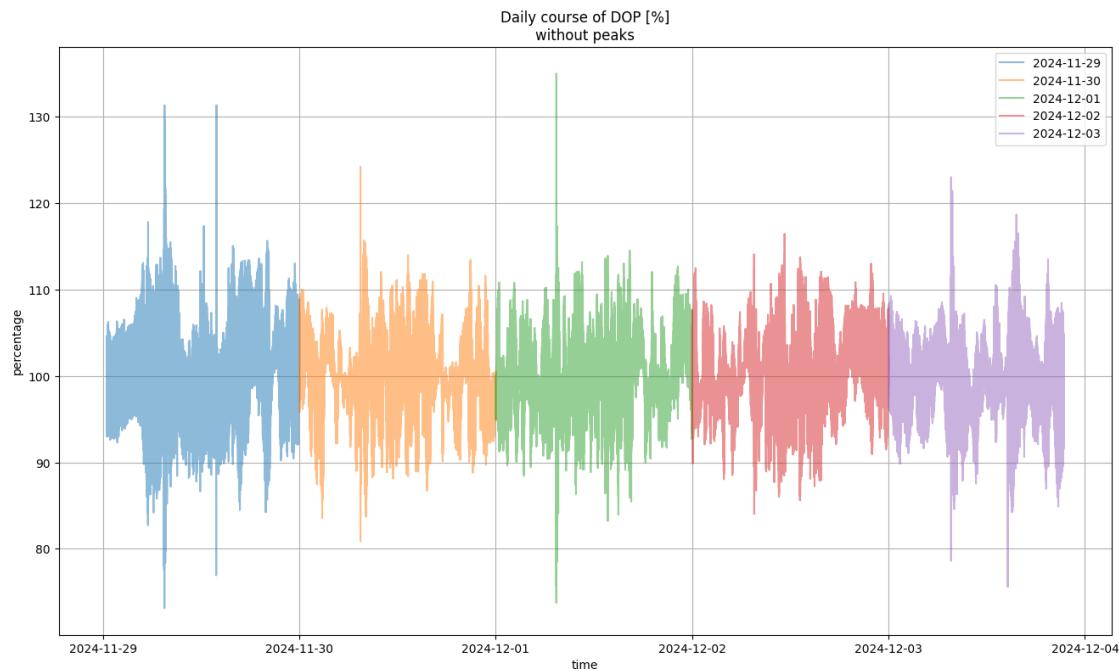
```

50%      9.950000e+01
75%      1.021600e+02
max      1.350300e+02
Name: DOP[%] , dtype: float64

```

```
[23]: new_degree_daily = new_degree.groupby(new_degree.index.date)
new_degree_daily_list = list(new_degree_daily)
```

```
[24]: plt.figure(figsize = (16,9))
for date, df_day in new_degree_daily_list:
    values = df_day
    plt.plot(values, label=str(date), alpha = 0.5)
plt.grid()
plt.legend(loc = 'best')
plt.title('Daily course of DOP [%]\nwithout peaks')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



```
[25]: fig, ax = plt.subplots(figsize = (16,9))

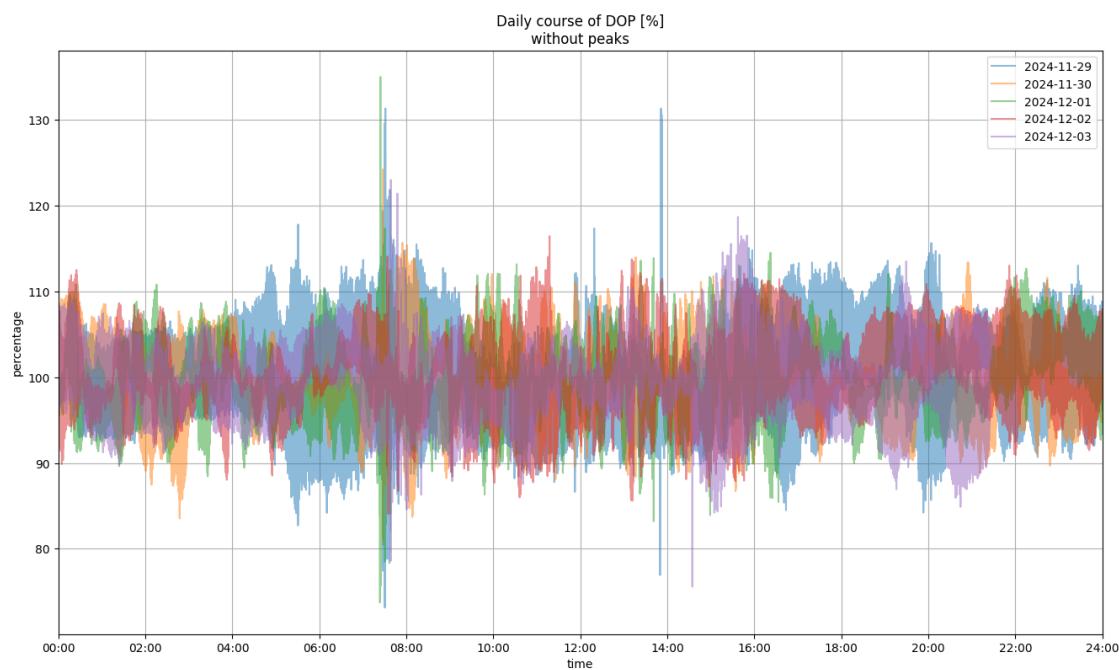
for date, df_day in new_degree_daily_list:
    times = (df_day.index - df_day.index.normalize()).total_seconds()
    values = df_day
    plt.plot(times, values, label=str(date) , alpha=0.5)
```

```

ax.xaxis.set_major_locator(ticker.MultipleLocator(3600 * 2))
ax.xaxis.set_major_formatter(ticker.FuncFormatter(format_time))
ax.set_xlim(0, 24 * 3600)

plt.grid()
plt.legend(loc = 'best')
plt.title('Daily course of DOP [%]\nwithout peaks')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()

```



2.4 Tägliche Normalverteilung mit Histogramm

```

[26]: ydata1 = np.array(new_degree_daily_list[day][1])
mu1 = np.mean(ydata1)
sigma1 = np.std(ydata1)
x1 = np.linspace(ydata1.min(),ydata1.max(),len(ydata1))
y1 = norm.pdf(x1, mu1, sigma1)

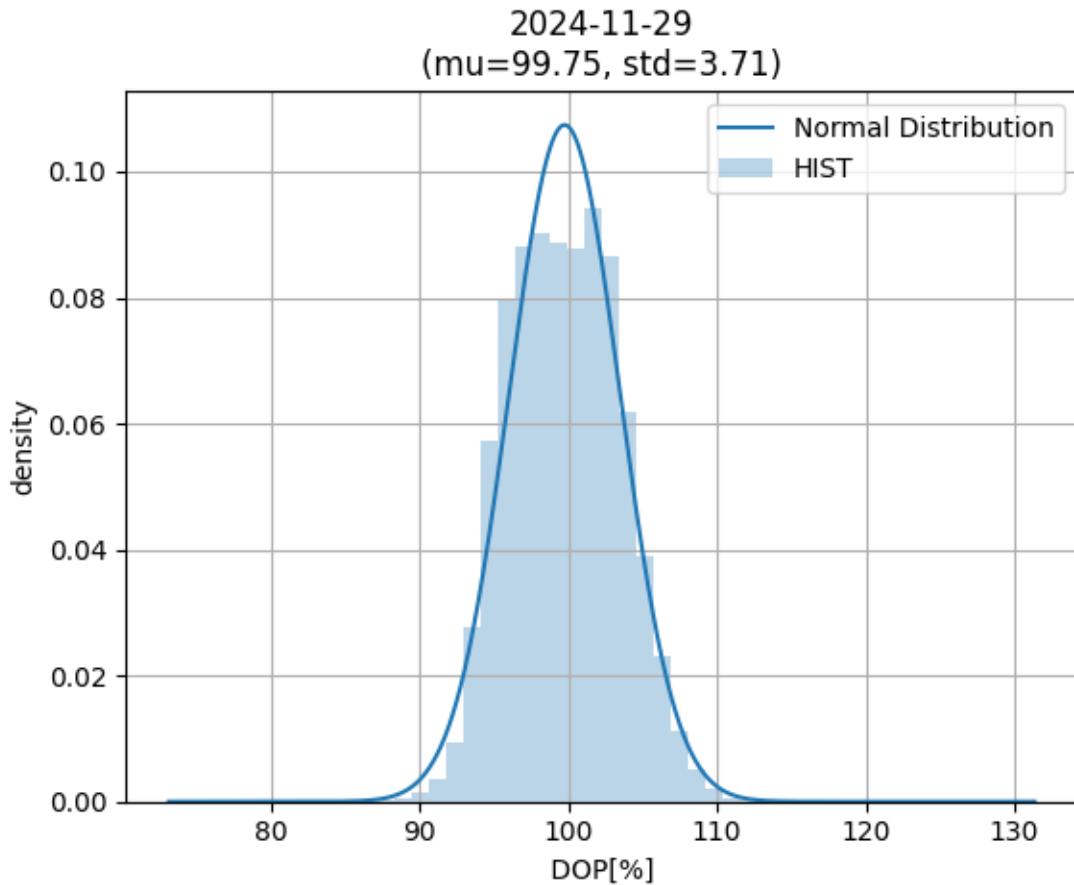
plt.plot(x1, y1, label = 'Normal Distribution', color=colors[day])
plt.hist(ydata1, bins = 50, density = True, color=colors[day], alpha = 0.3, label = "HIST")

```

```

plt.title(f'{new_degree_daily_list[day][0]}\n(mu={mu1:.2f}, std={sigma1:.2f})')
plt.legend(loc = 'best')
plt.xlabel(columns[11])
plt.ylabel('density')
plt.grid()
plt.show()

```



```

[27]: fig, axs = plt.subplots(len(new_degree_daily_list), 1, figsize=(8, 16),
                           sharex=False)

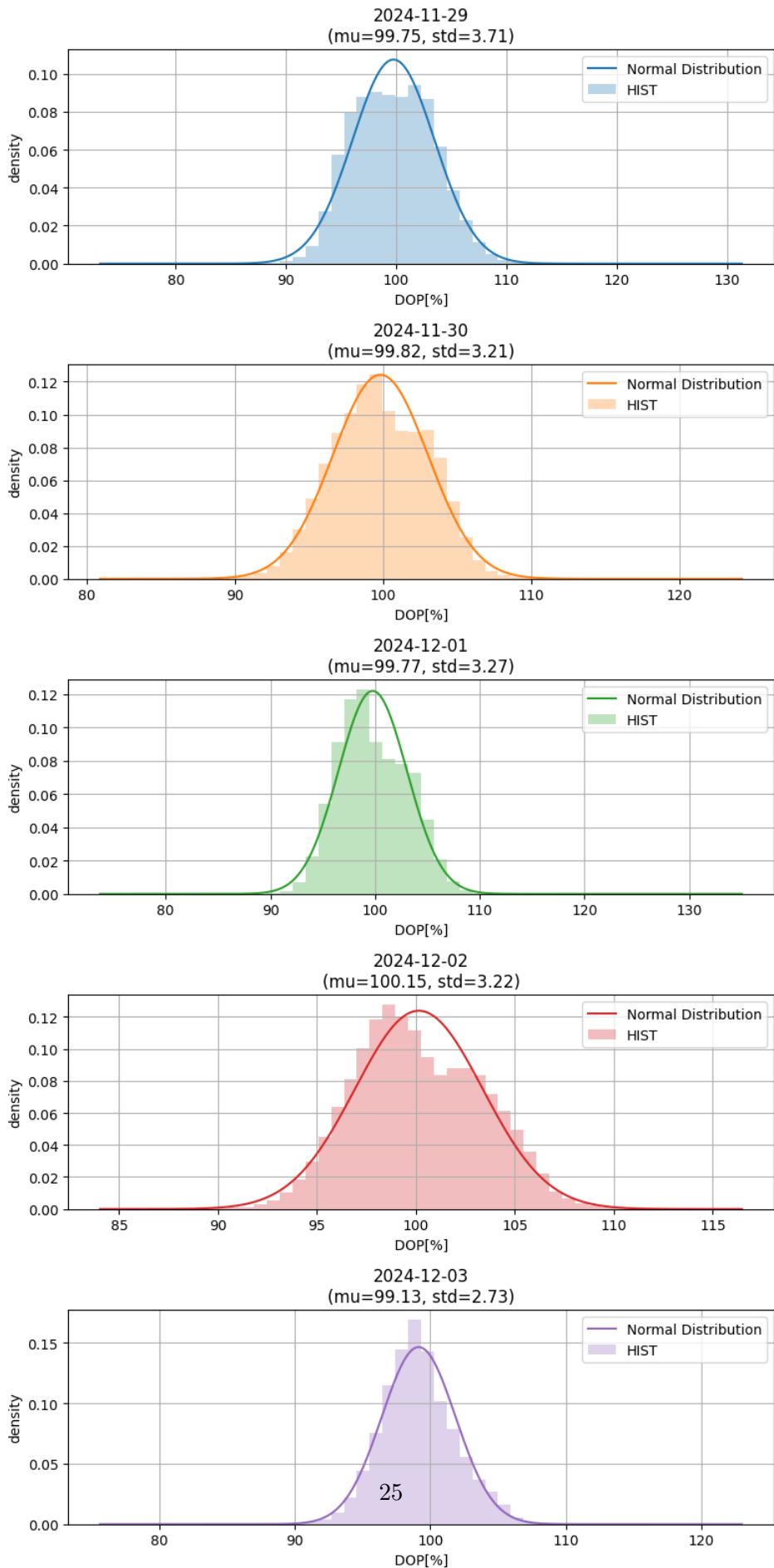
for i in range(len(new_degree_daily_list)):
    ax = axs[i] if len(new_degree_daily_list) > 1 else axs
    ydata1 = np.array(new_degree_daily_list[i][1])
    mu1 = np.mean(ydata1)
    sigma1 = np.std(ydata1)
    x1 = np.linspace(ydata1.min(), ydata1.max(), len(ydata1))
    y1 = norm.pdf(x1, mu1, sigma1)

```

```
    ax.plot(x1, y1, label = 'Normal Distribution', color=colors[i])
    ax.hist(ydata1, bins = 50, density = True, color=colors[i], alpha = 0.3, label = "HIST")

    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'{degree_daily_list[i][0]}\n(mu={mu1:.2f}, std={sigma1:.2f})')
    ax.set_xlabel(columns[11])
    ax.set_ylabel('density')

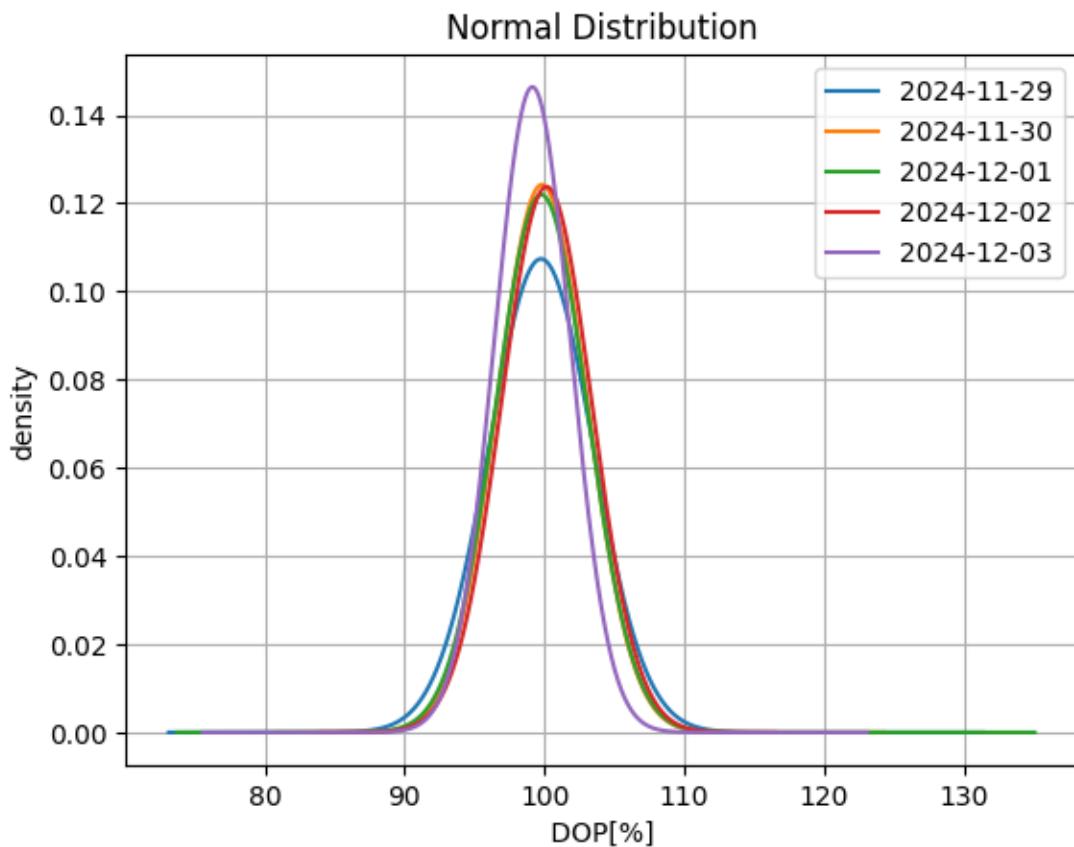
plt.tight_layout()
plt.show()
```



```
[28]: for i in range(len(new_degree_daily_list)):
    ydata1 = np.array(new_degree_daily_list[i][1])
    mu1 = np.mean(ydata1)
    sigma1 = np.std(ydata1)
    x1 = np.linspace(ydata1.min(),ydata1.max(),len(ydata1))
    y1 = norm.pdf(x1, mu1, sigma1)

    plt.plot(x1, y1, label = new_degree_daily_list[i][0])

