

UNIVERSITÉ LIBRE DE BRUXELLES

DÉPARTEMENT D'INFORMATIQUE



INFO-F403 - INTRODUCTION TO LANGUAGE THEORY AND
COMPILING

Project Report – Part 2

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Contents

1	Grammar	2
1.1	Unproductive and unreachable symbols (a)	2
1.2	Priority and associativity of the operators (b)	2
1.2.1	Arithmetic expressions	2
1.2.2	Boolean expressions	3
1.3	Removing left recursion	4

1 Grammar

1.1 Unproductive and unreachable symbols (a)

In the given grammar, there is no unproductive and/or unreachable symbols.

1.2 Priority and associativity of the operators (b)

Note In this section, P&A refers to priority and associativity of the operators, AE to arithmetic expression and BE to boolean expression.

1.2.1 Arithmetic expressions

Since an arithmetic expression must always be process first before being compared to another one in a boolean expression, we will consider those two separately.

First let's consider the P&A of the arithmetic expressions. We have the following P&A:

-	right
*, /	left
+, -	left

And the following grammar:

$$\begin{aligned}
 \langle \text{ExprArith} \rangle &\rightarrow [\text{VarName}] \\
 \langle \text{ExprArith} \rangle &\rightarrow [\text{Number}] \\
 \langle \text{ExprArith} \rangle &\rightarrow (\langle \text{ExprArith} \rangle) \\
 \langle \text{ExprArith} \rangle &\rightarrow - \langle \text{ExprArith} \rangle \\
 \langle \text{ExprArith} \rangle &\rightarrow \langle \text{ExprArith} \rangle \langle \text{Op} \rangle \langle \text{ExprArith} \rangle \\
 \langle \text{Op} \rangle &\rightarrow + \\
 \langle \text{Op} \rangle &\rightarrow - \\
 \langle \text{Op} \rangle &\rightarrow * \\
 \langle \text{Op} \rangle &\rightarrow /
 \end{aligned}$$

As mention in the course page 111, an AE must be a *sum of products*, more specifically in our case a $\{sum, subtraction\}$ of $\{products, division\}$. We will use the same atom definition in the course, with **Number** as the constant rule and **VarName** as the id rule. The minus operator as a right associativity, meaning that it is always linked to the atom next to the operator, so we will set this operator directly as an atom rule.

Same thing goes for the parenthesis. The must be handled without considering the operators outside the parenthesis, so as an atom.

We have the following grammar results:

$$\begin{aligned}
 \langle \text{ExprArith} \rangle &\rightarrow \langle \text{ExprArith} \rangle \langle \text{SumSubOp} \rangle \langle \text{ExprProd} \rangle \\
 \langle \text{ExprArith} \rangle &\rightarrow \langle \text{ExprProd} \rangle \\
 \langle \text{ExprProd} \rangle &\rightarrow \langle \text{ExprProd} \rangle \langle \text{ProdOp} \rangle \langle \text{Atom} \rangle \\
 \langle \text{ExprProd} \rangle &\rightarrow \langle \text{Atom} \rangle \\
 \langle \text{SumSubOp} \rangle &\rightarrow +
 \end{aligned}$$

$$\langle \text{SumSubOp} \rangle \rightarrow -$$

$$\langle \text{ProdOp} \rangle \rightarrow *$$

$$\langle \text{ProdOp} \rangle \rightarrow /$$

$$\langle \text{Atom} \rangle \rightarrow [\text{VarName}]$$

$$\langle \text{Atom} \rangle \rightarrow [\text{Number}]$$

$$\langle \text{Atom} \rangle \rightarrow - \langle \text{Atom} \rangle$$

$$\langle \text{Atom} \rangle \rightarrow (\langle \text{ExprArith} \rangle)$$

1.2.2 Boolean expressions

For boolean expressions we have the following P&A:

not	right
>, <, >=, <=, =, <> /	left
and	left
or	left

And the following grammar:

$$\langle \text{Cond} \rangle \rightarrow \langle \text{Cond} \rangle \langle \text{BinOp} \rangle \langle \text{Cond} \rangle$$

$$\langle \text{Cond} \rangle \rightarrow \text{not } \langle \text{SimpleCond} \rangle$$

$$\langle \text{Cond} \rangle \rightarrow \langle \text{SimpleCond} \rangle$$

$$\langle \text{SimpleCond} \rangle \rightarrow \langle \text{ExprArith} \rangle \langle \text{Comp} \rangle \langle \text{ExprArith} \rangle$$

$$\langle \text{BinOp} \rangle \rightarrow \text{and}$$

$$\langle \text{BinOp} \rangle \rightarrow \text{or}$$

$$\langle \text{Comp} \rangle \rightarrow =$$

$$\langle \text{Comp} \rangle \rightarrow >=$$

$$\langle \text{Comp} \rangle \rightarrow >$$

$$\langle \text{Comp} \rangle \rightarrow <=$$

$$\langle \text{Comp} \rangle \rightarrow <$$

$$\langle \text{Comp} \rangle \rightarrow \diamond$$

Following the same principle as for AE, we have here *disjonction of conjunctions of comparaisons*. By using the same mechanics as above, we have this grammar:

$$\langle \text{Cond} \rangle \rightarrow \langle \text{Cond} \rangle \text{ or } \langle \text{ConjCond} \rangle$$

$$\langle \text{Cond} \rangle \rightarrow \langle \text{ConjCond} \rangle$$

$$\langle \text{ConjCond} \rangle \rightarrow \langle \text{ConjCond} \rangle \text{ and } \langle \text{AtomCond} \rangle$$

$$\langle \text{ConjCond} \rangle \rightarrow \langle \text{AtomCond} \rangle$$

$$\langle \text{AtomCond} \rangle \rightarrow \langle \text{SimpleCond} \rangle$$

$$\langle \text{AtomCond} \rangle \rightarrow \text{not } \langle \text{SimpleCond} \rangle$$

$$\langle \text{SimpleCond} \rangle \rightarrow \langle \text{ExprArith} \rangle \langle \text{Comp} \rangle \langle \text{ExprArith} \rangle$$

$$\langle \text{Comp} \rangle \rightarrow =$$

$$\langle \text{Comp} \rangle \rightarrow >=$$

$\langle Comp \rangle \rightarrow >$
 $\langle Comp \rangle \rightarrow <=$
 $\langle Comp \rangle \rightarrow <$
 $\langle Comp \rangle \rightarrow \diamond$

1.3 Removing left recursion

For the new AE:

$\langle ExprArith \rangle \rightarrow \langle ExprProd \rangle \langle ExprArithPrime \rangle$
 $\langle ExprArithPrime \rangle \rightarrow \langle SumSubOp \rangle \langle ExprProd \rangle \langle ExprArithPrime \rangle$
 $\langle ExprArithPrime \rangle \rightarrow \backslash \epsilon$

$\langle ExprProd \rangle \rightarrow \langle Atom \rangle \langle ExprProdPrime \rangle$
 $\langle ExprProdPrime \rangle \rightarrow \langle ProdOp \rangle \langle Atom \rangle \langle ExprProdPrime \rangle$
 $\langle ExprProdPrime \rangle \rightarrow \backslash \epsilon$

$\langle SumSubOp \rangle \rightarrow +$
 $\langle SumSubOp \rangle \rightarrow -$

$\langle ProdOp \rangle \rightarrow *$
 $\langle ProdOp \rangle \rightarrow /$

$\langle Atom \rangle \rightarrow [VarName]$
 $\langle Atom \rangle \rightarrow [Number]$

$\langle ExprArith \rangle \rightarrow - \langle Atom \rangle$
 $\langle ExprArith \rangle \rightarrow (\langle ExprArith \rangle)$

For the new BE:

$\langle Cond \rangle \rightarrow \langle ConjCond \rangle \langle CondPrime \rangle$

$\langle CondPrime \rangle \rightarrow or \langle ConjCond \rangle \langle CondPrime \rangle$
 $\langle CondPrime \rangle \rightarrow \backslash \epsilon$

$\langle ConjCond \rangle \rightarrow \langle AtomCond \rangle \langle ConjCondPrime \rangle$

$\langle ConjCondPrime \rangle \rightarrow and \langle AtomCond \rangle \langle ConjCondPrime \rangle$
 $\langle ConjCondPrime \rangle \rightarrow \backslash \epsilon$

$$\langle AtomCond \rangle \rightarrow \langle SimpleCond \rangle$$
$$\langle AtomCond \rangle \rightarrow not \langle SimpleCond \rangle$$
$$\langle SimpleCond \rangle \rightarrow \langle ExprArith \rangle \langle Comp \rangle \langle ExprArith \rangle$$
$$\langle Comp \rangle \rightarrow =$$
$$\langle Comp \rangle \rightarrow >=$$
$$\langle Comp \rangle \rightarrow >$$
$$\langle Comp \rangle \rightarrow <=$$
$$\langle Comp \rangle \rightarrow <$$
$$\langle Comp \rangle \rightarrow \diamond$$