

multivarious.rvs for random variables

Distribution	$f_X(x)$ or $p_N(n)$	$F_X(x)$	$F_X^{-1}(p)$	X
beta	beta.pdf(x, a, b, q, p)	beta.cdf(x, [a, b, q, p])	beta.inv(F, a, b, q, p)	beta.rnd(a, b, q, p, N, R, seed)
binomial	binomial.pmf(n, m, p)	binomial.cdf(n, m, p)	--	binomial.rnd(m, p, N, R, seed)
chi2	chi2.pdf(x, k)	chi2.cdf(x, k)	chi2.inv(p, k)	chi2.rnd(k, N, R, seed)
exponential	exponential.pdf(x, meanX)	exponential.cdf(x, meanX)	exponential.inv(P, meanX)	exponential.rnd(meanX, N, R, seed)
extreme_value_I	extreme_value_I.pdf(x, meanX, covnX)	extreme_value_I.cdf(x, [meanX, covnX])	extreme_value_I.inv(p, meanX, covnX)	extreme_value_I.rnd(meanX, covnX, N, R, seed)
extreme_value_II	extreme_value_II.pdf(x, m, s, k)	extreme_value_II.cdf(x, [m, s, k])	extreme_value_II.inv(P, m, s, k)	extreme_value_II.rnd(m, s, k, N, R, seed)
gamma	gamma.pdf(x, meanX, covnX)	gamma.cdf(x, [meanX, covnX])	gamma.inv(P, meanX, covnX)	gamma.rnd(meanX, covnX, N, R, seed)
gev	gev.pdf(x, m, s, k)	gev.cdf(x, [m, s, k])	gev.inv(p, m, s, k)	gev.rnd(m, s, k, N, R, seed)
laplace	laplace.pdf(x, meanX, sdvnX)	laplace.cdf(x, [meanX, sdvnX])	laplace.inv(P, meanX, sdvnX)	laplace.rnd(meanX, sdvnX, N, R, seed)
lognormal	lognormal.pdf(x, mednX, covnX)	lognormal.cdf(x, [mednX, covnX])	lognormal.inv(P, mednX, covnX)	lognormal.rnd(mednX, covnX, N, R, seed)
normal	normal.pdf(x, meanX, sdvnX)	normal.cdf(x, [meanX, sdvnX])	normal.inv(p, meanX, sdvnX)	normal.rnd(meanX, sdvnX, N, R, seed)
poisson	poisson.pmf(k, t, T)	poisson.cdf(k, t, T)	--	poisson.rnd(t, T, N, R, seed)
quadratic	quadratic.pdf(x, a, b)	quadratic.cdf(x, [a, b])	quadratic.inv(u, a, b)	quadratic.rnd(a, b, N, R, seed)
rayleigh	rayleigh.pdf(x, meanX)	rayleigh.cdf(x, meanX)	rayleigh.inv(P, meanX)	rayleigh.rnd(meanX, N, R, seed)
students_t	students_t.pdf(t, k)	students_t.cdf(t, k)	students_t.inv(p, k)	students_t.rnd(k, N, R, seed)
triangular	triangular.pdf(x, a, b, c)	triangular.cdf(x, [a, b, c])	triangular.inv(p, a, b, c)	triangular.rnd(a, b, c, N, R, seed)
uniform	uniform.pdf(x, a, b)	uniform.cdf(x, [a, b])	uniform.inv(F, a, b)	uniform.rnd(a, b, N, R, seed)

Naming Conventions

Common Parameters:

- `x` , `t` , `k` , `n` : Evaluation points or event counts
- `N` : Number of samples (columns) to generate
- `R` : Correlation matrix ($n \times n$), optional. If None, uncorrelated samples
- `seed` : Random seed for reproducibility, optional

Distribution-Specific Parameters:

Bounds & Location:

- `a` , `b` : Lower and upper bounds (uniform, triangular, quadratic, beta)
- `c` : Mode (triangular)
- `meanX` , `mednX` : Mean or median
- `m` : Location parameter (extreme value, GEV)

Scale & Shape:

- `sdvnX` : Standard deviation
- `covnX` : Coefficient of variation (std/mean)
- `s` : Scale parameter (extreme value, GEV)
- `k` : Shape parameter or degrees of freedom (chi2, students_t, GEV)
- `q` , `p` : Shape parameters (beta)

Event/Count Parameters:

- `m` : Number of attempts (binomial)
 - `p` : Probability of success (binomial)
 - `t` : Time duration (poisson)
 - `T` : Mean return period (poisson)
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Notes

1. CDF signature pattern:

- Single-parameter distributions use direct parameter: `cdf(x, param)`
- Multi-parameter distributions use params array: `cdf(x, [param1, param2, ...])`
- This design facilitates curve fitting to empirical data

2. Return shapes:

- PDF/PMF, CDF: Returns `(n, N)` array for n random variables
- INV: Returns `(n, N)` or broadcast shape
- RND: Returns `(n, N)` array, or `(N,)` if n=1 (flattened for single variable)

3. Correlation:

- All `rnd()` functions support correlation matrix R via Gaussian copula method
- Correlation applies to the underlying standard normal or uniform variates

4. Discrete distributions:

- Binomial and Poisson have `pmf` (probability mass function) instead of `pdf`
 - No `inv` function for discrete distributions (not uniquely defined)
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Example Usage

```
import numpy as np
from multivariate.rvs import normal, lognormal, beta

# Single uncorrelated variable
x = np.linspace(-3, 3, 100)
f = normal.pdf(x, meanX=0, sdvnX=1)

# Multiple correlated variables can be specified as simple "lists"
meanX = [1.0, 2.0, 3.0] # mean values for three normal rv's
sdvnX = [0.5, 0.6, 0.7] # standard deviations for 3 normal rv's
R = [[1.0, 0.5, 0.3],    # orrelation matrix among three rv's
      [0.5, 1.0, 0.4],
      [0.3, 0.4, 1.0]])

# generate a sample 1000 values of three correlated normal rv's
X = normal.rnd(meanX, sdvnX, N=1000, R=R) # Shape: (3, 1000)

# Compute the marginal CDFs for each of the three normal rv's
F = normal.cdf(x, [meanX, sdvnX])
```