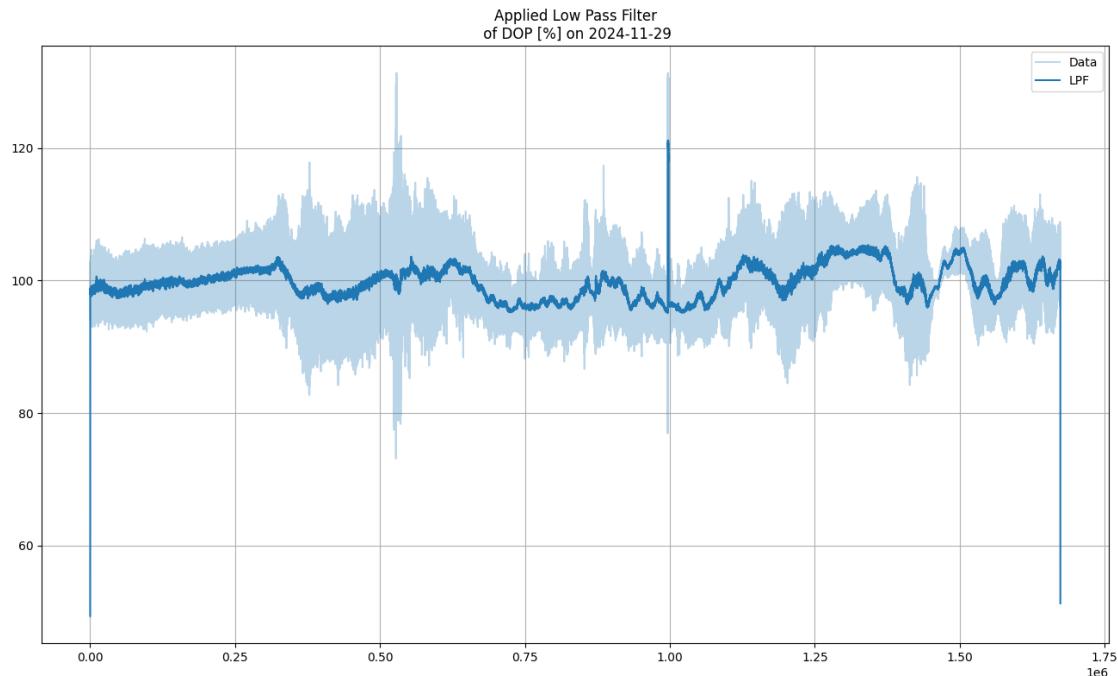
plt.title(f'Normal Distribution')
plt.legend(loc = 'best')
plt.xlabel(columns[11])
plt.ylabel('density')
plt.grid()
plt.show()
```



2.5 Filterung mittels Tief- und Hochpass

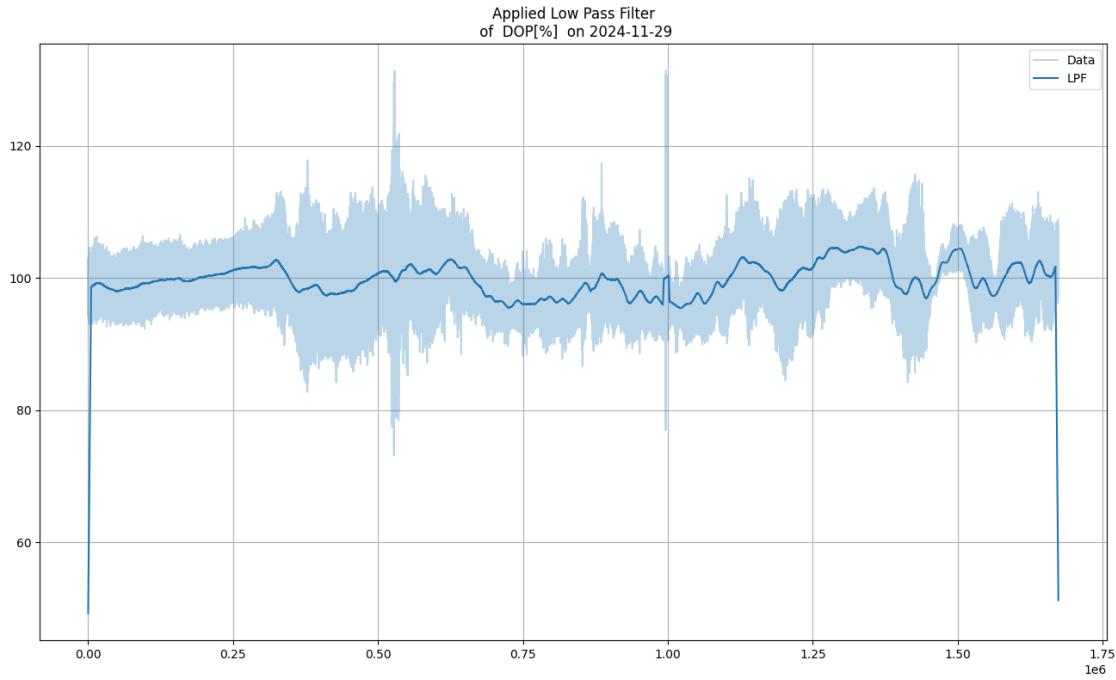
```
[29]: ydata = np.array(new_degree_daily_list[day][1])

lps = lowpass(ydata, 100)
plt.figure(figsize = (16,9))
plt.plot(ydata, label = 'Data', color = colors[day], alpha=0.3)
plt.plot(lps, label = 'LPF', color = colors[day])
plt.title(f'Applied Low Pass Filter\nof DOP [%] on\n{new_degree_daily_list[day][0]}')
plt.grid()
plt.legend(loc = 'best')
plt.show()
```



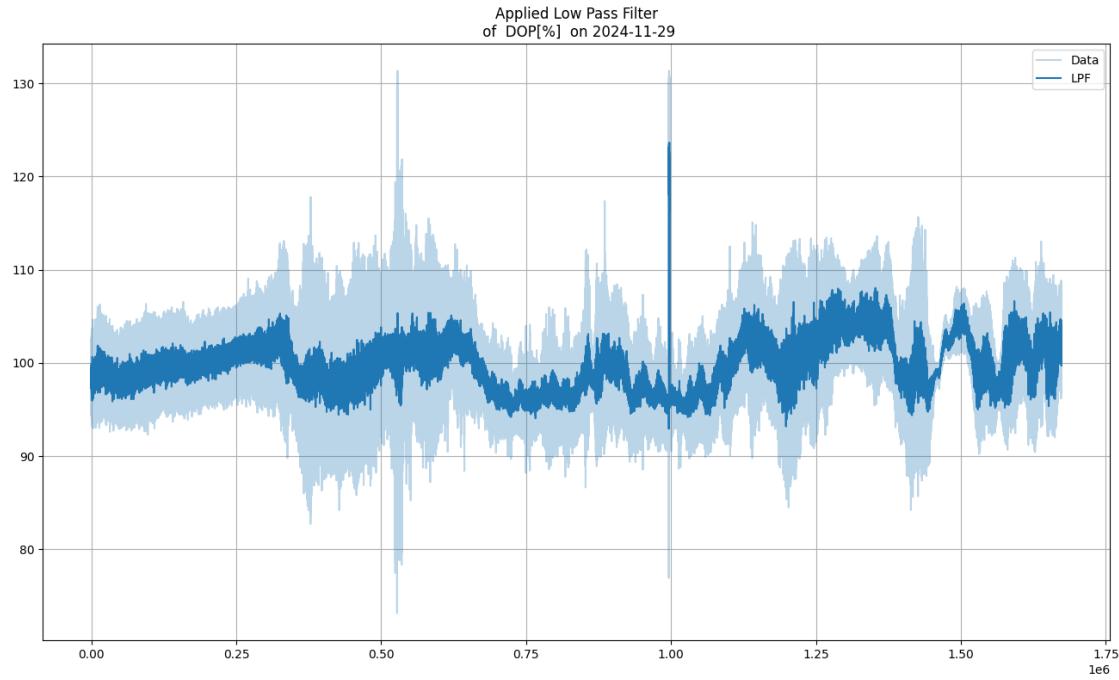
```
[30]: ydata = np.array(new_degree_daily_list[day][1])

lps = lowpass(ydata, 10000)
plt.figure(figsize = (16,9))
plt.plot(ydata, label = 'Data', color = colors[day], alpha=0.3)
plt.plot(lps, label = 'LPF', color = colors[day])
plt.title(f'Applied Low Pass Filter\nof {columns[11]} on\n{new_degree_daily_list[day][0]}')
plt.grid()
plt.legend(loc = 'best')
plt.show()
```



```
[32]: cutoff = 1.0
btype='low'

ydata = np.array(new_degree_daily_list[day][1])
lps = butter_filter(ydata, cutoff = cutoff, btype=btype)
plt.figure(figsize = (16,9))
plt.plot(ydata, label = 'Data', color = colors[day], alpha=0.3)
plt.plot(lps, label = 'LPF', color = colors[day])
plt.title(f'Applied Low Pass Filter\n of {columns[11]} on\n {new_degree_daily_list[day][0]}')
plt.grid()
plt.legend(loc = 'best')
plt.show()
```

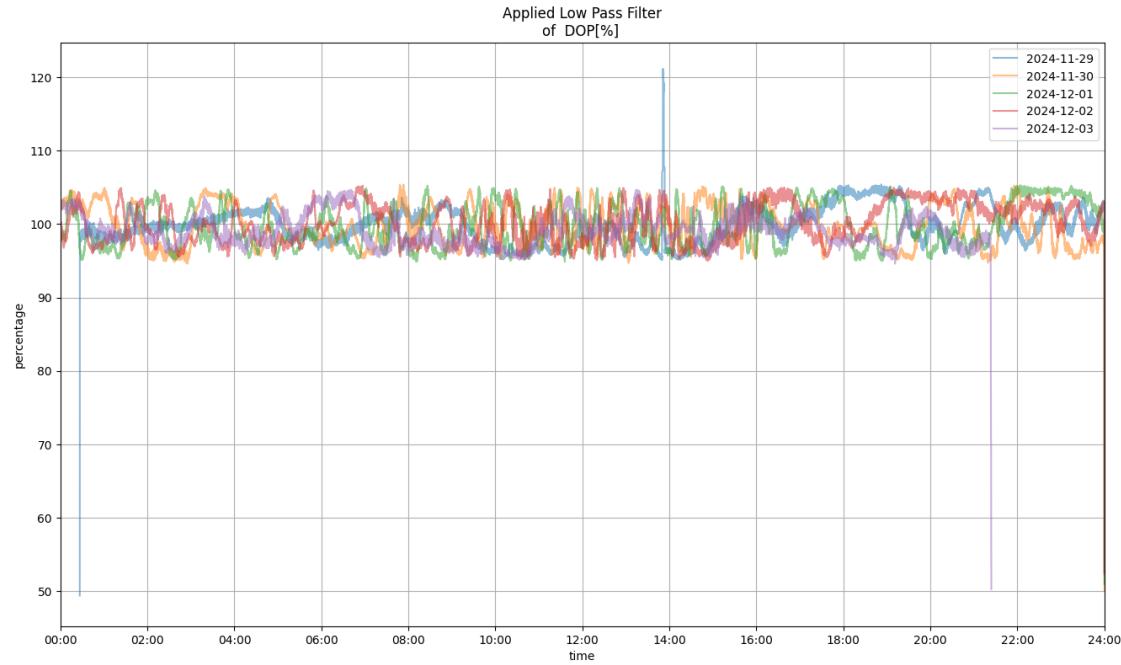


```
[33]: fig, ax = plt.subplots(figsize = (16,9))

for date, df_day in new_degree_daily_list:
    times = (df_day.index - df_day.index.normalize()).total_seconds()
    ydata = np.array(df_day)
    lps = lowpass(ydata, 100)
    plt.plot(times, lps[:-1], label=str(date) , alpha=0.5)

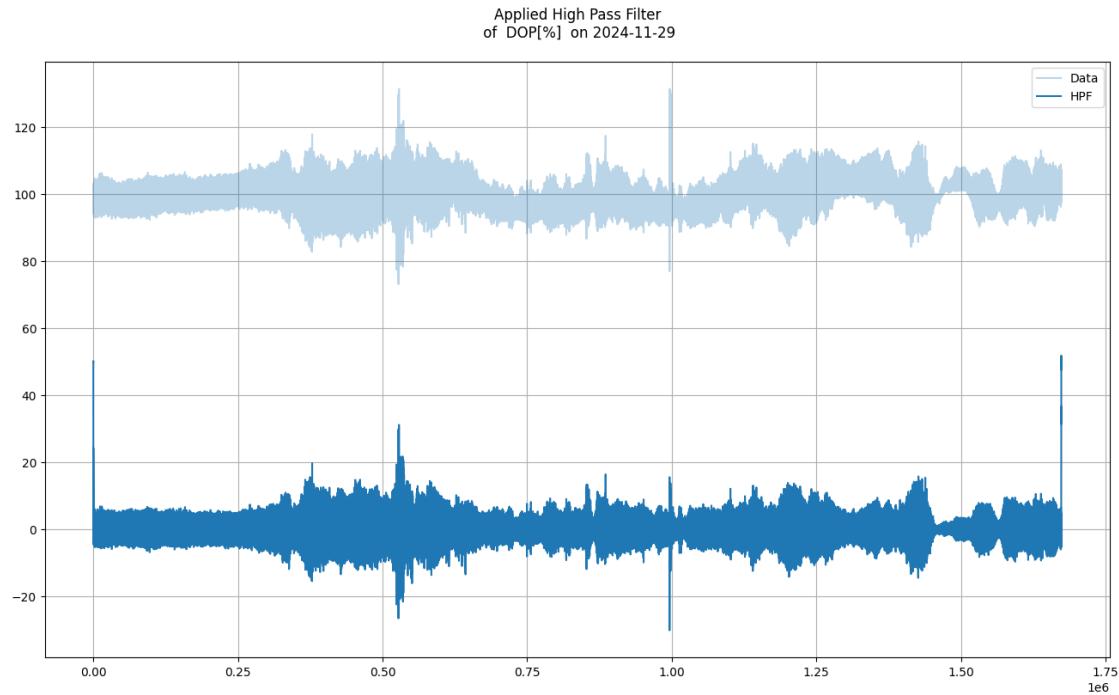
ax.xaxis.set_major_locator(ticker.MultipleLocator(3600 * 2))
ax.xaxis.set_major_formatter(ticker.FuncFormatter(format_time))
ax.set_xlim(0, 24 * 3600)

plt.grid()
plt.legend(loc = 'best')
plt.title(f'Applied Low Pass Filter\nof {columns[11]}')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



