

Algorithms

Topological Homework 2

Mostafa S. Ibrahim

Teaching, Training and Coaching for more than a decade!

Artificial Intelligence & Computer Vision Researcher

PhD from Simon Fraser University - Canada

Bachelor / Msc from Cairo University - Egypt

Ex-(Software Engineer / ICPC World Finalist)



Problem 1#: [LeetCode 444](#) - Sequence Reconstruction

- *Rewriting the statement*
- Recall: a **subsequence** of a given sequence is a sequence that can be derived from the given sequence by **deleting** some or no elements **without** changing the **order** of the remaining elements.
 - [2, 4, 7] is subsequence of [1, 2, 3, 4, 5, 6, 7]
 - [7, 4, 2] is NOT subsequence of [1, 2, 3, 4, 5, 6, 7] as the order is maintained
- Given a list of sequences *seqs*, a sequence S is called supersequence if it contains ALL the sequences in *seqs*
 - S = [1,2,3] is supersequence for seqs = [[1,2],[1,3],[2,3]]
- Given *seq* and *org* (a **permutation** of the integers from 1 to n, with $1 \leq n \leq 10^4$) return true IFF *org* is the **shortest and unique** supersequence for *seq*
 - Only **one shortest** super-sequence is possible

Signature

- C++: `bool sequenceReconstruction(vector<int> &org, vector<vector<int>> &seqs)`
- Java: `public boolean sequenceReconstruction(int[] org, List<List<Integer>> seqs)`
- Python: `def sequenceReconstruction(self, org: List[int], seqs: List[List[int]]) -> bool`
- Javascript: `var sequenceReconstruction = function(org, seqs)`

- `1 <= n <= 10^4`
- `org` is a permutation of `{1,2,...,n}`.
- `1 <= seqs[i].length <= 10^5`
- `seqs[i][j]` fits in a 32-bit signed integer.

Example 1:

Input: org = [1,2,3], seqs = [[1,2],[1,3]]

Output: false

Explanation: [1,2,3] is not the only one sequence that can be reconstructed, because [1,3,2] is also a valid sequence that can be reconstructed.

Example 2:

Input: org = [1,2,3], seqs = [[1,2]]

Output: false

Explanation: The reconstructed sequence can only be [1,2].

Example 3:

Input: org = [1,2,3], seqs = [[1,2],[1,3],[2,3]]

Output: true

Explanation: The sequences [1,2], [1,3], and [2,3] can uniquely reconstruct the original sequence [1,2,3].

Example 4:

Input: org = [4,1,5,2,6,3], seqs = [[5,2,6,3],[4,1,5,2]]

Output: true

Problem #2: [LeetCode 310](#) - Minimum Height Trees

A tree is an undirected graph in which any two vertices are connected by *exactly* one path. In other words, any connected graph without simple cycles is a tree.

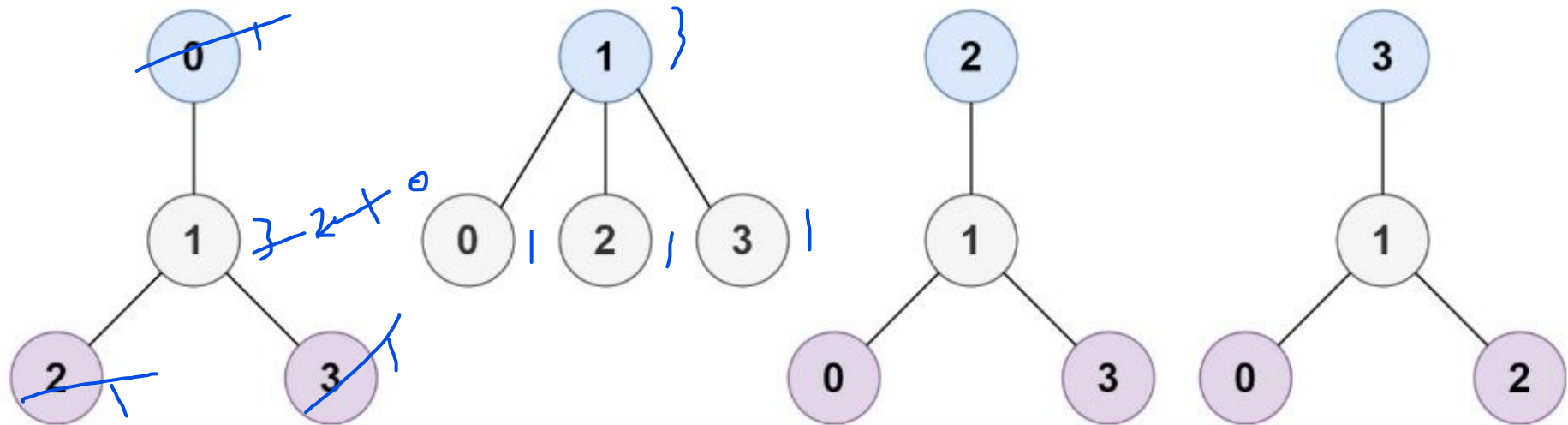
Given a tree of n nodes labelled from 0 to $n - 1$, and an array of $n - 1$ edges where $edges[i] = [a_i, b_i]$ indicates that there is an undirected edge between the two nodes a_i and b_i in the tree, you can choose any node of the tree as the root. When you select a node x as the root, the result tree has height h . Among all possible rooted trees, those with minimum height (i.e. $\min(h)$) are called **minimum height trees** (MHTs).

