

overview

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Dark-Fiber Charakterisierung für entanglement polarisierter QKD

Übersicht und Aufbereitung von Messverfahren und Messdaten

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Datensatz: Nordhausen - Sundhausen

1 Einleitung: Kenngrößen, Messgerät und Datengrundlage

1.1 Ressourcen und Literatur

- [Messdaten](#)
- [Messgerät](#)
- [Abbildung: Poincaré-Kugel](#)

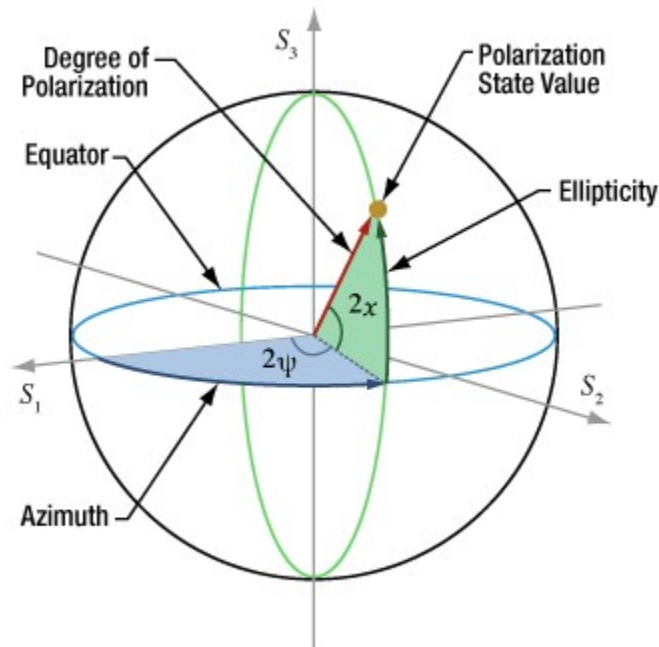
1.2 Kenngrößen: Bedeutung und Einheiten

Kenngröße	Einheit	Bedeutung
Time	date hh:mm:ss	absoluter Messzeitpunkt
Elapsed Time	hh:mm:ss:ms	relativer Messzeitpunkt
Normalized s1, s2, s3	-	Normierte Stokes-Komponenten
S0	mW	Gesamtleistung
S1, S2, S3	mW	Stokes-Komponenten
Azimuth	°	Winkel in der Poincaré-Kugel (horizontaler Winkel)
Ellipticity	°	Maß für elliptische Polarisation (vertikaler Winkel)
DOP	%	Degree of Polarization
DOCP	%	Degree of Circular Polarization (Zirkularitätsmaß)

Kenngöße	Einheit	Bedeutung
DOLP	%	Degree of Linear Polarization (Linearitätsmaß)
Power	mW / dBm	Gesamtleistung
Pol Power	mW / dBm	Polarisierter Anteil (= DOP × Gesamtleistung)
Unipol Power	mW / dBm	Unpolarisierter Anteil (= (1-DOP) × Gesamtleistung)
Phase Difference	°	Phasenunterschied zw. Polarisationsmoden
Power-Split-Ratio	-	Leistungsverhältnis zweier Polarisationsrichtungen
Warning	-	Hinweis für fehlerhafte Messung

```
[1]: from IPython.display import Image
Image(filename="./poincare.jpg")
```

[1]:



1.3 Messgerät und Messverfahren

Kenngöße	Info
Device	PAX1000IR2/M
Serial Number	M00773008
Firmware Version	1.2.1
Software Version	1.4.2002.183
Wavelength [nm]	1560
Basic Sample Rate [Hz]	100
Operating Mode	revolutions for one measurement, 2048 points for FFT

2 Aufbereitung der Messdaten

2.1 Verwendete Libraries / Softwaretools

```
[3]: import pandas as pd
import matplotlib.pyplot as plt
import numpy as np
import io
import datetime
import requests

from prettytable import PrettyTable
```

2.2 Eigene Hilfsfunktionen

```
[4]: def fast_parse_elapsed(s):
    try:
        d, h, m, s, ms = s.replace('.', ':').split(':')
        return pd.Timedelta(days=int(d), hours=int(h), minutes=int(m),
↪seconds=int(s), milliseconds=int(ms))
    except:
        return pd.NaT
```

2.3 Datenaufbereitungsschritte

```
[5]: filename = '29.11.2024_10d.csv'
skip = 8
sep = ";
```

```
[6]:
```

```

columns = ['Time[date hh:mm:ss] ', ' Elapsed Time [hh:mm:ss:ms]', ' Normalized_
↳s 1 ', ' Normalized s 2 ', ' Normalized s 3 ', ' S 0 [mW]', ' S 1 [mW]', ' S_
↳2 [mW]', ' S 3 [mW]', ' Azimuth[°] ', ' Ellipticity[°] ', ' DOP[%] ', '_
↳DOCP[%] ', ' DOLP[%] ', ' Power[mW] ', ' Pol Power[mW] ', ' Unpol Power[mW]_
↳', ' Power[dBm] ', ' Pol Power[dBm] ', ' Unpol Power[dBm] ', '_
↳Power-Split-Ratio ', ' Phase Difference[°] ', ' Warning']
for c in range(len(columns)):
    print(c, ': ', columns[c])

```

```

0 : Time[date hh:mm:ss]
1 : Elapsed Time [hh:mm:ss:ms]
2 : Normalized s 1
3 : Normalized s 2
4 : Normalized s 3
5 : S 0 [mW]
6 : S 1 [mW]
7 : S 2 [mW]
8 : S 3 [mW]
9 : Azimuth[°]
10 : Ellipticity[°]
11 : DOP[%]
12 : DOCP[%]
13 : DOLP[%]
14 : Power[mW]
15 : Pol Power[mW]
16 : Unpol Power[mW]
17 : Power[dBm]
18 : Pol Power[dBm]
19 : Unpol Power[dBm]
20 : Power-Split-Ratio
21 : Phase Difference[°]
22 : Warning

```

3 Analyse der Messdaten

3.1 Fehler (Warning)

```
[7]: warning = pd.read_csv(filename, skiprows=skip, usecols=[columns[22]], sep=sep)
```

```
[8]: warning.info()
```

```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 7092298 entries, 0 to 7092297
Data columns (total 1 columns):
#   Column      Dtype
---  -
0    Warning    float64
dtypes: float64(1)

```

memory usage: 54.1 MB

```
[9]: warning.isnull().sum()
```

```
[9]: Warning      7092298  
     dtype: int64
```

3.2 Zeitwerte (Time, Elapsed Time)

```
[10]: time = pd.read_csv(filename, skiprows=skip, usecols=[columns[0], columns[1]],  
      ↪ sep=sep)
```

```
[11]: time.info()
```

```
<class 'pandas.core.frame.DataFrame'>  
RangeIndex: 7092298 entries, 0 to 7092297  
Data columns (total 2 columns):  
 #   Column                                Dtype  
---  ---  
 0   Time[date hh:mm:ss]                  object  
 1   Elapsed Time [hh:mm:ss:ms]           object  
dtypes: object(2)  
memory usage: 108.2+ MB
```

```
[12]: time.isnull().sum()
```

```
[12]: Time[date hh:mm:ss]                0  
     Elapsed Time [hh:mm:ss:ms]         0  
     dtype: int64
```

```
[13]: time[columns[0]] = pd.to_datetime(time[columns[0]])  
     time['time_difference'] = time[columns[0]].diff()  
     time['time_frequency'] = 1 / time['time_difference'].dt.total_seconds()  
     time['time_difference']
```

```
[13]: 0                                NaT  
     1      0 days 00:00:00.060000  
     2      0 days 00:00:00.050000  
     3      0 days 00:00:00.050000  
     4      0 days 00:00:00.050000  
     ...  
7092293  0 days 00:00:05.160000  
7092294  0 days 00:00:00.040000  
7092295  0 days 00:00:00.050000  
7092296  0 days 00:00:02.590000  
7092297  0 days 00:00:00.470000  
Name: time_difference, Length: 7092298, dtype: timedelta64[ns]
```

```
[14]: time[columns[1]] = time[columns[1]].apply(fast_parse_elapsed)
time['elapsed_time_difference'] = time[columns[1]].diff()
time['elapsed_time_frequency'] = 1 / time['elapsed_time_difference'].dt.
    ↳total_seconds()
time['elapsed_time_difference']
```

```
[14]: 0                                     NaT
1      0 days 00:00:00.060000
2      0 days 00:00:00.048000
3      0 days 00:00:00.056000
4      0 days 00:00:00.052000
...
7092293 0 days 00:00:05.155000
7092294 0 days 00:00:00.047000
7092295 0 days 00:00:00.048000
7092296 0 days 00:00:02.585000
7092297 0 days 00:00:00.477000
Name: elapsed_time_difference, Length: 7092298, dtype: timedelta64[ns]
```

```
[15]: t = PrettyTable([' ', 'Time', 'Elapsed Time'])
t.add_row(['Max', time['time_difference'].max(),
    ↳time['elapsed_time_difference'].max()])
t.add_row(['Min', time['time_difference'].min(),
    ↳time['elapsed_time_difference'].min()])
t.add_row(['Mean', time['time_difference'].mean(),
    ↳time['elapsed_time_difference'].mean()])
t.add_row(['Std', time['time_difference'].std(),
    ↳time['elapsed_time_difference'].std()])
t.add_row(['Most', time['time_difference'].value_counts(dropna=True).idxmax(),
    ↳time['elapsed_time_difference'].value_counts(dropna=True).idxmax()])
t.add_row(['Mean Frequency', time['time_frequency'].mean(),
    ↳time['elapsed_time_frequency'].mean()])

t
```

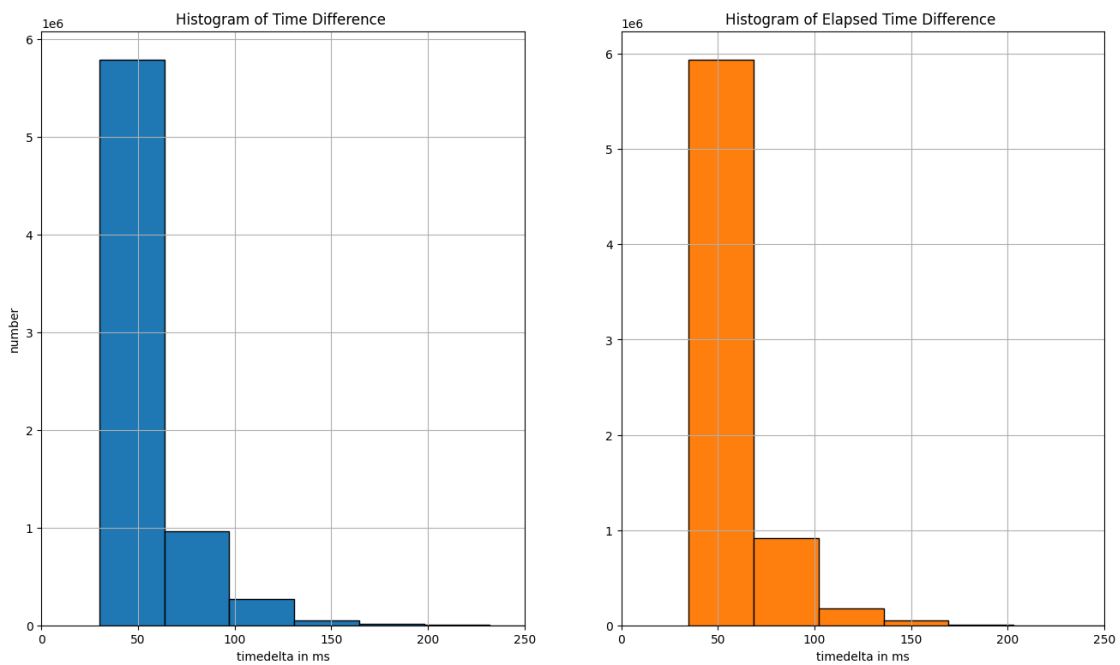
```
[15]: +-----+-----+-----+
|          |          Time          |          Elapsed Time          |
+-----+-----+-----+
|      Max      | 0 days 00:00:08.440000 | 0 days 00:00:08.433000 |
|      Min      | 0 days 00:00:00.030000 | 0 days 00:00:00.035000 |
|      Mean      | 0 days 00:00:00.059365613 | 0 days 00:00:00.059365613 |
|      Std       | 0 days 00:00:00.043810670 | 0 days 00:00:00.043698223 |
|      Most      | 0 days 00:00:00.050000 | 0 days 00:00:00.051000 |
| Mean Frequency | 18.0609712139089      | 17.991727639966633      |
+-----+-----+-----+
```

```
[16]: time_difference = time['time_difference'].dt.total_seconds() * 1000
elapsed_time_difference = time['elapsed_time_difference'].dt.total_seconds() * 1000

plt.figure(figsize = (16,9))
plt.subplot(1, 2, 1)
plt.hist(time_difference, bins=250, color='tab:blue', edgecolor='black')
plt.xlim([0, 250])
plt.grid()
plt.xlabel('timedelta in ms')
plt.ylabel('number')
plt.title('Histogram of Time Difference ')

plt.subplot(1, 2, 2)
plt.hist(elapsed_time_difference, bins=250, color='tab:orange', edgecolor='black')
plt.xlim([0, 250])
plt.grid()
plt.xlabel('timedelta in ms')
plt.title('Histogram of Elapsed Time Difference ')

plt.show()
```



```
[17]: plt.figure(figsize = (16,9))
plt.subplot(1, 2, 1)
```

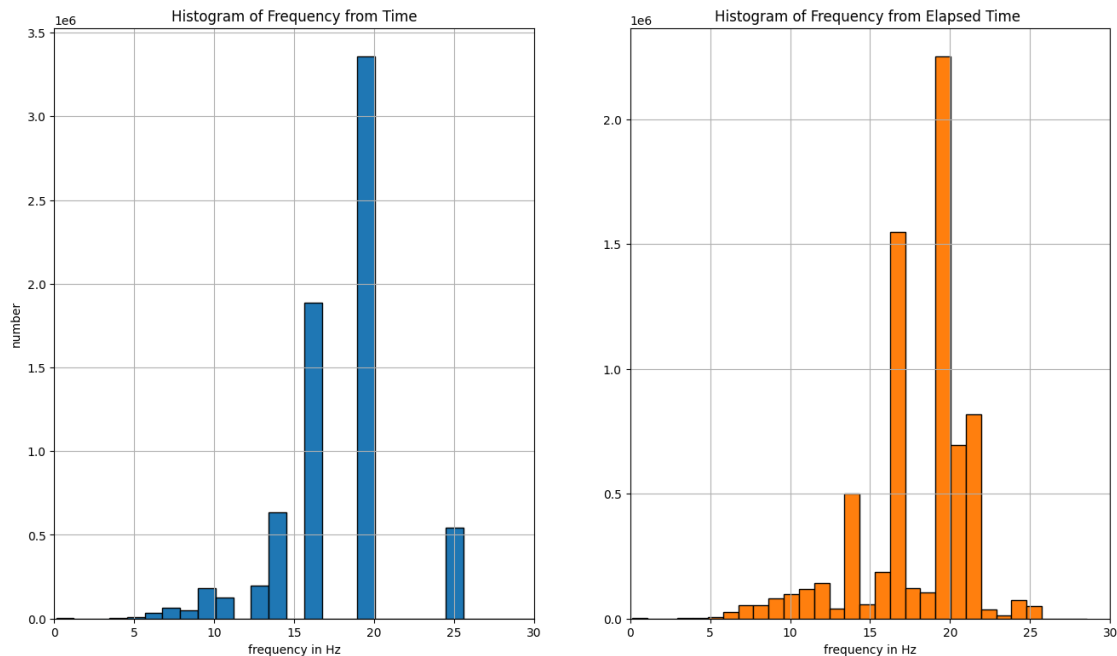
```

plt.hist(time['time_frequency'], bins=30, color='tab:blue', edgecolor='black')
plt.xlim([0, 30])
plt.grid()
plt.xlabel('frequency in Hz')
plt.ylabel('number')
plt.title('Histogram of Frequency from Time')

plt.subplot(1, 2, 2)
plt.hist(time['elapsed_time_frequency'], bins=30, color='tab:orange',
        edgecolor='black')
plt.xlim([0, 30])
plt.grid()
plt.xlabel('frequency in Hz')
plt.title('Histogram of Frequency from Elapsed Time ')

plt.show()

