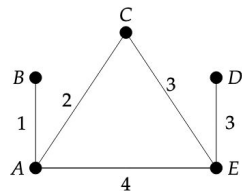


Centrality metrics

Subtask 1

1.1 - Summary of centrality metrics

- path-based centrality [4]
 - temporal closeness
 - temporal betweenness
- spectral centrality [3, 4, 5]
 - temporal communicability centrality [4]
 - temporal eigenvector-based [5]
 - generalization by using a supra-centrality matrix
 - joint, marginal and conditional centralities
 - average centrality over time, first-order mover scores
 - temporal page rank [3]



[4]

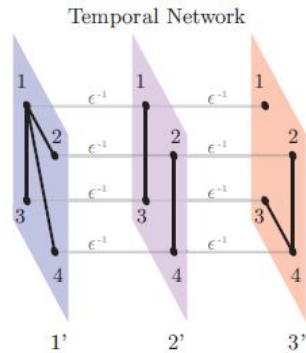
$$\mathbb{C}(\epsilon) = \begin{bmatrix} \epsilon \mathbf{C}^{(1)} & \mathbf{I} & 0 & \dots \\ \mathbf{I} & \epsilon \mathbf{C}^{(2)} & \mathbf{I} & \ddots \\ 0 & \mathbf{I} & \epsilon \mathbf{C}^{(3)} & \ddots \\ \vdots & \ddots & \ddots & \ddots \end{bmatrix}$$

[5]

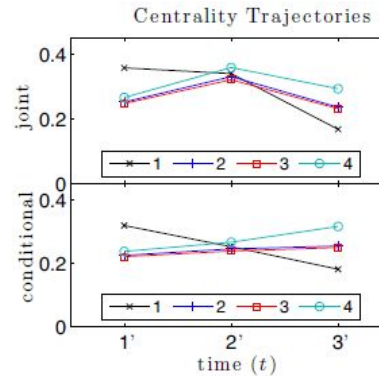
Subtask 1

1.2 - What would be the impact on centrality metric if we ignore the temporal aspect

- aggregation: could simulate information going from the future to the past [4]
- unable to examine trajectories and temporal states [5]



[5]



Subtask 1

1.3 - What are the assumptions (constraints, hyperparameters) involved in temporal-based centrality measurements?

- online algorithms [4]
 - only applicable for networks with slow dissemination rate
- shortest path-based (hyperparameter t) [4]
 - snapshot method
 - looks at aggregated time period (chronological order disregarded)
 - paths in between snapshot time periods not taken into consideration
 - Temporal closeness
 - considered paths only in certain time interval
 - higher order aggregate network
 - disregards chronological order within aggregation
 - representation as global importance (single value)
- eigenvector-based: [5]
 - discrete representation
 - supra-centrality matrix nonnegative and irreducible
 - hyperparameter: ϵ for temporal coupling strength

additional notes we had for slide 4:

- eigenvector-based: [5]
 - discrete representation (and continuous with binned timestamps)
 - time (interlayer) edges are undirected -> no causality represented
 - C has to be nonnegative and irreducible (for every w respectively e) -> network constraints:
 - network associated with C (if it would display a new graph as adjacency matrix without considering time extra) has to be strongly connected
 - sufficient: when all centrality matrices C_t are nonnegative and sum over those has strongly connected associated network
 - hyperparameter: w respective e , weights the influence of interlayer connections (how much the other timesteps influence a timestep) i.e. defines the (temporal) coupling, very important
 - computational cost $NT \times NT$ can be high for large networks with many timesteps
- online algorithm: node is updated every time network changed [4]

Subtask 2

2.1 - Summarize the temporal effect on centrality

general effect: times are considered in addition to topological aspects -> shortest temporal path based on topology and latency [6]

comparison of different centrality metrics for dynamic networks (temporality) on different datasets from several domains [7]

- different centrality metrics lead to different results (not necessarily one definitive central node)
- centrality is meaningless as a metric if dataset is extremely dynamic and does not have longer-term center
- nodes that are temporarily inactive might still have high centrality value (on important temporal path)
- low global average centrality might give false impression for important but only temporarily active nodes

=> snapshot method only applicable to a limited extent [7]

=> temporal eigenvector less accurate than temporal closeness (considers paths that can go backwards in time) [6, 7] 6

Subtask 2

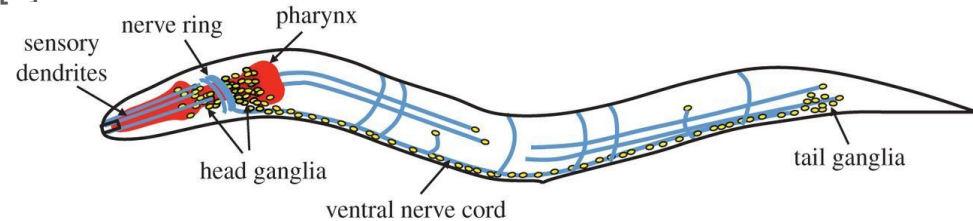
2.2. - three networks that, in your opinion, are most closely related to the the phenomenon of event propagation on an evolving graph

- urban transport system (spatio-temporal) [6]
 - propagation of passenger travel
 - speed: averaged speed of serving trains in time interval



[8]

- biological neural network (spatio-temporal) [6]
 - signal transmission between neurons
 - structure: synaptic connections



- mobile phone communication (temporal only) [6]
 - calls and sms as edges

[9]

Subtask 2

2.3 - What are the types of node importance (or phenomenon) that temporal-based centrality metric helps to capture?

- node aspects: spatial, temporal and topological [6]
- how quickly information from the node reaches the rest of the network -> temporal in-closeness [6]
 - temporal in-closeness: based on distances to all nodes
- how much the network relies on the node for connecting -> path betweenness [6]
 - path betweenness: based on shortest paths that pass through it
 - in experiments: mostly affects the giant strong component size
- how important the node is for fast information propagation throughout the network -> betweenness efficiency [6]
 - betweenness efficiency: takes the reciprocal temporal distance of shortest paths through node into account
 - in experiments: mostly affects the temporal efficiency/robustness

Subtask 2

2.4 - What are the limitations of the temporal-based centrality measures to rank or identify nodes by importance?

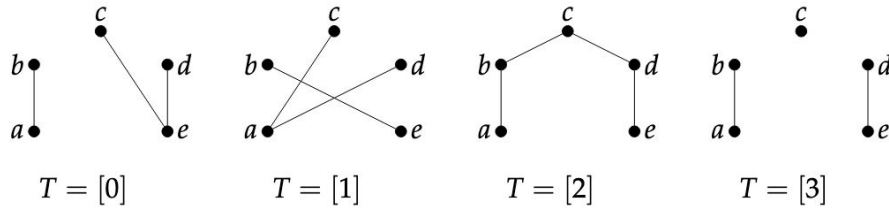


Figure 1.4: A representation of a dynamic graph in the form of 4 snapshots representing each 1 instant.

[4]

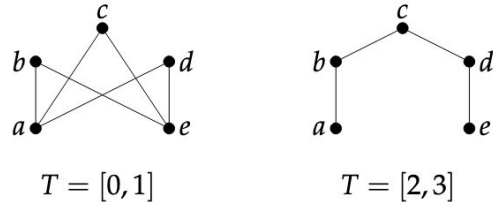


Figure 1.5: A representation of a dynamic graph in Figure 1.4 in the form of 2 snapshots representing each 2 instants.

[4]

additional notes we had for slide 9:

- the observation window plays a role (is a parameter) [6]
- purely temporal without spatial: assumption of instantaneous propagation (not considering spatial aspect: distance and speed), temporally shortest path: only considers (minimum) latency and not (minimum) distance, in their experiments: attacks were then not so effective [6]
- limit of temporal in-closeness: does not represent how much the network relies on the node for connecting (source of fragility) [6]
 - in their experiments: mostly identifies sink nodes for information flow -> their deactivation does not have so much influence on the network performance -> TC-based attack not so effective
- limit of path betweenness: does not represent which nodes are important for fast propagation throughout the network [6]
- limit of degree-based: does not consider global network information [6]
 - in their exp. : D-based attack not so effective

Usage in WPs

- in WP 2: failure in more central nodes probably spreads faster
- in WP 3: could use centrality to identify which nodes to attack
 - like in paper [6]

Sources

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