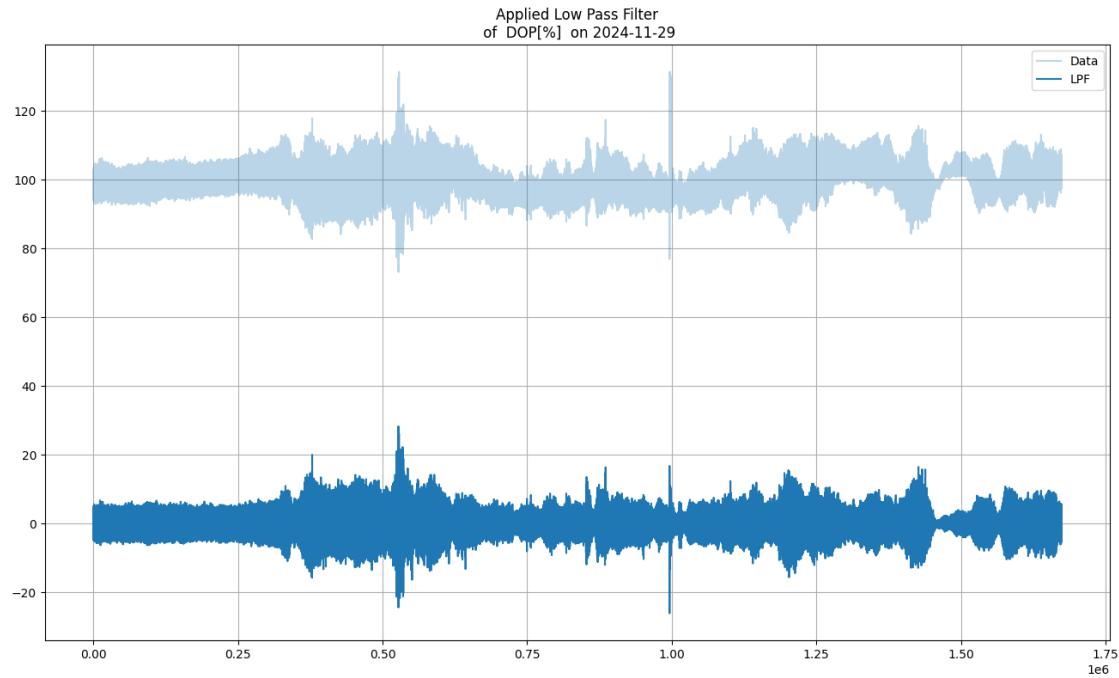
```
[34]: ydata = np.array(new_degree_daily_list[day][1])

hps = highpass(ydata, 100)
plt.figure(figsize = (16,9))
plt.plot(ydata, label = 'Data', color=colors[day], alpha=0.3)
plt.plot(hps, label = 'HPF', color=colors[day])
plt.title(f'Applied High Pass Filter\n of {columns[11]} on\n{new_degree_daily_list[day][0]}\n')
plt.grid()
plt.legend(loc = 'best')
plt.show()
```



```
[36]: cutoff = 1.0
btype='high'

ydata = np.array(new_degree_daily_list[day][1])
lps = butter_filter(ydata, cutoff = cutoff, btype=btype)
plt.figure(figsize = (16,9))
plt.plot(ydata, label = 'Data', color = colors[day], alpha=0.3)
plt.plot(lps, label = 'LPF', color = colors[day])
plt.title(f'Applied Low Pass Filter\n of {columns[11]} on\n ↵{new_degree_daily_list[day][0]}')
plt.grid()
plt.legend(loc = 'best')
plt.show()
```

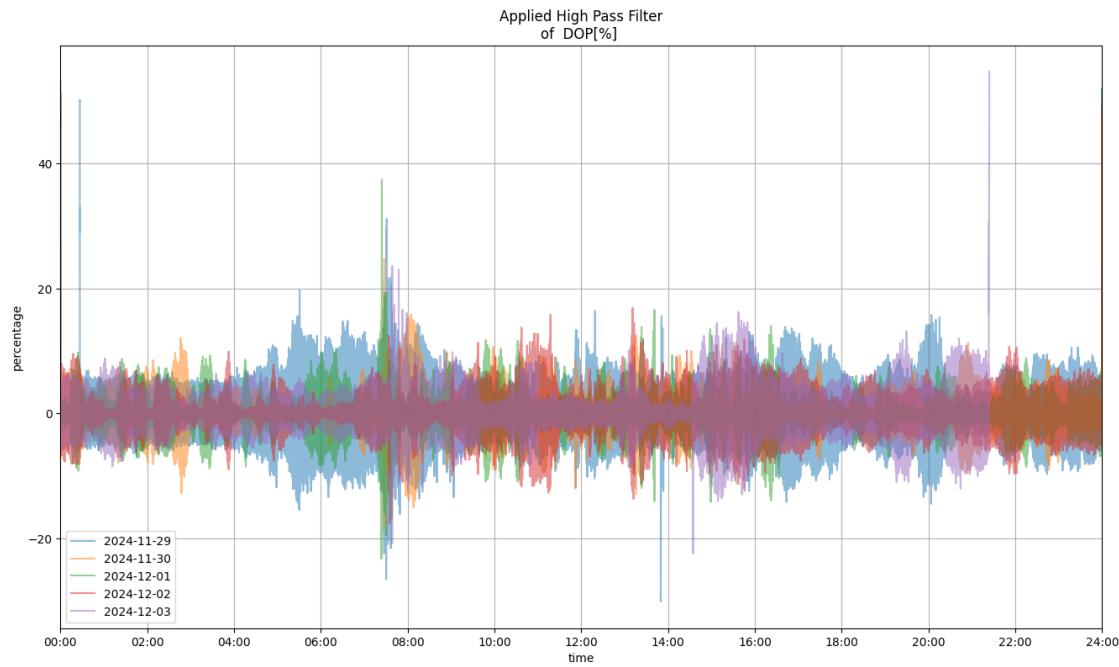


```
[35]: fig, ax = plt.subplots(figsize = (16,9))

for date, df_day in new_degree_daily_list:
    times = (df_day.index - df_day.index.normalize()).total_seconds()
    ydata = np.array(df_day)
    hps = highpass(ydata, 100)
    plt.plot(times, hps, label=str(date) , alpha=0.5)

ax.xaxis.set_major_locator(ticker.MultipleLocator(3600 * 2))
ax.xaxis.set_major_formatter(ticker.FuncFormatter(format_time))
ax.set_xlim(0, 24 * 3600)

plt.grid()
plt.legend(loc = 'best')
plt.title(f'Applied High Pass Filter\nof {columns[11]}')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



3 Winkelparameter (Azimut [°], Elliptizität [°])

```
[37]: angle = pd.read_csv(filename, skiprows=skip, sep=sep, usecols=[columns[0], columns[9], columns[10]])
```

```
[38]: angle[columns[0]] = pd.to_datetime(angle[columns[0]])
angle.set_index(columns[0], inplace=True)
```

3.1 Tägliche Aufteilung der Messdaten

```
[39]: angle_daily = angle.groupby(angle.index.date)
angle_daily_list = list(angle_daily)
```

```
[40]: for date, df_day in angle_daily_list:
    print(date, '\n')
    print(df_day.describe())
    print('')
```

2024-11-29

	Azimuth[°]	Ellipticity[°]
count	1.676194e+06	1.676194e+06
mean	5.728160e+00	-1.144504e+00
std	2.365813e+01	1.490541e+01
min	-9.000000e+01	-4.468000e+01

25%	-5.880000e+00	-1.364000e+01
50%	6.930000e+00	1.240000e+00
75%	2.023000e+01	1.106000e+01
max	9.000000e+01	4.454000e+01

2024-11-30

	Azimuth[°]	Ellipticity[°]
count	1.500099e+06	1.500099e+06
mean	2.428019e+00	1.063311e+00
std	5.500757e+01	1.903680e+01
min	-9.000000e+01	-4.497000e+01
25%	-4.778000e+01	-1.415000e+01
50%	8.700000e-01	1.020000e+00
75%	5.337000e+01	1.478000e+01
max	9.000000e+01	4.498000e+01

2024-12-01

	Azimuth[°]	Ellipticity[°]
count	1.429572e+06	1.429572e+06
mean	7.651423e+00	-2.963670e+00
std	5.176796e+01	1.858525e+01
min	-9.000000e+01	-4.496000e+01
25%	-3.570000e+01	-1.659000e+01
50%	9.750000e+00	-3.400000e+00
75%	5.514000e+01	9.940000e+00
max	9.000000e+01	4.496000e+01

2024-12-02

	Azimuth[°]	Ellipticity[°]
count	1.368538e+06	1.368538e+06
mean	2.967946e+00	-4.818185e+00
std	4.593922e+01	1.803721e+01
min	-9.000000e+01	-4.496000e+01
25%	-2.711000e+01	-1.765000e+01
50%	-7.500000e-01	-6.490000e+00
75%	3.369000e+01	7.630000e+00
max	9.000000e+01	4.497000e+01

2024-12-03

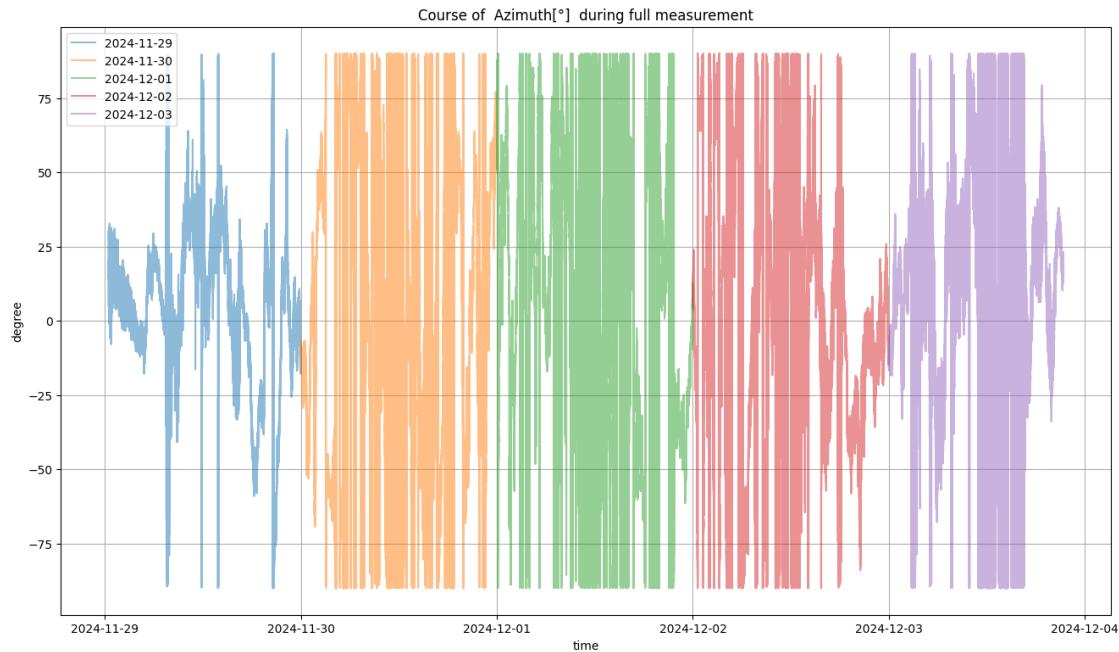
	Azimuth[°]	Ellipticity[°]
count	1.117895e+06	1.117895e+06
mean	8.673327e+00	-1.437671e+01
std	4.252360e+01	1.777982e+01
min	-9.000000e+01	-4.498000e+01

```

25% -1.337000e+01 -2.748000e+01
50% 1.513000e+01 -1.789000e+01
75% 3.113000e+01 -4.460000e+00
max 9.000000e+01 4.408000e+01

```

```
[41]: plt.figure(figsize = (16,9))
for date, df_day in angle_daily_list:
    values = df_day[columnns[9]]
    plt.plot(values, label=str(date), alpha=0.5)
plt.grid()
plt.legend(loc = 'best')
plt.title(f'Course of {columnns[9]} during full measurement')
plt.xlabel('time')
plt.ylabel('degree')
plt.show()
```



```
[42]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(16, 16), sharex=False)

for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    df_day = angle_daily_list[i][1][columnns[9]]

    ax.plot(df_day.index, df_day, label=columnns[9], color=colors[i])
    ax.grid()
```

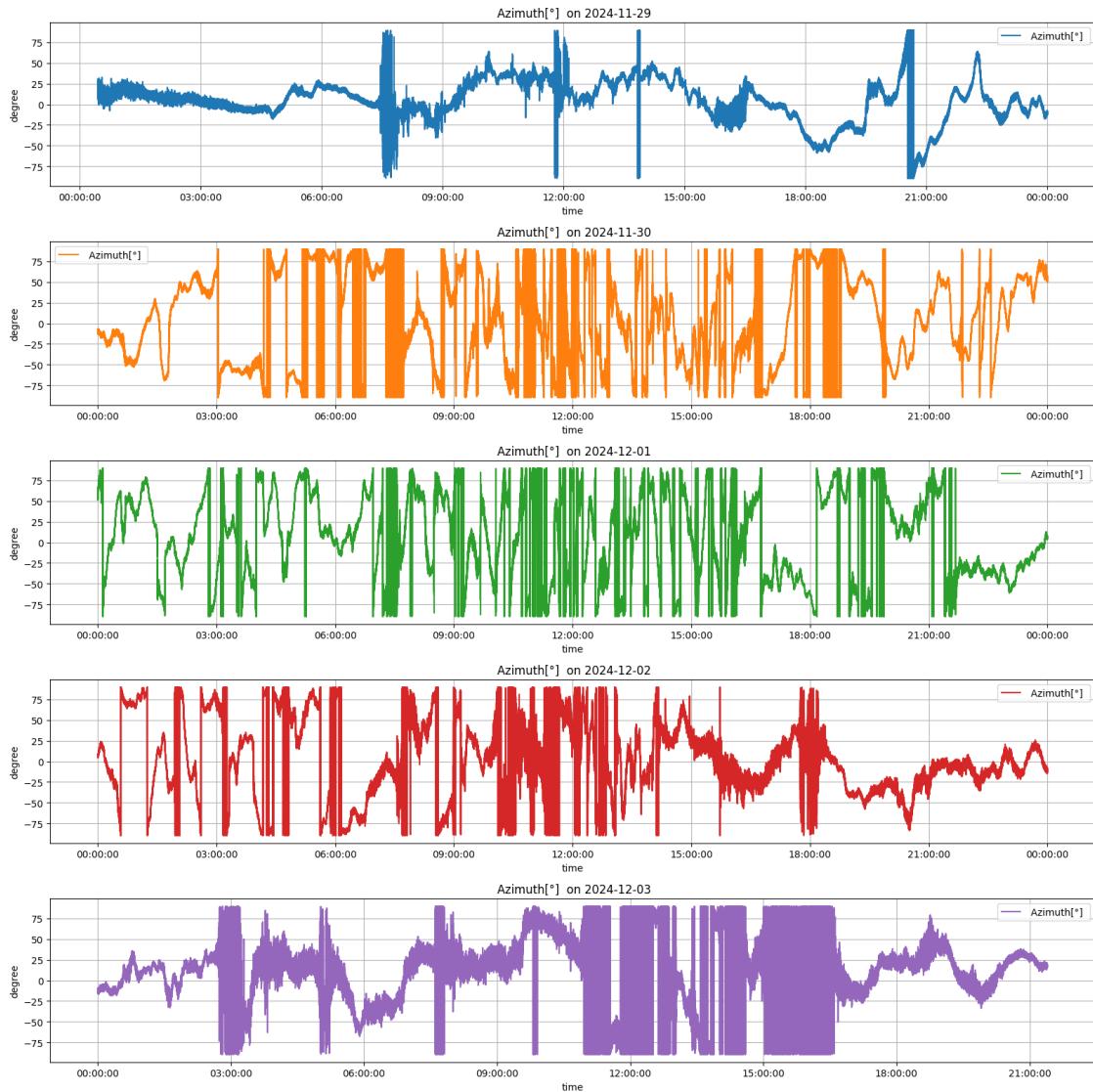
```

    ax.legend(loc='best')
    ax.set_title(f'{columns[9]} on {angle_daily_list[i][0]}')
    ax.set_xlabel('time')
    ax.set_ylabel('degree')