```



3.3 Polarisationsgrade (DOP, DOCP, DOLP)

```

[18]: degree = pd.read_csv(filename, skiprows=skip, usecols=[columns[0], columns[11],
        columns[12], columns[13]], sep=sep)

```

```

[19]: degree[columns[0]] = pd.to_datetime(degree[columns[0]])
degree.set_index(columns[0], inplace=True)

```



```
[20]: degree.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 7092298 entries, 2024-11-29 00:26:44.470000 to 2024-12-03
21:24:03.030000
Data columns (total 3 columns):
 #   Column      Dtype
---  -
 0   DOP[%]      float64
 1   DOCP[%]     float64
 2   DOLP[%]     float64
dtypes: float64(3)
memory usage: 216.4 MB
```

```
[21]: degree.isnull().sum()
```

```
[21]: DOP[%]      0
      DOCP[%]   0
      DOLP[%]   0
      dtype: int64
```

```
[22]: degree.describe()
```

```
[22]:
```

	DOP [%]	DOCP [%]	DOLP [%]
count	7.092298e+06	7.092298e+06	7.092298e+06
mean	9.968967e+01	4.793726e+01	8.010235e+01
std	4.684479e+00	2.783318e+01	2.170073e+01
min	-3.703300e+03	0.000000e+00	5.000000e-02
25%	9.737000e+01	2.435000e+01	6.955000e+01
50%	9.950000e+01	4.698000e+01	8.768000e+01
75%	1.021500e+02	7.092000e+01	9.591000e+01
max	2.895590e+03	9.977200e+02	3.700080e+03

```
[23]: plt.figure(figsize = (16,9))
      plt.subplot(1, 3, 1)
      plt.hist(degree[columns[11]], bins=200, color='tab:blue', edgecolor='black')
      plt.xlim([0, 200])
      plt.grid()
      plt.xlabel(columns[11])
      plt.ylabel('number')
      plt.title('Histogram of DOP[%] ')

      plt.subplot(1, 3, 2)
      plt.hist(degree[columns[12]], bins=200, color='tab:orange', edgecolor='black')
      plt.xlim([0, 200])
      plt.grid()
      plt.xlabel(columns[12])
      plt.title('Histogram of DOCP[%] ')

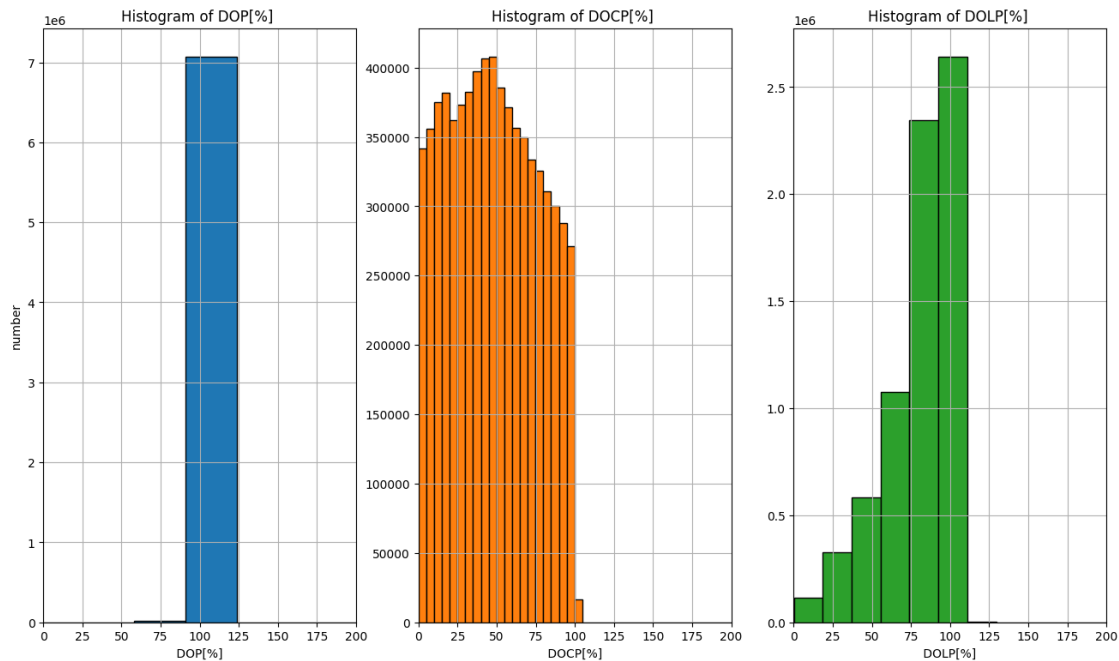
```

```

plt.subplot(1, 3, 3)
plt.hist(degree[columns[13]], bins=200, color='tab:green', edgecolor='black')
plt.xlim([0, 200])
plt.grid()
plt.xlabel(columns[13])
plt.title('Histogram of DOLP[%] ')

plt.show()

```



```

[24]: one_second = datetime.timedelta(seconds=1)
      one_minute = datetime.timedelta(minutes=1)
      one_hour = datetime.timedelta(hours=1)
      one_day = datetime.timedelta(days=1)

      start_time = datetime.datetime.strptime(str(degree.index[0]), '%Y-%m-%d %H:%M:
      ↪%S.%f')
      end_time_second = start_time + one_second
      end_time_minute = start_time + one_minute
      end_time_hour = start_time + one_hour
      end_time_day = start_time + one_day

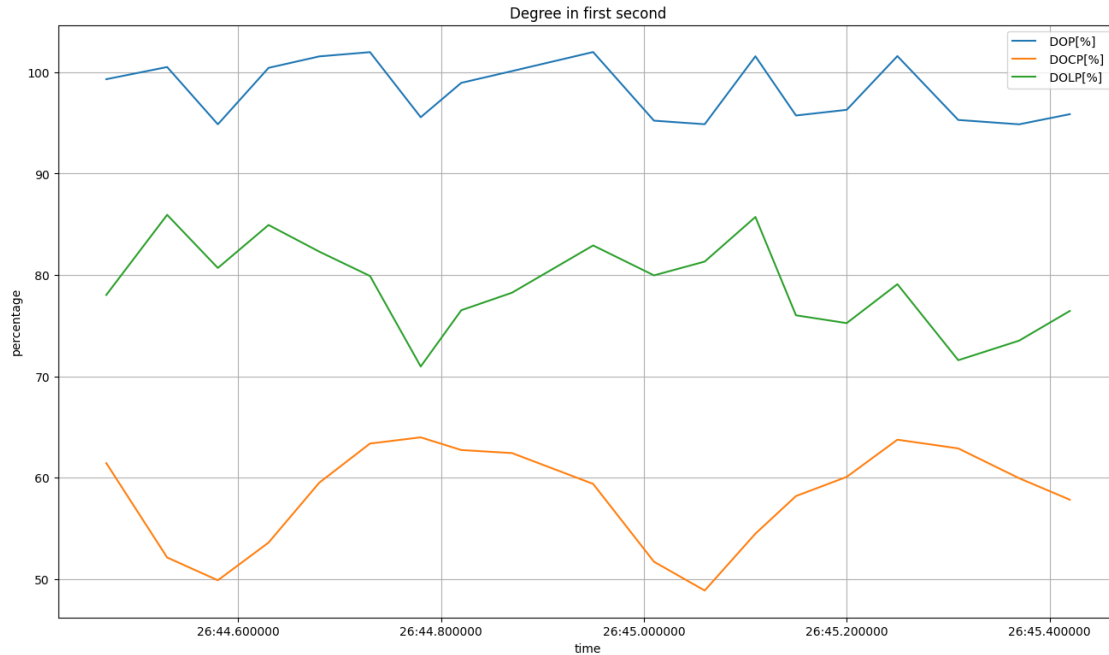
[25]: first_second = degree.loc[(degree.index >= start_time) & (degree.index <
      ↪end_time_second)]
      first_second

```

```
[25]:
```

	DOP [%]	DOCP [%]	DOLP [%]
Time[date hh:mm:ss]			
2024-11-29 00:26:44.470	99.31	61.44	78.03
2024-11-29 00:26:44.530	100.51	52.13	85.93
2024-11-29 00:26:44.580	94.86	49.88	80.69
2024-11-29 00:26:44.630	100.43	53.60	84.93
2024-11-29 00:26:44.680	101.56	59.51	82.30
2024-11-29 00:26:44.730	101.98	63.37	79.90
2024-11-29 00:26:44.780	95.56	63.98	70.97
2024-11-29 00:26:44.820	98.95	62.73	76.52
2024-11-29 00:26:44.870	100.11	62.43	78.25
2024-11-29 00:26:44.950	101.99	59.39	82.91
2024-11-29 00:26:45.010	95.22	51.71	79.96
2024-11-29 00:26:45.060	94.87	48.87	81.32
2024-11-29 00:26:45.110	101.57	54.48	85.72
2024-11-29 00:26:45.150	95.73	58.19	76.02
2024-11-29 00:26:45.200	96.29	60.08	75.25
2024-11-29 00:26:45.250	101.59	63.75	79.09
2024-11-29 00:26:45.310	95.29	62.89	71.59
2024-11-29 00:26:45.370	94.86	59.95	73.52
2024-11-29 00:26:45.420	95.86	57.83	76.45

```
[26]: plt.figure(figsize = (16,9))
plt.plot(first_second.index, first_second[columns[11]], label = columns[11])
plt.plot(first_second.index, first_second[columns[12]], label = columns[12])
plt.plot(first_second.index, first_second[columns[13]], label = columns[13])
plt.grid()
plt.legend(loc = 'best')
plt.title('Degree in first second')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



```
[27]: first_minute = degree.loc[(degree.index >= start_time) & (degree.index <
    ↪end_time_minute)]
first_minute
```

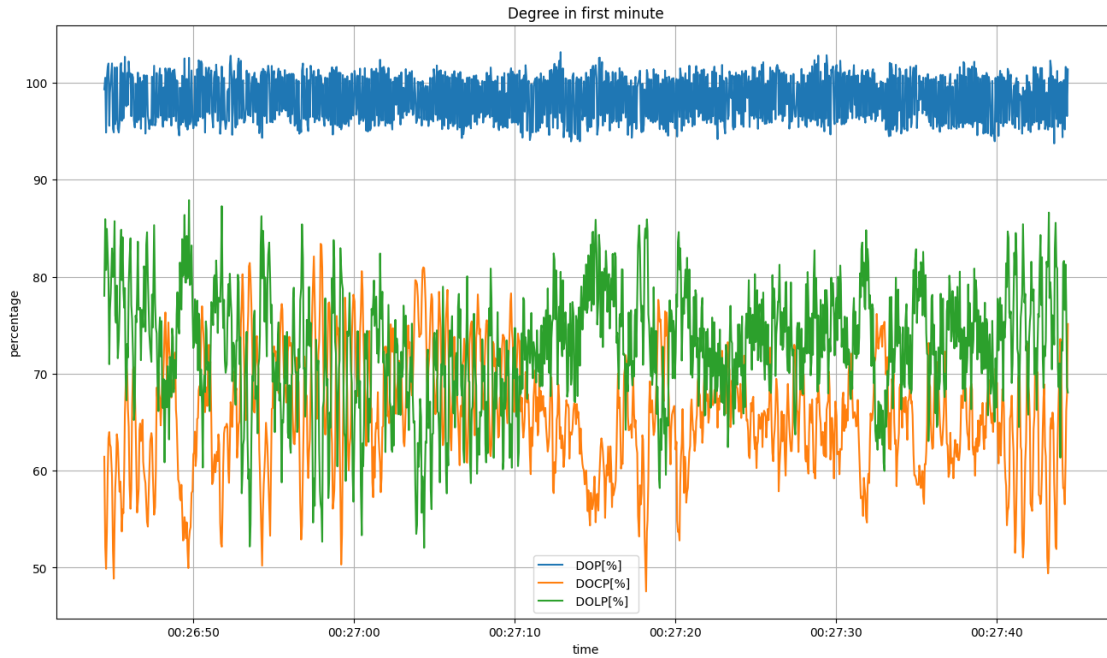
```
[27]:
```

	DOP [%]	DOCP [%]	DOLP [%]
Time[date hh:mm:ss]			
2024-11-29 00:26:44.470	99.31	61.44	78.03
2024-11-29 00:26:44.530	100.51	52.13	85.93
2024-11-29 00:26:44.580	94.86	49.88	80.69
2024-11-29 00:26:44.630	100.43	53.60	84.93
2024-11-29 00:26:44.680	101.56	59.51	82.30
...
2024-11-29 00:27:44.230	95.18	56.54	76.57
2024-11-29 00:27:44.280	101.63	61.04	81.25
2024-11-29 00:27:44.320	101.53	66.18	77.00
2024-11-29 00:27:44.370	96.55	67.93	68.61
2024-11-29 00:27:44.420	101.37	75.12	68.06

[1242 rows x 3 columns]

```
[28]: plt.figure(figsize = (16,9))
plt.plot(first_minute.index, first_minute[columns[11]], label = columns[11])
plt.plot(first_minute.index, first_minute[columns[12]], label = columns[12])
plt.plot(first_minute.index, first_minute[columns[13]], label = columns[13])
plt.grid()
```

```
plt.legend(loc = 'best')
plt.title('Degree in first minute')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



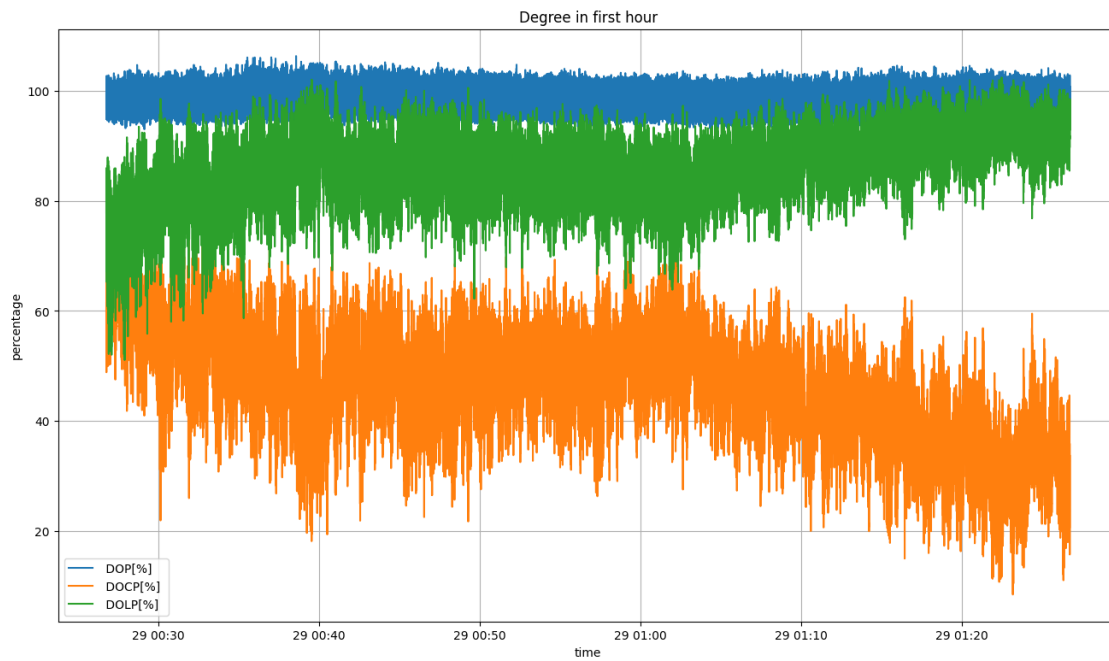
```
[29]: first_hour = degree.loc[(degree.index >= start_time) & (degree.index < end_time_hour)]
first_hour
```

```
[29]:
```

