1

Q1. a) Convert to simple English sentences

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i) \pi_{sname}(\pi_{sid}(\sigma_{tagname='PPE'}ProductTag) \bowtie (\sigma_{cost<6}Catalog)) \bowtie Suppliers)
```

Get the names of the suppliers that have PPE that costs less than 6. [Outputs the suppliers that have products tagged with 'PPE' and a cost of less than 6]

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ii) \pi_{sname}(\pi_{sid}(\sigma_{tagname='PPE'}ProductTag)\bowtie(\sigma_{cost<6}Catalog)\bowtie Suppliers)
```

Nothing is returned from this operation.

 $[(\sigma_{tagname='PPE'}ProductTag) \bowtie (\sigma_{cost<6}Catalog)$ returns the products with tag PPE and cost ; 6, columns are: tid, pid, tagname, sid, pid, cost. Natural join with supplier looks at common sid, so that returns the suppliers with products of tag PPE and cost ; 6. Projecting sid will result in each tuple only having an sid. Projecting the sname of a table where the tuples have only sid results in nothing being returned.]

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iii) \pi_{sname}(\sigma_{tagname='PPE'}ProductTag)\bowtie(\sigma_{cost<6}Catalog)\bowtie Suppliers )\cap\pi_{sname}(\sigma_{tagname='SuperTech'}ProductTag)\bowtie(\sigma_{cost<6}Catalog)\bowtie Suppliers )
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Gets the names of the suppliers that offer PPE made by SuperTech that costs less than 6.

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 \begin{array}{l} \mathrm{iv}) \\ \pi_{sid}( \\ \hspace{0.5cm} (\sigma_{tagname='PPE'}ProductTag) \bowtie (\sigma_{cost<6}Catalog) \bowtie Suppliers \\ ) \cup \pi_{sid}( \\ \hspace{0.5cm} (\sigma_{tagname='SuperTech'}ProductTag) \bowtie (\sigma_{cost<6}Catalog) \bowtie Suppliers \\ ) \end{array}
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Gets the supplier IDs of suppliers that offer PPE or (inclusive) SuperTech products, both having a cost less than 6.

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v) \pi_{sname}(\\ (\pi_{sid,sname}(\\ (\sigma_{tagname='PPE'}ProductTag)\bowtie(\sigma_{cost<6}Catalog)\bowtie Suppliers)\\ )\cap(\pi_{sid,sname}(\\ (\sigma_{tagname='SuperTech'}ProductTag)\bowtie(\sigma_{cost<6}Catalog)\bowtie Suppliers)\\ ))
```

Get the names of the suppliers that offer PPE made up SuperTech with a cost less than 6.

Q1. b) Write relational algebra

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i) \pi_{sname}(\sigma_{(tagname='PPE')\vee(tagname='Testing')}ProductTag \bowtie Catalog \bowtie Suppliers)
ii) (\pi_{sid}((\sigma_{tagname='PPE'}ProductTag) \bowtie (\sigma_{cost<10 \land cost>420}Catalog) \bowtie Suppliers))
iii) (\pi_{sid}((\sigma_{tagname='PPE'}ProductTag) \bowtie (\sigma_{cost>10 \land cost<1337}Catalog) \bowtie Suppliers))
iv)
R1 := \sigma_{tagname = 'Cleaning'} Product Tag
R2 := \pi_{sid,pid}(R1 \bowtie Catalog)
R3 := \pi_{pid}(R1 \bowtie Catalog)
R4 := R2 \div R3
(or without \div)
R4 := \pi_{R1.sid, Suppliers.pid}(R2 \times Suppliers)
R5 := \rho_{R4(sid,pid)}(R4)
R6 := \pi_{sid}(R5 - R2)
R7 := \pi_{sid}(Suppliers) - R6
v)
R1 := \rho_{S1}(\rho_{(sid,cost)}(\pi_{Suppliers.sid,Catalog.cost}(Catalog \bowtie Product)))
R2 := \rho_{S2}(\rho_{(sid,cost)}(\pi_{Suppliers.sid,Catalog.cost}(Catalog \bowtie Product)))
R3 := \sigma_{S1.cost} > S_{2.cost \cdot 1.2}(\sigma_{S1.sid} != S_{2.sid}(R1 \times R1))
R4 := \rho_{(sid)}(\pi_{S1.sid}(R3))
vi)
R1 := \rho_{P1}(Catalog)
R2 := \rho_{P2}(Catalog)
R3 := P1 \times P2
R4 := \sigma_{(P1.pid=P2.pid)} \land (P1.sid!=P2.sid)(R3)
R5 := \rho_{(pid)}(\pi_{P1.pid}(R4))
vii)
R1 := \sigma_{tagname = 'SuperTech'}(ProductTag) \bowtie Suppliers
R2 := \rho_{R2(sid,cost)}(\sigma_{scountry='USA'}(R1))
R3 := \rho_{R3}(R2)
R4 := \rho_{R4(sid,cost)}(R2 \bowtie_{R2.cost < R3.cost} (R3))
R5 := R2 - R4
R6 := \pi_{sid}(R5)
R1 := \sigma_{tagname = 'SuperTech'}(ProductTag) \bowtie Suppliers
R2 := \rho_{R2(sid,cost)}(\sigma_{scountry='USA'}(R1))
R3 := \rho_{R3}(R2)
R4 := \rho_{R4(sid,cost)}(R2 \bowtie_{R2.cost < R3.cost} (R3))
R5 := R2 - R4 [Most Expensive]
R6 := R2 - R5 [Table excluding most expensive]
R7 := \rho_{R7(sid,cost)}(\sigma_{scountry='USA'}(R6))
R8 := \rho_{R8}(R7)
R9 := \rho_{R9(sid,cost)}(R7 \bowtie_{R7.cost < R8.cost} (R8))
R10 := R6 - R9
R11 := \pi_{sid}(R10)
R1 := \rho_{R1(pid,sid,cost)}(\pi_{Product.pid,Suppliers.sid}(Product \bowtie Catalog \bowtie Suppliers))
R2 := \pi_{pid}(R1)
R3 := R1 \div R2
R4 := \sigma_{cost < 69}(R3)
R5 := \pi_{sid}(R4)
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x) $\pi_{pid}(Product \bowtie \sigma_{quantity=0}(Inventory))$