

1)

Selection Sort.

Assuming sorting in ascending order:

T H I S Q U E S T I O N (start)  
 E H I S Q U T S T I O N (swap T with E)  
 E H I S Q U T S T I O N (H stays)  
 E H I S Q U T S T I O N (I stays)  
 E H I I Q U T S T S O N (swap S with I)  
 E H I I N U T S T S O Q (swap Q with N)  
 E H I I N O T S T S U Q (swap U with O)  
 E H I I N O Q S T S U T (swap T with Q)  
 E H I I N O Q S T S U T (S stays)  
 E H I I N O Q S S T U T (swap T with S)  
 E H I I N O Q S S T U T (T stays)  
 E H I I N O Q S S T T U (swap T with U)  
 E H I I N O Q S S T T U (sorted)

2)

Insertion Sort:

Assuming sorting in ascending order:

T H I S Q U E S T I O N (start)  
 H T I S Q U E S T I O N (put T after H)  
 H I T S Q U E S T I O N (put I after H)  
 H I S T Q U E S T I O N (put S after I)  
 H I Q S T U E S T I O N (put Q after I)  
 H I Q S T U E S T I O N (U same place)  
 E H I Q S T U S T I O N (put E in front)  
 E H I Q S S T U T I O N (put S after first S)  
 E H I Q S S T T U I O N (put T after first T)  
 E H I I Q S S T T U O N (put I after first I)  
 E H I I O Q S S T T U N (put O after I)  
 E H I I N O Q S S T T U (put N after I)  
 E H I I N O Q S S T T U (sorted)

3)

Shell sort h sequence 5, 2, 1

M U C H L O N G E R Q U E S T I O N (start h=5 sequences first)

M U C H L O N G E R Q U E S T I O N (insertion sort underlined: MOQI)  
 I U C H L M N G E R O U E S T Q O N

I U C H L M N G E R O U E S T Q O N (insertion sort underlined: UNUO)  
 I N C H L M O G E R O U E S T Q U N

I N C H L M O G E R O U E S T Q U N (insertion sort underlined: CGEN)

I N C H L M O E E R O U G S T Q U N

I N C H L M O E E R O U G S T Q U N (insertion sort underlined: HES)  
I N C E L M O E H R O U G S T Q U N

I N C E L M O E H R O U G S T Q U N (insertion sort underlined: LRT)  
I N C E L M O E H R O U G S T Q U N

(h=2 now)

I N C E L M O E H R O U G S T Q U N (insertion sort underlined: ICLOHOGTU)  
C N G E H M I E L R O U O S T Q U N

C N G E H M I E L R O U O S T Q U N (insertion sort underlined: NEMERUSQN)  
C E G E H M I N L N O Q O R T S U U

(h=1 now)

C E G E H M I N L N O Q O R T S U U (just do insertion sort all whole list for this part)  
C E E G H I L M N N O O Q R S T U U (after the h=1, this is the result and we are done)

4)

Yes insertion sort does work better than selection sort if all keys are identical. Selection sort will still traverse the array  $N+(N-1)+(N-2)+\dots+1$  which is  $O(N^2)$ . Insertion sort compares the adjacent key and if they are all the same, the inner loop breaks and so insertion will take only  $O(N)$ .

5)

Selection sort will work better for all keys in reverse order (well it depends on what you define work). Computational complexity wise, both selection and insertion will be  $O(N^2)$  for reverse order. However, insert sort requires  $O(N^2)$  search and  $O(N^2)$  swaps, but selection sort will only require  $O(N^2)$  search but  $O(N)$  swap.

6)

Let's say list A is a list with duplicate items (e.g. [1, 5, 3, 2, 2, 2, 4, 4, 5]). We first sort the list A using a sorting algorithm ([1, 2, 2, 2, 3, 4, 4, 5, 5]). Then we go through elements in list checking  $A[i]$  and  $A[i+1]$ . We start a new empty list and add the element to it if  $A[i] \neq A[i+1]$ . This will produce a list of unique items.

7)

We first created new empty list and put the results of the each word sorted into that. Then we use a nested loop to print out the duplicates next to each other. Make sure to use a flag so that multiple items are not printed multiple times. The code is below on the next page.

```

1  from functools import reduce
2
3  li = ['racing', 'secura', 'saucer', 'caring', 'random']
4  def jumble(ali):
5      result = []
6      for item in ali:
7          result.append(reduce(lambda a, b : a + b, sorted(item)))
8      flag = []
9      for i in range(len(ali)):
10         if i in flag:
11             continue
12         else:
13             print(ali[i], end=" ")
14             for j in range(i+1, len(ali)):
15                 if(result[i] == result[j]):
16                     flag.append(j)
17                     print(ali[j], end=" ")
18             print("\n")
19
20 print(li)
21 jumble(li)

```

```

['racing', 'secura', 'saucer', 'caring', 'random']
racing caring

secura saucer

random

```

8)

The h-sequence of powers of 2 is bad for shellsort because it doesn't compare odd numbers until the end at  $h=1$ . So if things are very out of order in odd places, it will be bad. Using sequences of powers of 2, the complexity is  $O(N^2)$  with no improvement over insertion sort.

An example is: [200, 50, 190, 40, 180, 30, 170, 20, 160, 10, 150]

When input is in reverse order, it is the worst case for each step of the insertion sort of powers of 2 and also the largest numbers are in the odds and in reverse.

9)

A reason selection sort is not used for h-sorting in shellsort is that selection sort is slower than insertion sort when the list is close to being all sorted. After each h-step, the shellsort becomes more partially sorted, so there's an advantage to using insertion sort.