Projet Analyse De Donnée

L3

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Content:

- Why Data Analyses
- Data Manipulation (Pandas Library)
- ➤ Data Visualisation (Matplotlib, Pyplot, Seaborn)
- > Linear Regression
- Principle Component Analysis
- ➤ Non-Negative Matrix Factorization
- Orthogonal Matching pursuit

NEEDS:

- ➤ Basic Python Skills (Lists, Dictionaries, Functions, methods,....)
- Working with DataFrames (Data Cleaning and manipulation with Pandas Library)
- Working with Matrices (Numpy Library)
- Mathematics behind Machine learning Techniques (Mostly probability and statistics)
- ➤ Machine learning library (Scipy or Sklearn)

QUESTION:

Input:

| longitude | latitude | housing_median_age | total_rooms | total_bedrooms | population | households | median_income | median_house_value | ocean_proximity |
|-----------|----------|--------------------|-------------|----------------|------------|------------|---------------|--------------------|-----------------|
| -122.23 | 37.88 | 41.0 | 880.0 | 129.0 | 322.0 | 126.0 | 8.3252 | 452600.0 | NEAR BAY |
| -122.22 | 37.86 | 21.0 | 7099.0 | 1106.0 | 2401.0 | 1138.0 | 8.3014 | 358500.0 | NEAR BAY |
| -122.24 | 37.85 | 52.0 | 1467.0 | 190.0 | 496.0 | 177.0 | 7.2574 | 352100.0 | NEAR BAY |
| -122.25 | 37.85 | 52.0 | 1274.0 | 235.0 | 558.0 | 219.0 | 5.6431 | 341300.0 | NEAR BAY |
| -122.25 | 37.85 | 52.0 | 1627.0 | 280.0 | 565.0 | 259.0 | 3.8462 | 342200.0 | NEAR BAY |

Output:

-121.32 39.43 18.0 1860.0 409.0 741.0 349.0 1.8672 ?? INLAND



QUESTION:

Input:



| species | margin1 | margin2 | margin3 | margin4 | margin5 | margin6 | margin7 | margin8 | texture55 | texture56 | texture57 | texture58 |
|-----------------------|----------|----------|----------|----------|----------|----------|----------|---------|---------------|-----------|-----------|-----------|
| Acer_Opalus | 0.007812 | 0.023438 | 0.023438 | 0.003906 | 0.011719 | 0.009766 | 0.027344 | 0.0 | 0.007812 | 0.000000 | 0.002930 | 0.002930 |
| Pterocarya_Stenoptera | 0.005859 | 0.000000 | 0.031250 | 0.015625 | 0.025391 | 0.001953 | 0.019531 | 0.0 | 0.000977 | 0.000000 | 0.000000 | 0.000977 |
| Quercus_Hartwissiana | 0.005859 | 0.009766 | 0.019531 | 0.007812 | 0.003906 | 0.005859 | 0.068359 | 0.0 | 0.154300 | 0.000000 | 0.005859 | 0.000977 |

Output:

0.000000 0.003906 0.023438 0.005859 0.021484 0.019531 0.023438 0.0 ... 0.000000 0.000977 0.000000 0.000000



Install Python

- https://www.python.org/
- > pip Python package management system: python3 -m pip --version
- > install jupyter notebook: python3 -m pip install -U jupyter
- > Install pandas: pip install pandas

- o The Jupyter Notebook is the original web application for creating and sharing computational documents.
- Pandas the main tool of data analyse
- o Pandas permits us to import data from various sources for example (CSV), and manipute them.

DataFrames:

https://insights.stackoverflow.com/survey

How to use Pandas to work with DataFrame......

- 1. How to read data from csv file,
- 2. Take a look at the datafram,
- 3. Where dataframe comes from, its equivalent in python
- 4. Series objects and accessing multi-columns
- 5. Indexing
- 6. Accessing rows in DataFrames
- 7. Setting index for data frame
- 8. Changing columns' names
- 9. Changing single row's values

Numpy:

As a Data Analyst how to collect data?

- > List?
- Collection of values
- ➤ Hold different types
- Change, add, remove
- > What we need more?
- ➤ Mathematical operations over collections
- > Speed

Numpy:

Body mass Index:

```
Height = [1.73, 1.68, 1.71, 1.89, 1.79]
Weight = [65.4, 59.2, 63.6, 88.4, 68.7]
Weight / Height ** 2
                                          Traceback (most recent call last)
TypeError
<ipython-input-43-0f6f8ba4f85f> in <module>
---> 1 Weight / Height ** 2
TypeError: unsupported operand type(s) for ** or pow(): 'list' and 'int'
                      Looping over elements?
           To Solve:
                                                      Not fast and efficient
```

Numpy (numeric python):

Solution?

nympy arrays:

- > Alternative to python lists
- > Calculations over entire arrays
- > Easy and Fast

To Install:

pip3 install numpy

Numpy

```
import numpy as np
np_height = np.array(Height)
np height
array([1.73, 1.68, 1.71, 1.89, 1.79])
np weight = np.array(Weight)
np_weight
array([65.4, 59.2, 63.6, 88.4, 68.7])
 bmi = np_weight / np_height**2
 bmi
 array([21.85171573, 20.97505669, 21.75028214, 24.7473475 , 21.44127836])
```

Numpy

Python is able to treat numpy arrays as single elements.

Where the speed comes from?

Numpy arrays collect values of the same type:

- Either integer
- Either float
- String
-

Numpy (Remarks)

```
np.array([1.0 , "Hossein" , True])
array(['1.0', 'Hossein', 'True'], dtype='<U32')</pre>
```

- Nympy array, is a data type in python.
- It has its own methods.
- These methods might act differently on arrays compared to other types.

Numpy (Remarks)

Example:

```
python_list = [1,2,3]
numpy_array = np.array([1,2,3])

python_list + python_list

[1, 2, 3, 1, 2, 3]
numpy_array+numpy_array
array([2, 4, 6])
```

Numpy (Subsetting)

Example:

```
bmi
array([21.85171573, 20.97505669, 21.75028214, 24.7473475 , 21.44127836])
                                               Referring to specific index
bmi[2]
21.750282138093777
                                                 Looking for specific values
bmi > 21
array([ True, False, True, True, True])
bmi[bmi<21]
array([20.97505669])
```

Numpy (2D)

```
type(np_height)
numpy.ndarray
np 2d = np.array([[1.73, 1.68, 1.71, 1.89, 1.79],
                 [65.4 , 59.2 , 63.6 , 88.4 , 68.7]])
np_2d
array([[ 1.73, 1.68, 1.71, 1.89, 1.79],
       [65.4 , 59.2 , 63.6 , 88.4 , 68.7 ]])
np_2d.shape
(2, 5)
```

Numpy (2D)

```
np 2d = np.array([[1.73, 1.68, 1.71, 1.89, 1.79],
                 [65.4 , 59.2 , 63.6 , 88.4 , 68.7]])
np_2d
array([[ 1.73, 1.68, 1.71, 1.89, 1.79],
      [65.4 , 59.2 , 63.6 , 88.4 , 68.7 ]])
np_2d[0]
array([1.73, 1.68, 1.71, 1.89, 1.79])
np_2d[0][2]
1.71
                                                           Two ways to select
np_2d[0,2]
1.71
np_2d[0,1:3]
array([1.68, 1.71])
```

Numpy (Basic Statistics)

```
np_2d = np.array([Height,
                  Weight])
np_2d
array([[ 1.73, 1.68, 1.71, 1.89, 1.79],
       [65.4 , 59.2 , 63.6 , 88.4 , 68.7 ]])
np.mean(np_2d[0,:])
1.7600000000000000
np.median(np_2d[0,:])
1.73
np.sum(np_2d[0,:])
8.8
```

Numpy (Data Generation)

```
height = np.round(np.random.normal(1.75,2.0, 5000),2)
weight = np.round(np.random.normal(10.32,15.0, 5000),2)

np_city = np.column_stack((height,weight))

np_city.shape
(5000, 2)
```

Numpy (Data Generation)

```
np.zeros([4,5],dtype = int)
array([[0, 0, 0, 0, 0],
       [0, 0, 0, 0, 0],
       [0, 0, 0, 0, 0],
       [0, 0, 0, 0, 0]])
np.ones([4,5], dtype = int)
array([[1, 1, 1, 1, 1],
       [1, 1, 1, 1, 1],
       [1, 1, 1, 1, 1],
       [1, 1, 1, 1, 1]])
     np.full((2,3), 6, dtype = int)
     array([[6, 6, 6],
            [6, 6, 6]]
```

Numpy (Dtype)

> Python types: int, float, bool,...

