

Q4. Saying Random is not enough

4.1

1. *random_theta()*: The function finds random θ_1 and θ_2 . θ is chosen randomly from degrees(ϕ) and then converted to radians.

$$\theta_1 = \phi_1 \cdot \frac{\pi}{180}$$
$$\theta_2 = \phi_2 \cdot \frac{\pi}{180}$$

2. *cord(R)*: The function takes the radius as the input and returns length of the cord between θ_1 and θ_2 . It first calls *random_theta()*, and find the absolute value of their difference ($\theta = |\theta_1 - \theta_2|$). Then the length of the cord is calculated using the following formula,

$$\text{cord length} = 2R \cdot \sin(\theta/2)$$

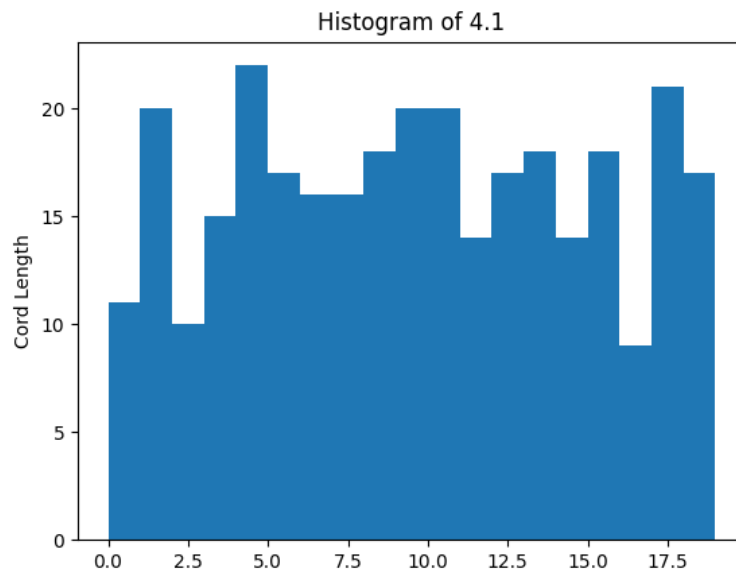
3. *find_cords1(R)*: The function takes radius R as input, then draw the histogram as the output. It iterates 1000 times, calls *cord(R)* for each iteration and append the result in *cord_len*. Then we calculate the value of appropriate bins for the histogram, and then plot it using matplotlib.

```
1
2
3 def find_bins(n, val_range):
4     interval = m.sqrt(n)
5     width_interval = val_range/interval
6     return width_interval
7
8 # 4.1
9 -----
10
11 def random_theta():
12     theta1 = np.random.uniform(0,360)*(m.pi/180)    #random theta 1
13     theta2 = np.random.uniform(0,360)*(m.pi/180)    #random theta 2
14     return (theta1,theta2)
15
16 def cord(R):
17     angle = random_theta()
18     theta = abs(angle[0] - angle[1])    #theta between the two radius(theta1 and theta2)
19     l = 2*R*m.sin(theta/2)    #length of cord = 2rsin(theta/2)
20     return(l)
21
22 def find_cords1(R):
23     cord_len = []
24     I = 100    #iterations
25
26     for _ in range(I):
27         cord_len.append(cord(R))
```

4.2

```
1 #Finding bins
2 rng = max(cord_len) - min(cord_len)
3 width = int(find_bins(I, rng))
4
5 #bin val list
6 bin_lst = [x*width for x in range(int(m.sqrt(I)))]
7 print(len(cord_len))
8
9 arr=plt.hist(cord_len, bins = bin_lst)
10 for i in range(int(m.sqrt(I))-1):
11     plt.text(arr[1][i],arr[0][i],str(arr[0][i]))
12 plt.title("Histogram of 4.1")
```

Figure 1: Histogram of 4.1



```

13 plt.ylabel("Cord Length")
14 plt.xlabel("bins")
15 #plt.savefig("Q4/Q4(1).png")
16 plt.show()
17
18 # 4.2
-----
19 def random_cord(R):
20
21     theta = np.random.uniform(0,360)*(m.pi/180)
22     point_at_radius = np.random.uniform(0,R)    #point at R
23
24     #cartesian coordinates at the picked point
25     x = point_at_radius*m.cos(theta)
26     y = point_at_radius*m.sin(theta)
27
28     #finding base line from center to point_at_radius using distance formula
29     base = m.sqrt(x**2+y**2)
30
31     #perpendicular using pythagorean theorem, p = sqrt(h^2-b^2)
32     perp = m.sqrt(R**2-base**2)
33
34     #length of the cord
35     l = 2*perp

```

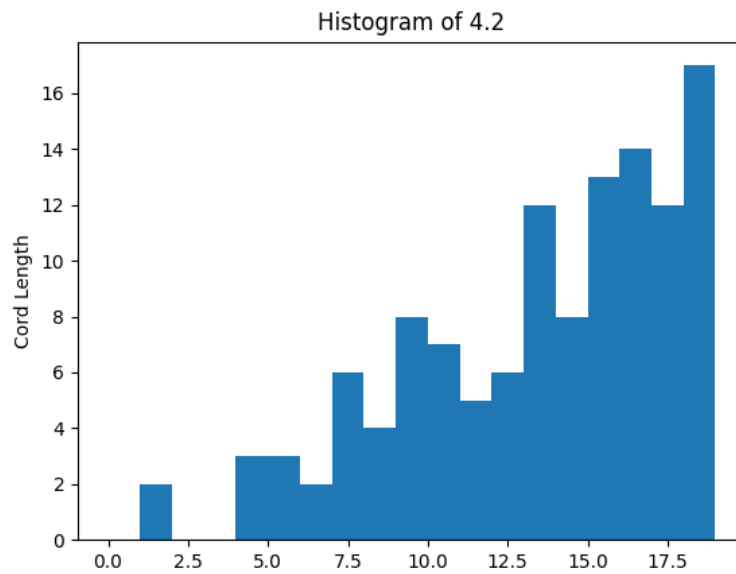
4.3

```

1     return l
2
3
4 def find_cords2(R):
5
6     cord_len = []
7     I = 1000    #iterations
8
9     for _ in range(I):
10         cord_len.append(random_cord(R))
11
12     plt.hist(cord_len, bins = range(0,R))
13     plt.title("Histogram of 4.2")
14     plt.ylabel("Cord Length")
15     plt.savefig("Q4/Q4(2).png")
16     plt.show()

```

Figure 2: Histogram of 4.2



```
17
18 # 4.3
19
20 def p_to_o(cord):
21     return m.sqrt(cord[0]**2+cord[1]**2)
22
23 def random_point(R):
24
25     x = np.random.uniform(-R,R) #random point x
26     y = np.random.uniform(-R,R) #random point y
27
28     return (x,y)
29
30 def cal_cord(R,pnt):
31     #finding adjacent from the random point.
32     adj = p_to_o(pnt)
33
34     #length of opposite
35     opp = m.sqrt(R**2-adj**2)
36
37     #length of the cord
38     l = 2*opp
39
40     return l
```

Figure 3: Histogram of 4.3

