Prediction of uncertainty of 10-coefficient compressor maps for extreme operating conditions

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Abstract. Empirical compressor maps are a simple and reliable approach for heating and cooling system designers to estimate compressor refrigerant mass flow rate and power consumption quickly. These maps were used for a long time since most compressor manufacturers build the maps with extensive test matrices, leading to good accuracy. However, the situation changes when engineers extrapolate the maps to investigate the compressor??s performance under extreme operating conditions such as for cold climate heat pump applications or under conditions with system faults. Engineers are not confident on the exact uncertainty of the extrapolation, and often claim that the inaccuracy of their studies is a result of high extrapolation uncertainty. This paper presents a method to estimate the extrapolation uncertainty due to the structure of the test matrix that trains the manufacturer maps and helps the investigators to understand if the extrapolation is the main cause of their inaccuracy. To verify that the method can estimate the uncertainty due to extrapolation, the study builds 10-coefficient compressor maps trained by different test matrices of the same size and different operating points. The maps are used to estimate the compressor performance under different operating points and their estimation uncertainties are compared. The results show that the component of the uncertainty that depends on the structure of the test matrix is small at operating conditions within the test matrix but the uncertainty grows significantly as the estimation becomes further away from the operating conditions within the test matrices. Some comment:)

1. Introduction

Empirical compressor maps for positive displacement compressors, such as the 10-coefficient polynomials outlined in ANSI/AHRI Standard 540 [1] and European Standard EN 12900 [2] are widely used in academia and industry. These maps are trained with experimental data and then used to calculate power input, mass flowrate, current, and compressor efficiency. However, the maps contain squared and cubic terms of the inputs (suction and discharge dew point temperature) and are therefore potentially inaccurate when used at points other than the training data. Manufacturers often state an accuracy of $\pm 5\%$ for tabulated performance data

(e.g. [3] or [4]). This paper shows a method that estimates the resulting uncertainty for the 10 coefficient polynomial at a certain point other than the training data set. This paper does not address interpolation between different speeds of variable speed compressors. The methodology can be extended to predict the uncertainty of the outputs for interpolating between fixed speeds rather than using different fixed speed compressor maps as done by e.g. [5] and [6].

2. Linear regression

Finding the coefficients of the 10 coefficient maps can be treated as a liniear regression problem, which the evaporation and condensing temperature and their linear, squared and cubed combinations being the independent variables \vec{x} and the power consumption of the compressor being the estimated dependend variable y. To better understand the uncertainty sources of the model, a brief review of linear regression along with how this applies to the polynomial compressor map is shown subsequently.

2.1. Review

Linear regression is used to estimate the parameters of a linear model. Measurement data always includes error, therefore only an estimate of the true parameters can be obtained. If we had the true model parameters $\vec{\beta}_{true}$, then we could use the independent inputs to our model (\vec{x}^T) to calculate the true output y_{true} up to an error ε caused by measurement error,

$$y_{true} = \vec{x}^T \vec{\beta}_{true} + \varepsilon. \tag{1}$$

Unfortunately it is not possible to obtain the true model, since all measurement data that is used for training the model has measurement error. Therefore, we need to estimate the model parameters to be able to calculate an estimate of the output. To emphasize the difference between the two models, a hat ($\hat{}$) is used for both, estimated parameters $\hat{\beta}$ and estimated output, \hat{y} ,

$$\hat{y} = \vec{x}^T \hat{\vec{\beta}}.\tag{2}$$

The parameters for the model can be estimated using measuremnt data, for non-weighted reduction of the squares of the errrors it can be shown that the parmeter vector $\hat{\beta}$ can be calculated as

$$\hat{\vec{\beta}} = (\mathbf{X}_{train}^T \mathbf{X}_{train})^{-1} \mathbf{X}_{train}^T \vec{y}_{train}, \tag{3}$$

where the training data input matrix \mathbf{X}_{train} , composed of input data vectors $\vec{x}_{train,i}$ for each data point i is constructed as