	DOP[%]	DOCP[%]	DOLP[%]
Time[date hh:mm:ss]			
2024-11-29 00:26:44.470	99.31	61.44	78.03
2024-11-29 00:26:44.530	100.51	52.13	85.93
2024-11-29 00:26:44.580	94.86	49.88	80.69
2024-11-29 00:26:44.630	100.43	53.60	84.93
2024-11-29 00:26:44.680	101.56	59.51	82.30
...
2024-11-29 01:26:44.270	97.02	16.86	95.54
2024-11-29 01:26:44.320	100.73	21.51	98.41
2024-11-29 01:26:44.370	94.44	24.55	91.19
2024-11-29 01:26:44.410	102.79	33.64	97.13
2024-11-29 01:26:44.460	98.43	35.79	91.69

```
[74525 rows x 3 columns]
```

```
[30]: plt.figure(figsize = (16,9))
plt.plot(first_hour.index, first_hour[columns[11]], label = columns[11])
plt.plot(first_hour.index, first_hour[columns[12]], label = columns[12])
plt.plot(first_hour.index, first_hour[columns[13]], label = columns[13])
plt.grid()
plt.legend(loc = 'best')
plt.title('Degree in first hour')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



```
[31]: first_day = degree.loc[(degree.index >= start_time) & (degree.index <
    ↪end_time_day)]
first_day
```

```
[31]:
```

Time[date hh:mm:ss]	DOP [%]	DOCP [%]	DOLP [%]
2024-11-29 00:26:44.470	99.31	61.44	78.03
2024-11-29 00:26:44.530	100.51	52.13	85.93
2024-11-29 00:26:44.580	94.86	49.88	80.69
2024-11-29 00:26:44.630	100.43	53.60	84.93
2024-11-29 00:26:44.680	101.56	59.51	82.30
...
2024-11-30 00:26:44.160	98.01	8.74	97.61
2024-11-30 00:26:44.240	105.00	20.62	102.95

```

2024-11-30 00:26:44.310    105.94    11.68    105.29
2024-11-30 00:26:44.370    104.75    14.71    103.71
2024-11-30 00:26:44.420    105.19    11.84    104.52

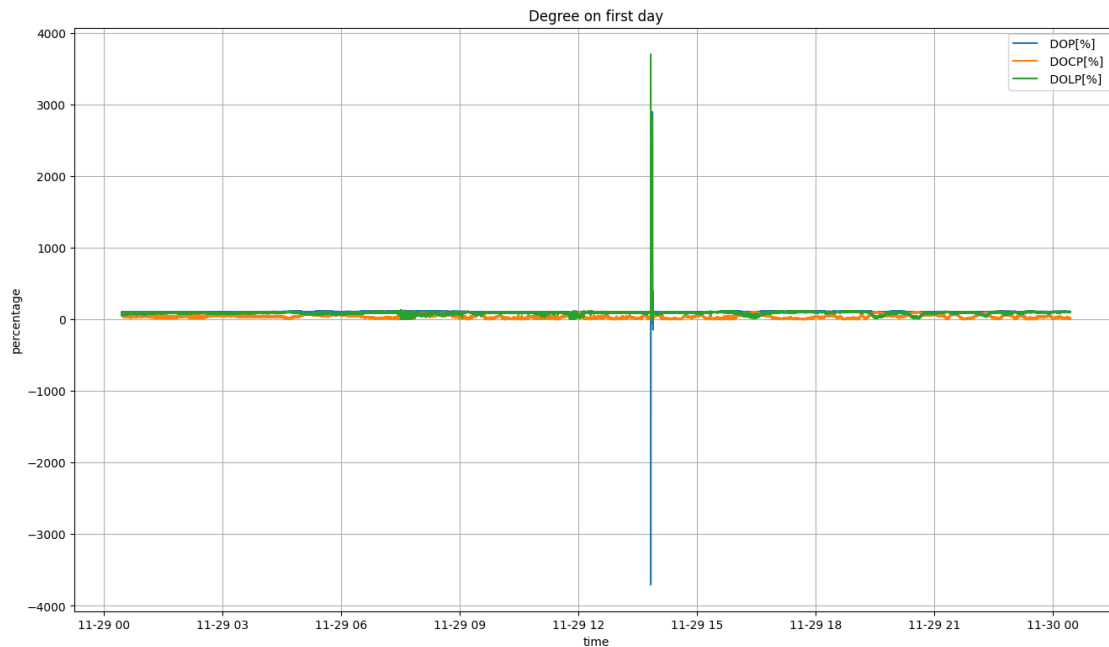
```

[1703970 rows x 3 columns]

```

[32]: plt.figure(figsize = (16,9))
plt.plot(first_day.index, first_day[columns[11]], label = columns[11])
plt.plot(first_day.index, first_day[columns[12]], label = columns[12])
plt.plot(first_day.index, first_day[columns[13]], label = columns[13])
plt.grid()
plt.legend(loc = 'best')
plt.title('Degree on first day')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()

```



```

[33]: degree_seconds_resample = degree.resample('s').mean()
degree_seconds_resample.info()

```

```

<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 421040 entries, 2024-11-29 00:26:44 to 2024-12-03 21:24:03
Freq: s
Data columns (total 3 columns):
 #   Column      Non-Null Count  Dtype
---  -

```

```

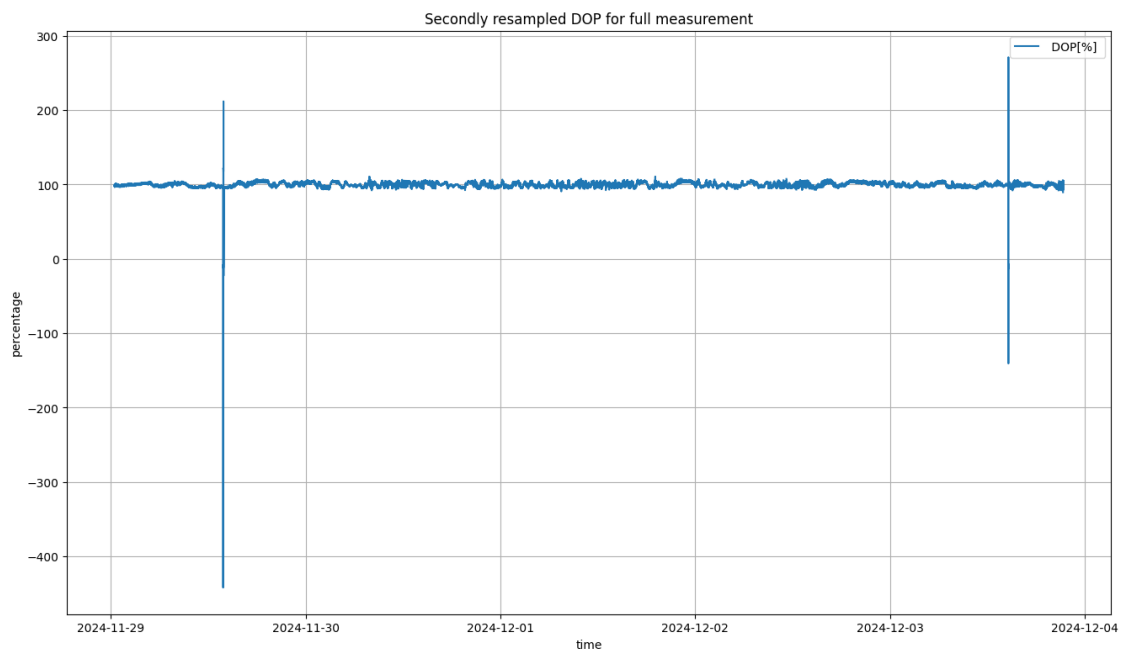
0    DOP[%]    418526 non-null float64
1    DOCP[%]   418526 non-null float64
2    DOLP[%]   418526 non-null float64
dtypes: float64(3)
memory usage: 12.8 MB

```

```

[34]: plt.figure(figsize = (16,9))
plt.plot(degree_seconds_resample.index, degree_seconds_resample[columns[11]],
         label = columns[11])
plt.grid()
plt.legend(loc = 'best')
plt.title('Secondly resampled DOP for full measurement')
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()

```



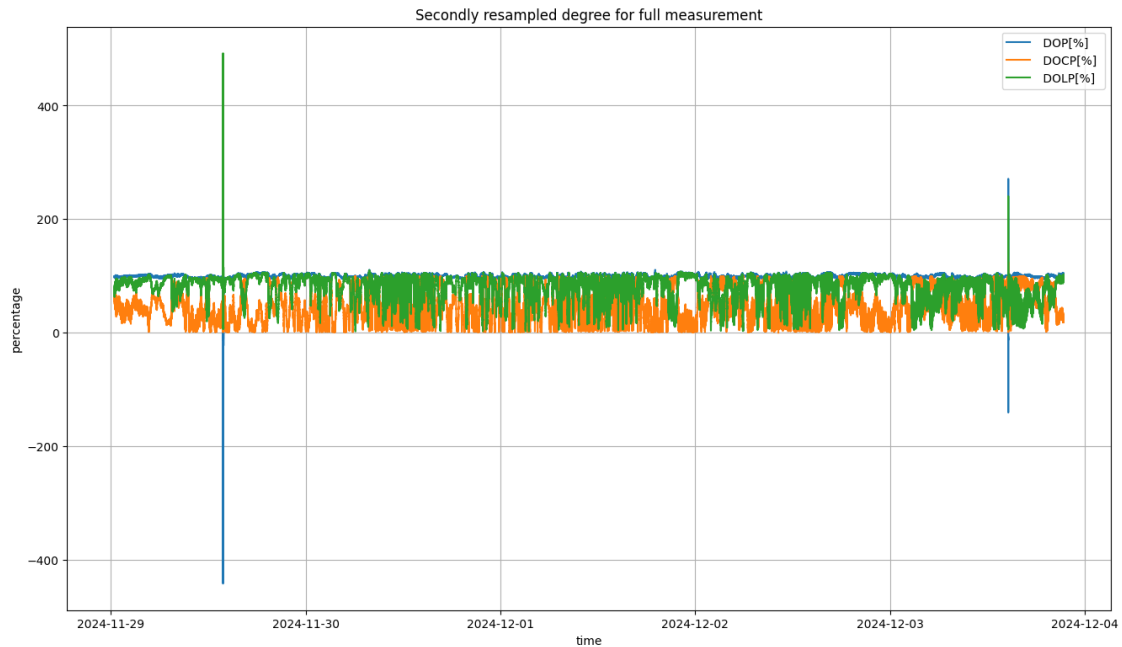
```

[35]: plt.figure(figsize = (16,9))
plt.plot(degree_seconds_resample.index, degree_seconds_resample[columns[11]],
         label = columns[11])
plt.plot(degree_seconds_resample.index, degree_seconds_resample[columns[12]],
         label = columns[12])
plt.plot(degree_seconds_resample.index, degree_seconds_resample[columns[13]],
         label = columns[13])
plt.grid()
plt.legend(loc = 'best')
plt.title('Secondly resampled degree for full measurement')

```



```
plt.xlabel('time')
plt.ylabel('percentage')
plt.show()
```



3.4 Energie (Power, Pol Power, Unipol Power [mW/dBm])

```
[36]: power_mw = pd.read_csv(filename, skiprows=skip, usecols=[columns[0], ↵
↵ columns[14], columns[15], columns[16]], sep=sep)
```

```
[37]: power_mw[columns[0]] = pd.to_datetime(power_mw[columns[0]])
power_mw.set_index(columns[0], inplace=True)
```

```
[38]: power_mw.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 7092298 entries, 2024-11-29 00:26:44.470000 to 2024-12-03
21:24:03.030000
Data columns (total 3 columns):
#   Column          Dtype
---  -
0    Power[mW]       float64
1    Pol Power[mW]   float64
2    Unpol Power[mW] float64
dtypes: float64(3)
memory usage: 216.4 MB
```

```
[39]: power_mw.isnull().sum()
```

```
[39]: Power[mW]          0
      Pol Power[mW]      0
      Unpol Power[mW]    0
      dtype: int64
```

```
[40]: power_mw.describe()
```

```
[40]:
```

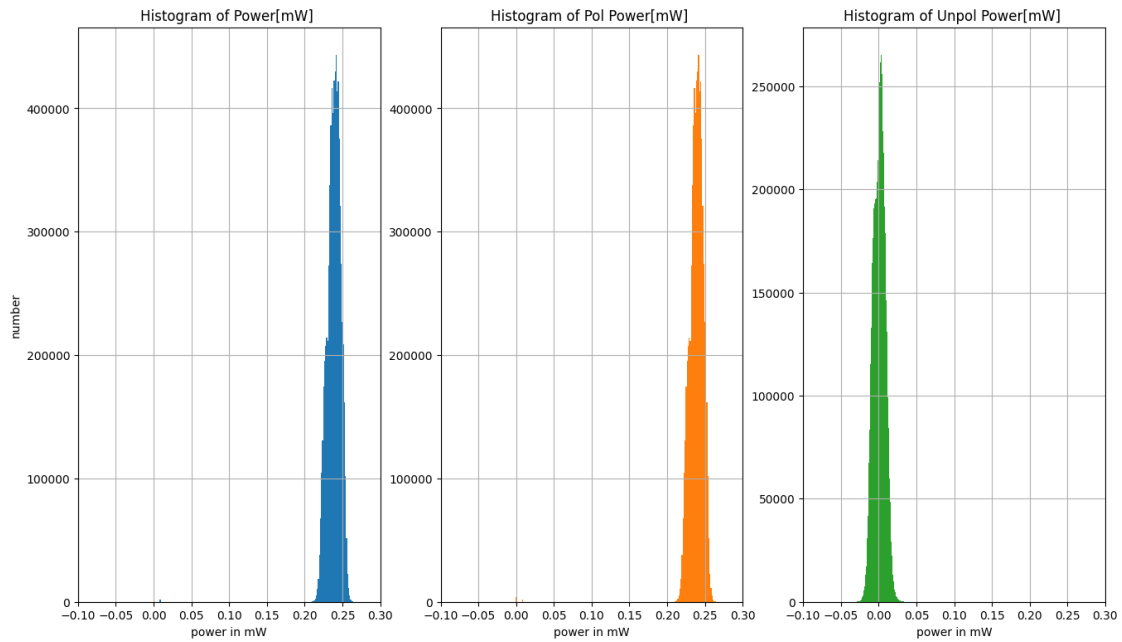
	Power[mW]	Pol Power[mW]	Unpol Power[mW]
count	7.092298e+06	7.092298e+06	7.092298e+06
mean	2.386558e-01	2.378043e-01	8.514209e-04
std	1.068249e-02	7.764705e-03	7.812574e-03
min	-2.843000e-04	1.245000e-06	-7.365000e-02
25%	2.331000e-01	2.350000e-01	-5.019000e-03
50%	2.393000e-01	2.382000e-01	1.185000e-03
75%	2.450000e-01	2.410000e-01	6.408000e-03
max	2.754000e-01	2.882000e-01	7.396000e-02