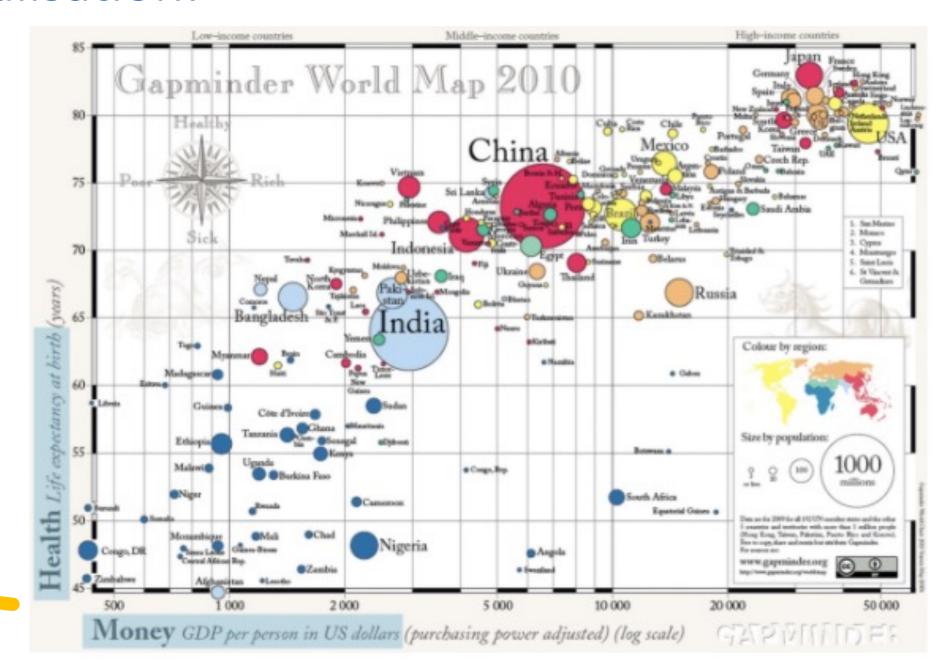
Their size depends on the platform they are applied to...

> Dtypes: numpy numerical types are instances of dtype objects. The numpy types have fixed-sizes.

np.int32, np.int64, np.bool8, np.float32, np.float64

```
z = np.zeros([2,3], dtype = np.bool8)
z
array([[False, False, False],
       [False, False, False]])
type(z)
numpy.ndarray
z.dtype
dtype('bool')
```

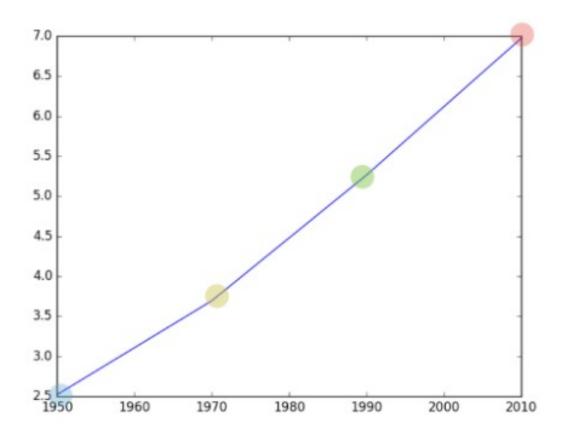
Data Visualisation:



The most important visualization library: Matplotlib:

```
import matplotlib.pyplot as plt
                    years = [1950, 1970, 1990, 2010]
                    pop = [2.519, 3.692, 5.263, 6.972]
                    plt.plot(years , pop)
                    plt.show()
                     7
                     6
                     5
                     4
                     3
                       1950
                              1960
                                    1970
                                           1980
                                                  1990
                                                        2000
                                                               2010
```

plt.plot():

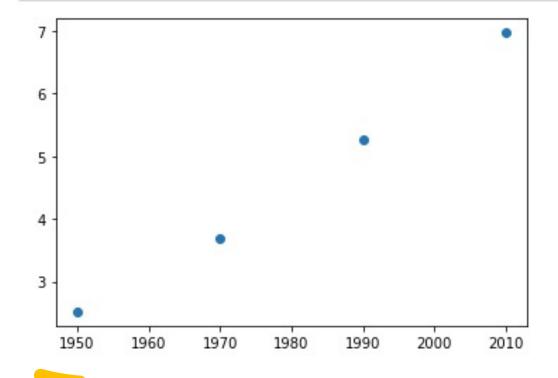


```
year = [1950 , 1970 , 1990 , 2010]
pop = [2.519, 3.692, 5.263, 6.972]
```

plt.scatter():

```
years = [1950,1970,1990,2010]
pop = [2.519, 3.692, 5.263, 6.972]
```

```
plt.scatter(years , pop)
plt.show()
```

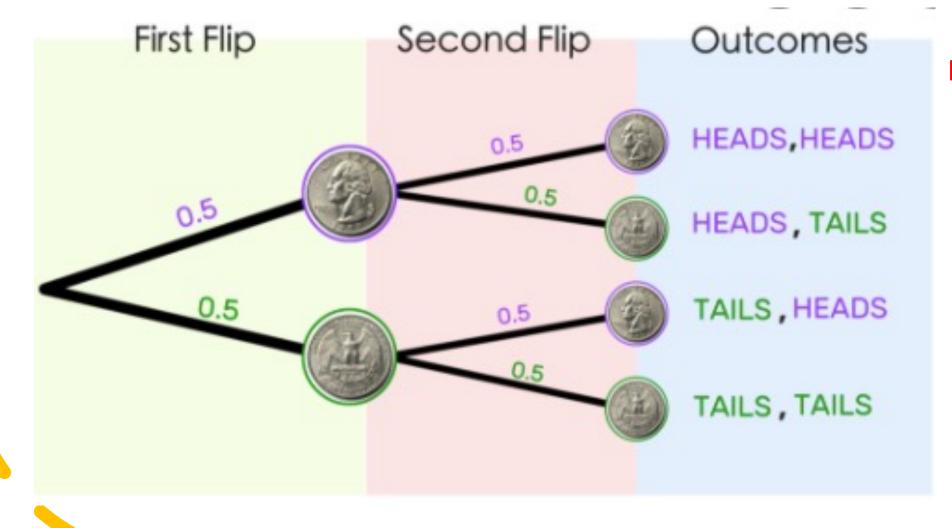


Scatter plot is used when we need to measure the correlation between two attributes.

plt.scatter():

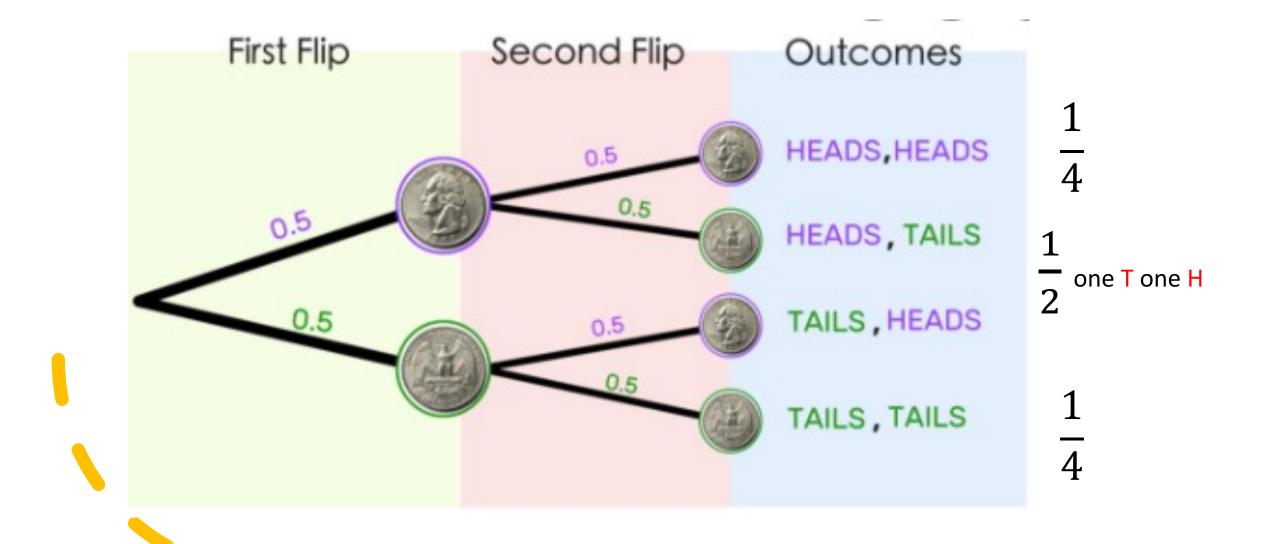
```
np.corrcoef(years, pop)
array([[1. , 0.99664316],
       [0.99664316, 1.
import scipy.stats as st
st.pearsonr(years, pop)
(0.996643163032238, 0.0033568369677620113)
  Correlation
                        P-value
```

P-Value:



Probabilities?