    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S'))

plt.tight_layout()
plt.show()

```

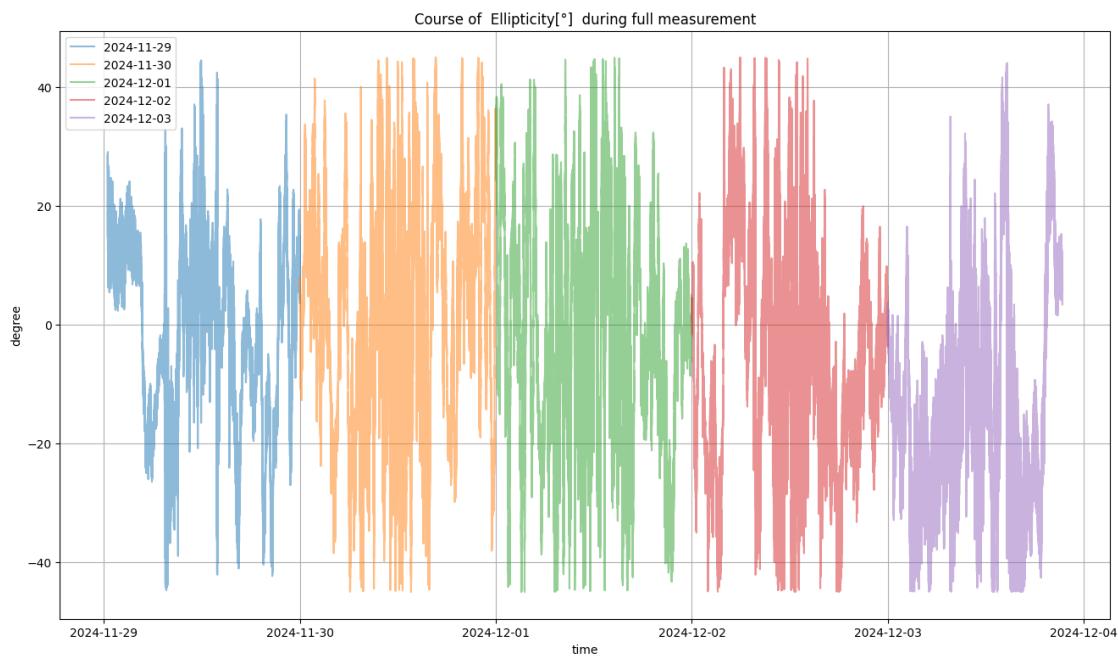


```
[43]: plt.figure(figsize = (16,9))
for date, df_day in angle_daily_list:
    values = df_day[columns[10]]
```

```

plt.plot(values, label=str(date), alpha=0.5)
plt.grid()
plt.legend(loc = 'best')
plt.title(f'Course of {columns[10]} during full measurement')
plt.xlabel('time')
plt.ylabel('degree')
plt.show()

```



```

[44]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(16, 16),
                           sharex=False)

for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    df_day = angle_daily_list[i][1][columns[10]]

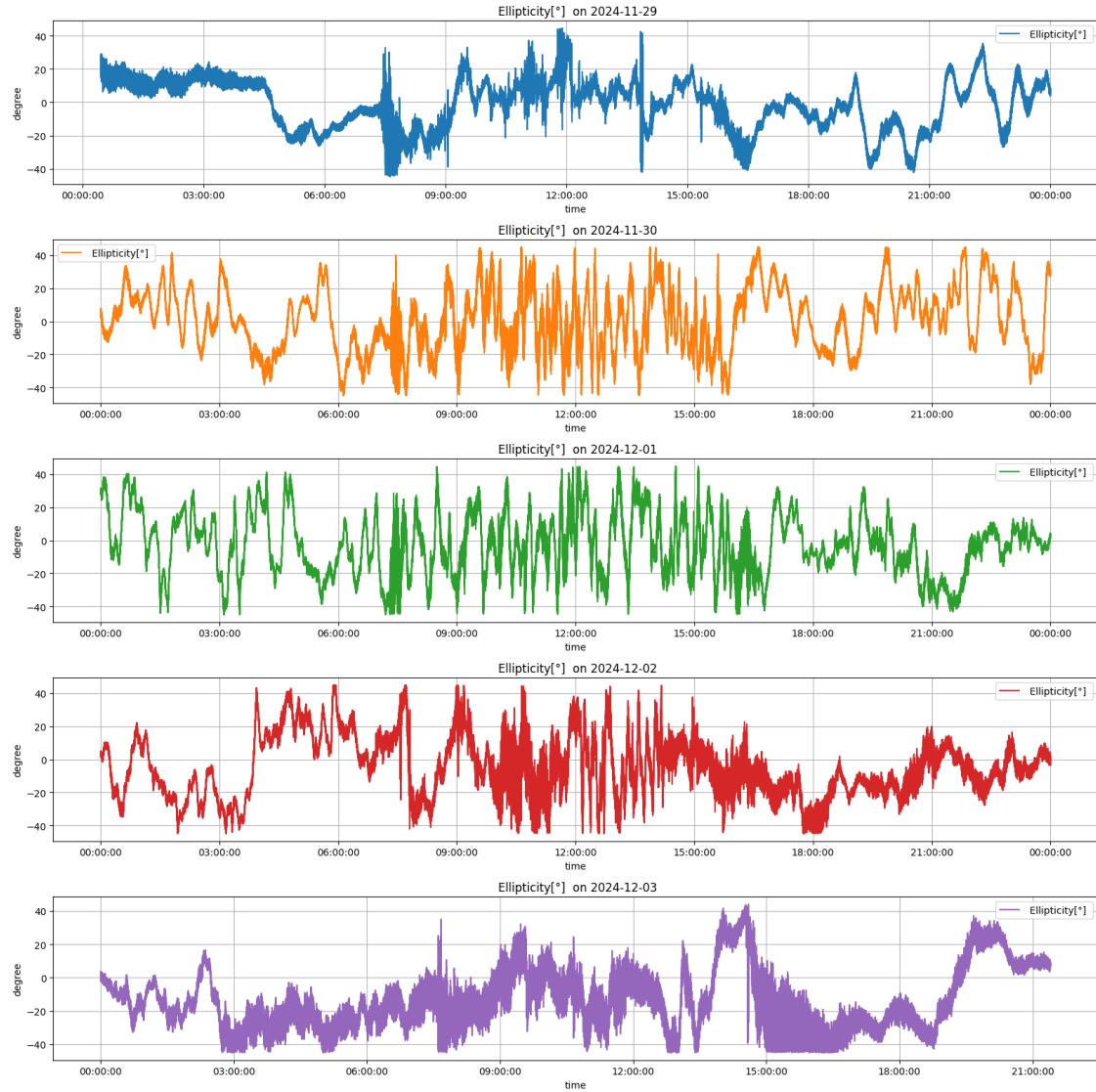
    ax.plot(df_day.index, df_day, label=columns[10], color=colors[i])
    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'{columns[10]} on {angle_daily_list[i][0]}')
    ax.set_xlabel('time')
    ax.set_ylabel('degree')

    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S'))

plt.tight_layout()

```

```
plt.show()
```



3.2 Tägliche Normalverteilung mit Histogramm

```
[45]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(8, 16), sharex=False)

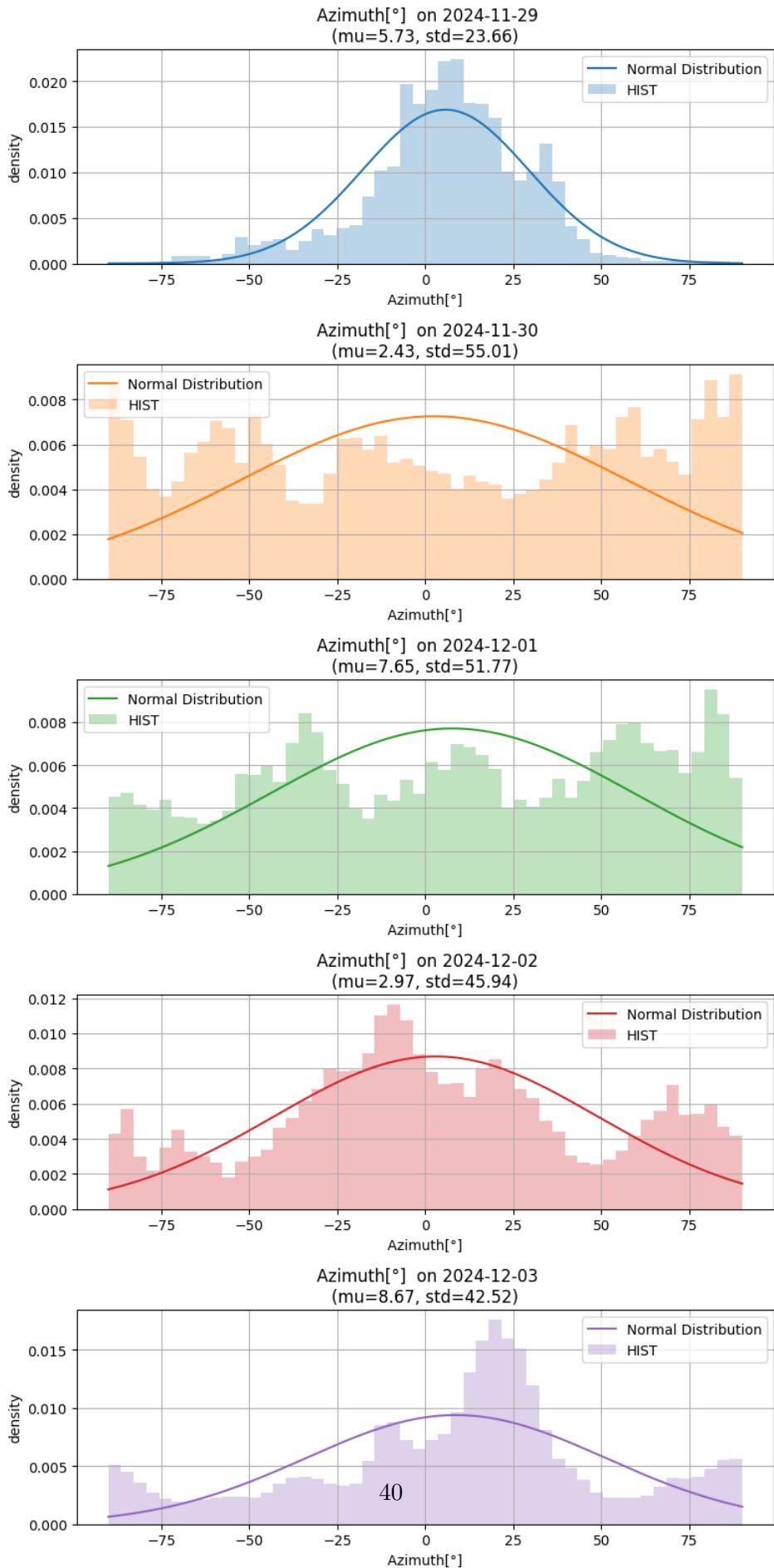
for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    ydata1 = np.array(angle_daily_list[i][1][columns[9]])
    mu1 = np.mean(ydata1)
    sigma1 = np.std(ydata1)
    x1 = np.linspace(ydata1.min(), ydata1.max(), len(ydata1))
```

```
y1 = norm.pdf(x1, mu1, sigma1)

ax.plot(x1, y1, label = 'Normal Distribution', color=colors[i])
ax.hist(ydata1, bins = 50, density = True, color=colors[i], alpha = 0.3,□
label = "HIST")

ax.grid()
ax.legend(loc='best')
ax.set_title(f'{columns[9]} on {angle_daily_list[i][0]}\n(mu={mu1:.2f},□
std={sigma1:.2f})')
ax.set_xlabel(columns[9])
ax.set_ylabel('density')

plt.tight_layout()
plt.show()
```



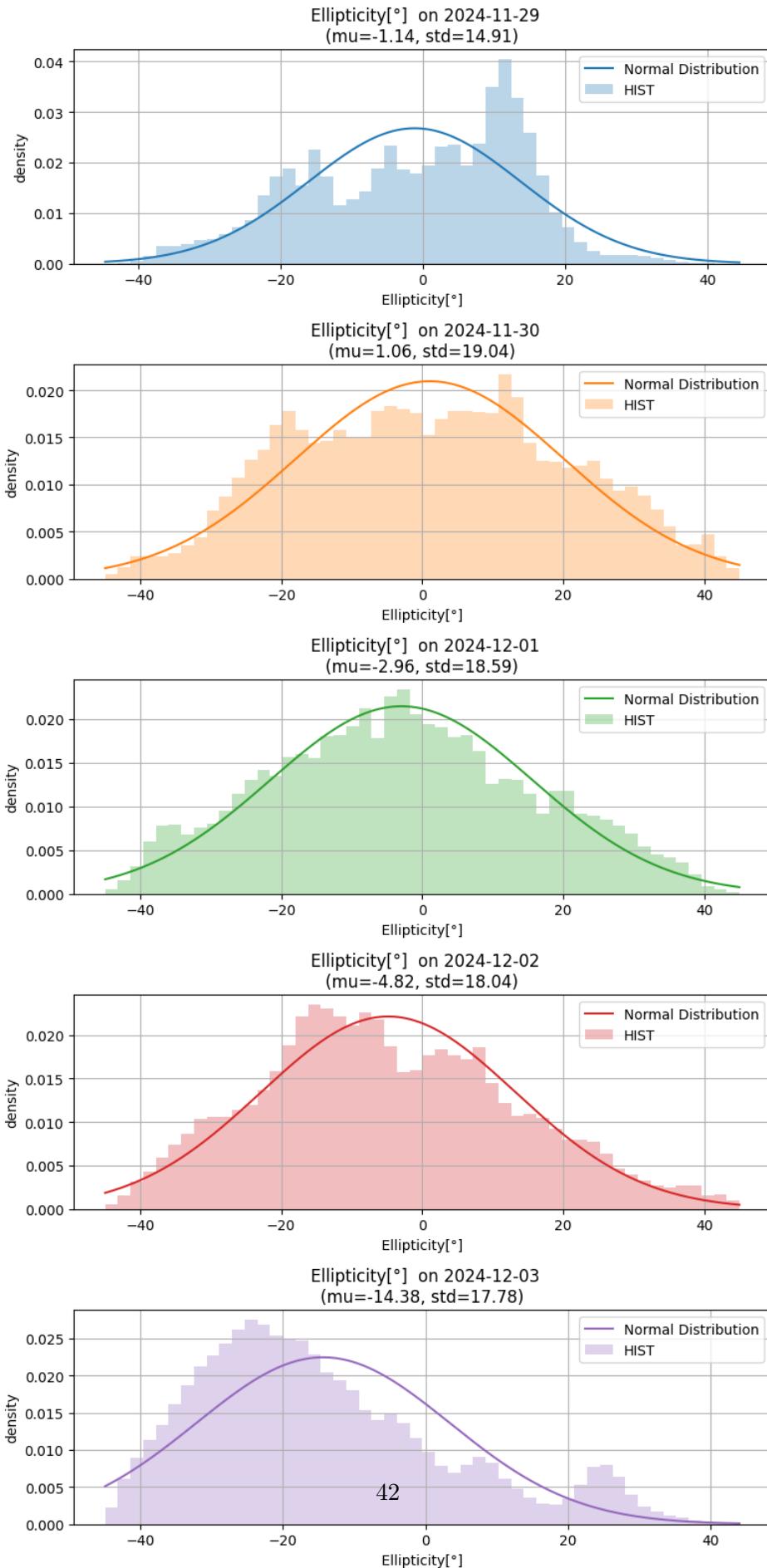
```
[46]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(8, 16), sharex=False)

for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    ydata1 = np.array(angle_daily_list[i][1][columns[10]])
    mu1 = np.mean(ydata1)
    sigma1 = np.std(ydata1)
    x1 = np.linspace(ydata1.min(), ydata1.max(), len(ydata1))
    y1 = norm.pdf(x1, mu1, sigma1)

    ax.plot(x1, y1, label = 'Normal Distribution', color=colors[i])
    ax.hist(ydata1, bins = 50, density = True, color=colors[i], alpha = 0.3, label = "HIST")

    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'{columns[10]} on {angle_daily_list[i][0]}\n(mu={mu1:.2f},\nstd={sigma1:.2f})')
    ax.set_xlabel(columns[10])
    ax.set_ylabel('density')

plt.tight_layout()
plt.show()
```



3.3 Filterung mittels Tief- und Hochpass

```
[47]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(8, 16), sharex=False)