```
[41]: plt.figure(figsize = (16,9))
      plt.subplot(1, 3, 1)
      plt.hist(power_mw[columns[14]], bins=200, color='tab:blue')
      plt.xlim([-0.1, 0.3])
      plt.grid()
      plt.xlabel('power in mW')
      plt.ylabel('number')
      plt.title('Histogram of Power[mW] ')

      plt.subplot(1, 3, 2)
      plt.hist(power_mw[columns[14]], bins=200, color='tab:orange')
      plt.xlim([-0.1, 0.3])
      plt.grid()
      plt.xlabel('power in mW')
      plt.title('Histogram of Pol Power[mW] ')

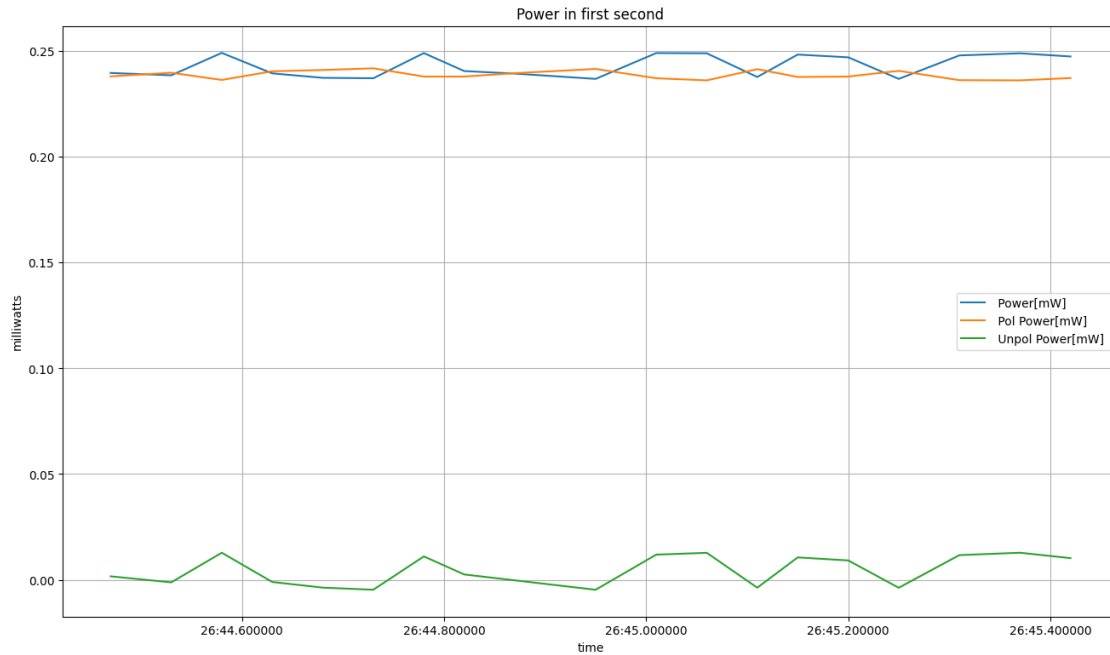
      plt.subplot(1, 3, 3)
      plt.hist(power_mw[' Unpol Power[mW]'], bins=200, color='tab:green')
      plt.xlim([-0.1, 0.3])
      plt.grid()
      plt.xlabel('power in mW')
      plt.title('Histogram of Unpol Power[mW] ')

      plt.show()
```



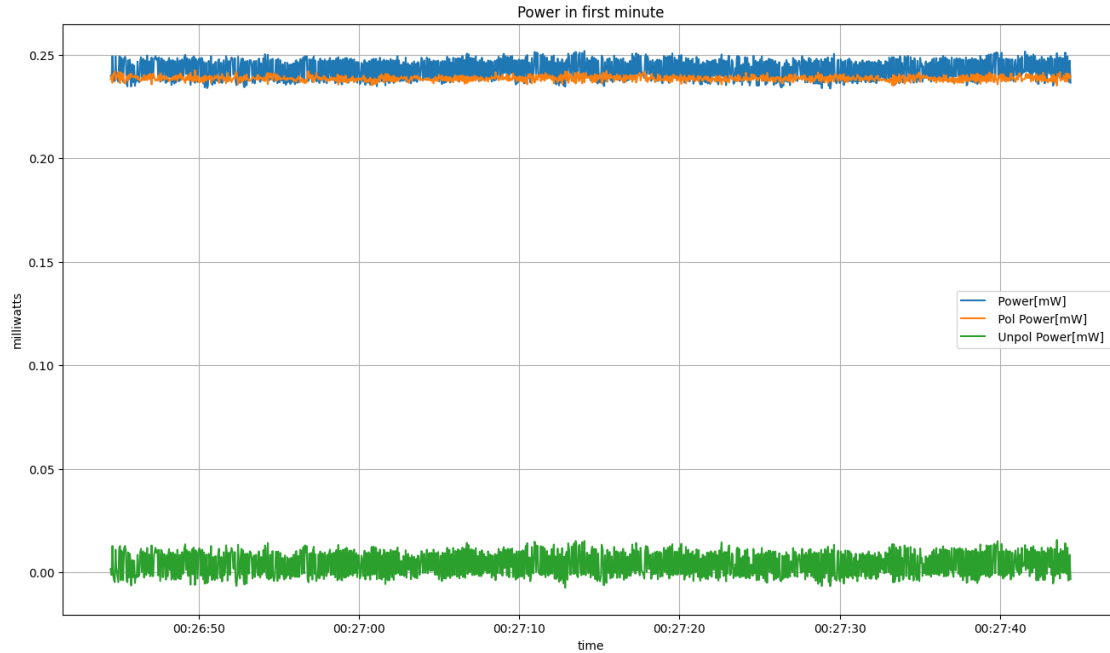
```
[42]: first_second = power_mw.loc[(power_mw.index >= start_time) & (power_mw.index <
    ↪end_time_second)]

plt.figure(figsize = (16,9))
plt.plot(first_second.index, first_second[columns[14]], label = columns[14])
plt.plot(first_second.index, first_second[columns[15]], label = columns[15])
plt.plot(first_second.index, first_second[columns[16]], label = columns[16])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power in first second')
plt.xlabel('time')
plt.ylabel('milliwatts')
plt.show()
```



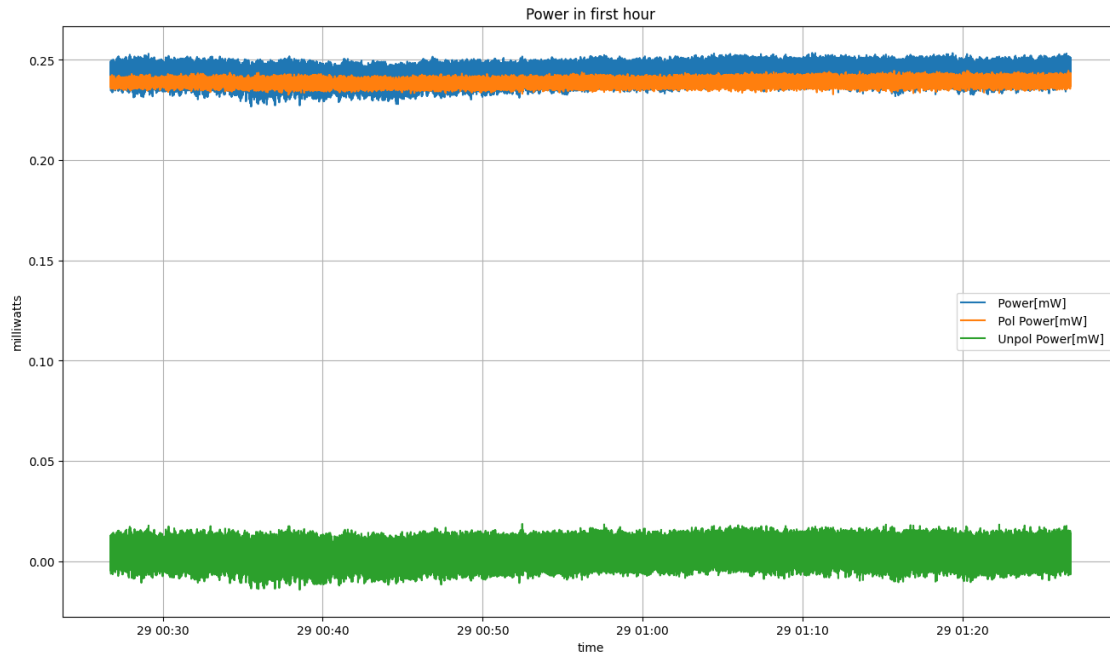
```
[43]: first_minute = power_mw.loc[(power_mw.index >= start_time) & (power_mw.index <
    ↪end_time_minute)]

plt.figure(figsize = (16,9))
plt.plot(first_minute.index, first_minute[columns[14]], label = columns[14])
plt.plot(first_minute.index, first_minute[columns[15]], label = columns[15])
plt.plot(first_minute.index, first_minute[columns[16]], label = columns[16])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power in first minute')
plt.xlabel('time')
plt.ylabel('milliwatts')
plt.show()
```



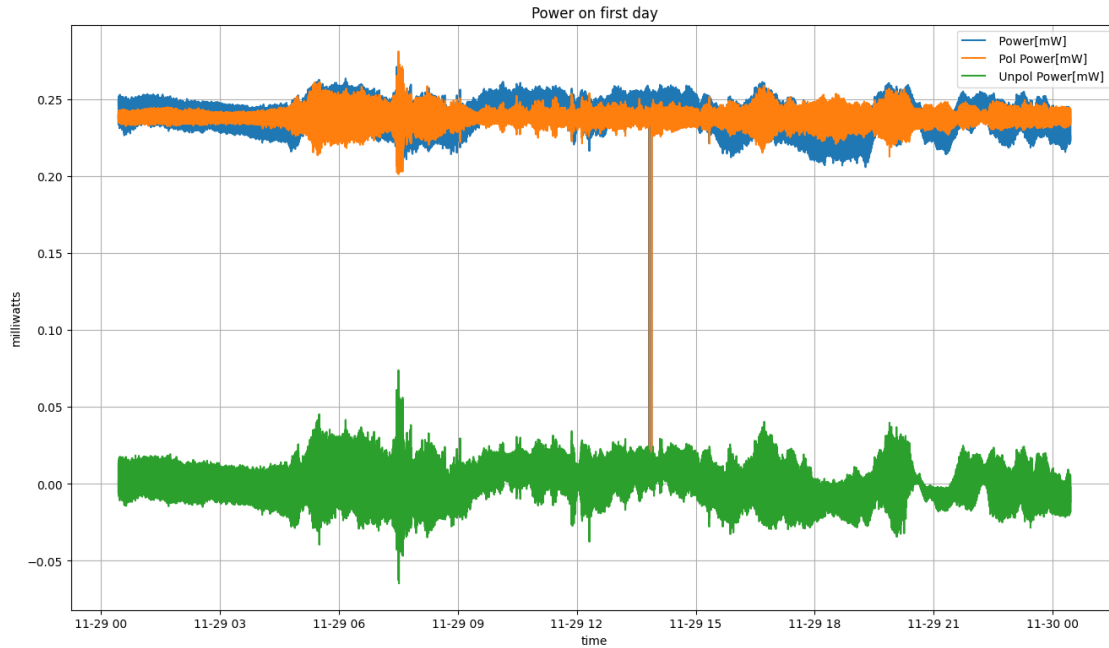
```
[44]: first_hour = power_mw.loc[(power_mw.index >= start_time) & (power_mw.index <
    ↪end_time_hour)]

plt.figure(figsize = (16,9))
plt.plot(first_hour.index, first_hour[columns[14]], label = columns[14])
plt.plot(first_hour.index, first_hour[columns[15]], label = columns[15])
plt.plot(first_hour.index, first_hour[columns[16]], label = columns[16])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power in first hour')
plt.xlabel('time')
plt.ylabel('milliwatts')
plt.show()
```



```
[45]: first_day = power_mw.loc[(power_mw.index >= start_time) & (power_mw.index <
    ↪end_time_day)]

plt.figure(figsize = (16,9))
plt.plot(first_day.index, first_day[columns[14]], label = columns[14])
plt.plot(first_day.index, first_day[columns[15]], label = columns[15])
plt.plot(first_day.index, first_day[columns[16]], label = columns[16])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power on first day')
plt.xlabel('time')
plt.ylabel('milliwatts')
plt.show()
```

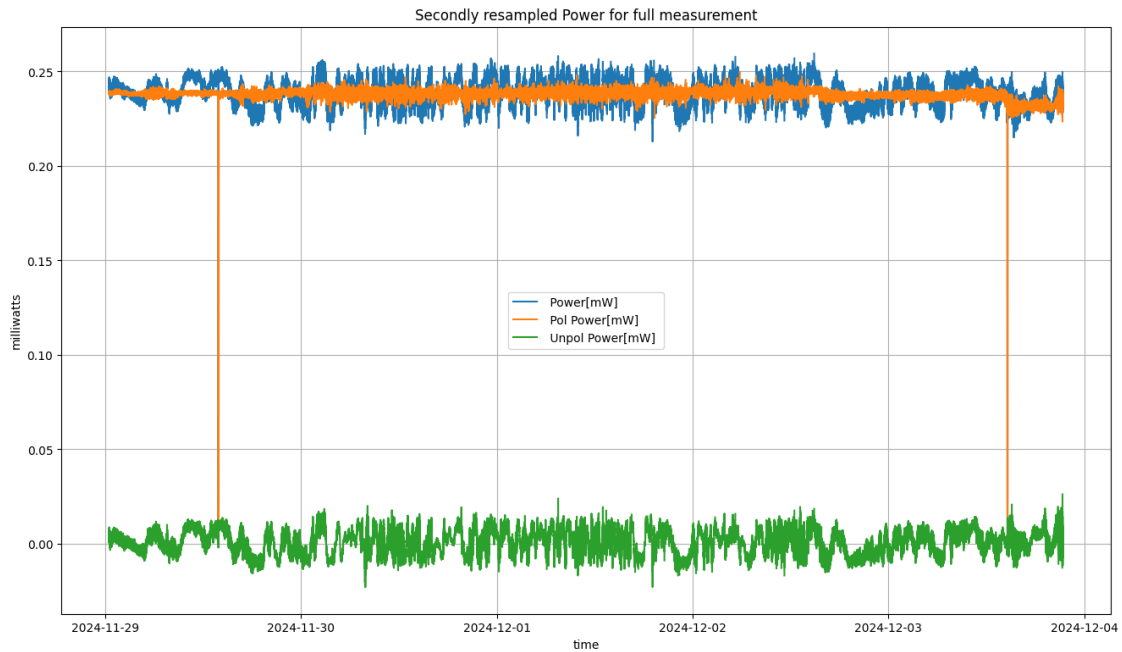


```
[46]: power_mw_seconds_resample = power_mw.resample('s').mean()
power_mw_seconds_resample.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 421040 entries, 2024-11-29 00:26:44 to 2024-12-03 21:24:03
Freq: s
Data columns (total 3 columns):
#   Column                Non-Null Count  Dtype
---  -
0   Power[mW]             418526 non-null float64
1   Pol Power[mW]         418526 non-null float64
2   Unpol Power[mW]       418526 non-null float64
dtypes: float64(3)
memory usage: 12.8 MB
```

```
[47]: plt.figure(figsize = (16,9))
plt.plot(power_mw_seconds_resample.index,
↳ power_mw_seconds_resample[columns[14]], label = columns[14])
plt.plot(power_mw_seconds_resample.index,
↳ power_mw_seconds_resample[columns[15]], label = columns[15])
plt.plot(power_mw_seconds_resample.index,
↳ power_mw_seconds_resample[columns[16]], label = columns[16])
plt.grid()
plt.legend(loc = 'best')
plt.title('Secondly resampled Power for full measurement')
plt.xlabel('time')
```

