Numpy, TF, and Visualization

Start by importing necessary packages

We will begin by importing necessary libraries for this notebook. Run the cell below to do so.

```
import numpy as np
import matplotlib.pyplot as plt
import math
import tensorflow as tf
```

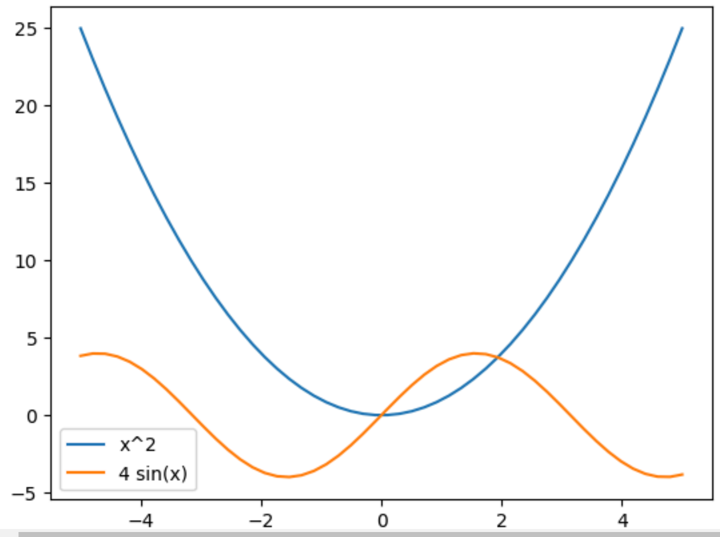
Visualizations

Visualization is a key factor in understanding deep learning models and their behavior. Typically, pyplot from the matplotlib package is used, capable of visualizing series and 2D data.

Below is an example of visualizing series data.

```
x = np.linspace(-5, 5, 50) # create a linear spacing from x = -5.0 to 5.0 with 50 steps

y1 = x**2      # create a series of points {y1}, which corresponds to the function f(x) = y^2
y2 = 4*np.sin(x) # create another series of points {y2}, which corresponds to the function f(x) = 4*sin(x)  NOTE: we have to use np.sin a
# to use math.sin, we could have used a list comprehension instead: y2 = [math.sin(xi) for xi in x]

# by default, matplotlib will behave like MATLAB with hold(True), overplotting until a new figure object is created
plt.plot(x, y1, label="x^2")        # plot y1 with x as the x-axis series, and label the line "x^2"
plt.plot(x, y2, label="4 sin(x)")   # plot y2 with x as the x-axis series, and label the line "4 sin(x)"
plt.legend()                        # have matplotlib show the label on the plot
```

```
<matplotlib.legend.Legend at 0x79152aaf4190>
```



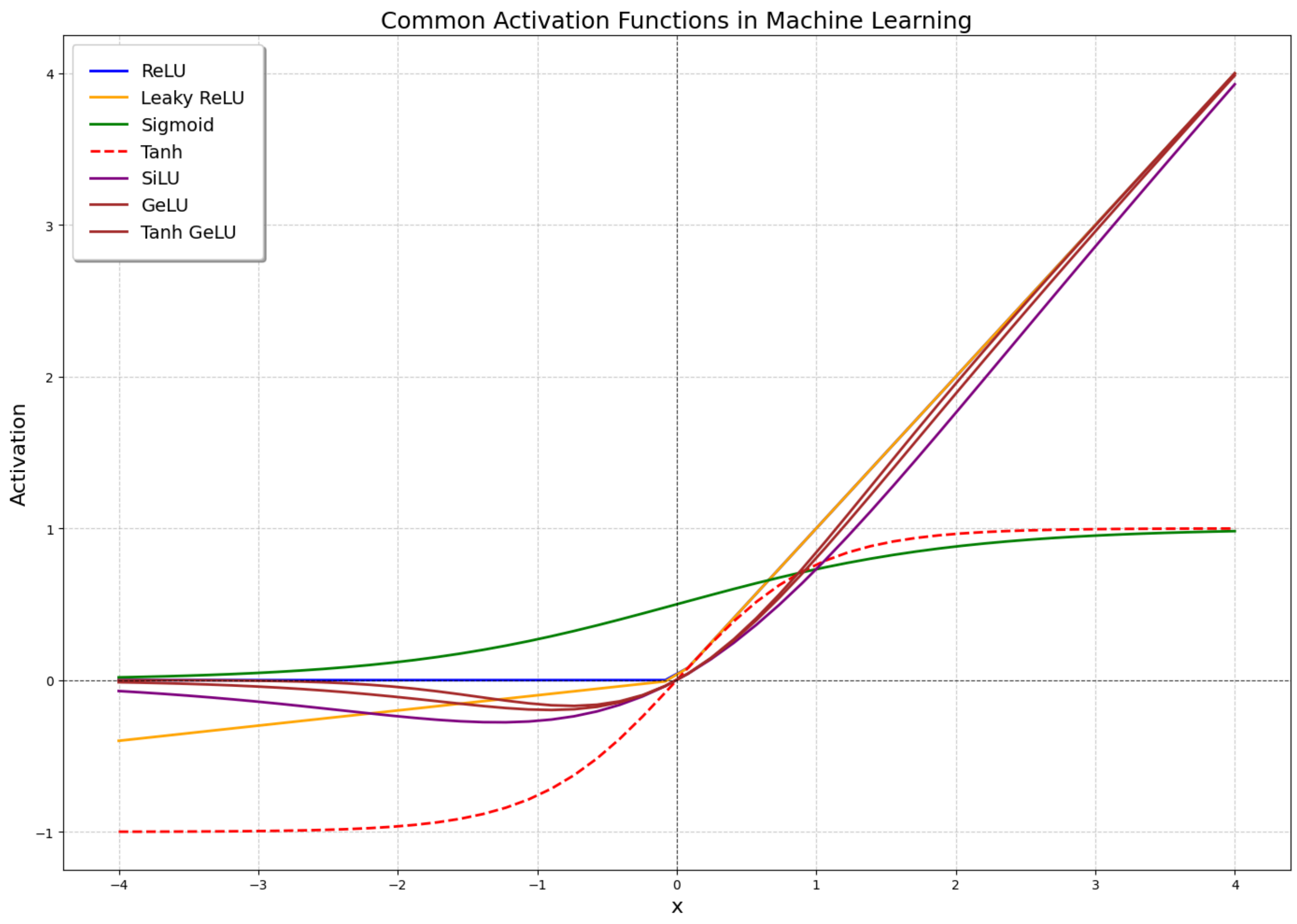
More complex formatting can be added to increase the visual appeal and readability of plots (especially for paper quality figures). To try this out, let's consider plotting a few of the more common activation functions used in machine learning. Below, plot the following activation functions for $x \in [-4, 4]$:

- ReLU: $max(x, 0)$
- Leaky-ReLU: $max(0.1 \cdot x, x)$
- Sigmoid: $\sigma(x) = 1/(1 + e^{-x})$
- Hyperbolic Tangent: $\tanh(x) = (e^x - e^{-x})/(e^x + e^{-x})$
- SiLU: $x \cdot \sigma(x)$
- GeLU: $x \cdot \frac{1}{2}\left(1 + \text{erf}\left(\frac{x}{\sqrt{2}}\right)\right)$
- tanh GELU: $x \cdot \frac{1}{2}\left(1 + \tanh\left(\frac{x}{\sqrt{2}}\right)\right)$

Plot the GELU and tanh GELU using the same color, but with tanh using a dashed line (tanh is a common approximation as the error-function is computationally expensive to compute). You may also need to adjust the legend to make it easier to read. I recommend using ChatGPT to help find the formatting options here.

Question 1

```
import numpy as np
import matplotlib.pyplot as plt
from scipy.special import erf

# Define activation functions
def relu(x):
    return np.maximum(x, 0)

def leaky_relu(x):
    return np.maximum(0.1 * x, x)

def sigmoid(x):
    return 1 / (1 + np.exp(-x))

def tanh(x):
    return np.tanh(x)

def silu(x):
    return x * sigmoid(x)

def gelu(x):
    return x * 0.5 * (1 + erf(x / np.sqrt(2)))

def tanh_gelu(x):
    return x * 0.5 * (1 + np.tanh(x / np.sqrt(2)))

# Generate x values
x = np.linspace(-4, 4, 50)

# Generate y values for each activation function
y_relu = relu(x)
y_leaky_relu = leaky_relu(x)
y_sigmoid = sigmoid(x)
y_tanh = tanh(x)
y_silu = silu(x)
y_gelu = gelu(x)
y_tanh_gelu = tanh_gelu(x)

# Plot
plt.figure(figsize=(14, 10))

# Plot each function
plt.plot(x, y_relu, label='ReLU', color='blue', linewidth=2)
plt.plot(x, y_leaky_relu, label='Leaky ReLU', color='orange', linewidth=2)
plt.plot(x, y_sigmoid, label='Sigmoid', color='green', linewidth=2)
plt.plot(x, y_tanh, label='Tanh', linestyle='--', color='red', linewidth=2)
plt.plot(x, y_silu, label='SiLU', color='purple', linewidth=2)
plt.plot(x, y_gelu, label='GeLU', color='brown', linewidth=2)
plt.plot(x, y_tanh_gelu, label='Tanh GeLU', color='brown', linewidth=2)

# Add labels and title
plt.xlabel('x', fontsize=16)
plt.ylabel('Activation', fontsize=16)
plt.title('Common Activation Functions in Machine Learning', fontsize=18)

# Customize legend
plt.legend(loc='upper left', fontsize=14, frameon=True, shadow=True, borderpad=1)

# Add grid
plt.grid(True, linestyle='--', alpha=0.6)

# Highlight axes
plt.axhline(0, color='black', linewidth=0.8, linestyle='--', alpha=0.7)
plt.axvline(0, color='black', linewidth=0.8, linestyle='--', alpha=0.7)

# Tight layout for better spacing
plt.tight_layout()

# Show the plot
plt.show()
```



Answer to the following questions from the the plot you just created:

1. Which activation function is the least computationally expensive to compute?
2. Are there better choices to ensure more stable training? What downfalls do you think it may have?
3. Are there any cases where you would not want to use either activation function?

Question 2

Answer: 1.Computationally Least Expensive: ReLU, because it only has to perform a max(x, 0) operation. 2.What Works Best for Stability vS Gradients: Tanh, Sigmoid, SiLU, and GeLU offer smoother gradients but: Also Tanh/Sigmoid: Have vanishing gradients and are computationally expensive SiLU/GeLU: More stable but also expensive. 3.When Not to Use: ReLU: Do not use if you have a dead neuron problem. Sigmoid/Tanh: Don't use in deep networks (vanishing gradients). SiLU/GeLU: Use cautiously in resource-constrained settings. Leaky ReLU: Is not the best if smooth gradient flow is the preference..

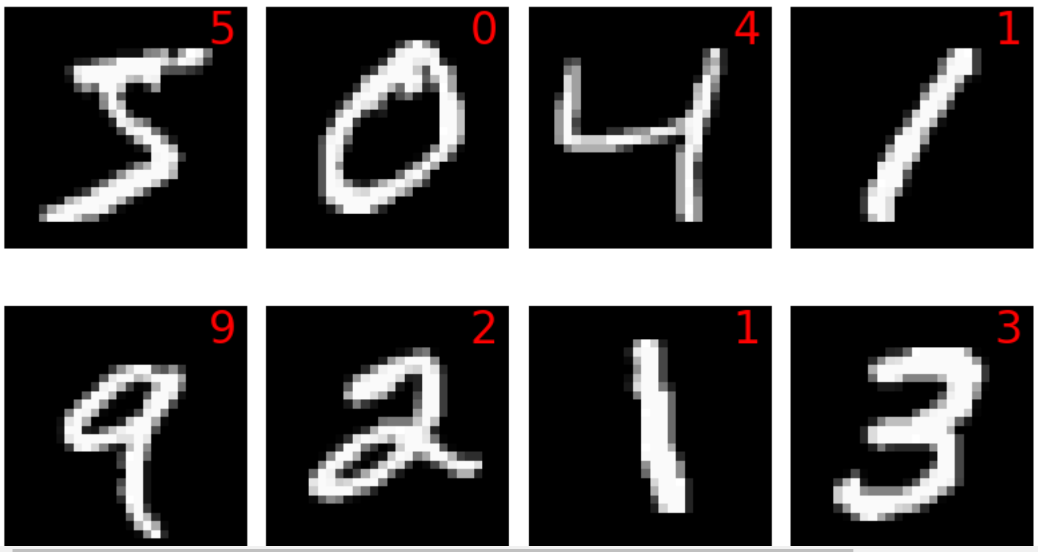
Visualizing 2D data

In many cases, we also want the ability to visualize multi-dimensional data such as images. To do so, matplotlib has the imshow method, which can visualize single channel data with a heatmap, or RGB data with color.

Let's consider visualizing the first 8 training images from the MNIST dataset. MNIST consists of hand drawn digits with their corresponding labels (a number from 0 to 9).

We will use the tensorflow keras dataset library to load the dataset, and then visualize the images with a matplotlib subplot. Because we have so many images, we should arrange them in a grid (4 horizontal, 2 vertical), and plot each image in a loop. Furthermore, we can append the label to each image using the matplotlib utility.

```
from tensorflow.keras.datasets import mnist

(train_images, train_labels), (test_images, test_labels) = mnist.load_data()

# Define the grid dimensions
rows, cols = 2, 4

# Create a figure and axes for the grid
fig, axes = plt.subplots(rows, cols, figsize=(8, 5))

# Iterate through the grid
for i in range(rows):
    for j in range(cols):
        index = i * cols + j
        ax = axes[i, j]

        # Display the image
        ax.imshow(train_images[index], cmap='gray')

        # Display the label on top of the image in red text
        ax.text(0.9, 0.9, str(train_labels[index]), color='red',
                transform=ax.transAxes, fontsize=24,
                ha='center', va='center')

        # Turn off axis labels
        ax.axis('off')

# Adjust spacing and layout
plt.tight_layout()
```



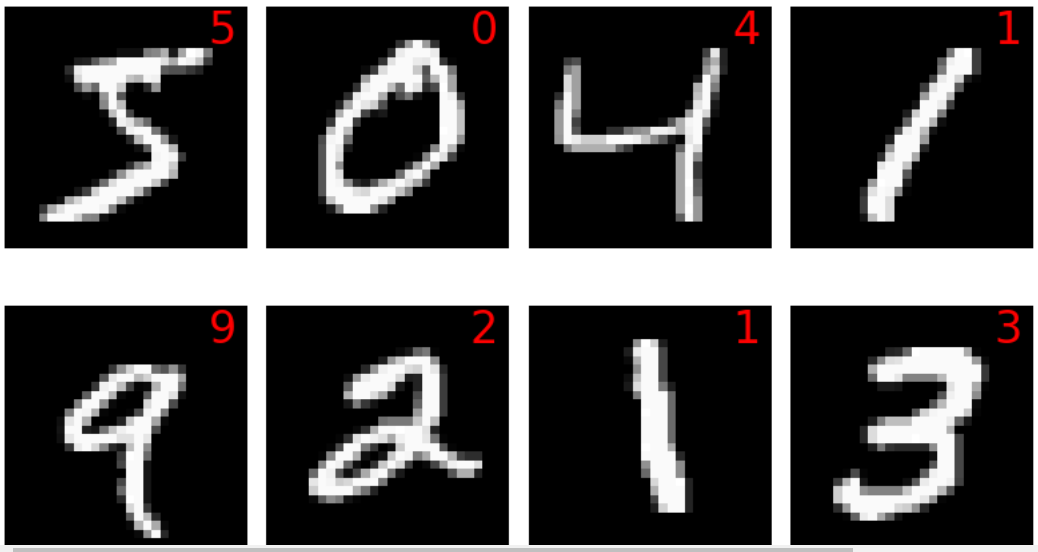
Another popular image dataset for benchmarking and evaluation is CFAR-10. This dataset consists of small (32 x 32 pixel) RGB images of objects that fall into one of 10 classes:

0. airplane
1. automobile
2. bird
3. cat
4. deer
5. dog
6. frog
7. horse
8. ship
9. truck

Plot the first 32 images in the dataset using the same method above.

Question 3

```
import matplotlib.pyplot as plt
from tensorflow.keras.datasets import mnist

# Load the MNIST dataset
(train_images, train_labels), (test_images, test_labels) = mnist.load_data()

# Define the grid dimensions
rows, cols = 2, 4

# Create a figure and axes for the grid
fig, axes = plt.subplots(rows, cols, figsize=(8, 5))

# Iterate through the grid and display the images
for i in range(rows):
    for j in range(cols):
        index = i * cols + j
        ax = axes[i, j]

        # Display the image
        ax.imshow(train_images[index], cmap='gray')

        # Display the label on top of the image in red text
        ax.text(0.9, 0.9, str(train_labels[index]), color='red',
                transform=ax.transAxes, fontsize=24,
                ha='center', va='center')

        # Turn off axis labels
        ax.axis('off')

# Adjust spacing and layout
plt.tight_layout()

# Show the plot
plt.show()
```



Visualizing Tensors

Aside from visualzing linear functions and images, we can also visualize entire tensors from DL models.

```
# first, let's download an existing model to inspect
model = tf.keras.applications.VGG16(weights='imagenet')

# can then print the summary of what the model is composed of
print(model.summary())
```

```
Model: "vgg16"
┏━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━┳━━━━━━━━━━━━━━━━━━━━━━━━┳━━━━━━━━━━━━━━━┓
┃ Layer (type)                    ┃ Output Shape           ┃       Param # ┃
┡━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━╇━━━━━━━━━━━━━━━━━━━━━━━━╇━━━━━━━━━━━━━━━┩
│ input_layer_4 (InputLayer)      │ (None, 224, 224, 3)    │             0 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block1_conv1 (Conv2D)           │ (None, 224, 224, 64)   │         1,792 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block1_conv2 (Conv2D)           │ (None, 224, 224, 64)   │        36,928 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block1_pool (MaxPooling2D)      │ (None, 112, 112, 64)   │             0 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block2_conv1 (Conv2D)           │ (None, 112, 112, 128)  │        73,856 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block2_conv2 (Conv2D)           │ (None, 112, 112, 128)  │       147,584 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block2_pool (MaxPooling2D)      │ (None, 56, 56, 128)    │             0 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block3_conv1 (Conv2D)           │ (None, 56, 56, 256)    │       295,168 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block3_conv2 (Conv2D)           │ (None, 56, 56, 256)    │       590,080 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block3_conv3 (Conv2D)           │ (None, 56, 56, 256)    │       590,080 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block3_pool (MaxPooling2D)      │ (None, 28, 28, 256)    │             0 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block4_conv1 (Conv2D)           │ (None, 28, 28, 512)    │     1,180,160 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block4_conv2 (Conv2D)           │ (None, 28, 28, 512)    │     2,359,808 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block4_conv3 (Conv2D)           │ (None, 28, 28, 512)    │     2,359,808 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block4_pool (MaxPooling2D)      │ (None, 14, 14, 512)    │             0 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block5_conv1 (Conv2D)           │ (None, 14, 14, 512)    │     2,359,808 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block5_conv2 (Conv2D)           │ (None, 14, 14, 512)    │     2,359,808 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block5_conv3 (Conv2D)           │ (None, 14, 14, 512)    │     2,359,808 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ block5_pool (MaxPooling2D)      │ (None, 7, 7, 512)      │             0 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ flatten (Flatten)               │ (None, 25088)          │             0 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ fc1 (Dense)                     │ (None, 4096)           │   102,764,544 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ fc2 (Dense)                     │ (None, 4096)           │    16,781,312 │
├─────────────────────────────────┼────────────────────────┼───────────────┤
│ predictions (Dense)             │ (None, 1000)           │     4,097,000 │
└─────────────────────────────────┴────────────────────────┴───────────────┘
```

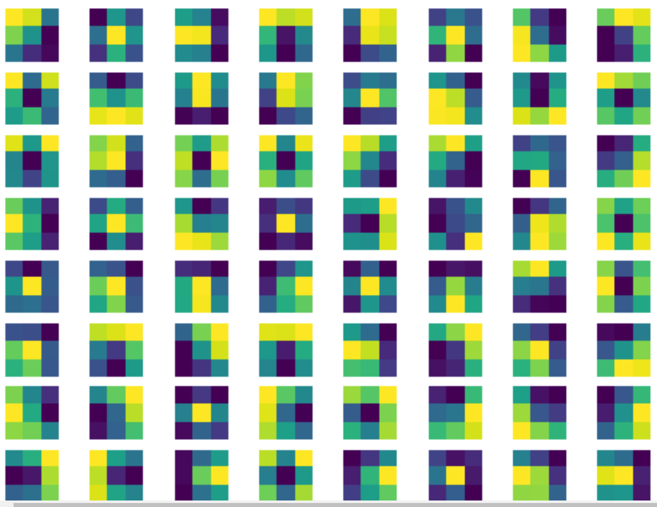
```python
# we can also print the model layers based on index to better understand the structure
for i,layer in enumerate(model.layers):
  print(f"{i}: {layer}")
```

```
0: <InputLayer name=input_layer_4, built=True>
1: <Conv2D name=block1_conv1, built=True>
2: <Conv2D name=block1_conv2, built=True>
3: <MaxPooling2D name=block1_pool, built=True>
4: <Conv2D name=block2_conv1, built=True>
5: <Conv2D name=block2_conv2, built=True>
6: <MaxPooling2D name=block2_pool, built=True>
7: <Conv2D name=block3_conv1, built=True>
8: <Conv2D name=block3_conv2, built=True>
9: <Conv2D name=block3_conv3, built=True>
10: <MaxPooling2D name=block3_pool, built=True>
11: <Conv2D name=block4_conv1, built=True>
12: <Conv2D name=block4_conv2, built=True>
13: <Conv2D name=block4_conv3, built=True>
14: <MaxPooling2D name=block4_pool, built=True>
15: <Conv2D name=block5_conv1, built=True>
16: <Conv2D name=block5_conv2, built=True>
17: <Conv2D name=block5_conv3, built=True>
18: <MaxPooling2D name=block5_pool, built=True>
19: <Flatten name=flatten, built=True>
20: <Dense name=fc1, built=True>
21: <Dense name=fc2, built=True>
22: <Dense name=predictions, built=True>
```

Not all of these layers contain weights, for example, MaxPooling2D is a stateless operation, and so is Flatten. Conv2D and Dense are the two layer types that can be visualized. That said, let's visualize the filter kernels in the first convoluton layer.

```python
# next we can extract som
layer = model.layers[1] # Get the first convolutional layer
weights = layer.get_weights()[0]
```

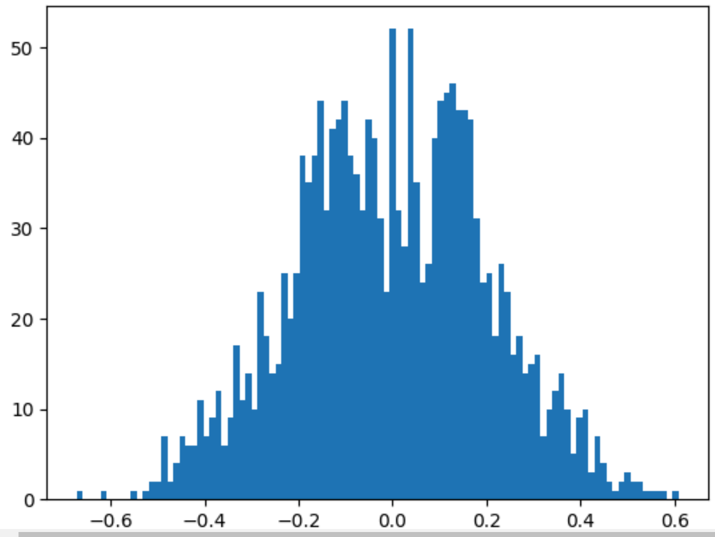
```
n_filters = weights.shape[-1]

for i in range(n_filters):
    plt.subplot(8, 8, i+1)  # Assuming 64 filters, adjust if necessary
    plt.imshow(weights[:, :, 0, i], cmap="viridis")
    plt.axis('off')
```



Aside from visualizing the weights directly, we can also compute and visualize the weight distribution using a histogram.

```
# we can use the mean and var (variance) functions built in to calculate some simple statistics
print(f"weight tensor has mean: {weights.mean()} and variance: {weights.var()}")

# we need to call .flatten() on the tensor so that all the histogram sees them as a 1D array. Then we can plot with 100 bins to get a bi
plt.hist(weights.flatten(), bins=100)
```

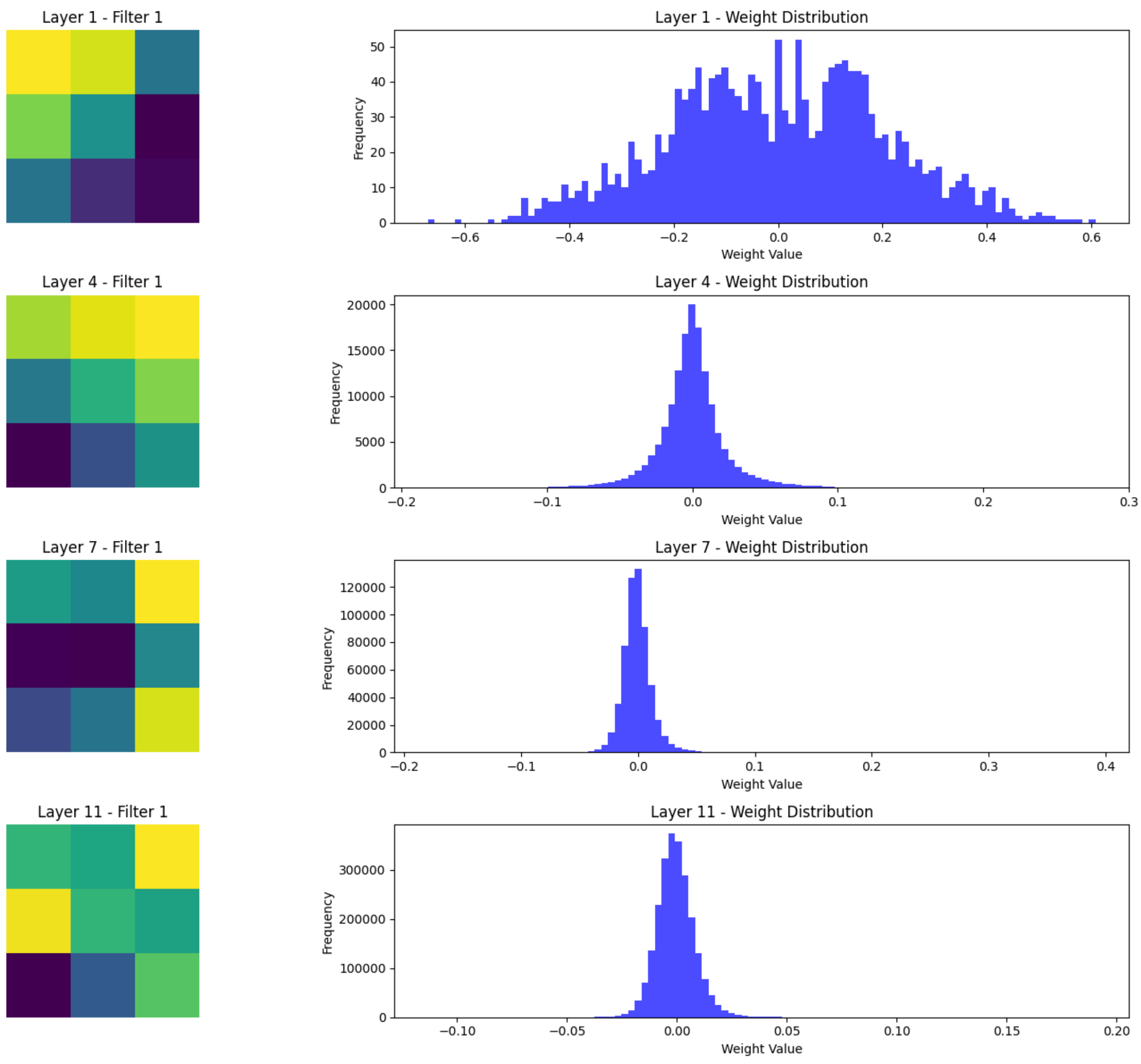
```
weight tensor has mean: -0.0024379086680710316 and variance: 0.04272466152906418
(array([ 1.,  0.,  0.,  0.,  1.,  0.,  0.,  0.,  0.,  1.,  0.,  1.,  2.,
         2.,  7.,  2.,  4.,  7.,  6.,  6., 11.,  7.,  9., 12.,  6.,  9.,
        17., 11., 14., 10., 23., 18., 14., 15., 25., 20., 25., 38., 35.,
        38., 44., 32., 41., 42., 44., 38., 36., 32., 42., 40., 31., 23.,
        52., 32., 28., 52., 35., 24., 26., 40., 44., 45., 46., 43., 43.,
        42., 31., 24., 25., 18., 26., 23., 16., 18., 14., 15., 16.,  7.,
        10., 12., 14., 10.,  5.,  9., 10.,  3.,  7.,  4.,  2.,  1.,  2.,
         3.,  2.,  2.,  1.,  1.,  1.,  1.,  0.,  1.]),
 array([-0.67140007, -0.65860093, -0.64580172, -0.63300258, -0.62020344,
        -0.60740429, -0.59460509, -0.58180594, -0.5690068 , -0.55620766,
        -0.54340845, -0.53060931, -0.51781017, -0.50501096, -0.49221182,
        -0.47941267, -0.4666135 , -0.45381436, -0.44101518, -0.42821604,
        -0.41541687, -0.40261772, -0.38981855, -0.37701941, -0.36422023,
        -0.35142106, -0.33862191, -0.32582274, -0.3130236 , -0.30022442,
        -0.28742528, -0.27462611, -0.26182696, -0.24902779, -0.23622863,
        -0.22342947, -0.21063031, -0.19783115, -0.185032  , -0.17223284,
        -0.15943368, -0.14663452, -0.13383536, -0.12103619, -0.10823704,
        -0.09543788, -0.08263872, -0.06983955, -0.0570404 , -0.04424123,
        -0.03144208, -0.01864292, -0.00584376,  0.0069554 ,  0.01975456,
         0.03255372,  0.04535288,  0.05815204,  0.0709512 ,  0.08375036,
         0.09654953,  0.10934868,  0.12214784,  0.134947  ,  0.14774616,
         0.16054532,  0.17334448,  0.18614364,  0.1989428 ,  0.21174197,
         0.22454113,  0.23734029,  0.25013945,  0.26293859,  0.27573776,
         0.28853691,  0.30133608,  0.31413525,  0.3269344 ,  0.33973357,
         0.35253271,  0.36533189,  0.37813103,  0.39093021,  0.40372935,
         0.41652852,  0.42932767,  0.44212684,  0.45492601,  0.46772516,
         0.48052433,  0.49332348,  0.50612265,  0.51892179,  0.53172094,
         0.54452014,  0.55731928,  0.57011843,  0.58291757,  0.59571677,
         0.60851592]),
 <BarContainer object of 100 artists>)
```

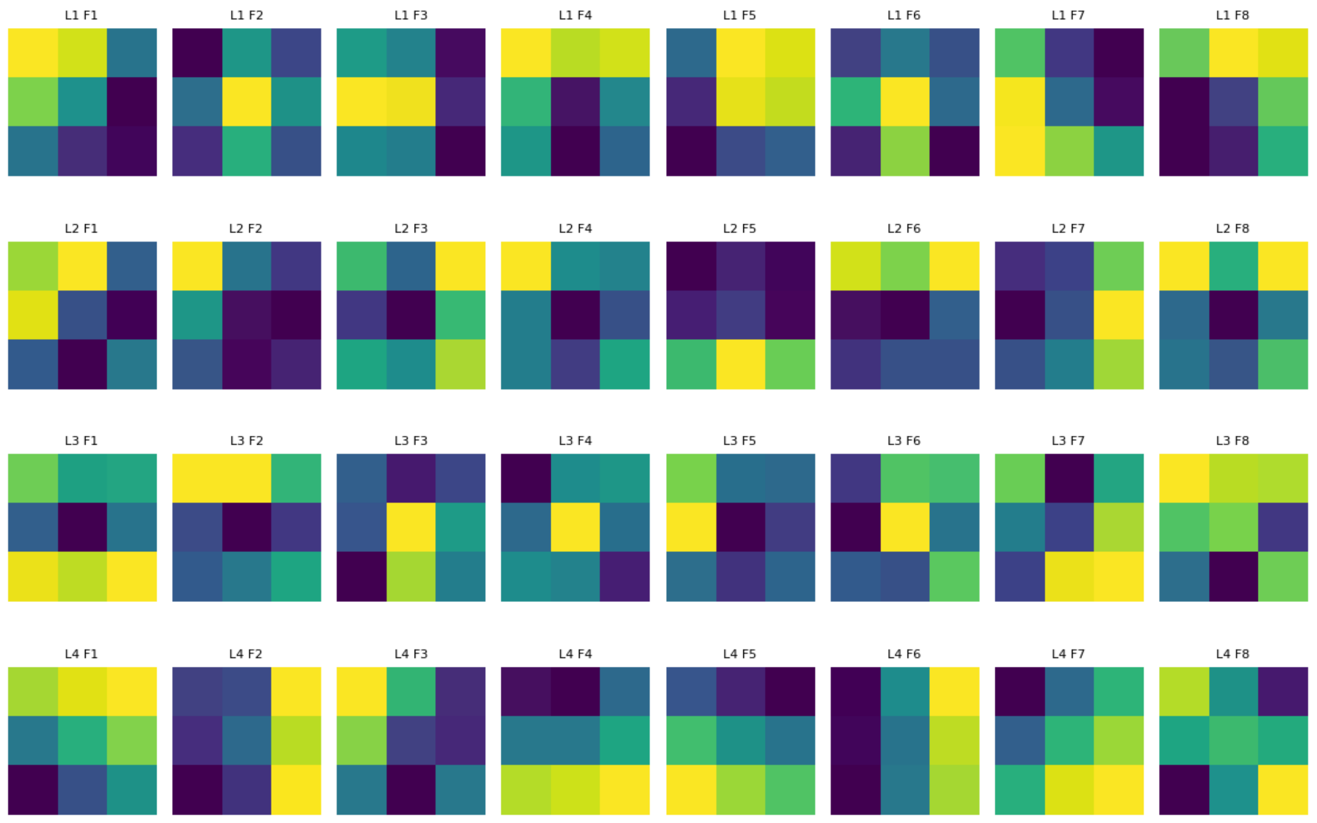


Look through the other weight tensors in the network and note any patterns that can be observed. Plot some examples in a subplot grid (include at least 4 plots). You can also overplot on the same subplot if you find that helpful for visualization.

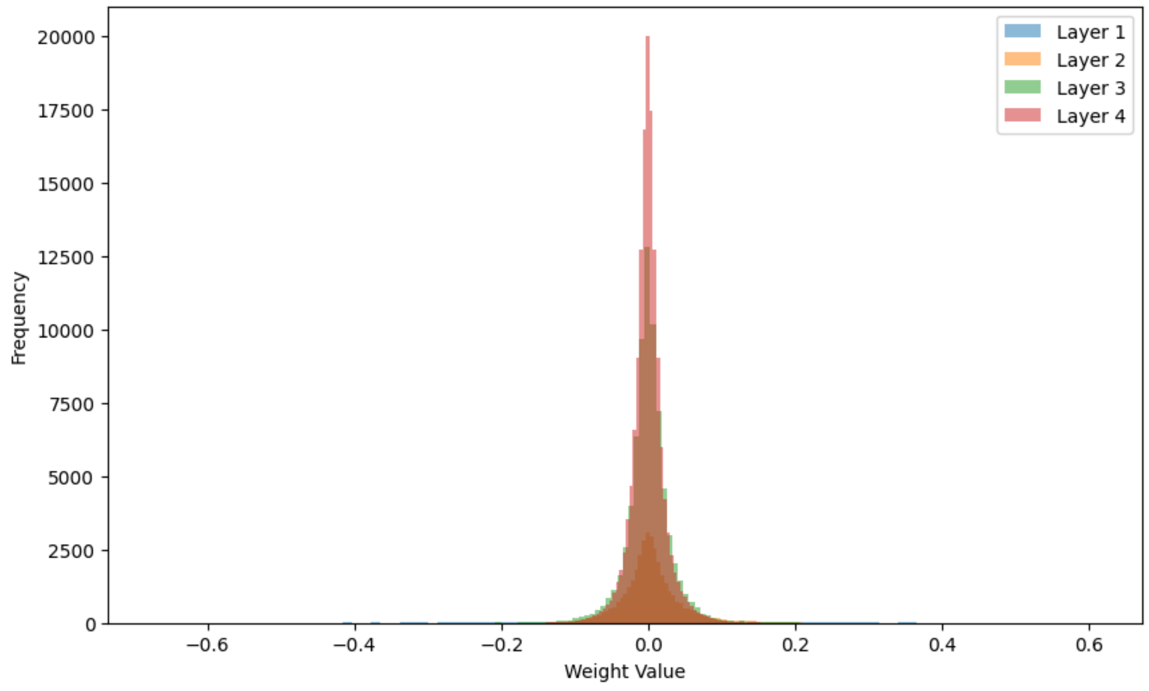
Question 4

```
import matplotlib.pyplot as plt
import tensorflow as tf
import numpy as np

# Load the VGG16 model
model = tf.keras.applications.VGG16(weights='imagenet')

# Extract Conv2D layers' weights
conv_layers = [layer for layer in model.layers if isinstance(layer, tf.keras.layers.Conv2D)]
weights_list = [layer.get_weights()[0] for layer in conv_layers]

# Function to visualize filters and their distributions
def visualize_weights(weights_list, layer_indices):
    plt.figure(figsize=(16, 12))

    for idx, layer_idx in enumerate(layer_indices):
        weights = weights_list[layer_idx]
        n_filters = weights.shape[-1]

        # Visualize the first filter of the layer
        plt.subplot(len(layer_indices), 2, 2 * idx + 1)
        plt.imshow(weights[:, :, 0, 0], cmap="viridis")
        plt.axis('off')
        plt.title(f"Layer {layer_idx+1} - Filter 1", fontsize=12)
        # Plot weight distribution
        plt.subplot(len(layer_indices), 2, 2 * idx + 2)
        plt.hist(weights.flatten(), bins=100, alpha=0.7, color='blue')
        plt.xlabel("Weight Value")
        plt.ylabel("Frequency")
        plt.title(f"Layer {layer_idx+1} - Weight Distribution", fontsize=12)

    plt.tight_layout()
    plt.show()

# Visualize selected layers
visualize_weights(weights_list, [0, 3, 6, 10])  # Adjust layer indices as needed
import matplotlib.pyplot as plt
import tensorflow as tf

# Load the VGG16 model
model = tf.keras.applications.VGG16(weights='imagenet')

# Get weights of specific layers (e.g., Conv2D layers)
conv_layers = [layer for layer in model.layers if isinstance(layer, tf.keras.layers.Conv2D)]
weights_list = [layer.get_weights()[0] for layer in conv_layers]

# Visualize the weights of the first four Conv2D layers
plt.figure(figsize=(12, 8))
for i in range(4):
    weights = weights_list[i]
    n_filters = weights.shape[-1]

    # Visualize the first 8 filters of the layer
    for j in range(8):
        plt.subplot(4, 8, i * 8 + j + 1)
        plt.imshow(weights[:, :, 0, j], cmap="viridis")
        plt.axis('off')
        plt.title(f"L{i+1} F{j+1}", fontsize=8)

# Adjust layout and display
plt.tight_layout()
plt.show()

# Analyze weight distributions
plt.figure(figsize=(10, 6))
for i in range(4):
    weights = weights_list[i]
    plt.hist(weights.flatten(), bins=100, alpha=0.5, label=f"Layer {i+1}")

plt.xlabel("Weight Value")
plt.ylabel("Frequency")
plt.title("Weight Distributions of the First 4 Conv2D Layers")
plt.legend()
plt.show()
```





Weight Distributions of the First 4 Conv2D Layers


Layer 1
Layer 2
Layer 3
Layer 4
Frequency
Weight Value
20000
17500
15000
12500
10000
7500
5000
2500
0
−0.6
−0.4
−0.2
0.0
0.2
0.4
0.6

We can also visualize the activations within the network, this is done by applying a forward pass with a data input, and extracting the intermediate result. Below is an example output from the first convolution layer.

```
import tensorflow as tf
import matplotlib.pyplot as plt
from tensorflow.keras.applications.vgg16 import VGG16
from tensorflow.keras.datasets import mnist

# Step 1: Load MNIST dataset
(train_images, train_labels), (test_images, test_labels) = mnist.load_data()

# Step 2: Select one image (e.g., the 5th image, index 4)
image = train_images[4]

# Step 3: Ensure the image has a channel dimension (i.e., grayscale to RGB)
image_expanded = tf.expand_dims(image, axis=-1)  # (28, 28) -> (28, 28, 1)

# Step 4: Resize image to 224x224 (VGG16 input size)
image_resized = tf.image.resize(image_expanded, [224, 224])

# Step 5: Convert the grayscale image to 3 channels by repeating the single channel
image_resized_rgb = tf.repeat(image_resized, 3, axis=-1)  # Now shape is (224, 224, 3)

# Step 6: Normalize the image (VGG16 preprocessing expects values between -1 and 1)
image_resized_rgb = image_resized_rgb / 255.0  # Normalize to [0, 1]
image_resized_rgb = image_resized_rgb - 0.5  # Normalize to [-0.5, 0.5]

# Step 7: Add batch dimension (VGG16 expects a batch of images)
image_resized_rgb = tf.expand_dims(image_resized_rgb, axis=0)  # Shape is now (1, 224, 224, 3)

# Step 8: Load the VGG16 model with ImageNet weights
model = VGG16(weights='imagenet')

# Step 9: Create an intermediate model to extract activations from the first convolutional layer
first_conv_layer = model.layers[2]  # The first Conv2D layer is at index 2
activation_model = tf.keras.models.Model(inputs=model.input, outputs=first_conv_layer.output)

# Step 10: Get the activations from the first convolutional layer
activations = activation_model.predict(image_resized_rgb)

# Step 11: Get the number of filters in the first convolutional layer
num_filters = activations.shape[-1]

# Step 12: Plot the feature maps (activations) of the first convolutional layer
plt.figure(figsize=(12, 12))

for i in range(num_filters):
    plt.subplot(8, 8, i + 1)
    plt.imshow(activations[0, :, :, i], cmap="viridis")
    plt.axis('off')
    plt.title(f"Filter {i+1}", fontsize=8)

plt.tight_layout()
plt.show()
```