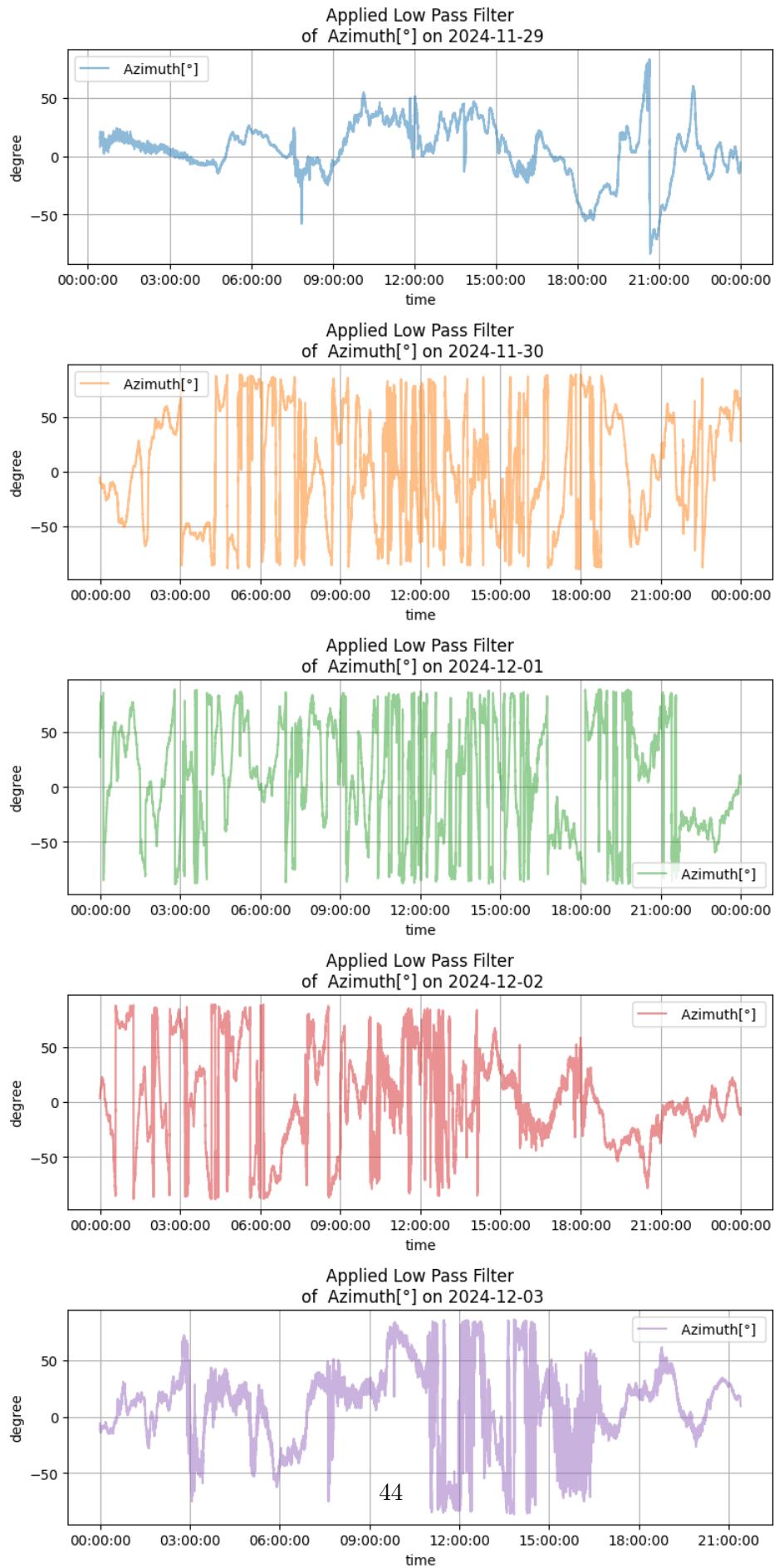
for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    df_day = angle_daily_list[i][1][columns[9]]
    ydata = np.array(df_day)
    lps = lowpass(ydata, 100)

    ax.plot(df_day.index, lps[:-1], label=columns[9], color=colors[i], alpha=0.
            ↵5)

    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'Applied Low Pass Filter\n of {columns[9]} on ↵
    ↵{angle_daily_list[i][0]}')
    ax.set_xlabel('time')
    ax.set_ylabel('degree')

    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S')))

plt.tight_layout()
plt.show()
```

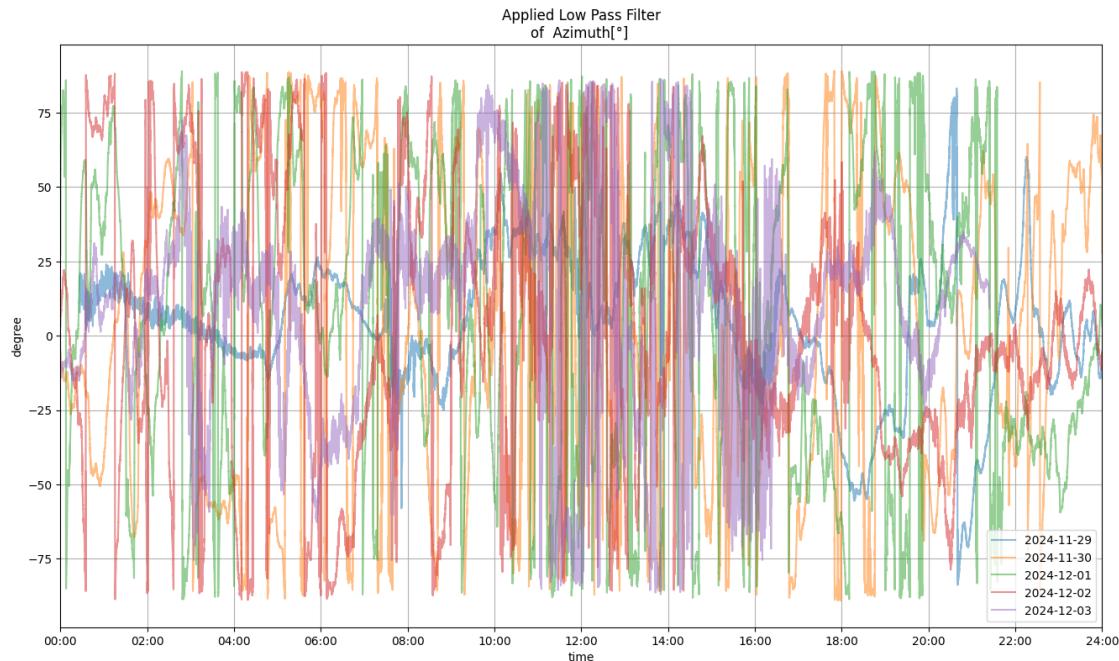


```
[48]: fig, ax = plt.subplots(figsize = (16,9))

for date, df_day in angle_daily_list:
    times = (df_day.index - df_day.index.normalize()).total_seconds()
    ydata = np.array(df_day[column[9]])
    lps = lowpass(ydata, 100)
    plt.plot(times, lps[:-1], label=str(date) , alpha=0.5)

ax.xaxis.set_major_locator(ticker.MultipleLocator(3600 * 2))
ax.xaxis.set_major_formatter(ticker.FuncFormatter(format_time))
ax.set_xlim(0, 24 * 3600)

plt.grid()
plt.legend(loc = 'best')
plt.title(f'Applied Low Pass Filter\nof {columns[9]}')
plt.xlabel('time')
plt.ylabel('degree')
plt.show()
```



```
[49]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(8, 16), sharex=False)
```

```

for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    df_day = angle_daily_list[i][1][columns[10]]
    ydata = np.array(df_day)
    lps = lowpass(ydata, 100)

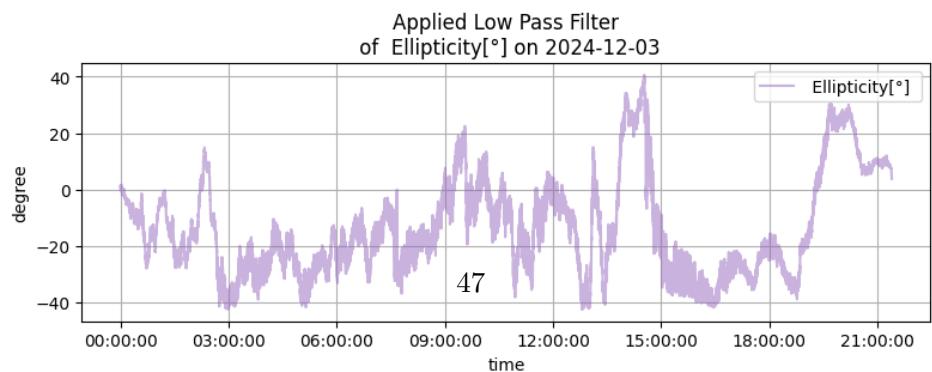
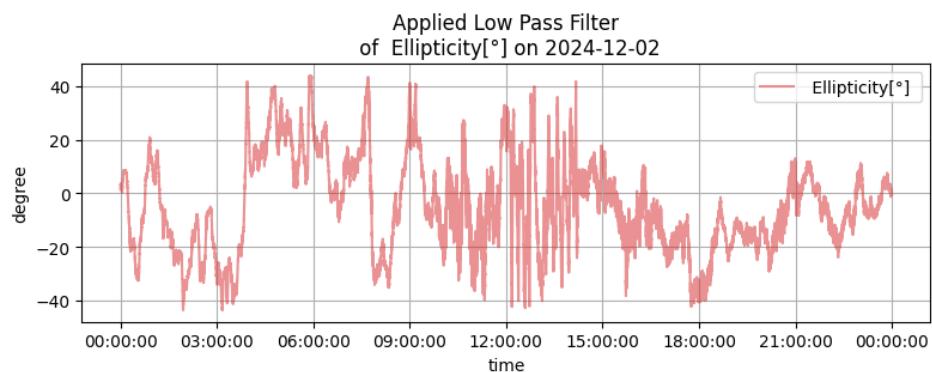
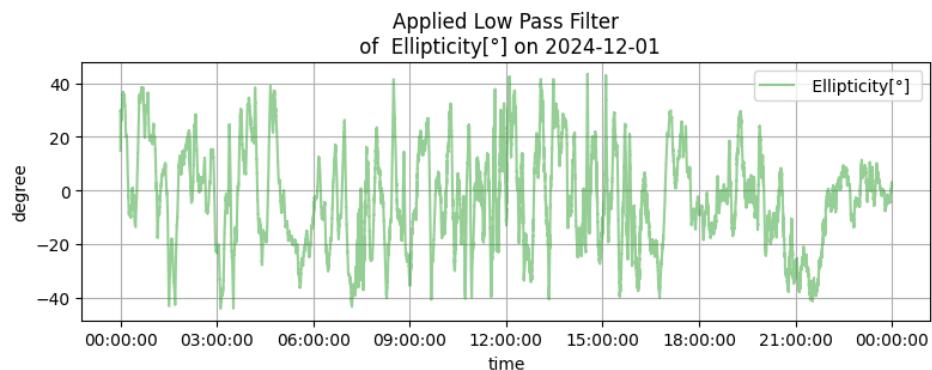
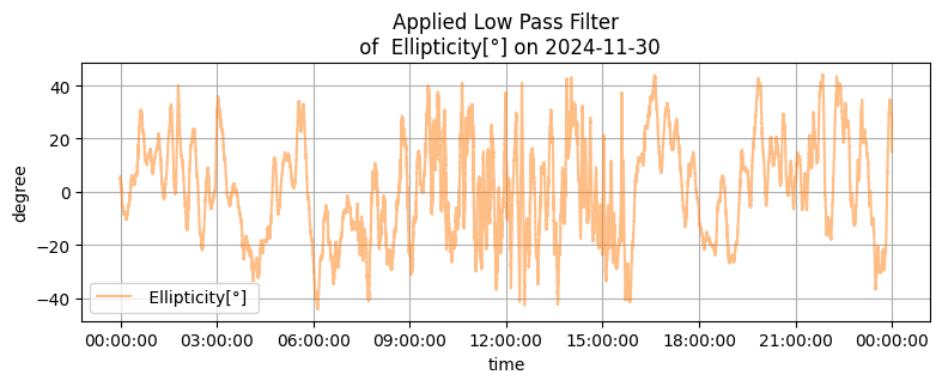
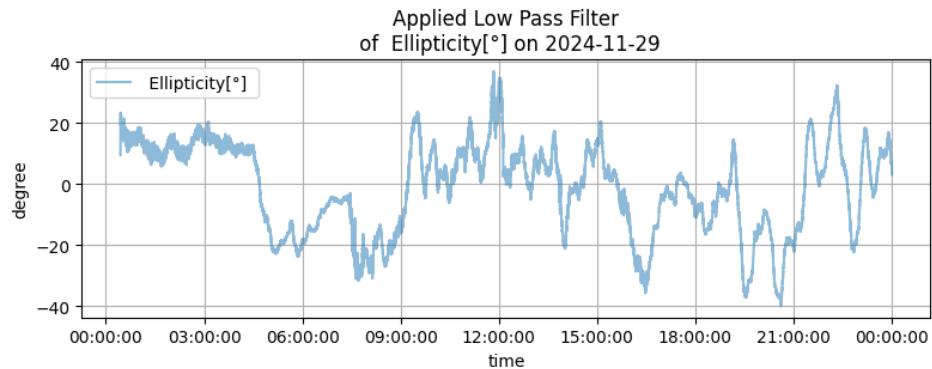
    ax.plot(df_day.index, lps[:-1], label=columns[10], color=colors[i], alpha=0.
            ↵5)

    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'Applied Low Pass Filter\n of {columns[10]}on
            ↵{angle_daily_list[i][0]}')
    ax.set_xlabel('time')
    ax.set_ylabel('degree')

    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S')))

plt.tight_layout()
plt.show()

```

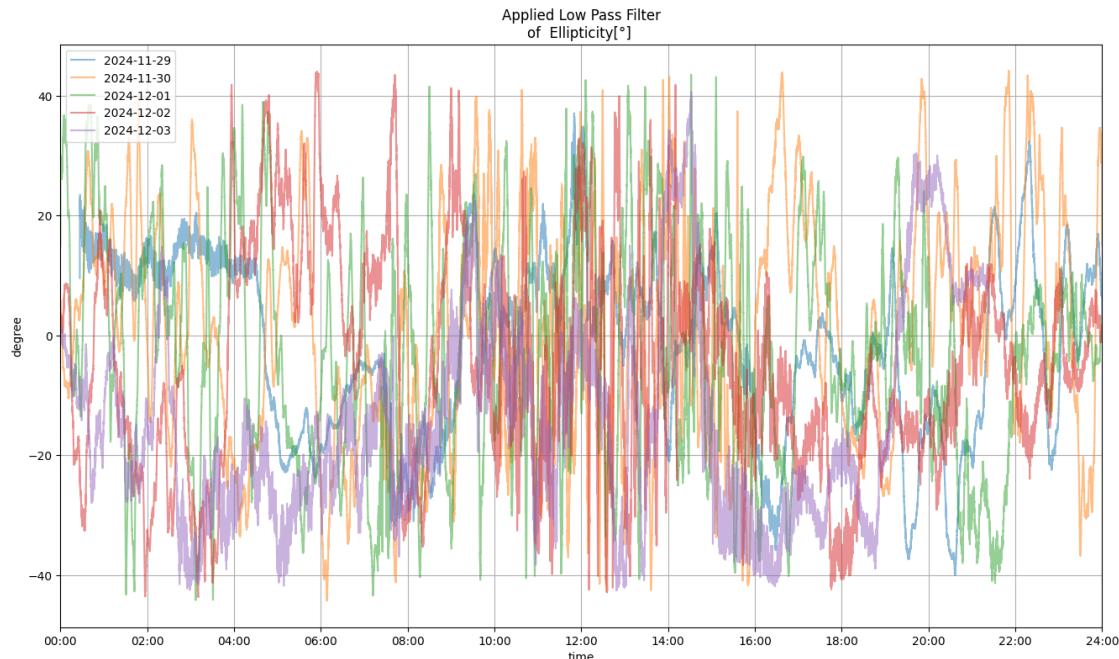


```
[50]: fig, ax = plt.subplots(figsize = (16,9))

for date, df_day in angle_daily_list:
    times = (df_day.index - df_day.index.normalize()).total_seconds()
    ydata = np.array(df_day[column[10]])
    lps = lowpass(ydata, 100)
    plt.plot(times, lps[:-1], label=str(date) , alpha=0.5)

ax.xaxis.set_major_locator(ticker.MultipleLocator(3600 * 2))
ax.xaxis.set_major_formatter(ticker.FuncFormatter(format_time))
ax.set_xlim(0, 24 * 3600)

plt.grid()
plt.legend(loc = 'best')
plt.title(f'Applied Low Pass Filter\nof {column[10]}')
plt.xlabel('time')
plt.ylabel('degree')
plt.show()
```



