

## Combination

with 12 comments

In mathematics a [combination](#) is a way of selecting several things out of a larger group, where (unlike permutations) order does not matter. More formally a k-combination of a set S is a subset of k distinct elements of S. If the set has n elements the number of k-combinations is equal to the [binomial coefficient](#). In this post we will see different methods to calculate the binomial.

### 1. Using Factorials

We can calculate nCr directly using the factorials.

$nCr = n! / (r! * (n-r)!)$

```
1  #include<iostream>
2  using namespace std;
3
4  long long C(int n, int r)
5  {
6      long long f[n + 1];
7      f[0]=1;
8      for (int i=1;i<=n;i++)
9          f[i]=i*f[i-1];
10     return f[n]/f[r]/f[n-r];
11 }
12
13 int main()
14 {
15     int n,r,m;
16     while (~scanf("%d%d",&n,&r))
17     {
18         printf("%lld\n",C(n, min(r,n-r)));
19     }
20 }
```

But this will work for only factorial below 20 in C++. For larger factorials you can either write big factorial library or use a language like Python. The time complexity is O(n).

I am



A graduate from Institute of Technology,BHU. Coding, maths, number theory, oeis, music, reality shows, cs1.6 and sleeping, that pretty much sums up my life :)

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If we have to calculate  $nCr \bmod p$  (where  $p$  is a prime), we can calculate factorial mod  $p$  and then use modular inverse to find  $nCr \bmod p$ . If we have to find  $nCr \bmod m$  (where  $m$  is not prime), we can factorize  $m$  into primes and then use [Chinese Remainder Theorem](#) (CRT) to find  $nCr \bmod m$ .

```
1  #include<iostream>
2  using namespace std;
3  #include<vector>
4
5  /* This function calculates (a^b)%MOD */
6  long long pow(int a, int b, int MOD)
7  {
8      long long x=1,y=a;
9      while(b > 0)
10     {
11         if(b%2 == 1)
12         {
13             x=(x*y);
14             if(x>MOD) x%=MOD;
15         }
16         y = (y*y);
17         if(y>MOD) y%=MOD;
18         b /= 2;
19     }
20     return x;
21 }
22
23 /* Modular Multiplicative Inverse
24 Using Euler's Theorem
25  $a^{(\phi(m))} = 1 \pmod{m}$ 
26  $a^{-1} = a^{(m-2)} \pmod{m}$  */
27 long long InverseEuler(int n, int MOD)
28 {
29     return pow(n,MOD-2,MOD);
30 }
31
32 long long C(int n, int r, int MOD)
33 {
34     vector<long long> f(n + 1,1);
35     for (int i=2; i<=n;i++)
36         f[i]= (f[i-1]*i) % MOD;
37     return (f[n]*((InverseEuler(f[r], MOD) * InverseEuler(f[n-r], MOD)) % MOD)) %
38 }
39
40 int main()
41 {
```

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```

42     int n,r,p;
43     while (~scanf("%d%d%d",&n,&r,&p))
44     {
45         printf("%lld\n",C(n,r,p));
46     }
47 }

```

## 2. Using Recurrence Relation for nCr

The recurrence relation for nCr is  $C(i,k) = C(i-1,k-1) + C(i-1,k)$ . Thus we can calculate nCr in time complexity  $O(n*r)$  and space complexity  $O(n*r)$ .

```

1  #include<iostream>
2  using namespace std;
3  #include<vector>
4
5  /*
6   C(n,r) mod m
7   Using recurrence:
8   C(i,k) = C(i-1,k-1) + C(i-1,k)
9   Time Complexity: O(n*r)
10  Space Complexity: O(n*r)
11  */
12
13  long long C(int n, int r, int MOD)
14  {
15      vector< vector<long long> > C(n+1,vector<long long> (r+1,0));
16
17      for (int i=0; i<=n; i++)
18      {
19          for (int k=0; k<=r && k<=i; k++)
20              if (k==0 || k==i)
21                  C[i][k] = 1;
22              else
23                  C[i][k] = (C[i-1][k-1] + C[i-1][k])%MOD;
24      }
25      return C[n][r];
26  }
27  int main()
28  {

```

July 2011

| M                     | T  | W  | T  | F                     | S  | S         |
|-----------------------|----|----|----|-----------------------|----|-----------|
|                       |    |    |    | 1                     | 2  | 3         |
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```

28 | {
29 |     int n,r,m;
30 |     while (~scanf("%d%d%d",&n,&r,&m))
31 |     {
32 |         printf("%lld\n",C(n, r, m));
33 |     }
34 | }

```

We can easily reduce the space complexity of the above solution by just keeping track of the previous row as we don't need the rest rows.

```

1 | #include<iostream>
2 | using namespace std;
3 | #include<vector>
4 |
5 | /*
6 |     Time Complexity: O(n*r)
7 |     Space Complexity: O(r)
8 | */
9 | long long C(int n, int r, int MOD)
10 | {
11 |     vector< vector<long long> > C(2,vector<long long> (r+1,0));
12 |
13 |     for (int i=0; i<=n; i++)
14 |     {
15 |         for (int k=0; k<=r && k<=i; k++)
16 |             if (k==0 || k==i)
17 |                 C[i&1][k] = 1;
18 |             else
19 |                 C[i&1][k] = (C[(i-1)&1][k-1] + C[(i-1)&1][k])%MOD;
20 |     }
21 |     return C[n&1][r];
22 | }
23 |
24 | int main()
25 | {
26 |     int n,r,m,i,k;
27 |     while (~scanf("%d%d%d",&n,&r,&m))
28 |     {
29 |         printf("%lld\n",C(n, r, m));
30 |     }
31 | }

```

### 3. Using expansion of nCr

Since



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$$C(n,k) = \frac{n! / ((n-k)!k!)}{[n(n-1)\dots(n-k+1)][(n-k)\dots(1)]} = \frac{1}{[(n-k)\dots(1)][k(k-1)\dots(1)]}$$

We can cancel the terms:  $[(n-k)\dots(1)]$  as they appear both on top and bottom, leaving:

$$\frac{n(n-1)\dots(n-k+1)}{k(k-1)\dots(1)}$$

which we might write as:

$$C(n,k) = 1, \quad \text{if } k = 0 \\ = (n/k) * C(n-1, k-1), \quad \text{otherwise}$$

```

1  #include<iostream>
2  using namespace std;
3
4  long long C(int n, int r)
5  {
6      if (r==0) return 1;
7      else return C(n-1,r-1) * n / r;
8  }
9
10 int main()
11 {
12     int n,r,m;
13     while (~scanf("%d%d", &n, &r))
14     {
15         printf("%lld\n", C(n, min(r,n-r)));
16     }
17 }
```

#### 4. Using Matrix Multiplication

In the [last post](#) we learned how to use Fast Matrix Multiplication to calculate functions having linear equations in logarithmic time. Here we have the recurrence relation  $C(i,k) = C(i-1,k-1) + C(i-1,k)$ .

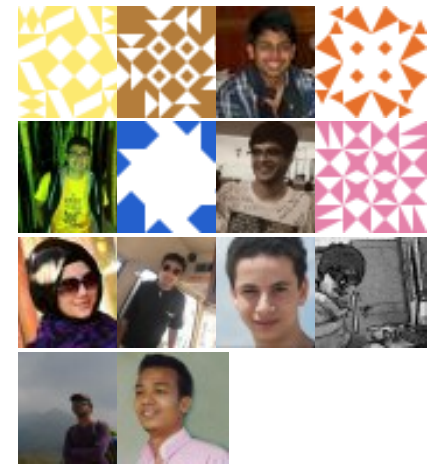
If we take  $k=3$  we can write,

$$C(i-1,1) + C(i-1,0) = C(i,1)$$

$$C(i-1,2) + C(i-1,1) = C(i,2)$$

$$C(i-1,3) + C(i-1,2) = C(i,3)$$

Now on the left side we have four variables  $C(i-1,0)$ ,  $C(i-1,1)$ ,  $C(i-1,2)$  and  $C(i-1,3)$ .



On the right side we have three variables  $C(i,1)$ ,  $C(i,2)$  and  $C(i,3)$ .

We need those two sets to be the same, except that the right side index numbers should be one higher than the left side index numbers. So we add  $C(i,0)$  on the right side. NOW let's get our all important Matrix.

$$\begin{pmatrix} . & . & . & . \\ . & . & . & . \\ . & . & . & . \\ . & . & . & . \end{pmatrix} \begin{pmatrix} C(i-1,0) \\ C(i-1,1) \\ C(i-1,2) \\ C(i-1,3) \end{pmatrix} = \begin{pmatrix} C(i,0) \\ C(i,1) \\ C(i,2) \\ C(i,3) \end{pmatrix}$$

The last three rows are trivial and can be filled from the recurrence equations above.

$$\begin{pmatrix} . & . & . & . \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{pmatrix} \begin{pmatrix} C(i-1,0) \\ C(i-1,1) \\ C(i-1,2) \\ C(i-1,3) \end{pmatrix} = \begin{pmatrix} C(i,0) \\ C(i,1) \\ C(i,2) \\ C(i,3) \end{pmatrix}$$

The first row, for  $C(i,0)$ , depends on what is supposed to happen when  $k = 0$ . We know that  $C(i,0) = 1$  for all  $i$  when  $k=0$ .

So the matrix reduces to

$$\begin{pmatrix} . & . & . & . \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{pmatrix} \begin{pmatrix} C(i-1,0) \\ C(i-1,1) \\ C(i-1,2) \\ C(i-1,3) \end{pmatrix} = \begin{pmatrix} C(i,0) \\ C(i,1) \\ C(i,2) \\ C(i,3) \end{pmatrix}$$

And this then leads to the general form:

$$\begin{pmatrix} . & . & . & . \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{pmatrix}^i \begin{pmatrix} C(0,0) \\ C(0,1) \\ C(0,2) \\ C(0,3) \end{pmatrix} = \begin{pmatrix} C(i,0) \\ C(i,1) \\ C(i,2) \\ C(i,3) \end{pmatrix}$$

For example if we want  $C(4,3)$  we just raise the above matrix to the 4th power.

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{pmatrix}^4 \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 4 \\ 6 \\ 4 \end{pmatrix}$$

Here's a C++ code.

```
1 | #include<iostream>
2 | using namespace std;
3 |
4 | /*
```

```

5      C(n,r) mod m
6      Using Matrix Exponentiation
7      Time Complexity: O((r^3)*log(n))
8      Space Complexity: O(r*r)
9  */
10
11  long long MOD;
12
13  template< class T >
14  class Matrix
15  {
16      public:
17          int m,n;
18          T *data;
19
20          Matrix( int m, int n );
21          Matrix( const Matrix< T > &matrix );
22
23          const Matrix< T > &operator=( const Matrix< T > &A );
24          const Matrix< T > operator*( const Matrix< T > &A );
25          const Matrix< T > operator^( int P );
26
27          ~Matrix();
28  };
29
30  template< class T >
31  Matrix< T >::Matrix( int m, int n )
32  {
33      this->m = m;
34      this->n = n;
35      data = new T[m*n];
36  }
37
38  template< class T >
39  Matrix< T >::Matrix( const Matrix< T > &A )
40  {
41      this->m = A.m;
42      this->n = A.n;
43      data = new T[m*n];
44      for( int i = 0; i < m * n; i++ )
45          data[i] = A.data[i];
46  }
47
48  template< class T >
49  Matrix< T >::~~Matrix()
50  {

```

```

51     delete [] data;
52 }
53
54 template< class T >
55 const Matrix< T > &Matrix< T >::operator=( const Matrix< T > &A )
56 {
57     if( &A != this )
58     {
59         delete [] data;
60         m = A.m;
61         n = A.n;
62         data = new T[m*n];
63         for( int i = 0; i < m * n; i++ )
64             data[i] = A.data[i];
65     }
66     return *this;
67 }
68
69 template< class T >
70 const Matrix< T > Matrix< T >::operator*( const Matrix< T > &A )
71 {
72     Matrix C( m, A.n );
73     for( int i = 0; i < m; ++i )
74         for( int j = 0; j < A.n; ++j )
75         {
76             C.data[i*C.n+j]=0;
77             for( int k = 0; k < n; ++k )
78                 C.data[i*C.n+j] = (C.data[i*C.n+j] + (data[i*n+k]*A.data[k*A.n+j]
79             }
80     return C;
81 }
82
83 template< class T >
84 const Matrix< T > Matrix< T >::operator^( int P )
85 {
86     if( P == 1 ) return (*this);
87     if( P & 1 ) return (*this) * ((*this) ^ (P-1));
88     Matrix B = (*this) ^ (P/2);
89     return B*B;
90 }
91
92 long long C(int n, int r)
93 {
94     Matrix<long long> M(r+1,r+1);
95     for (int i=0;i<(r+1)*(r+1);i++)
96         M.data[i]=0;