```
plt.ylabel('milliwatts')
plt.show()
```



```
[48]: power_dbm = pd.read_csv(filename, skiprows=skip, usecols=[columns[0],
↳ columns[17], columns[18], columns[19]], sep=sep)
```

```
[49]: power_dbm[columns[0]] = pd.to_datetime(power_dbm[columns[0]])
power_dbm.set_index(columns[0], inplace=True)
```

```
[50]: power_dbm.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 7092298 entries, 2024-11-29 00:26:44.470000 to 2024-12-03
21:24:03.030000
Data columns (total 3 columns):
#   Column          Dtype
---  -
0    Power[dBm]      float64
1    Pol Power[dBm]   float64
2    Unpol Power[dBm] float64
dtypes: float64(3)
memory usage: 216.4 MB
```

```
[51]: power_dbm.isnull().sum()
```



```
[51]: Power[dBm]          0
      Pol Power[dBm]      0
      Unpol Power[dBm]    0
      dtype: int64
```

```
[52]: power_dbm.describe()
```

```
[52]:
```

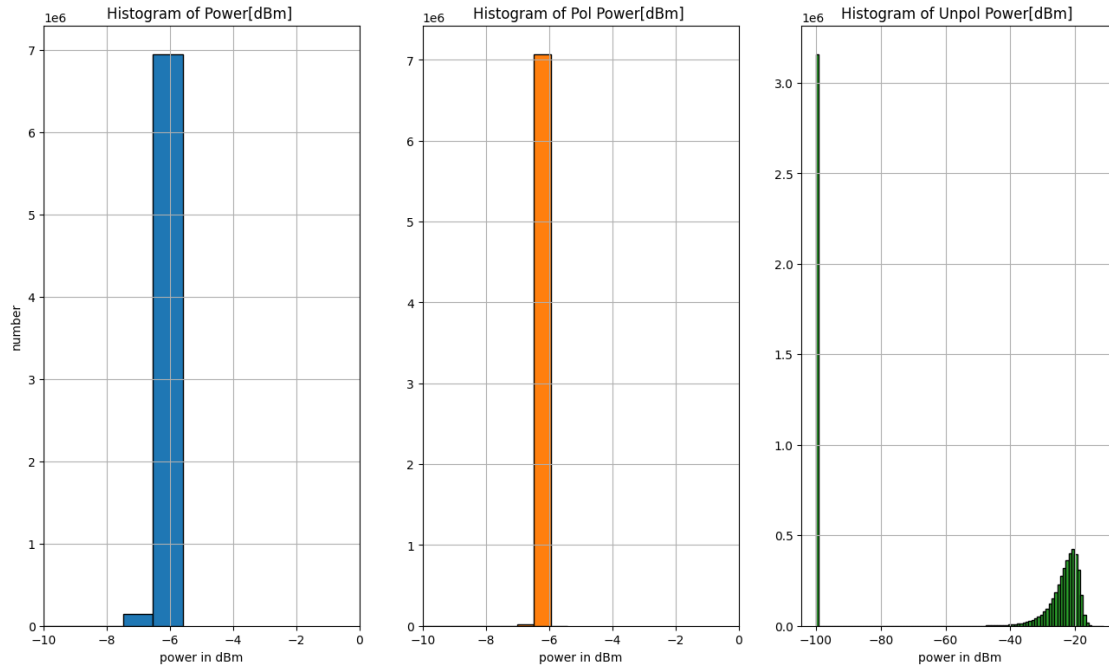
	Power[dBm]	Pol Power[dBm]	Unpol Power[dBm]
count	7.092298e+06	7.092298e+06	7.092298e+06
mean	-6.275016e+00	-6.260080e+00	-5.751649e+01
std	2.178382e+00	9.656586e-01	3.821717e+01
min	-9.999000e+01	-5.904900e+01	-9.999000e+01
25%	-6.324000e+00	-6.289000e+00	-9.999000e+01
50%	-6.210000e+00	-6.230000e+00	-2.926400e+01
75%	-6.108000e+00	-6.181000e+00	-2.193300e+01
max	-5.601000e+00	-5.403000e+00	-1.131000e+01

```
[53]: plt.figure(figsize = (16,9))
      plt.subplot(1, 3, 1)
      plt.hist(power_dbm[columns[17]], bins=100, color='tab:blue', edgecolor='black')
      plt.xlim([-10, 0])
      plt.grid()
      plt.xlabel('power in dBm')
      plt.ylabel('number')
      plt.title('Histogram of Power[dBm] ')

      plt.subplot(1, 3, 2)
      plt.hist(power_dbm[columns[18]], bins=100, color='tab:orange',
               edgecolor='black')
      plt.xlim([-10, 0])
      plt.grid()
      plt.xlabel('power in dBm')
      plt.title('Histogram of Pol Power[dBm] ')

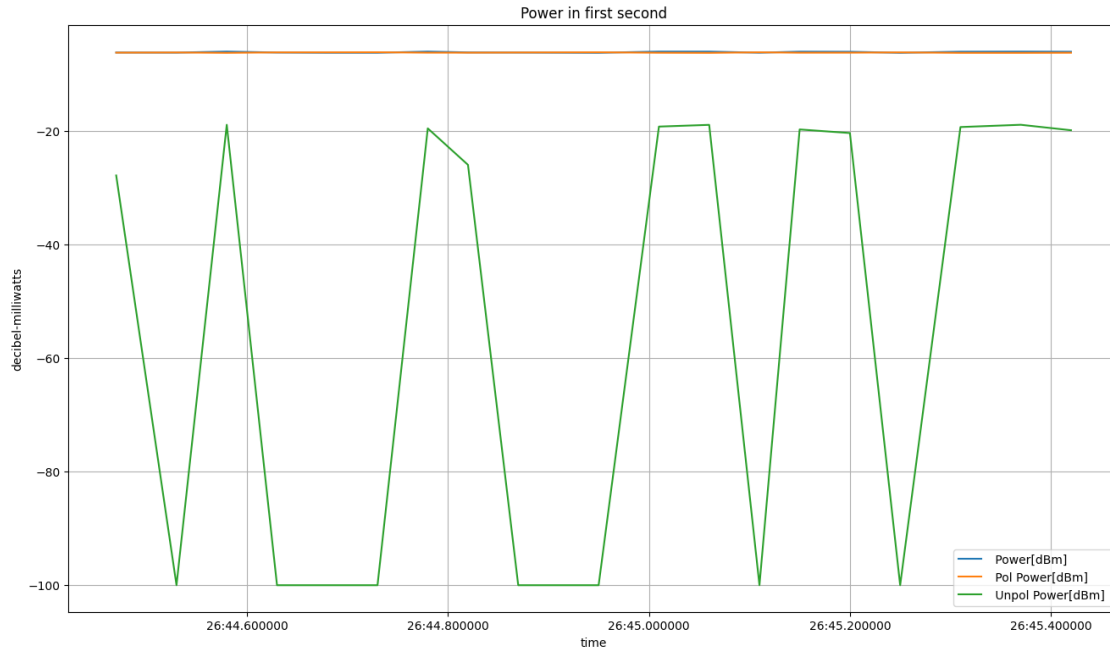
      plt.subplot(1, 3, 3)
      plt.hist(power_dbm[columns[19]], bins=100, color='tab:green', edgecolor='black')
      plt.grid()
      plt.xlabel('power in dBm')
      plt.title('Histogram of Unpol Power[dBm] ')

      plt.show()
```



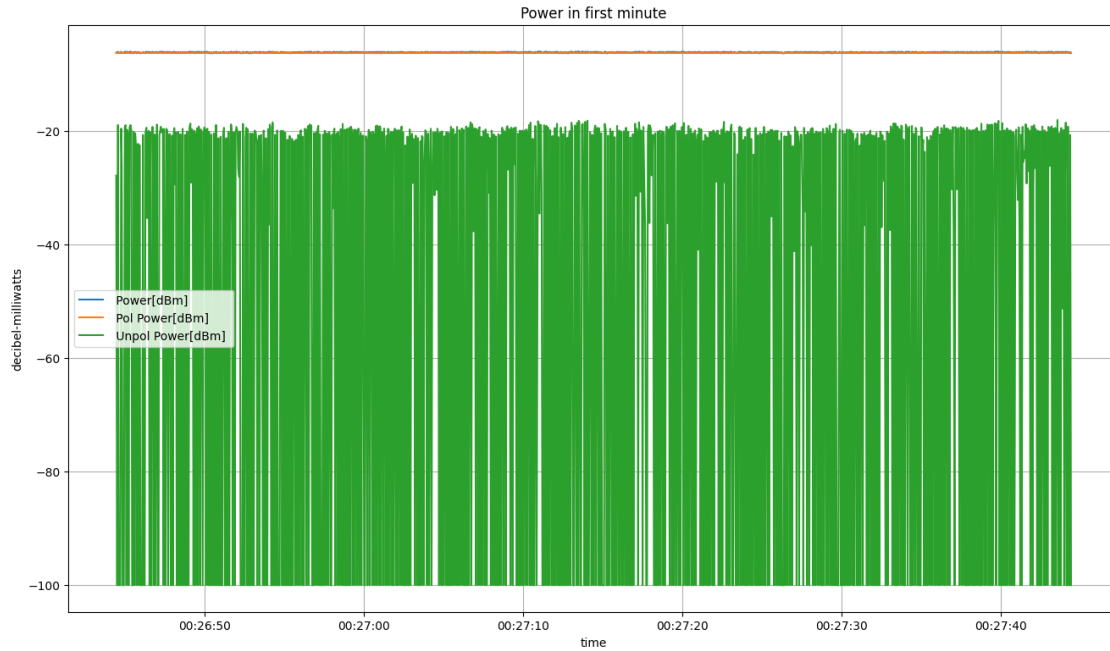
```
[54]: first_second = power_dbm.loc[(power_dbm.index >= start_time) & (power_dbm.index
    ↪ < end_time_second)]

plt.figure(figsize = (16,9))
plt.plot(first_second.index, first_second[columns[17]], label = columns[17])
plt.plot(first_second.index, first_second[columns[18]], label = columns[18])
plt.plot(first_second.index, first_second[columns[19]], label = columns[19])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power in first second')
plt.xlabel('time')
plt.ylabel('decibel-milliwatts')
plt.show()
```



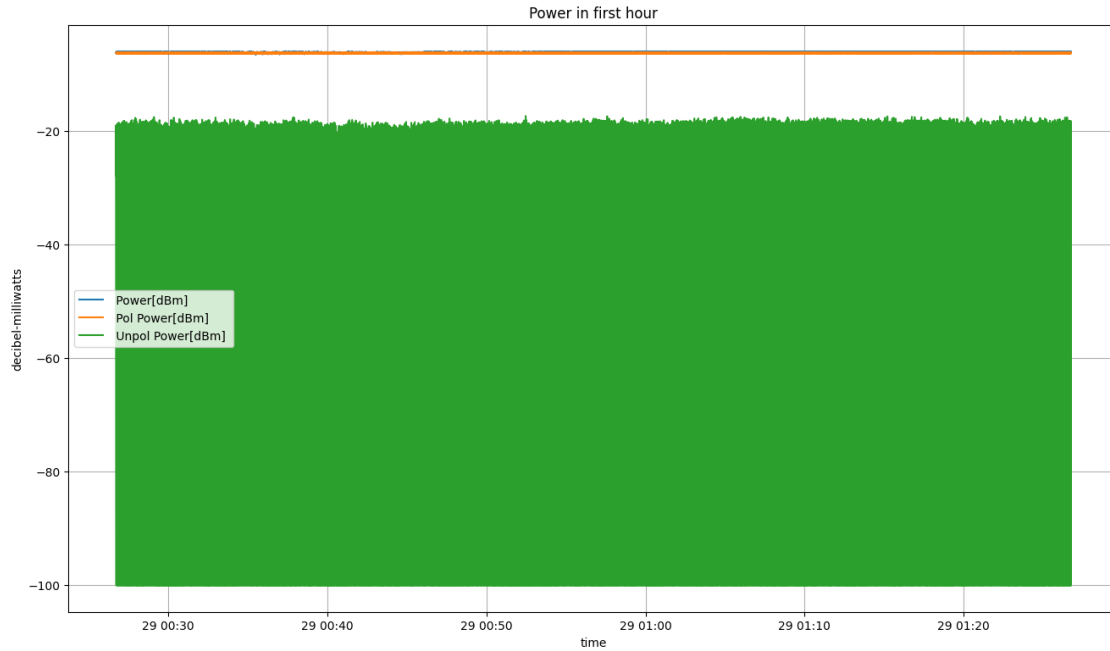
```
[55]: first_minute = power_dbm.loc[(power_dbm.index >= start_time) & (power_dbm.index
    ↪ < end_time_minute)]

plt.figure(figsize = (16,9))
plt.plot(first_minute.index, first_minute[columns[17]], label = columns[17])
plt.plot(first_minute.index, first_minute[columns[18]], label = columns[18])
plt.plot(first_minute.index, first_minute[columns[19]], label = columns[19])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power in first minute')
plt.xlabel('time')
plt.ylabel('decibel-milliwatts')
plt.show()
```



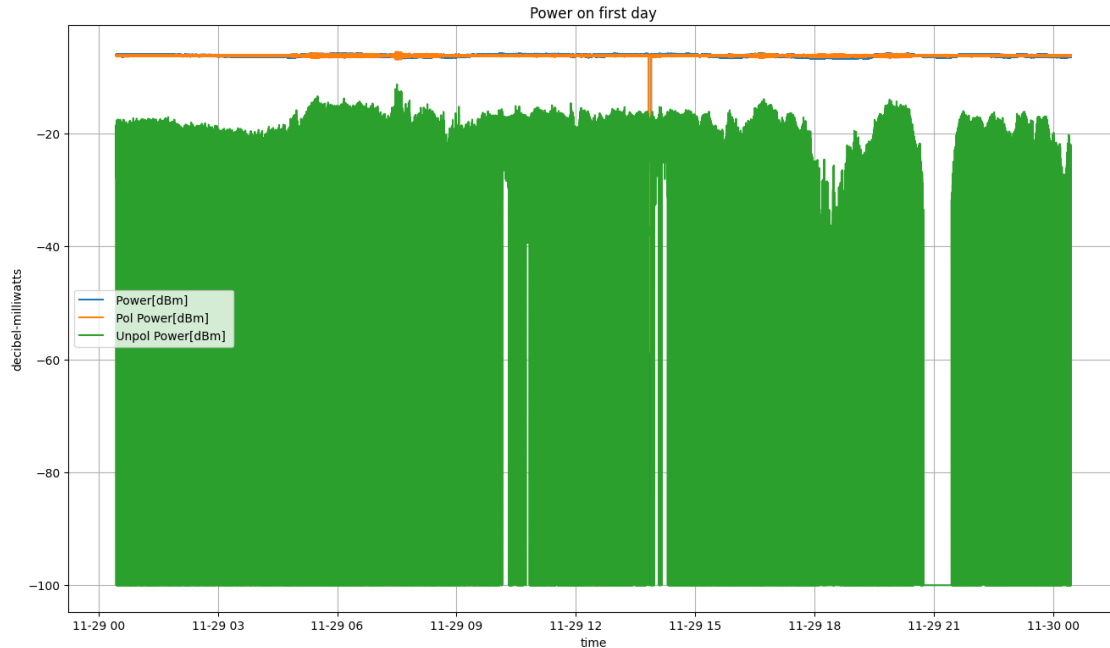
```
[56]: first_hour = power_dbm.loc[(power_dbm.index >= start_time) & (power_dbm.index <
    ↪end_time_hour)]

plt.figure(figsize = (16,9))
plt.plot(first_hour.index, first_hour[columns[17]], label = columns[17])
plt.plot(first_hour.index, first_hour[columns[18]], label = columns[18])
plt.plot(first_hour.index, first_hour[columns[19]], label = columns[19])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power in first hour')
plt.xlabel('time')
plt.ylabel('decibel-milliwatts')
plt.show()
```