```
[51]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(8, 16), sharex=False)
```

```

for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    df_day = angle_daily_list[i][1][columns[9]]
    ydata = np.array(df_day)
    hps = highpass(ydata, 100)

    ax.plot(df_day.index, hps, label=columns[9], color=colors[i], alpha=0.5)

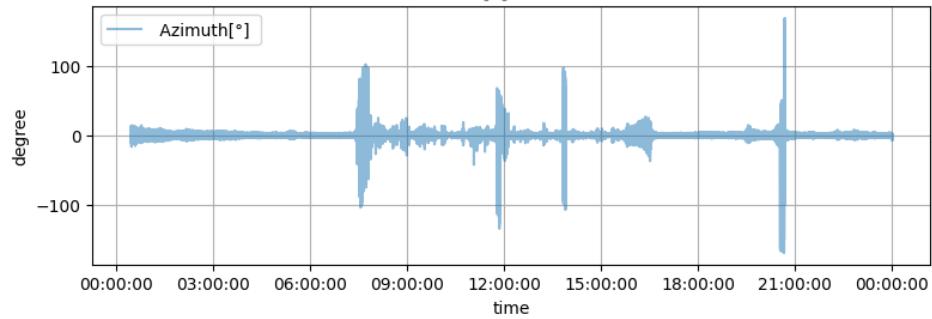
    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'Applied High Pass Filter\n of {columns[9]} on '
    ↪{angle_daily_list[i][0]}'')
    ax.set_xlabel('time')
    ax.set_ylabel('degree')

    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S')))

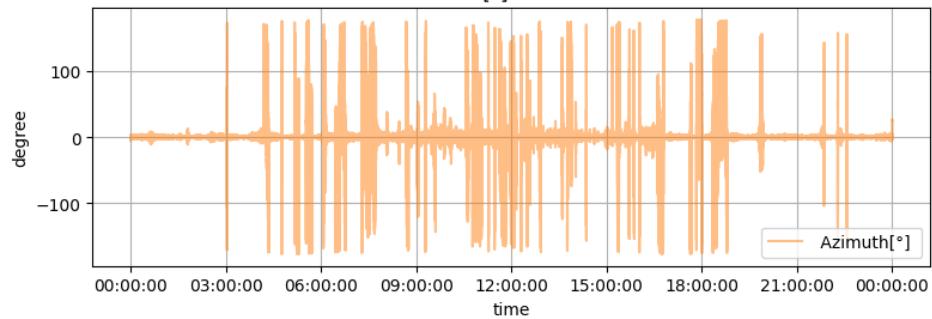
plt.tight_layout()
plt.show()

```

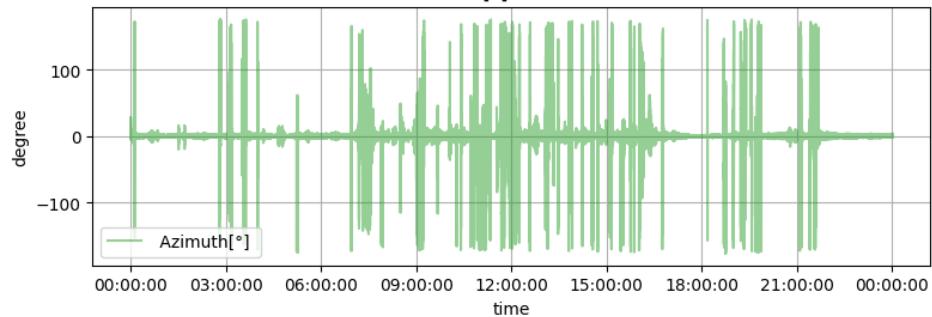
Applied High Pass Filter
of Azimuth[°] on 2024-11-29



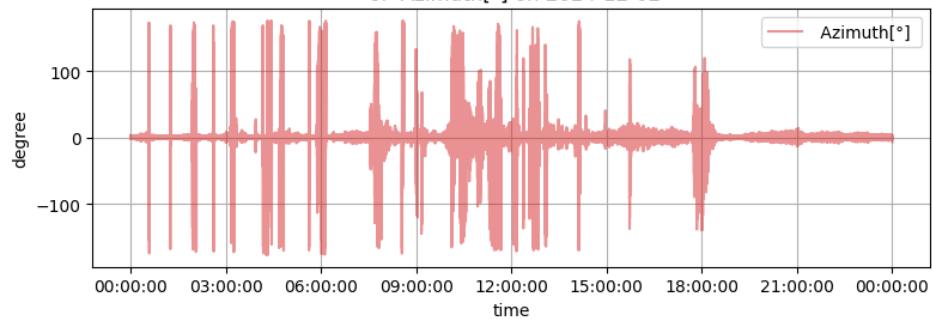
Applied High Pass Filter
of Azimuth[°] on 2024-11-30



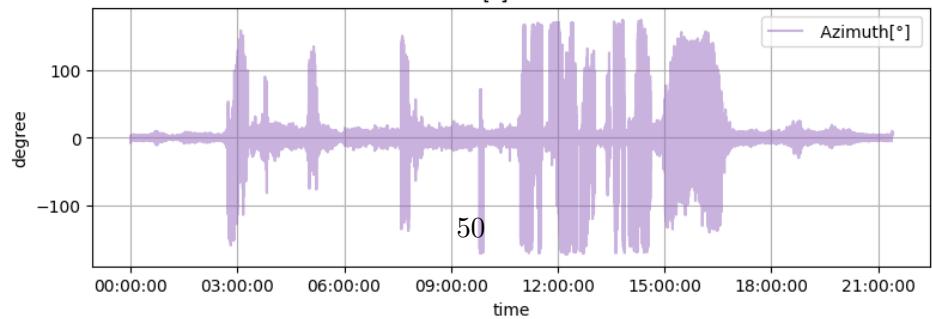
Applied High Pass Filter
of Azimuth[°] on 2024-12-01



Applied High Pass Filter
of Azimuth[°] on 2024-12-02



Applied High Pass Filter
of Azimuth[°] on 2024-12-03



```
[52]: fig, axs = plt.subplots(len(angle_daily_list), 1, figsize=(8, 16), sharex=False)

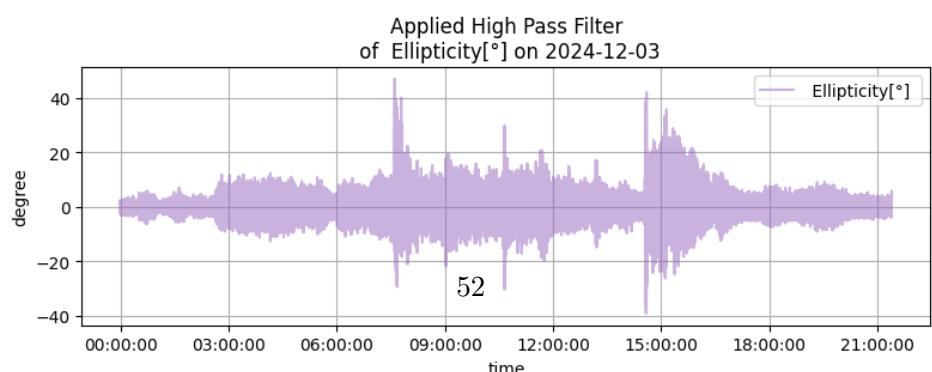
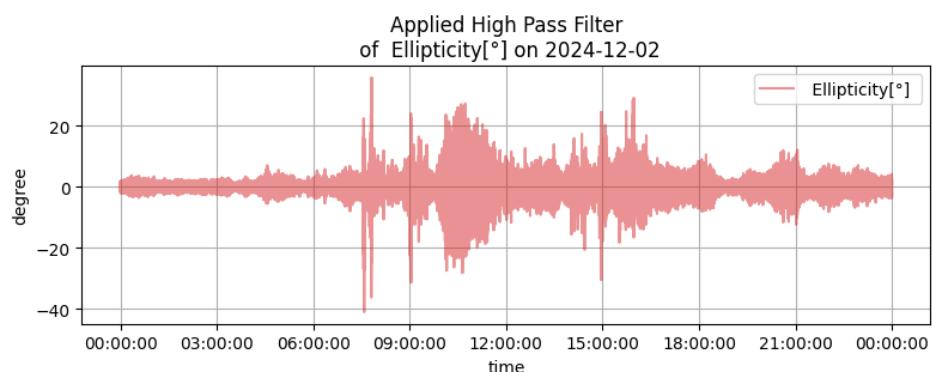
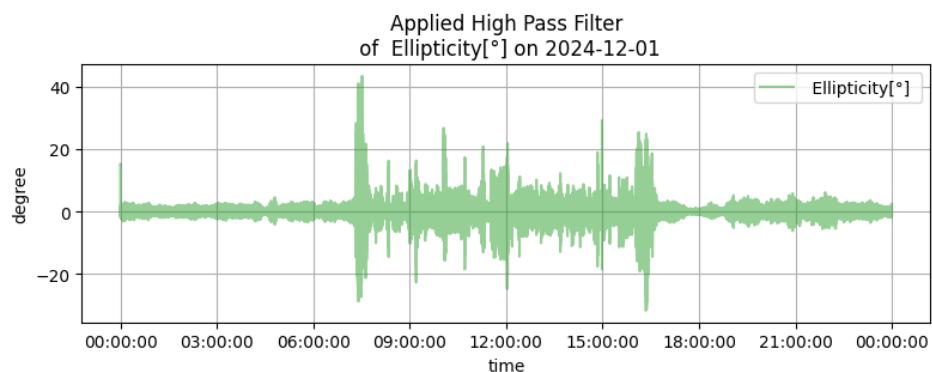
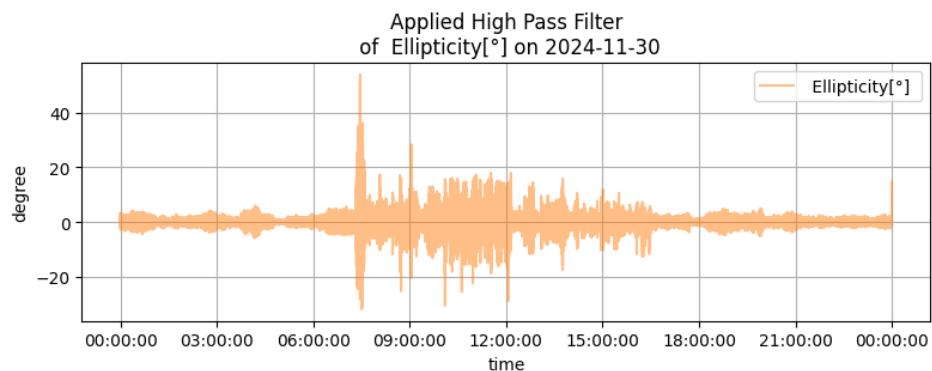
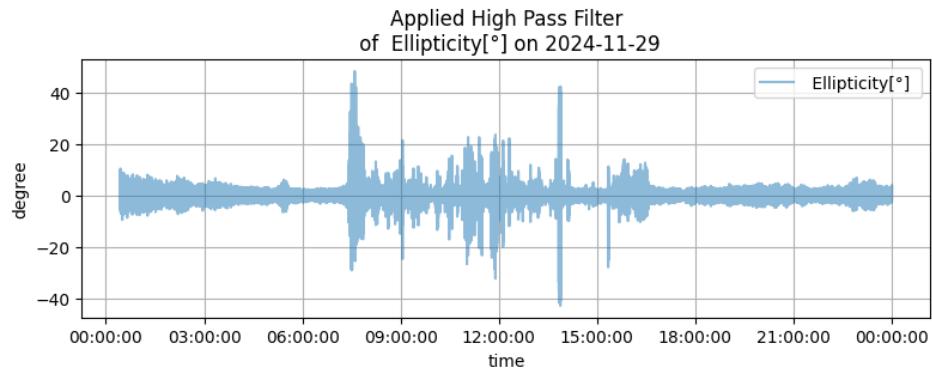
for i in range(len(angle_daily_list)):
    ax = axs[i] if len(angle_daily_list) > 1 else axs
    df_day = angle_daily_list[i][1][columns[10]]
    ydata = np.array(df_day)
    hps = highpass(ydata, 100)

    ax.plot(df_day.index, hps, label=columns[10], color=colors[i], alpha=0.5)

    ax.grid()
    ax.legend(loc='best')
    ax.set_title(f'Applied High Pass Filter\n of {columns[10]} on {angle_daily_list[i][0]}')
    ax.set_xlabel('time')
    ax.set_ylabel('degree')

    ax.xaxis.set_major_formatter(mdates.DateFormatter('%H:%M:%S'))

plt.tight_layout()
plt.show()
```



3.4 Darstellung auf der Poincaré-Kugel

3.4.1 Visualisierung mit dem Python-Tool „py_pol“

```
[53]: one_second = datetime.timedelta(seconds=1)
one_minute = datetime.timedelta(minutes=1)
one_hour = datetime.timedelta(hours=1)
one_quater = datetime.timedelta(hours=6)
one_half = datetime.timedelta(hours=12)
one_day = datetime.timedelta(days=1)

start_time = datetime.datetime.strptime(str(angle.index[0]), '%Y-%m-%d %H:%M:%S.%f')
end_time_second = start_time + one_second
end_time_minute = start_time + one_minute
end_time_hour = start_time + one_hour
end_time_quater = start_time + one_quater
end_time_half = start_time + one_half
end_time_day = start_time + one_day
```

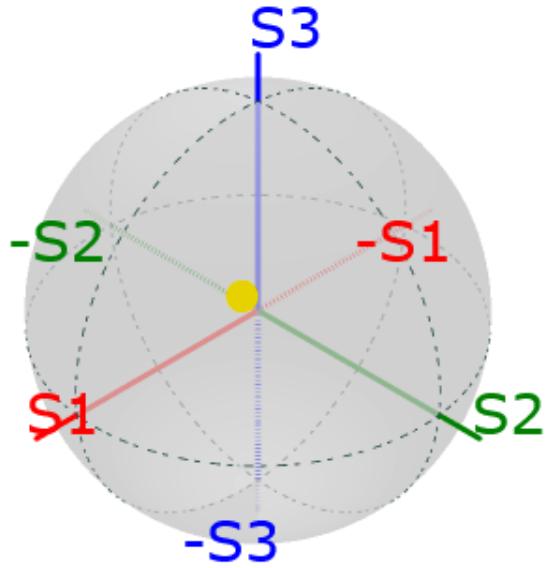
```
[80]: first_val = angle.iloc[0]

az = np.array(first_val[columns[9]]) * degrees
el = np.array(first_val[columns[10]]) * degrees

S = Stokes("Calculated Point")
S.general_azimuth_ellipticity(az, el)

fig = S.draw_poincare(kind="scatter")
#fig.show()
Image(filename="../img/first_val.png")
```

```
[80]:
```



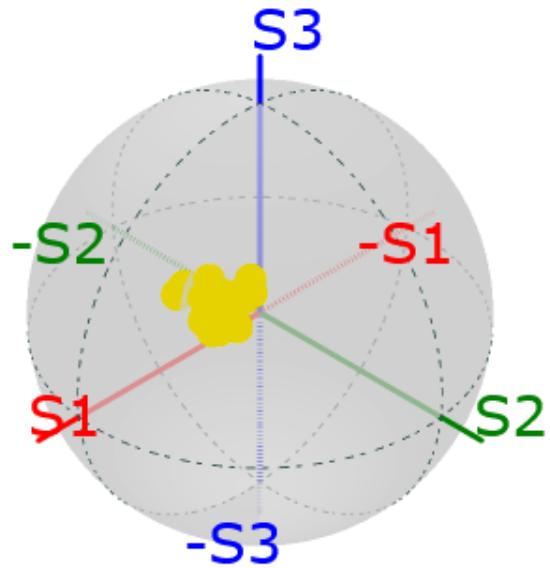
```
[81]: first_second = angle.loc[(angle.index >= start_time) & (angle.index < end_time_second)]

az = np.array(first_second[columns[9]].values) * degrees
el = np.array(first_second[columns[10]].values) * degrees

