

12.3.7

$$n=17 \quad \hat{\beta}_0 = 12.08 \quad \hat{\beta}_1 = 34.60 \quad \hat{\sigma}^2 = 17.65 \quad S_{xx} = 1096 \quad \bar{x} = 53.2$$

$$1-\alpha = .05$$

$$\alpha = .05$$

$$t_{\frac{\alpha}{2}, n-2} = t_{.025, 15}$$

$$t_{.025, 15} = 2.131$$

$$y_{H_0} \in \left( 12.08 + (34.60 \times 40) \pm 2.131 \sqrt{17.65 \times \left( \frac{18}{1096} + \frac{(40-53.2)^2}{1096} \right)} \right)$$

$$y_{H_0} \in (1386, 1406)$$

12.4.10

$$X_{VAL} = 35 \quad \text{confidence interval} = 99\%$$

$$\text{Sample size, } n=7 \quad \text{Degrees of freedom, } df_{n-2}=5$$

$$t_{\alpha/2} = 4.032$$

$$\bar{x} = 34.40 \quad \sum (x - \bar{x})^2 = S_{xx} = 26.92$$

$$SE = 1.0085$$

$$\text{Predicted } Y \text{ at } X = 35 \text{ is } \hat{y} = 114.5876 + -2.1142(35) = 70.4142$$

$$\text{standard error} = SE \sqrt{(1/n + (x - \bar{x})^2 / S_{xx})} = 1.40$$

$$\text{margin of error, } E = t^* \text{Std error} = t^* \hat{SE}(\hat{y}) = 4.032(1.40)$$

$$3.986 = 1.607$$

$$\text{Confidence lower limit} = \hat{y} + E = 70.414 - 1.607 = 68.81$$

$$\text{Confidence Upper limit} = \hat{y} + E = 70.414 + 1.607 = 72.02$$

5 12.4.2

Same as 12.5.1