

To find $c = a * b$, where n is the maximum number of digits in a, b , B is the base of a, b , and a_0, a_1 are the least and most $n/2$ -digit part of a respectively, and the same goes for b with b_0, b_1 :

$$\begin{aligned}c_0 &= a_0 * b_0 \\c_1 &= a_1 * b_0 + a_0 * b_1 = (a_1 + a_0) * (b_1 + b_0) \\c_2 &= a_1 * b_1 \\c &= a * b = c_2 B^n + (c_1 - c_2 - c_0) B^{n/2} + c_0\end{aligned}$$

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Let's try $2205 * 1132$ (where $n = 4$, $B = 10$):

$$\begin{aligned}c_0 &= 5 * 32 \\c_1 &= (22 + 5) * (11 + 32) = 27 * 43 \\c_2 &= 22 * 11\end{aligned}$$

$c_0 = 5 * 32$ (where $n = 2$). Since we end up with $n/2 = 1$, we can calculate these single-digit-operand products in the traditional way:

$$\begin{aligned}c_0 &= 5 * 2 = 10 \\c_1 &= (0 + 5) * (3 + 2) = 5 * 5 = 25 \\c_2 &= 0 * 3 = 0 \\c &= 0 * 10^2 + (25 - 0 - 10)10^{2/2} + 10 = 160\end{aligned}$$

We'll save $c_0 = 160$ for the final calculation.
 $c_1 = 27 * 43$. Again, we're multiplying single digits:

$$\begin{aligned}c_0 &= 7 * 3 = 21 \\c_1 &= (2 + 7) * (4 + 3) = 9 * 7 = 63 \\c_2 &= 2 * 4 = 8 \\c &= 8 * 10^2 + (63 - 8 - 21)10^{2/2} + 21 = 1161\end{aligned}$$

Which means $c_1 = 1161$.
 $c_2 = 22 * 11$:

$$\begin{aligned}c_0 &= 2 * 1 = 2 \\c_1 &= (2 + 2) * (1 + 1) = 4 * 2 = 8 \\c_2 &= 2 * 1 = 2 \\c &= 2 * 10^2 + (8 - 2 - 2)10^{2/2} + 2 = 242\end{aligned}$$

Which means $c_2 = 242$.
We can come back to our original c :

$$\begin{aligned}c &= a * b = 2205 * 1132 \\&= c_2 B^n + (c_1 - c_2 - c_0) B^{n/2} + c_0 \\&= 242 * 10^4 + (1161 - 242 - 160)10^{4/2} + 160 \\&= 2496060\end{aligned}$$

Which leaves us with $2205 * 1132 = 2496060$.