S = Stokes("Calculated Points")
S.general_azimuth_ellipticity(az, el)

fig = S.draw_poincare(kind="scatter")
#fig.show()
Image(filename="../img/first_second.png")
```

[81]:



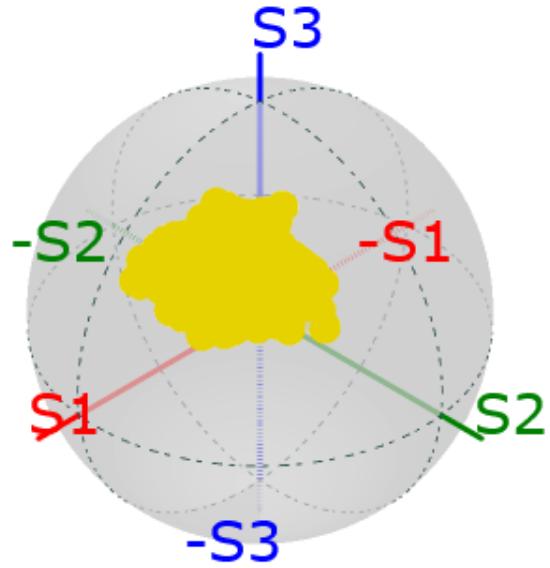
```
[82]: first_minute = angle.loc[(angle.index >= start_time) & (angle.index < end_time_minute)]

az = np.array(first_minute[columns[9]].values) * degrees
el = np.array(first_minute[columns[10]].values) * degrees

S = Stokes("Calculated Points")
S.general_azimuth_ellipticity(az, el)

fig = S.draw_poincare(kind="scatter")
#fig.show()
Image(filename="../img/first_minute.png")
```

[82]:



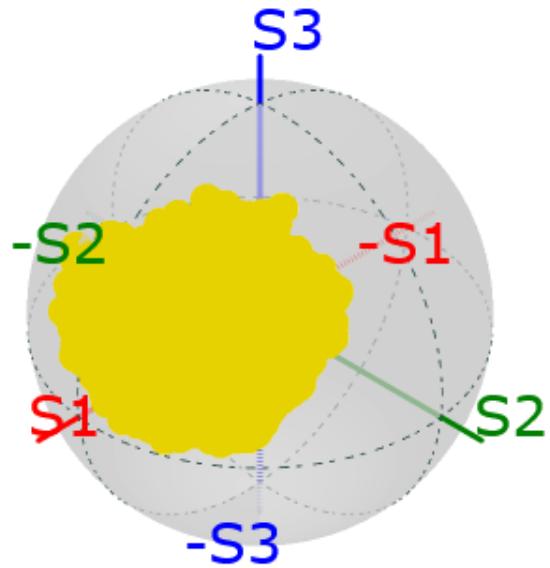
```
[83]: first_hour = angle.loc[(angle.index >= start_time) & (angle.index < end_time_hour)]

az = np.array(first_hour[columns[9]].values) * degrees
el = np.array(first_hour[columns[10]].values) * degrees

S = Stokes("Calculated Points")
S.general_azimuth_ellipticity(az, el)

fig = S.draw_poincare(kind="scatter")
#fig.show()
Image(filename='./img/first_hour.png')
```

[83]:



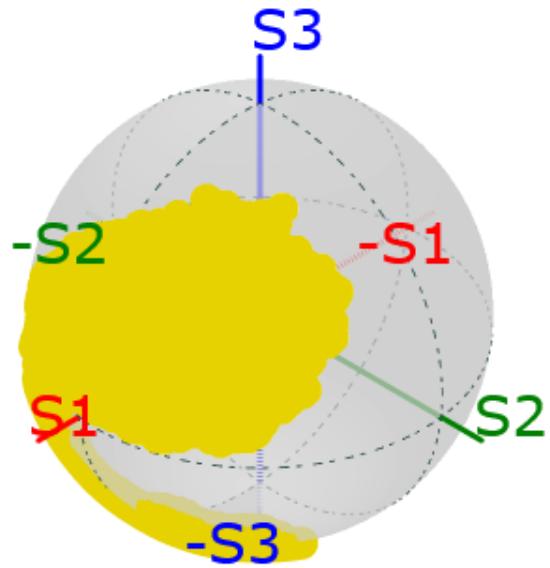
```
[84]: first_quater = angle.loc[(angle.index >= start_time) & (angle.index < end_time_quater)]

az = np.array(first_quater[cOLUMNS[9]].values) * degrees
el = np.array(first_quater[cOLUMNS[10]].values) * degrees

S = Stokes("Calculated Points")
S.general_azimuth_ellipticity(az, el)

fig = S.draw_poincare(kind="scatter")
#fig.show()
Image(filename="../img/first_quater.png")
```

[84]:



3.4.2 Eigene Berechnung und Visualisierung der Daten

```
[59]: normalized_stokes = pd.read_csv(filename, skiprows=skip, usecols=[columns[2], columns[3], columns[4]], sep=sep, nrows=19)
x,y,z = convert_angel(first_second[columns[9]].values, first_second[columns[10]].values)

data = pd.DataFrame({
    "S1": x,
    "Normalized S1": normalized_stokes[columns[2]],
    "S2": y,
    "Normalized S2": normalized_stokes[columns[3]],
    "S3": z,
    "Normalized S3": normalized_stokes[columns[4]]})
```

```

    "S3": z,
    "Normalized S3": normalized_stokes[columns[4]]
)
print(data)

```

	S1	Normalized S1	S2	Normalized S2	S3	Normalized S3
0	0.596336	0.60	0.511483	0.51	0.618683	0.62
1	0.701573	0.70	0.488696	0.49	0.518624	0.52
2	0.700520	0.70	0.482535	0.48	0.525769	0.53
3	0.655133	0.66	0.534695	0.53	0.533762	0.53
4	0.646914	0.65	0.488193	0.49	0.585807	0.59
5	0.604898	0.60	0.497930	0.50	0.621421	0.62
6	0.550527	0.55	0.498488	0.50	0.669649	0.67
7	0.569661	0.57	0.523097	0.52	0.633921	0.63
8	0.613659	0.61	0.484291	0.48	0.623607	0.62
9	0.661133	0.66	0.472976	0.47	0.582407	0.58
10	0.720448	0.72	0.431179	0.43	0.543174	0.54
11	0.717083	0.72	0.469604	0.47	0.515038	0.52
12	0.701476	0.70	0.469243	0.47	0.536416	0.54
13	0.687339	0.69	0.397475	0.40	0.607930	0.61
14	0.656328	0.66	0.424273	0.42	0.623880	0.62
15	0.645526	0.65	0.435085	0.44	0.627691	0.63
16	0.645842	0.65	0.383778	0.38	0.660002	0.66
17	0.706732	0.71	0.317914	0.32	0.632029	0.63
18	0.736016	0.74	0.307279	0.31	0.603208	0.60

```
[60]: print("Original normalized S1 equals calculated S1? ", data['Normalized S1'].
    ↪equals(round(data['S1'], 2)))
print("Original normalized S2 equals calculated S2? ", data['Normalized S2'].
    ↪equals(round(data['S2'], 2)))
print("Original normalized S3 equals calculated S3? ", data['Normalized S3'].
    ↪equals(round(data['S3'], 2)))
```

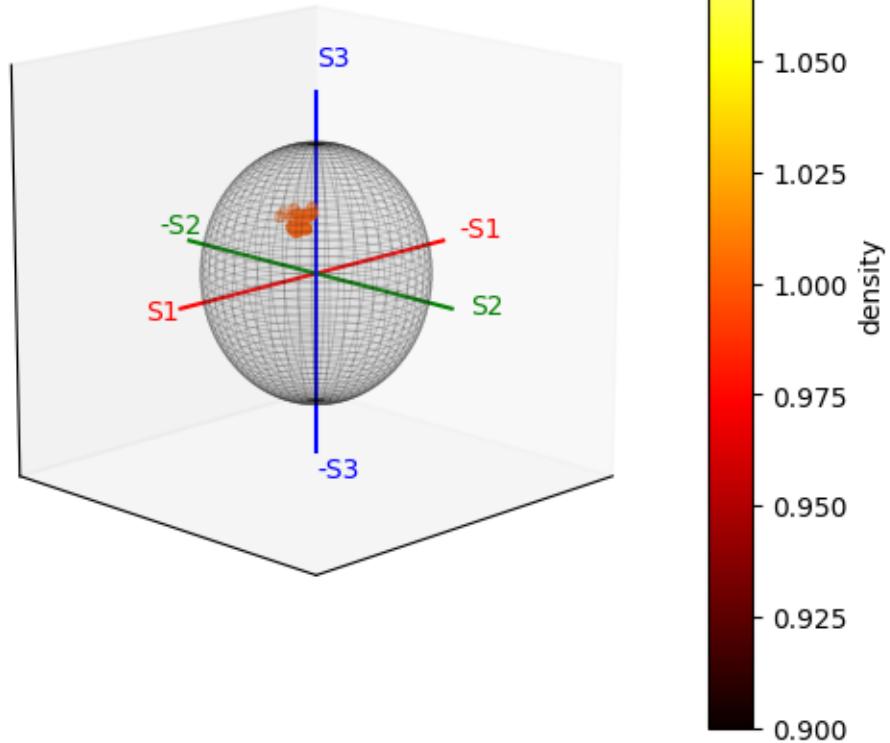
```
Original normalized S1 equals calculated S1? True
Original normalized S2 equals calculated S2? True
Original normalized S3 equals calculated S3? True
```

```
[62]: #%matplotlib notebook # interaktiver Plot-Mode
%matplotlib inline # statischer Plot-Mode
```

```
UsageError: unrecognized arguments: # statischer Plot-Mode
```

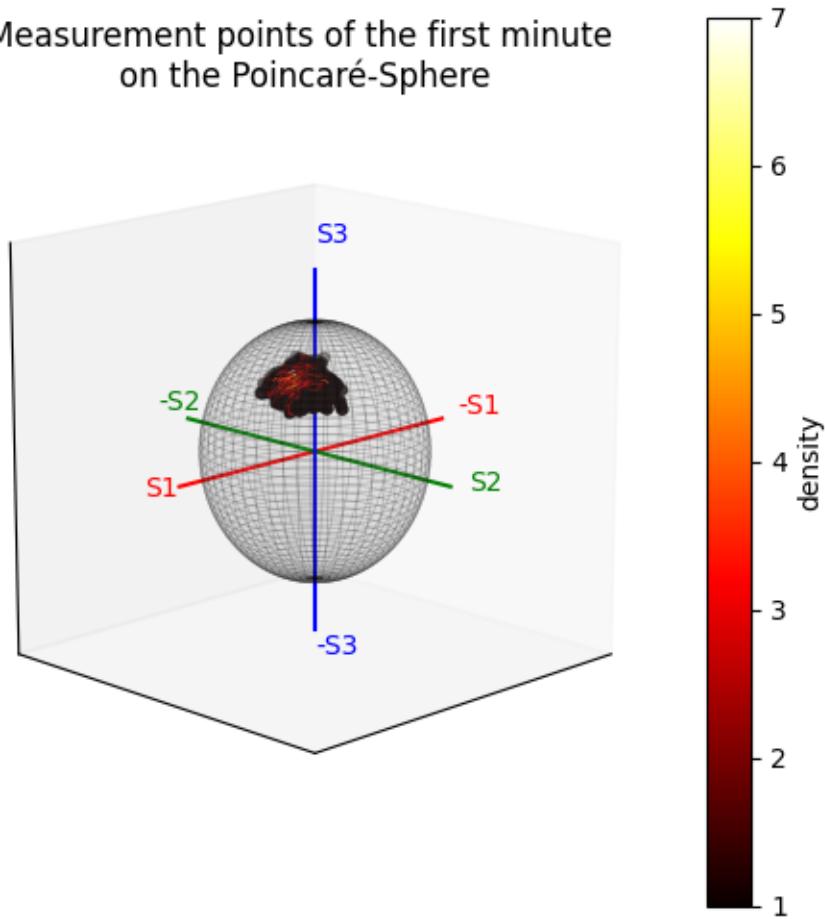
```
[65]: title = 'Measurement points of the first second \non the Poincaré-Sphere'
x,y,z = convert_angel(first_second[columns[9]].values, ↪
    ↪first_second[columns[10]].values)
freq = calculate_freq(x, y, z)
plot_poincare(x, y, z, freq, title=title)
```

Measurement points of the first second
on the Poincaré-Sphere



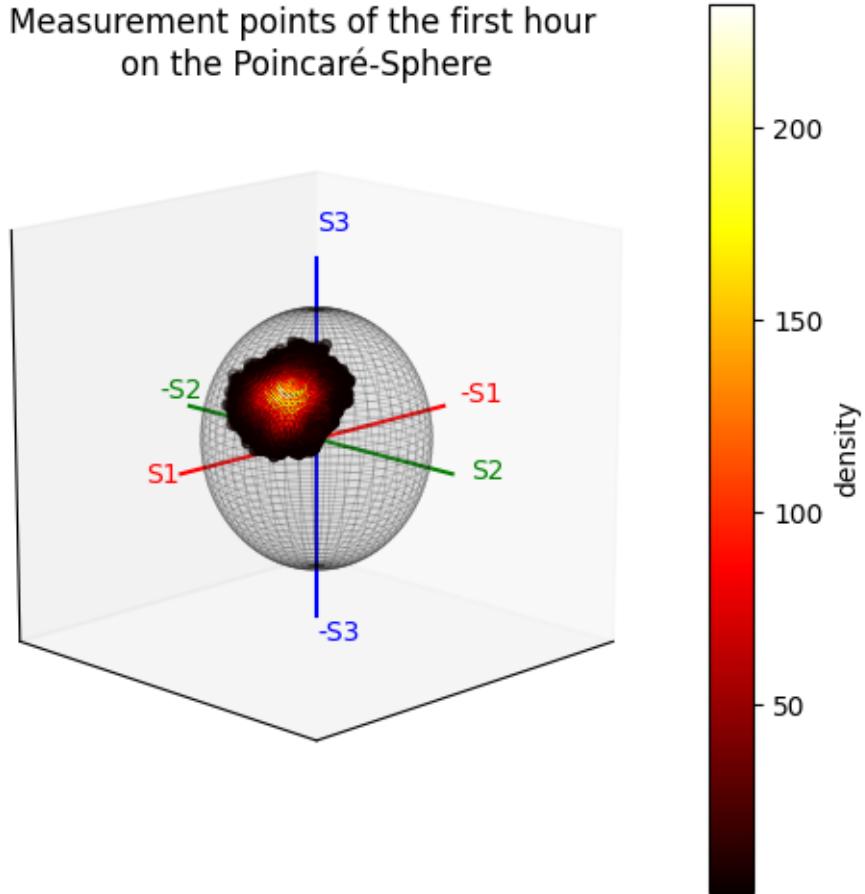
```
[66]: title = 'Measurement points of the first minute \non the Poincaré-Sphere'
x,y,z = convert_angle(first_minute[columns[9]].values,
                     first_minute[columns[10]].values)
freq = calculate_freq(x, y, z)
plot_poincare(x, y, z, freq, title=title)
```

Measurement points of the first minute
on the Poincaré-Sphere



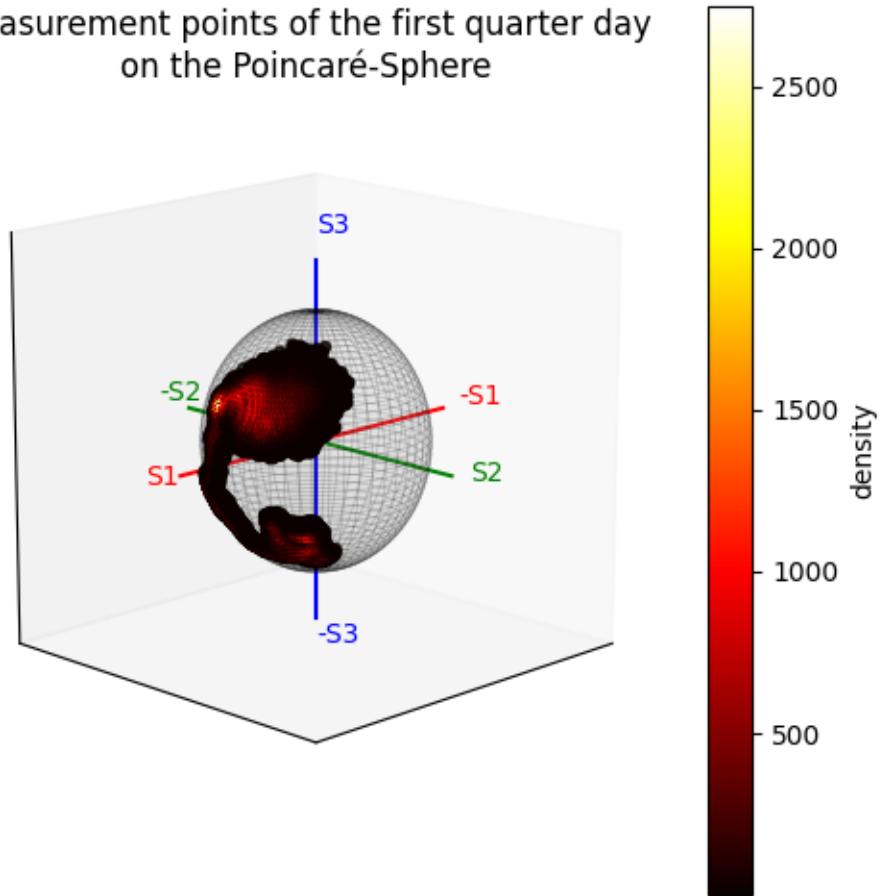
```
[67]: title = 'Measurement points of the first hour \non the Poincaré-Sphere'
x,y,z = convert_angel(first_hour[column[9]].values, first_hour[column[10]].values)
freq = calculate_freq(x, y, z)
plot_poincare(x, y, z, freq, title=title)
```

Measurement points of the first hour
on the Poincaré-Sphere



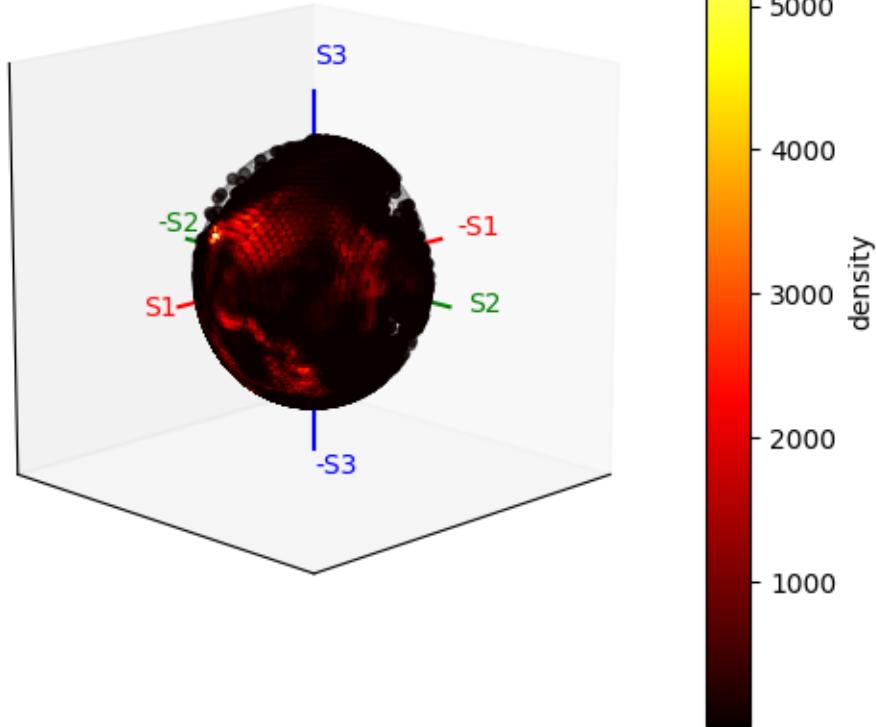
```
[68]: title = 'Measurement points of the first quarter day \non the Poincaré-Sphere'
x,y,z = convert_angle(first_quarter[columns[9]].values,_
    ↪first_quarter[columns[10]].values)
freq = calculate_freq(x, y, z)
plot_poincare(x, y, z, freq, title=title)
```

Measurement points of the first quarter day
on the Poincaré-Sphere