```



```

97     M.data[0]=1;
98     for (int i=1;i<r+1;i++)
99     {
100         M.data[i*(r+1)+i-1]=1;
101         M.data[i*(r+1)+i]=1;
102     }
103     return (M^n).data[r*(r+1)];
104 }
105
106 int main()
107 {
108     int n,r;
109     while (~scanf("%d%d%lld",&n,&r,&MOD))
110     {
111         printf("%lld\n",C(n, r));
112     }
113 }

```

## 5. Using the power of prime p in n factorial

The power of prime p in n factorial is given by

$$\varepsilon_p = \left\lfloor \frac{n}{p} \right\rfloor + \left\lfloor \frac{n}{p^2} \right\rfloor + \left\lfloor \frac{n}{p^3} \right\rfloor \dots$$

If we call the power of p in n factorial, the power of p in nCr is given by

$$e = \text{countFact}(n,i) - \text{countFact}(r,i) - \text{countFact}(n-r,i)$$

To get the result we multiply  $p^e$  for all p less than n.

```

1  #include<iostream>
2  using namespace std;
3  #include<vector>
4
5  /* This function calculates power of p in n! */
6  int countFact(int n, int p)
7  {
8      int k=0;
9      while (n>0)
10     {
11         k+=n/p;
12         n/=p;
13     }
14     return k;
15 }
16
17 /* This function calculates (a^b)%MOD */
18 long long pow(int a, int b, int MOD)
19 {

```

```

20     long long x=1,y=a;
21     while(b > 0)
22     {
23         if(b%2 == 1)
24         {
25             x=(x*y);
26             if(x>MOD) x%=MOD;
27         }
28         y = (y*y);
29         if(y>MOD) y%=MOD;
30         b /= 2;
31     }
32     return x;
33 }
34
35 long long C(int n, int r, int MOD)
36 {
37     long long res = 1;
38     vector<bool> isPrime(n+1,1);
39     for (int i=2; i<=n; i++)
40         if (isPrime[i])
41         {
42             for (int j=2*i; j<=n; j+=i)
43                 isPrime[j]=0;
44             int k = countFact(n,i) - countFact(r,i) - countFact(n-r,i);
45             res = (res * pow(i, k, MOD)) % MOD;
46         }
47     return res;
48 }
49
50 int main()
51 {
52     int n,r,m;
53     while (scanf("%d%d%d",&n,&r,&m))
54     {
55         printf("%lld\n",C(n,r,m));
56     }
57 }

```

## 6. Using [Lucas Theorem](#)

For non-negative integers m and n and a prime p, the following congruence relation holds:

$$\binom{m}{n} \equiv \prod_{i=0}^k \binom{m_i}{n_i} \pmod{p},$$

where

$$m = m_k p^k + m_{k-1} p^{k-1} + \dots + m_1 p + m_0,$$

and

$$n = n_k p^k + n_{k-1} p^{k-1} + \dots + n_1 p + n_0$$

are the base p expansions of m and n respectively.

We only need to calculate nCr only for small numbers (less than equal to p) using any of the above methods.

```
1  #include<iostream>
2  using namespace std;
3  #include<vector>
4
5  long long SmallC(int n, int r, int MOD)
6  {
7      vector< vector<long long> > C(2,vector<long long> (r+1,0));
8
9      for (int i=0; i<=n; i++)
10     {
11         for (int k=0; k<=r && k<=i; k++)
12             if (k==0 || k==i)
13                 C[i&1][k] = 1;
14             else
15                 C[i&1][k] = (C[(i-1)&1][k-1] + C[(i-1)&1][k])%MOD;
16     }
17     return C[n&1][r];
18 }
19
20 long long Lucas(int n, int m, int p)
21 {
22     if (n==0 && m==0) return 1;
23     int ni = n % p;
24     int mi = m % p;
25     if (mi>ni) return 0;
26     return Lucas(n/p, m/p, p) * SmallC(ni, mi, p);
27 }
28
29 long long C(int n, int r, int MOD)
30 {
31     return Lucas(n, r, MOD);
32 }
33
34 int main()
35 {
36
37     int n,r,p;
38     while (~scanf("%d%d%d",&n,&r,&p))
39     {
40         printf("%lld\n",C(n,r,p));
```

```

41 |     }
42 | }

```

## 7. Using special $n! \bmod p$

We will calculate  $n$  factorial mod  $p$  and similarly inverse of  $r! \bmod p$  and  $(n-r)! \bmod p$  and multiply to find the result. But while calculating factorial mod  $p$  we remove all the multiples of  $p$  and write

$$n! \bmod p = 1 * 2 * \dots * (p-1) * 1 * 2 * \dots * (p-1) * 2 * 1 * 2 * \dots * n.$$

We took the usual factorial, but excluded all factors of  $p$  (1 instead of  $p$ , 2 instead of  $2p$ , and so on). Lets call this *strange factorial*.