P-Value:



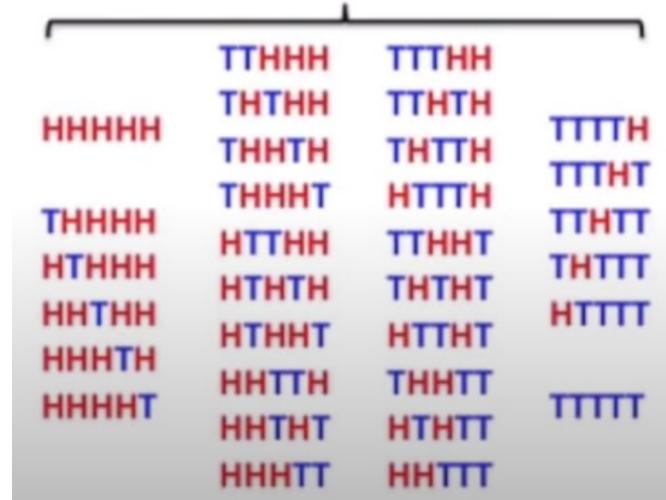
P-Value (flipping a coin 5 times):

$$p(HHHHHH) = \frac{1}{32}$$

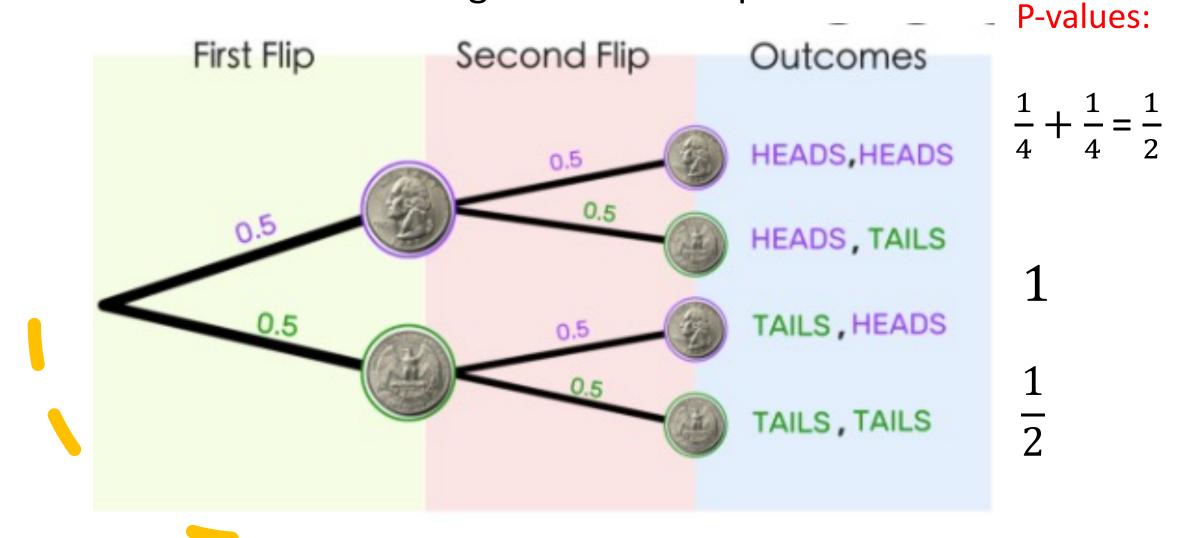
$$p(TTTTT) = \frac{1}{32}$$

Outcomes

$$p - value(HHHHHH) = \frac{1}{32} + \frac{1}{32} = 0.0625$$



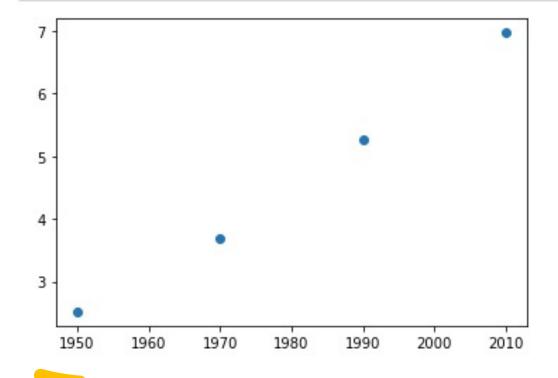
P-Value: probability that random chance generated the data or somethig else that is equal or rarer.



plt.scatter():

```
years = [1950,1970,1990,2010]
pop = [2.519, 3.692, 5.263, 6.972]
```

```
plt.scatter(years , pop)
plt.show()
```

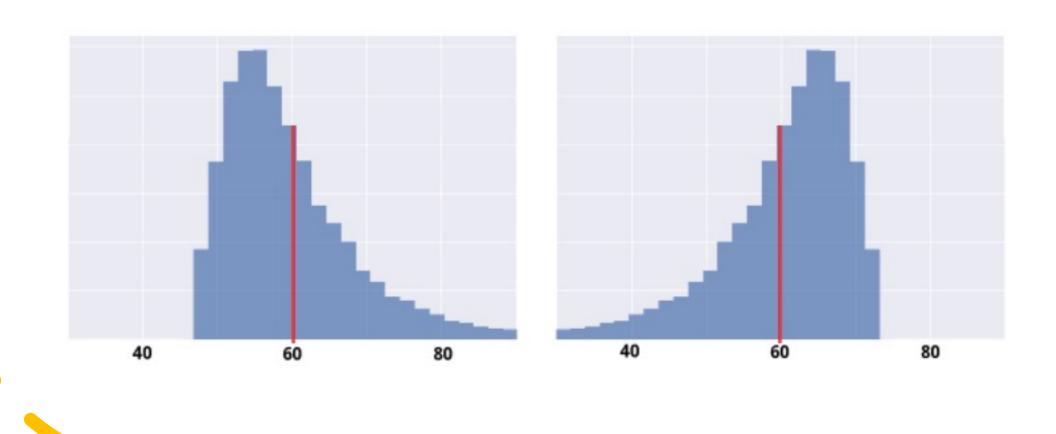


Scatter plot is used when we need to measure the correlation between two attributes.

plt.hist() :

```
values = [0,0.6,1.4,1.6,2.2,2.5,2.6,3.2,3.5,3.9,4.2,6]
plt.hist(values , bins = 3)
(array([4., 6., 2.]),
 array([0., 2., 4., 6.]),
 <BarContainer object of 3 artists>)
 6
 5
 4
 3
 2 .
                 2
                       3
                                    5
```

plt.hist():



Distribution of Data:

- ➤ Which is the most frequent data? statistics.mode()
- > The data is centered around which point? Nupmy.mean()
- ➤ What is the value observed in 50% of the time? Numpy.median()
- ➤ How vary the values are ? np.std()

Distribution of Data:

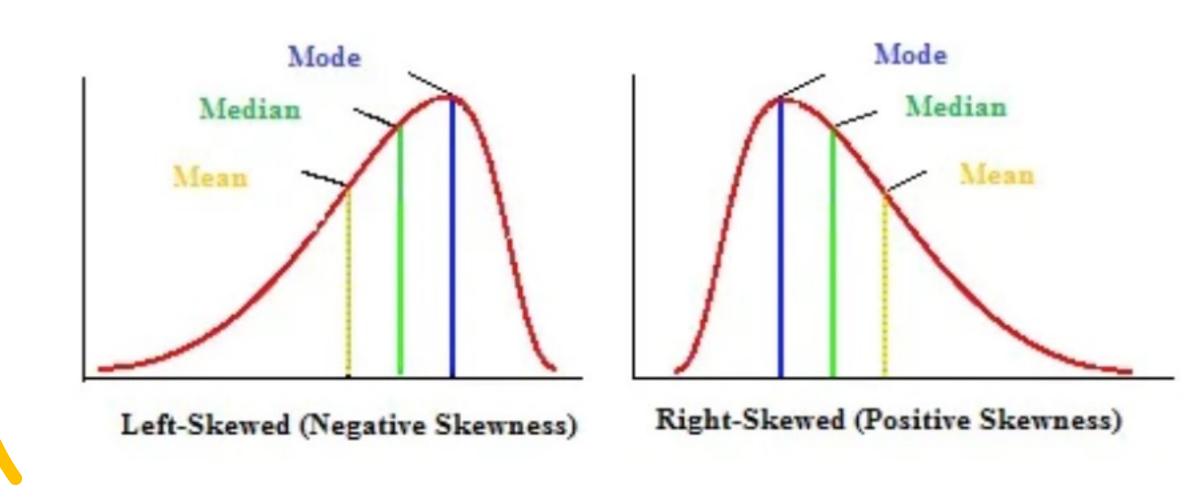
Most of the time it takes 80 mins Half of the times it takes 80 mins On average it takes 80 mins How long does it take to go from City A to city B



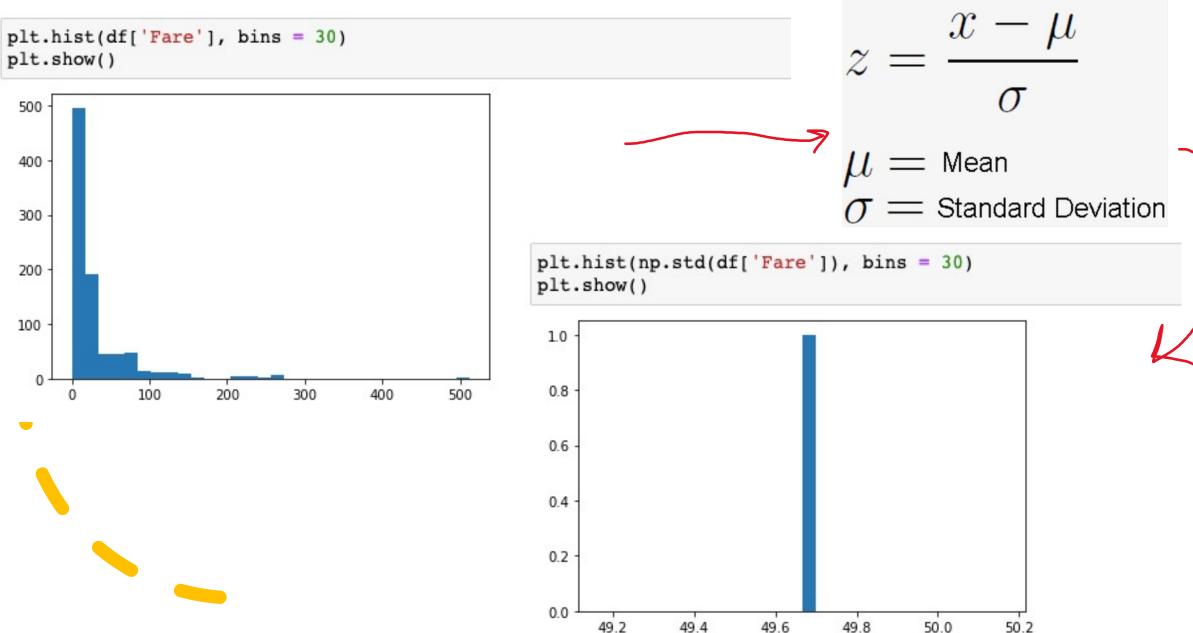
Distribution of Data:

```
values
[0, 0.6, 1.4, 1.6, 2.2, 2.5, 2.6, 3.2, 3.5, 3.9, 4.2, 6]
                                                              mode
import numpy as np
np.mean(values)
2.641666666666666
                                                               50% 50%
np.median(values)
2.55
                                                                median
import statistics as sts
sts.mode(values)
                                                                   mean
```

Distribution of Data:



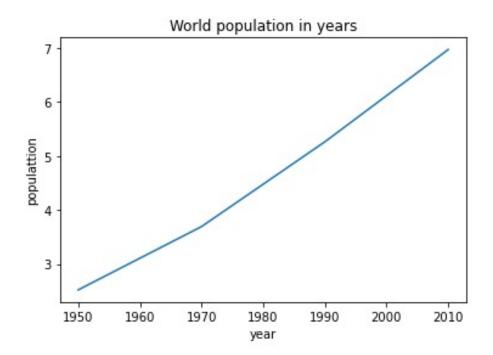
Distribution of Data:



- ➤ Add labels to the axis: plt.xlabel(), plt.ylabel()
- ➤ Add Title to the plot : plt.title()
- ➤ Changing values one the axis: plt.xticks(), plt.yticks()
- ➤ Labeling values on the axis

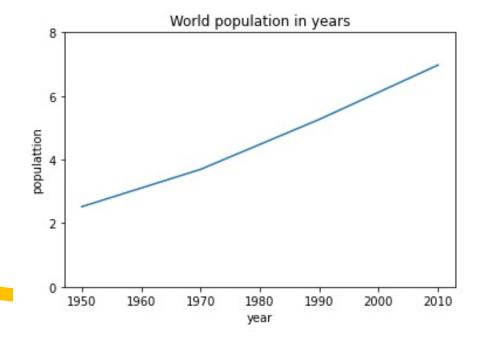
```
years = [1950,1970,1990,2010]
pop = [2.519, 3.692, 5.263, 6.972]
np_years = np.array(years)
np_pop = np.array(pop)
plt.plot(np_years , np_pop)
plt.xlabel('year')
plt.ylabel('populattion')
plt.title('World population in years')
```

Text(0.5, 1.0, 'World population in years')



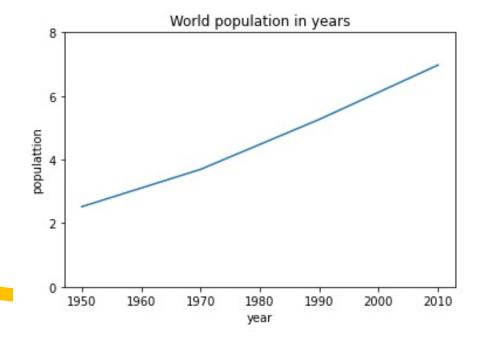
```
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pop = [2.519, 3.692, 5.263, 6.972]
np_years = np.array(years)
np_pop = np.array(pop)
plt.plot(np_years , np_pop)
plt.xlabel('year')
plt.ylabel('populattion')
plt.yticks([0,2,4,6,8])
plt.title('World population in years')
```

Text(0.5, 1.0, 'World population in years')



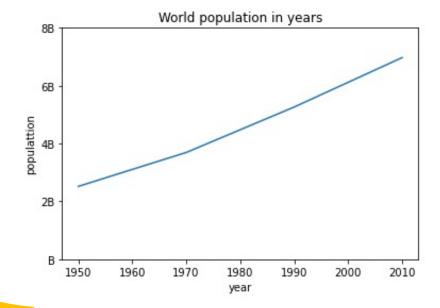
```
years = [1950,1970,1990,2010]
pop = [2.519, 3.692, 5.263, 6.972]
np_years = np.array(years)
np_pop = np.array(pop)
plt.plot(np_years , np_pop)
plt.xlabel('year')
plt.ylabel('populattion')
plt.yticks([0,2,4,6,8])
plt.title('World population in years')
```

Text(0.5, 1.0, 'World population in years')



```
years = [1950,1970,1990,2010]
pop = [2.519, 3.692, 5.263, 6.972]
np_years = np.array(years)
np_pop = np.array(pop)
plt.plot(np_years , np_pop)
plt.xlabel('year')
plt.ylabel('populattion')
plt.yticks([0,2,4,6,8],['B','2B','4B','6B','8B'])
plt.title('World population in years')
```

Text(0.5, 1.0, 'World population in years')



Machine Learning:

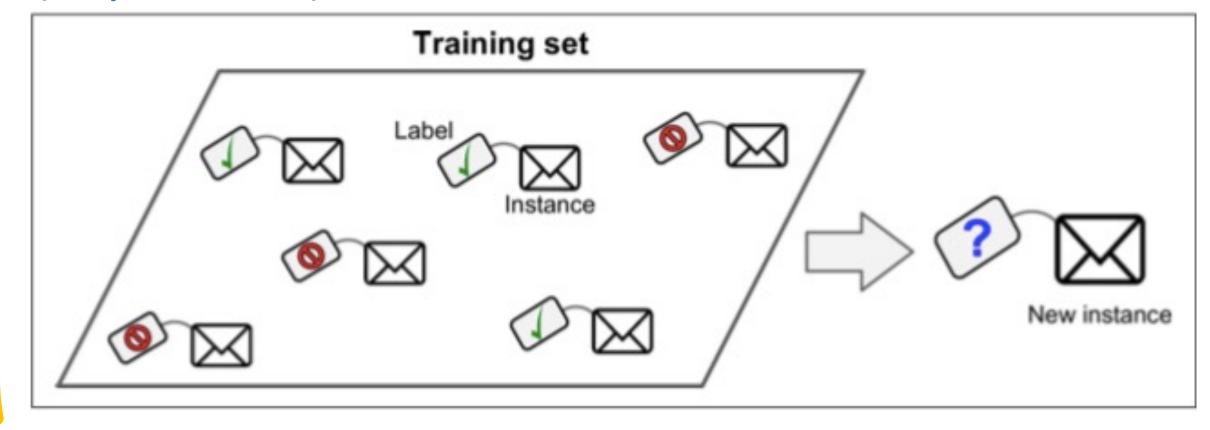
How you write a code with traditional programming technique to detect spams?

- > What a spam looks like, what are the patterns,
- ➤ Write a detection algorithm for each pattern,... .

Problem??

There is an infinite number of patterns!

ML (Supervised):



In ML, the model will learn (based on some examples) which patterns are representative of a spam.

Classification

ML (Supervised):

Value



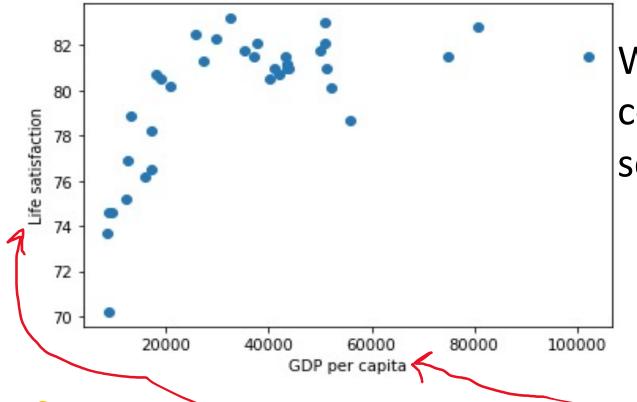
Given a set of Instances and their corresponging value, we can quess what is the value of a newly entered instance.

Regression

| | Country GDP per capita Life sat | | Life satisfaction |
|---|---------------------------------|-----------|-------------------|
| 0 | Australia | 50961.865 | 82.1 |
| 1 | Austria | 43724.031 | 81.0 |
| 2 | Belgium | 40106.632 | 80.5 |
| 3 | Brazil | 8669.998 | 73.7 |
| 4 | Canada | 43331.961 | 81.5 |
| 5 | Chile | 13340.905 | 78.9 |
| 6 | Czech Republic | 17256.918 | 78.2 |

Given a GDP per capita in a country, can you guess what is the life satisfaction index?

```
import numpy as np
plt.scatter(data['GDP per capita'] , data['Life satisfaction'])
x = np.array([1000 , 100000])
plt.xlabel('GDP per capita')
plt.ylabel('Life satisfaction')
plt.show()
```

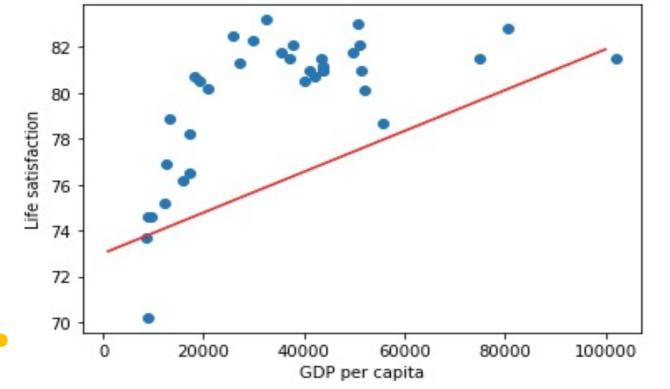


What is the simplest and common pattern in the scatter plot?

$$y = \theta_0 + \theta_1 x$$

```
import numpy as np
plt.scatter(data['GDP per capita'] , data['Life satisfaction'])
x = np.array([1000 , 100000])
t_0 = 73

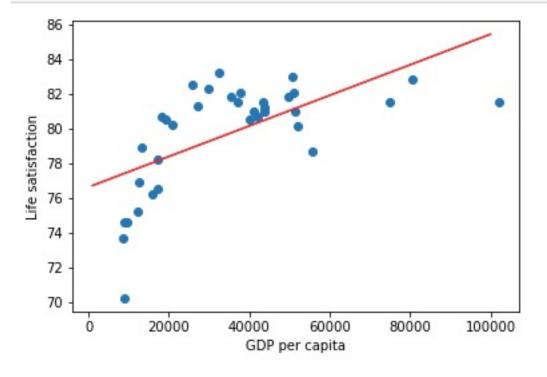
t_1 = 8.9e-05
plt.plot(x , t_0 + t_1*x , c = 'red')
plt.xlabel('GDP per capita')
plt.ylabel('Life satisfaction')
plt.show()
```



life satisfaction = $\theta_0 + \theta_1 * GDP per Capita$



```
import numpy as np
plt.scatter(data['GDP per capita'] , data['Life satisfaction'])
x = np.array([1000 , 100000])
t_0 = 76.61443338
t_1 = 8.82017196e-05
plt.plot(x , t_0 + t_1*x , c = 'red')
plt.xlabel('GDP per capita')
plt.ylabel('Life satisfaction')
plt.show()
```



life satisfaction = $\theta_0 + \theta_1 * GDP per Capita$

ML (Linear Assumption):

| GDP per capita | Life satisfaction |
|----------------|-------------------|
| 50961.865 | 82.1 |
| 43724.031 | 81.0 |
| 40106.632 | 80.5 |
| 8669.998 | 80.5 73.7 |
| 43331.961 | 81.5 |
| 13340.905 | 78.9 |
| 17256.918 | 78.2 |
| 52114.165 | 80.1 |
| 17288.083 | 76.5 |
| 41973.988 | 80.7 |

$$\hat{\mathbf{y}}^{(i)} = \theta_0 + \theta_1 \times \mathbf{x}^{(i)}$$

Main assumption: The data follows a linear model:

$$life\ satisfaction = \theta_0 + \theta_1 * GDP\ per\ Capita$$

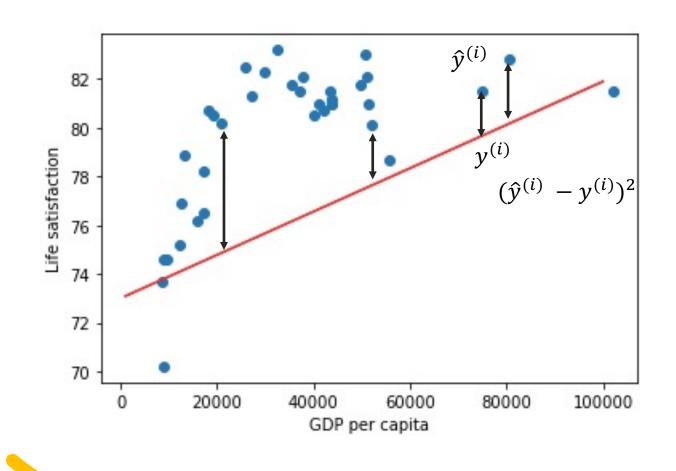
➤ How you know which values make your model perform best?

- Fitness Function
- Cost Function (typically used for linear regression problems.)

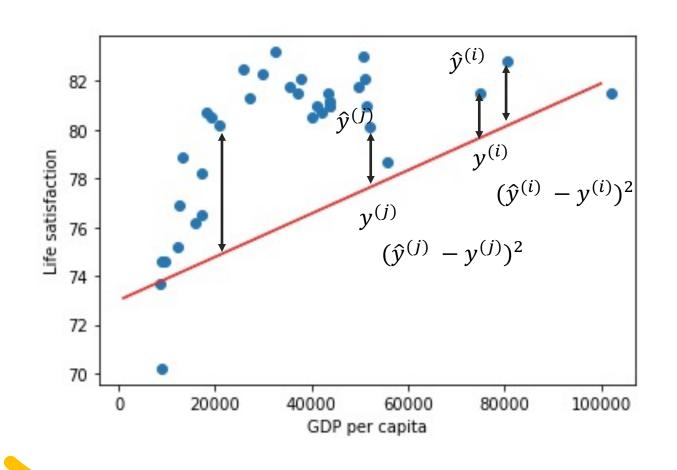
Linear Regression algorithm comes into play:

you feed it your training examples and it finds the parameters that make the linear model fit best to your data. This is called *training* the model.

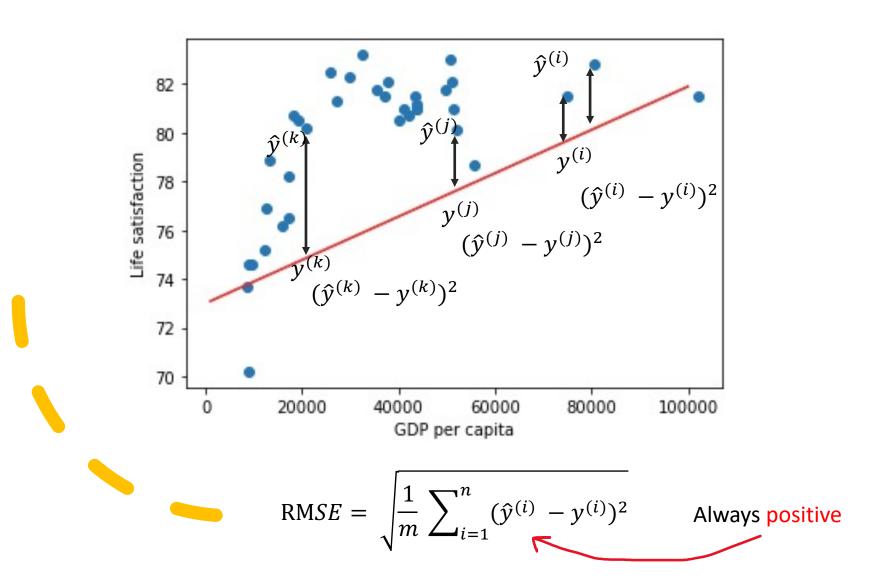
Cost Function:



Cost Function:



Cost Function: Root Mean Square Error



Sklearn (Python library for sklearn)

```
from sklearn.linear_model import LinearRegression
```

```
model = LinearRegression()
```

```
model.fit(data[['GDP per capita']], data[['Life satisfaction']])
```

Model Training

Sklearn (Python library for sklearn)

```
model.predict(data[['GDP per capita']])
array([[81.10935751],
       [80.47096811],
       [80.15190729],
       [77.37914212]
       [80.43638686],
       [77.79112415],
       [78.13652323],
       [81.21099235],
       [78.13927203],
       [80.3166113],
       [79.9374337],
       [80.23039615],
       [78.20773465],
       [77.69401308],
       [81.09989505],
               Model Prediction
```

| Life satisfaction | | |
|-------------------|------|--|
| 0 | 82.1 | |
| 1 | 81.0 | |
| 2 | 80.5 | |
| - 3 | 73.7 | |
| 4 | 81.5 | |
| 5 | 78.9 | |
| 6 | 78.2 | |
| 7 | 80.1 | |
| 8 | 76.5 | |
| 9 | 80.7 | |
| 10 | 82.1 | |
| 11 | 81.0 | |
| 12 | 80.7 | |
| 13 | 75.2 | |
| 14 | 83.0 | |
| 15 | 81.0 | |

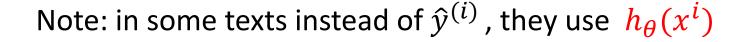
ML (Example): Predictor (A combination of attributes) Life satisfaction GDP per capita Target variable 50961.865 82.1 43724.031 81.0 Training (Minimizing RMSE) 40106.632 80.5 **Predictions** 8669.998 73.7 Samples 43331.961 81.5 [[81.10935751], 13340.905 78.9 [80.47096811], [80.15190729], 17256.918 78.2 [77.37914212], 52114.165 80.1 [80.43638686], [77.79112415], 76.5 17288.083 [78.13652323], [81.21099235], 41973.988 80.7 [78.13927203], [80.3166113], Assumption of Linearity

ML:

Note: In general their might be more than one attribute:

- \succ In this case, the first attribute of simple (i) is represented by variable $x_1^{(i)}$,
- \succ The second attribute would be $x_2^{(i)}$
-
- \succ The attribute p would be $x_p^{(i)}$

$$\hat{y}^{(i)} = \theta_0 + \theta_1 \times x_1^{(i)} + \theta_2 \times x_2^{(i)} + \dots + \theta_p \times x_p^{(i)}$$
Hyperplane



How the training part works? (The minimization of RMSE)

Min RMSE =
$$\sqrt{\frac{1}{m} \sum_{i=1}^{n} (\hat{y}^{(i)} - y^{(i)})^2}$$

Is equal to Min
$$(\theta^T X - y)^2$$

$$\theta = \begin{bmatrix} \theta_0 & \theta_1 & \theta_2 & \dots & \theta_p \end{bmatrix} \qquad X = \begin{pmatrix} 1 & x_1^1 & x_2^1 & \dots & x_p^1 \\ 1 & x_1^2 & x_2^2 & \dots & x_p^2 \\ \vdots & \vdots & \dots & \vdots & \vdots \\ 1 & x_1^n & x_2^n & \dots & x_p^n \end{pmatrix} \qquad y = \begin{bmatrix} y^{(1)} \\ y^{(2)} \\ y^{(3)} \\ \vdots \\ y^{(n)} \end{bmatrix}$$

How the training part works? (The minimization of RMSE)

$$Min \quad (\theta^T X - y)^2$$

$$\arg\min_{\theta\in\mathbb{R}^{p+1}} (\theta X - Y)^T (\theta X - Y)$$

$$\nabla_{\theta}(\theta X - Y)^{T} (\theta X - Y) = 0$$

$$-2X^{T}(y - \theta X) = 0$$

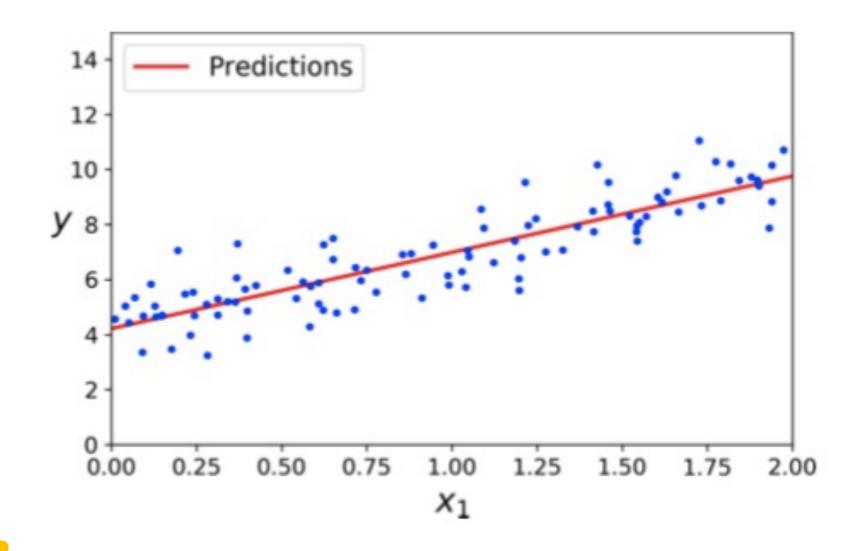
Normal Equation

$$\theta = (X^T X)^{-1} X^T y$$

It has a solution only when $(X^T X)^{-1}$ is inversible (when it's determinant is non-zero).

Let's test the normal equation by generating random data that follow linear pattern:

```
import numpy as np
                                                           Predictor
X = 2 * np.random.rand(100, 1)
y = 4 + 3 * X + np.random.randn(100, 1)
                                                           Target Variable
                 X
                                                  у
                 array([[0.10797752],
                                                  array([[ 3.5573093 ],
                         [0.72385904],
                                                           7.87380775],
                         [0.42813739],
                                                           7.2598704 ],
                         [1.41056299],
                                                           6.19588811],
                         [1.28648117],
                                                           9.13845766],
                                                           4.230945321,
                         [0.21776623],
                                                           8.61517587],
                         [1.03717871],
                                                           4.21443654],
                         [0.365245],
                                                           6.3025794 ],
                         [0.20016469],
                                                          [ 4.38441334],
                         [0.20727274],
```



```
X_b = np.c_[np.ones((100, 1)), X] # add x0 = 1 to each instance Create matrix X theta_best = np.linalg.inv(X_b.T.dot(X_b)).dot(X_b.T).dot(y)
```

Predictor

```
X b
                  , 0.10797752],
array([[1.
                  , 0.72385904],
       [1.
                                               theta_best
       [1.
                  , 0.42813739],
                  , 1.41056299],
       [1.
                  , 1.28648117],
       [1.
                                               array([[4.06669028],
       [1.
                  , 0.21776623],
                                                        [2.9236695 ]])
                  , 1.03717871],
       [1.
       [1.
                  , 0.365245 ],
                  , 0.20016469],
       [1.
                  , 0.20727274],
       [1.
```

ML (Exercise):

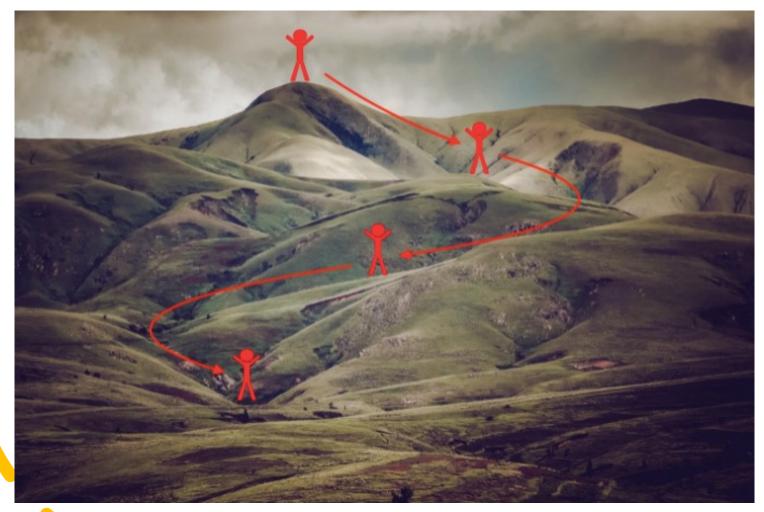
Calculate normal equation for the dataset of GDP per capita / Life satisfaction.

ML (Gradient Descent):

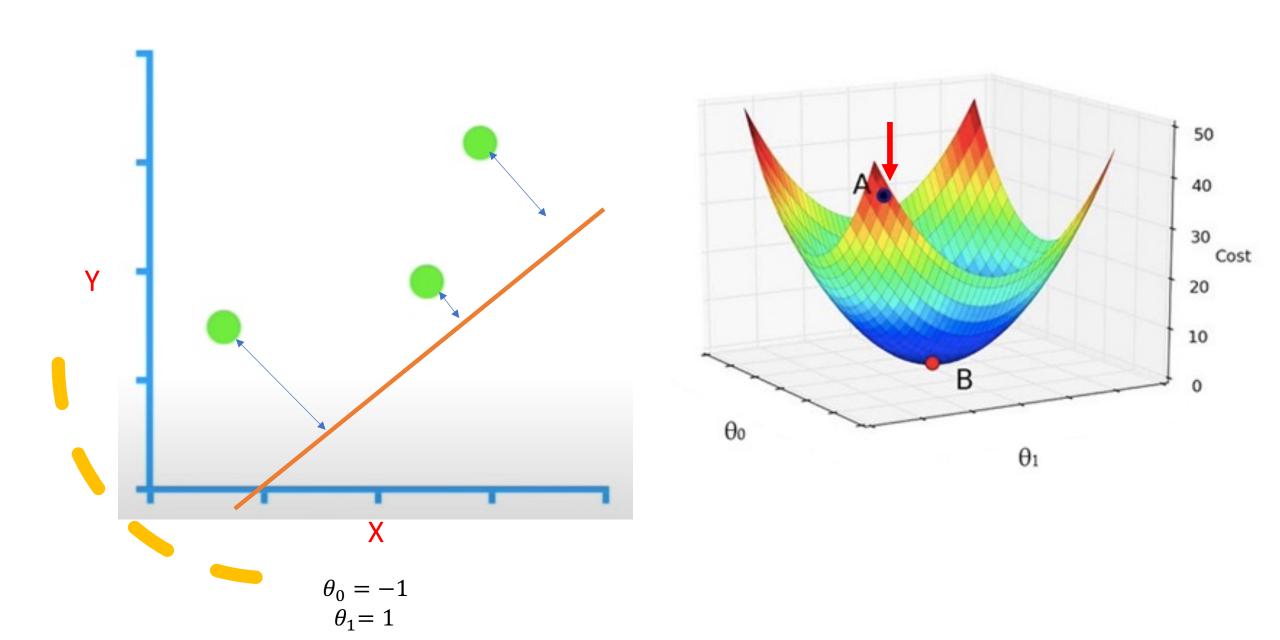
- > Problems with normal equations:
- 1. In many real cases $(X^TX)^{-1}$ is not invertible,
- 2. Even if it is for bid data sets the computational cost is $O(n^3)$ or $O(n^{2.4})$.

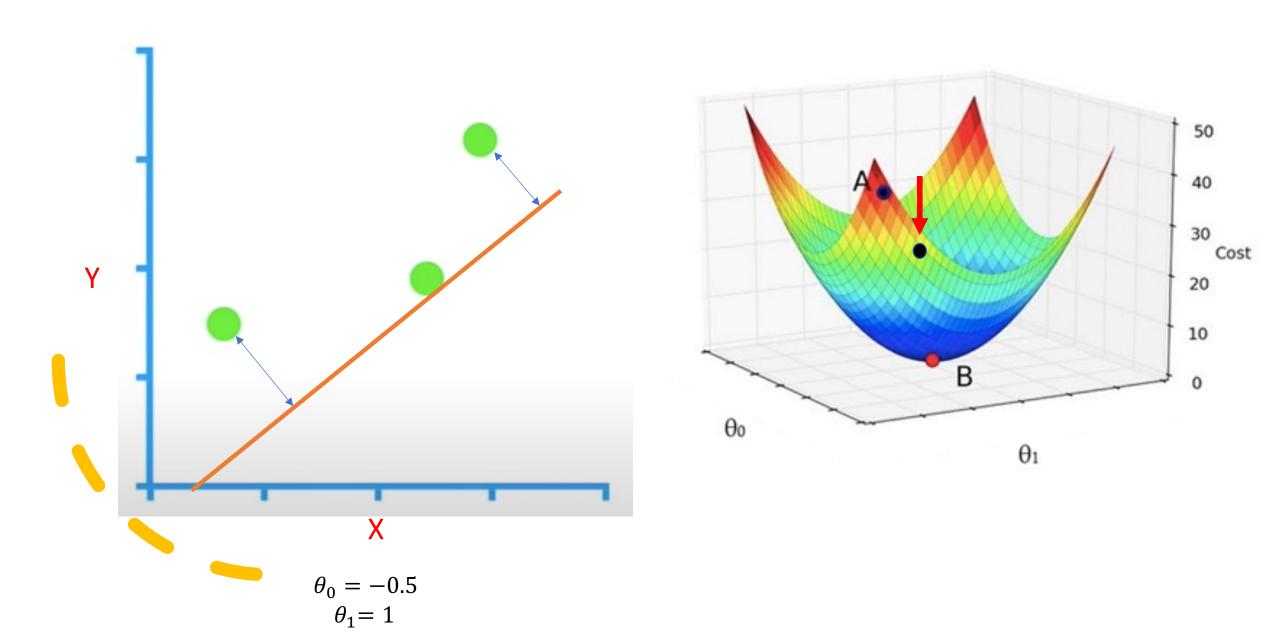
 \triangleright So, instead of calculating θ from the normal equation, the learning algorithms use a technique to estimate this value which is called Gradient Descent.

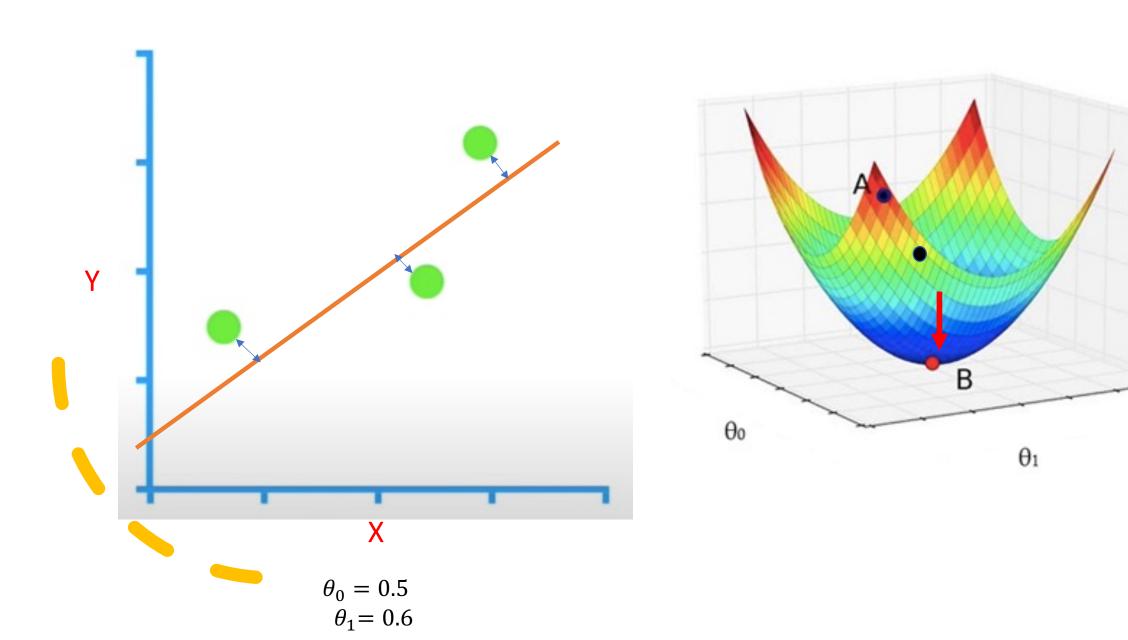
- 1. Start with some initial parameters θ ,
- 2. Tweaking the parameters (θ) iteratively, in a way that it reduces the cost function.



- 1. Start from a position (x, y),
- 2. Find the negative slope (to descend)
- 3. Take appropriate size step.







Cost

- \triangleright Suppose we start with initial θ_0 and θ_1 .
- > In which direction we should go to reduce the cost function?

$$MSE = (h_{\theta}(x^{(1)}) - y^{(1)})^{2} + (h_{\theta}(x^{(2)}) - y^{(2)})^{2} + (h_{\theta}(x^{(3)}) - y^{(3)})^{2}$$

$$\frac{d(MSE)}{d(\theta_{0})} = \frac{d(MSE)}{d(h_{\theta})} \times \frac{d(h_{\theta})}{d(\theta_{0})}$$

$$\frac{d(MSE)}{d(\theta_{0})} = 2 h_{\theta}(x^{(1)}) (h_{\theta}(x^{(1)}) - y^{(1)}) \times 1 + 2 h_{\theta}(x^{(2)}) (h_{\theta}(x^{(2)}) - y^{(2)}) \times 1 + 2 h_{\theta}(x^{(3)}) (h_{\theta}(x^{(3)}) - y^{(3)}) \times 1$$

$$\frac{d(MSE)}{d(\theta_1)} = \frac{d(MSE)}{d(h_{\theta})} \times \frac{d(h_{\theta})}{d(\theta_1)}$$

$$\frac{d(MSE)}{d(\theta_1)} = 2 h_{\theta}(x^{(1)}) (h_{\theta}(x^{(1)}) - y^{(1)}) \times x^{(1)} + 2 h_{\theta}(x^{(2)}) (h_{\theta}(x^{(2)}) - y^{(2)}) \times x^{(1)} + 2 h_{\theta}(x^{(3)}) (h_{\theta}(x^{(3)}) - y^{(3)}) \times x^{(1)}$$

> Step sizes:

Step size
$$(\theta_0)$$
 = slope $(\frac{d(MSE)}{d(\theta_0)}) \times learning \ rate$

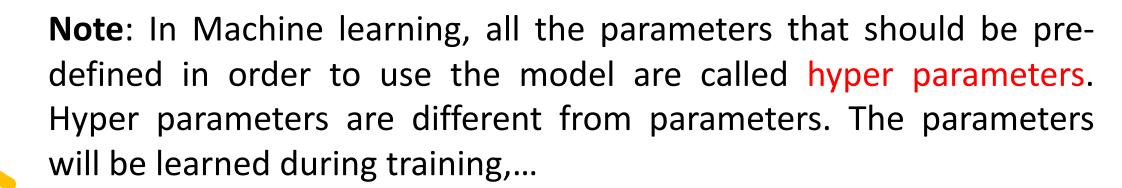
Step size
$$(\theta_1) = \text{slope}(\frac{d(MSE)}{d(\theta_1)}) \times learning \ rate$$

Update Functions:

new
$$\theta_0$$
 = previous θ_0 - step size θ_0 new θ_1 = previous θ_1 - step size θ_1

ML (Gradient Descent-summary):

- 1. Random initialization of parameters (θ_0 , θ_1 , θ_2 ,...),
- 2. Calculate the slopes using gradient descent and chain rule,
- 3. Compute the steps using a pre-defined learning rate,
- 4. Update the parameters,



ML (Error Calculation):

Calculate the Root Mean Square Error for the predictions you made using linear regression for the dataframe GDP per capita/life satisfaction(Use the fonctionalities of numpy).

ML (Error Calculation):

Sub-module metrics and the function mean_squared_error of Sklearn.

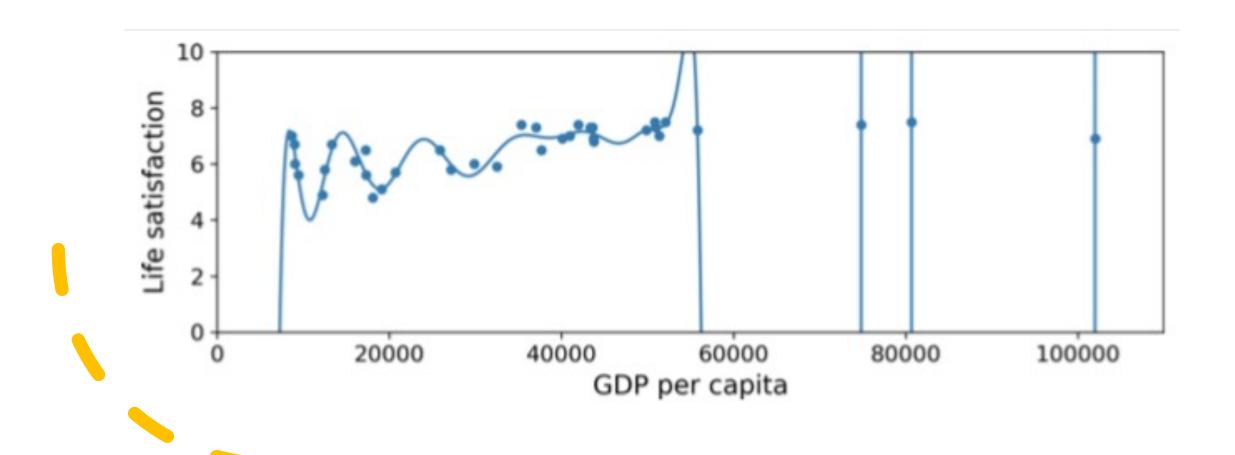
```
from sklearn.metrics import mean_squared_error
mse = mean_squared_error(np.array(data['Life satisfaction']) , predictions)
rmse = np.sqrt(mse)
```

ML (Question):

- ➤ Is this error reliable for future predictions?
- > Does it mean that our model will perform the best to predict?

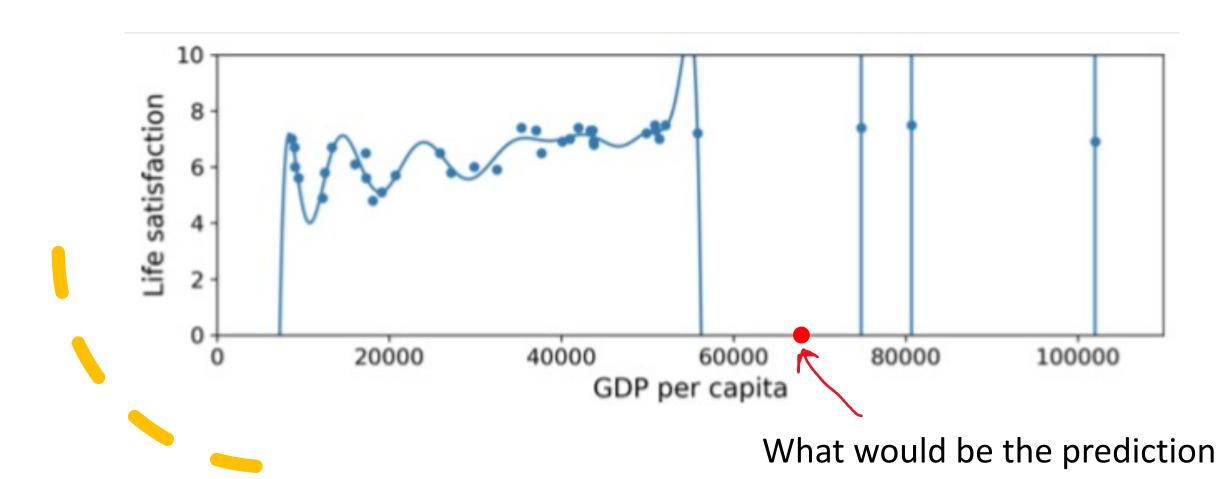
ML (Challenges of training):

Overfitting



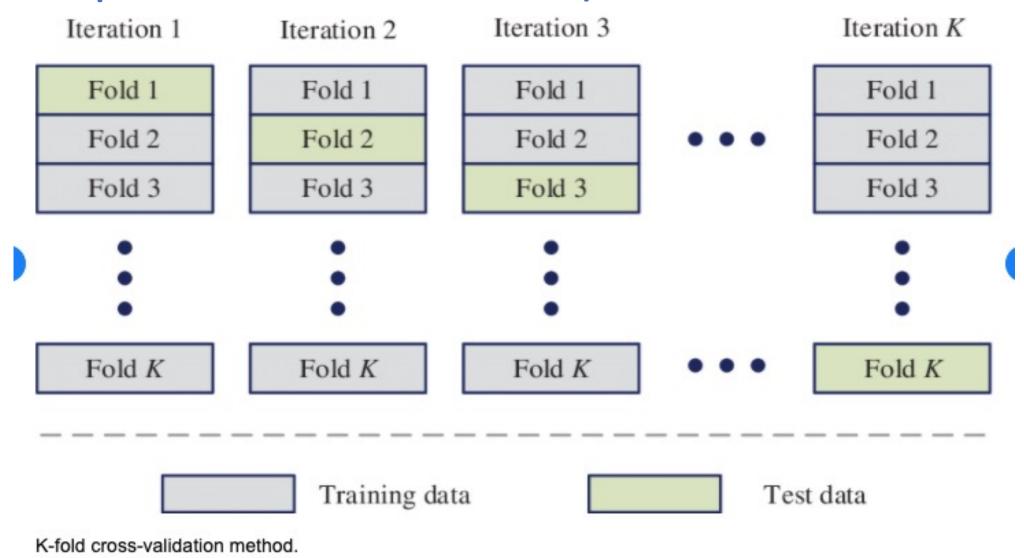
ML (Challenges of training):

Overfitting



value for this point?

ML (Concept of cross validation):



ML (Concept of cross validation):