Physiologically based pharmacokinetic model

ODE system : Time varying state

```
// Concentrations in the tissues and in the capillary blood of the tissues
double CA_free = APlas_free/VPlas;        // mg/L, Free PFOSC concentration in the plasma
double CA = CA_free/Free;                 // mg/L, Concentration of total PFOS in plasma

double CL = AL/VL;                        // mg/L, Concentration of parent drug in the tissue of liver
double CVL = CL/PL;                       // mg/L, Concentration of parent drug in the capillary blood of liver

double CKb = AKb/VKb;                     // mg/L, Concentration of PFOS in Kidney blood
double CVK = CKb/PK;                      // mg/L, Concentration of PFOS in Kidney blood
double CK = CVK*PK;                       // mg/L, Concentration of PFOS in Kidney compartment

double CRest = ARest/VRest;               // mg/L, Crest drug concentration in the rest of the body (mg/L)
double CVRest = CRest/PRest;              // mg/L, Concentration of parent drug in the capillary blood of the rest of body

// Kidney compartment plus 2 subcompartment (Proximal Tubule cells: PTC, Filtrate: Fil)
// Concentration in kidney, PTC and fil

double CPTC = APTC/VPTC;                  // mg/L, Concentration of PFOS in PTC blood
double Cfil = AFil/Vfil;                  // mg/L, Concentration of PFOS in FIL blood

// Virtual compartment:
// Basolateral transport : (baso)
// Diffusion            : (dif)
// Apical transport     : (apical)
// efflux clearance     : (efflux)
// Clearance via glormerular filtration (CL)

double RA_baso = (Vmax_baso*CKb)/(Km_baso+CKb);        // mg/h, Rate of basolateral transporters
dxdt_A_baso = RA_baso;                                 // mg, Amount of basolateral transporters
double RA_apical = (Vmax_apical*Cfil)/(Km_apical + Cfil);  // mg/h, Rate of apical transporter
dxdt_A_apical = RA_apical;                             // mg, Amount of apical transporter
double Rdif = Kdif*(CKb - CPTC);                       // mg/h, Rate of diffusion from into the PTC
dxdt_Adif = Rdif;                                      // mg, Amount moved via glomarular filtration
double RAefflux = Kefflux*APTC;                        // mg/h, Rate of efflux clearance rate from PTC to blood
dxdt_Aefflux = RAefflux;                               // mg, Amount of efflux clearance rate from PTC to blood
double RCI = CA*GFR*Free;                 // mg/h, Rate of clearance (CL) to via glormerular filtration (GFR)
dxdt_ACI = RCI;                                        // mg, Amount of clearance via GFR
```


Legend
- Oral exposure route
- IV exposure route
- Dynamic compartment
- Elimination compartment
- Elimination
- Blood flow
- Passive transport
- Active transport

