

Winter Term 20/21

# Graph Neural Networks

## Org & Introduction

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1. Organization and Motivation for Machine Learning on Graphs
2. Overview of Graph Theory and Network Science (metrics and topology)
3. Discovering Graph Structures (Clustering, Community)
4. Message Passing and Node Classification

## **Descriptive models**

5. Graph Representation Learning
6. Link Analysis - PageRank
7. Graph Convolutional Neural Networks
8. Graph Recurrent Networks
9. Graph Attention Networks
10. Temporal Graph Neural Networks

## **Prediction models**

11. Deep Generative Models for Graphs
12. Cascading behavior and Failure Propagation
13. Influence maximization
14. Outbreak minimization

## **Intervention models**

## **Phase-1: Foundations and Groundwork** (First 3 weeks)

90% of teaching and a few small tasks like setting up the environment, studying datasets, and learning how to use libraries. Lectures happening twice a week and individual meetings on-demand during the week.

## **Phase-2: Exploration and Exploitation** (Short lectures)

30 min teaching and quick project status updates (5-10 min maximum). We will keep having individual meetings on demand.

## **Phase-3: Consolidation** (Last two weeks)

writing the final report, which is a summary of the results that you would have presented in the weekly update meetings.

**Team size:** two, two persons or individual

## **Project proposal in three stages:**

- 1- Abstract (250 words): [Context][Problem][Investigation approach] - **in two weeks**
- 2- Related work (1 page, double column) containing summary and critique – **in four weeks**
- 3- Proposal - **first draft in six weeks**
  - Detail the problem (what is it, why should I care, why is it difficult)
  - Describe the dataset (source, size, main features, cite any papers that used it)
  - Determine the metrics and algorithms to be used (preliminary insights, it can change)
  - Discuss how you will evaluate your results (benchmarks and null-models)

## Datasets

- <http://networkrepository.com/>
- <https://snap.stanford.edu/data/>
- <https://networkdata.ics.uci.edu/>

## Tools (sorted by priority)

1. cuGraph: <https://github.com/rapidsai/cugraph> (Strongly recommend, fast)
2. NetworkX: <https://networkx.org/documentation/stable/tutorial.html> (great coverage of graph algorithms)
3. Snap for Python: <http://snap.stanford.edu/snappy/index.html>
4. Pytorch Geometric: <https://pytorch-geometric.readthedocs.io/en/latest/>
5. Github project: <https://github.com/orgs/hpi-sam/projects/3>

# Communicantion Plan

Motive	Content	Medium
<b>Artifacts</b>	Source code, Data Documentation, Wiki	Github - <a href="https://github.com/orgs/hpi-sam/">https://github.com/orgs/hpi-sam/</a>
<b>Papers</b>	Copyrighted material	Bib-Admin
<b>Messaging ad hoc</b>	Questions, Suggestions, Sharing	Our Slack group: <a href="https://graph-neural-networks.slack.com">graph-neural-networks.slack.com</a>
<b>Official communications</b>	Schedule, Orientations	Email
<b>Meetings</b>	Lectures, Status, Work meetings	Zoom, Skype
<b>Emergency</b>	Call, SMS, messaging	Chris mobile number (check my Slack profile)

## **To pass the project seminar, we expect sufficient contributions to:**

- the discussions in meetings (preliminary results and readings)
- the experiments
- the final report
- the final presentation

## **Grading:**

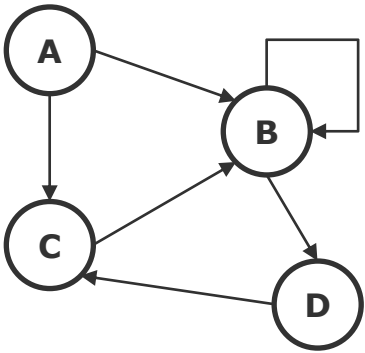
- project (60%)
- report (30%)
- presentation (10%)

# Basic Concepts

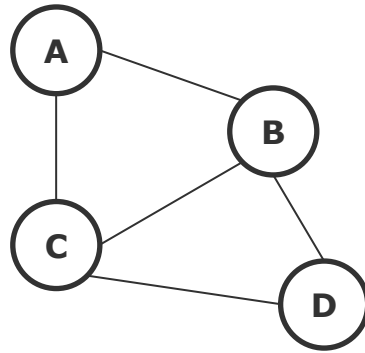


# Types of graphs

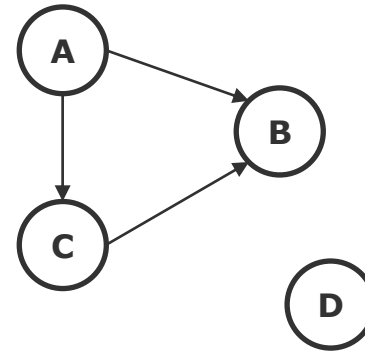
**Directed**



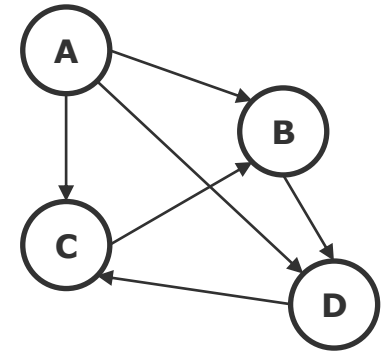
**Undirected**



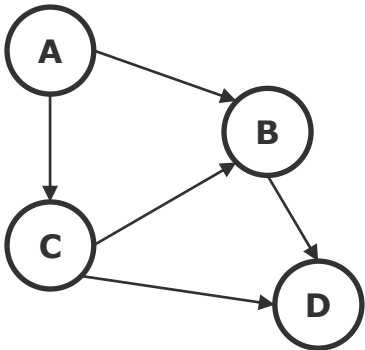
**Disconnected**



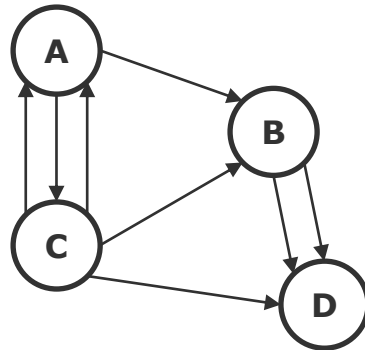
**Fully connected**



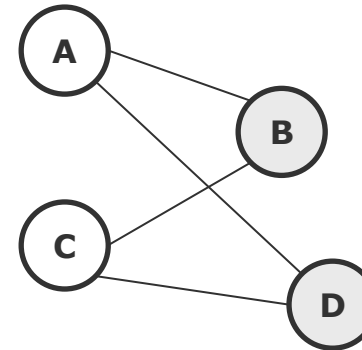
**Directed Acyclic Graph**



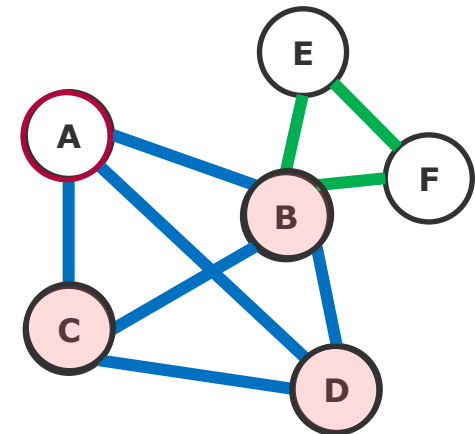
**Multigraph**



**Bipartite**



**Cliques**



**Ego network of A**

# Node and Edge degrees

Node degree: number of edges of node  $k_i$ , where  $i$  is the node index

Indegree: number of incoming edges

Outdegree: number of outgoing edges

Average degree:  $\bar{k} = \frac{1}{N} \sum_{i \in N} k_i = \frac{2E}{N}$   
, where  $E$  = number of edges,  $N$ =number of nodes

Maximum number of edges:  $E_{\max} = \binom{N}{2} = \frac{N(N-1)}{2}$

However, most real-world networks are sparse, i.e.,  $E \ll E_{\max}$

# Most real-world networks are sparse

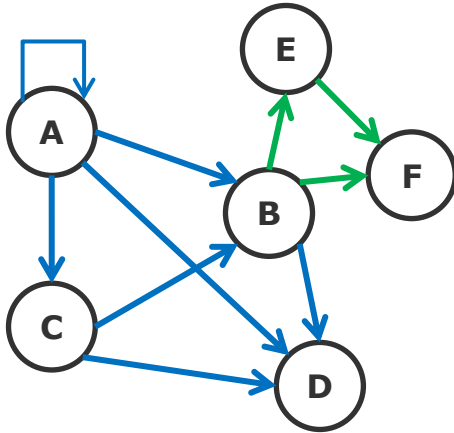
Network	$N$	$E$	$N_b$	$E_b$	$\bar{d}$	Description
Social networks						
DELICIOUS	147,567	301,921	0.40	0.65	4.09	delicio.us collaborative tagging social network
EPINIONS	75,877	405,739	0.48	0.90	10.69	Who-trusts-whom network from epinions [Richardson 03]
FLICKR	404,733	2,110,078	0.33	0.86	10.43	Flickr photo sharing social network [Kumar et al. 06]
LINKEDIN	6,946,668	30,507,070	0.47	0.88	8.78	Social network of professional contacts
LIVEJOURNAL01	3,766,521	30,629,297	0.78	0.97	16.26	Friendship network of a blogging community [Krumm et al. 06]
LIVEJOURNAL11	4,145,160	34,469,135	0.77	0.97	16.63	Friendship network of a blogging community [Krumm et al. 06]
LIVEJOURNAL12	4,843,953	42,845,684	0.76	0.97	17.69	Friendship network of a blogging community [Krumm et al. 06]
MESSENGER	1,878,736	4,079,161	0.53	0.78	4.34	Instant messenger social network
EMAIL-ALL	234,352	383,111	0.18	0.50	3.27	Research organization email network (all addresses) [Leskovec et al. 07b]
EMAIL-INOUT	37,803	114,199	0.47	0.82	6.04	(all addresses but email has to be sent both ways) [Leskovec et al. 07b]
EMAIL-INSIDE	986	16,064	0.90	0.99	32.58	(only emails inside the research organization) [Leskovec et al. 07b]
EMAIL-ENRON	33,696	180,811	0.61	0.90	10.73	Enron email data set [Klimt and Yang 04]
ANSWERS	488,484	1,240,189	0.45	0.78	5.08	Yahoo Answers social network
ANSWERS-1	26,971	91,812	0.56	0.87	6.81	Cluster 1 from Yahoo Answers
ANSWERS-2	25,431	65,551	0.48	0.80	5.16	Cluster 2 from Yahoo Answers
ANSWERS-3	45,122	165,648	0.53	0.87	7.34	Cluster 3 from Yahoo Answers
ANSWERS-4	93,971	266,199	0.49	0.82	5.67	Cluster 4 from Yahoo Answers
ANSWERS-5	5,313	11,528	0.41	0.73	4.34	Cluster 5 from Yahoo Answers
ANSWERS-6	290,351	613,237	0.40	0.71	4.22	Cluster 6 from Yahoo Answers
Information (citation) networks						
CIT-PATENTS	3,764,105	16,511,682	0.82	0.96	8.77	Citation network of all US patents [Leskovec et al. 07c]
CIT-HEP-PH	34,401	420,784	0.96	1.00	24.46	Citations between physics (ArXiv hep-th) [Gehrke et al. 03]
CIT-HEP-TH	27,400	352,021	0.94	0.99	25.69	Citations between physics (ArXiv hep-ph) [Gehrke et al. 03]
BLOG-NAT05-6M	29,150	182,212	0.74	0.96	12.50	Blog citation network (6 months of data) [Leskovec et al. 07c]

$$\bar{d} = \bar{k} = \text{average degree}$$

source :Leskovec, J., et al.  
"Community structure in large networks: Natural cluster sizes and the absence of large well-defined clusters." *Internet Mathematics* 6.1 (2009): 29-123.

# Adjacency matrix

**Cliques**



	<b>A</b>	<b>C</b>	<b>D</b>	<b>B</b>	<b>E</b>	<b>F</b>
<b>A</b>	1	1	1	1	0	0
<b>C</b>	1	0	1	1	0	0
<b>D</b>	1	1	0	1	0	0
<b>B</b>	1	1	1	0	1	1
<b>E</b>	0	0	0	1	0	1
<b>F</b>	0	0	0	1	1	0

However, adjacency matrix of real-world networks are full of zeros

# Motivation for Learning on Graphs and GNNs

## **Network Types**

- Event graphs
- Disease pathways
- Knowledge-graphs
- Scene graphs
- Heterogeneous graphs (different types of nodes and edges)

## **Scenarios**

- Clustering in Social network
- Protein interaction
- Cell similarity networks
- Failure propagation in infrastructure networks
- Fake news detection
- Side-effects of drugs
- Network attacks
- Traffic jams

## **Node classification**

What type of node is this?

## **Link prediction**

Are these two nodes connected?

With which strength?

## **Graph Classification**

Patterns of connectivity (motifs)

Network similarity (isomorphism)

## **Lecture-2: Overview of Graph Theory and Network Science (Wed 13h30 - 15h00)**

- Degree Distribution
- Path length
- Clustering Coefficient
- Null-Models for Graphs

### **First task:**

- Accept Slack invitation
- Study datasets
- See examples of use of Snap or NetworkX
- Think of scenarios



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