Return a list of all **MHTs'** root labels. You can return the answer in **any order**.

The **height** of a rooted tree is the number of edges on the longest downward path between the root and a leaf.

- C++: `vector<int> findMinHeightTrees(int n, vector<vector<int>> &edges)`
- Java: `public List<Integer> findMinHeightTrees(int n, int[][] edges)`
- Python: `def findMinHeightTrees(self, n: int, edges: List[List[int]]) -> List[int]:`
- Javascript: `var findMinHeightTrees = function(n, edges)`

Example 1:

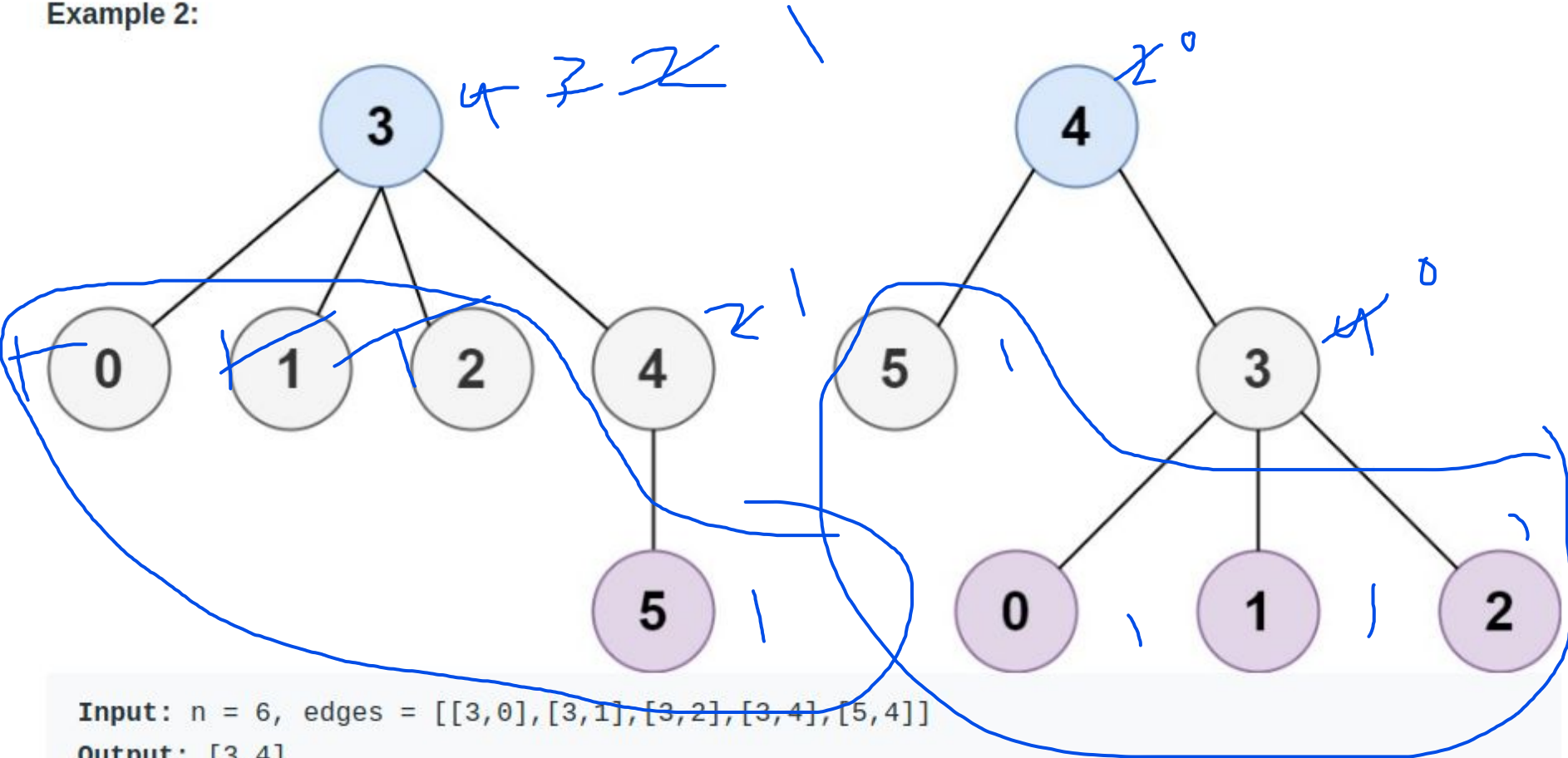


Input: $n = 4$, $\text{edges} = [[1,0],[1,2],[1,3]]$

Output: $[1]$

Explanation: As shown, the height of the tree is 1 when the root is the node with label 1 which is the only MHT.

