

Computability and Complexity: \neq SAT

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Proof Idea

To prove that \neq SAT is NP-complete we have to prove that a NP problem is reducible in polynomial time to \neq SAT.

a ou b ou c

f, f, f is not valid because it doesn't satisfy

List:

* Look at the bookmarks * Prove NP-Complete: Prove that it is 3SAT by adding more formulas confirming the !=assign

Proof

Hint proof

If we have a diffassign that satisfies the formula, it means that in each clause there is either two true with a false two false with a true. By taking the negation it will just convert the 2t1f to a 1t2f and the 2f1t to 1f2t which also satisfy the formula.

To prove that it is NP-complete we have to prove that all NP problems are reducible in P time to diffSAT. Since 3SAT is NP-complete, by reducing it to diffSAT it will prove that diffSAT is NP-Complete.

Note about the hint: the idea is to convert each clause into diffSAT. Since we know that if a diffassign satisfies a clause, it will also satisfy the neg of the clause.

3SAT clause: $c = (x \vee y \vee z)$

The idea is if $(x \vee y \vee z)$ is true, i.e. an assignment satisfies the formula, we must find a 3cnf-formula that is true also but never contains three true in any clauses.

Actually when converting we must find a formula that if c is sat, then there exists a diffassign that satisfies the new formula.

1 1 1 1 1 0 1 0 1 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0

if $c = T$

$(c \wedge x \wedge y) \wedge (\neg c \wedge z \wedge F)$