So *strange factorial* is really several blocks of construction:

$$1 * 2 * 3 * \dots * (p-1) * i$$

where  $i$  is a 1-indexed index of block taken again without factors  $p$ .

The last block could be *not* full. More precisely, there will be  $\text{floor}(n/p)$  full blocks and some tail (its result we can compute easily, in  $O(P)$ ).

The result in each block is multiplication  $1 * 2 * \dots * (p-1)$ , which is common to all blocks, and multiplication of all *strange indices*  $i$  from 1 to  $\text{floor}(n/p)$ .

But multiplication of all *strange indices* is really a strange factorial again, so we can compute it recursively. Note, that in recursive calls  $n$  reduces exponentially, so this is rather fast algorithm.

Here's the algorithm to calculate *strange factorial*.

```

1 | int factMOD(int n, int MOD)
2 | {
3 |     long long res = 1;
4 |     while (n > 1)
5 |     {
6 |         long long cur = 1;
7 |         for (int i=2; i<MOD; ++i)
8 |             cur = (cur * i) % MOD;
9 |         res = (res * powmod (cur, n/MOD, MOD)) % MOD;
10 |        for (int i=2; i<=n%MOD; ++i)
11 |            res = (res * i) % MOD;
12 |        n /= MOD;
13 |    }
14 |    return int (res % MOD);
15 | }

```

But we can still reduce our complexity.

By [Wilson's Theorem](#), we know  $(n-1)! \equiv -1 \pmod{n}$  for all primes  $n$ . SO our method reduces to:

```

1 | long long factMOD(int n, int MOD)

```

```

2 | {
3 |     long long res = 1;
4 |     while (n > 1)
5 |     {
6 |         res = (res * pow(MOD - 1, n/MOD, MOD)) % MOD;
7 |         for (int i=2, j=n%MOD; i<=j; i++)
8 |             res = (res * i) % MOD;
9 |         n/=MOD;
10 |    }
11 |    return res;
12 | }

```

Now in the above code we are calculating  $(-1)^{(n/p)}$ . If  $(n/p)$  is even what we are multiplying by 1, so we can skip that. We only need to consider the case when  $(n/p)$  is odd, in which case we are multiplying result by  $(-1)\%MOD$ , which ultimately is equal to  $MOD-res$ . SO our method again reduces to:

```

1 | long long factMOD(int n, int MOD)
2 | {
3 |     long long res = 1;
4 |     while (n > 0)
5 |     {
6 |         for (int i=2, m=n%MOD; i<=m; i++)
7 |             res = (res * i) % MOD;
8 |         if ((n/=MOD)%2 > 0)
9 |             res = MOD - res;
10 |    }
11 |    return res;
12 | }

```

Finally the complete code here:

```

1 | #include<iostream>
2 | using namespace std;
3 | #include<vector>
4 |
5 | /* This function calculates power of p in n! */
6 | int countFact(int n, int p)
7 | {
8 |     int k=0;
9 |     while (n>=p)
10 |    {
11 |        k+=n/p;
12 |        n/=p;
13 |    }
14 |    return k;

