

Title	Date	Time	Duration	Grade Release Date
Midterm Exam	March. 01, 2022	10:00 AM	90 minutes	March 07, 2022



	Elliott 405	Raspberry Pi Zero
Year	1957	2015
Price	£85,000 (1957)	\$5
Memory	16 KB	512 MB
Weight	3-6 tons	9 g
Size	21 cabinets, each 2m x 77cm x 77cm	65mm x 30mm x 5.4mm

Source: <https://www.spinellis.gr/blog/20151129/>

### Questions

**You must show your work and all steps for every question!**

**Q1: [10 marks: 5 marks each]** Explain the following terms in two or three sentences.

- Quantization
- Digital System

**Q2: [20 marks: 5 marks each]** Assuming an unsigned number system, show the maximum number and the smallest unit of increment given 3 integer and 2 fraction positions in the *hexadecimal* number system and their equal decimal values.

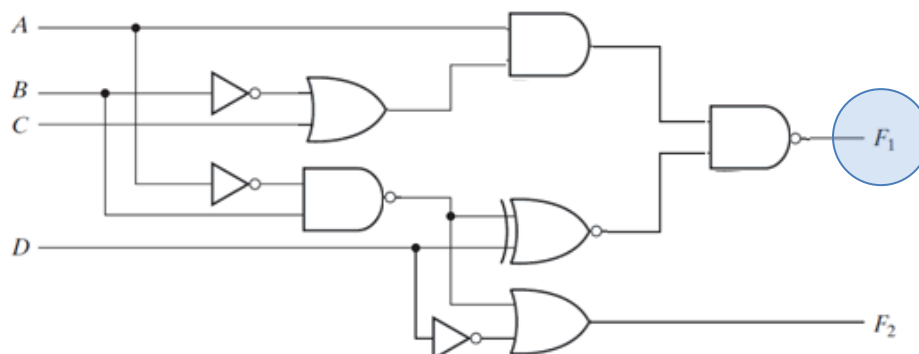
- $(\text{Max ?})_{16} = (?)_{10}$
- $(\text{Smallest Unit ?})_{16} = (?)_{10}$

**Q3: [15 marks]** Show the minimum possible error when converting  $(16.42)_{10}$  to base-9 if only 5 positions are given in total for both integer and fraction parts. Report the error in base-10.

**Q4: [15 marks]** Perform  $(+14) - (-1)$  in base-2 in (a) signed-magnitude and (b) signed-2's-complement. Use the least number of bits and check whether an overflow happens.

**Q5: [15 marks]** Analyze the logic circuit shown below only for F1:

- Show the truth table.
- $F1 = \prod (?)$



**Q6: [25 marks]** Design a 3-bit INCrementor, that is, the circuit generates the next number after the input number (e.g.,  $011 \rightarrow 100$ . Also,  $111 \rightarrow 000$ ):

- Show the truth table.
- Show the Boolean expressions for the outputs in PoS.
- Design an *efficient* circuit using NOR gates only.