Example 2:



Input: $n = 6$, edges = $[[3,0],[3,1],[3,2],[3,4],[5,4]]$

Output: $[3,4]$

Example 3:

Input: $n = 1$, $\text{edges} = []$

Output: $[0]$



Example 4:

Input: $n = 2$, $\text{edges} = [[0,1]]$

Output: $[0,1]$



Constraints:

- $1 \leq n \leq 2 * 10^4$
- $\text{edges.length} == n - 1$
- $0 \leq a_i, b_i < n$
- $a_i \neq b_i$
- All the pairs (a_i, b_i) are distinct.
- The given input is **guaranteed** to be a tree and there will be **no repeated** edges.

Problem #3: [LeetCode 329](#) - Longest Increasing Path in a Matrix

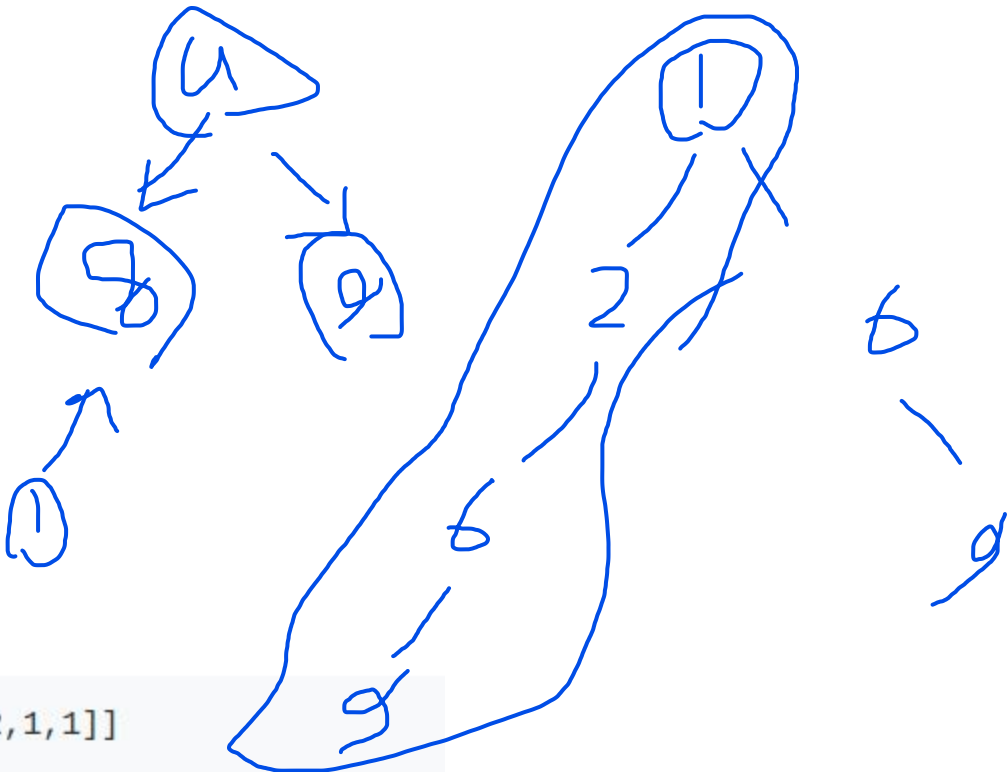
Given an $m \times n$ integers `matrix`, return *the length of the longest increasing path in `matrix`*.

From each cell, you can either move in four directions: left, right, up, or down. You **may not** move **diagonally** or move **outside the boundary** (i.e., wrap-around is not allowed).

- C++: `int longestIncreasingPath(vector<vector<int>>& matrix)`
- Java: `public int longestIncreasingPath(int[][] matrix)`
- Python: `def longestIncreasingPath(self, matrix: List[List[int]]) -> int`
- Javascript: `var longestIncreasingPath = function(matrix)`
- $1 \leq m, n \leq 200$
- $0 \leq \text{matrix}[i][j] \leq 2^{31} - 1$

Example 1:

9	9	4
6	6	8
2	1	1



Input: matrix = [[9,9,4],[6,6,8],[2,1,1]]

Output: 4

Explanation: The longest increasing path is [1, 2, 6, 9].

Example 2:

3 →	4 →	5 ↓
3	2	6
2	2	1

Input: matrix = [[3,4,5],[3,2,6],[2,2,1]]

Output: 4

Explanation: The longest increasing path is [3, 4, 5, 6]. Moving diagonally is not allowed.

Example 3:

Input: matrix = [[1]]

Output: 1

“Acquire knowledge and impart it to the people.”

“Seek knowledge from the Cradle to the Grave.”