```
[70]: first_half = angle.loc[(angle.index >= start_time) & (angle.index < end_time_half)]  
  
title = 'Measurement points of the first half day \non the Poincaré-Sphere'  
x,y,z = convert_angle(first_half[column[9]].values, first_half[column[10]].values)  
freq = calculate_freq(x, y, z)  
plot_poincare(x, y, z, freq, title=title)
```

Measurement points of the first half day
on the Poincaré-Sphere



```
[71]: angle_seconds_resample = angle.resample('s').mean().ffill()  
angle_seconds_resample.head()
```

```
[71]:
```

Time[date hh:mm:ss]	Azimuth[°]	Ellipticity[°]
2024-11-29 00:26:44	19.217000	18.165000
2024-11-29 00:26:45	12.858095	18.943810
2024-11-29 00:26:46	17.388500	19.627000
2024-11-29 00:26:47	17.231053	19.551053
2024-11-29 00:26:48	15.330952	22.748571

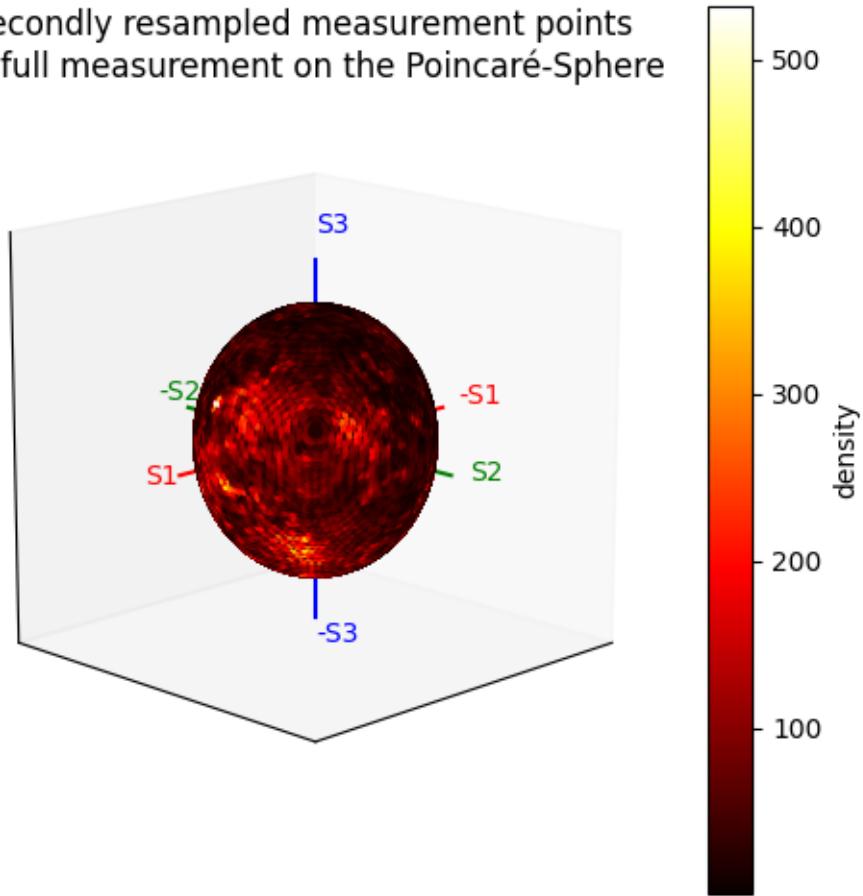
```
[72]: print(angle_seconds_resample.isnull().sum())  
print(type(angle.index))
```

```
Azimuth[°]      0  
Ellipticity[°]   0  
dtype: int64  
<class 'pandas.core.indexes.datetimes.DatetimeIndex'>
```

```
[74]: title= 'Secondly resampled measurement points \nfor full measurement on the\nPoincaré-Sphere'

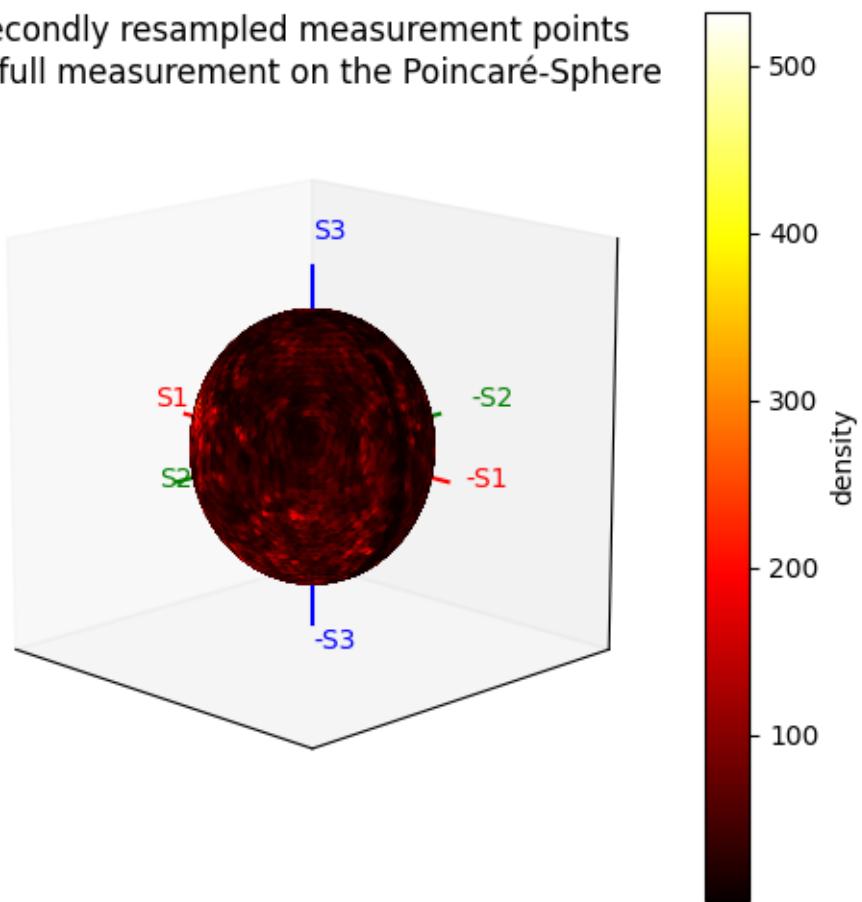
x,y,z = convert_angle(angle_seconds_resample[columns[9]].values, u
    ↪angle_seconds_resample[columns[10]].values)
freq = calculate_freq(x, y, z)
plot_poincare(x, y, z, freq, title=title)
```

Secondly resampled measurement points
for full measurement on the Poincaré-Sphere



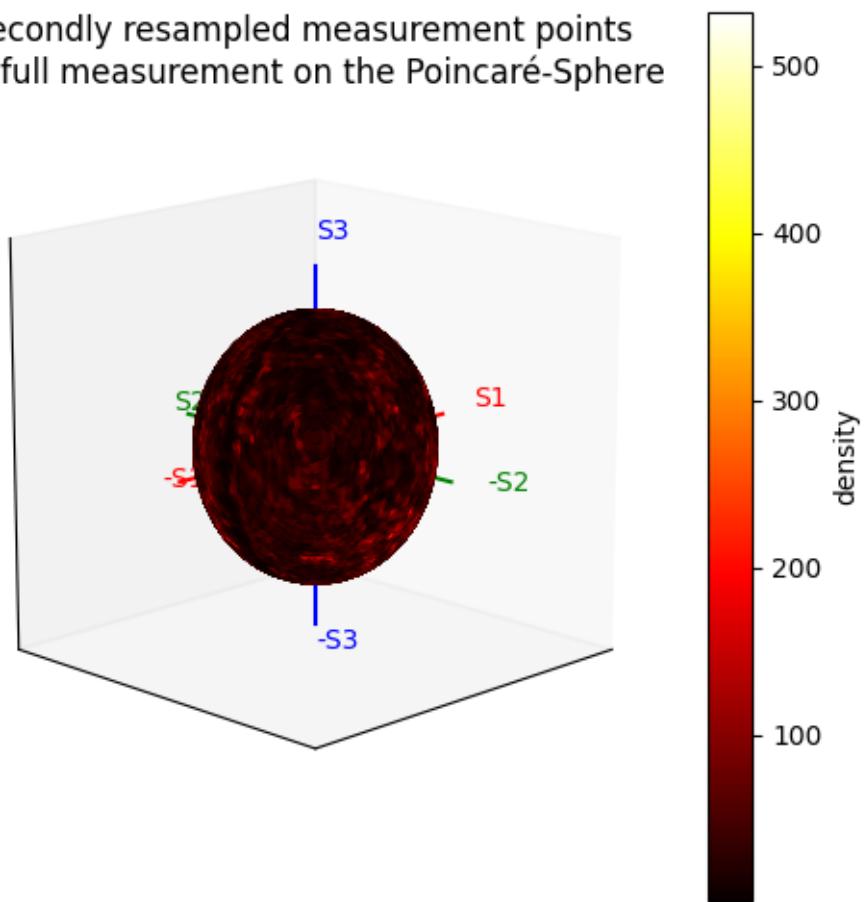
```
[75]: #elev=15, azim=45
title= 'Secondly resampled measurement points \nfor full measurement on the\nPoincaré-Sphere'
plot_poincare(x, y, z, freq, elev=15, azim=135, title=title)
```

Secondly resampled measurement points
for full measurement on the Poincaré-Sphere



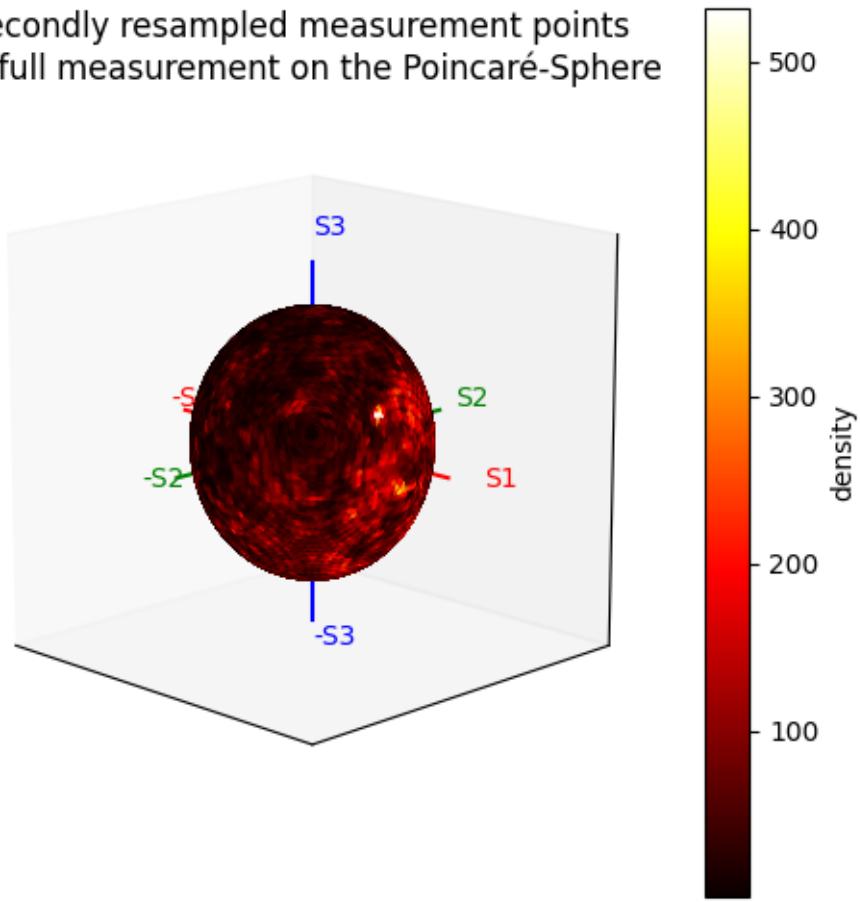
```
[76]: #elev=15, azim=45
title= 'Secondly resampled measurement points \nfor full measurement on the_\n\tPoincaré-Sphere'
plot_poincare(x, y, z, freq, elev=15, azim=225, title=title)
```

Secondly resampled measurement points
for full measurement on the Poincaré-Sphere



```
[77]: #elev=15, azim=45
title= 'Secondly resampled measurement points \nfor full measurement on the_\u2190Poincar\u00e9-Sphere'
plot_poincare(x, y, z, freq, elev=15, azim=315, title=title)
```

Secondly resampled measurement points
for full measurement on the Poincaré-Sphere



[]: