

# *A Performance Improvement Approach for Second-Order Optimization in Large Mini-batch Training*

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## Our Work Position

- *Data Parallel Distributed Deep Learning*
- *Second-Order Optimization*
- *Improve Generarization*

## Key Takeaways

- *Second-order optimization can converge faster than first-order optimization with low generarization performance*
- *Smoothing loss function can improve second-order optimization performance*

## Introduction / Motivation

- Accuracy  $\nearrow$  Model Size and Data Size  $\nearrow$
- Needs to Accelerate

## Second Order Optimization Approach

- Natural Gradient Descent
- K-FAC (Approximate Method)
- Experimental Methodology and Result

## Background / Problem

- Three Parallelism of Distributed Deep Learning
- Large Mini-Batch Training Problem
- Two Strategies

## Proposal to improve generalization

- Sharp Minima and Flat Minima
- Mixup Data Augmentation
- Smoothing Loss Function
- Experimental Methodology and Result

## Conclusion

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# 1. *Introduction / Motivation*

# *Improvement of recognition accuracy and increase of training time with increasing number of parameters of convolutional neural network (CNN)*

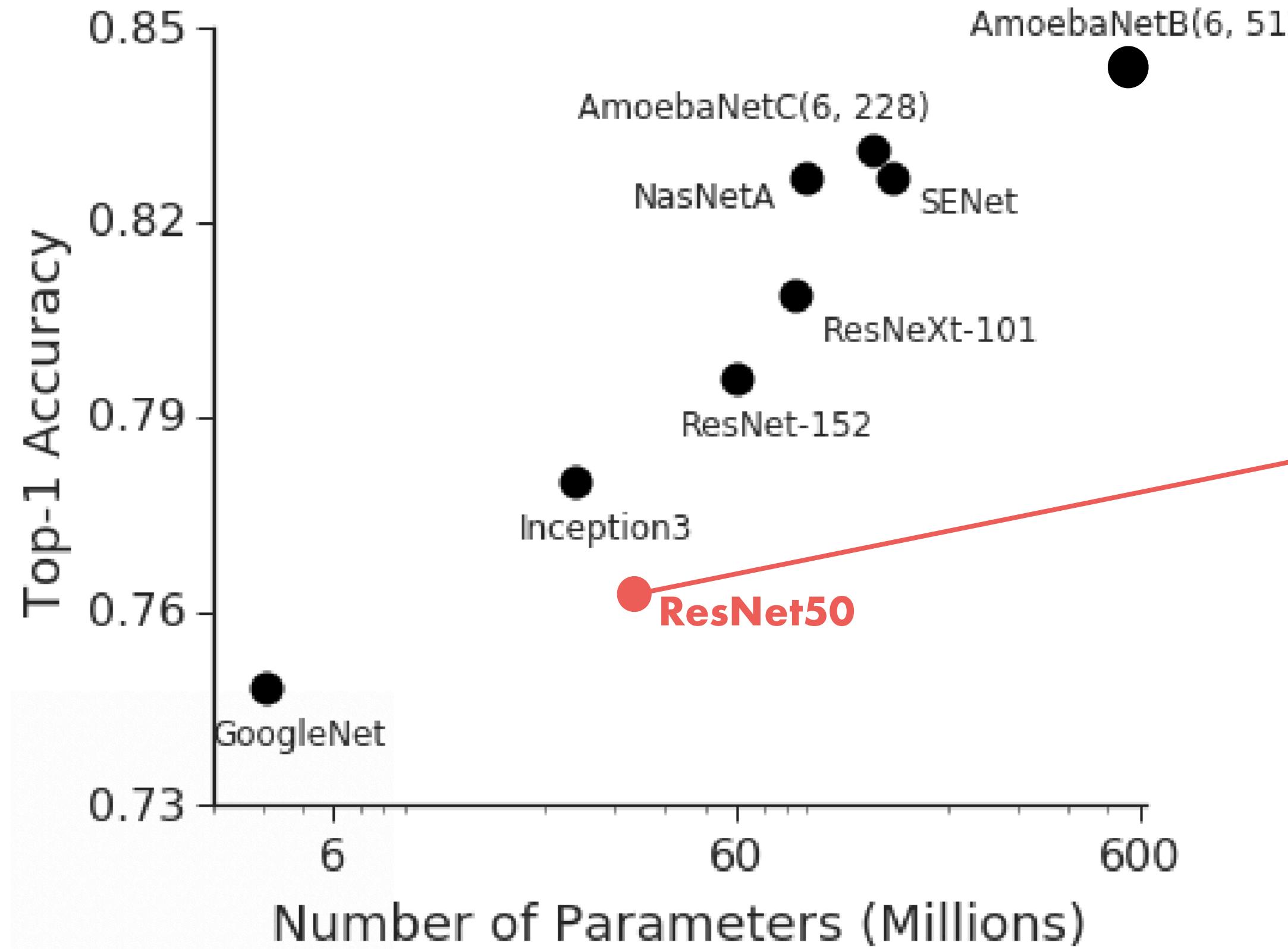
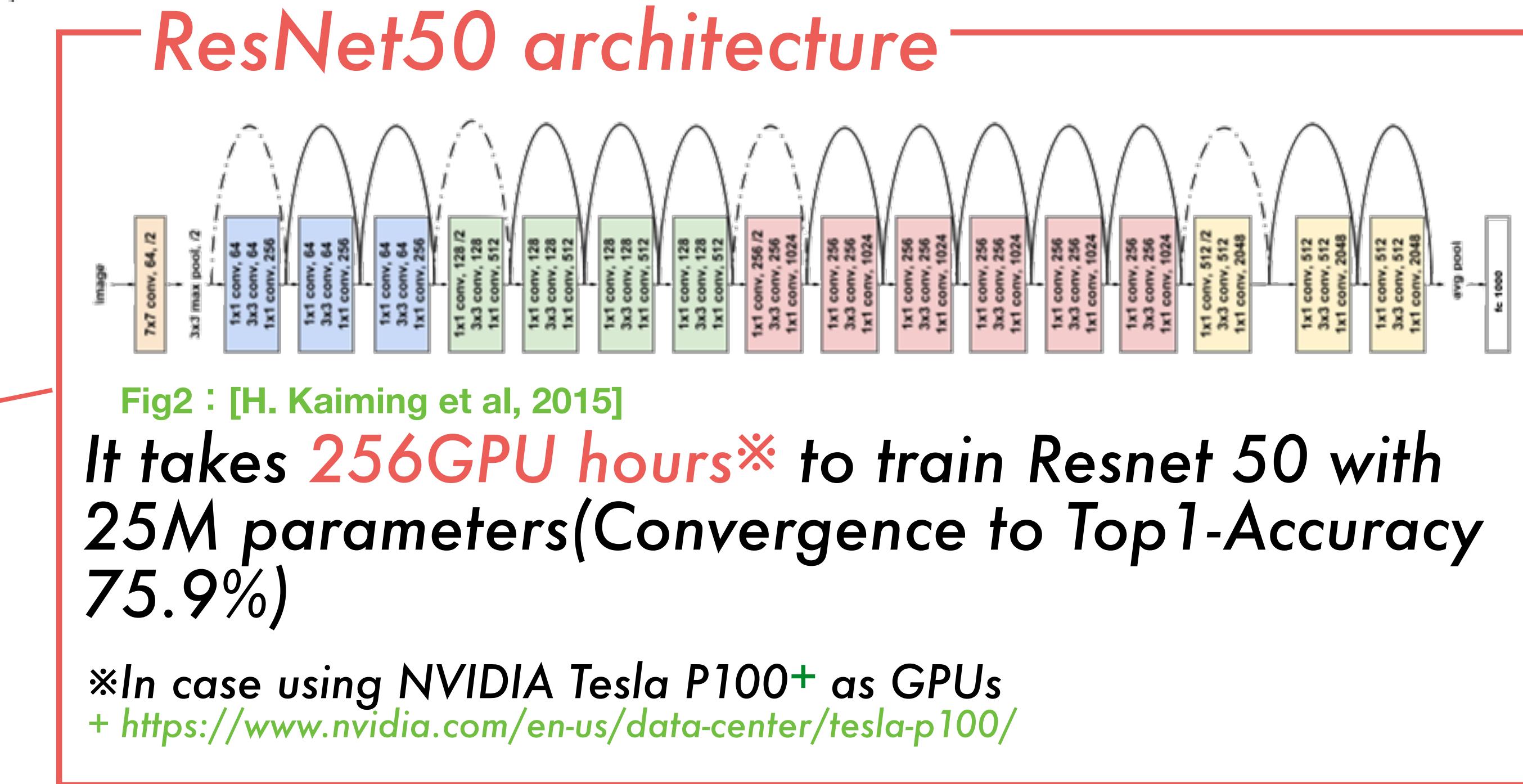


Fig1 : [Y. Huang et al, 2018]



*The figure shows the relationship between the recognition accuracy of ImageNet-1K 1000 class classification and the number of parameters of DNN model.*

# DNNs with a lot of parameters tend to show high recognition accuracy

# 1. Introduction / Motivation

Importance and time required of hyperparameter tuning in deep learning

**In deep learning, tuning of hyper-parameters is essential**

**Hyperparameters:**

- Learning rate
- Batch size
- Number of training iterations
- Number of layers of neural network
- Number of channels

**Even with the strategy of pruning, many trials with training to the end is necessary** [J. Bergstra et al. 2011]

It takes **256GPU hours**※ to train Resnet 50 with 25M parameters(Convergence to Top1-Accuracy 75.9%)

※In case using NVIDIA Tesla P100+ as GPUs  
+ <https://www.nvidia.com/en-us/data-center/tesla-p100/>

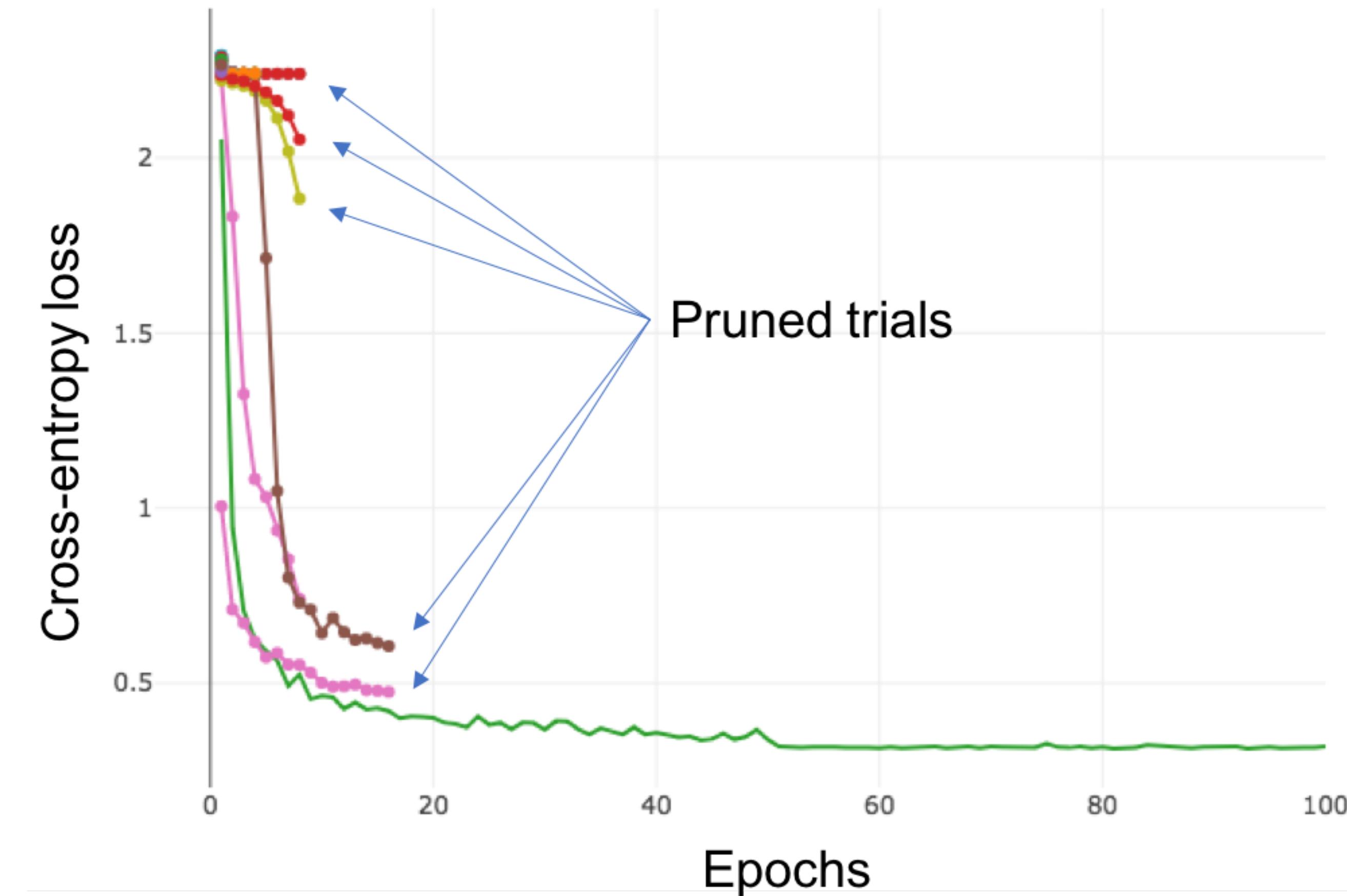


Fig3 : Pruning method in parameter tuning ref (<https://optuna.org>)

※ **Multiple Evaluations**

Time taken for hyper-parameter tuning

# 1. Introduction / Motivation

Necessity of distributed deep learning

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**It takes 256GPU hours\* to train Resnet 50 with 25M parameters (Convergence to Top1-Accuracy 75.9%)**

\*In case using NVIDIA Tesla P100+ as GPUs  
+ <https://www.nvidia.com/en-us/data-center/tesla-p100/>

**\* Multiple Evaluations**

**Time taken for hyper-parameter tuning**

**Hyper-parameter tuning is necessary, which requires a lot of time to obtain DNN with high recognition accuracy**

*Speeding up with 1 GPU is important, but there is a limit to speeding up*



**Needs to speed up by distributed deep learning**



**In large mini-batch training for accelerating, the recognition accuracy finally obtained is degraded**

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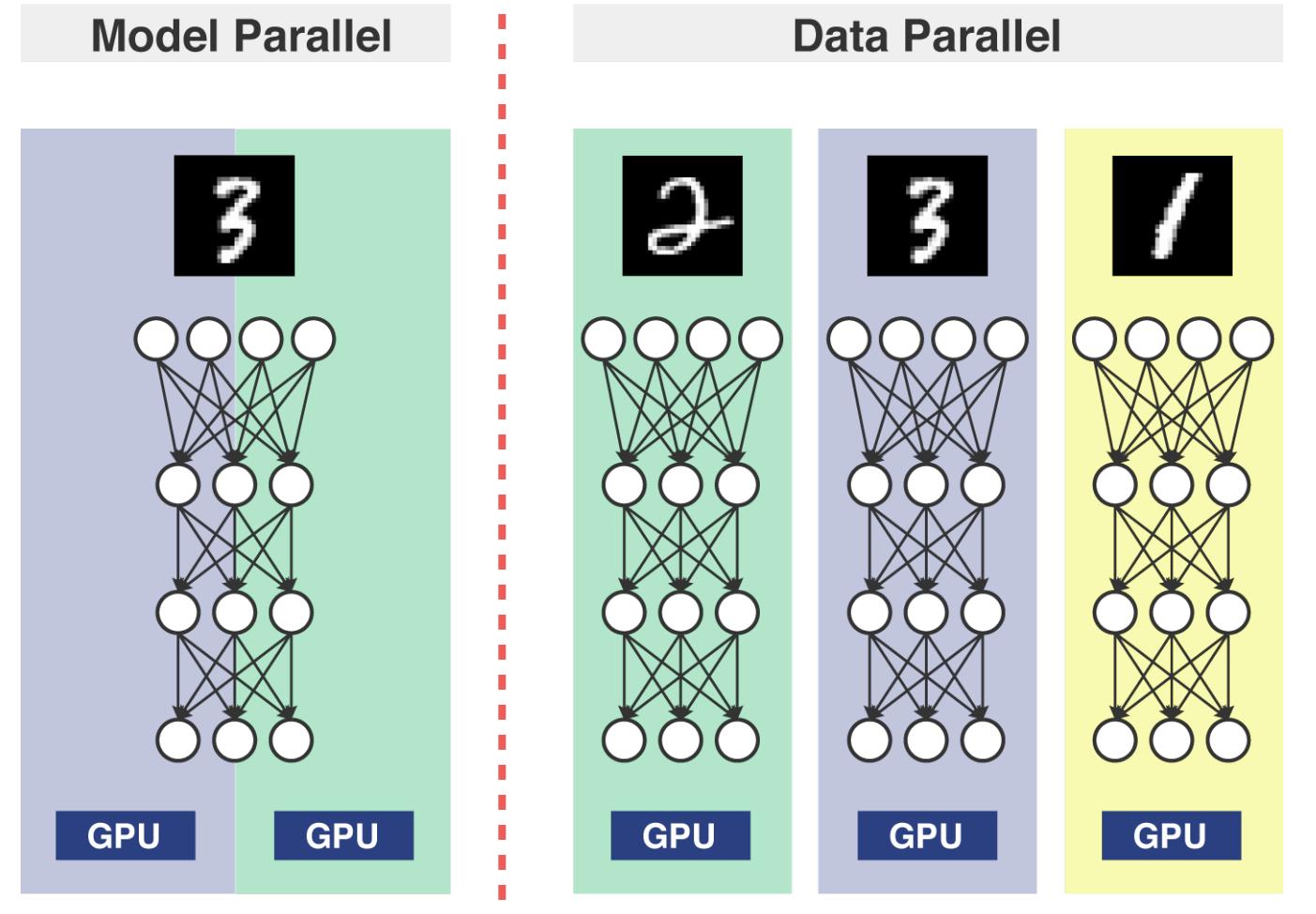
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# 2. Background / Problem

## Three Parallelism of Distributed Deep Learning

### A. Model Parallel/Data Parallel B. Parameter Server/Collective communication



### C. Sync/Async

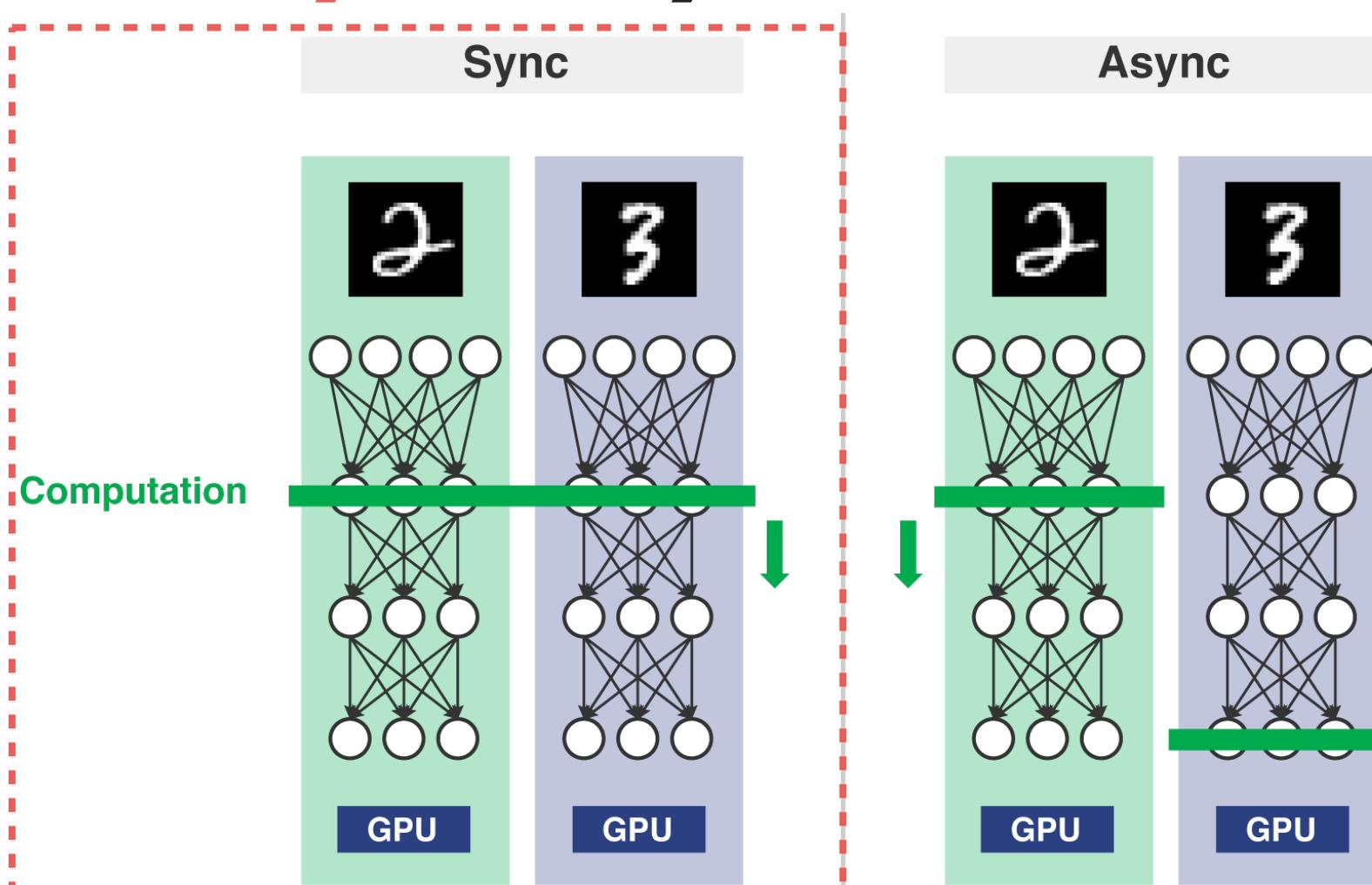


Fig4: Model/Data Parallel

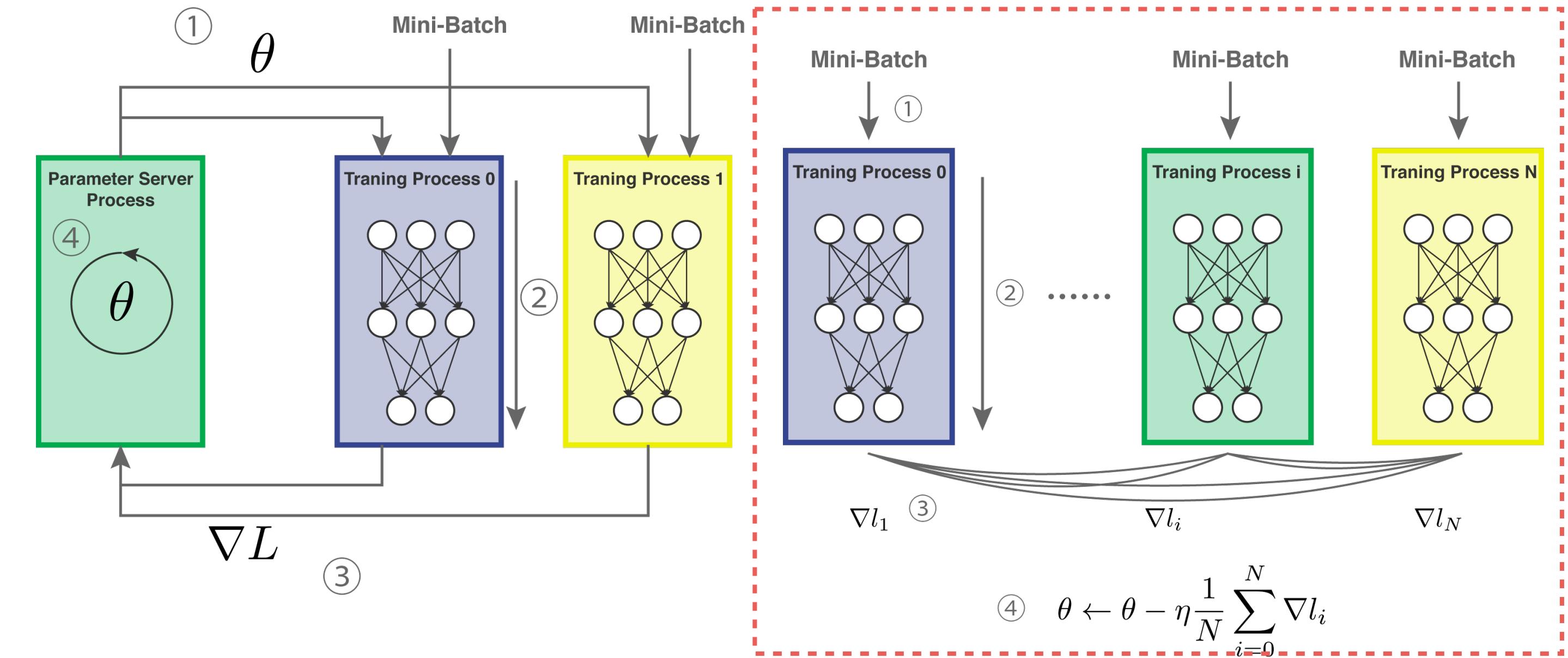


Fig5: How to communicate

- The parallelism of distributed deep learning is mainly the following three 「A. What」 「B. How」 「C. When」
- 「A. What」 Data parallel is essential for speeding up
- 「B. How」 Adapt collective communication method for speeding up
- 「C. When」 There are pros and cons, and it is an unsolved problem that it is better to adopt which. In this research, we deal with synchronous type as in the previous research [J. Chen et al, 2018]

Fig6: When does parameter update

## 2. Background / Problem

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Three Parallelism of Distributed Deep Learning

### Synchronous Data Parallel Distributed Deep Learning

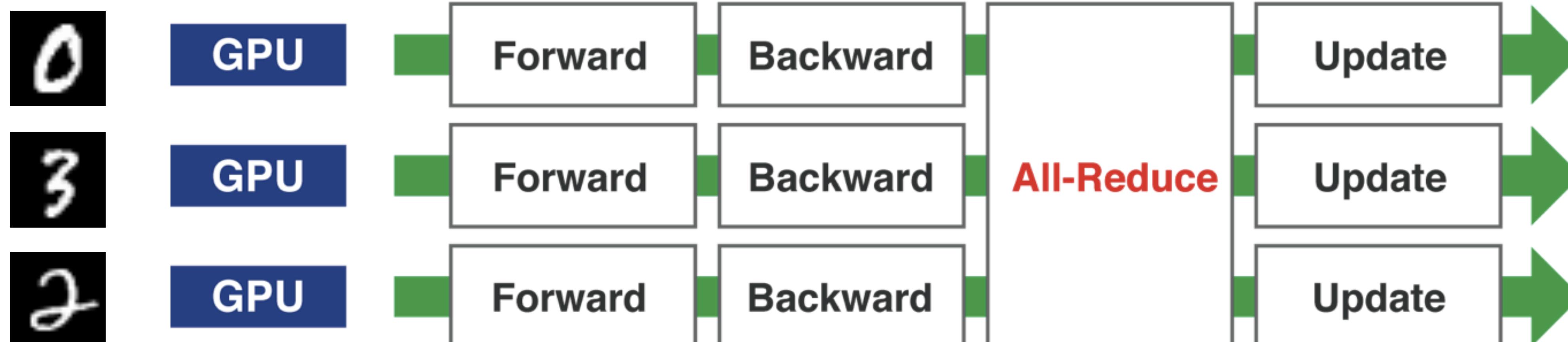
Expect speedup by increasing the batch size  
=> Large Mini-Batch Training

Single GPU Training / Small Batch Training



e.g. **batch size = 1**

Multi GPUs Training / Large Batch Training



e.g. **batch size = 3**

Fig7: Difference Between Distributed Deep Learning and Deep Learning

## 2. Background / Problem

### Three Parallelism of Distributed Deep Learning

Increasing Mini-Batch Size  
= |Input data used for one update|

Synchronous Data Parallel  
Distributed Deep Learning  
= Large Mini-Batch Training

Training with large mini-batch (LB) in SGD is generally faster in training time than with small mini-batch (SB), but that the achievable recognition accuracy is degraded [Y. Yang et al. 2017]

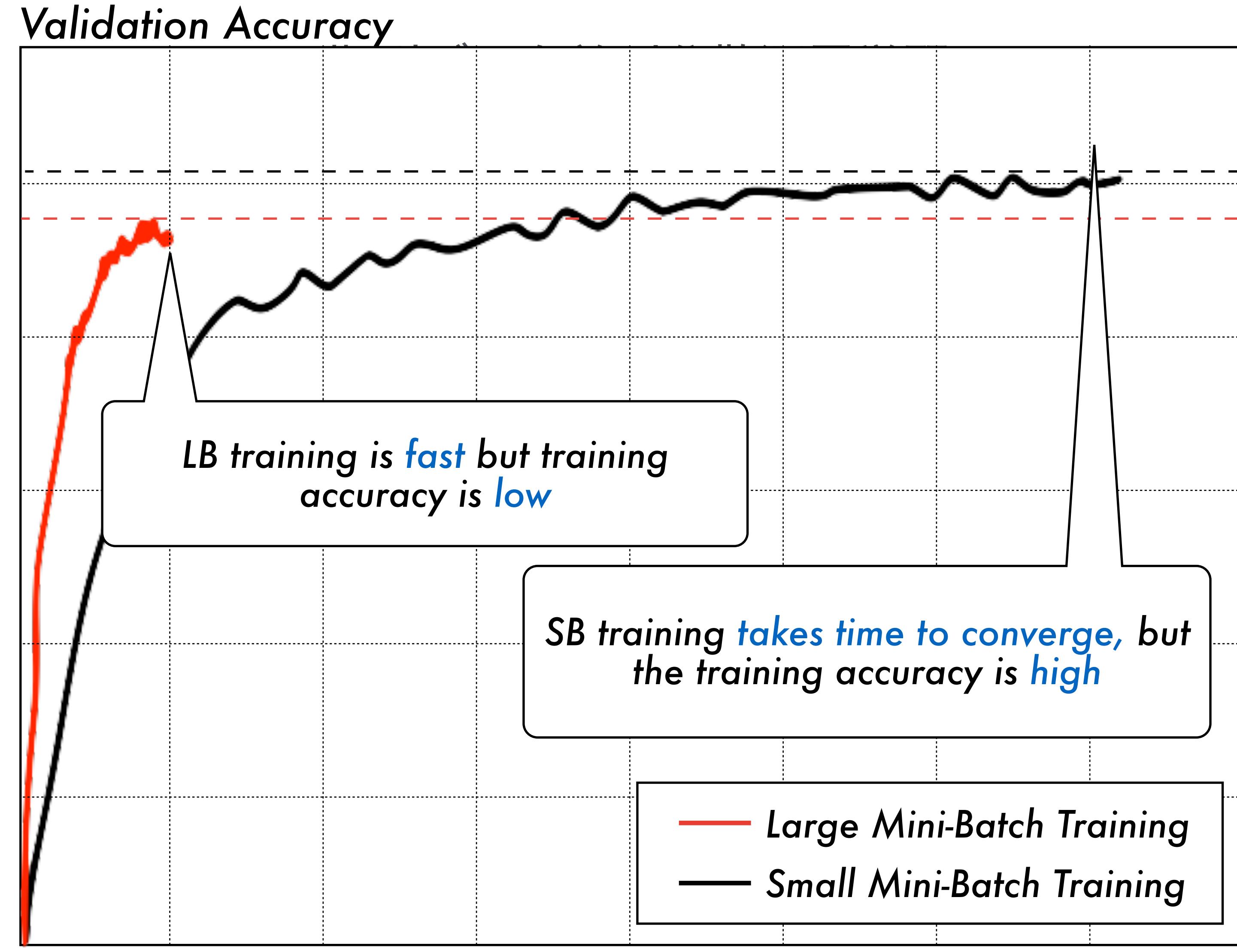


Fig8 : Convergence accuracy and training time at SB/LB using SGD Training Time

## 2. Background / Problem

### Difference between Large Mini-Batch Training and Small Mini-batch Training

**Large Mini-batch Training is not the same optimization as Small Mini-Batch Training**  
 There is a problem due to **two differences**

Supervised Learning (Optimization Problem)

$$\theta^* = \arg \min_{\theta} \frac{1}{|S|} \sum_{(\mathbf{x}, \mathbf{y}) \in S} L(\mathbf{y}, f(\mathbf{x}; \theta))$$

Loss Function      Objective Function

$$= \arg \min_{\theta} E(\theta)$$

$S$  : Train Data

By Increasing the Batch-Size  $|S|$ ,  
**It is expected to converge in more accurate directions with less iterations**

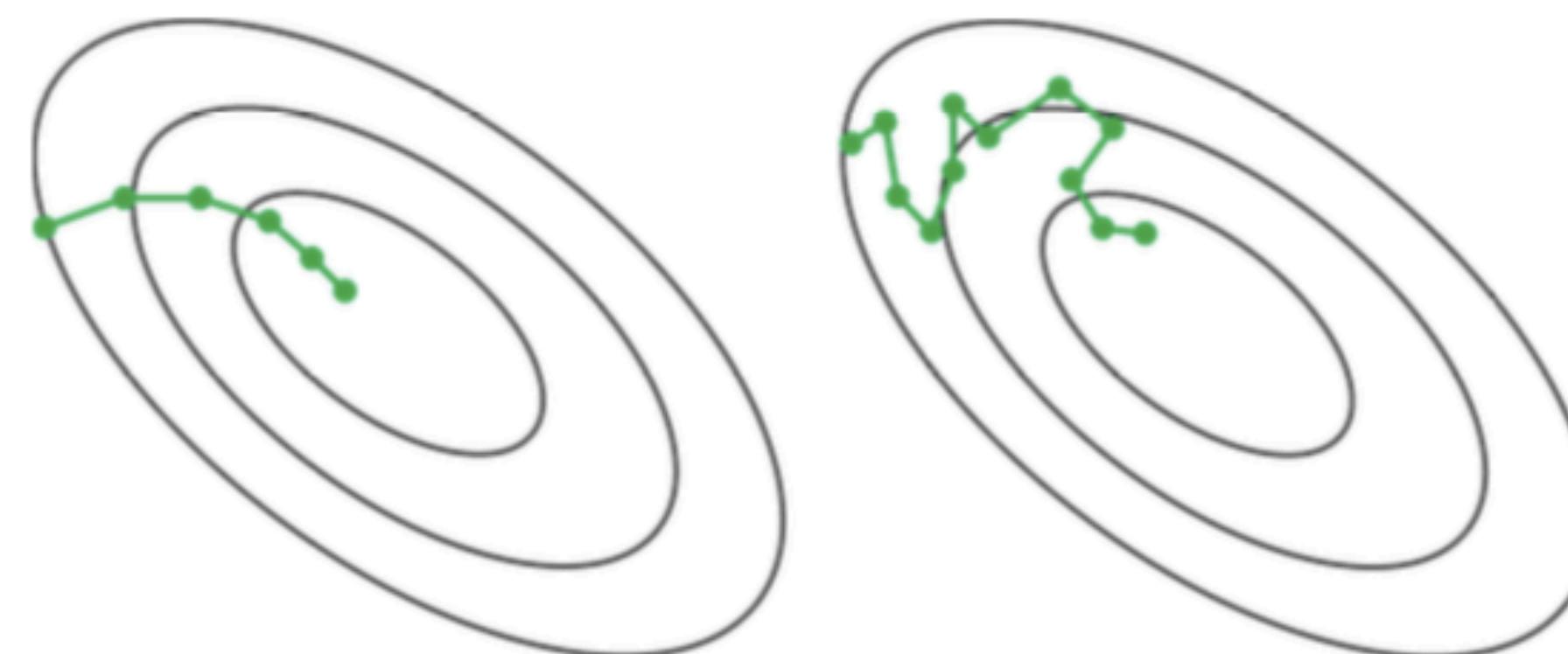


Fig9 : Left figure (LB training update appearance), Right figure (SB training update appearance)

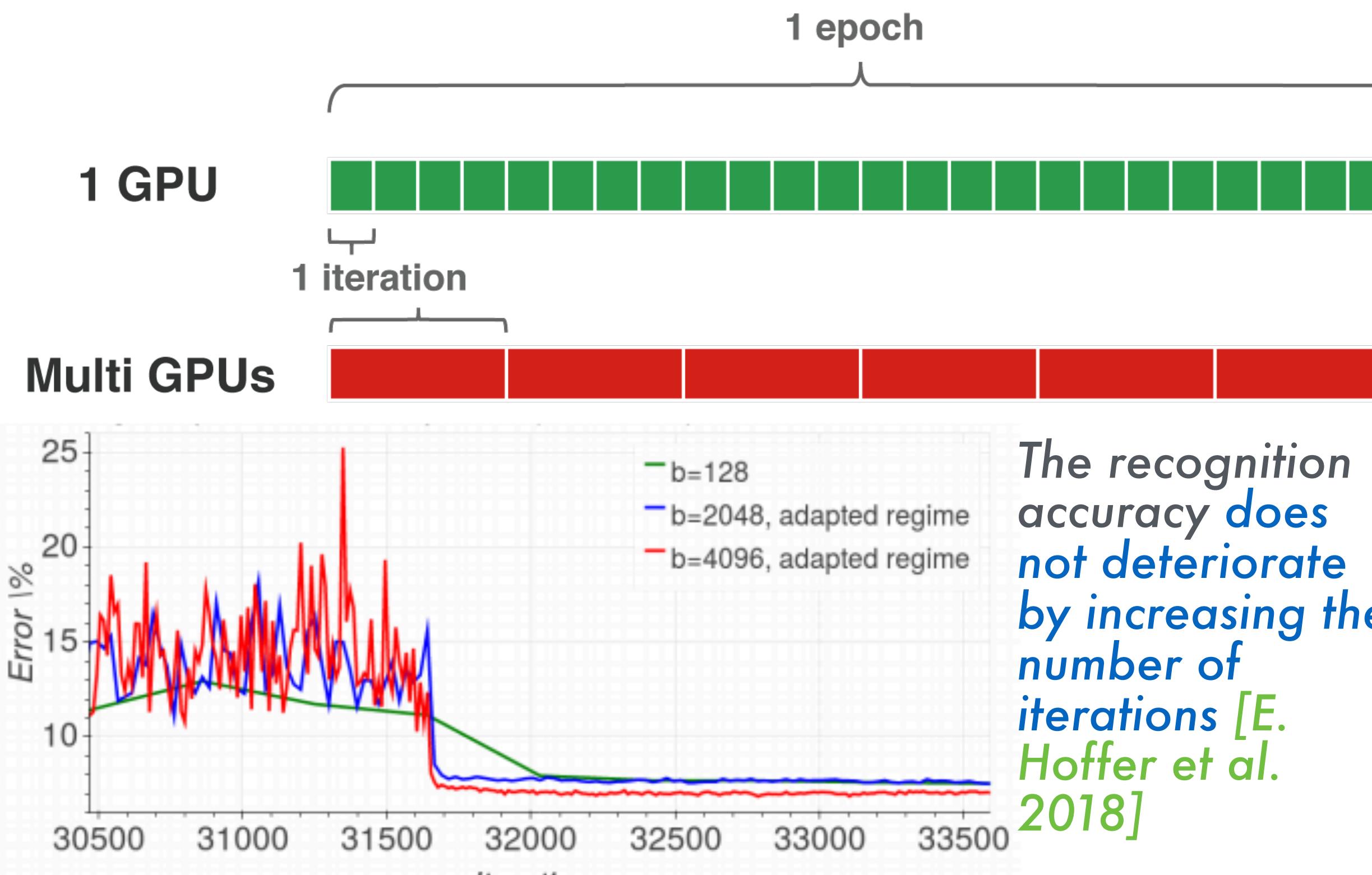
## 2. Background / Problem

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### Difference between Large Mini-Batch Training and Small Mini-batch Training and Problems

#### Problem 1.

#### Decreased number of iterations (number of updates)



(b) Validation error - zoomed

Fig10 : [E. Hoffer et al. 2018]

=> But that doesn't allow for speeding up by distributed deep learning

#### Problem 2 .

#### The gradient of the objective function is more accurate and the variance is reduced

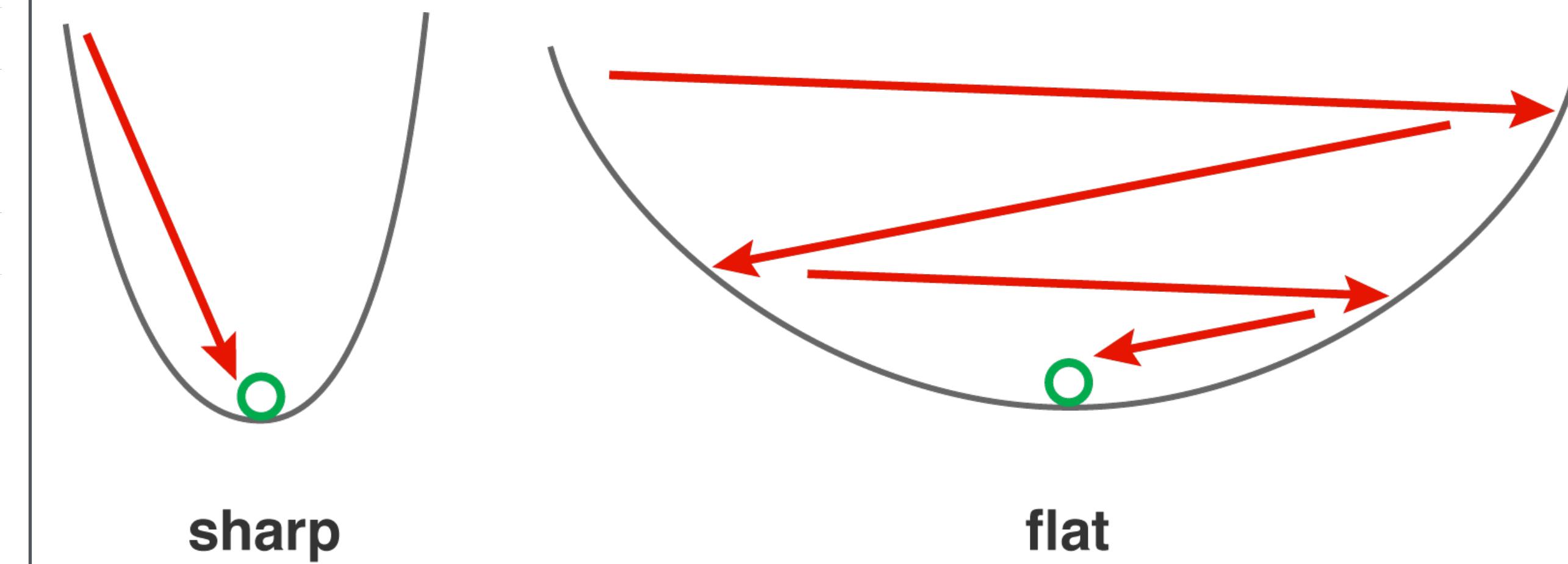


Fig11: Concept Sketch of Sharp Minimum and Flat Minimum

Good generalization is expected because it is possible to adjust noise in SB training [S. Mandt et al 2017]

In LB training, the noise is not appropriate and generalization performance is degraded [S. Smith et al. 2018]

=> It is necessary to prevent the accuracy degradation that is a side effect of speeding up

## 2. Background / Problem

Two Strategy to deal with Problems

### Problem 1.

**Decreased number of iterations  
(number of updates)**

=> Have to converge with few iteration

### Strategy 1.

**Use of natural gradient method (NGD)**

$$\theta^* = \arg \min_{\theta} \frac{1}{|S|} \sum_{(\mathbf{x}, \mathbf{y}) \in S} L(\mathbf{y}, f(\mathbf{x}; \theta))$$

In large mini-batch training, the data for each batch is statistically stable, and using NGD has a large effect of considering the curvature of the parameter space, and the direction of one update vector can be calculated more correctly [S. Amari 1998]. Convergence with fewer iterations can be expected

### Problem 2.

**The gradient of the objective function is more accurate and the variance is reduced**

=> Have to avoid SharpMinima

### Strategy 2.

**Smoothing the objective function**

$$\theta^* = \arg \min_{\theta} \frac{1}{|S|} \sum_{(\mathbf{x}, \mathbf{y}) \in S} L(\mathbf{y}, f(\tilde{\mathbf{x}}; \theta))$$

By linear interpolation of the input data in large mini-batch training, the convergence to Flat Minimum is promoted in optimization of the loss function, and generalization performance is aimed to be improved.

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- *K-FAC (Approximate Method)*
- *Experimantal Methodology and Result*

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# 3. Second Order Optimization Approach

## Mini-Batch Training

- **Gradient Descent**

DNN has a large number of parameters

-> **Gradient method using loss function gradient that is easy to calculate is mainstream**

- **SGD; Stochastic Gradient Descent**

Large-scale Training data

-> Randomly extract a small number of training cases (on-line stochastic optimization)

-> **Process multiple training data in parallel(mini-batch)**

### Stochastic Gradient Descent Method using Mini-Batch

$$\boldsymbol{\theta}^{(t+1)} = \boldsymbol{\theta}^{(t)} - \epsilon \frac{1}{|B|} \sum_{(\mathbf{x}, \mathbf{y}) \in B} \nabla L(\mathbf{y}, f(\mathbf{x}; \boldsymbol{\theta}))$$

*Gradient of loss function*

$\boldsymbol{\theta}^{(t)}$  : Parameter after  $t$  times update

$$\nabla L = \frac{\partial L}{\partial \boldsymbol{\theta}}$$

$\epsilon > 0$  : Learning Rate

$S \supset B$  : mini-batch (randomly extract)

## 2. Background / Problem

Two Strategy to deal with Problems

**Problem 1.**  
**Decreased number of iterations**  
**(number of updates)**  
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By linear interpolation of the input data in large mini-batch training, the convergence to Flat Minimum is promoted in optimization of the loss function, and generalization performance is aimed to be improved.

# 3. Second Order Optimization Approach

## Gradient Descent and Natural Gradient Method

### Supervised Learning (Optimization Problem)

$$\theta^* = \arg \min_{\theta} \frac{1}{|S|} \sum_{(\mathbf{x}, \mathbf{y}) \in S} L(\mathbf{y}, f(\mathbf{x}; \theta)) = \arg \min_{\theta} E(\theta)$$

*S : Train Data*

## Stochastic Gradient Descent

- It is difficult to get out of local solutions and plateaus
- When the learning rate is increased, the values vibrate and diverge at the saddle point

### Stochastic Gradient Descent (SGD)

$$\theta^{(t+1)} = \theta^{(t)} - \epsilon \nabla E(\theta^{(t)})$$

*Gradient of Loss Function*

## Natural Gradient Descent

- An optimization method proposed by [S. Amari 1998] based on information geometry
- Use Fisher information matrix as Riemann metric (= curvature matrix)
- Set the update direction well and expect faster convergence

### Natural Gradient Descent (NGD)

$$\theta^{(t+1)} = \theta^{(t)} - \epsilon F_{\theta^{(t)}}^{-1} \nabla E(\theta^{(t)})$$

*Gradient of Loss Function*

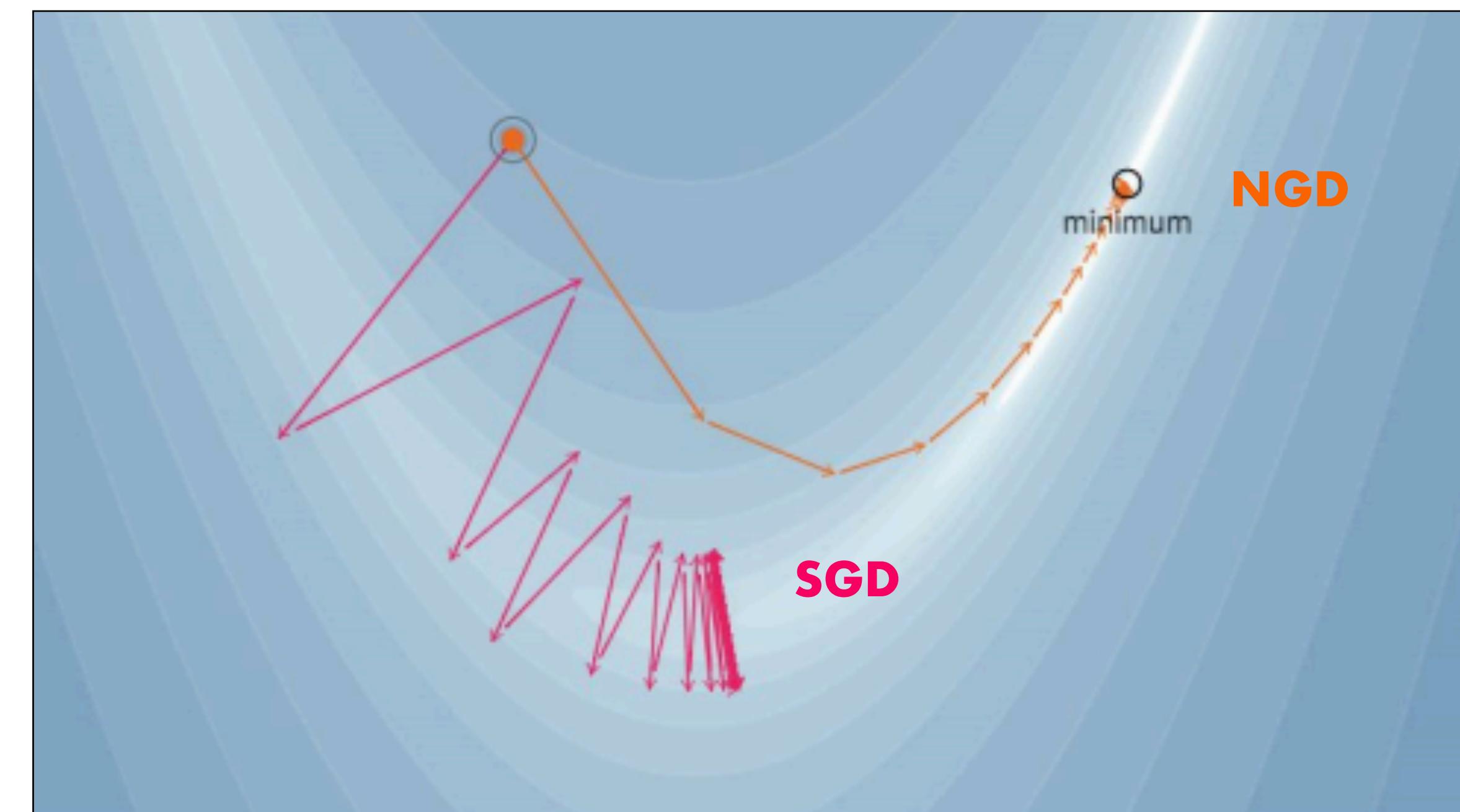
*F<sub>θ<sup>(t)</sup></sub>: Fisher Information Matrix*

# 3. Second Order Optimization Approach

## Natural Gradient Method Pros and Cons in deep learning

### Pros

- It is expected to converge with a smaller number of iterations compared to (an improved method of) SGD
- It is expected that model parameters can be updated in the correct direction using the gradient curvature of the statistically stable loss function when the batch size is large



### Cons

- Inverse calculation of huge Fisher information matrix ( $N \times N$ ) is required for huge parameters ( $N$ )
- For example, about  $N = 3.5 \times 10^6$  (about 12 PB memory consumption) for ResNet-50

Natural Gradient Descent (NGD)

$$\theta^{(t+1)} = \theta^{(t)} - \epsilon F_{\theta^{(t)}}^{-1} \nabla E(\theta^{(t)})$$

Gradient of Loss Function  
 $F_{\theta^{(t)}}: \text{Fisher Information Matrix}$

=> **Natural Gradient Approximation Method**

# 3. Second Order Optimization Approach

Three strategies to Approximate the Natural Gradient (K-FAC)

It is **difficult to calculate** the inverse of **Fisher information matrix (FIM)** in the update equation, **considering the number of parameters of recent DNN**.

## 3 Strategies to Approximate

### ① Approximate FIM (and inverse)

N. Roux et al., 2008, D. Kingma et al., 2015,  
 R. Grosse et al., 2015, [J. Martens et al., 2015],  
 P. Luo, 2016, [R. Grosse et al., 2016],  
 A. Botev et al., 2017, [J. Ba et al., 2017]

Approximation method targeted by this work : K-FAC

### ② Bring the FIM closer to the identity matrix

K. Cho et al., 2013, G. Desjardins et al. 2015,  
 B. Neyshabur et al., 2015, T. Salimans et al., 2016

### ③ Approximate update vector

S. Krishnan et al., 2017

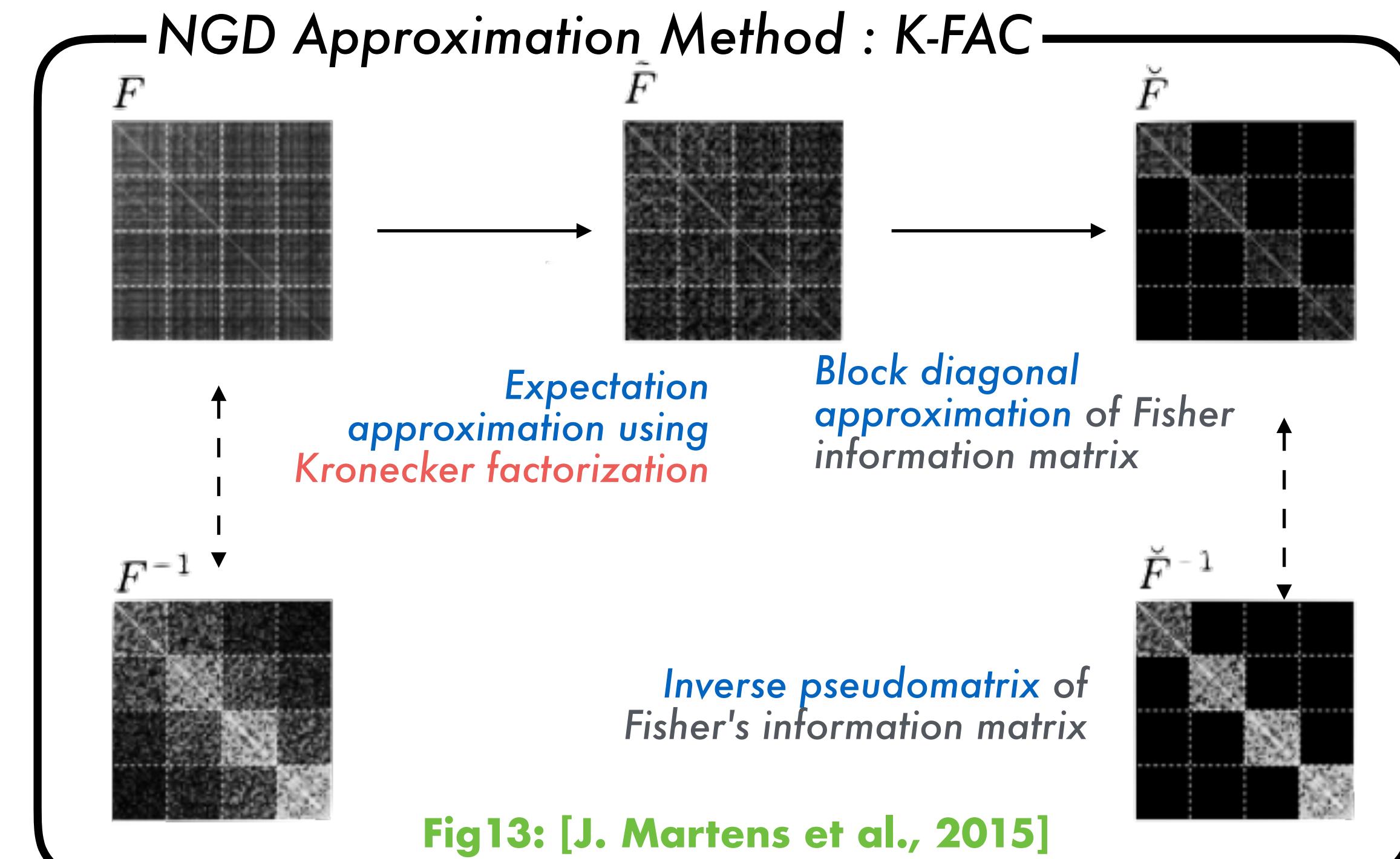
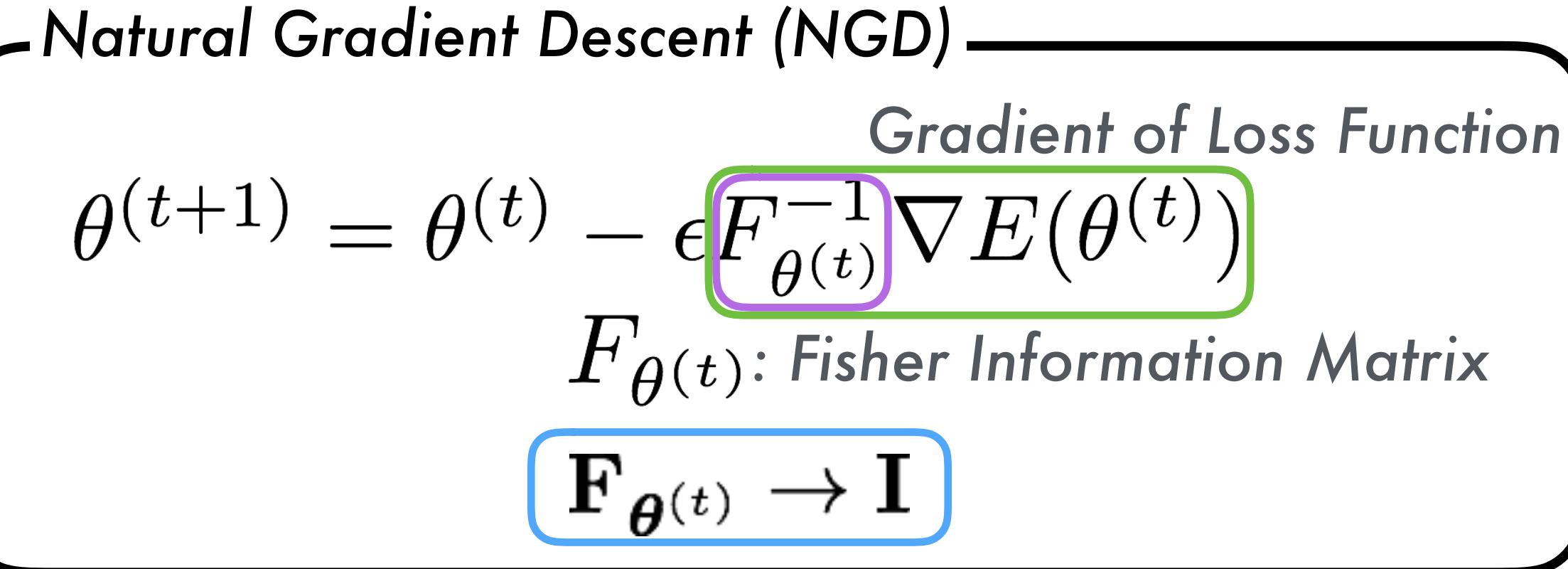


Fig13: [J. Martens et al., 2015]

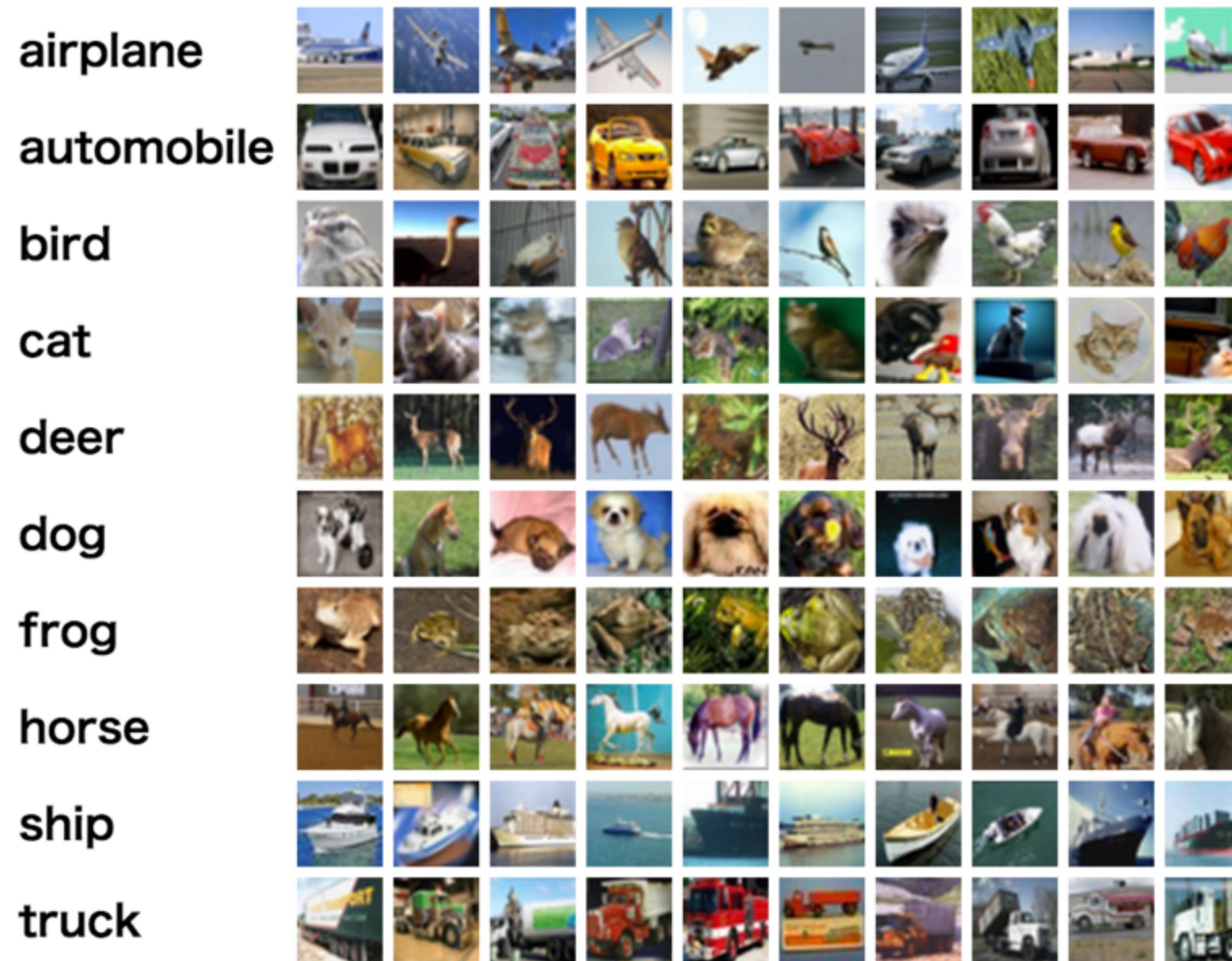
# 3. Second Order Optimization Approach

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## Experimental Methodology

### Data Set : CIFAR-10

The CIFAR-10 dataset is a data set of  $32 \times 32$  pixels (RGB) color image labeled with 10 classes of {airplane, automobile, bird, cat, deer, dog, frog, horse, ship, truck}.



### DNN Model : Lenet5

Lenet5 which is a simple multilayer neural network model by the structure proposed by LeCun et al was used as a DNN model.

Layer Type	Description
Convolution	Filter Size $5 \times 5$ , Output Channel 6
MaxPooling	Kernel Size $2 \times 2$
Convolution	Filter Size $5 \times 5$ , Output Channel 16
MaxPooling	Kernel Size $2 \times 2$
FC	Output Size 120
FC	Output Size 84
FC	Output Size 10

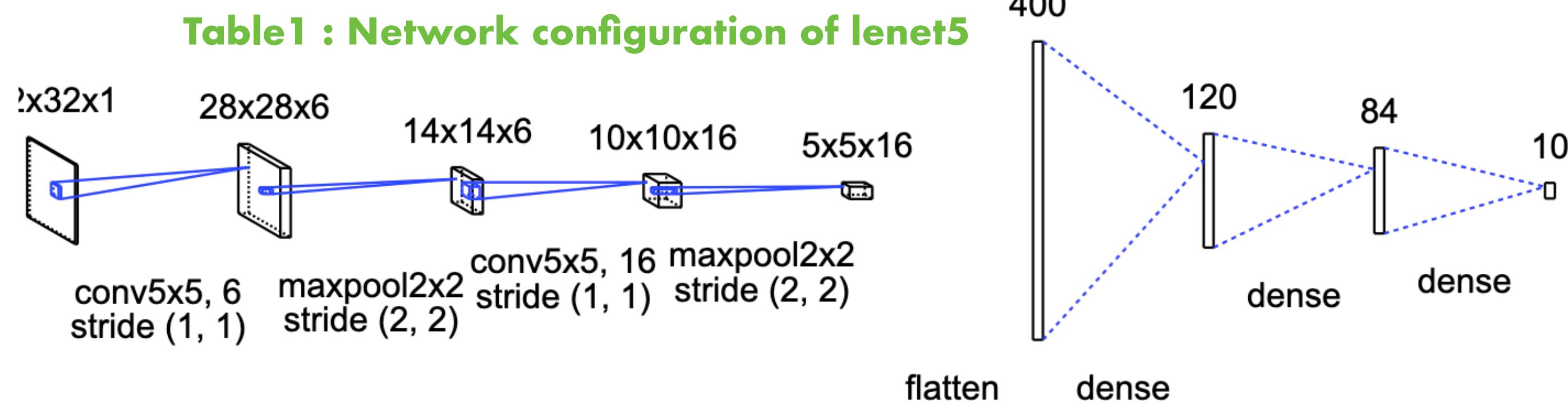


Fig14 : Category of training data set CIFAR-10 used in experiment and its sample example

Fig15 : Network configuration of lenet5

# 3. Second Order Optimization Approach

## Experimental Methodology

### Program for Training: Chainer, PyTorch

Using Chainer, which is an open source software library for machine learning, we constructed the DNN model and implemented its training with the programming language Python.

We use Chainer\_K-FAC to implement distributed deep learning using K-FAC.

For visualization of the loss function, PyTorch which is an open source software library for machine learning was used with reference to [L. Hao et al. 2018]

### Computational Environment: (ABCi; AI Bridging Cloud Infrastructure)

All experiments were performed on the ABCI(AI Bridging Cloud Infrastructure) supercomputer at AIST.

For the experiment, one computation node is used, and one node consists of NVIDIA Tesla V100 x 4GPU and Intel Xeon Gold 6148 2.4 GHz, 20 Cores x 2CPU.

CentOS 7.4, Python 3.6.5, cuDNN 7.4, CUDA 9.2 are used as the software environment. **Table2 : Hyper Parameter used in Experiment**

### Training Strategy

The model of the network is trained using mini-batch extracted randomly from the training data, and **SGD / K-FAC is used as the optimization method**. It is used that learning rate decay for stabilizing convergence, weight decay for suppressing over training of values of parameters during training and momentum for adjusting the steepest vector calculated during training. The hyperparameter used in this experiment is shown in right table.

Weight Decay	1e-4
Momentum	0.9
Learning Rate(SB SGD)	5e-3 → 2.5e-3 (71epoch)
Learning Rate(SB SGD no mixup)	1e-3 → 5e-4 (71epoch)
Learning Rate(LB SGD)	1e-2 → 5e-3 (71epoch)
Learning Rate(LB SGD no mixup)	5e-3 → 2.5e-3 (71epoch)
Learning Rate(SB K-FAC)	5e-3 → 2.5e-3 (71epoch)
Learning Rate(SB K-FAC no mixup)	2e-3 → 1e-3 (71epoch)
Learning Rate(LB K-FAC)	8e-3 → 4e-3 (71epoch)
Learning Rate(LB K-FAC no mixup)	4e-3 → 2e-3 (71epoch)
Mixup Alpha(SB K-FAC)	0.9
Mixup Alpha(LB K-FAC)	0.7
Epoch	150
Batch Size	128 or 2048

### 3. Second Order Optimization Approach

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#### Experiment Result

##### Experiment 1: Training by SGD/K-FAC method without Smoothing etc. (K-FAC Advantage)

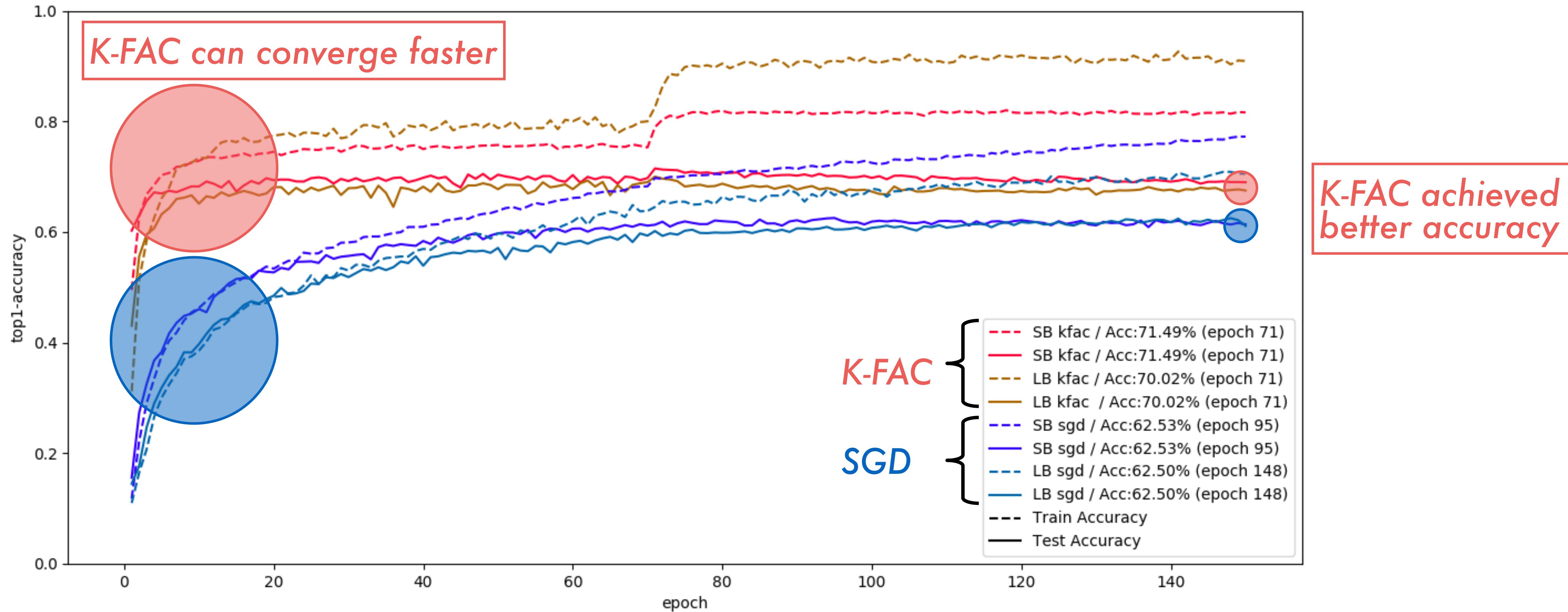


Fig16: Training of CIFAR 10 in LeNet5 using SGD/K-FAC method. SB shows batch size 128, LB shows batch size 2K.

# 3. Second Order Optimization Approach

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## Experimental Result

### Experiment1: Training by SGD/K-FAC method without Smoothing etc. (K-FAC Advantage)

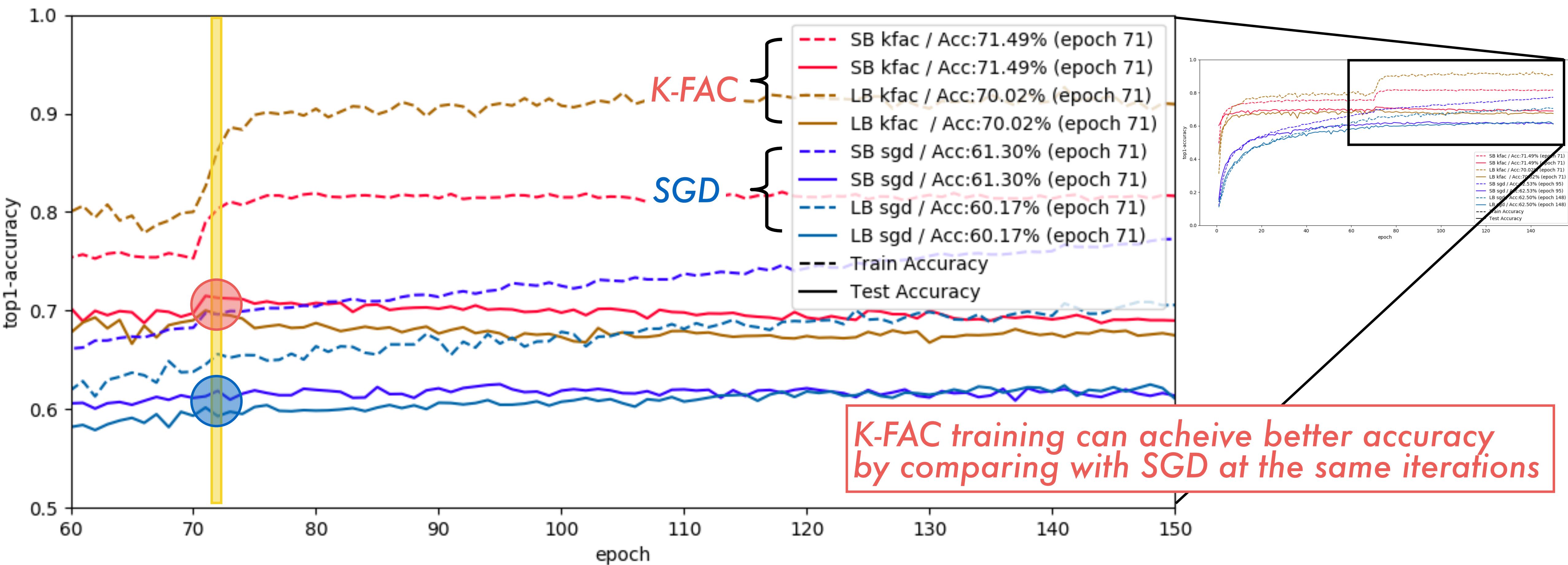


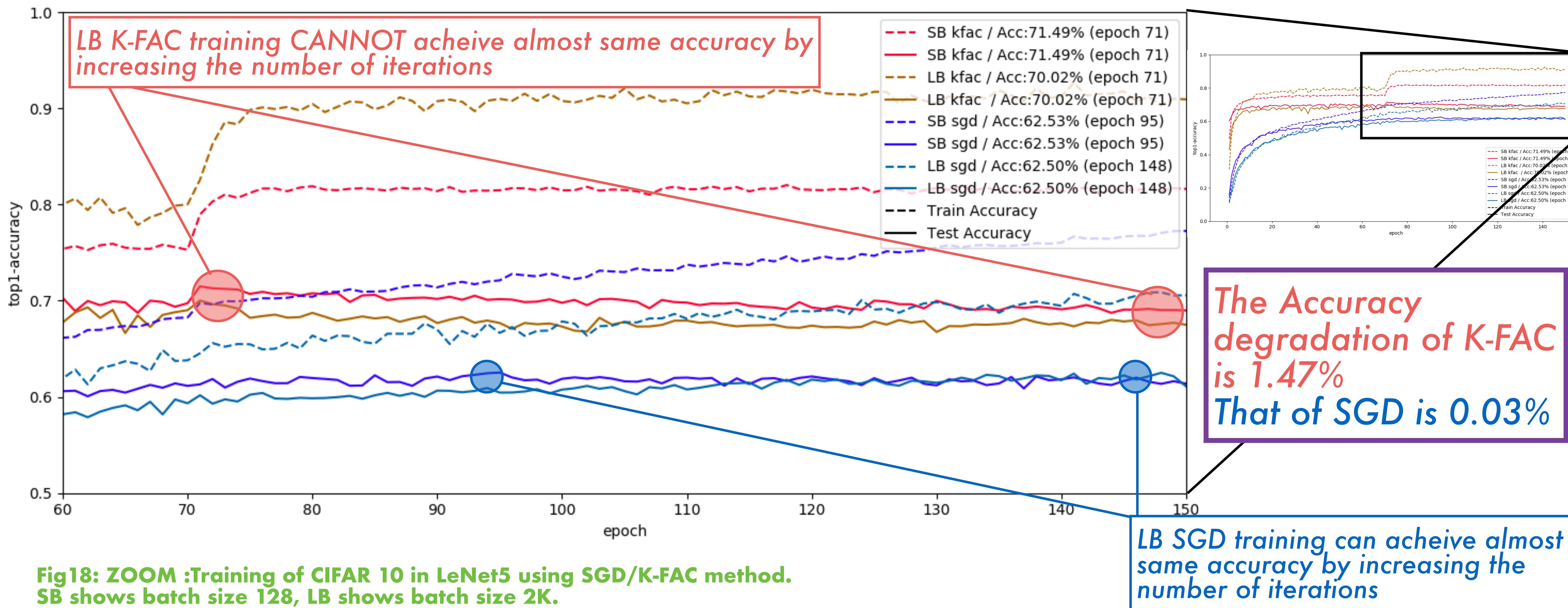
Fig17: ZOOM :Training of CIFAR 10 in LeNet5 using SGD/K-FAC method (same epochs). SB shows batch size 128, LB shows batch size 2K.

# 3. Second Order Optimization Approach

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## Experimental Result

### Experiment1: Training by SGD/K-FAC method without Smoothing etc. (K-FAC Disadvantage)



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**Strategy 2.**  
**Smoothing the objective function**

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By linear interpolation of the input data in large mini-batch training, the convergence to Flat Minimum is promoted in optimization of the loss function, and generalization performance is aimed to be improved.

# 4. Proposal to improve generalization

## Sharp Minima and Flat Minima

**Q, Why does the generalization performance of large mini-batch training deteriorate?**

-> Because it converges to **Sharp Minimum for LB (large batch size)** and **Flat Minimum for SB (small batch size)** [N. Keskar et al, 2017]

### FlatMinimum :

characterized by a significant number of large positive eigenvalues in  $\nabla^2 f(x)$ , and tend to generalize less well

**Optimal solution converged by SB Training**

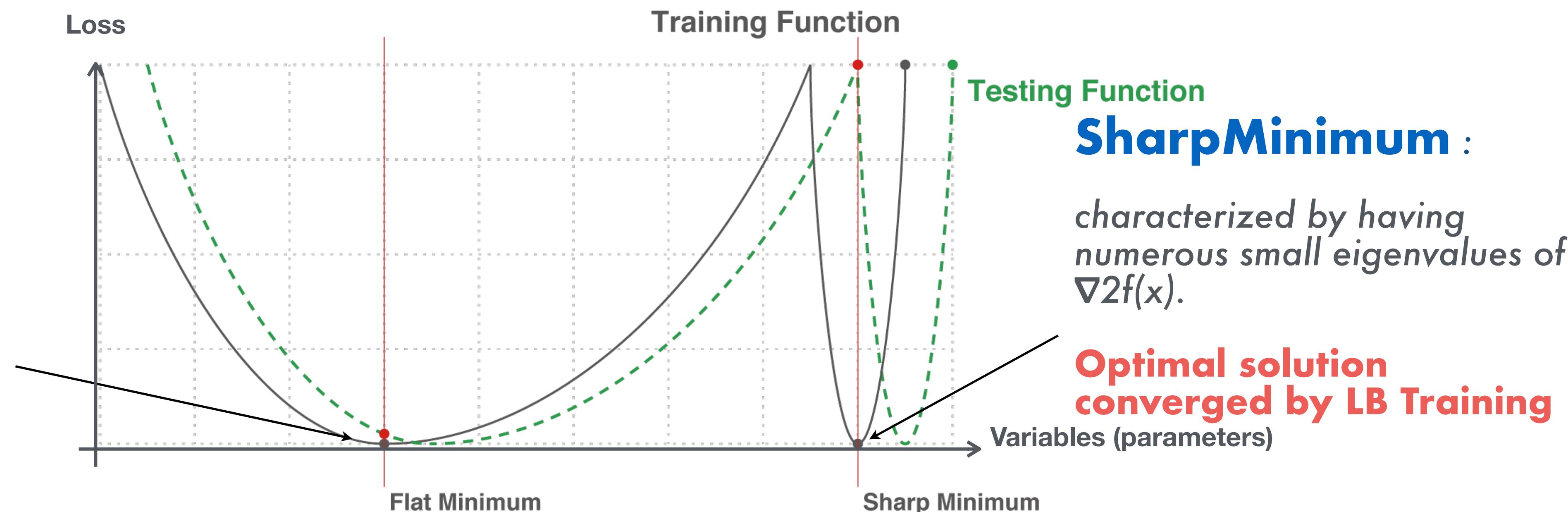


Fig19 : A Conceptual Sketch of Flat and Sharp Minima

**Aim to converge on Flat Minimum, not Sharp Minimum**  
 -> Our Strategy : Use of Data Augmentation

### SharpMinimum :

characterized by having numerous small eigenvalues of  $\nabla^2 f(x)$ .

**Optimal solution converged by LB Training**

# 4. Proposal to improve generalization

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## Data Augmentation

### Data Augmentation

- Generate training samples with artificial noise added to training data
- Especially in image recognition, clipping, inversion, deformation, addition of noise, RGB value manipulation, etc. are common. [P. Y. Simard, et al., 2004]
- Performance improvement is expected by adding the generated image to the original data for training

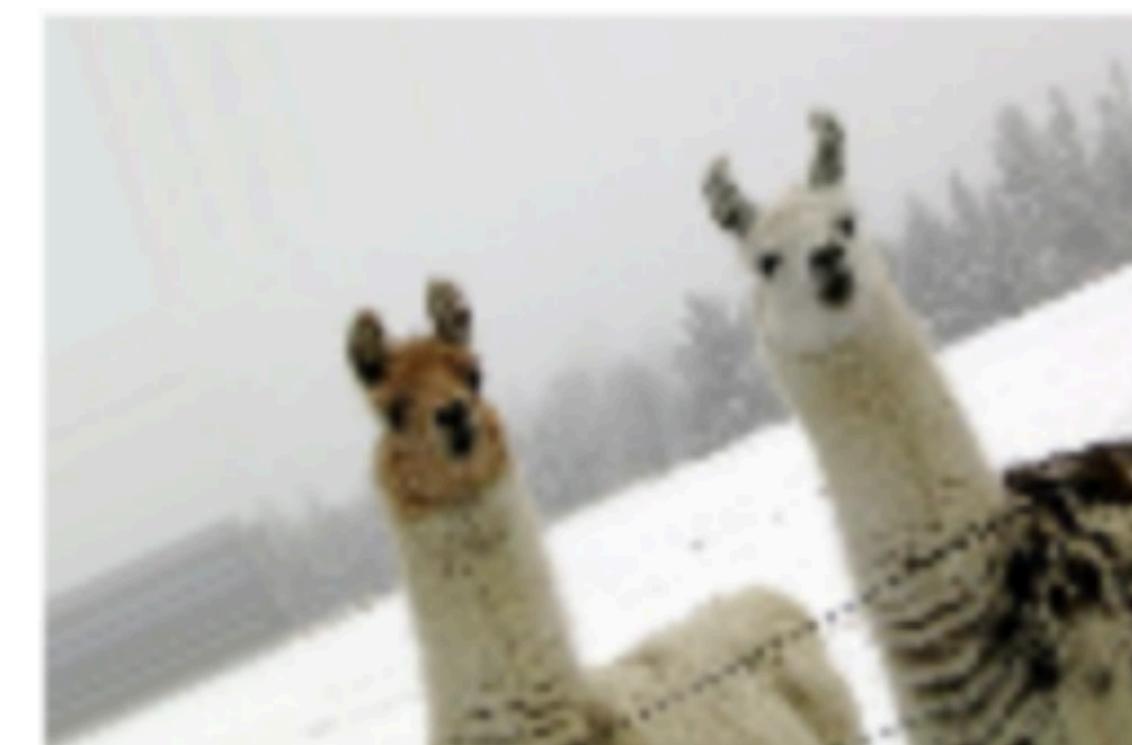


Fig20 : Data Augmentation (inversion / cut out example)

# 4. Proposal to improve generalization

Mixup: Data Augmentation Method for Linear Interpolation of Training Data

## Mixup [H. Zhang et al. 2018]

- **Linear interpolation of both label / data from two data to**
- *Data Augmentation methods, such as Mixup, are not developed for the improvement of generalization performance in large mini-batch training.*
- *However, as a solution to the reduced noise and variance that is a problem in large mini-batch training, we **verified whether generalization performance can be improved by playing the role of objective function smoothing.***

Optimization Problem:  $\theta^* = \arg \min_{\theta} \frac{1}{|\mathcal{S}|} \sum_{(x,y) \in \mathcal{S}} L(y, f(x; \theta))$

Try Smoothing of Loss Function by Linear Interpolating Input Data x

From training data  $(x_i, y_i), (x_j, y_j)$  Which are randomly selected  
 Generate a new training sample  $(\tilde{x}, \tilde{y})$  as follows

$$\tilde{x} = \lambda x_i + (1 - \lambda) x_j \quad \lambda \in [0, 1], \lambda \sim Be(\alpha, \alpha)$$

$$\tilde{y} = \lambda y_i + (1 - \lambda) y_j$$

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## Mixup [H. Zhang et al. 2018]

- **Linear interpolation of both label / data from two data to**

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$$\tilde{y} = \lambda y_i + (1 - \lambda)y_j$$

Thus, by using the beta distribution,  
 finer tuning can be performed for interpolation of training data

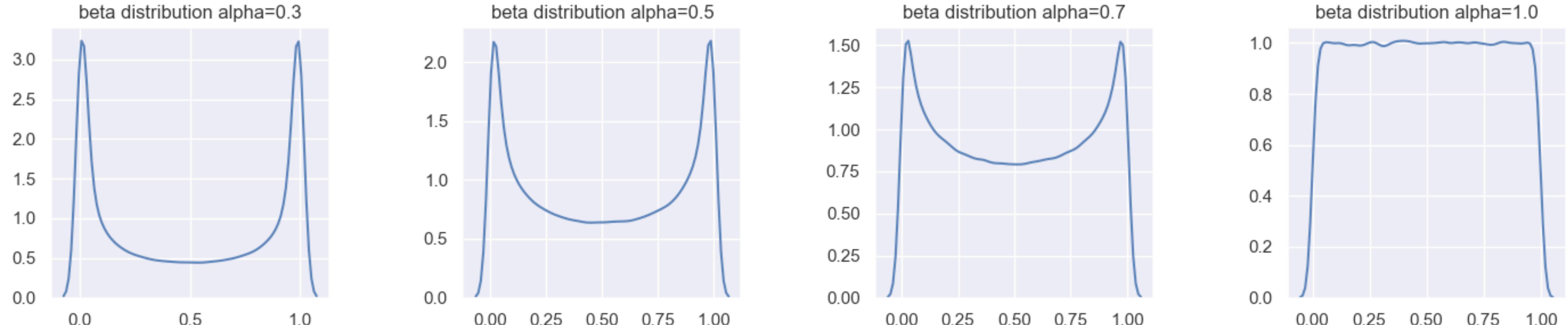
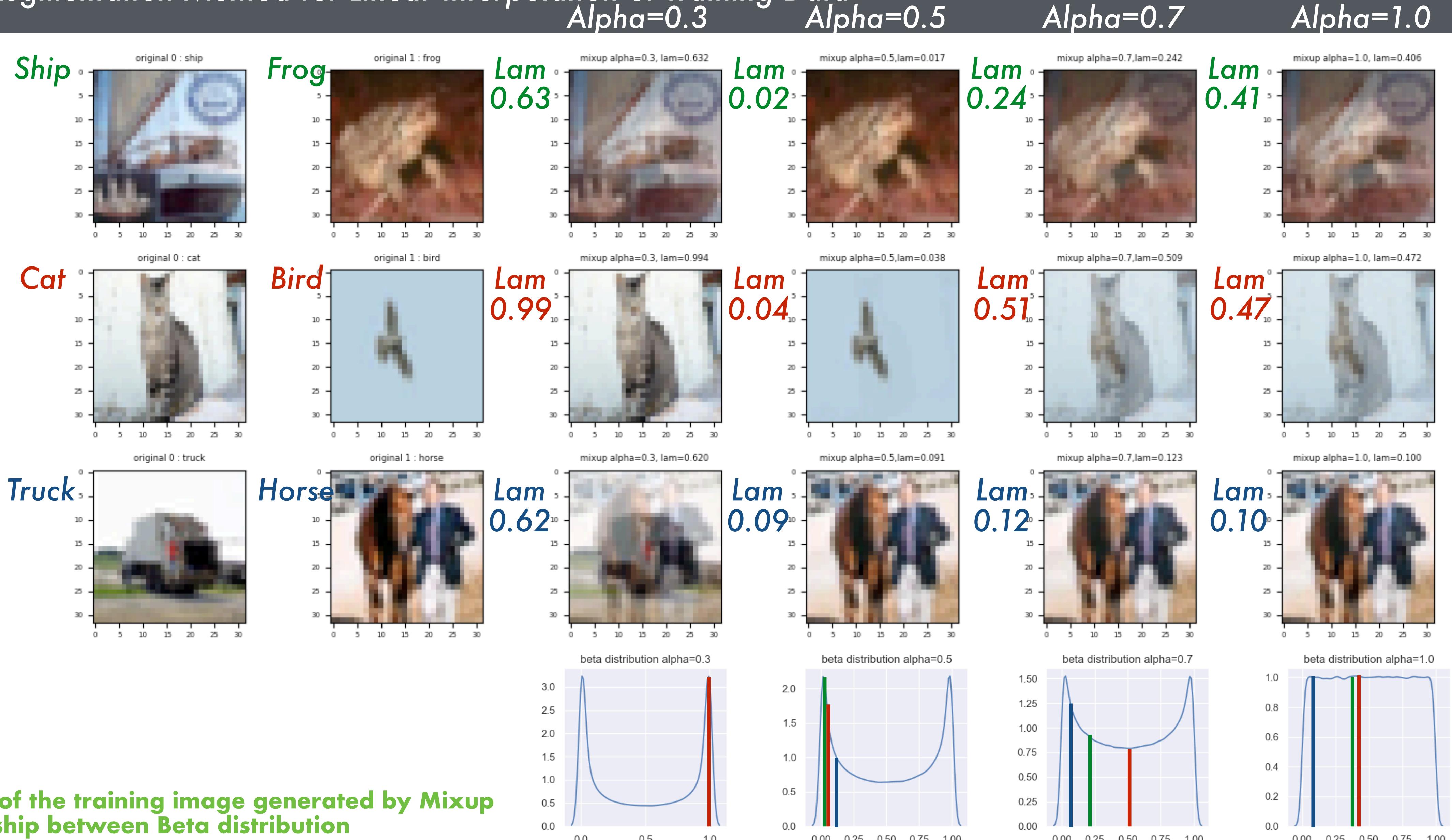


Fig21 : Example of Beta distribution (distribution chart in 10000 trials)

# 4. Proposal to improve generarization

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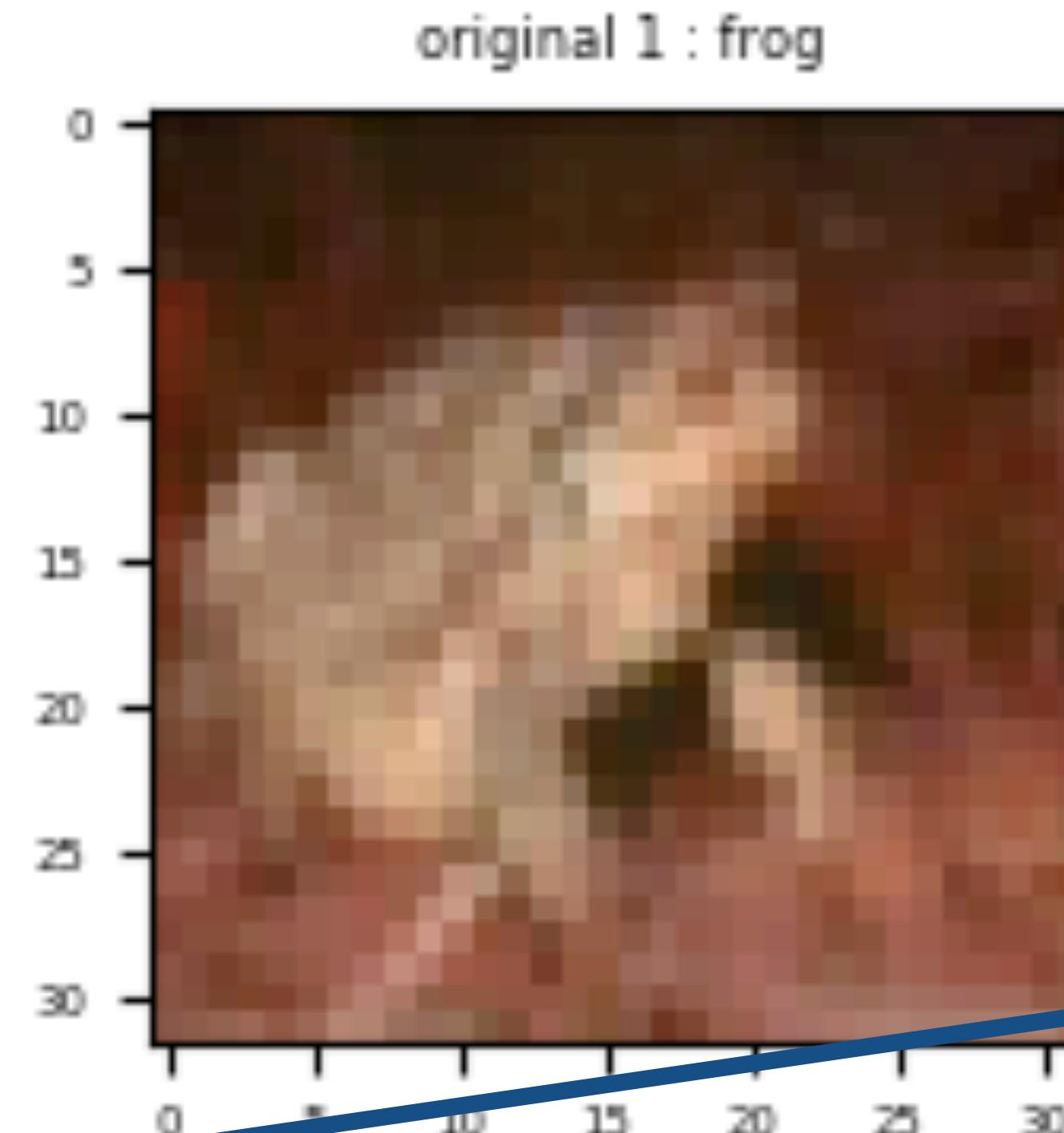
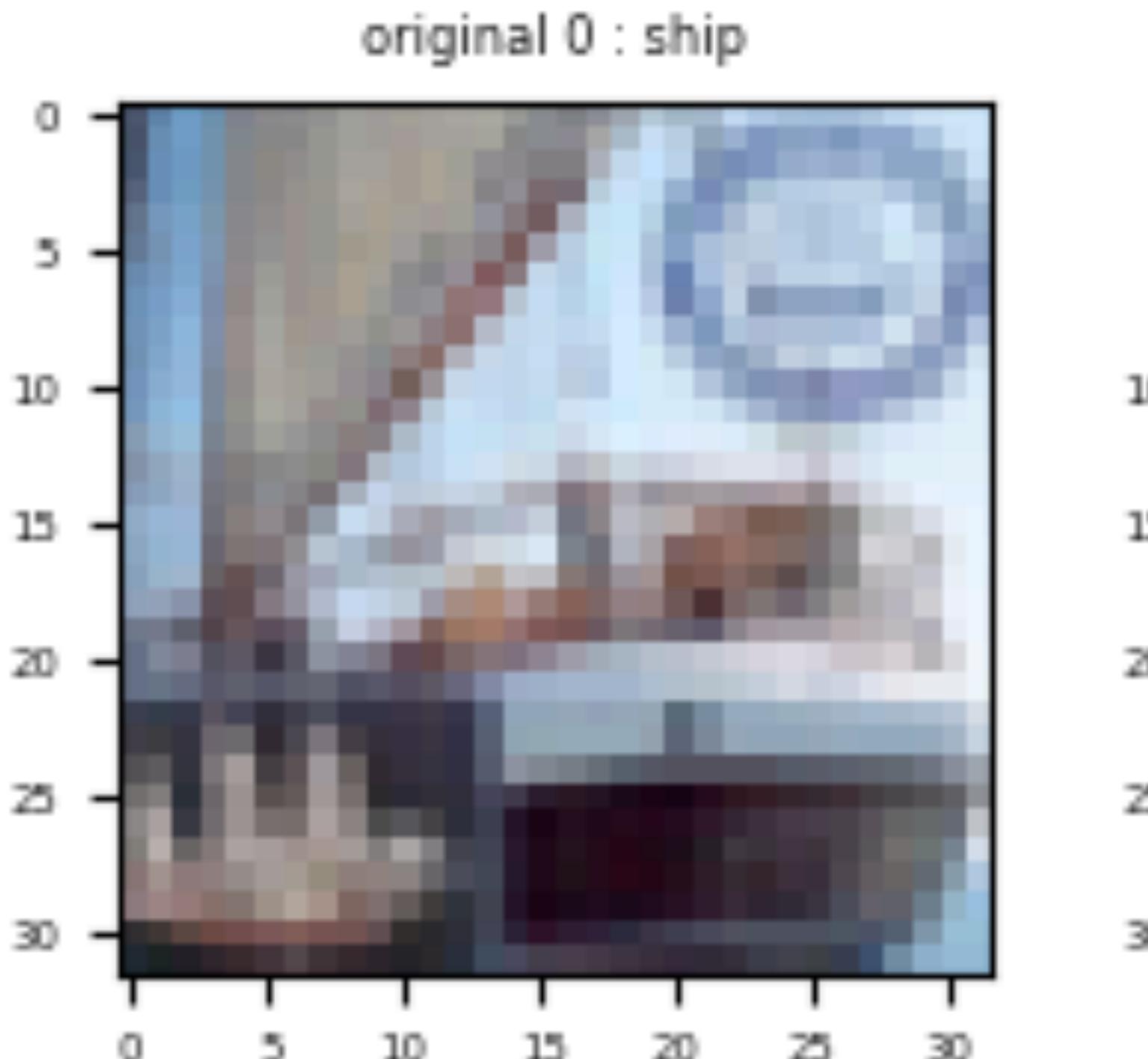
Mixup: Data Augmentation Method for Linear Interpolation of Training Data



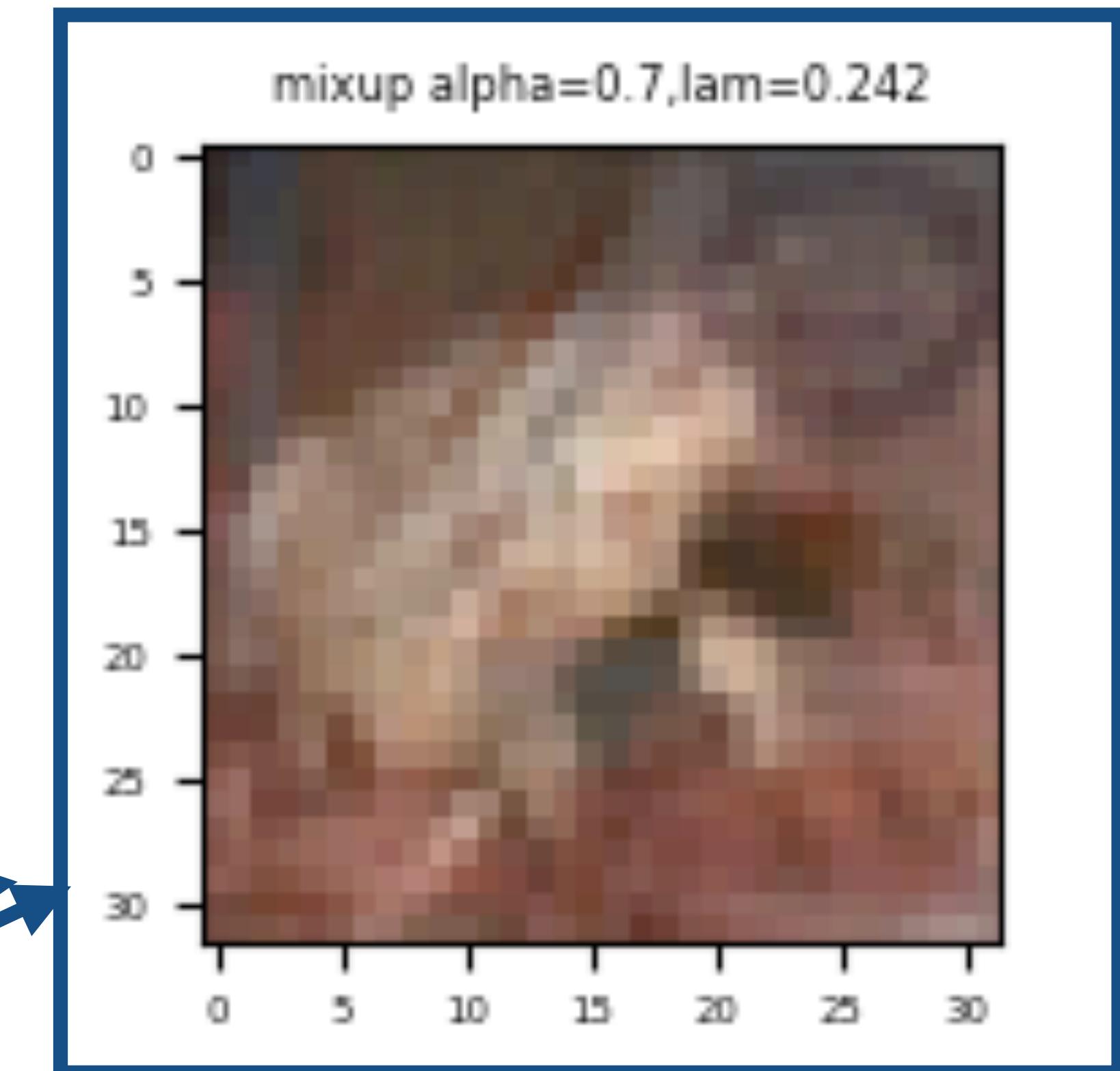
## 4. *Proposal to improve generalization*

# Calculation method of training loss using Mixup

## Fig23 : Example of learning image generated by Mixup and Lambda



*This image is used to evaluate Loss*



*Ship Loss*  $\times \lambda$  + *Frog Loss*  $\times (1-\lambda)$  = *Mixup (Ship and Frog) Loss*

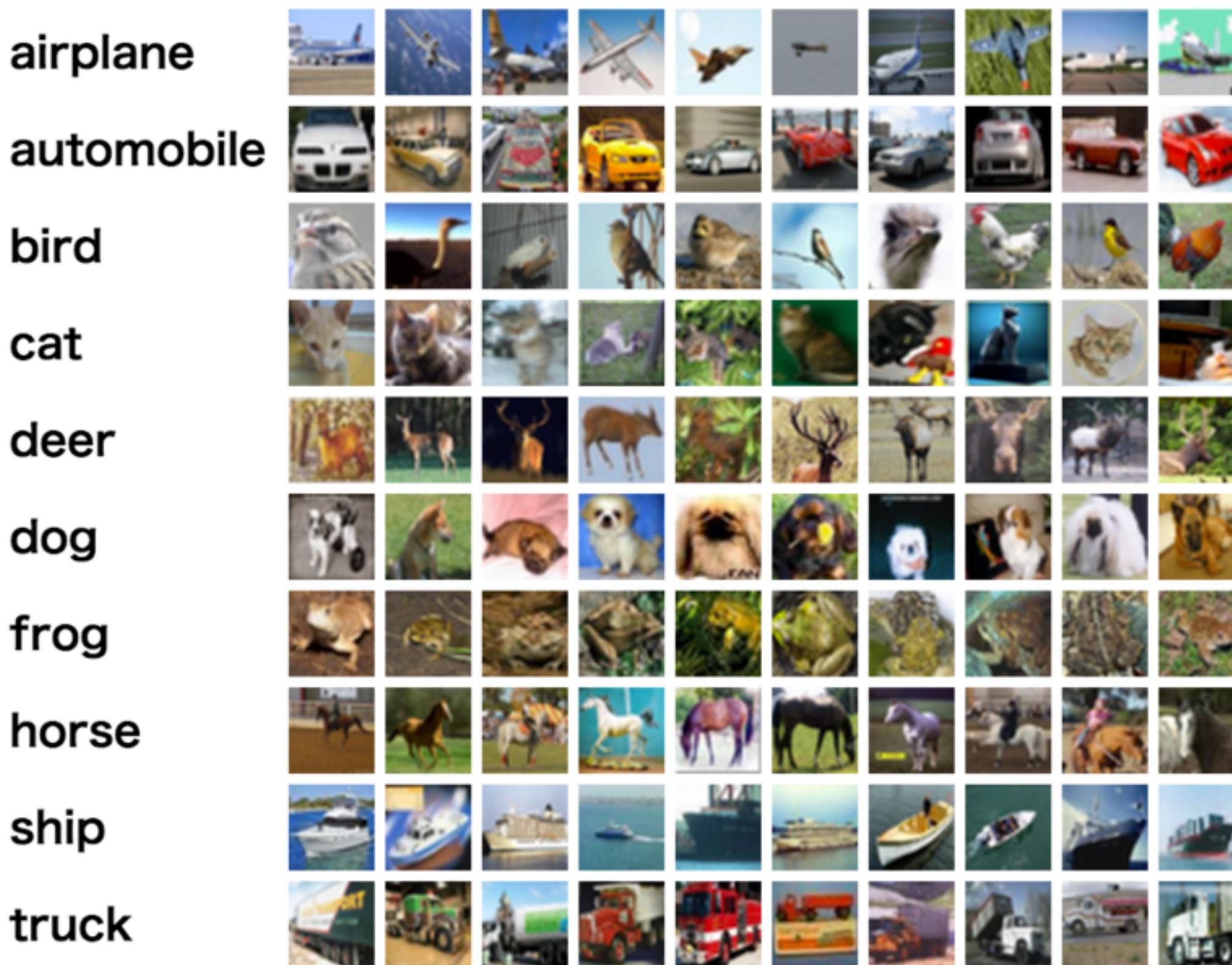
Since  $\lambda = 0.242$  this time, the loss is large if it can not be inferred as a Frog than Ship

## 4. *Proposal to improve generalization*

# *Experimental Methodology*

# Data Set : CIFAR-10

The CIFAR-10 dataset is a data set of  $32 \times 32$  pixels (RGB) color image labeled with 10 classes of {airplane, automobile, bird, cat, deer, dog, frog, horse, ship, truck}.

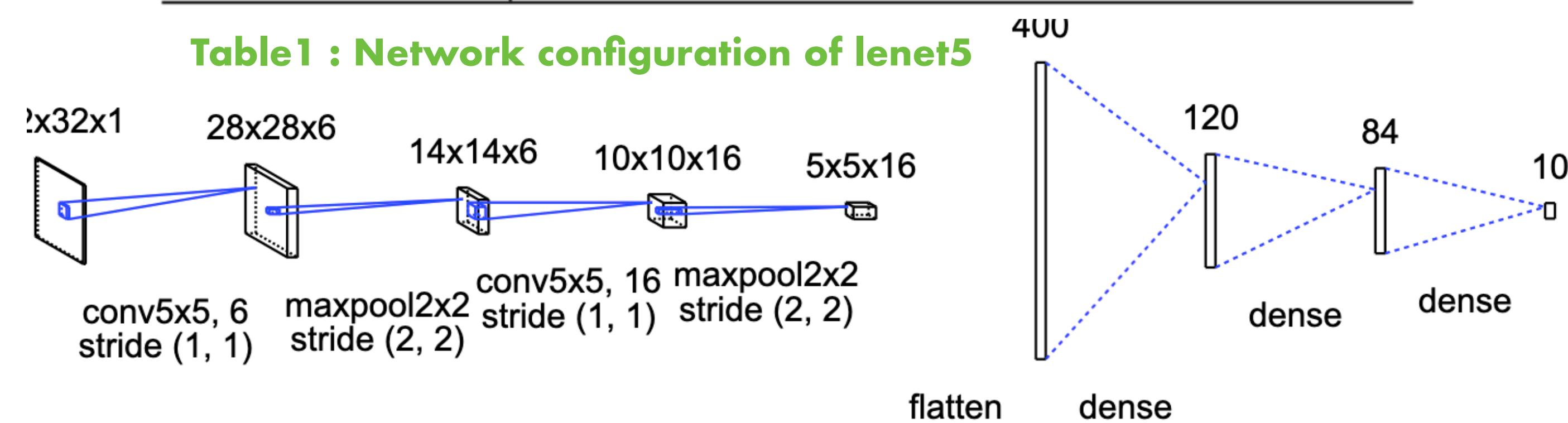


# DNN Model : Lenet5

*Lenet5 which is a simple multilayer neural network model by the structure proposed by LeCun et al was used as a DNN model.*

Layer Type	Description
Convolution	Filter Size $5 \times 5$ , Output Channel 6
MaxPooling	Kernel Size $2 \times 2$
Convolution	Filter Size $5 \times 5$ , Output Channel 16
MaxPooling	Kernel Size $2 \times 2$
FC	Output Size 120
FC	Output Size 84
FC	Output Size 10

## Table 1 : Network configuration of lenet5



## Fig14 : Category of training data set CIFAR-10 used in experiment and its sample example

## Fig15 : Network configuration of lenet5

# 4. Proposal to improve generalization

## Experimental Methodology

### Program for Training: Chainer, PyTorch

Using Chainer, which is an open source software library for machine learning, we constructed the DNN model and implemented its training with the programming language Python.

We use Chainer\_K-FAC to implement distributed deep learning using K-FAC.

For visualization of the loss function, PyTorch which is an open source software library for machine learning was used with reference to [L. Hao et al. 2018]

### Computational Environment: (ABCi; AI Bridging Cloud Infrastructure)

All experiments were performed on the ABCI(AI Bridging Cloud Infrastructure) supercomputer at AIST.

For the experiment, one computation node is used, and one node consists of NVIDIA Tesla V100 x 4GPU and Intel Xeon Gold 6148 2.4 GHz, 20 Cores x 2CPU.

CentOS 7.4, Python 3.6.5, cuDNN 7.4, CUDA 9.2 are used as the software environment. **Table2 : Hyper Parameter used in Experiment**

### Training Strategy

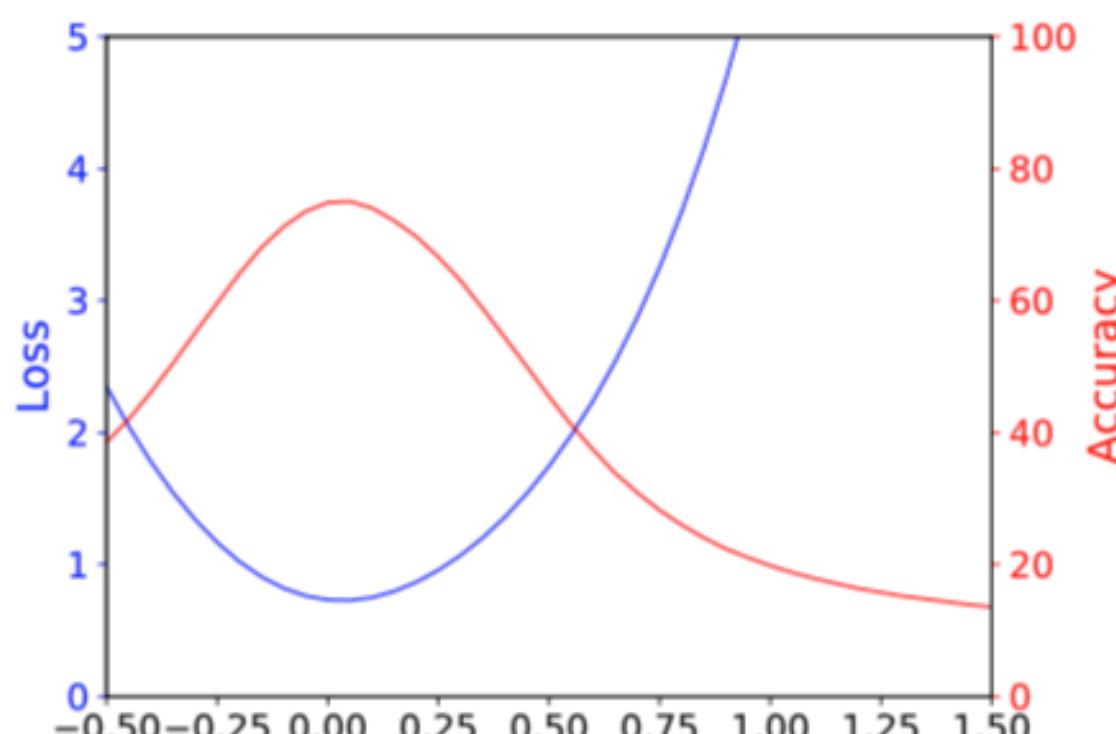
The model of the network is trained using mini-batch extracted randomly from the training data, and **SGD / K-FAC is used as the optimization method**. It is used that learning rate decay for stabilizing convergence, weight decay for suppressing over training of values of parameters during training and momentum for adjusting the steepest vector calculated during training. The hyperparameter used in this experiment is shown in right table.

Weight Decay	1e-4
Momentum	0.9
Learning Rate(SB SGD)	5e-3 → 2.5e-3 (71epoch)
Learning Rate(SB SGD no mixup)	1e-3 → 5e-4 (71epoch)
Learning Rate(LB SGD)	1e-2 → 5e-3 (71epoch)
Learning Rate(LB SGD no mixup)	5e-3 → 2.5e-3 (71epoch)
Learning Rate(SB K-FAC)	5e-3 → 2.5e-3 (71epoch)
Learning Rate(SB K-FAC no mixup)	2e-3 → 1e-3 (71epoch)
Learning Rate(LB K-FAC)	8e-3 → 4e-3 (71epoch)
Learning Rate(LB K-FAC no mixup)	4e-3 → 2e-3 (71epoch)
Mixup Alpha(SB K-FAC)	0.9
Mixup Alpha(LB K-FAC)	0.7
Epoch	150
Batch Size	128 or 2048

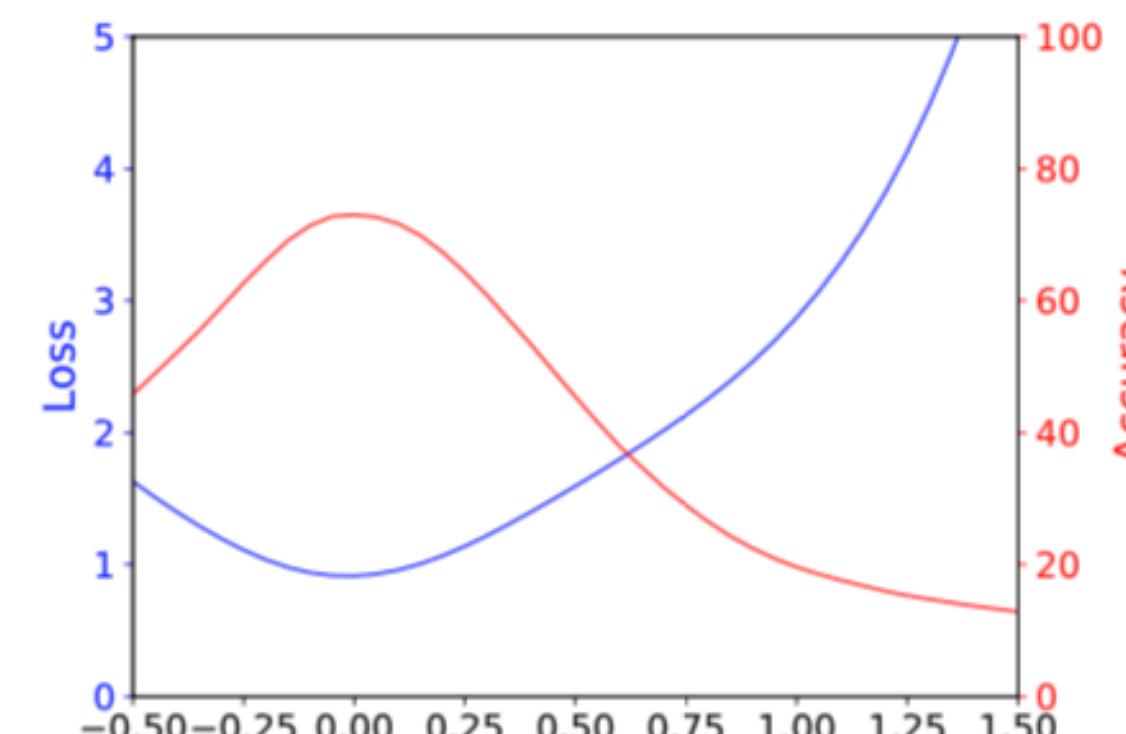
# 4. Proposal to improve generalization

## Experimental Result

### Experiment2: Visualization of Loss Function in K-FAC Training using Mixup



(a) Loss Function obtained from Optimization by K-FAC without Mixup



(b) Loss Function obtained from Optimization by K-FAC with Mixup

#### How to plot this graph?

The blue line shows the loss value, and the red line shows the Top1- Accuracy. The horizontal axis shows the amount of change in parameter space.

$$f(\alpha) = L(\theta^* + \alpha\delta)$$

$\alpha$  : scalar value,  $[-0.5, 1.5]$  in the graph on the left

$\delta$  : Gaussian noise of the same dimension as the parameter

$\theta^*$ : Optimal solution in training (X-coordinate 0)

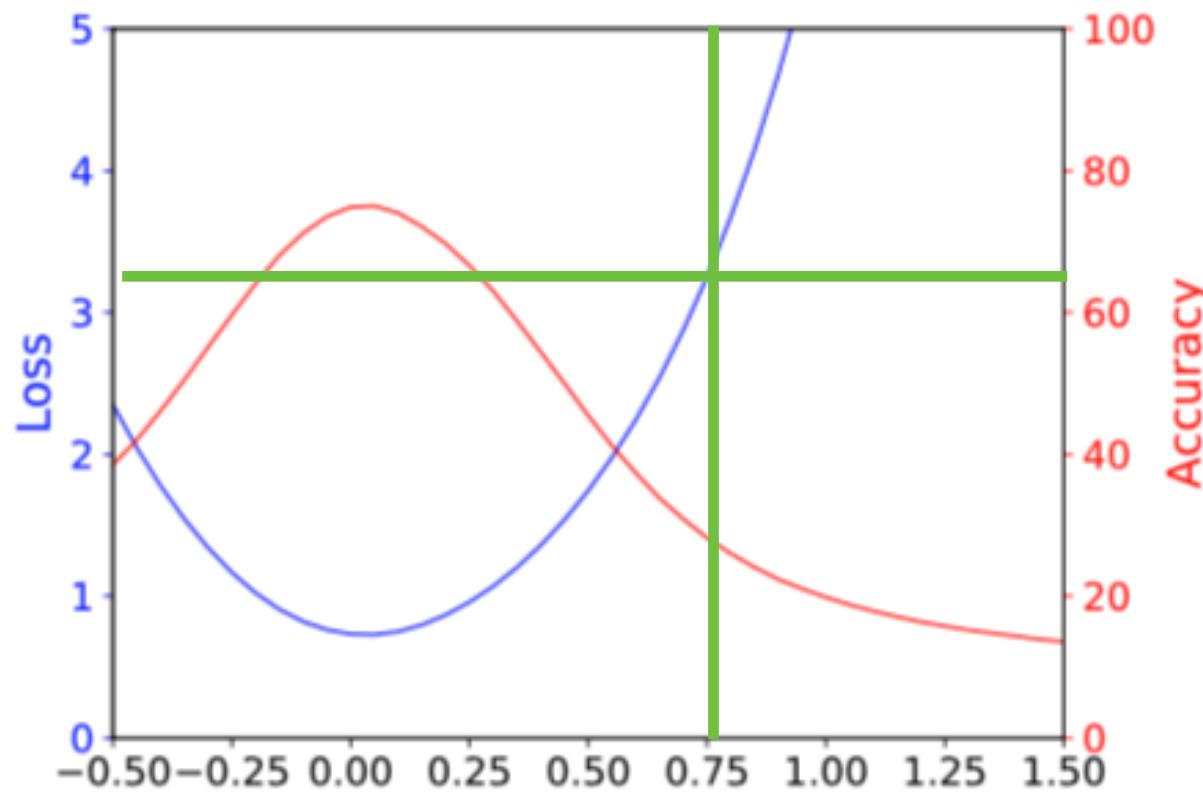
Fig24: One-dimensional linear interpolation diagram of the solution obtained by training using K-FAC method

# 4. Proposal to improve generalization

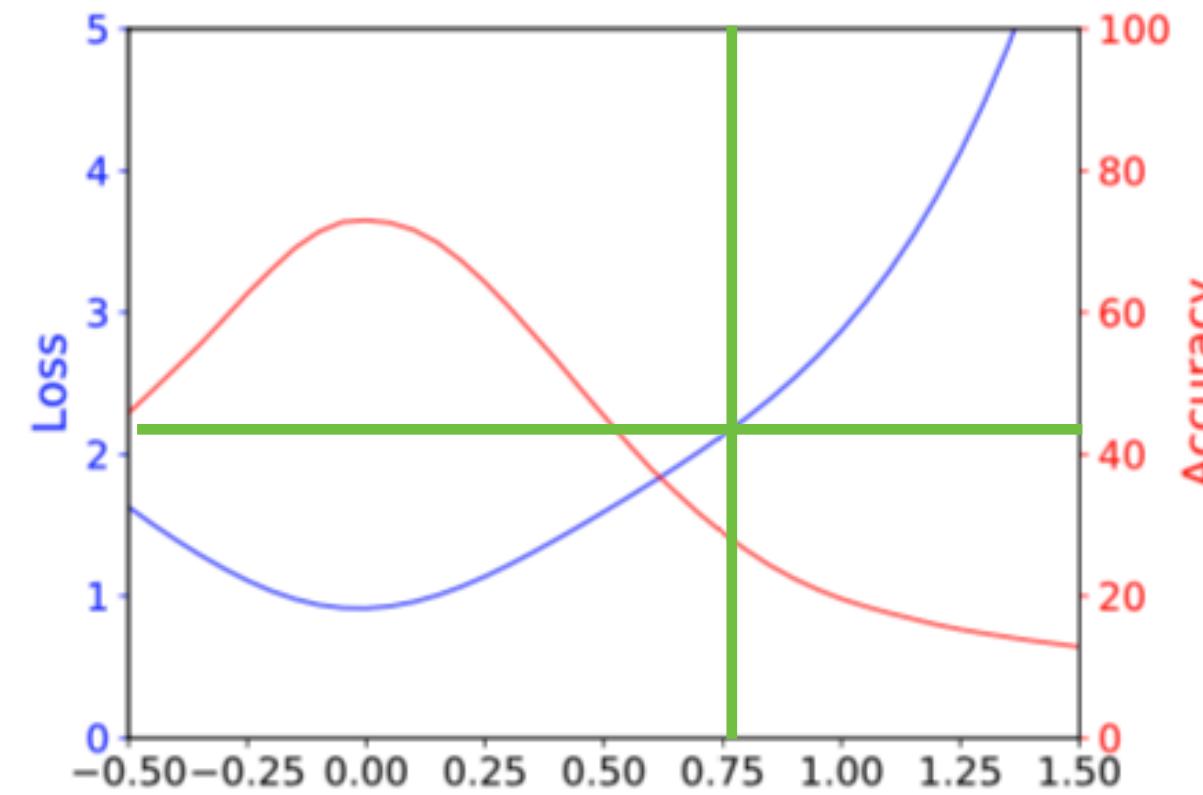
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## Experimental Result

### Experiment2: Visualization of Loss Function in K-FAC Training using Mixup



(a) Loss Function obtained from Optimization by K-FAC without Mixup



(b) Loss Function obtained from Optimization by K-FAC with Mixup

By linear interpolation of input data in large mini-batch training, it can be confirmed that convergence to Flat Minimum is explicitly promoted in optimization of loss function

Fig25: One-dimensional linear interpolation diagram of the solution obtained by training using K-FAC method

# 4. Proposal to improve generarization

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## Experimantal Result

### Experiment3: SGD/K-FAC Training with Smoothed Loss Function (LB comparison with and without Mixup)

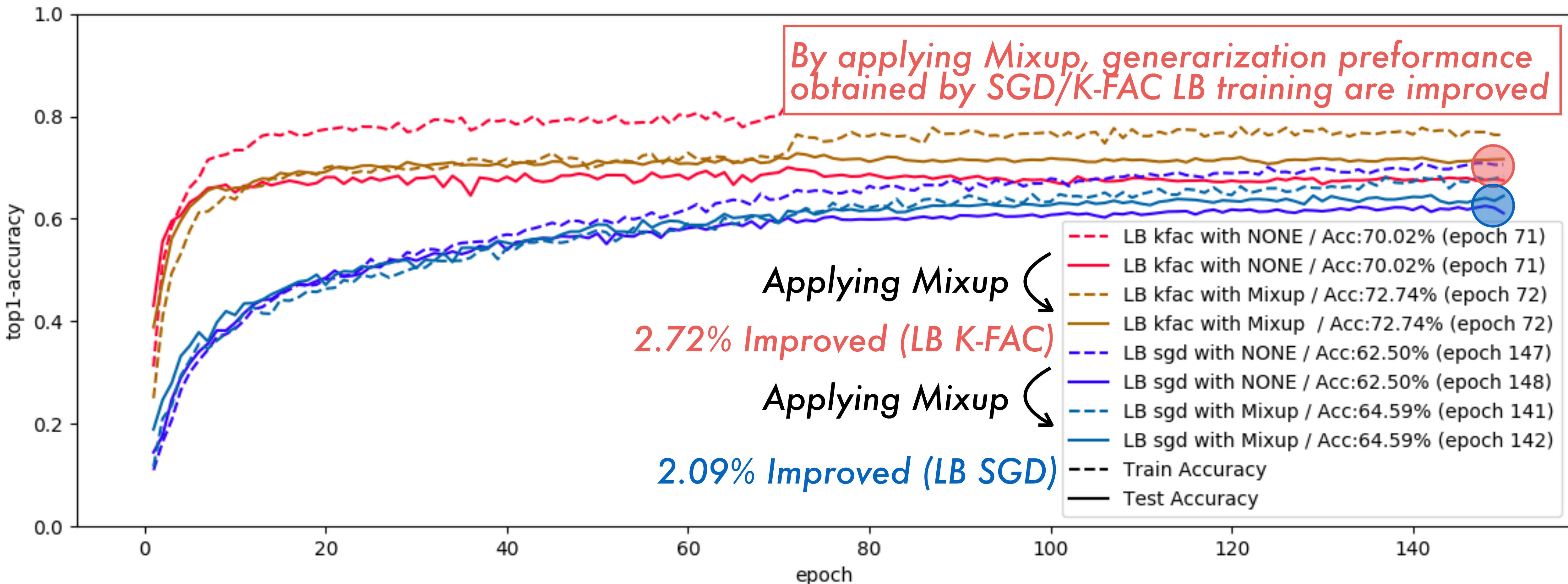


Fig26: Training of CIFAR 10 in LeNet 5 using SGD/K-FAC method. SB shows batch size 128, LB shows batch size 2K

# 4. Proposal to improve generalization

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## Experimental Result

### Experiment3: SGD/K-FAC Training with Smoothed Loss Function (with Mixup comparison SGD and K-FAC)

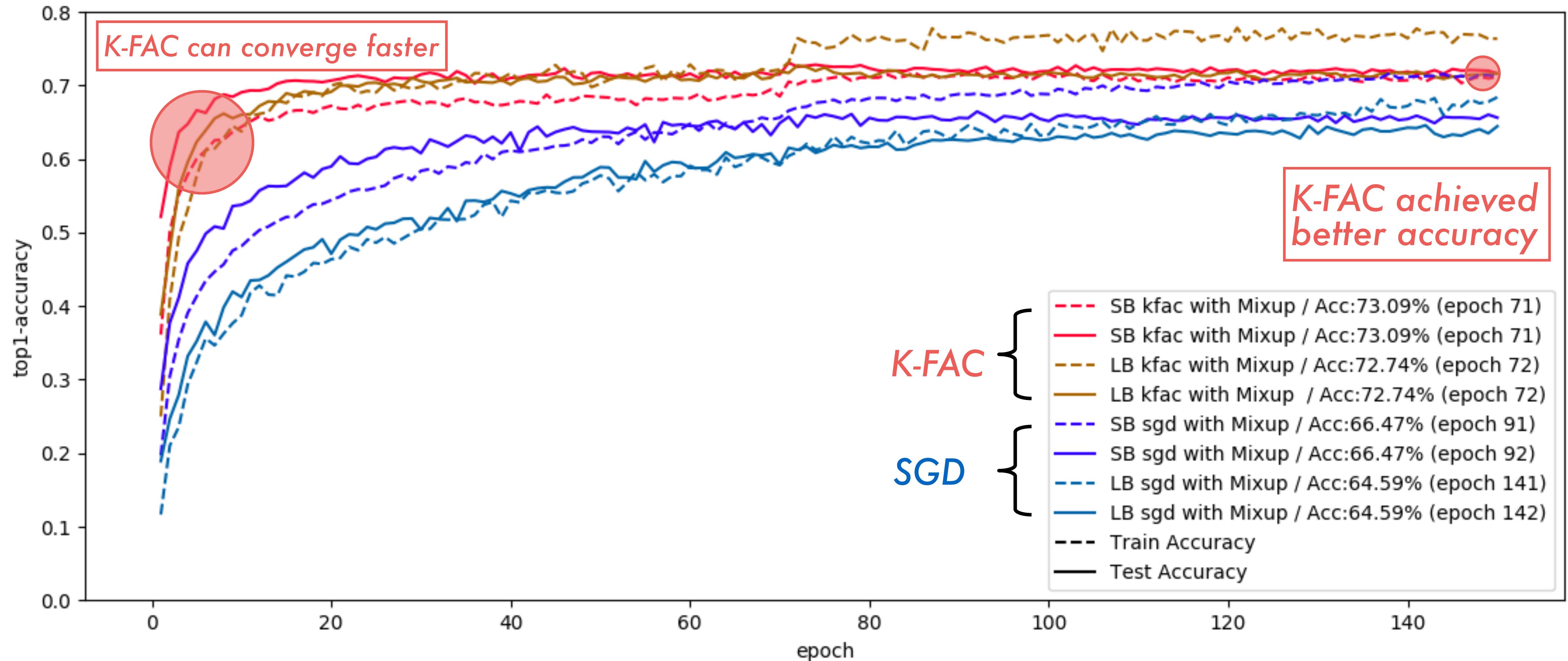


Fig27: Training of CIFAR 10 in LeNet 5 using SGD/K-FAC method with Smoothing. SB shows batch size 128, LB shows batch size 2K

# 4. Proposal to improve generalization

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## Experimental Result

### Experiment3: SGD/K-FAC Training with Smoothed Loss Function (with Mixup comparison SGD and K-FAC)

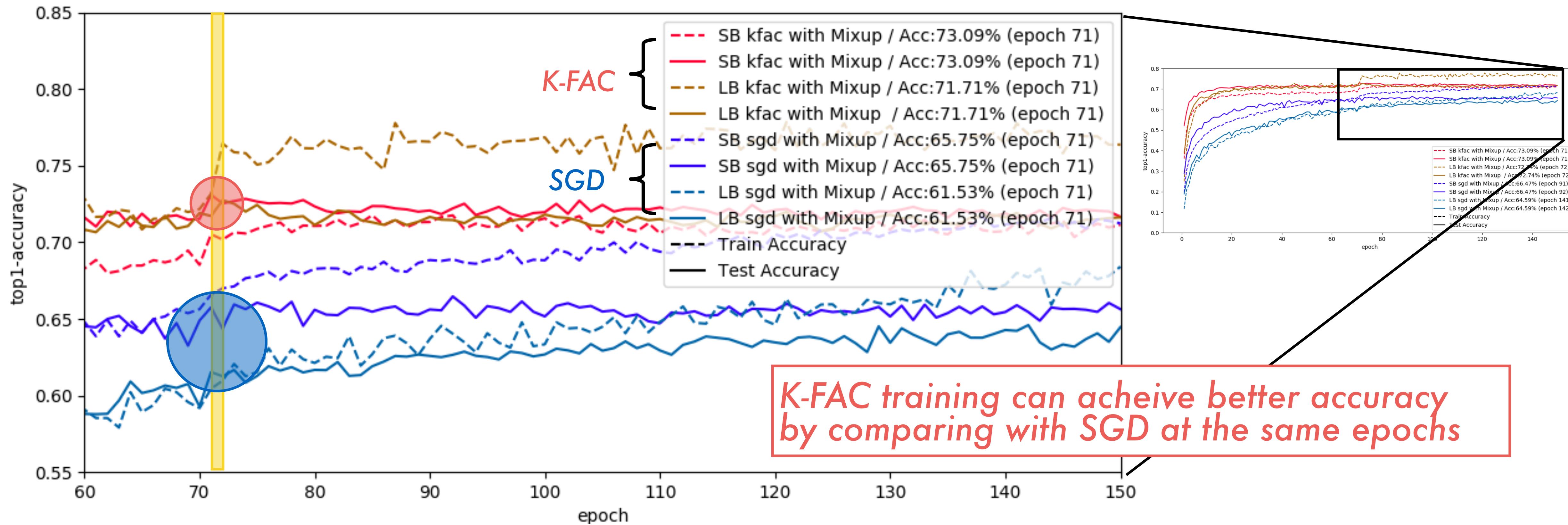


Fig28: ZOOM : Training of CIFAR 10 in LeNet 5 using SGD/K-FAC method with Smoothing (same epochs). SB shows batch size 128, LB shows batch size 2K

# 4. Proposal to improve generalization

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## Experimental Result

### Experiment3: SGD/K-FAC Training with Smoothed Loss Function (with Mixup comparison SGD and K-FAC)

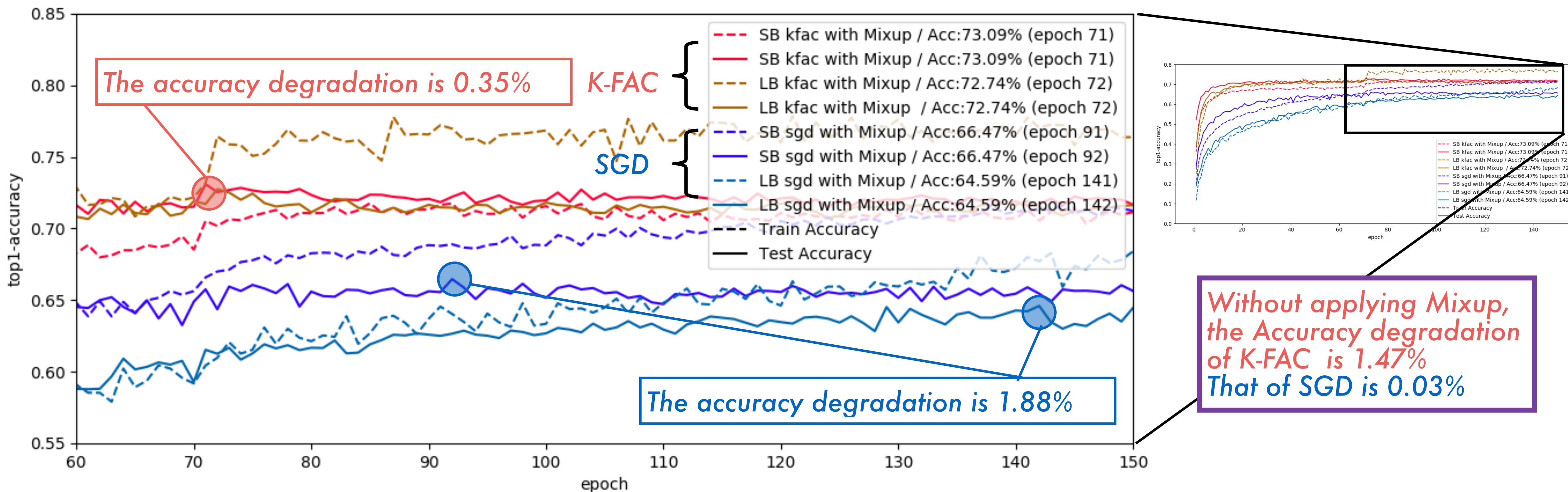


Fig29: ZOOM : Training of CIFAR 10 in LeNet 5 using SGD/K-FAC method with Smoothing. SB shows batch size 128, LB shows batch size 2K

# 4. Proposal to improve generalization

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## Experimental Result

### Experiment3: K-FAC Training with Smoothed Loss Function (K-FAC comparison with and without Mixup)

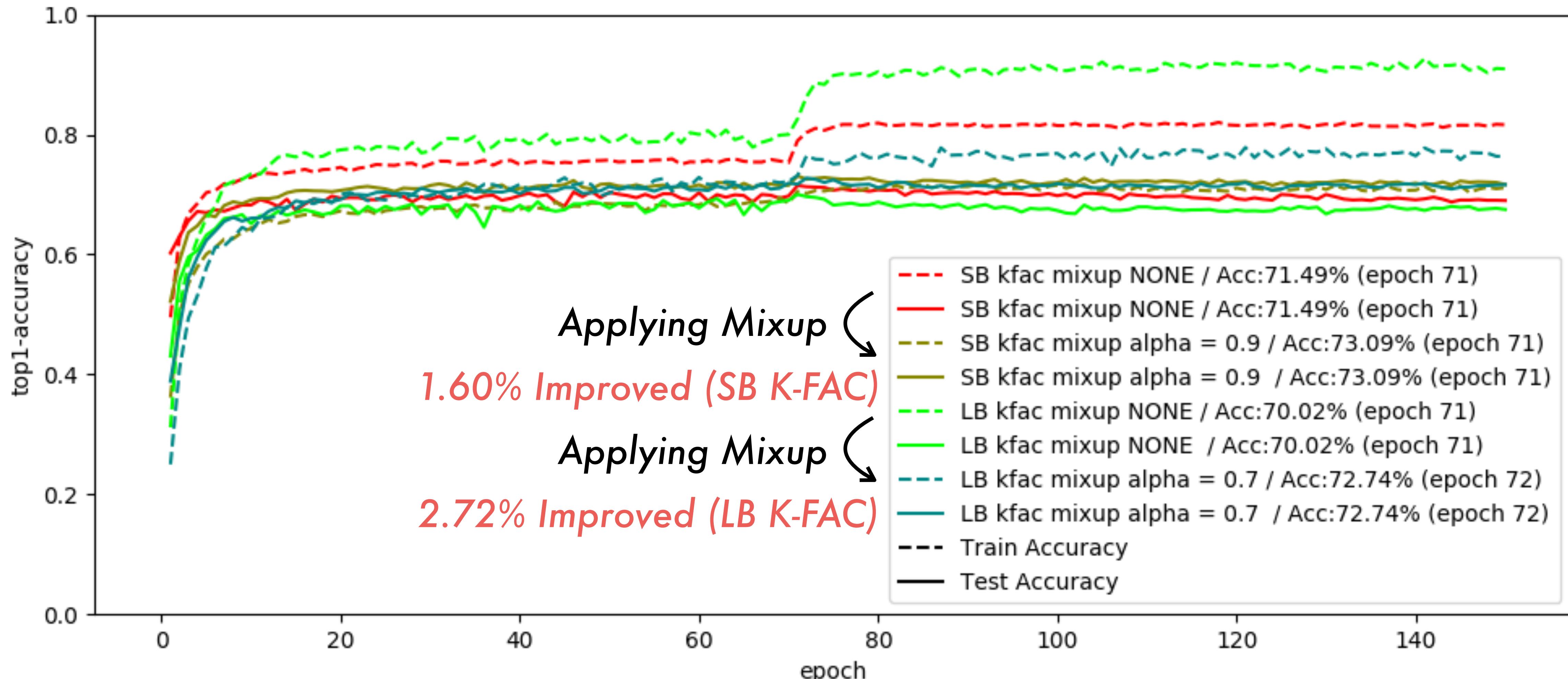


Fig30: Training of CIFAR 10 in LeNet 5 using K-FAC method with Smoothing. SB shows batch size 128, LB shows batch size 2K

# 4. Proposal to improve generalization

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## Experimental Result

### Experiment3: K-FAC Training with Smoothed Loss Function (K-FAC comparison with and without Mixup)

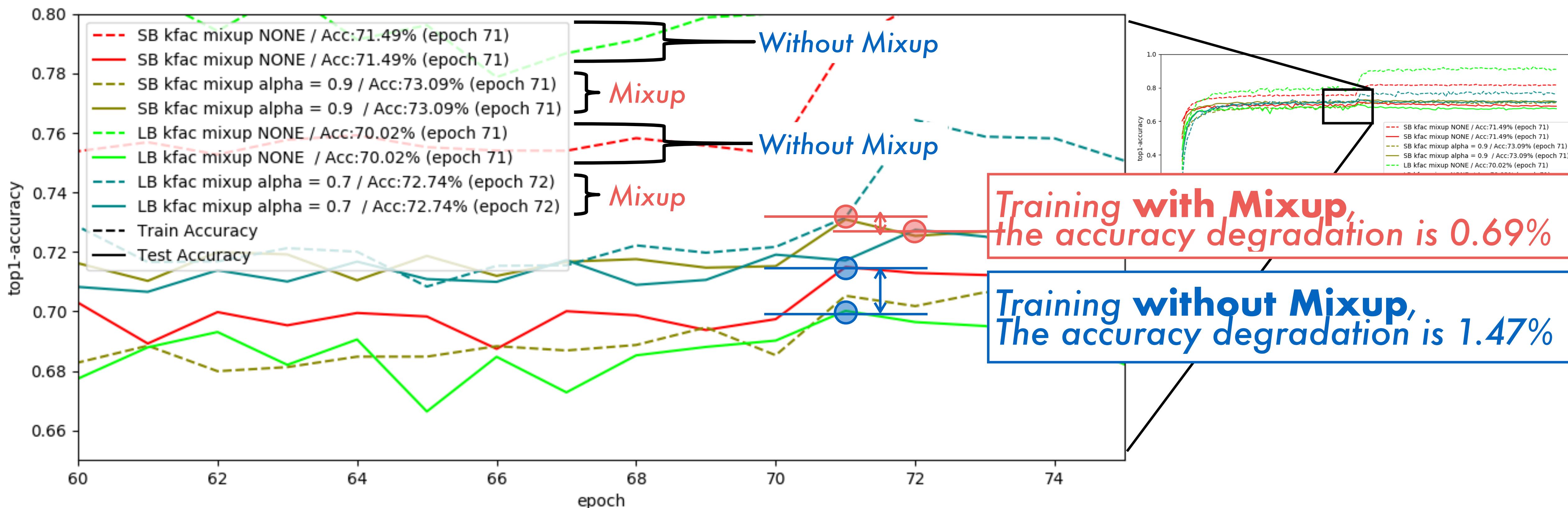


Fig31: ZOOM : Training of CIFAR 10 in LeNet 5 using K-FAC method with Smoothing. SB shows batch size 128, LB shows batch size 2K

By applying Mixup, generalization performance is improved and performance degradation due to LB is reduced

## Introduction / Motivation

- Accuracy  $\nearrow$  Model Size and Data Size  $\nearrow$
- Needs to Accelerate

## Second Order Optimization Approach

- Natural Gradient Descent
- K-FAC (Approximate Method)
- Experimantal Methodology and Result

## Background / Problem

- Three Parallelism of Distributed Deep Learning
- Large Mini-Batch Training Problem
- Two Strategies

## Proposal to improve generarization

- Sharp Minima and Flat Minima
- Mixup Data Augmentation
- Smoothing Loss Functionl
- Experimantal Methodology and Result

## Conclusion

## Our Work Position

- Data Parallel Distributed Deep Learning
- Second-Order Optimization
- Improve Generalization

## Contribution

- Point out the problem of generalization performance degradation by second-order optimization
- Validate whether it is possible to improve generalization performance degradation problem by focusing on smoothness of loss function
- Discover shape change of loss function by Mixup
- Succeeded in suppressing degradation of generalization performance to less than half of conventional methods

## Future work

- Perform experiments with a larger data set and DNN model
- mathematical elucidation is required for the relationship between deterioration of generalization performance due to a decrease in the number of updates and due to a decline variance of the gradient

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*Thanks!*  
Q&A

*Backup*

# 4. Proposal to improve generalization

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## Experimental Result

### Experiment3: SGD Training with Smoothed Loss Function (comparison with and without Mixup)

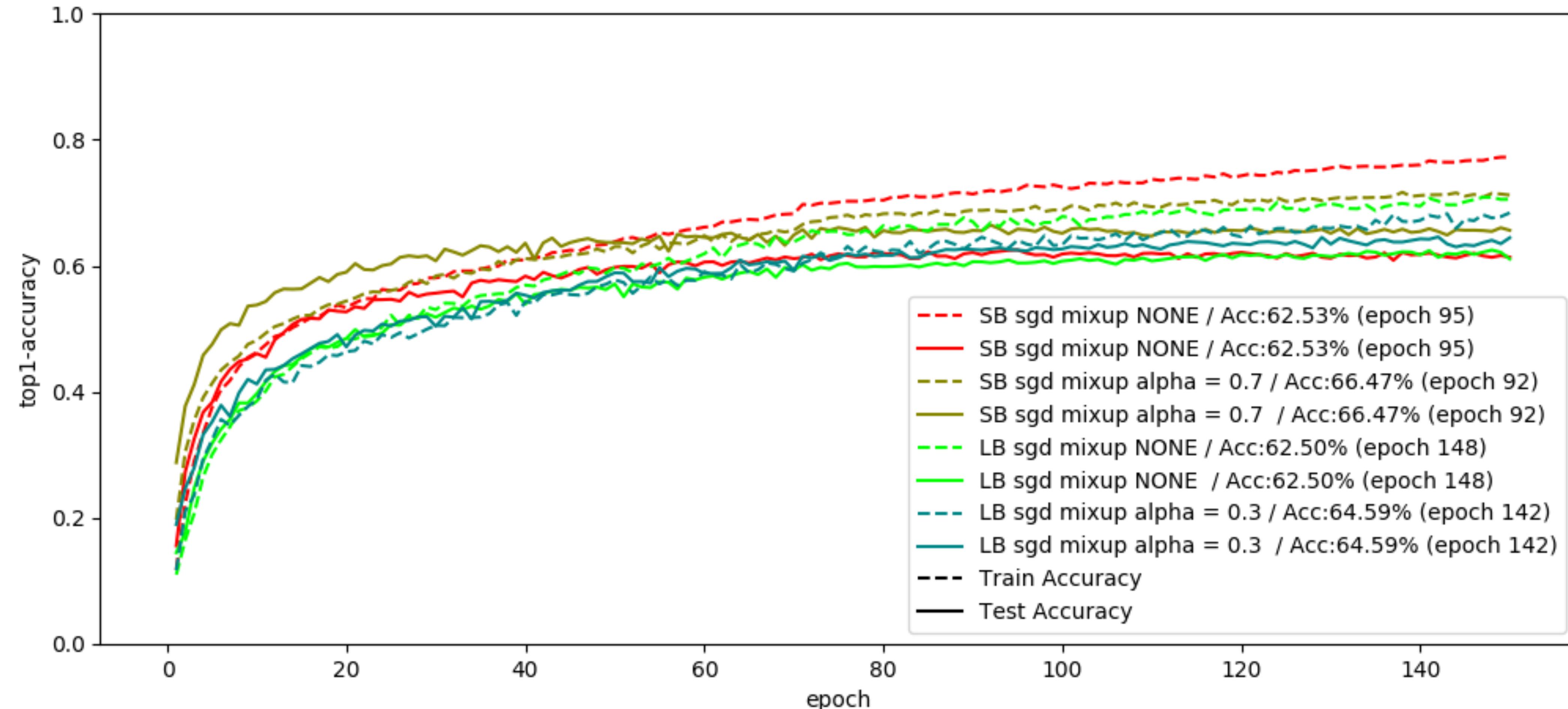


Fig25: Training of CIFAR 10 in LeNet 5 using SGD method with Smoothing. SB shows batch size 128, LB shows batch size 2K