Figure
A. PBPK model
B. Subcompartment for gastrointestinal tract
C. Subcompartment for renal excretion and reabsorption

```
// PFOS in plasma
double RPlas_free = (QRest*CVRest*Free)+(QK*CVK*Free)+(QL*CVL*Free)-(QC*CA*Free)+RAefflux; // mg/h, Rate of change in the plasma
double RPlas = (QRest*CVRest)+(QK*CVK)+(QL*CVL)-(QC*CA);
dxdt_APlas_free = RPlas_free;             // mg, Amount in the plasma
dxdt_APlas = RPlas;                       // mg, Amount in the plasma
dxdt_AUCCA_free = CA_free;                // mg*h/L, Area under curve of PFOS in liver compartment

// Proximal Tubule Cells (PTC)
double RPTC = Rdif + RA_apical + RA_baso - RAefflux;  // mg/h, Rate of change in PTC
dxdt_APTC = RPTC;                         // mg, Amount moved in PTC
dxdt_AUCCPTC = CPTC;                      // mg*h/L, Area under curve of PFOS in the compartment of PTC

// Proximal Tubule Lumen/ Filtrate (Fil)
double Rfil = CA*GFR*Free - RA_apical - AFil*Kurine;  // mg/h, Rate of change in Fil
dxdt_AFil = Rfil;                         // mg, Amount moved in Fil
dxdt_AUCfil = Cfil;                       // mg*h/L, Area under curve of PFOS in the compartment of Fil

// Urine elimination
double Rurine = Kurine*AFil;              // mg/h, Rate of change in urine
dxdt_Aurine = Rurine;                     // mg, Amount in urine
double Curine = Rurine/Kvoid; //

// Kidney compartment
double RKb = QK*(CA-CVK)*Free - CA*GFR*Free - Rdif - RA_baso; // mg/h, Rate of change in Kidney compartment
dxdt_AKb = RKb;                           // mg, Amount in kidney compartment
dxdt_AUCKb = CK;                          // mg*h/L, Area under curve of PFOS in the Kidney compartment

// PFOS in the compartment of rest of body, flow-limited model
double RRest = QRest*(CA-CVRest)*Free;    // mg/h, Rate of change in rest of body
dxdt_ARest = RRest;                       // mg, Amount in rest of body
