

Algorithms

Sorting Homework 3

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Problem #1: [LeetCode 581](#) - Shortest Unsorted Continuous Subarray

- Given an integer array `nums`, you need to find **one continuous subarray** that if you **only sort** this subarray in ascending order, then the **whole array** will be **sorted in ascending** order.
 - Return the shortest such subarray and output its length.
- `int findUnsortedSubarray(vector<int> &nums)`
- First: Develop $O(n \log n)$ solution
- Second: Develop $O(n)$ time and $O(1)$ space solution
 - It requires analysis and **observation** skills
 - When we mention $O(n)$: 99% of the time I don't mean count sort

Examples

Example 1:

Input: `nums = [2,6,4,8,10,9,15]`

Output: 5

Explanation: You need to sort [6, 4, 8, 10, 9] in ascending order to make the whole array sorted in ascending order.

Example 2:

Input: `nums = [1,2,3,4]`

Output: 0

Example 3:

Input: `nums = [1]`

Output: 0

Problem #2: [LeetCode 826](#) - Most Profit Assigning Work

You have n jobs and m workers. You are given three arrays: `difficulty`, `profit`, and `worker` where:

- `difficulty[i]` and `profit[i]` are the difficulty and the profit of the i^{th} job, and
- `worker[j]` is the ability of j^{th} worker (i.e., the j^{th} worker can only complete a job with difficulty at most `worker[j]`).

Every worker can be assigned **at most one job**, but one job can be **completed multiple times**.

- For example, if three workers attempt the same job that pays `$1`, then the total profit will be `$3`. If a worker cannot complete any job, their profit is `$0`.

Return the maximum profit we can achieve after assigning the workers to the jobs.

- `int maxProfitAssignment(vector<int> &diff, vector<int> &pro, vector<int> &worker)`
- We can do a brute force algorithm in $O(NM)$. Can you do better?

Example 1:

Input: difficulty = [2,4,6,8,10], profit = [10,20,30,40,50], worker = [4,5,6,7]

Output: 100

Explanation: Workers are assigned jobs of difficulty [4,4,6,6] and they get a profit of [20,20,30,30] separately.

Example 2:

Input: difficulty = [85,47,57], profit = [24,66,99], worker = [40,25,25]

Output: 0

Problem #3: [LeetCode 1887](#) - Reduction Operations to Make the Array Elements Equal

- *Note: Simplified problem statement*
- Given an integer array, your goal is to make all values **equal**.
- In each step you perform the following operations:
 - Find the largest value in nums (idx i).
 - Find the **next** largest value in nums **strictly** smaller than largest (idx j)
 - Reduce the large to small: `nums[i] = nums[j]`
- Return the **number of operations** to make all elements in nums equal.
- `int reductionOperations(vector<int> &nums)`
- Find $O(n \log n)$ approach

Example 1:

Input: `nums = [5,1,3]`

Output: `3`

Explanation: It takes 3 operations to make all elements in `nums` equal:

1. largest = 5 at index 0. nextLargest = 3. Reduce `nums[0]` to 3. `nums = [3,1,3]`.
2. largest = 3 at index 0. nextLargest = 1. Reduce `nums[0]` to 1. `nums = [1,1,3]`.
3. largest = 3 at index 2. nextLargest = 1. Reduce `nums[2]` to 1. `nums = [1,1,1]`.

Example 2:

Input: `nums = [1,1,1]`

Output: `0`

Explanation: All elements in `nums` are already equal.

Example 3:

Input: `nums = [1,1,2,2,3]`

Output: `4`

Explanation: It takes 4 operations to make all elements in `nums` equal:

1. largest = 3 at index 4. nextLargest = 2. Reduce `nums[4]` to 2. `nums = [1,1,2,2,2]`.
2. largest = 2 at index 2. nextLargest = 1. Reduce `nums[2]` to 1. `nums = [1,1,1,2,2]`.
3. largest = 2 at index 3. nextLargest = 1. Reduce `nums[3]` to 1. `nums = [1,1,1,1,2]`.
4. largest = 2 at index 4. nextLargest = 1. Reduce `nums[4]` to 1. `nums = [1,1,1,1,1]`.

“Acquire knowledge and impart it to the people.”

“Seek knowledge from the Cradle to the Grave.”