```
[57]: first_day = power_dbm.loc[(power_dbm.index >= start_time) & (power_dbm.index <
    ↪end_time_day)]

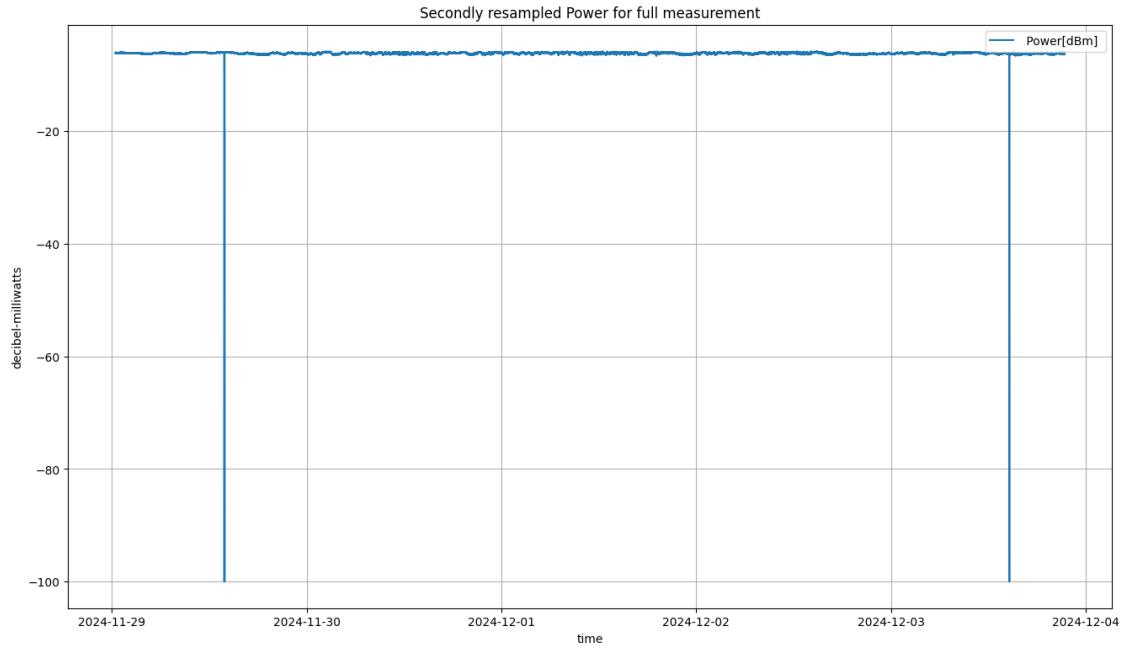
plt.figure(figsize = (16,9))
plt.plot(first_day.index, first_day[columns[17]], label = columns[17])
plt.plot(first_day.index, first_day[columns[18]], label = columns[18])
plt.plot(first_day.index, first_day[columns[19]], label = columns[19])
plt.grid()
plt.legend(loc = 'best')
plt.title('Power on first day')
plt.xlabel('time')
plt.ylabel('decibel-milliwatts')
plt.show()
```



```
[58]: power_dbm_seconds_resample = power_dbm.resample('s').mean()
power_dbm_seconds_resample.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 421040 entries, 2024-11-29 00:26:44 to 2024-12-03 21:24:03
Freq: s
Data columns (total 3 columns):
#   Column                Non-Null Count  Dtype
---  -
0   Power[dBm]            418526 non-null float64
1   Pol Power[dBm]        418526 non-null float64
2   Unpol Power[dBm]      418526 non-null float64
dtypes: float64(3)
memory usage: 12.8 MB
```

```
[59]: plt.figure(figsize = (16,9))
plt.plot(power_dbm_seconds_resample.index,
↳ power_dbm_seconds_resample[columns[17]], label = columns[17])
plt.grid()
plt.legend(loc = 'best')
plt.title('Secondly resampled Power for full measurement')
plt.xlabel('time')
plt.ylabel('decibel-milliwatts')
plt.show()
```



```
[60]: plt.figure(figsize = (16,9))
plt.plot(power_dbm_seconds_resample.index,
         ↪power_dbm_seconds_resample[columns[17]], label = columns[17])
plt.plot(power_dbm_seconds_resample.index,
         ↪power_dbm_seconds_resample[columns[18]], label = columns[18])
plt.plot(power_dbm_seconds_resample.index,
         ↪power_dbm_seconds_resample[columns[19]], label = columns[19])
plt.grid()
plt.legend(loc = 'best')
plt.title('Secondly resampled Power for full measurement')
plt.xlabel('time')
plt.ylabel('decibel-milliwatts')
plt.show()
```



3.5 Winkel (Azimuth, Ellipticity)

```
[61]: angle = pd.read_csv(filename, skiprows=skip, usecols=[columns[0], columns[9],
↪ columns[10]], sep=sep)
```

```
[62]: angle[columns[0]] = pd.to_datetime(angle[columns[0]])
angle.set_index(columns[0], inplace=True)
```

```
[63]: angle.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 7092298 entries, 2024-11-29 00:26:44.470000 to 2024-12-03
21:24:03.030000
Data columns (total 2 columns):
#   Column          Dtype
---  -
0    Azimuth[°]      float64
1    Ellipticity[°]  float64
dtypes: float64(2)
memory usage: 162.3 MB
```

```
[64]: angle.isnull().sum()
```

```
[64]: Azimuth[°]      0
Ellipticity[°]      0
dtype: int64
```



```
[65]: angle.describe()
```

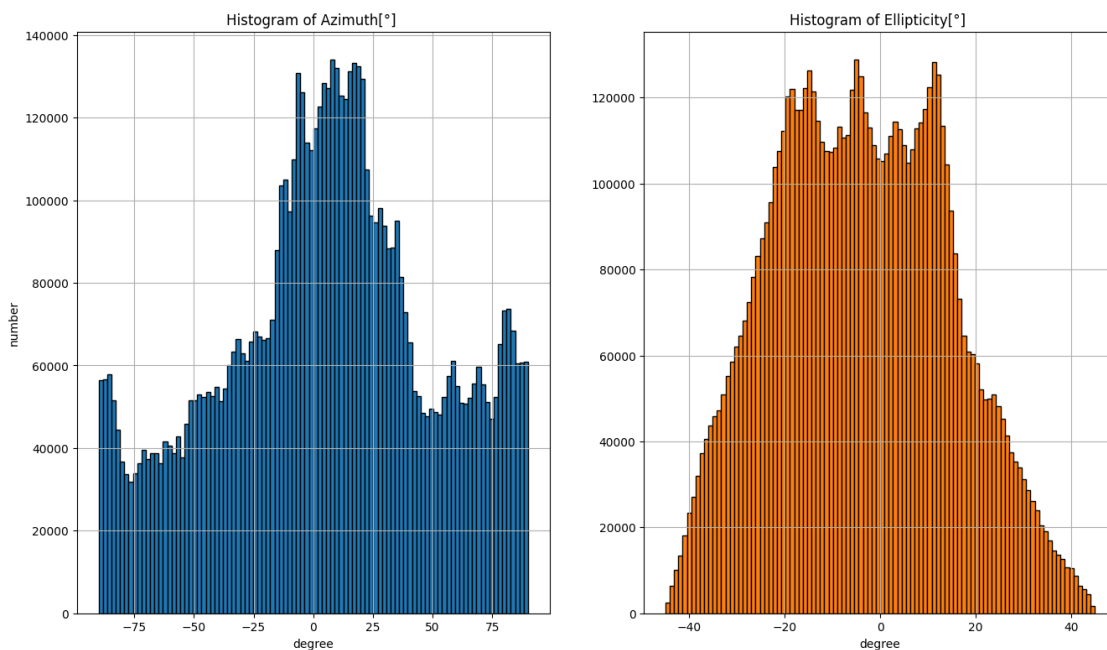
```
[65]:
```

	Azimuth[°]	Ellipticity[°]
count	7.092298e+06	7.092298e+06
mean	5.349416e+00	-3.838762e+00
std	4.483804e+01	1.833112e+01
min	-9.000000e+01	-4.498000e+01
25%	-2.413000e+01	-1.805000e+01
50%	7.080000e+00	-4.300000e+00
75%	3.522000e+01	1.001000e+01
max	9.000000e+01	4.498000e+01

```
[66]: plt.figure(figsize = (16,9))
plt.subplot(1, 2, 1)
plt.hist(angle[columns[9]], bins=100, color='tab:blue', edgecolor='black')
plt.grid()
plt.xlabel('degree')
plt.ylabel('number')
plt.title('Histogram of Azimuth[°] ')

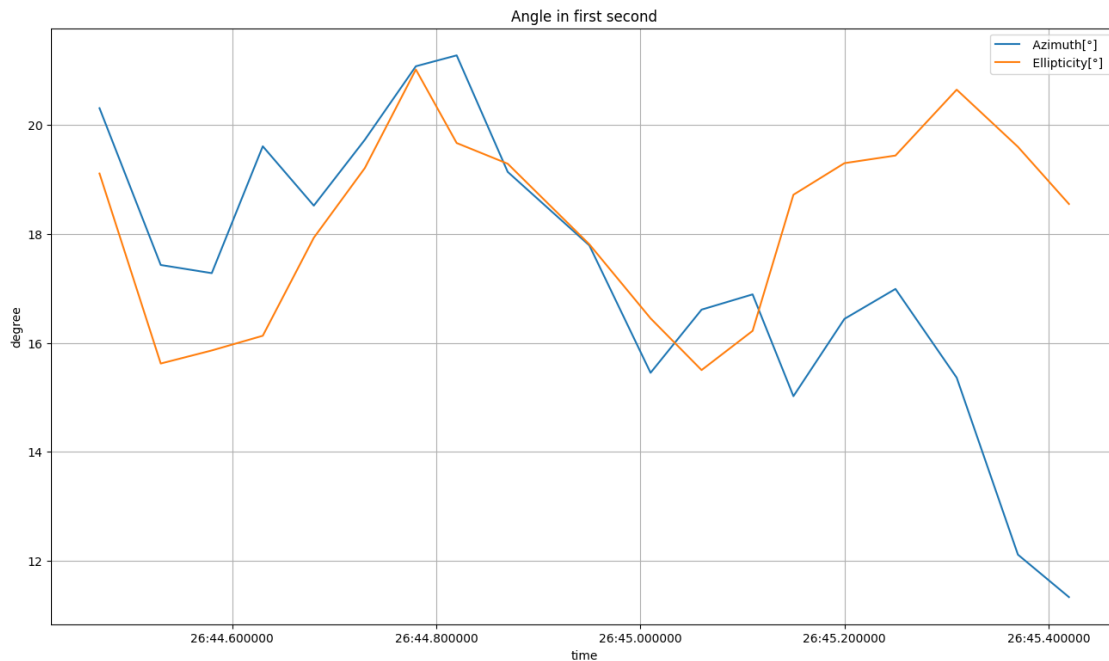
plt.subplot(1, 2, 2)
plt.hist(angle[columns[10]], bins=100, color='tab:orange', edgecolor='black')
plt.grid()
plt.xlabel('degree')
plt.title('Histogram of Ellipticity[°] ')

plt.show()
```



```
[67]: first_second = angle.loc[(angle.index >= start_time) & (angle.index <
    ↪end_time_second)]

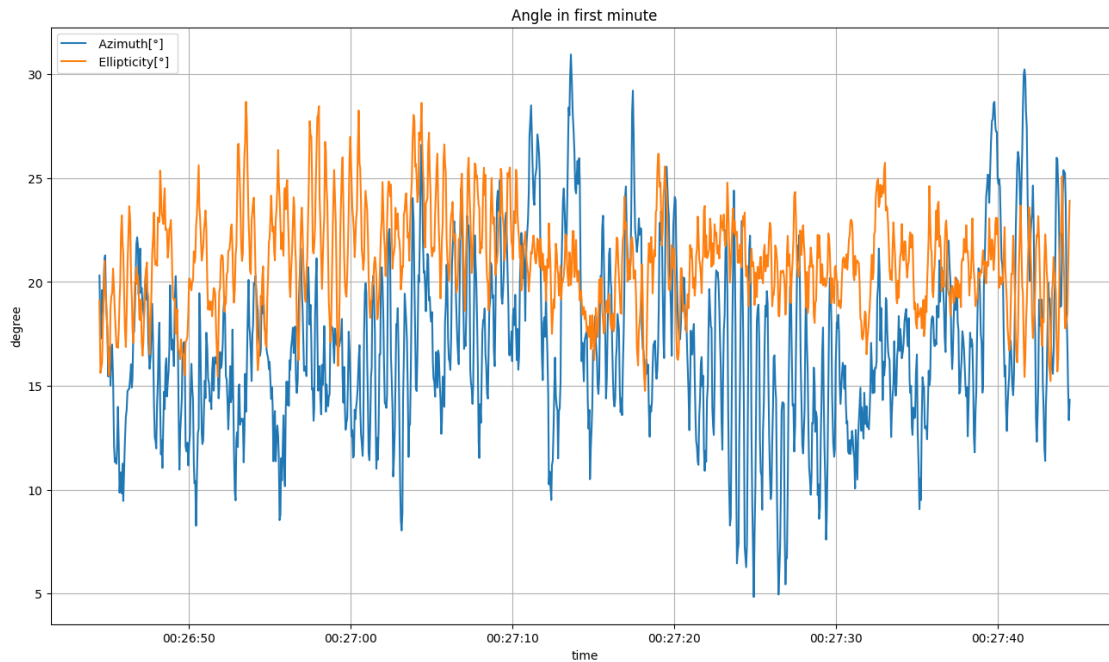
plt.figure(figsize = (16,9))
plt.plot(first_second.index, first_second[columns[9]], label = columns[9])
plt.plot(first_second.index, first_second[columns[10]], label = columns[10])
plt.grid()
plt.legend(loc = 'best')
plt.title('Angle in first second')
plt.xlabel('time')
plt.ylabel('degree')
plt.show()
```



```
[68]: first_minute = angle.loc[(angle.index >= start_time) & (angle.index <
    ↪end_time_minute)]

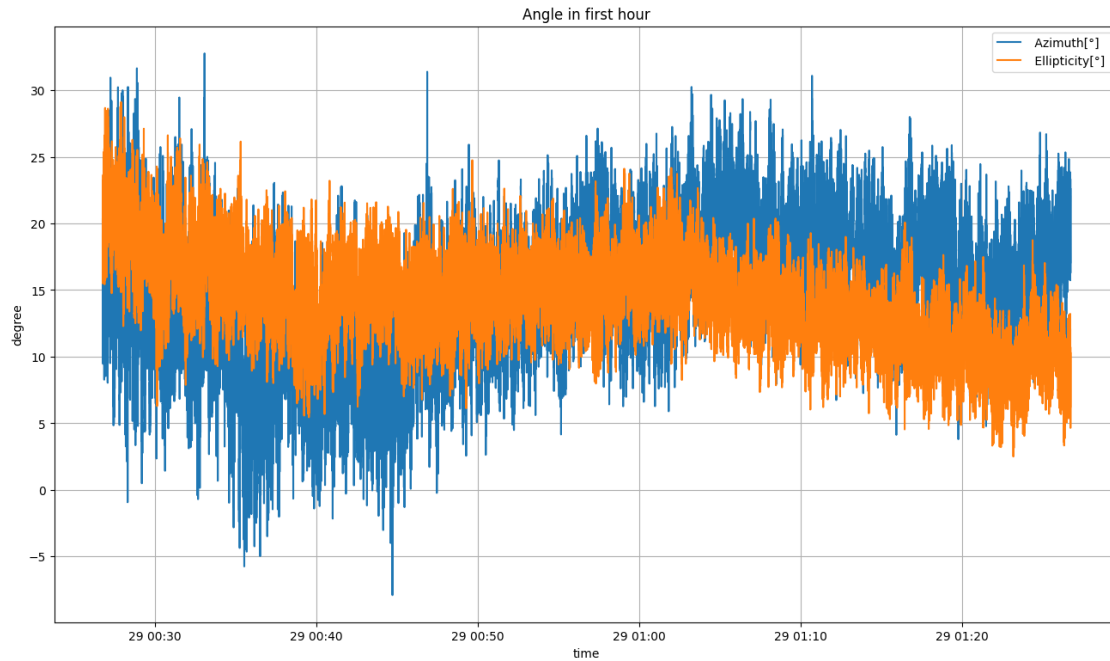
plt.figure(figsize = (16,9))
plt.plot(first_minute.index, first_minute[columns[9]], label = columns[9])
plt.plot(first_minute.index, first_minute[columns[10]], label = columns[10])
plt.grid()
plt.legend(loc = 'best')
plt.title('Angle in first minute')
plt.xlabel('time')
```