dxdt_AUCCRest = CRest;                    // mg*h/L, Area under curve of PFOS in the compartment of rest of body

// Gastrointestinal (GI) tract
// Stomach compartment
double RST = - K0*AST - GE*AST;           // mg/h, Rate of chagne in Stomach compartment
dxdt_AST = RST;                           // mg, Amount in Stomach
double RabsST = K0*AST;                   //  mg/h, Rate of absorption in the stomach
dxdt_AabsST = RabsST;                     // mg, Amount absorbed in the stomach

// Small intestine compartment
double RSI = GE*AST - Kabs*ASI - Kunabs*ASI;  // mg/h, Rate of chagne in Small intestine compartment
dxdt_ASI = RSI;                           // mg, Amount in Small intestine
double RabsSI = Kabs*ASI;                 // mg/h, Rate of absorption in the Small intestine
dxdt_AabsSI = RabsSI;                     // mg, Amount absorbed in the Small intestine
double Total_oral_uptake = AabsSI + AabsST;  // mg, Total oral uptake in the GI

// Biliary excretion
double Abile = Kbile*AL;                  // mg, Amount of PFOS in bile excretion
double amount_per_gram_liver = (AL/ML)*1000;  // ug/g, Amount of PFOS in liver per gram liver

// Feces compartment
double Rfeces = Kbile*AL+ Kunabs*ASI;     // mg/h, Rate of change in feces compartment
dxdt_Afeces = Rfeces;                     // mg, Amount of the feces compartment

// PFOS in liver compartment, flow-limited model
double RL = QL*(CA-CVL)*Free - Kbile*AL + Kabs*ASI + K0*AST; // mg/h, Rate of chagne in liver compartment
dxdt_AL = RL;                             // mg, Amount in liver compartment
dxdt_AUCCL = CL;                          // mg*h/L, Area under curve of PFOS in liver compartment
```
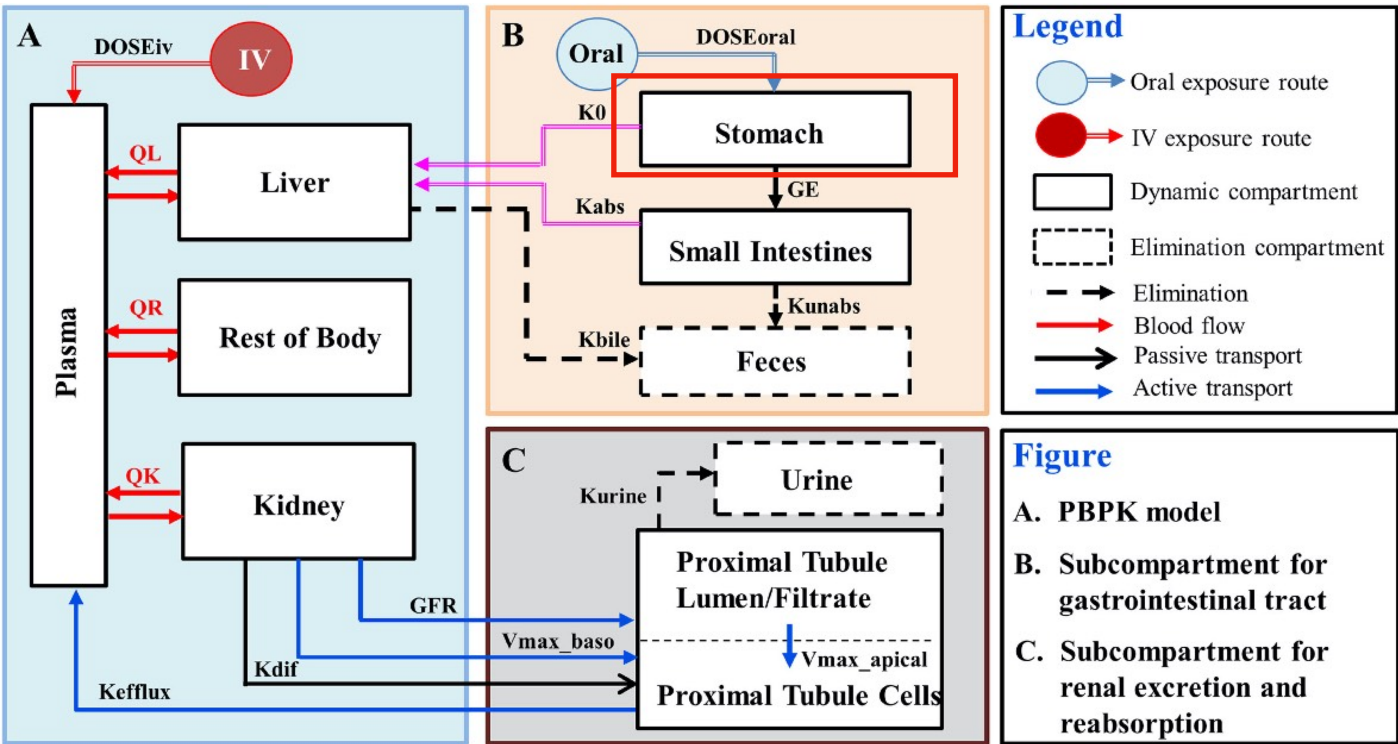
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double CVK = CKb/PK;                       // mg/L, Concentration of PFOS in Kidney compartment
double CK = CVK*PK;                        // mg/L, Concentration of PFOS in Kidney compartment

double CRest = ARest/VRest;                // mg/L, Crest drug concentration in the rest of the body (mg/L)
double CVRest = CRest/PRest;               // mg/L, Concentration of parent drug in the capillary blood of the rest of body

// Kidney compartment plus 2 subcompartment (Proximal Tubule cells: PTC, Filtrate: Fil)
// Concentration in kidney, PTC and fil

double CPTC = APTC/VPTC;                    // mg/L, Concentration of PFOS in PTC blood
double Cfil = AFil/Vfil;                    // mg/L, Concentration of PFOS in FIL blood

// Virtual compartment:
// Basolateral transport : (baso)
// Diffusion             : (dif)
// Apical transport      : (apical)
// efflux clearance      : (efflux)
// Clearance via glormerular filtration (CL)

double RA_baso = (Vmax_baso*CKb)/(Km_baso+CKb);         // mg/h, Rate of basolateral transporters
dxdt_A_baso = RA_baso;                                   // mg, Amount of basolateral transporters
double RA_apical = (Vmax_apical*Cfil)/(Km_apical + Cfil);  // mg/h, Rate of apical transporter
dxdt_A_apical = RA_apical;                               // mg, Amount of apical transporter
double Rdif = Kdif*(CKb - CPTC);                         // mg/h, Rate of diffusion from into the PTC
dxdt_Adif = Rdif;                                        // mg, Amount moved via glomarular filtration
double RAefflux = Kefflux*APTC;                          // mg/h, Rate of efflux clearance rate from PTC to blood
dxdt_Aefflux = RAefflux;                                 // mg, Amount of efflux clearance rate from PTC to blood
double RCI = CA*GFR*Free;                // mg/h, Rate of clearance (CL) to via glormerular filtration (GFR)
dxdt_ACI = RCI;                                          // mg, Amount of clearance via GFR
```

// PFOS in plasma
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double RPlas_free = (QRest*CVRest*Free)+(QK*CVK*Free)+(QL*CVL*Free)-(QC*CA*Free)+RAefflux; // mg/h, Rate of change in the plasma
double RPlas = (QRest*CVRest)+(QK*CVK)+(QL*CVL)-(QC*CA);
dxdt_APlas_free = RPlas_free;                 // mg, Amount in the plasma
dxdt_APlas = RPlas;                           // mg, Amount in the plasma
dxdt_AUCCA_free = CA_free;                    // mg*h/L, Area under curve of PFOS in liver compartment

// Proximal Tubule Cells (PTC)
double RPTC = Rdif + RA_apical + RA_baso - RAefflux; // mg/h, Rate of change in PTC
dxdt_APTC = RPTC;                             // mg, Amount moved in PTC
dxdt_AUCCPTC = CPTC;                          // mg*h/L, Area under curve of PFOS in the compartment of PTC

// Proximal Tubule Lumen/ Filtrate (Fil)
double Rfil = CA*GFR*Free - RA_apical - AFil*Kurine; // mg/h, Rate of change in Fil
dxdt_AFil = Rfil;                             // mg, Amount moved in Fil
dxdt_AUCfil = Cfil;                           // mg*h/L, Area under curve of PFOS in the compartment of Fil

// Urine elimination
double Rurine = Kurine*AFil;                  // mg/h, Rate of change in urine
dxdt_Aurine = Rurine;                         // mg, Amount in urine
double Curine = Rurine/Kvoid; //

// Kidney compartment
double RKb = QK*(CA-CVK)*Free - CA*GFR*Free - Rdif - RA_baso; // mg/h, Rate of change in Kidney compartment
dxdt_AKb = RKb;                               // mg, Amount in kidney compartment
dxdt_AUCKb = CK;                              // mg*h/L, Area under curve of PFOS in the Kidney compartment

// PFOS in the compartment of rest of body, flow-limited model
double RRest = QRest*(CA-CVRest)*Free;        // mg/h, Rate of change in rest of body
dxdt_ARest = RRest;                           // mg, Amount in rest of body
dxdt_AUCCRest = CRest;                        // mg*h/L, Area under curve of PFOS in the compartment of rest of body

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// Stomach compartment
double RST = - K0*AST - GE*AST;               // mg/h, Rate of chagne in Stomach compartment
dxdt_AST = RST;                               // mg, Amount in Stomach
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double RSI = GE*AST - Kabs*ASI - Kunabs*ASI;  // mg/h, Rate of chagne in Small intestine compartment
dxdt_ASI = RSI;                               // mg, Amount in Small intestine
double RabsSI = Kabs*ASI;                      // mg/h, Rate of absorption in the Small intestine
dxdt_AabsSI = RabsSI;                         // mg, Amount absorbed in the Small intestine
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// Biliary excretion
double Abile = Kbile*AL;                       // mg, Amount of PFOS in bile excretion
double amount_per_gram_liver = (AL/ML)*1000;   // ug/g, Amount of PFOS in liver per gram liver

// Feces compartment
double Rfeces = Kbile*AL+ Kunabs*ASI;          // mg/h, Rate of change in feces compartment
dxdt_Afeces = Rfeces;                         // mg, Amount of the feces compartment

// PFOS in liver compartment, flow-limited model
double RL = QL*(CA-CVL)*Free - Kbile*AL + Kabs*ASI + K0*AST; // mg/h, Rate of chagne in liver compartment
dxdt_AL = RL;                                 // mg, Amount in liver compartment
dxdt_AUCCL = CL;                              // mg*h/L, Area under curve of PFOS in liver compartment
```


Legend
- Oral exposure route
- IV exposure route
- Dynamic compartment
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Figure
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