

1)

3, 17, -5, 4, 13, 8, 7, 6, 9

3, 17, -5, 4, 13, 8, 7, 6, 9 (17  $\leq$  -5)3, -5, 17, 4, 13, 8, 7, 6, 9 (3  $\leq$  -5)-5, 3, 17, 4, 13, 8, 7, 6, 9 (17  $\leq$  9)-5, 3, 9, 4, 13, 8, 7, 6, 17 (13  $\leq$  6)-5, 3, 9, 4, 6, 8, 7, 13, 17 (9  $\leq$  7)

-5, 3, 7, 4, 6, 8, 9, 13, 17

The 7th smallest is 9.

2)

9, 8, 6, 4, -100

9, 8, 6, 4, -100 (9  $\leq$  -100)-100, 8, 6, 4, 9 (-100  $\leq$  -100)-100, 8, 6, 4, 9 (8  $\leq$  4)-100, 4, 6, 8, 9 (4  $\leq$  4)

-100, 4, 6, 8, 9

The median is 6.

3)

3, 1, 2, 4, 5, 8, 7, 6, 9

3 cannot be possible pivot because 1 is not greater than 3.

1 cannot be possible pivot because 3 is not less than 1.

2 cannot be possible pivot because 3 is not less than 2.

4 CAN be a possible pivot because everything left is less and everything right is greater.

5 CAN be a possible pivot because everything left is less and everything right is greater.

8 cannot be possible pivot because 6 is not greater than 8.

7 cannot be possible pivot because 6 is not greater than 7.

6 cannot be possible pivot because 7 is not less than 6.

9 CAN be possible pivot because everything left is less than 9.

The possible pivots are 4, 5, 9.

4)

1, 2, 3, 4, 5 (Random num: 0, so 1 stays in place)

1, 2, 3, 4, 5 (Random num: 1, so 2 stays in place)

1, 3, 2, 4, 5 (Random num: 1, so 2 and 3 exchange)

1, 4, 2, 3, 5 (Random num: 1, so 4 and 3 exchange)

1, 4, 2, 5, 3 (Random num: 3, so 4 and 3 exchange)

So sequence of random numbers is 0,1,1,1,3. These represents the indices.

5)

a) this bad shuffles generates  $N^N$  permutations. So with  $N = 3$  in this problem. Total permutations is  $3^3 = 27$ .

b) KFY shuffle generates  $N!$  permutations. So with  $N = 3$  in this problem. Total permutations is  $3! = 6$ .

c) This is a problem because 27 from the bad shuffle does not evenly divide 6, leading to uneven distribution of permutations. Therefore there is a bias that some permutations are overrepresented and some underrepresented.