```
In []: import numpy as np
    import pandas as pd
    import matplotlib.pyplot as plt
    from sklearn.linear_model import LinearRegression
    from sklearn.preprocessing import PolynomialFeatures
In []: # Loading the data
data = pd.read_csv('data.csv')
display(data)
```

	Var_X	Var_Y
0	-0.33532	6.66854
1	0.02160	3.86398
2	-1.19438	5.16161
3	-0.65046	8.43823
4	-0.28001	5.57201
5	1.93258	-11.13270
6	1.22620	-5.31226
7	0.74727	-4.63725
8	3.32853	3.80650
9	2.87457	-6.06084
10	-1.48662	7.22328
11	0.37629	2.38887
12	1.43918	-7.13415
13	0.24183	2.00412
14	-2.79140	4.29794
15	1.08176	-5.86553
16	2.81555	-5.20711
17	0.54924	-3.52863
18	2.36449	-10.16202
19	-1.01925	5.31123

```
In [ ]: # plting the data
data.plot();
```

```
Var_X
   7.5
                                                                   Var Y
   5.0
   2.5
   0.0
 -2.5
 -5.0
 -7.5
-10.0
         0.0
                 2.5
                         5.0
                                 7.5
                                        10.0
                                                12.5
                                                        15.0
                                                                17.5
```

```
In [ ]: # Spliting the data
        X = data['Var_X'].values.reshape(-1, 1)
        y = data['Var Y'].values
        display(X, y)
        array([[-0.33532],
               [ 0.0216 ],
               [-1.19438],
               [-0.65046],
               [-0.28001],
               [ 1.93258],
               [1.2262],
               [ 0.74727],
               [ 3.32853],
               [ 2.87457],
               [-1.48662],
               [ 0.37629],
               [ 1.43918],
               [ 0.24183],
               [-2.7914],
               [ 1.08176],
               [ 2.81555],
               [ 0.54924],
               [ 2.36449],
               [-1.01925]]
        array([ 6.66854, 3.86398,
                                       5.16161, 8.43823,
                                                             5.57201, -11.1327 ,
                -5.31226, -4.63725,
                                       3.8065 , -6.06084,
                                                             7.22328,
                                                                       2.38887,
                                       4.29794,
                                                 -5.86553, -5.20711, -3.52863,
                -7.13415, 2.00412,
               -10.16202,
                           5.31123])
In [ ]: # Create polynomial features
        # default degree is 2
        poly_features_D2 = PolynomialFeatures()
        poly_features_D3 = PolynomialFeatures(3)
        poly features D4 = PolynomialFeatures(4)
        poly_features_D5 = PolynomialFeatures(5)
        x2 = poly_features_D2.fit_transform(X)
        x3 = poly_features_D3.fit_transform(X)
        x4 = poly_features_D4.fit_transform(X)
        x5 = poly_features_D5.fit_transform(X)
```

displaying x2 , x3 and x4 just for example display(pd.DataFrame(x2), pd.DataFrame(x3), pd.DataFrame(x4))

	0	1	2
0	1.0	-0.33532	0.112440
1	1.0	0.02160	0.000467
2	1.0	-1.19438	1.426544
3	1.0	-0.65046	0.423098
4	1.0	-0.28001	0.078406
5	1.0	1.93258	3.734865
6	1.0	1.22620	1.503566
7	1.0	0.74727	0.558412
8	1.0	3.32853	11.079112
9	1.0	2.87457	8.263153
10	1.0	-1.48662	2.210039
11	1.0	0.37629	0.141594
12	1.0	1.43918	2.071239
13	1.0	0.24183	0.058482
14	1.0	-2.79140	7.791914
15	1.0	1.08176	1.170205
16	1.0	2.81555	7.927322
17	1.0	0.54924	0.301665
18	1.0	2.36449	5.590813
19	1.0	-1.01925	1.038871

0 1 2 0 1.0 -0.33532 0.112440 -0.03770 1 1.0 0.02160 0.000467 0.00001 2 1.0 -1.19438 1.426544 -1.70383 3 1.0 -0.65046 0.423098 -0.27520 4 1.0 -0.28001 0.078406 -0.02195 5 1.0 1.93258 3.734865 7.21792 6 1.0 1.22620 1.503566 1.84367 7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	0 1
1 1.0 0.02160 0.000467 0.000016 2 1.0 -1.19438 1.426544 -1.70383 3 1.0 -0.65046 0.423098 -0.27520 4 1.0 -0.28001 0.078406 -0.02195 5 1.0 1.93258 3.734865 7.21792 6 1.0 1.22620 1.503566 1.84367 7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	U
2 1.0 -1.19438 1.426544 -1.70383 3 1.0 -0.65046 0.423098 -0.27520 4 1.0 -0.28001 0.078406 -0.02195 5 1.0 1.93258 3.734865 7.21792 6 1.0 1.22620 1.503566 1.84367 7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	
3 1.0 -0.65046 0.423098 -0.27520 4 1.0 -0.28001 0.078406 -0.02195 5 1.0 1.93258 3.734865 7.21792 6 1.0 1.22620 1.503566 1.84367 7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	1 1
4 1.0 -0.28001 0.078406 -0.02195 5 1.0 1.93258 3.734865 7.21792 6 1.0 1.22620 1.503566 1.84367 7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	2 1
5 1.0 1.93258 3.734865 7.21792 6 1.0 1.22620 1.503566 1.84367 7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	3 1
6 1.0 1.22620 1.503566 1.84367 7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	4 1
7 1.0 0.74727 0.558412 0.41728 8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	5 1
8 1.0 3.32853 11.079112 36.87715 9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	6 1
9 1.0 2.87457 8.263153 23.75301 10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	7 1
10 1.0 -1.48662 2.210039 -3.28548 11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	8 1
11 1.0 0.37629 0.141594 0.05328 12 1.0 1.43918 2.071239 2.98088	9 1
12 1.0 1.43918 2.071239 2.98088	I 0 1
	l 1 1
	l 2 1
13 1.0 0.24183 0.058482 0.01414	I 3 1
14 1.0 -2.79140 7.791914 -21.75034	l 4 1
15 1.0 1.08176 1.170205 1.26588	I 5 1
16 1.0 2.81555 7.927322 22.31977	l 6 1
17 1.0 0.54924 0.301665 0.16568	I 7 1
18 1.0 2.36449 5.590813 13.21942	18 1
19 1.0 -1.01925 1.038871 -1.05886	l 9 1

```
0 1.0 -0.33532
                           0.112440
                                     -0.037703
                                              1.264264e-02
          1 1.0 0.02160
                           0.000467
                                     0.000010 2.176782e-07
          2 1.0 -1.19438
                           1.426544
                                     -1.703835 2.035027e+00
          3 1.0 -0.65046
                           0.423098
                                     -0.275208
                                              1.790121e-01
          4 1.0 -0.28001
                           0.078406
                                     -0.021954 6.147438e-03
          5 1.0 1.93258
                           3.734865
                                     7.217926 1.394922e+01
          6 1.0 1.22620
                                     1.843673 2.260712e+00
                           1.503566
          7 1.0
                 0.74727
                           0.558412
                                     0.417285 3.118245e-01
          8 1.0 3.32853 11.079112
                                     36.877157 1.227467e+02
          9 1.0
                 2.87457
                           8.263153
                                     23.753011 6.827969e+01
         10 1.0 -1.48662
                           2.210039
                                     -3.285488 4.884272e+00
         11 1.0 0.37629
                           0.141594
                                     0.053280
                                              2.004891e-02
         12 1.0 1.43918
                           2.071239
                                     2.980886 4.290031e+00
         13 1.0 0.24183
                           0.058482
                                      0.014143 3.420115e-03
         14 1.0 -2.79140
                           7.791914 -21.750349 6.071392e+01
         15 1.0
                1.08176
                                     1.265881 1.369379e+00
                           1.170205
         16 1.0 2.81555
                           7.927322
                                     22.319771 6.284243e+01
         17 1.0 0.54924
                           0.301665
                                     0.165686
                                              9.100152e-02
         18 1.0 2.36449
                           5.590813
                                    13.219421 3.125719e+01
         19 1.0 -1.01925
                           1.038871
                                     -1.058869 1.079252e+00
In [ ]: # showing the different degrees
         # 1. the Linear
         Linear = LinearRegression()
         Linear.fit(X, y)
         LinearRegression()
Out[ ]:
In [ ]: # I know I didn't split the data into trainning and testing
         # as this is just a test
         y1 = Linear.predict(X)
         array([ 2.21611784, 1.24911677, 4.54356358, 3.06992462, 2.06626681,
Out[ ]:
                -3.92828908, -2.01449828, -0.71693631, -7.71032746, -6.48041655,
                 5.33532754, 0.28815743, -2.59152363, 0.65244904, 8.87035962,
                -1.62316792, -6.32051404, -0.1804149 , -5.09846008, 4.069085 ])
         pd.DataFrame({'y1': y1, 'y': y}).plot();
```

3

0

1

2

```
7.5
   5.0
   2.5
   0.0
 -2.5
 -5.0
 -7.5
-10.0
         0.0
                 2.5
                         5.0
                                7.5
                                       10.0
                                               12.5
                                                        15.0
                                                               17.5
```

```
In [ ]: Linear.fit(x2, y)
        y2 =Linear.predict(x2)
        y2
        array([ 1.84578332, 0.77610159, 4.64343625, 2.83547842, 1.67645806,
Out[]:
               -4.0255836 , -2.43238113, -1.23095514, -6.54737621, -5.81861156,
                5.66700621, -0.23299811, -2.93518632, 0.14321961, 10.6819701,
               -2.08036143, -5.71739853, -0.70555706, -4.89474699, 4.04752251])
In [ ]: pd.DataFrame({'y2': y2, 'y': y}).plot();
          10
           5
           0
          -5
         -10
              0.0
                   2.5
                         5.0
                               7.5
                                    10.0
                                          12.5
                                               15.0
                                                     17.5
        Linear.fit(x3, y)
In [ ]:
        y3 =Linear.predict(x3)
        у3
        array([ 4.48222683, 1.88230375, 9.03265795, 6.52198786, 4.09463527,
Out[ ]:
               -8.49556163, -6.39672831, -3.49169832, 0.95776844, -4.65092976,
                9.63289367, -0.80305802, -7.36089053, 0.21346967, 2.43039622,
               -5.6145034 , -5.17972144, -2.08593807, -7.8719917 , 8.3985015 ])
In [ ]: pd.DataFrame({'y3': y3, 'y': y}).plot();
```

```
10 - 5 - 0 - 5 - 10.0 12.5 15.0 17.5
```

```
In [ ]:
        Linear.fit(x4, y)
         y4 =Linear.predict(x4)
        y4
        array([ 5.19641403,
                                3.23885556,
                                              7.00399695,
                                                             6.34330534,
Out[]:
                  4.93719303, -10.48940158, -6.37026049,
                                                            -2.34493858,
                  4.37232952, -5.7001477,
                                              6.7478636 ,
                                                             0.7092552 ,
                 -7.96880783,
                                1.72612006,
                                              4.12622364,
                                                            -5.19188792,
                 -6.55748759, -0.67958875, -10.36912438,
                                                             6.96590788])
        pd.DataFrame({'y4': y4, 'y': y}).plot();
In [ ]:
           7.5
           5.0
           2.5
           0.0
          -2.5
          -5.0
          -7.5
         -10.0
                                 7.5
                                            12.5
                                                  15.0
                           5.0
                                      10.0
                                                       17.5
                0.0
                     2.5
        Linear.fit(x5, y)
In [ ]:
        y5 =Linear.predict(x5)
        у5
        array([ 5.70182022,
                                3.60634262,
                                              6.73006389,
                                                             6.75796177,
Out[]:
                  5.4361751 , -10.63037595,
                                            -6.87602358,
                                                            -2.60656549,
                  3.64317897, -5.12968991,
                                              5.90070852,
                                                             0.78268161,
                 -8.46091817, 1.92155724,
                                              4.31346811,
                                                            -5.65979089,
                 -5.95116748, -0.76792072,
                                             -9.99727319,
                                                             6.98158735])
        pd.DataFrame({'y5': y5, 'y': y}).plot();
In [ ]:
         # welcome to the overfitting area 🤏
```