$$\mathbf{X}_{train} = \begin{bmatrix} \vec{x}_{train,1} & \cdots & \vec{x}_{train,i} & \cdots & \vec{x}_{train,n} \end{bmatrix}^T, \tag{4}$$

where n is the total number of data points. The output training data vector is composed of output values $y_{train,i}$ for each data point as

$$\vec{y}_{train} = \begin{bmatrix} y_{train,1} & \cdots & y_{train,i} & \cdots & y_{train,n} \end{bmatrix}^T.$$
 (5)

The accuracy σ of the model for the training data points is

$$\sigma = \sqrt{\frac{\sum_{i} (y_{train,i} - \vec{x}^T \hat{\vec{\beta}})^2}{n-1}}.$$
 (6)

2.2. Polynomial compressor map as linear regression problem

ANSI/AHRI Standard 540 [1] estimates the compressor power consumption \hat{W} as

$$\hat{W} = \beta_1 + \beta_2 T_{evap} + \beta_3 T_{cond} + \beta_4 T_{evap}^2 + \beta_5 T_{evap} T_{cond} + \beta_6 T_{cond}^2 + \beta_7 T_{evap}^3 + \beta_8 T_{evap}^2 T_{cond} + \beta_9 T_{evap} T_{cond}^2 + \beta_{10} T_{cond}^3,$$
(7)

where β_i are the (estimated) model coefficients and T_{evap} , T_{cond} are the evaporation and condensing dew point temperatures. Referring to eqn. 2, \hat{W} takes the place of \hat{y} , the vector composed of β_i is $\hat{\beta}$, and the vector of independent variables, \vec{x} is the vector of the independent variables (here: dew point temperatures),

$$\vec{x} = \begin{bmatrix} 1 & T_{evap} & T_{cond} & T_{evap}^2 & T_{evap}T_{cond} & T_{cond}^2 & T_{evap}^3 & T_{evap}^2T_{cond} & T_{evap}T_{cond} & T_{cond}^3 \end{bmatrix}^T$$
(8)

3. Uncertainty of steady state measurements

The training data for compressor maps is obtained from steady state time series data. Steady state time series data does not show any significant monotonic trend in average value but rather shows periodic and random fluctuations (noise) around an average value. The mean value a of the measured variable can be defined as

$$a = \sum_{i=1}^{N} \frac{a_{mea}(t_i)}{N},\tag{9}$$

where $a_{mea}(t_i)$ is a discrete measurement of the variable at time step i, and N is the number of measurements. Measurement devices have an uncertainty which can be considered time independend, often called zero order uncertainty. The limited number of samples in combination with the fluctuations of the variable leads to a second (first order) uncertainty. Zero-order uncertainty is typically provided by the manufacturer of the measurement device, such as $\pm 0.5 K$ for T-type thermocouples, or 0.5% of the measured flowrate for Coriolis mass flowmeters. First-order uncertainty is not known in advance but rather needs to be approximated by statistically analyzing the time series data of the steady state measurement. Taylor and Kuyatt (1994)?? give the overall measurement uncertainty as

$$\Delta a = \sqrt{\sum_{i=1}^{N} \left(\frac{\Delta a_{mea}(t_i)}{N}\right)^2 + \left(\frac{t_{N-1,1-\alpha/2}}{N}\right)^2 \frac{\sum_{i=1}^{N} (a_{mea}(t_i) - a)^2}{N - 1}}$$
(10)

where $t_{N-1,1-\alpha}$ is the statistic of the student t distribution with a degree of freedom of N-1 and level at $1-\alpha/2$. The first part of the uncertainty is the sum of squares of the zero-order uncertainty of each observation within the steady state measurement. The second part of the uncertainty is given as the confidence interval of the average value at the level of $1-\alpha/2$. In practice, α is taken as 0.1, and a 95% confidence interval is usually used in the approximation.

4. Generating experimental results of steady state data with uncertainties from compressor map data

For this paper, no real measurement data are taken for training data, and only ideal compressor performance data from the manufacturers without uncertainty is available. In order to test the uncertainty calculation of the compressor map output, some training data is needed. Hence it is necessary to approximate a set of training data with uncertainties from the ideal compressor performance data. If the ideal compressor performance data are the true values

of the measurement, its measurement value will be different from its true value because it is subjected to the zero-order uncertainty of the measurement device and the first-order uncertainty of the noise of the measurement environment. Assuming that the uncertainty is the confidence interval of the measurement value at a level of $1 - \alpha/2$ and the measurement value follows a normal distribution with a mean value around the true value of the measurement, the standard deviation of the normal distribution will be given by

$$\sigma_{mea} = \frac{\sqrt{(\Delta a_{zero-order}(a = a_{true}))^2 + (\Delta a_{first-order}(a = a_{true}))^2}}{z_{1-\alpha/2}}$$
(11)

where $z_{1-\alpha/2}$ is the z-normal distribution statistics given at a level of $1-\alpha/2$. The observations within steady state can then be approximated by running a random number generator following a normal distribution with mean at the true value of a and standard deviation at mea multiple times. These values can then be analyzed with the method listed in the section 3 to calculate the value and uncertainty of steady state measurement.

5. Sources of uncertainty

Uncertainty of the compressor map output is the range where the true value of the map output may be relative to the map output. It consists of multiple components and can be grouped as follows:

- Uncertainty due to inputs
- Uncertainty due to training data
- Uncertainty due of model random error
- Uncertainty due to outputs

5.1. Uncertainty due to inputs

Uncertainty due to inputs is the uncertainty propagated to the map output due to the uncertainty in the inputs to the maps. The inputs to the map (evaporating and condenser temperature) are usually obtained by converting pressure measurement to saturation temperature with refrigerant equations of state, and the estimated saturation temperature contains uncertainty from both the equation of state and the pressure measurement. The equation of state of R22 estimates saturation pressure at an uncertainty of 0.2% [7]. When the equation of state estimates an saturation temperature at a given pressure, this uncertainty is transformed into a component of the uncertainty of the saturation temperature as shown in Eqns. (12) and (13).

$$\frac{\Delta P_{sat,EOS}}{P_{sat}(T)} = 0.002 \tag{12}$$

$$\Delta T_{sat,EOS} = \left| \frac{\partial T_{sat}(P)}{\partial P} \right| \Delta P_{sat,EOS} \tag{13}$$

where $\Delta P_{sat,EOS}$ is the uncertainty of saturation pressure as a result of uncertainty of the equation of state, $P_{sat}(T)$ is the saturation pressure from temperature T, $\Delta T_{sat,EOS}$ is the uncertainty of saturation temperature as a result of uncertainty of the equation of state and $T_{sat}(P)$ is the saturation temperature at pressure P.

The component of the uncertainty due to pressure measurement in saturation temperature values is calculated by Eqn. (14).

$$\Delta T_{sat,mea} = \left| \frac{\partial T_{sat}(P)}{\partial P} \right| \Delta P_{sat,mea} \tag{14}$$

where $\Delta T_{sat,mea}$ is the uncertainty of saturation temperature as a result of pressure measurement and $\Delta P_{sat,mea}$ is the uncertainty of pressure measurement.

The overall uncertainty of the saturation temperature is given by Eqn. (15).

$$\Delta T_{sat} = \sqrt{\left(\Delta T_{sat,EOS}\right)^2 + \left(\Delta T_{sat,mea}\right)^2} \tag{15}$$

The uncertainty of the map output propagated from the inputs of condensing temperature and evaporating temperature can be given by Eqn. (16).

$$\Delta \hat{W}_{input} = \sqrt{\left(\frac{\partial \hat{W}}{\partial T_{evap}} \Delta T_{evap}\right)^2 + \left(\frac{\partial \hat{W}}{\partial T_{cond}} \Delta T_{cond}\right)^2}$$
 (16)

where $\Delta \dot{W}_{input}$ is the uncertainty due to inputs at the map output

5.2. Uncertainty due to training data

Uncertainty due to training data is the uncertainty propagated to the map output from the training data through the map coefficients. This can be understood by considering the estimation of the map coefficients as a function of the training data as Eqn. (17).

$$\hat{\vec{\beta}} = g(T_{evap,train,1}, ..., T_{evap,train,n}, T_{cond,train,1}, ..., T_{cond,train,n}, \dot{W}_{train,1}, ..., \dot{W}_{train,n})$$
(17)

The uncertainty propagated to the map output through function g and $\hat{\vec{\beta}}$ in Eqn. (17) is calculated by Eqn. (18).

$$\Delta \hat{W}_{train} = \begin{cases}
\Sigma_{j=1}^{n} \left(\sum_{i=1}^{m} \left(\frac{\hat{\partial W}}{\partial \beta_{i}} \frac{\partial \beta_{i}}{\partial T_{evap,train,j}} \right) \Delta T_{evap,train,j} \right)^{2} \\
+ \Sigma_{j=1}^{n} \left(\sum_{i=1}^{m} \left(\frac{\hat{\partial W}}{\partial \beta_{i}} \frac{\partial \beta_{i}}{\partial T_{cond,train,j}} \right) \Delta T_{cond,train,j} \right)^{2} \\
\sqrt{+ \Sigma_{j=1}^{n} \left(\sum_{i=1}^{m} \left(\frac{\hat{\partial W}}{\partial \beta_{i}} \frac{\partial \beta_{i}}{\partial \dot{W}_{,train,j}} \right) \Delta \dot{W}_{train,j} \right)^{2}}
\end{cases} (18)$$

where $\Delta \dot{W}_{train}$ is the uncertainty due to training data at the map output.

5.3. Uncertainty due to model random error

In linear regression, the random error ε in Eqn. (EQUATION NUMBER TO BE ADDED) is assumed to be normally distributed around zero with some finite variance. This variance becomes part of the uncertainty of the uncertainty of the map output and can be presented in the form of confidence intervals. Statistic textbooks [8,9] illustrated that the confidence interval of the variance can be calculated as Eqn. (19).

$$\Delta \hat{W}_{model} = t_{n-m,1-\alpha/2} \sigma \sqrt{1 + \vec{x}^T (\mathbf{X}_{train}^T \mathbf{X}_{train})^{-1} \vec{x}}$$
(19)

where $\Delta \hat{W}_{train}$ is the uncertainty due to model random error at the map output. One significant term in Eqn. (19) is $\vec{x}^T (\mathbf{X}_{train}^T \mathbf{X}_{train})^{-1} \vec{x}$ which is the leverage of a regression model [10]. It estimates how deviated the current input vector to the map is relative to the training data of the regression model, and its magnitude grows with the deviation. This helps to understand if the estimation is related to the training data and if the model is applicable at the current situation described by the input vector.

5.4. Uncertainty due to output

Uncertainty of the map output should represent the probable range where the true value lies relative to the map output. However, since the map is built from data obtained from measured power consumption but not the true values of the power consumption, the uncertainty components of the map output propagated from other sources only estimate the uncertainty of the estimation with the measured power consumption. Another component of uncertainty must be introduced so that the map output uncertainty is the uncertainty to the true map output. This uncertainty component can be approximated with the uncertainty of the measured power consumption with its true values as Eqn. (20).

$$\Delta \hat{W}_{output} = \frac{1}{n} \sum_{i=1}^{n} \frac{\Delta \dot{W}_{train,i}}{\dot{W}_{train,i}}$$
(20)

5.5. Overall uncertainty

The overall uncertainty of the map output is given by the square of the sum of all uncertainty components as Eqn. (21).

$$\Delta \hat{W} = \sqrt{\left(\Delta \hat{W}_{input}\right)^{2} + \left(\Delta \hat{W}_{train}\right)^{2} + \left(\Delta \hat{W}_{model}\right)^{2} + \left(\Delta \hat{W}_{output}\right)^{2}} \tag{21}$$

6. Results and discussion

To study how the calculation of compressor map output uncertainty helps to determine the applicability of the map, the performance data of a 4.5kW R22 reciprocating compressor listed in its manufacturers specification is used. The tabulated performance data shows the compressor power consumption at different evaporating and condensing temperature with a constant suction superheat 11 K within its operating range as shown in figure 1.

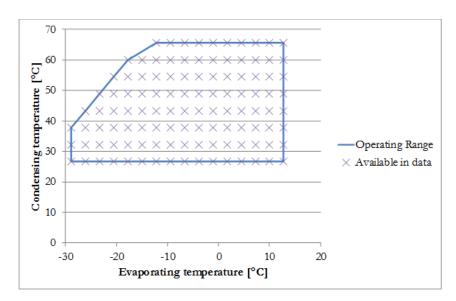


Figure 1. Operating envelope of compressor chosen for this study and available data points from manufacturer map.

Since the manufacturer data do not include experimental uncertainty, it is assumed that the data in the specification are the true values of the performance, and they are used to approximate the observations during steady state experiments with the assumptions in Table 1.

The steady state experiment is assumed to have been conducted for 10 minutes with data acquired at 0.1Hz. The experimental observations at all data points in Figure 1 are generated

Table 1. Assumptions to approximate results in experiments of steady state compressor operation

Variable	Zero-order uncertainty	First-order uncertainty			
Power consumption	0.50%	3%			
Evaporating pressure	0.80%	0.9kPa			
Condensing pressure	0.80%	0.4kPa			

by the method listed in section 4.

6.1. Study cases

To examine if the applicability of compressor map changes with the conditions of the training data, various compressor maps trained from different ranges of data are compared. Six maps with different ranges of training data are designed for the study and the ranges of the training data in these maps are shown in Figure 2.

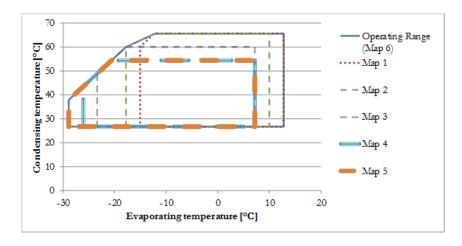


Figure 2. Range of training data for different maps.

Figure 2 shows that map 1 to 5 have their ranges of training data shifting from the top right-handed corner of the operating range of the compressor to its bottom left-handed corner, and map 6 covers the entire operating range. Since it is unfair to compare maps that are generated by different number of data points, the training data points in each map are arranged such that each map contains 70 data points.

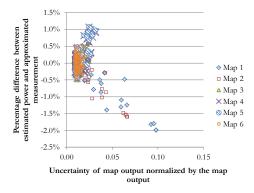
6.2. Comparison of maps

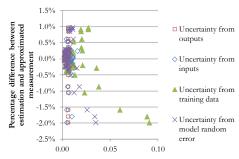
6.3. Effect of range of training data on map output

To study how the range of training data affects map output accuracy and uncertainty, the difference between the map output and approximated measurement and the map output uncertainty for all available data points are plotted in Figure 3, and their uncertainty components are plotted in Figure 4.

Figure 3 shows that inaccurate map outputs are associated with higher uncertainty and the uncertainty calculation method is a good indicator of the accuracy of the map output. Figure 4 shows that the high uncertainty of the inaccurate data points in Figure 3 are results of high uncertainty from model random error and training data.

The increase of uncertainty from model random error with inaccuracy can be explained by the leverage term $\vec{x}^T (\mathbf{X}_{train}^T \mathbf{X}_{train})^{-1} \vec{x}$ in Eqn. (19). When the inputs to the map become more





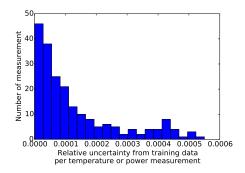
Uncertainty components normalized by model output

Figure 3. Change of accuracy of maps with output uncertainty in different maps.

Figure 4. Change of accuracy of maps with different uncertainty components.

different from the training data points of the map, the applicability and the accuracy of the map decrease. This is associated with an increase of leverage and the uncertainty from model random error. Hence the uncertainty of model random error increases as the applicability and the accuracy of the map decreases.

To explain the increase of uncertainty from training data with a decrease of map accuracy in Figure 4, the squared terms in Eqn. (18) are labeled as uncertainty from training data per measurement, and their values from two map outputs of Map 1 are plotted as histograms as shown in Figures 5 and 6.



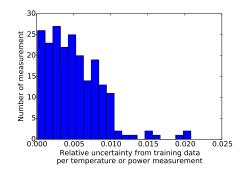


Figure 5. Histogram of uncertainty terms in Eqn. (18) for $T_{evap} = -1.1^{\circ}C$ and $T_{cond} = 60.0^{\circ}C$.

Figure 6. Histogram of uncertainty terms in Eqn. (18) for $T_{evap} = -28.9^{\circ}C$ and $T_{cond} = 26.7^{\circ}C$.

Figure 5 shows a histogram that is more left-skewed than Figure 6. This is because Figure 5 is obtained from a data point inside the training data range of Map 1 in Figure (FIGURE NUMBER TO BE ADDED FROM TEST CASE), and the map only needs information from a few data points around $T_{evap} = -1.1^{\circ}C$ and $T_{cond} = 60.0^{\circ}C$ to estimate its map output. Hence the estimation does not depend on most of the data points, and their training data uncertainties do not propagate to the map output as shown by Figure 5.

However, the map output at the condition in Figure 6 is conducted with the condition at the lower left handed corner in Figure (FIGURE NUMBER HERE), and is far away from most of the training data points of Map 1. To estimate the map output at this condition, the estimation is done by extrapolation and is significantly by multiple data points in the training data. If

any of these significant training data points change, the estimation result at this condition will be changed significantly. Hence much more training data points propagate their uncertainty to the map output in Figure 6 than that in Figure 5. This also explains that the uncertainty of training data is a significant component in the extrapolation uncertainty of the map output and it increases as the map applicability and accuracy decrease.

6.4. Effect of number of training data points on map output

To understand how the number of training data points affect the map output, another map (Map 7) was created with the same range of training data as Map 1 and 22 data points only, and its data points are listed in the appendix. The accuracy of Map 7 is compared with that of Map 1 in Table 2.

Map	Coefficient of variation based on training data poinst only (cov_{train})	
Map 1 Map 7		0.31% 1.15%

Table 2. Coefficients of variation of Maps 1 and 7.

Table 2 shows that the accuracy of Map 7 is similar to that of Map 1 at the training data points, but the analysis with all available data points shows that Map 7 is less accurate than that of Map 1. This shows that despite similar range of training data, fewer training data points reduces map accuracy. But to know if the reduction of accuracy happens at extrapolation, the accuracy of the map outputs is compared with the uncertainty from model random error and the uncertainty from training data as shown in Figures 7 and 8.

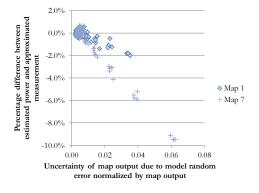


Figure 7. Change of accuracy of maps with uncertainty from model random error in Maps 1 and 7.

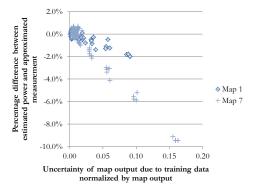


Figure 8. Change of accuracy of maps with uncertainty from training data in Maps 1 and 7.

Figures 7 and 8 show that both the accuracy of Maps 1 and 7 decreases as their uncertainty from model random error and the uncertainty from training data increase, and the reduction of Map 1 accuracy in both figures are more rapid than Map 7. Since the uncertainty components in both figures are indicators of the map applicability, Map 7, despite having the same range of training data as Map 1, is less applicable and accurate as Map 1 because it is constructed with

fewer training data points. This shows that map accuracy and applicability is not only affected by the range of training data but also the number of trianing data points.

7. Conclusions

To conclude, this paper demonstrates how uncertainty of 10-coefficient compressor maps can be calculated based on the uncertainty due to inputs, the uncertainty due to model random error, the uncertainty due to training data and the uncertainty from outputs. It shows that a method to assess the acuracy and applicability of the map output without measured data outside the training data. It also shows that the range of training data and the number of training data points affect the accuracy and applicability of the map.

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Appendix

Table A1. Training data

$T_{cond} \ [^{\circ}C]$	$T_{evap} \ [^{\circ}C]$	\dot{W} [W]	Map 1	Map 2	Map 3	Map 4	Map 5	Map 6	Map 7
26.65 ± 0.31	-28.89 ± 0.20	1672.3 ± 10.1							
26.66 ± 0.31	-26.09 ± 0.20	1756.2 ± 10.5				$\sqrt{}$		·	
26.63 ± 0.32	-23.34 ± 0.24	1845.0 ± 12.0			$\sqrt{}$			$\sqrt{}$	
26.69 ± 0.45	-20.56 ± 0.22	1917.3 ± 12.1				$\sqrt{}$	$\sqrt{}$	•	
26.67 ± 0.31	-17.77 ± 0.22	1987.9 ± 13.1		$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
26.68 ± 0.31	-14.99 ± 0.23	2051.7 ± 13.2	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	•	$\sqrt{}$
26.66 ± 0.31	-12.25 ± 0.23	2119.0 ± 14.0	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	·
26.66 ± 0.31	-9.45 ± 0.24	2185.3 ± 13.9	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	•	
26.65 ± 0.31	-6.66 ± 0.24	2249.1 ± 14.1	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
26.65 ± 0.31	-3.90 ± 0.25	2320.3 ± 14.7	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	•	
26.69 ± 0.31	-1.13 ± 0.25	2397.2 ± 16.2	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
26.66 ± 0.31	1.70 ± 0.26	2466.9 ± 16.3	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	V	1/
26.66 ± 0.31	4.44 ± 0.27	2536.8 ± 17.1	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	V
26.66 ± 0.31	7.23 ± 0.27	2624.8 ± 16.8	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	1/	v 1/	v 1/	1/
26.68 ± 0.31	10.01 ± 0.28	2717.1 ± 17.6	$\sqrt{}$	$\sqrt{}$	V	V	V	V	V
26.70 ± 0.31	12.79 ± 0.28	2808.1 ± 18.6	$\sqrt{}$	V				\checkmark	
32.21 ± 0.32	-28.88 ± 0.20	1686.0 ± 10.7	V				. /	V	
32.21 ± 0.32 32.24 ± 0.32	-26.13 ± 0.19	1817.7 ± 12.2				. /	$\sqrt{}$	\checkmark	
32.24 ± 0.32 32.21 ± 0.32	-20.13 ± 0.19 -23.33 ± 0.21	1950.9 ± 12.4			/	V	$\sqrt{}$	V	
32.21 ± 0.32 32.23 ± 0.32	-20.56 ± 0.21 -20.56 ± 0.25	2072.8 ± 13.8			V /	$\sqrt{}$	$\sqrt{}$	/	
32.23 ± 0.32 32.21 ± 0.32	-20.30 ± 0.23 -17.77 ± 0.22	2072.8 ± 13.8 2192.6 ± 14.2		/	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
32.21 ± 0.32 32.24 ± 0.32	-17.77 ± 0.22 -15.02 ± 0.23	2192.0 ± 14.2 2305.9 ± 14.7	/	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	/	/
			$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	V
32.18 ± 0.32	-12.22 ± 0.23	2407.7 ± 16.0	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	/	
32.26 ± 0.32	-9.44 ± 0.24	2530.9 ± 15.4	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	/
32.23 ± 0.32	-6.69 ± 0.24	2653.7 ± 17.4	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$,	$\sqrt{}$
32.19 ± 0.32	-3.90 ± 0.25	2749.0 ± 17.9	/	/	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
32.24 ± 0.32	-1.13 ± 0.25	2853.2 ± 20.3	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$,	/
32.22 ± 0.32	1.64 ± 0.26	2982.5 ± 18.3	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	\checkmark
32.22 ± 0.32	4.47 ± 0.27	3099.6 ± 20.3	,	,	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$,	
32.23 ± 0.32	7.21 ± 0.27	3223.1 ± 20.9	$\sqrt{}$	$\sqrt{}$	\checkmark	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
32.21 ± 0.32	10.01 ± 0.28	3357.7 ± 21.8	$\sqrt{}$	$\sqrt{}$				$\sqrt{}$,
32.23 ± 0.32	12.79 ± 0.28	3484.5 ± 22.0	$\sqrt{}$,	$\sqrt{}$	$\sqrt{}$
37.75 ± 0.34	-28.90 ± 0.20	1598.1 ± 11.2				,	$\sqrt{}$	$\sqrt{}$	
37.77 ± 0.33	-26.09 ± 0.20	1782.5 ± 11.3			,	$\sqrt{}$	$\sqrt{}$,	
37.80 ± 0.34	-23.31 ± 0.22	1949.3 ± 12.0			$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
37.79 ± 0.34	-20.55 ± 0.26	2114.0 ± 13.4		,	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$,	
37.80 ± 0.34	-17.79 ± 0.22	2281.3 ± 14.5	,	$\sqrt{}$,	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$,
37.78 ± 0.34	-15.02 ± 0.23	2436.0 ± 14.5	$\sqrt{}$,	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$,	$\sqrt{}$
37.81 ± 0.34	-12.21 ± 0.23	2588.4 ± 16.4	$\sqrt{}$	$\sqrt{}$		$\sqrt{}$		$\sqrt{}$	
37.78 ± 0.34	-9.45 ± 0.24	2742.2 ± 17.1			$\sqrt{}$	$\sqrt{}$		$\sqrt{}$	
37.76 ± 0.34	-6.72 ± 0.24	2892.5 ± 19.4	$\sqrt{}$	$\sqrt{}$		$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
37.76 ± 0.34	-3.91 ± 0.25	3049.7 ± 19.8	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
37.77 ± 0.34	-1.12 ± 0.25	3194.3 ± 20.0	$\sqrt{}$	$\sqrt{}$		$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
37.82 ± 0.30	1.66 ± 0.26	3364.8 ± 21.8			$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$
37.78 ± 0.34	4.43 ± 0.26	3512.7 ± 22.5	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
37.78 ± 0.34	$7.21 {\pm} 0.27$	3665.8 ± 24.2	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$
37.79 ± 0.46	$9.98 {\pm} 0.28$	3830.4 ± 25.5		$\sqrt{}$					
37.73 ± 0.34	12.79 ± 0.28	4002.3 ± 25.6	$\sqrt{}$					$\sqrt{}$	
43.33 ± 0.35	-26.09 ± 0.24	1660.6 ± 10.2				$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	
$43.32 {\pm} 0.35$	-23.32 ± 0.21	1883.8 ± 11.8			$\sqrt{}$	$\sqrt{}$	$\sqrt{}$		
43.34 ± 0.35	-20.56 ± 0.22	2088.4 ± 13.6			$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	$\sqrt{}$	