

Eternal Sunshine of the Spotless Mind - Michel Gondry, 2004 https://www.youtube.com/watch?v=07-QBnEkgXU

Indexing is finding the whole information quicker using only part of it.

Part of information is called <u>Search Key</u>. It points to the whole information.

Primary Key
Surrogate Key
Candidate Key
Foreign Key



Index

How to find a webpage in WWW?

```
Search Key = 'UWindsor'
Whole Information = https://www.uwindsor.ca
```

- > 10¹⁰/seconds by no index, traverse all webpages
- < 0.31 seconds by Google
- ~ 0 seconds by ?

```
SELECT * FROM Director WHERE Id=1
SELECT * FROM Director WHERE LastName='Kubrick'
SELECT * FROM Director WHERE LastName='Kubrick' AND FirstName = 'Stanley'
```

CREATE [UNIQUE] INDEX IndexName ON TableName (c1, c2, ...);

Could be any name, but by convention we follow this: IX_ColumnName1_ColumnName2_...
UIX_ColumnName1_ColumnName2_...

UNIQUE INDEX does not allow duplicate in indexed columns. A way to create a <u>candidate key</u> set of columns in a table.

```
SQL × INDEX
```

SELECT * FROM Director WHERE Id = 1

CREATE UNIQUE INDEX LINE CREATE UNIQUE INDEX UIX_Id ON Director(Id)

By default, most DBMSs CREATE UNIQUE INDEX on primary key set of a table.

What other columns of a table should to be indexed?

- o Those columns of table that appears a lot in WHERE clause.
- o The search key of the table to find a single or range of rows.

It's a tuning task: - NBA

- o After the DB goes under heavy load DB designer need to increase retrieval speed.
- o Recently is done automatically by DBMS

SELECT * FROM Director WHERE LastName = 'Kubrick' CREATE INDEX IX_LastName ON Director(LastName)

7 8) Fum man.

```
ALTER TABLE TableName ADD [UNIQUE] INDEX IndexName ON (c1, c2, ...); ALTER TABLE TableName DROP INDEX IndexName;
```

SELECT * FROM Director WHERE LastName = 'Kubrick' AND FirstName = 'Stanley'

Which one?

- A) CREATE INDEX IX_LastName_FirstName ON Director(LastName, FirstName)
- B)) CREATE INDEX IX_FirstName_LastName ON Director(FirstName, LastName) ~
- C) CREATE INDEX IX_FirstName ON Director(FirstName)
- D) CREATE INDEX IX_LastName ON Director(LastName)
- E) All
- F) A & B are the same

As far as DB designer is concerned, knowing how to CREATE | ADD | DROP INDEX in SQL is more than enough.

However, knowing the implementation details inside DBMS helps DB designer with right decisions about indexing.

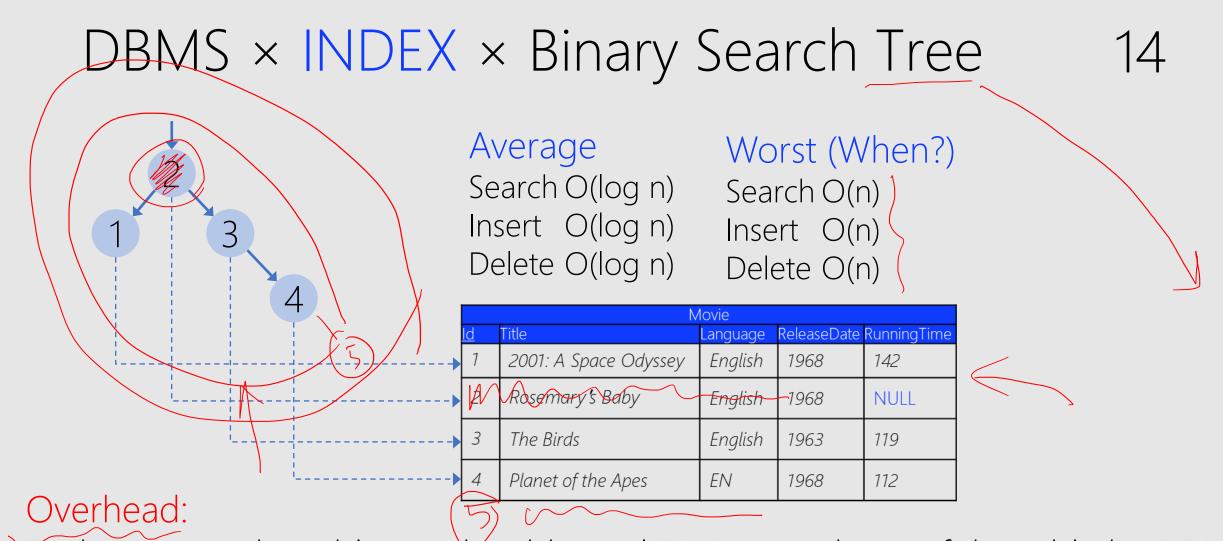
DBMS × INDEX × Binary Search Tree

Movie				
<u>ld</u>	Title	Language	ReleaseDate	RunningTime
1	2001: A Space Odyssey	English	1968	142
2	Rosemary's Baby	English	1968	NULL
3	The Birds	English	1963	119
4	Planet of the Apes	EN	1968	112

SELECT * FROM Movie WHERE Id = 1

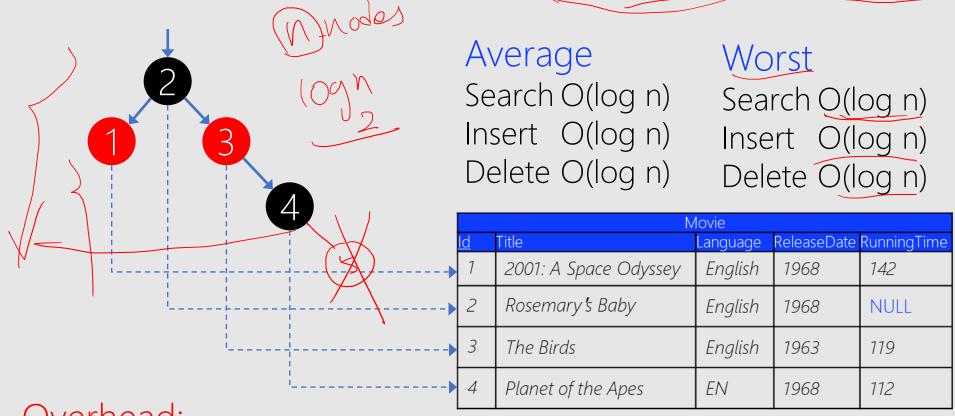
- A Sequential search, check all movies' Id with the given Id, i.e., 1
- B.) Binary search, after sorting elements in the list by Id -> (09 h
- C. Having an index structure:

 A. Creating a Binary Search Tree (BST)



Each DML on the table needs additional DML on indexes of the table by DBMS

DBMS × INDEX × Balanced Binary Tree 15



Overhead:

Each DML on the table needs additional DML on indexes of the table by DBMS

DBMS × INDEX × B-tree

Balanced Multi-way Tree

Bayer, R.; McCreight, E. (1972) Organization and Maintenance of Large Ordered Indexes Acta Informatica, 1 (3): 173–189

@Boeing

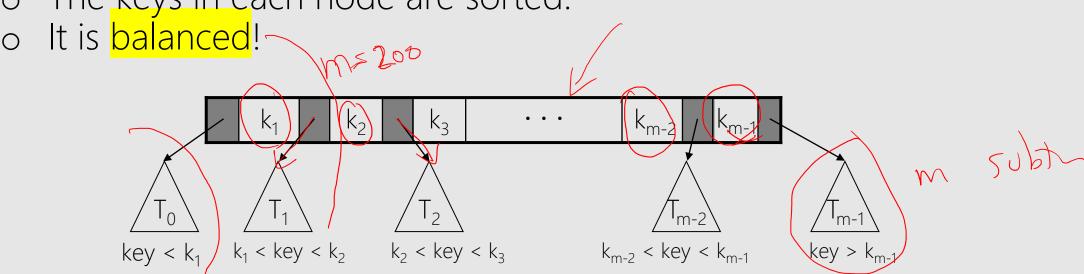


DBMS × INDEX × B-tree

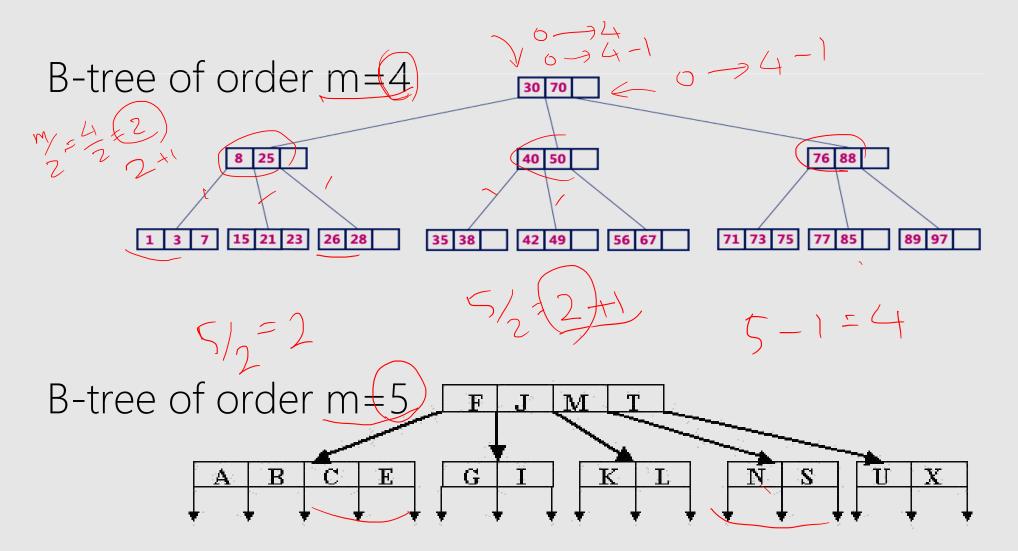
B-tree of order (m) (branching factor) is a tree in which:

o 0 ≤ #keys in root ≤ (m-1) o 0 ≤ #subtrees in root ≤ m ≤ (m-1) o (½ m) ≤ #keys in other nodes ≤ (m-1) o 1+(½ m) ≤ #subtrees in other nodes ≤ m,

o The keys in each node are sorted.



DBMS × INDEX × B-tree



DBMS × INDEX × B-tree

The height h of a B-tree of order m, with a total of n keys:

$$\log_m^{(n+1)} \le h \le 1 + \log_{\lceil m/2 \rceil}^{(n+1/2)}$$

If m = 300 and n = 16,000,000 then $h \neq 4$.

i.e., the worst case finding a key in such B-tree requires? accesses.

<u>INSERT</u> DELETE Overflow, more than m-1 keys

Underflow, less than m/2 keys

Empty B-tree of order m=3

Empty B-tree of order m=3



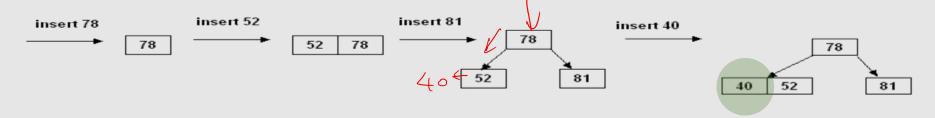
Empty B-tree of order m=3



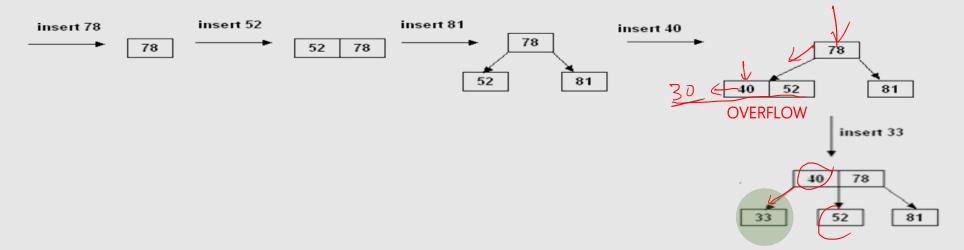
Empty B-tree of order m=3



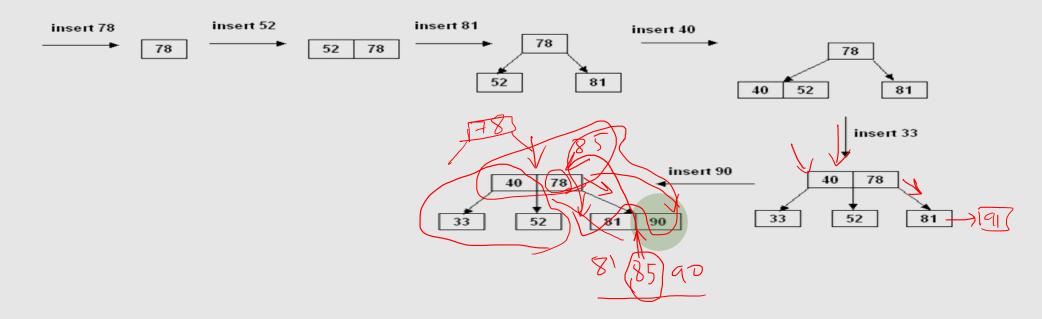
Empty B-tree of order m=3



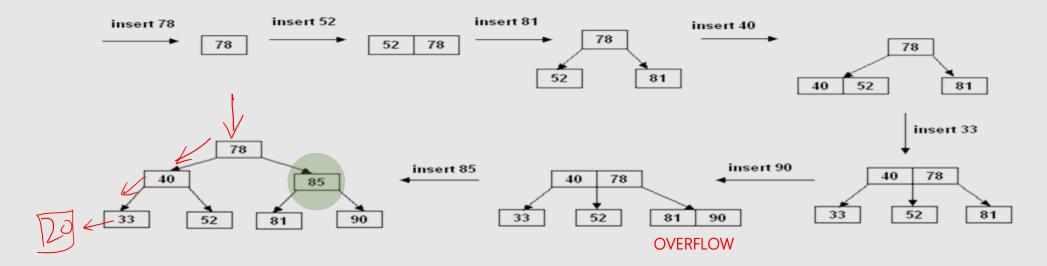
Empty B-tree of order m=3



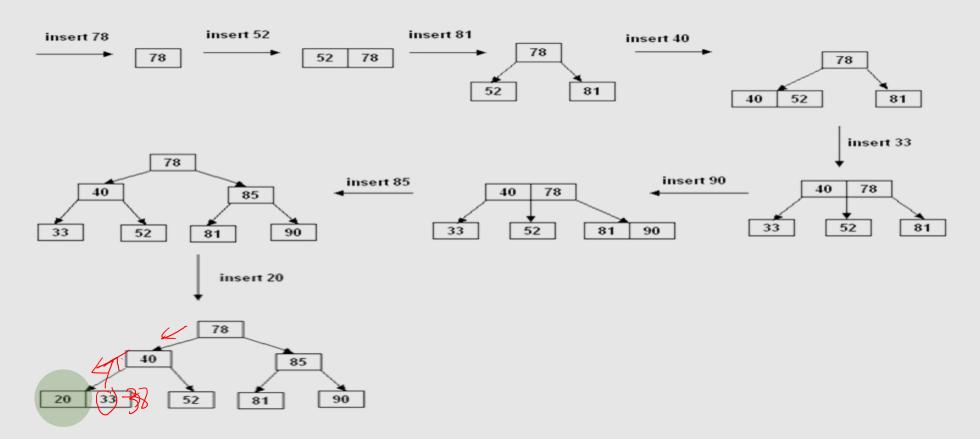
Empty B-tree of order m=3



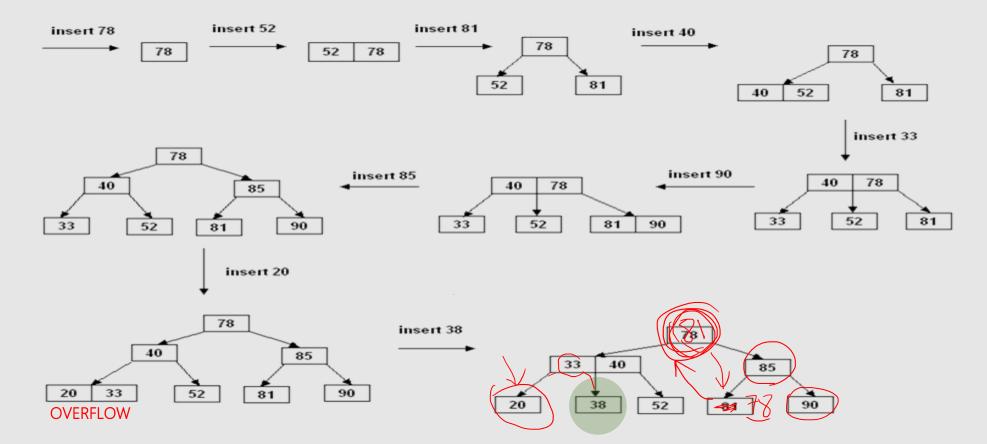
Empty B-tree of order m=3



Empty B-tree of order m=3



Empty B-tree of order $m=3_2$ Insert the keys 78, 52, 81, 40, 33, 90, 85, 20, and 38 in order



```
INSERT(key):
```

Find the correct spot in a <u>leaf node</u> and do insert.

WHILE OVERFLOW

Split it into two

IF the node has parent

Insert the middle key to the parent (propagate)

Create right and left siblings

ELSE

Create a new root node

```
B-tree × DELETE
```

DELETE can happen at <u>leaf</u> or <u>non-leaf!</u>

```
IF the key is in a leaf node

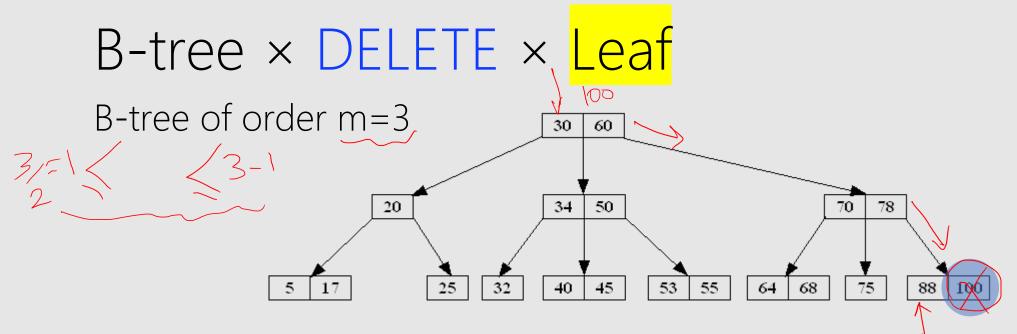
Delete the key ×

ELSE //non-leaf

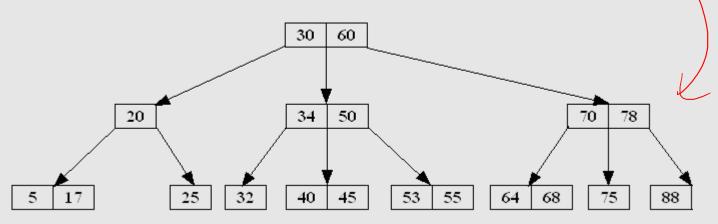
Replace it with a key in a leaf

Delete the key in the leaf
```

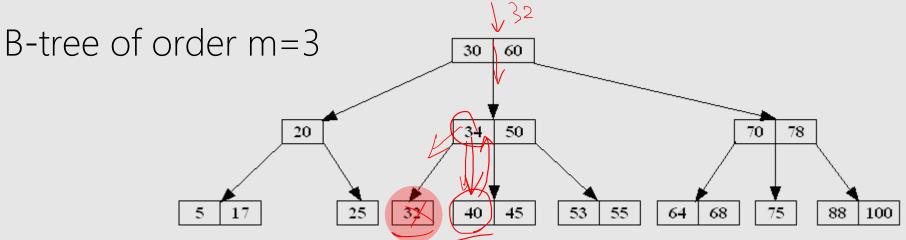
The actual delete always happen at leaf node.



Simple delete key in leaf node. There is no underflow.







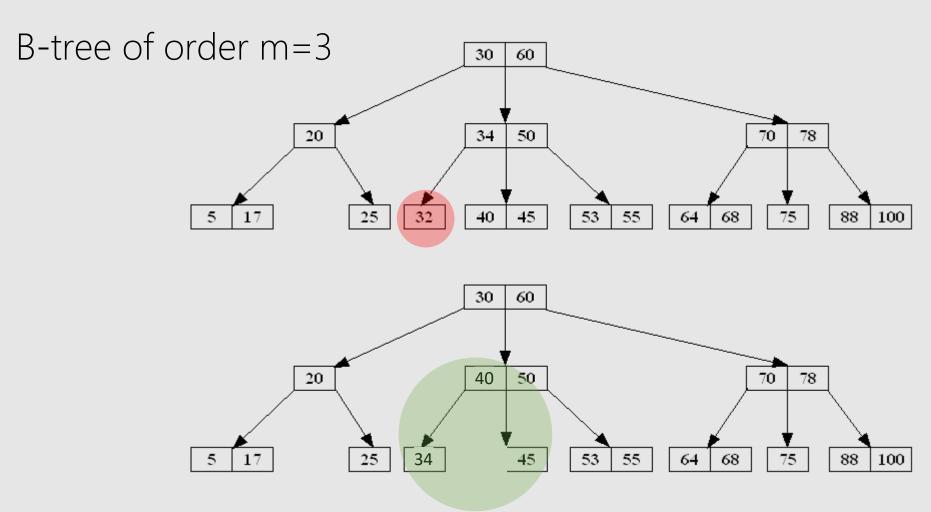
Delete the key, UNDERFLOW!

Merge with right | left sibling & parent key and sort: [34, 40, 45] OVERFLOW:

Split by middle key: [34], [45]

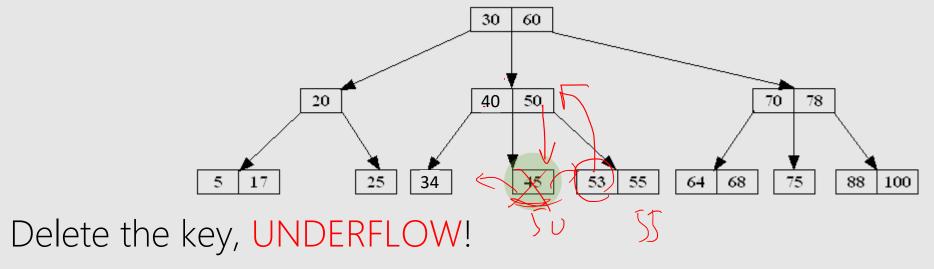
Movie middle key to parent: [40]

B-tree × DELETE × Leaf



B-tree × DELETE × Leaf

B-tree of order m=3

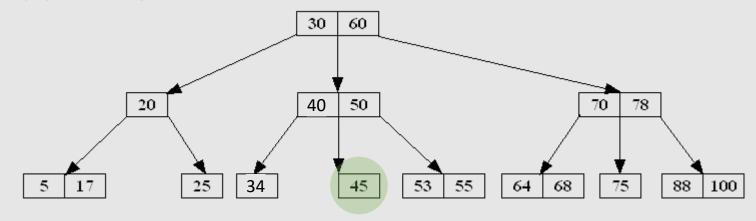


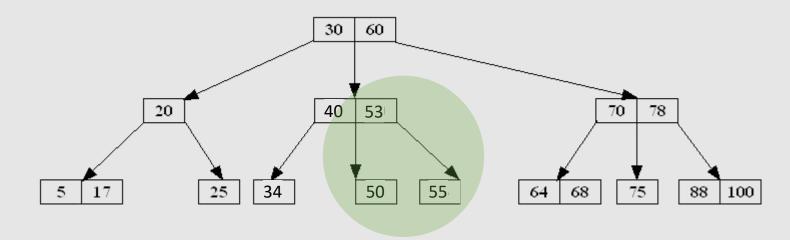
Merge with right | left sibling & parent key and sort: [50, 53, 55] OVERFLOW:

Split by middle key: [50], [55] Movie middle key to parent: [53]

B-tree × DELETE × Leaf

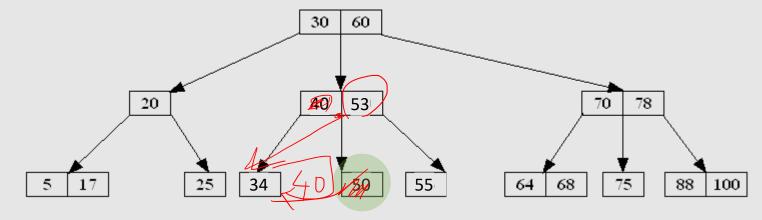
B-tree of order m=3





B-tree × DELETE × Leaf

B-tree of order m=3



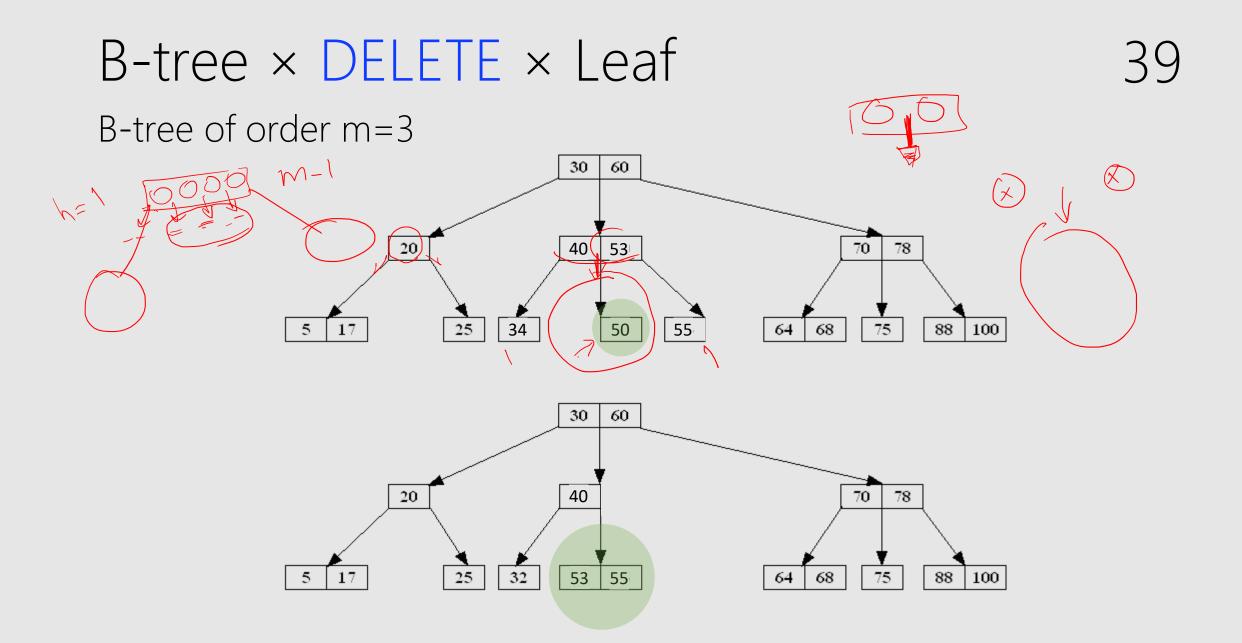
Delete the key, UNDERFLOW!

Merge with right | left sibling & parent key and sort: [53, 55]

OVERFLOW:

Split by middle key

Movie middle key to parent



B-tree × DELETE × Leaf

DELETE(key):

Find the key

IF the key is in a leaf node

Delete the key

IF (NOT root) & UNDERFLOW

· Merge with a adjacent sibling with more keys (right | left) & parent key

IF OVERFLOW

Split based on middle key

Replace middle key with the parent key

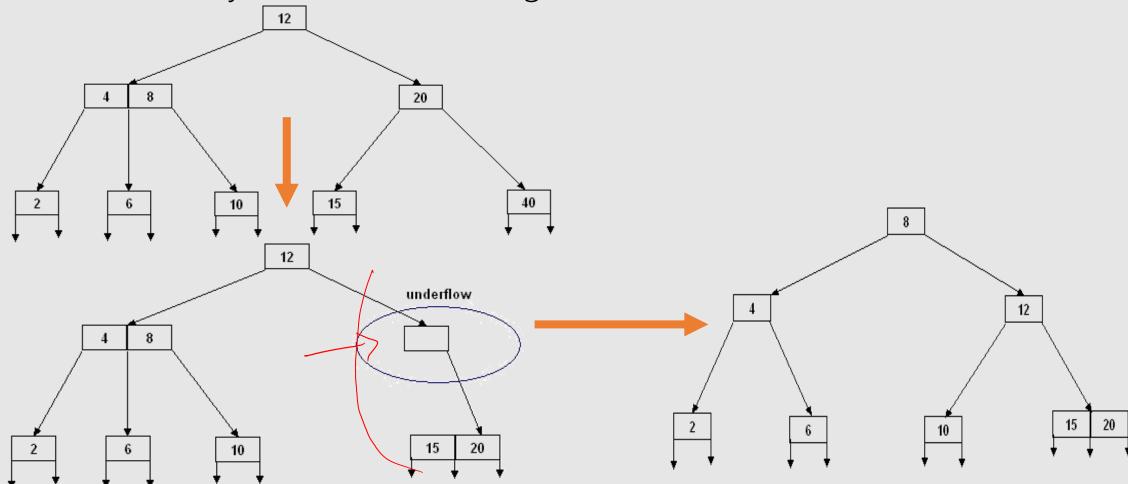
ELSE //parent node lost a key and might UNDERFLOW

IF UNDERFLOW in parent

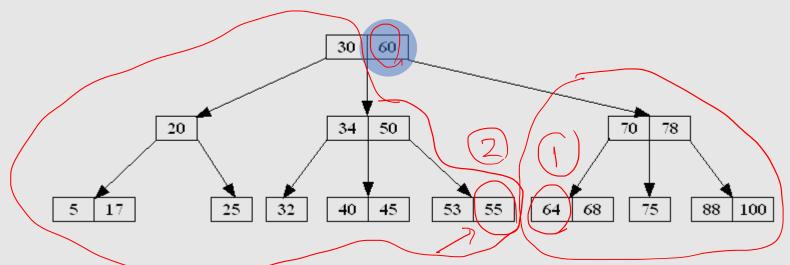
-GO-TO

B-tree × DELETE × Leaf

Delete the key 40 in the following B-tree of order 3:

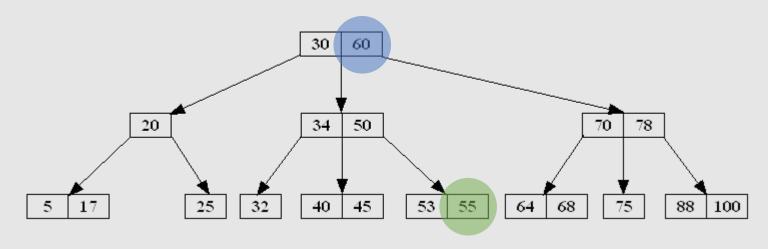


B-tree of order m=3



To replace the current key with a key in leaves, what would be the options?

B-tree of order m=3

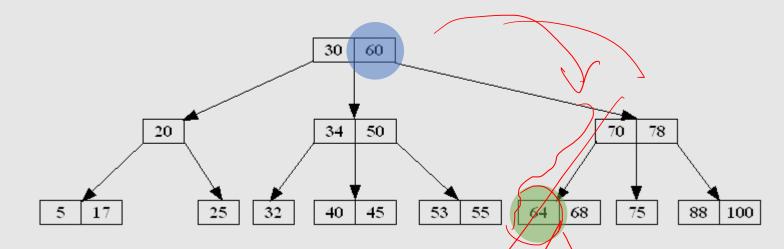


PREDECESSOR(key): Largest key less than the current key

Largest key in left subtree of the current key

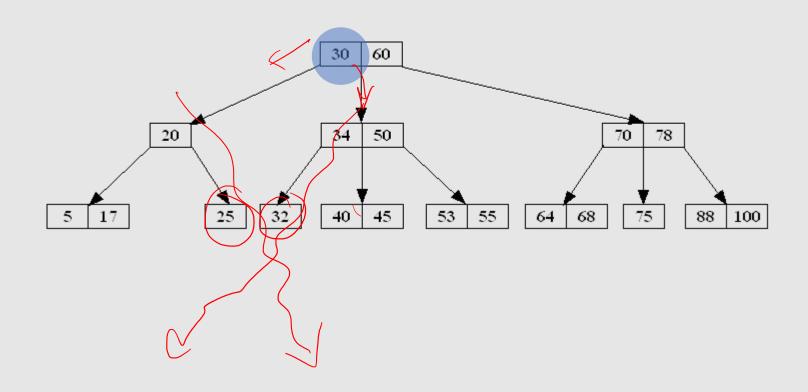
Right-most key in left subtree of the current key

B-tree of order m=3

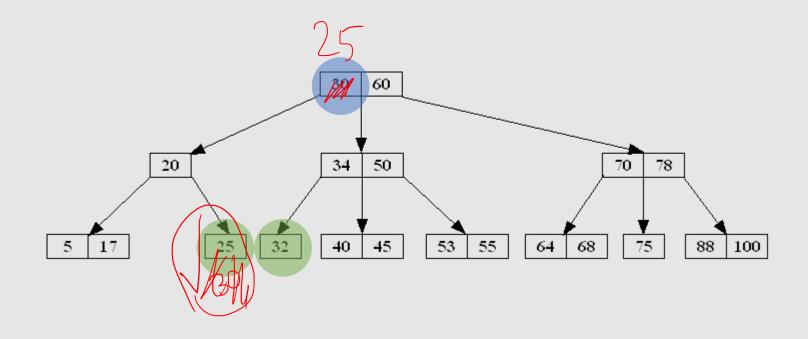


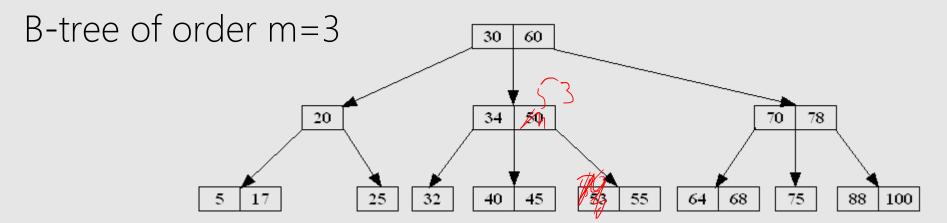
SUCCESSOR(key): Smallest greater than the current key
Smallest in right subtree of the current key
Left-most key in right subtree of the current key

B-tree of order m=3

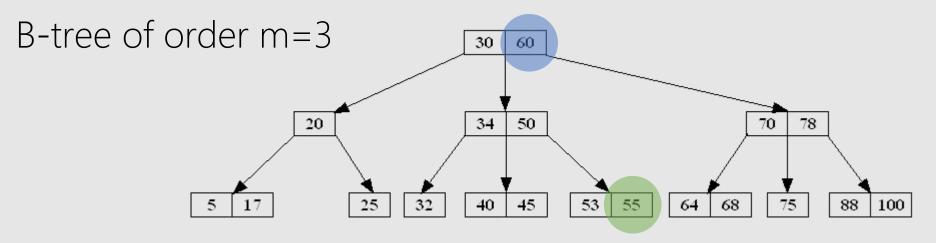


B-tree of order m=3

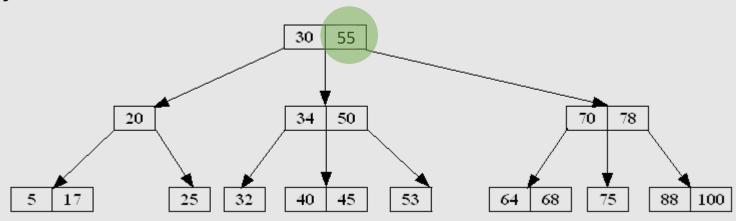


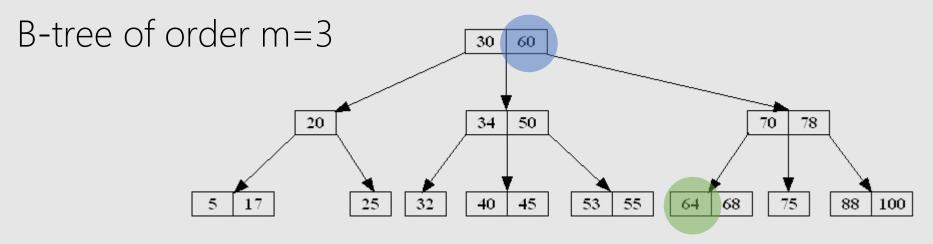


PREDECESSOR	Key	SUCCESSOR
17	20	25
25	30	32
32	34	40
45	50	(53)
55	60	64
68	70	75
75	78	88

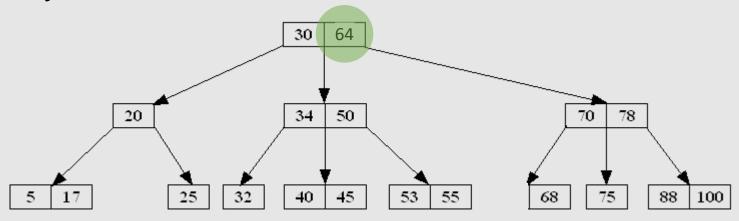


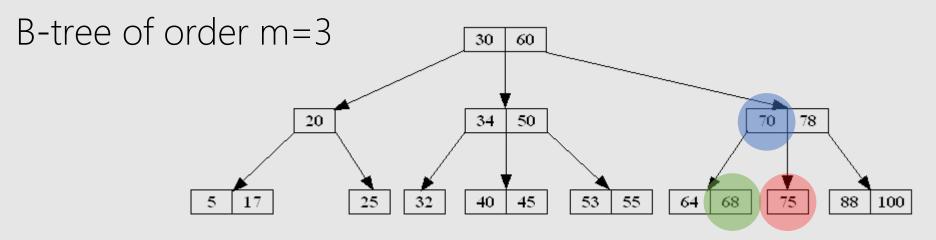
Replace key with PREDECESSOR in non-leaf node





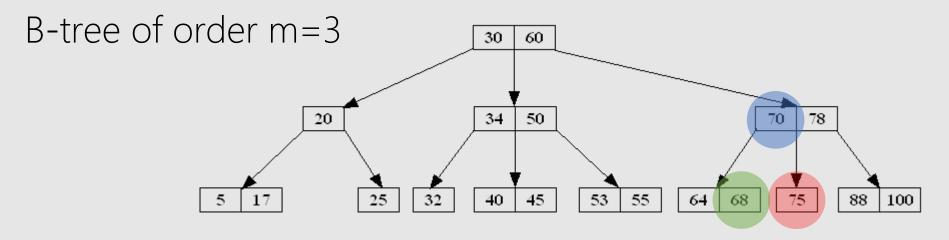
Or replace key with SUCCESSOR in non-leaf node

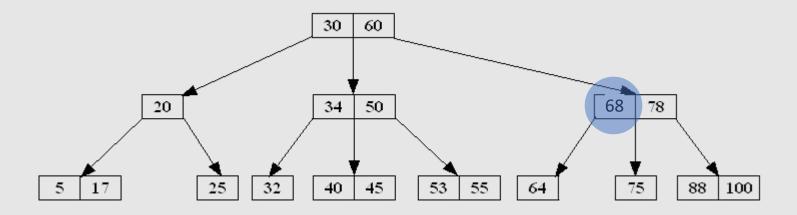


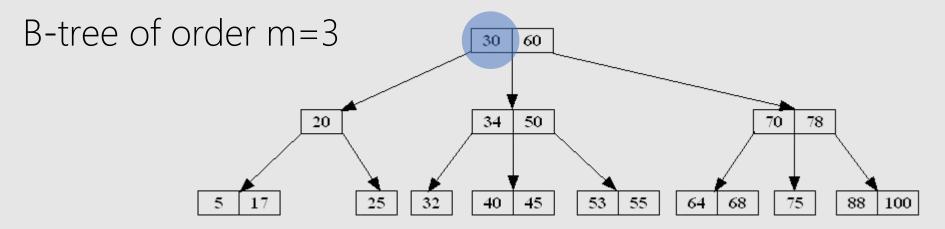


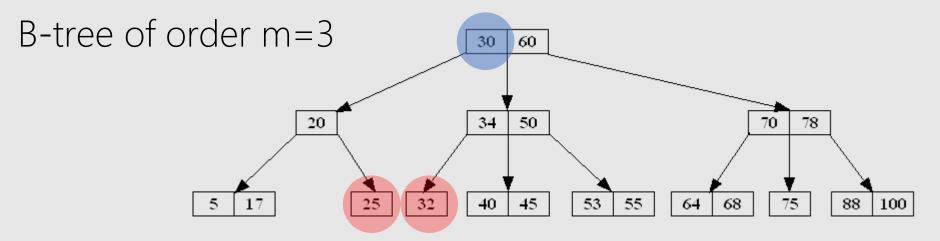
To choose between SUCCESSOR | PREDESSESOR:

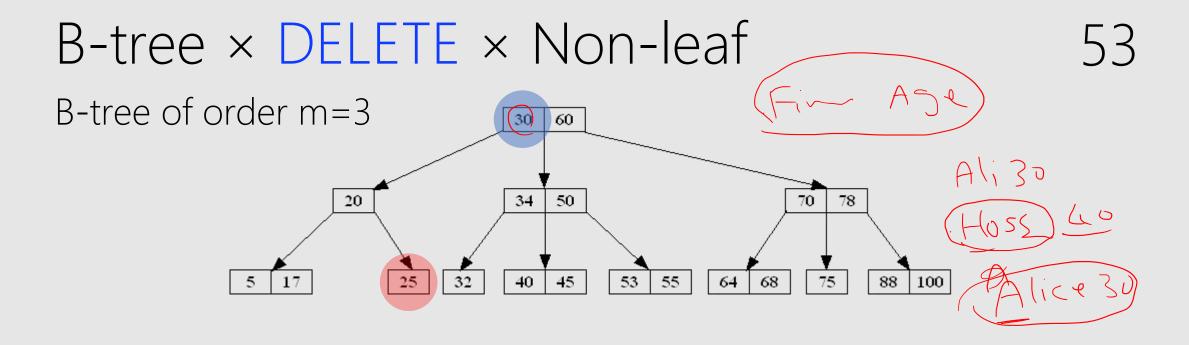
The one whose node is bigger.

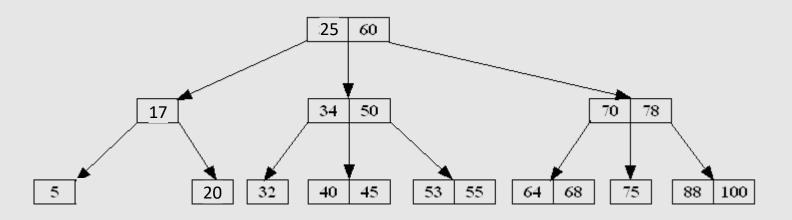












```
54
```

```
DELETE(key):
Find the key
IF the key is in a non-leaf node
  key' = PREDECESSOR(key)
  key" = SUCCESSOR(key)
  |F| |NODE(key')| >= |NODE(key'')|
      DELETE(key')
   ELSE
      DELETE(key'')
```

The actual delete always happen at leaf node.

DBMS × SQL × INDEX

55

SELECT * FROM Director WHERE LastName = 'Kubrick' AND FirstName = 'Stanley'

Which one?

- A) CREATE INDEX IX_LastName_FirstName ON Director(LastName, FirstName)
- B) CREATE INDEX IX_FirstName_LastName ON Director(FirstName, LastName)
- C) CREATE INDEX IX_FirstName ON Director(FirstName) 50%
- D) CREATE INDEX IX_LastName ON Director(LastName) 507
- E) (All
- F) A & B are the same

DBMS × SQL × INDEX

SELECT * FROM Director WHERE LastName = 'Kubrick' AND FirstName = 'Stanley'

Which one?

- A) CREATE INDEX IX_LastName_FirstName ON Director(LastName, FirstName) 100% helps
- A) CREATE INDEX IX_FirstName_LastName ON Director(FirstName, LastName) 100% helps
- A) CREATE INDEX IX_FirstName ON Director(FirstName)
- 50% helps. Finding FirstName is fast, but after that sequential search to find LastName
- A) CREATE INDEX IX_LastName ON Director(LastName)
- 50% helps. Finding LastName is fast, but after that sequential search to find FirstName
- A) All
- Having 4 indexes on a table is too much overhead
- A) A & B are the same
- The sorting in B-tree is different, but the effect (help) is the same.

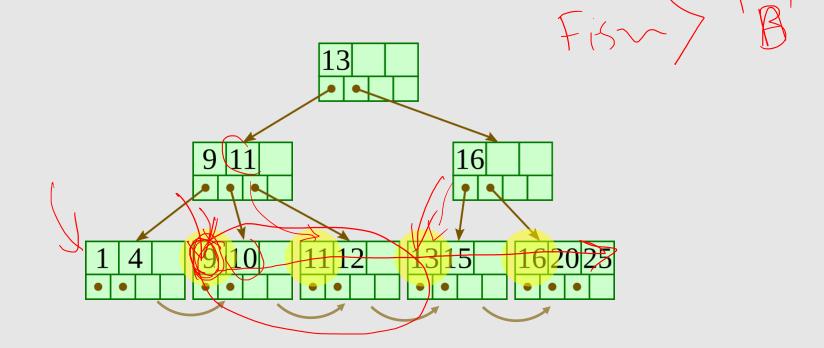
DBMS × INDEX × B+-Tree

B+-tree is an extension to B-tree in which

Leaf nodes has a copy of all parents key.

- Leaf nodes are linked together in order to support range

queries



DBMS × INDEX × B+-Tree

B+-tree is an extension to B-tree in which

- Leaf nodes has a copy of all parents key.
- Leaf nodes are linked together in order to support range queries

SELECT * FROM Movie WHERE ReleaseDate BETWEEN 1960 AND 2000

B+-tree is the de facto standard for indexing in DBMS

DBMS × INDEX × B+-Tree

CREATE INDEX IX_DateOfBirth_PlaceOfBirth ON Director(DateOfBirth, PlaceOfBirth)

Helps with which one?

- A) SELECT * FROM Director WHERE DateOfBirth = 1955 AND PlaceOfBirth = 'USA'
- B) SELECT * FROM Director WHERE DateOfBirth = 1955
- C) SELECT * FROM Director WHERE PlaceOfBirth = 'USA'
- D) SELECT * FROM Director WHERE DateOfBirth BETWEEN 1955 AND 1980
- E) ALL
- F) None

DBMS × INDEX × Best Practice

What columns should be indexed by default on any DB?

Why?

- A. Unique Indexes on Primary Keys

 SELECTs usually have primary keys in WHERE clause

 Joins are usually based on primary keys equal to foreign keys
- B. Unique Indexes on Candidate Keys
 To provide uniqueness check
 SELECTs usually have candidate keys in WHERE clause
- C. Indexes on Foreign Keys

Joins are usually based on primary keys equal to foreign keys

DBMS × INDEX × Book

```
2<sup>nd</sup> Ed.
```

CH08: Indexes in SQL

CH14: Index Structures (B-tree, HashTable, Bitmap, ...)

1st Ed.

CH06: The Database Language SQL (6.6.5 & 6.6.6)

CH13: Index Structures (B-tree, HashTable)

CH14: Multidimensional & Bitmap Indexes