```
plt.ylabel('degree')
plt.show()
```



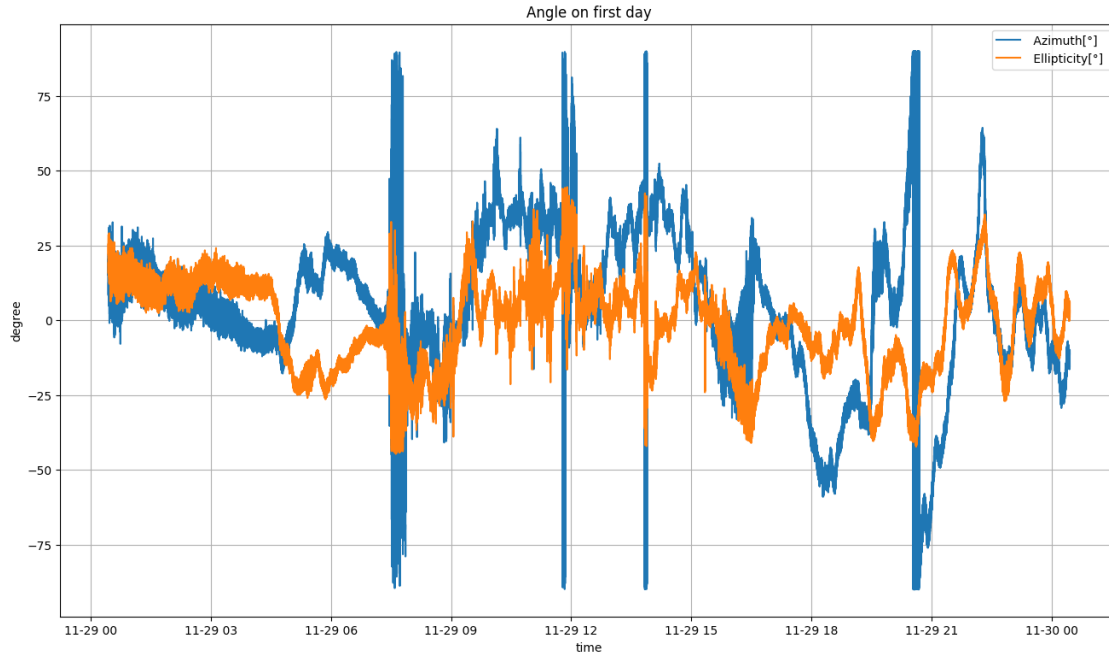
```
[69]: first_hour = angle.loc[(angle.index >= start_time) & (angle.index <
    ↪end_time_hour)]

plt.figure(figsize = (16,9))
plt.plot(first_hour.index, first_hour[columns[9]], label = columns[9])
plt.plot(first_hour.index, first_hour[columns[10]], label = columns[10])
plt.grid()
plt.legend(loc = 'best')
plt.title('Angle in first hour')
plt.xlabel('time')
plt.ylabel('degree')
plt.show()
```



```
[70]: first_day = angle.loc[(angle.index >= start_time) & (angle.index <
    ↪end_time_day)]

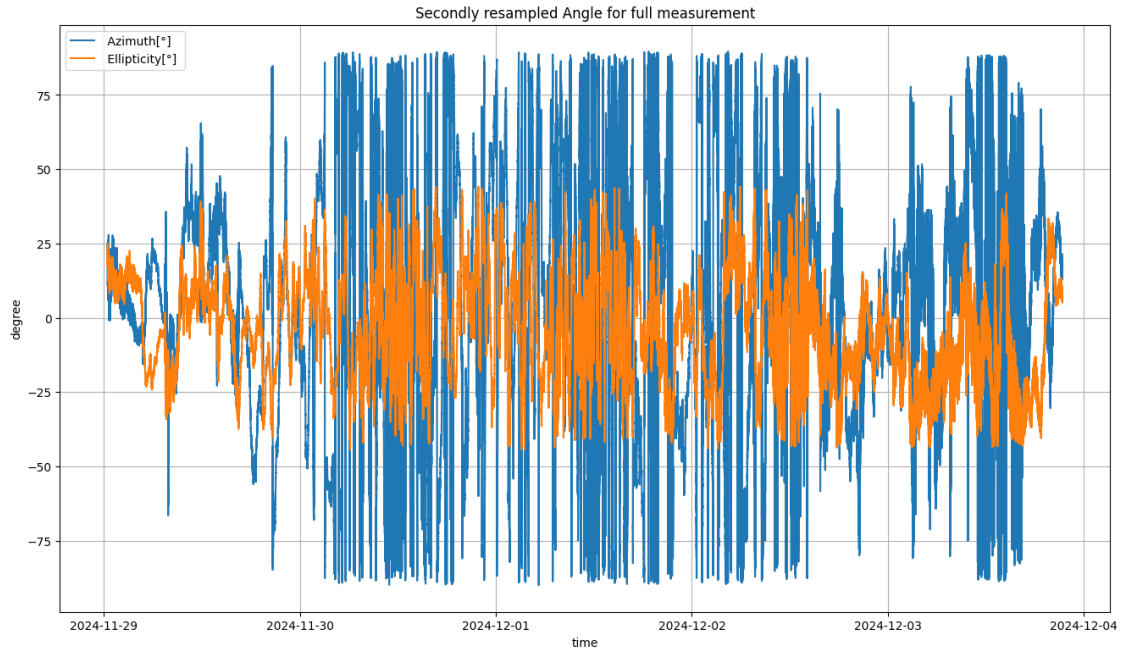
plt.figure(figsize = (16,9))
plt.plot(first_day.index, first_day[columns[9]], label = columns[9])
plt.plot(first_day.index, first_day[columns[10]], label = columns[10])
plt.grid()
plt.legend(loc = 'best')
plt.title('Angle on first day')
plt.xlabel('time')
plt.ylabel('degree')
plt.show()
```



```
[71]: angle_seconds_resample = angle.resample('s').mean()
      angle_seconds_resample.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 421040 entries, 2024-11-29 00:26:44 to 2024-12-03 21:24:03
Freq: s
Data columns (total 2 columns):
#   Column          Non-Null Count  Dtype
---  -
0   Azimuth[°]      418526 non-null float64
1   Ellipticity[°]  418526 non-null float64
dtypes: float64(2)
memory usage: 9.6 MB
```

```
[72]: plt.figure(figsize = (16,9))
      plt.plot(angle_seconds_resample.index, angle_seconds_resample[columns[9]],
               ↪label = columns[9])
      plt.plot(angle_seconds_resample.index, angle_seconds_resample[columns[10]],
               ↪label = columns[10])
      plt.grid()
      plt.legend(loc = 'best')
      plt.title('Secondly resampled Angle for full measurement')
      plt.xlabel('time')
      plt.ylabel('degree')
      plt.show()
```



3.6 Stokes-Parameter (S0, S1, S2, S3 / Normalized S1, S2, S3)

```
[73]: stokes = pd.read_csv(filename, skiprows=skip, usecols=[columns[0], columns[5],
↪ columns[6], columns[7], columns[8]], sep=sep)
```

```
[74]: stokes[columns[0]] = pd.to_datetime(stokes[columns[0]])
stokes.set_index(columns[0], inplace=True)
```

```
[75]: stokes.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 7092298 entries, 2024-11-29 00:26:44.470000 to 2024-12-03
21:24:03.030000
Data columns (total 4 columns):
#   Column      Dtype
---  -
0    S 0 [mW]   float64
1    S 1 [mW]   float64
2    S 2 [mW]   float64
3    S 3 [mW]   float64
dtypes: float64(4)
memory usage: 270.5 MB
```

```
[76]: stokes.isnull().sum()
```

```
[76]: S 0 [mW]    0
      S 1 [mW]    0
      S 2 [mW]    0
      S 3 [mW]    0
      dtype: int64
```

```
[77]: stokes.describe()
```

```
[77]:
```

	S 0 [mW]	S 1 [mW]	S 2 [mW]	S 3 [mW]
count	7.092298e+06	7.092298e+06	7.092298e+06	7.092298e+06
mean	2.386558e-01	4.826444e-02	1.702841e-02	-2.669778e-02
std	1.068249e-02	1.413223e-01	1.286800e-01	1.294159e-01
min	-2.843000e-04	-2.557000e-01	-2.594000e-01	-2.460000e-01
25%	2.331000e-01	-6.597000e-02	-8.226000e-02	-1.400000e-01
50%	2.393000e-01	8.051000e-02	2.759000e-02	-3.555000e-02
75%	2.450000e-01	1.711000e-01	1.209000e-01	8.157000e-02
max	2.754000e-01	2.572000e-01	2.684000e-01	2.430000e-01

```
[78]: normalized_stokes = pd.read_csv(filename, skiprows=skip, usecols=[columns[0],  
    ↪ columns[2], columns[3], columns[4]], sep=sep)
```

```
[79]: normalized_stokes[columns[0]] = pd.to_datetime(normalized_stokes[columns[0]])  
normalized_stokes.set_index(columns[0], inplace=True)
```

```
[80]: normalized_stokes.info()
```

```
<class 'pandas.core.frame.DataFrame'>  
DatetimeIndex: 7092298 entries, 2024-11-29 00:26:44.470000 to 2024-12-03  
21:24:03.030000  
Data columns (total 3 columns):  
#   Column          Dtype  
---  ---  
0   Normalized s 1   float64  
1   Normalized s 2   float64  
2   Normalized s 3   float64  
dtypes: float64(3)  
memory usage: 216.4 MB
```

```
[81]: normalized_stokes.isnull().sum()
```

```
[81]: Normalized s 1    0  
      Normalized s 2    0  
      Normalized s 3    0  
      dtype: int64
```

```
[82]: normalized_stokes.describe()
```

```
[82]:
```

	Normalized s 1	Normalized s 2	Normalized s 3
count	7.092298e+06	7.092298e+06	7.092298e+06
mean	2.034914e-01	7.109757e-02	-1.129362e-01
std	5.928214e-01	5.405157e-01	5.451928e-01
min	-1.000000e+00	-1.000000e+00	-1.000000e+00
25%	-2.800000e-01	-3.500000e-01	-5.900000e-01
50%	3.400000e-01	1.200000e-01	-1.500000e-01
75%	7.200000e-01	5.100000e-01	3.400000e-01
max	1.000000e+00	1.000000e+00	1.000000e+00

3.7 Power-Split-Ratio & Phase Difference

```
[83]: modality = pd.read_csv(filename, skiprows=skip, usecols=[columns[0],
↳ columns[20], columns[21]], sep=sep)
```

```
[84]: modality[columns[0]] = pd.to_datetime(modality[columns[0]])
modality.set_index(columns[0], inplace=True)
```

```
[85]: modality.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 7092298 entries, 2024-11-29 00:26:44.470000 to 2024-12-03
21:24:03.030000
Data columns (total 2 columns):
#   Column                Dtype
---  -
0   Power-Split-Ratio     float64
1   Phase Difference[°]    float64
dtypes: float64(2)
memory usage: 162.3 MB
```

```
[86]: modality.isnull().sum()
```

```
[86]: Power-Split-Ratio      0
Phase Difference[°]        0
dtype: int64
```

```
[87]: modality.describe()
```

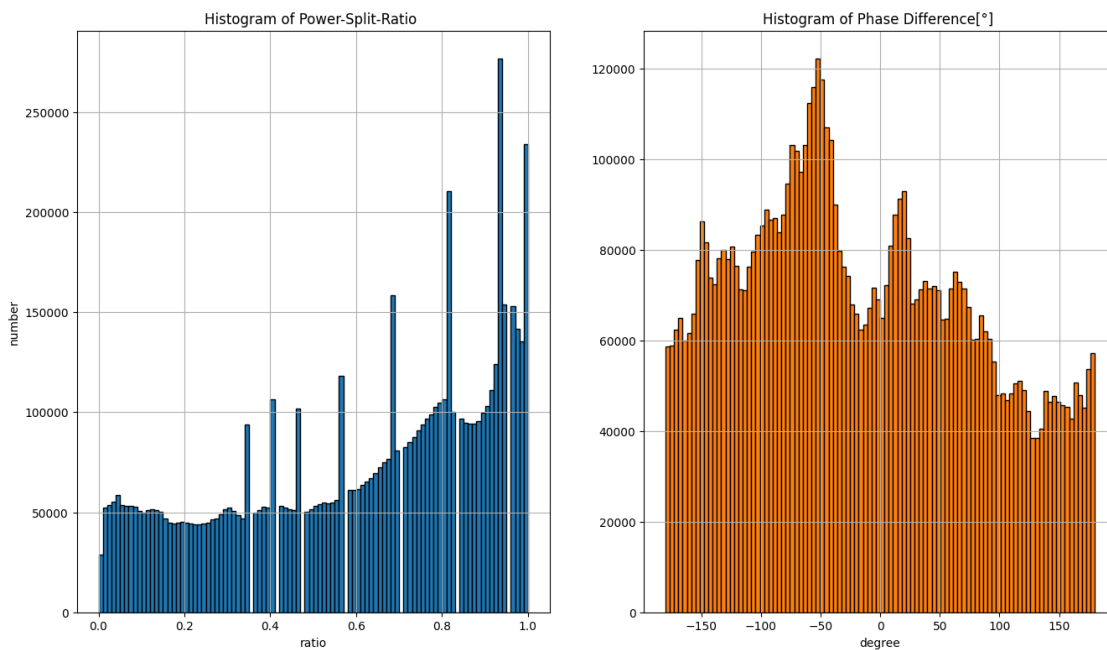
```
[87]:
```

	Power-Split-Ratio	Phase Difference[°]
count	7.092298e+06	7.092298e+06
mean	6.017494e-01	-1.623205e+01
std	2.964305e-01	9.624108e+01
min	0.000000e+00	-1.800000e+02
25%	3.600000e-01	-9.366000e+01
50%	6.700000e-01	-2.880000e+01
75%	8.600000e-01	5.927000e+01
max	1.000000e+00	1.800000e+02


```
[88]: plt.figure(figsize = (16,9))
plt.subplot(1, 2, 1)
plt.hist(modality[columns[20]], bins=100, color='tab:blue', edgecolor='black')
plt.grid()
plt.xlabel('ratio')
plt.ylabel('number')
plt.title('Histogram of Power-Split-Ratio ')

plt.subplot(1, 2, 2)
plt.hist(modality[columns[21]], bins=100, color='tab:orange', edgecolor='black')
plt.grid()
plt.xlabel('degree')
plt.title('Histogram of Phase Difference[°] ')

plt.show()
```



```
[89]: first_second = modality.loc[(modality.index >= start_time) & (modality.index <
    ↪end_time_second)]

fig, ax1 = plt.subplots(figsize=(16, 9))

ax1.plot(first_second.index, first_second[columns[20]], color='tab:blue',
    ↪label=columns[20])
ax1.set_xlabel('time')
ax1.set_ylabel('ratio')
```