```

```

15 }
16
17 /* This function calculates (a^b)%MOD */
18 long long pow(int a, int b, int MOD)
19 {
20     long long x=1,y=a;
21     while(b > 0)
22     {
23         if(b%2 == 1)
24         {
25             x=(x*y);
26             if(x>MOD) x%=MOD;
27         }
28         y = (y*y);
29         if(y>MOD) y%=MOD;
30         b /= 2;
31     }
32     return x;
33 }
34
35 /* Modular Multiplicative Inverse
36 Using Euler's Theorem
37  $a^{\phi(m)} = 1 \pmod{m}$ 
38  $a^{-1} = a^{(m-2)} \pmod{m}$  */
39 long long InverseEuler(int n, int MOD)
40 {
41     return pow(n,MOD-2,MOD);
42 }
43
44 long long factMOD(int n, int MOD)
45 {
46     long long res = 1;
47     while (n > 0)
48     {
49         for (int i=2, m=n%MOD; i<=m; i++)
50             res = (res * i) % MOD;
51         if ((n/=MOD)%2 > 0)
52             res = MOD - res;
53     }
54     return res;
55 }
56
57 long long C(int n, int r, int MOD)
58 {
59     if (countFact(n, MOD) > countFact(r, MOD) + countFact(n-r, MOD))
60         return 0;

```

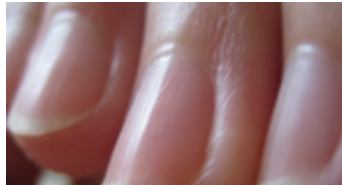
```

61
62     return (factMOD(n, MOD) *
63             ((InverseEuler(factMOD(r, MOD), MOD) *
64              InverseEuler(factMOD(n-r, MOD), MOD)) % MOD)) % MOD;
65 }
66
67 int main()
68 {
69     int n,r,p;
70     while (~scanf("%d%d%d",&n,&r,&p))
71     {
72         printf("%lld\n",C(n,r,p));
73     }
74 }

```

-fR0D

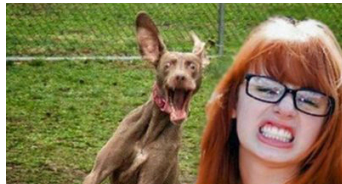
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Written by fR0DDY  
July 31, 2011 at 5:30 PM

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are you calculating the time and space complexity on the basis of code you are writing  
or by using the calculus proofs or simply through wikipedia



[gauravalgo](#)

August 3, 2011 at [12:22 AM](#)

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On the basis of code.



fR0DDY

August 22, 2011 at [3:00 PM](#)

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i think i must congratulate fr0ddy for this beautiful technical blog but then



[gauravalgo](#)



there are beginners who do not understand this article at first site so i recommend them to

go through this writeup of euclid algorithm and modular inverse

<http://algorithmsolver.blogspot.com/2011/09/euclid-algorithm-and-its-applications.html>

[Reply](#)



September 7, 2011 at [4:55 PM](#)

Awesome post. I use this post as a cheat book for all my programming contests 😊



[Suraj Chandran](#)

February 5, 2012 at [11:20 PM](#)

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Just to make this blog better – you use header and printf/scanf functions for IO..

Thanks.



[valker](#)

June 29, 2012 at [12:57 AM](#)

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Hi

Can you provide algorithm to calculate sum of digits in  $2^{1000}$ ??

Thanks.



[minoz](#)

August 20, 2012 at [2:34 AM](#)

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Hi Froddy,

This is a very nice post.

I just found a small bug in one of your code.

In point 1. Using factorials .

The code written below this

“If we have to calculate  $nCr \bmod p$  (where  $p$  is a prime), we can calculate factorial mod  $p$  and then use modular inverse to find  $nCr \bmod p$ . If we have to find  $nCr \bmod m$  (where  $m$  is not prime), we can factorize  $m$  into primes and then use Chinese Remainder Theorem (CRT) to find  $nCr \bmod m$ .”

Here in function “long long C(int n, int r, int MOD)”

at line 34 it should be



[Gaurav](#)

February 3, 2013 at [3:06 AM](#)

vector  $f(n+1,1)$ ; instead of vector  $f(n,1)$ ;

[Reply](#)

Thanks for pointing that out. Edited.



**fR0DDY**

February 3, 2013 at [9:38 AM](#)

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Can you tell me which method would you prefer for a general question with a  $n$  as high as  $10^9$  ?



**[mayanknatani](#)**

May 31, 2013 at [4:37 PM](#)

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how we calculate  $a^{(-1)\%mod}$  , if mod is not a prime number ?



**[Avneet](#)**

June 5, 2013 at [12:49 AM](#)

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See this post: <https://comeoncodeon.wordpress.com/2011/10/09/modular-multiplicative-inverse/>



**fR0DDY**

June 5, 2013 at [8:26 AM](#)

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Use Chinese Remainder Theorem



**fR0DDY**

June 17, 2013 at [8:29 PM](#)

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