```

ax1.grid()

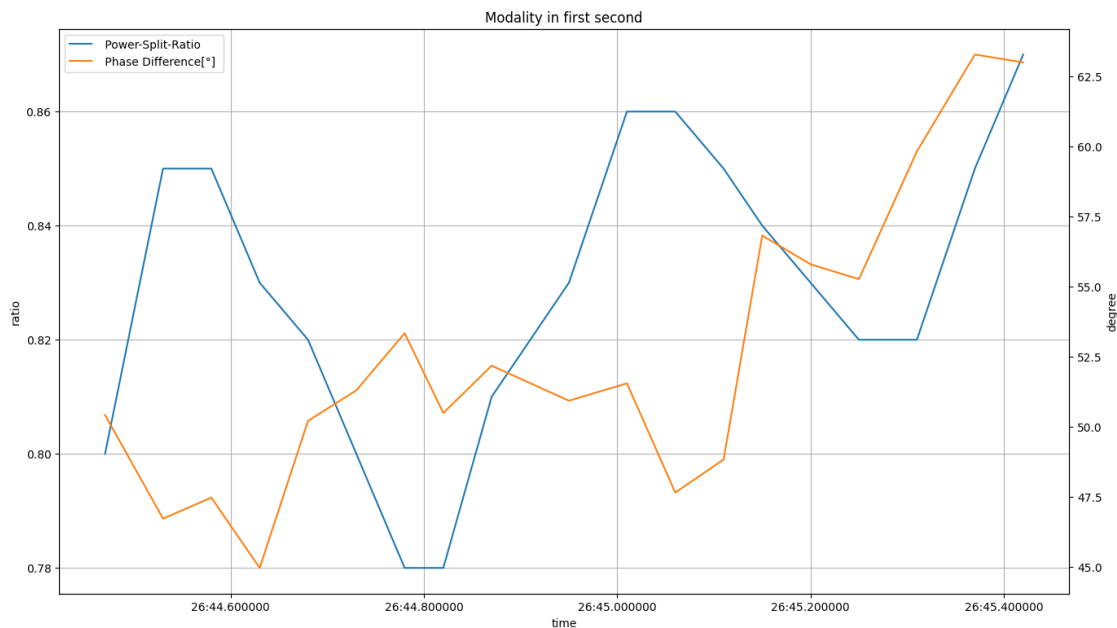
ax2 = ax1.twinx()
ax2.plot(first_second.index, first_second[columns[21]], color='tab:orange',
        ↪label=columns[21])
ax2.set_ylabel('degree')

plt.title('Modality in first second')

lines_1, labels_1 = ax1.get_legend_handles_labels()
lines_2, labels_2 = ax2.get_legend_handles_labels()
plt.legend(lines_1 + lines_2, labels_1 + labels_2, loc='best')

plt.show()

```



```

[90]: first_minute = modality.loc[(modality.index >= start_time) & (modality.index <
        ↪end_time_minute)]

fig, ax1 = plt.subplots(figsize=(16, 9))

ax1.plot(first_minute.index, first_minute[columns[20]], color='tab:blue',
        ↪label=columns[20])
ax1.set_xlabel('time')
ax1.set_ylabel('ratio')
ax1.grid()

```

```

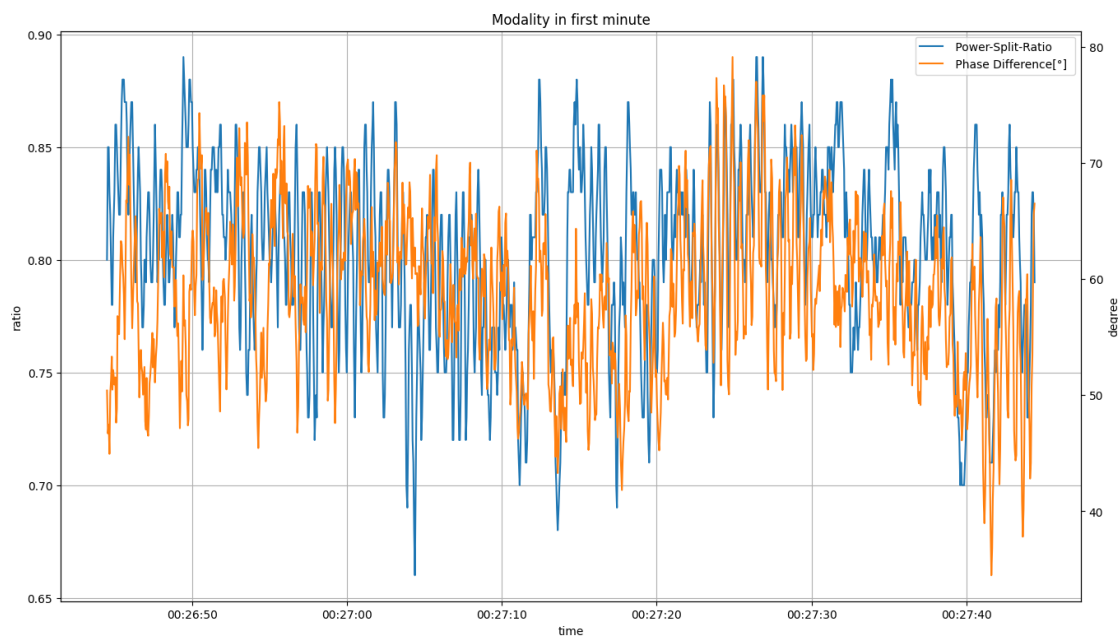
ax2 = ax1.twinx()
ax2.plot(first_minute.index, first_minute[columns[21]], color='tab:orange',
        ↪label=columns[21])
ax2.set_ylabel('degree')

plt.title('Modality in first minute')

lines_1, labels_1 = ax1.get_legend_handles_labels()
lines_2, labels_2 = ax2.get_legend_handles_labels()
plt.legend(lines_1 + lines_2, labels_1 + labels_2, loc='best')

plt.show()

```



```

[91]: first_hour = modality.loc[(modality.index >= start_time) & (modality.index <
        ↪end_time_hour)]

fig, ax1 = plt.subplots(figsize=(16, 9))

ax1.plot(first_hour.index, first_hour[columns[20]], color='tab:blue',
        ↪label=columns[20])
ax1.set_xlabel('time')
ax1.set_ylabel('ratio')
ax1.grid()

ax2 = ax1.twinx()

```

```

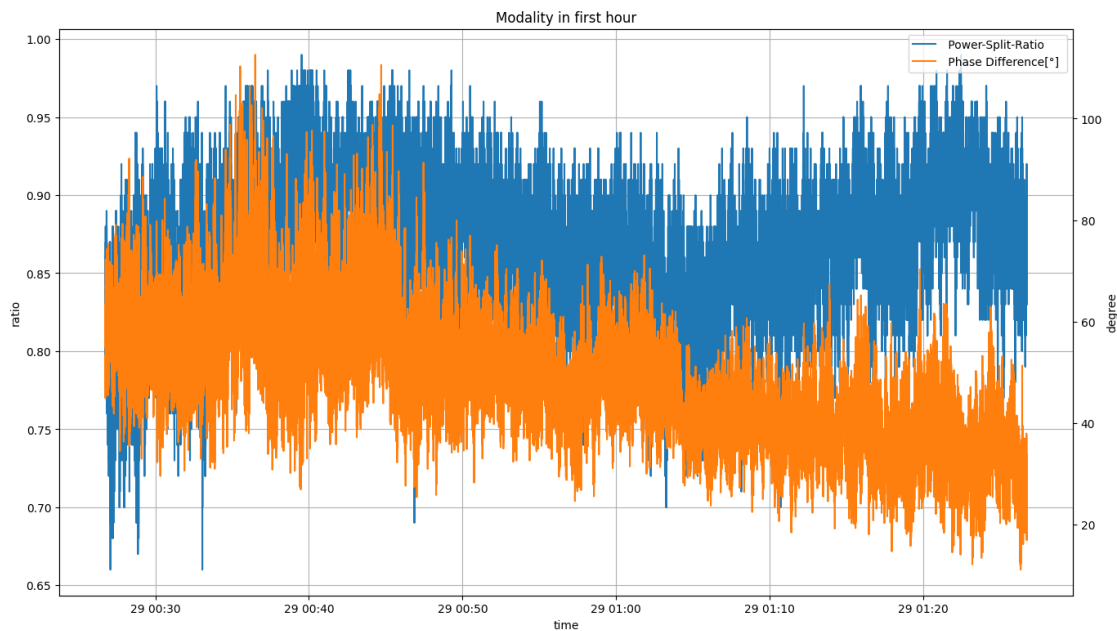
ax2.plot(first_hour.index, first_hour[columns[21]], color='tab:orange',
        ↪label=columns[21])
ax2.set_ylabel('degree')

plt.title('Modality in first hour')

lines_1, labels_1 = ax1.get_legend_handles_labels()
lines_2, labels_2 = ax2.get_legend_handles_labels()
plt.legend(lines_1 + lines_2, labels_1 + labels_2, loc='best')

plt.show()

```



```

[92]: first_day = modality.loc[(modality.index >= start_time) & (modality.index <
    ↪end_time_day)]

fig, ax1 = plt.subplots(figsize=(16, 9))

ax1.plot(first_day.index, first_day[columns[20]], color='tab:blue',
        ↪label=columns[20])
ax1.set_xlabel('time')
ax1.set_ylabel('ratio')
ax1.grid()

ax2 = ax1.twinx()
ax2.plot(first_day.index, first_day[columns[21]], color='tab:orange',
        ↪label=columns[21])

```

```

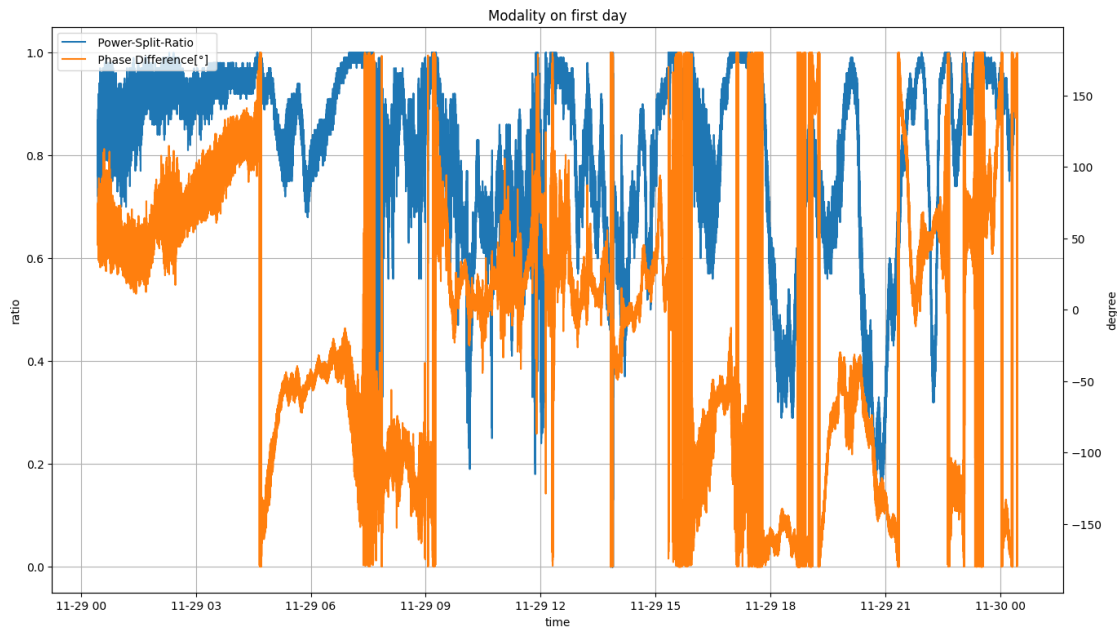
ax2.set_ylabel('degree')

plt.title('Modality on first day')

lines_1, labels_1 = ax1.get_legend_handles_labels()
lines_2, labels_2 = ax2.get_legend_handles_labels()
plt.legend(lines_1 + lines_2, labels_1 + labels_2, loc='best')

plt.show()

```



```

[93]: modality_seconds_resample = modality.resample('s').mean()
      modality_seconds_resample.info()

```

```

<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 421040 entries, 2024-11-29 00:26:44 to 2024-12-03 21:24:03
Freq: s
Data columns (total 2 columns):
 #   Column                Non-Null Count  Dtype
---  -
 0   Power-Split-Ratio     418526 non-null float64
 1   Phase Difference[°]    418526 non-null float64
dtypes: float64(2)
memory usage: 9.6 MB

```

```

[94]: fig, ax1 = plt.subplots(figsize=(16, 9))

```

```

ax1.plot(modality_seconds_resample.index,
        ↪modality_seconds_resample[columns[20]], color='tab:blue', label=columns[20])
ax1.set_xlabel('time')
ax1.set_ylabel('ratio')
ax1.grid()

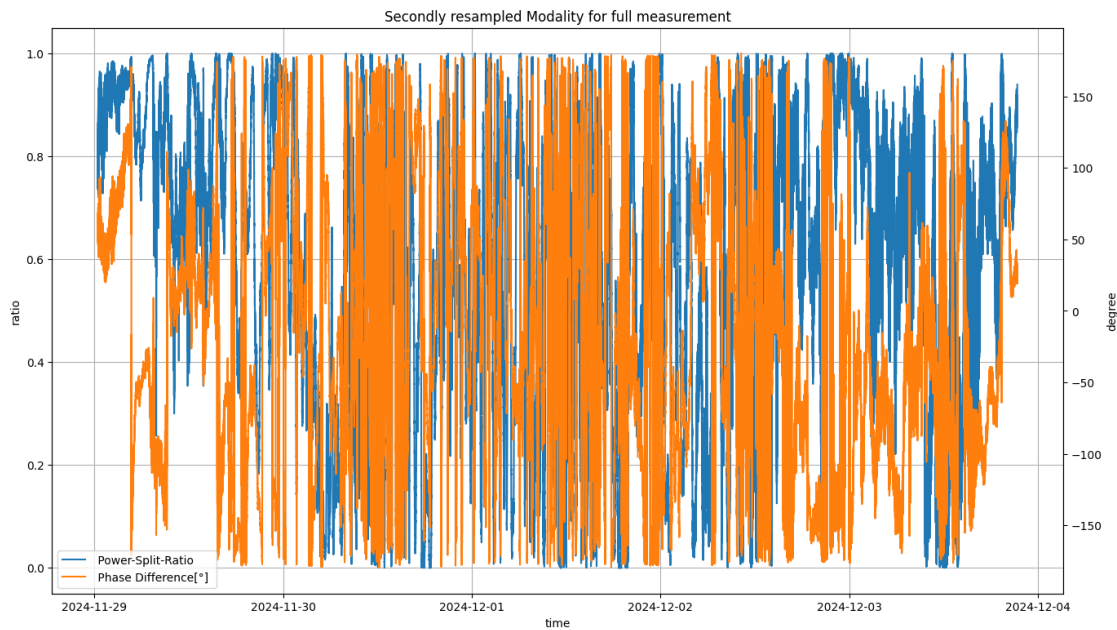
ax2 = ax1.twinx()
ax2.plot(modality_seconds_resample.index,
        ↪modality_seconds_resample[columns[21]], color='tab:orange',
        ↪label=columns[21])
ax2.set_ylabel('degree')

plt.title('Secondly resampled Modality for full measurement')

lines_1, labels_1 = ax1.get_legend_handles_labels()
lines_2, labels_2 = ax2.get_legend_handles_labels()
plt.legend(lines_1 + lines_2, labels_1 + labels_2, loc='best')

plt.show()

```



[]: