

PowerFactory 2021

Technical Reference

Common Result Variables for Terminals and Elements

Load Flow Calculation

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1 General Description

This document describes the common variables available for monitoring in *PowerFactory* for the terminals and for the single- and multiple-port elements (primary equipment). These are the parameters that can be selected to be displayed in the result boxes and in the flexible data page of the elements, which are not specific to a certain element.

Variables starting with capital letters are expressed in absolute values and variables starting with a lower case letters are expressed in per unit values.

1.1 Terminals

For the terminals ($\mathit{ElmTerm}$) only the set $\mathit{Currents}$, $\mathit{Voltages}$ and Powers displays common result variables that can be monitored after a calculation. The identification name of a result variable contains the letter m to denominate that it is a common monitoring variable (in opposite to c which stands for calculation variable), a semicolon and the name of the variable. For example, the result variable $\mathit{Voltage}$, $\mathit{Magnitude}$ has the following identification name m:u.

For the unbalanced representation, the phase result variables get a slightly different identification name where the name of the phase is added. For example: m:u:A.

1.2 Elements (single and multiple port)

For the single- and multiple-port elements (ex.: *ElmSym*, *ElmLne*, *ElmTr3*, etc.), there are two sets containing common result variables that can be monitored after a calculation:

- · Currents, Voltages and Powers
- · Bus Results

1.2.1 Currents, Voltages and Powers

The identification name of the variables available in this set is similar to the one used for the terminals with the difference that for the elements also the connection point name is added.

For example $m:i1:_LOCALBUS$ is the magnitude of the positive-sequence current of the connected element. If the result variable is shown for a certain type of an element, the real connection point name is used. For example m:i1:bushv is the magnitude of the positive-sequence current flowing through the HV connection of a transformer and m:i1:busi is the magnitude of the positive-sequence current flowing through the connection `busi' of a line.

For the unbalanced representation, the phase result variables get a slightly different identification name where the name of the phase is added. For example: m:i1:LOCALBUS:A, m:i1:bushv:A, m:I:bus1:A.

The result variables available for the elements in p.u. values are based on the element (not on the terminal). Due to this, the same variable for a port element and a terminal may have a different value. For example, if the nominal voltage of an element differs from the nominal voltage of a terminal, the positive sequence voltage magnitude m:u will have a different value compared to m:u of a terminal.

1.2.2 Bus Results

The result variables available in the *Bus Results* set for the terminals are actually the variables from the connected terminal i.e. they are the same as the variables available in the *Currents*, *Voltages and Powers* set from the terminals.

There are two differences regarding the identification name:

- the letter 'n' is used to denominate that this is a node (terminal) variable
- the connection-point name is also used

The result variables in p.u. values from this set are based on the terminal. Please note that if for example for a certain element n:u1:bus1 and m:u1:bus1 are displayed, the result will be different if the nominal voltage of the element differs from the nominal voltage of the terminal.

2 Balanced Load Flow calculation

The balanced load flow calculations uses positive sequence network representation which is valid for balanced symmetrical networks. The resulting quantities are positive sequence quantities.

For DC terminals and elements, the variables displaying imaginary values are zero.

2.1 Result variables for terminals

As described in Section 1.2.2, the result variables from the *Bus Results* set from the port elements are equivalent to the result variables from the *Currents, Voltages and Currents* set for the terminals.

The result variables available for terminals after a balanced Load Flow calculation are presented in the following sub chapters.

2.1.1 Voltage related variables for terminals

The voltage related variables for the terminals are all based on the positive-sequence, phase to ground complex voltage \underline{u} resulting from the balanced load flow. The relationship between the absolute and per unit value voltage is $\underline{U} = \underline{u} \cdot U_{base}$ where the base voltage is $U_{base} = uknom/\sqrt{3}$ where uknom is the nominal line to line voltage of the terminal.

Description Name Unit Positive-Sequence Voltage, Magnitude u1p.u.Positive-Sequence Voltage, Real-Part u1rp.u.Positive-Sequence Voltage, Imaginary-Part u1ip.u.Voltage, Magnitude up.u.Voltage, Real Part urp.u.Voltage, Imaginary Part uip.u.UkVLine-Ground Voltage, Magnitude UlkVLine-Line Voltage, Magnitude Voltage, Angle phiudegphiurelVoltage, Relative Angle degVoltage, Magnitude % u1pc% Voltage, Magnitude upc

Voltage Deviation

Table 2.1: Voltage related variables for terminals

The result variables from Table 2.1 are calculated as follows:

%

du

• u1 is obtained as the magnitude of the complex voltage \underline{u} as:

$$u1 = \sqrt{\underline{u}.r^2 + \underline{u}.i^2}$$

• u1r is obtained from the complex voltage \underline{u} as:

$$u1r = \underline{u}.r$$

• u1i is obtained from the complex voltage \underline{u} as:

$$u1i = \underline{u}.i$$

• *u* is equal to the positive sequence voltage magnitude:

$$u = u1$$

• ur is obtained as:

$$ur = u1r$$

ui is obtained as:

$$ui = u1i$$

• U is obtained as:

$$U=u\cdot uknom/\sqrt{3}$$

where uknom is the nominal voltage of the terminal.

• *Ul* is obtained as:

$$Ul = u \cdot uknom$$

• phiu is obtained from the complex voltage \underline{u} as:

$$phiu = \arctan\left(\frac{\underline{u}.i}{\underline{u}.r}\right) \cdot \frac{180}{\pi}$$

• phiurel is obtained using the Initial Angle of Bus Voltage phiini basic data parameter as:

$$phiurel = phiu - phiini \cdot \frac{180}{\pi}$$

• u1pc is obtained as:

$$u1pc = u \cdot 100$$

upc is obtained as:

$$upc = u \cdot 100$$

• du is obtained as:

$$du = upc - 100$$

2.1.2 Aggregated power variables for terminals

Table 2.2: Aggregated power variables for terminals

Name	Unit	Description
Pgen	MW	Generation, Active Power
Qgen	Mvar	Generation, Reactive Power
Pmot	MW	Motor Load, Active Power
Qmot	Mvar	Motor Load, Reactive Power
Pload	MW	General Load, Active Power
Qload	Mvar	General Load, Reactive Power
Pcomp	MW	Compensation (Losses)
Qcomp	Mvar	Compensation
Pnet	MW	External Networks, Active Power
Qnet	Mvar	External Networks, Reactive Power
Pflow	MW	Power Flow, Active Power
Qflow	Mvar	Power Flow, Reactive Power
Pout	MW	Outgoing Flow, Active Power
Qout	Mvar	Outgoing Power, Reactive Power
Sout	MVA	Outgoing Power, Apparent Power
cosphiout		Outgoing Power, Power Factor
Pbalance	MW	Active Power Balance (=0)
Qbalance	Mvar	Reactive Power Balance (=0)

The result variables from Table 2.2 are calculated as follows:

- Pgen is the active power sum of all synchronous, asynchronous and static generators connected to the terminal. If generation is defined in the MV Load (ElmLodmv), the generated active power is also added to this sum.
- *Qgen* is the reactive power sum of all synchronous, asynchronous and static generators connected to the terminal. If generation is defined in the MV Load (*ElmLodmv*), the generated reactive power is added to this sum.
- *Pmot* is the active power sum of all synchronous and asynchronous motors connected to the terminal.
- Qmot is the reactive power sum of all synchronous and asynchronous motors connected to the terminal.
- Pload is the active power sum of all loads connected to the terminal.
- Qload is the reactive power sum of all loads connected to the terminal.
- *Pcomp* is the active power sum of all shunts and filters connected to the terminal.
- Qcomp is the reactive power sum of all shunts and filters connected to the terminal.
- Pnet is the active power sum of all external network elements connected to the terminal.
- *Qnet* is the reactive power sum of all external network elements connected to the terminal.
- *Pflow* is the sum of all active power flowing out of the terminal.
- *Qflow* is the sum of all reactive power flowing out of the terminal.
- *Pout* is the sum of all active power flowing out of the terminal.

- Qout is the sum of reactive powers of all elements whose active power is flowing out of the terminal ($\sum Q$ if P > 0).
- Sout is calculated as:

$$Sout = \sqrt{Pout^2 + Qout^2}$$

cosphiout is obtained as:

$$cosphiout = \arctan\left(\frac{Qout}{Pout}\right)$$

- *Pbalance* is the sum of all active power at the terminal. This sum is always zero or near zero and is dependent on the maximum acceptable load flow error setting.
- *Qbalance* is the sum of all reactive power at the terminal. This sum is always zero or near zero and is dependent on the maximum acceptable load flow error setting.

2.1.3 Low-voltage analysis related variables for terminals

Table 2.3: Low-voltage analysis related variables for terminals

Name	Unit	Description
umin	p.u.	Minimum Voltage
Umin	kV	Minimum Voltage (Line to Neutral)
dumax	%	Maximum Voltage Drop along Feeder
dUmax	kV	Maximum Voltage Drop along Feeder
dUlmax	kV	Maximum Voltage Drop along Feeder (Line-Line)
Ulmin	kV	Minimum Voltage (Line to Line)

The result variables from Table 2.3 are calculated from a low-voltage load flow analysis where coincidence of low-voltage loads is considered.

2.1.4 Feeder losses variables for terminals

Table 2.4: Load flow, balanced, feeder losses variables (terminals)

Name	Unit	Description
LossPdown	MW	Losses, downstream
LossQdown	Mvar	Losses, downstream (Reactive Power)
LossPdownload	MW	Load losses, downstream
LossQdownload	Mvar	Load losses, downstream
LossPdownnoload	MW	No load losses, downstream
Loss Q down no load	Mvar	No load losses, downstream
$du_{-}feed$	%	Voltage difference relative to feeder begin

The result variables from Table 2.4 are calculated as follows:

 LossPdown is the sum of active power load and no-load losses of all elements downward the feeder.

- LossQdown is the sum of reactive power load and no-load losses of all elements downward the feeder.
- LossPdownload is the sum of active power load losses of all elements downward the feeder
- LossQdownload is the sum of reactive power load losses of all elements downward the feeder.
- LossPdownnoload is the sum of active power no-load losses of all elements downward the feeder.
- LossQdownnoload is the sum of reactive power no-load losses of all elements downward the feeder.
- du_-feed is obtained using the magnitude of the voltage where the feeder is defined u_{feeder} and the local positive sequence voltage magnitude:

$$du$$
- $feed = (u_{feeder} - u) \cdot 100$

2.2 Result variables for elements

The result variables available for single- and multiple-port elements after a balanced Load Flow calculation are presented in the following sub chapters.

2.2.1 Voltage related variables for elements

Similar as for the voltage related variables for the terminals, these variables are calculated from the same positive-sequence, phase to ground complex voltage \underline{u} resulting from the balanced load flow.

For the element based variables, the relationship between the absolute and per unit value voltage is $\underline{U} = \underline{u} \cdot U_{base}$ where the base voltage is $U_{base} = U_{nom_el}/\sqrt{3}$ where U_{nom_el} is the nominal line to line voltage of the element. Due to the change in base, the per unit values are multiplied with the factor $uknom/U_{nom_el}$.

Name Unit Description Positive-Sequence-Voltage, Magnitude u1p.u.Positive-Sequence Voltage, Real-Part u1rp.u.Positive-Sequence Voltage, Imaginary-Part u1ip.u.phiu1Positive-Sequence-Voltage, Angle degVoltage, Magnitude p.u.Voltage, Real Part urp.u.Voltage, Imaginary Part uip.u.Line-Ground Positive-Sequence-Voltage, Magnitude U1kVkVLine-Line Positive-Sequence-Voltage, Magnitude U1l

Table 2.5: Voltage related variables for elements

The result variables from Table 2.5 are calculated as follows:

• u1 is obtained from the complex voltage \underline{u} as:

$$u1 = \sqrt{\underline{u}.r^2 + \underline{u}.i^2} \cdot \frac{uknom}{U_{nom_el}}$$

where uknom is the nominal voltage of the connected terminal and U_{nom_el} is the nominal voltage of the element.

• u1r is obtained from the complex voltage \underline{u} as:

$$u1r = \underline{u}.r \cdot \frac{uknom}{U_{nom_el}}$$

• *u*1*i* is obtained from the complex voltage *u* as:

$$u1i = \underline{u}.i \cdot \frac{uknom}{U_{nom_el}}$$

• $\mathit{phiu}1$ is obtained from the complex voltage \underline{u} as:

$$phiu = \arctan\left(\frac{\underline{u}.i}{\underline{u}.r}\right) \cdot \frac{180}{\pi}$$

• phiurel is obtained using the Initial Angle of Bus Voltage phiini basic data parameter as:

$$phiurel = phiu - phiini \cdot \frac{180}{\pi}$$

• u is equal to the positive sequence voltage magnitude:

$$u = u1$$

• ur is obtained as:

$$ur = u1r$$

· ui is obtained as:

$$ui = u1i$$

• U1 is obtained as:

$$U1 = u \cdot U_{nom_el} / \sqrt{3}$$

• U1l is obtained as:

$$U1l = u \cdot U_{nom_el}$$

2.2.2 Current related variables for elements

The current related variables for the elements are all based on the positive-sequence complex current resulting from the balanced load flow. The relationship between the absolute and per unit value current is $\underline{I} = \underline{i} \cdot I_{nom_el}$ where $I_{nom_el} = \frac{MVA_{el}}{\sqrt{3} \cdot U_{nom_el}}$ is the nominal current of the element.

Table 2.6: Current related variables for elements

Name	Unit	Description
I1	kA	Positive-Sequence Current, Magnitude
phii1	deg	Positive-Sequence Current, Angle
I	kA	Current, Magnitude
phii	deg	Current, Angle
i1	p.u.	Positive-Sequence Current, Magnitude
i1r	p.u.	Positive-Sequence Current, Real Part
i1i	p.u.	Positive-Sequence Current, Imaginary Part
i	p.u.	Current, Magnitude
ir	p.u.	Current, Real Part
ii	p.u.	Current, Imaginary Part
i1P	p.u.	Positive-Sequence Active Current
i1Q	p.u.	Positive-Sequence Reactive Current
I1P	kA	Positive-Sequence Active Current
I1Q	kA	Positive-Sequence Reactive Current
phiui	deg	Angle between Voltage and Current
phiu1i1	deg	Angle between Voltage and Current in positive sequence system
inet	p.u.	Current, Magnitude, referred to network

The result variables from Table 2.6 are calculated as follows:

• *I*1 is obtained as the amplitude of the complex current *I*:

$$I1 = \sqrt{\underline{I}.r^2 + \underline{I}.i^2}$$

- $\mathit{phii1}$ is obtained from the complex voltage \underline{i}_{net} as:

$$phii1 = \arctan\left(\frac{\underline{I}.i}{I.r}\right) \cdot \frac{180}{\pi}$$

• *I* is equivalent to the positive sequence current magnitude:

$$I = I1$$

phii is obtained as:

$$phii = phii1$$

• i1 is obtained as:

$$i1 = \frac{I}{I_{nom_el}}$$

where I_{nom_el} is the nominal current of the element.

• i1r is obtained as:

$$i1r = \frac{\underline{I}.r}{I_{nom_el}}$$

• *i*1*i* is obtained as:

$$i1i = \frac{\underline{I}.i}{I_{nom_el}}$$

• i is obtained as:

$$i = i1$$

• ir is obtained as:

$$ir = i1r$$

• ii is obtained as:

$$ii = i1i$$

• *i*1*P* is obtained as:

$$i1P = i1 \cdot cosphi$$

where cosphi is the power factor of the element.

• i1Q is obtained as:

$$i1Q = i1 \cdot \sin(\phi)$$

where ϕ is the angle between the active and reactive power and can be also obtained as: $\phi = \arccos(cosphi)$.

• I1P is obtained as:

$$I1P = I1 \cdot cosphi$$

where cosphi is the power factor of the element.

• *I*1*Q* is obtained as:

$$I1Q = I1 \cdot \sin(\phi)$$

where ϕ is the angle between the active and reactive power and can be also obtained as: $\phi = \arccos(cosphi)$.

phiui is obtained as:

$$phiui=phiu-phii\\$$

• phiu1i1 is obtained as:

$$phiu1i1 = phiu1 - phii1$$

• *inet* is obtained as:

$$inet = \frac{I}{I_{nom_1MVA}}$$

where $I_{nom_1MVA}=\frac{1}{\sqrt{3}\cdot uknom}$ is the nominal current for 1MVA and uknom is the nominal voltage of the connected terminal.

2.2.3 Power related variables for elements

The apparent power is calculated as $\underline{S}=3\cdot\underline{U}_1\cdot\underline{I}^*$ where \underline{U}_1 is the positive sequence voltage.

Table 2.7: Power related variables for elements

Name	Unit	Description
S	MVA	Apparent Power
P	MW	Active Power
Q	Mvar	Reactive Power
cosphi		Power Factor
tanphi		tan(phi)
Psum	MW	Total Active Power
Qsum	Mvar	Total Reactive Power
Ssum	MVA	Total Apparent Power
cosphisum		Total Power Factor
tanphisum		Total tan(phi)
Spu	MVA/p.u.	Apparent Power per p.u. Voltage

The result variables from Table 2.7 are calculated as follows:

• S is obtained as the magnitude of the apparent power:

$$S=\sqrt{\underline{S}.r^2+\underline{S}.i^2}$$

• *P* is obtained as:

$$P = \underline{S}.r$$

• Q is obtained as:

$$Q = \underline{S}.i$$

cosphi is obtained as:

$$cosphi = cos\left(\arctan\left(\frac{Q}{P}\right)\right) = \frac{P}{S}$$

• tanphi is obtained as:

$$tanphi = \frac{Q}{P}$$

• *Psum* is equal to the magnitude of the active power:

$$Psum = P$$

• *Qsum* is equal to the magnitude of the reactive power:

$$Qsum = Q$$

• Ssum is equal to the magnitude of the apparent power:

$$Ssum = S$$

• cosphisum is obtained as:

$$cosphisum = cosphi$$

• tanphisum is obtained as:

$$tanphisum = tanphi$$

• Spu is obtained as:

$$Spu = \sqrt{3} \cdot uknom \cdot I$$

2.2.4 Miscellaneous variables for elements

Table 2.8: Miscellaneous variables for elements

Name	Unit	Description
Tfct	s	Fault Clearing Time
Brkload	%	Breaker Loading
Imax	kA	Maximum Current
Smax	MVA	Maximum Power

The result variables from Table 2.8 are calculated as follows:

- Tfct gives the fault clearing time of a fuse or a relay located in the local cubicle. If the fuse/relay model is not triggered with the Load Flow current, a default value of 9999,999s is used.
- Brkload is obtained as:

$$Brkload = \frac{I}{BrkInom} \cdot 100$$

where BrkInom is the rated current of a switch (input parameter Inom in TypSwitch).

- *Imax* is the maximum current from low-voltage load flow analysis (coincidence of low-voltage loads is considered).
- *Smax* is obtained as:

$$Smax = \sqrt{3} \cdot uknom \cdot Imax$$

3 Unbalanced Load Flow calculation

The balanced load flow calculations uses multi-phase network representation which is valid for unbalanced networks. The resulting quantities are phase quantities.

For DC terminals and elements, the variables displaying imaginary values are zero.

3.1 Result variables for terminals

As described in Section 1.2.2, the result variables from the *Bus Results* set from the port elements are equivalent to the result variables from the *Currents, Voltages and Currents* set for the terminals.

The result variables available for terminals after an unbalanced Load Flow calculation are presented in the following sub chapters.

3.1.1 Phase voltage related variables for terminals

The voltage related variables for the terminals are all based on the phase to ground complex voltages \underline{u}_A , \underline{u}_B and \underline{u}_C resulting from the unbalanced load flow. The relationship between the absolute and per unit value voltage is $\underline{U}_A = \underline{u}_A \cdot U_{base}$ where the base voltage is $U_{base} = uknom/\sqrt{3}$ where uknom is the nominal line to line voltage of the terminal.

Name	Unit	Description
ur:A	p.u.	Line-Ground Voltage, Real Part
ur:B	p.u.	Line-Ground Voltage, Real Part
ur:C	p.u.	Line-Ground Voltage, Real Part
ui:A	p.u.	Line-Ground Voltage, Real Part
ui:B	p.u.	Line-Ground Voltage, Real Part
ui:C	p.u.	Line-Ground Voltage, Real Part
u:A	p.u.	Line-Ground Voltage, Magnitude
u:B	p.u.	Line-Ground Voltage, Magnitude
u:C	p.u.	Line-Ground Voltage, Magnitude
upc:A	%	Line-Ground Voltage, Magnitude
upc:B	%	Line-Ground Voltage, Magnitude
upc:C	%	Line-Ground Voltage, Magnitude
U:A	kV	Line-Ground Voltage, Magnitude
U:B	kV	Line-Ground Voltage, Magnitude
U:C	kV	Line-Ground Voltage, Magnitude
phiu:A	deg	Line-Ground Voltage, Angle
phiu:B	deg	Line-Ground Voltage, Angle
phiu:C	deg	Line-Ground Voltage, Angle

Table 3.1: Phase voltage related variables for terminals

The result variables from Table 3.1 are calculated as follows:

• ur:A, ur:B, ur:C are the real part quantities of the resulting complex line to ground volt-

ages:

$$ur:A = \underline{u}_A.r$$

 $ur:B = \underline{u}_B.r$
 $ur:C = \underline{u}_C.r$

• ui:A, ui:B, ui:C are the imaginary part quantities of the resulting complex line to ground voltages:

$$\begin{aligned} ui:&A=\underline{u}_{A}.i\\ ui:&B=\underline{u}_{B}.i\\ ui:&C=\underline{u}_{C}.i \end{aligned}$$

• u:A, u:B, u:C are the magnitudes of the resulting line-ground voltages:

$$\begin{aligned} u : & A = \sqrt{ur : A^2 + ui : A^2} \\ u : & B = \sqrt{ur : B^2 + ui : B^2} \\ u : & C = \sqrt{ur : C^2 + ui : C^2} \end{aligned}$$

• upc:A, upc:B, upc:C are obtained as:

$$upc:A = u:A \cdot 100$$

 $upc:B = u:B \cdot 100$
 $upc:C = u:C \cdot 100$

• U:A, U:B, U:C are obtained as: for AC terminals (120°):

$$U:A = u:A \cdot uknom/\sqrt{3}$$

$$U:B = u:B \cdot uknom/\sqrt{3}$$

$$U:C = u:C \cdot uknom/\sqrt{3}$$

for AC/BI terminals (180°):

$$U:A = u:A \cdot uknom/2$$

 $U:B = u:B \cdot uknom/2$
 $U:C = u:C \cdot uknom/2$

where uknom is the nominal voltage of the terminal.

• phiu:A, phiu:B, phiu:C are obtained as:

$$\begin{aligned} phiu:A &= \arctan\left(\frac{ui:A}{ur:A}\right) \cdot \frac{180}{\pi} \\ phiu:B &= \arctan\left(\frac{ui:B}{ur:B}\right) \cdot \frac{180}{\pi} \\ phiu:C &= \arctan\left(\frac{ui:C}{ur:C}\right) \cdot \frac{180}{\pi} \end{aligned}$$

3.1.2 Line to line voltage related variables for terminals

The line to line voltages are calculated as the difference between the two phases:

for AC terminals (120°):

$$\underline{u}_{lA} = (\underline{u}_A - \underline{u}_B) / \sqrt{3}$$

$$\underline{u}_{lB} = (\underline{u}_B - \underline{u}_C) / \sqrt{3}$$

$$\underline{u}_{lC} = (\underline{u}_C - \underline{u}_A) / \sqrt{3}$$

for AC/BI terminals (180°):

$$\underline{u}_{lA} = (\underline{u}_A - \underline{u}_B) / 2$$

$$\underline{u}_{lB} = (\underline{u}_B - \underline{u}_C) / 2$$

$$\underline{u}_{lC} = (\underline{u}_C - \underline{u}_A) / 2$$

For a system containing two phases only the corresponding voltage phase difference is available $(\underline{u}_{lA} \text{ or } \underline{u}_{lB} \text{ or } \underline{u}_{lC})$.

For single phase systems, the line to line voltages are not available (cannot be calculated).

Table 3.2: Line to line voltage related variables for terminals

Name	Unit	Description
ul:A	p.u.	Line to Line Voltage, Magnitude
ul:B	p.u.	Line to Line Voltage, Magnitude
ul:C	p.u.	Line to Line Voltage, Magnitude
ulpc:A	%	Line to Line Voltage, Magnitude
ulpc:B	%	Line to Line Voltage, Magnitude
ulpc:C	%	Line to Line Voltage, Magnitude
Ul:A	kV	Line to Line Voltage, Magnitude
Ul:B	kV	Line to Line Voltage, Magnitude
Ul:C	kV	Line to Line Voltage, Magnitude
phiul:A	deg	Line to Line Voltage, Angle
phiul:B	deg	Line to Line Voltage, Angle
phiul:C	deg	Line to Line Voltage, Angle

The result variables from Table 3.2 are calculated as follows:

• *ul:A*, *ul:B*, *ul:C* are the magnitudes of the line to line voltages:

$$ul:A = \sqrt{\underline{u}_{lA} \cdot r^2 + \underline{u}_{lA} \cdot i^2}$$

$$ul:B = \sqrt{\underline{u}_{lB} \cdot r^2 + \underline{u}_{lB} \cdot i^2}$$

$$ul:C = \sqrt{\underline{u}_{lC} \cdot r^2 + \underline{u}_{lC} \cdot i^2}$$

• *ulpc:A*, *ulpc:B*, *ulpc:C* are obtained as:

$$ulpc:A = ul:A \cdot 100$$

 $ulpc:B = ul:B \cdot 100$
 $ulpc:C = ul:C \cdot 100$

• *Ul:A*, *Ul:B*, *Ul:C* are obtained as:

$$Ul:A = ul:A \cdot uknom$$

 $Ul:B = ul:B \cdot uknom$
 $Ul:C = ul:C \cdot uknom$

where uknom is the nominal voltage of the terminal.

• phiul:A, phiul:B, phiul:C are obtained as:

$$\begin{split} phiul: & A = \arctan\left(\frac{\underline{u}_{lA}.i}{\underline{u}_{lA}.r}\right) \cdot \frac{180}{\pi} \\ phiul: & B = \arctan\left(\frac{\underline{u}_{lB}.i}{\underline{u}_{lB}.r}\right) \cdot \frac{180}{\pi} \\ phiul: & C = \arctan\left(\frac{\underline{u}_{lC}.i}{\underline{u}_{lC}.r}\right) \cdot \frac{180}{\pi} \end{split}$$

3.1.3 Line to neutral voltage related variables for terminals

The line to neutral voltages are calculated as the difference between the phase and neutral complex voltages:

$$\underline{u}_{lnA} = \underline{u}_A - \underline{u}_n$$

$$\underline{u}_{lnB} = \underline{u}_B - \underline{u}_n$$

$$\underline{u}_{lnC} = \underline{u}_C - \underline{u}_n$$

Table 3.3: Line to neutral voltage related variables for terminals

Name	Unit	Description
uln:A	p.u.	Line-Neutral Voltage, Magnitude
uln:B	p.u.	Line-Neutral Voltage, Magnitude
uln:C	p.u.	Line-Neutral Voltage, Magnitude
Uln:A	kV	Line-Neutral Voltage, Magnitude
Uln:B	kV	Line-Neutral Voltage, Magnitude
Uln:C	kV	Line-Neutral Voltage, Magnitude
phiuln:A	deg	Line-Neutral Voltage, Angle
phiuln:B	deg	Line-Neutral Voltage, Angle
phiuln:C	deg	Line-Neutral Voltage, Angle
upht:A	p.u.	Phase Technology dependent Voltage, Magnitude
upht:B	p.u.	Phase Technology dependent Voltage, Magnitude
upht:C	p.u.	Phase Technology dependent Voltage, Magnitude
Upht:A	kV	Phase Technology dependent Voltage, Magnitude
Upht:B	kV	Phase Technology dependent Voltage, Magnitude
Upht:C	kV	Phase Technology dependent Voltage, Magnitude

If no neutral connection exists the values of the variables from Table 3.3 are set to zero. If neutral connection exists, the result variables are calculated as follows:

• $\mathit{uln}{:}A, \mathit{uln}{:}B, \mathit{uln}{:}C$ are the magnitudes of the line to neutral voltages:

$$\begin{split} uln:&A = \sqrt{\underline{u}_{lnA}.r^2 + \underline{u}_{lnA}.i^2} \\ uln:&B = \sqrt{\underline{u}_{lnB}.r^2 + \underline{u}_{lnB}.i^2} \\ uln:&C = \sqrt{\underline{u}_{lnC}.r^2 + \underline{u}_{lnC}.i^2} \end{split}$$

• *Uln:A*, *Uln:B*, *Uln:C* are obtained as: for AC terminals with neutral (120°):

$$Uln:A = uln:A \cdot uknom/\sqrt{3}$$

$$Uln:B = uln:B \cdot uknom/\sqrt{3}$$

$$Uln:C = uln:C \cdot uknom/\sqrt{3}$$

for AC/BI terminals with neutral (180°):

$$Uln:A = uln:A \cdot uknom/2$$

 $Uln:B = uln:B \cdot uknom/2$
 $Uln:C = uln:C \cdot uknom/2$

where *uknom* is the nominal voltage of the terminal.

• phiuln:A, phiuln:B, phiuln:C are obtained as:

$$\begin{split} phiuln:&A = \arctan\left(\frac{\underline{u}_{lnA}.i}{\underline{u}_{lnA}.r}\right) \cdot \frac{180}{\pi} \\ phiuln:&B = \arctan\left(\frac{\underline{u}_{lnB}.i}{\underline{u}_{lnB}.r}\right) \cdot \frac{180}{\pi} \\ phiuln:&C = \arctan\left(\frac{\underline{u}_{lnC}.i}{\underline{u}_{lnC}.r}\right) \cdot \frac{180}{\pi} \end{split}$$

• $upht:A,\ upht:B,\ upht:C$ are obtained depending if there is neutral connection or not. If there is neutral connection the variables are obtained as:

$$upht:A = uln:A$$

 $upht:B = uln:B$
 $upht:C = uln:C$

If there is no neutral connection as:

$$upht:A = ul:A$$

 $upht:B = ul:B$
 $upht:C = ul:C$

• *Upht:A*, *Upht:B*, *Upht:C* are obtained depending if there is neutral connection or not. If there is neutral connection the variables are obtained as:

$$Upht:A = Uln:A$$

 $Upht:B = Uln:B$
 $Upht:C = Uln:C$

If there is no neutral connection as:

$$Upht:A = Ul:A$$

 $Upht:B = Ul:B$
 $Upht:C = Ul:C$

3.1.4 0,1,2 sequence and neutral voltage related variables for terminals

In addition to the phase, line to line and line to neutral voltage quantities, also quantities in the positive, negative and zero sequence are available. \underline{u}_1 , \underline{u}_2 and \underline{u}_0 are obtained when the phase values are transformed to symmetrical components.

For 3-phase terminals:

$$\begin{split} \underline{u}0 &= \frac{1}{3} \left(\underline{u}_A + \underline{u}_B + \underline{u}_C \right) \\ \underline{u}1 &= \frac{1}{3} \left(\underline{u}_A + a \cdot \underline{u}_B + a^2 \cdot \underline{u}_C \right) \\ \underline{u}2 &= \frac{1}{3} \left(\underline{u}_A + a^2 \cdot \underline{u}_B + a \cdot \underline{u}_C \right) \end{split}$$

where $a=\angle 120^\circ$

For BI-phase terminals (180°):

$$\underline{u}0 = \frac{1}{2} (\underline{u}_A + \underline{u}_B)$$

$$\underline{u}1 = \frac{1}{2} (\underline{u}_A - \underline{u}_B)$$

$$\underline{u}2 = 0$$

For 2-phase terminals (120°):

$$\underline{u}0 = \frac{1}{\sqrt{3}} (\underline{u}_A + \underline{u}_B)$$

$$\underline{u}1 = \frac{1}{\sqrt{3}} (\underline{u}_A - \underline{u}_B)$$

$$\underline{u}2 = 0$$

For 1-phase terminals:

$$\underline{u}0 = 0$$
 $\underline{u}1 = \underline{u}_A$
 $\underline{u}2 = 0$

Table 3.4: 0,1,2 sequence voltage related variables for terminals

Name	Unit	Description
un	p.u.	Neutral-Ground Voltage, Magnitude
Un	kV	Neutral-Ground Voltage, Magnitude
phiun	deg	Neutral-Ground Voltage, Angle
um	p.u.	Average-Voltage, Magnitude
Um	kV	Average-Voltage, Magnitude
u0	p.u.	Zero-Sequence Voltage, Magnitude
U0	kV	Zero-Sequence Voltage, Magnitude
$U0\times3$	kV	3*U0
phiu0	deg	Zero-Sequence Voltage, Angle
u1	p.u.	Positive-Sequence Voltage, Magnitude
u1pc	%	Positive-Sequence Voltage, Magnitude
u1r	p.u.	Positive-Sequence Voltage, Real Part
u1i	p.u.	Positive-Sequence Voltage, Imaginary Part
U1	kV	Line-Ground Positive-Sequence Voltage, Magnitude
phiu1	deg	Positive-Sequence Voltage, Angle
phiurel	deg	Voltage, Relative Angle
u2	p.u.	Negative-Sequence Voltage, Magnitude
U2	kV	Line-Ground Negative-Sequence Voltage, Magnitude
phiu2	deg	Negative-Sequence Voltage, Angle
U1l	kV	Line to Line Positive-Sequence Voltage, Magnitude
U2l	kV	Line to Line Negative-Sequence Voltage, Magnitude
uphtmin	p.u.	Minimum of Phase Technology dependent Voltage, Magnitude
uphtmax	p.u.	Maximum of Phase Technology dependent Voltage, Magnitude
ubfac	%	Unbalance factor

The variables from Table 3.4 are calculated as follows:

• un is obtained from the neutral complex voltage as:

$$un = \sqrt{\underline{u}_n.r^2 + \underline{u}_n.i^2}$$

 Un is obtained as: for AC terminals (120°):

$$Un = un \cdot uknom/\sqrt{3}$$

for AC/BI terminals (180°):

$$Un = un \cdot uknom/2$$

where uknom is the nominal voltage of the terminal.

• phiun is obtained as:

$$phiun = \arctan\left(\frac{\underline{u}_n.i}{\underline{u}_n.r}\right) \cdot \frac{180}{\pi}$$

- ullet um is calculated by dividing the sum of phase voltage magnitudes of all phases by the number of phases.
- *Um* is obtained as: for AC terminals:

$$Um = um \cdot uknom/\sqrt{3}$$

for AC/BI terminals:

$$Um = um \cdot uknom/2$$

where *uknom* is the nominal voltage of the terminal.

• u0 is obtained from the zero sequence complex voltage as:

$$u0 = \sqrt{\underline{u_0} \cdot r^2 + \underline{u_0} \cdot i^2}$$

 U0 is obtained as: for AC terminals (120°):

$$U0 = u0 \cdot uknom/\sqrt{3}$$

for AC/BI terminals (180°):

$$U0 = u0 \cdot uknom/2$$

where uknom is the nominal voltage of the terminal.

- $U0\times3$ is calculated as $3\cdot U0$ for three phase, as $2\cdot U0$ for two phase and as U0 for single phase systems.
- phiu0 is obtained as:

$$phiu0 = \arctan\left(\frac{\underline{u}_0.i}{\underline{u}_0.r}\right) \cdot \frac{180}{\pi}$$

• u1 is obtained from the positive sequence complex voltage as:

$$u1 = \sqrt{\underline{u}_1 \cdot r^2 + \underline{u}_1 \cdot i^2}$$

• *u*1*pc* is obtained as:

$$u1pc = u1 \cdot 100$$

• u1r is obtained from the positive sequence complex voltage as:

$$u1r = \underline{u}_1.r$$

• *u*1*i* is obtained from the positive sequence complex voltage as:

$$u1i = \underline{u}_1.i$$

 U1 is obtained as: for AC terminals (120°):

$$U1 = u1 \cdot uknom/\sqrt{3}$$

for AC/BI terminals (180°):

$$U1 = u1 \cdot uknom/2$$

where *uknom* is the nominal voltage of the terminal.

phiu1 is obtained as:

$$phiu1 = \arctan\left(\frac{\underline{u}_1.i}{\underline{u}_1.r}\right) \cdot \frac{180}{\pi}$$

 phiurel is obtained by using the Initial Angle of Bus Voltage phiini basic data parameter as:

$$phiurel = phiu_1 - phiini \cdot \frac{180}{\pi}$$

• u2 is obtained from the negative sequence complex voltage as:

$$u2 = \sqrt{\underline{u}_2.r^2 + \underline{u}_2.i^2}$$

• U2 is obtained as (only for 3-phase terminals):

$$U2 = u2 \cdot uknom/\sqrt{3}$$

where uknom is the nominal voltage of the terminal.

• phiu2 is obtained as:

$$phiu2 = \arctan\left(\frac{\underline{u}_2.i}{\underline{u}_2.r}\right) \cdot \frac{180}{\pi}$$

 U1l is obtained as: for 2-phase and 3-phase terminals:

$$U1l = u1 \cdot uknom$$

for 1-phase terminals:

$$U1l = U1$$

- uphtmin is the minimum of upht:A, upht:B, upht:C.
- *uphtmax* is the maximum of *upht:A*, *upht:B*, *upht:C*.
- *ubfac* is calculated as:

$$ubfac = \frac{u2}{u1} \cdot 100$$

If number of phases is less then three, it is set to zero.

3.1.5 Aggregated power variables for terminals

Table 3.5: Aggregated power variables for terminals

Name	Unit	Description
Pgen	MW	Generation, Active Power
Qgen	Mvar	Generation, Reactive Power
Pmot	MW	Motor Load, Active Power
Qmot	Mvar	Motor Load, Reactive Power
Pload	MW	General Load, Active Power
Qload	Mvar	General Load, Reactive Power
Pcomp	MW	Compensation (Losses)
Qcomp	Mvar	Compensation
Pnet	MW	External Networks, Active Power
Qnet	Mvar	External Networks, Reactive Power
Pflow	MW	Power Flow, Active Power
Qflow	Mvar	Power Flow, Reactive Power
Pout	MW	Outgoing Flow, Active Power
Qout	Mvar	Outgoing Power, Reactive Power
Sout	MVA	Outgoing Power, Apparent Power
cosphiout		Outgoing Power, Power Factor
Pbalance	MW	Active Power Balance (=0)
Qbalance	Mvar	Reactive Power Balance (=0)

The result variables from Table 3.5 are equivalent as the variables presented from the balanced load flow calculation in Table 2.2. Please refer to Table 2.2 for more information.

3.1.6 Low-voltage analysis related variables for terminals

Table 3.6: Low-voltage analysis related variables for terminals

Name	Unit	Description	
umin	p.u.	Minimum Voltage	
Umin	kV	Minimum Voltage (Line to Neutral)	
dumax	%	Maximum Voltage Drop along Feeder	

The result variables from Table 3.6 are calculated from a low-voltage load flow analysis where coincidence of low-voltage loads is considered.

3.1.7 Feeder losses variables for terminals

Table 3.7: Load flow, unbalanced, feeder losses variables (terminals)

Name	Unit	Description	
LossPdown	MW	Losses, downstream	
LossQdown	Mvar	Losses, downstream (Reactive Power)	
LossPdownload	MW	Load losses, downstream	
LossQdownload	Mvar	Load losses, downstream	
LossPdownnoload	MW	No load losses, downstream	
Loss Q down no load	Mvar	No load losses, downstream	

Please refer to Table 2.4 for more information on the variables from Table 3.7.

3.2 Result variables for elements

The result variables available for for single- and multiple-port elements after an unbalanced Load Flow calculation are presented in the following sub chapters.

3.2.1 Voltage related variables for elements

The voltage related variables for the terminals are all based on the phase to ground complex voltages \underline{u}_A , \underline{u}_B , \underline{u}_C and \underline{u}_N resulting from the unbalanced load flow.

For the element based variables, the relationship between the absolute and per unit value voltage is $\underline{U}_A = \underline{u}_A \cdot U_{base}$ where the base voltage is $U_{base} = U_{nom_el}/\sqrt{3}$ where U_{nom_el} is the nominal line to line voltage of the element. Due to the change in base, the per unit values are multiplied with the factor $uknom/U_{nom_el}$.

Name	Unit	Description
ur:A	p.u.	Phase Voltage, Real Part
ur:B	p.u.	Phase Voltage, Real Part
ur:C	p.u.	Phase Voltage, Real Part
ur:N	p.u.	Phase Voltage, Real Part
ui:A	p.u.	Phase Voltage, Imaginary Part
ui:B	p.u.	Phase Voltage, Imaginary Part
ui:C	p.u.	Phase Voltage, Imaginary Part
ui:N	p.u.	Phase Voltage, Imaginary Part
u:A	p.u.	Phase Voltage, Magnitude
u: B	p.u.	Phase Voltage, Magnitude
u:C	p.u.	Phase Voltage, Magnitude
u:N	p.u.	Phase Voltage, Magnitude

Table 3.8: Voltage related variables for elements

The result variables from Table 3.8 are calculated as follows:

• ur:A, ur:B, ur:C, ur:N are obtained from the complex phase voltages as:

$$\begin{split} ur:&A = \underline{u}_{A}.r \cdot \frac{uknom}{U_{nom_el}} \\ ur:&B = \underline{u}_{B}.r \cdot \frac{uknom}{U_{nom_el}} \\ ur:&C = \underline{u}_{C}.r \cdot \frac{uknom}{U_{nom_el}} \\ ur:&N = \underline{u}_{N}.r \cdot \frac{uknom}{U_{nom_el}} \end{split}$$

where uknom is the nominal voltage of the connected terminal and U_{nom_el} is the nominal voltage of the element.

• ui:A, ui:B, ui:C, ui:N are obtained from the complex phase voltages as:

$$\begin{aligned} ui:A &= \underline{u}_{A}.i \cdot \frac{uknom}{U_{nom_el}} \\ ui:B &= \underline{u}_{B}.i \cdot \frac{uknom}{U_{nom_el}} \\ ui:C &= \underline{u}_{C}.i \cdot \frac{uknom}{U_{nom_el}} \\ ui:N &= \underline{u}_{N}.i \cdot \frac{uknom}{U_{nom_el}} \end{aligned}$$

where uknom is the nominal voltage of the connected terminal and $U_{nom.el}$ is the nominal voltage of the element.

• u:A, u:B, u:C, u:N are obtained from the complex phase voltages as:

$$\begin{split} u:&A = \sqrt{\underline{u}_A.r^2 + \underline{u}_A.i^2} \cdot \frac{uknom}{U_{nom_el}} \\ u:&B = \sqrt{\underline{u}_B.r^2 + \underline{u}_B.i^2} \cdot \frac{uknom}{U_{nom_el}} \\ u:&C = \sqrt{\underline{u}_C.r^2 + \underline{u}_C.i^2} \cdot \frac{uknom}{U_{nom_el}} \\ u:&N = \sqrt{\underline{u}_N.r^2 + \underline{u}_N.i^2} \cdot \frac{uknom}{U_{nom_el}} \end{split}$$

3.2.2 Current related variables for elements

The current related variables for the elements are all based on the complex phase current resulting from the unbalanced load flow. The relationship between the absolute and per unit value current is $\underline{I}_A = \underline{i}_A \cdot I_{nom_el}$ where $I_{nom_el} = \frac{MVA_{el}}{\sqrt{3} \cdot U_{nom_el}}$ is the nominal current of the element.

Name Unit Description I:AkAPhase Current, Magnitude $I{:}B$ Phase Current, Magnitude kAI:CkAPhase Current, Magnitude I:NkAPhase Current, Magnitude Phase Current, Angle phii:AdegPhase Current, Angle phii:Bdegphii:CPhase Current, Angle degphii:NPhase Current, Angle degPhase Current, Real Part ir:Ap.u.Phase Current, Real Part ir:Bp.u.ir:CPhase Current, Real Part p.u.ir:NPhase Current, Real Part p.u.Phase Current, Imaginary Part ii:Ap.u.ii:BPhase Current, Imaginary Part p.u.Phase Current, Imaginary Part ii:Cp.u.Phase Current, Imaginary Part ii:Np.u.Phase Current, Magnitude i:Ap.u.i:BPhase Current, Magnitude p.u.i:CPhase Current, Magnitude p.u.i:NPhase Current, Magnitude p.u.Angle between Voltage and Current phiui:Adegphiui:BAngle between Voltage and Current degAngle between Voltage and Current phiui:CdegAngle between Voltage and Current phiui:NdeqPhase Current, Magnitude, referred to network inet:Ap.u.inet:BPhase Current, Magnitude, referred to network p.u. $in et {:} C$ Phase Current, Magnitude, referred to network p.u.Phase Current, Magnitude, referred to network inet:Np.u.

Table 3.9: Current related variables for elements

The result variables from Table 3.9 are calculated as follows:

• *I*:*A*, *I*:*B*, *I*:*C*, *I*:*N* are obtained as amplitudes of the complex currents:

$$I:A = \sqrt{\underline{I}_A \cdot r^2 + \underline{I}_A \cdot i^2}$$

$$I:B = \sqrt{\underline{I}_B \cdot r^2 + \underline{I}_B \cdot i^2}$$

$$I:C = \sqrt{\underline{I}_C \cdot r^2 + \underline{I}_C \cdot i^2}$$

$$I:N = \sqrt{I_N \cdot r^2 + I_N \cdot i^2}$$

• phii:A, phii:B, phii:C, phii:N are obtained as:

$$phii:A = \arctan\left(\frac{\underline{I}_{A}.i}{\underline{I}_{A}.r}\right) \cdot \frac{180}{\pi}$$

$$phii:B = \arctan\left(\frac{\underline{I}_{B}.i}{\underline{I}_{B}.r}\right) \cdot \frac{180}{\pi}$$

$$phii:C = \arctan\left(\frac{\underline{I}_{C}.i}{\underline{I}_{C}.r}\right) \cdot \frac{180}{\pi}$$

$$phii:N = \arctan\left(\frac{\underline{I}_{N}.i}{\underline{I}_{N}.r}\right) \cdot \frac{180}{\pi}$$

• ir:A, ir:B, ir:C, ir:N are obtained as:

$$\begin{split} ir:&A = \frac{\underline{I}_A.r}{I_{nom_el}}\\ ir:&B = \frac{\underline{I}_B.r}{I_{nom_el}}\\ ir:&C = \frac{\underline{I}_C.r}{I_{nom_el}}\\ ir:&N = \frac{\underline{I}_N.r}{I_{nom_el}} \end{split}$$

• *ii:A*, *ii:B*, *ii:C*, *ii:N* are obtained as:

$$ii:A = \frac{\underline{I}_A.i}{I_{nom.el}}$$

$$ii:B = \frac{\underline{I}_B.i}{I_{nom.el}}$$

$$ii:C = \frac{\underline{I}_C.i}{I_{nom.el}}$$

$$ii:N = \frac{\underline{I}_N.i}{I_{nom.el}}$$

• *i:A*, *i:B*, *i:C*, *i:N* are obtained as:

$$\begin{split} i:&A = \frac{I:A}{I_{nom_el}}\\ i:&B = \frac{I:B}{I_{nom_el}}\\ i:&C = \frac{I:C}{I_{nom_el}}\\ i:&N = \frac{I:N}{I_{nom_el}} \end{split}$$

• phiui:A, phiui:B, phiui:C, phiui:N are obtained as:

$$\begin{split} phiui:&A = \arctan\left(\frac{\underline{u}_A.i}{\underline{u}_A.r}\right) \cdot \frac{180}{\pi} - phii:A \\ phiui:&B = \arctan\left(\frac{\underline{u}_B.i}{\underline{u}_B.r}\right) \cdot \frac{180}{\pi} - phii:B \\ phiui:&C = \arctan\left(\frac{\underline{u}_C.i}{\underline{u}_C.r}\right) \cdot \frac{180}{\pi} - phii:C \\ phiui:&N = \arctan\left(\frac{\underline{u}_N.i}{\underline{u}_N.r}\right) \cdot \frac{180}{\pi} - phii:N \end{split}$$

• inet:A, inet:B, inet:C, inet:N are obtained from the amplitude of the phase currents as:

$$inet:A = \frac{I:A}{I_{nom.1MVA}}$$

$$inet:B = \frac{I:B}{I_{nom.1MVA}}$$

$$inet:C = \frac{I:C}{I_{nom.1MVA}}$$

$$inet:N = \frac{I:N}{I_{nom.1MVA}}$$

where $I_{nom_1MVA}=\frac{1}{\sqrt{3}\cdot uknom}$ is the nominal current for 1MVA and uknom is the nominal voltage of the connected terminal.

3.2.3 Miscellaneous variables per phase for elements

Table 3.10: Miscellaneous variables per phase for elements

Name	Unit	Description
TfctPh:A	s	Fault Clearing Time
TfctPh:B	s	Fault Clearing Time
TfctPh:C	s	Fault Clearing Time
TfctPh:N	s	Fault Clearing Time
BrkloadPh:A	%	Breaker Loading
BrkloadPh:B	%	Breaker Loading
BrkloadPh:C	%	Breaker Loading
BrkloadPh:N	%	Breaker Loading

The result variables from Table 3.10 are calculated as follows:

- TfctPh:A, TfctPh:B, TfctPh:C, TfctPh:N give the fault clearing time of a fuse or a relay located in the local cubicle. If the fuse/relay model is not triggered with the Load Flow current, a default value of 9999,999s is used.
- BrkloadPh:A, BrkloadPh:B, BrkloadPh:C, BrkloadPh:N are calculated as:

$$BrkloadPh:A = \frac{I:A}{BrkInom} \cdot 100$$

$$BrkloadPh:B = \frac{I:B}{BrkInom} \cdot 100$$

$$BrkloadPh:C = \frac{I:C}{BrkInom} \cdot 100$$

$$BrkloadPh:N = \frac{I:N}{BrkInom} \cdot 100$$

where BrkInom is the rated current of a switch (input parameter Inom in TypSwitch) located in the cubicle.

3.2.4 0,1,2 sequence voltage related variables for elements

In addition to the phase, line to line and line to neutral voltage quantities, also quantities in the positive, negative and zero sequence are available.

For 3-phase elements:

$$\underline{u}0 = \frac{1}{3} (\underline{u}_A + \underline{u}_B + \underline{u}_C)$$

$$\underline{u}1 = \frac{1}{3} (\underline{u}_A + a \cdot \underline{u}_B + a^2 \cdot \underline{u}_C)$$

$$\underline{u}2 = \frac{1}{3} (\underline{u}_A + a^2 \cdot \underline{u}_B + a \cdot \underline{u}_C)$$

where $a = \angle 120^{\circ}$

For BI-phase elements (180°):

$$\underline{u}0 = \frac{1}{2} (\underline{u}_A + \underline{u}_B)$$

$$\underline{u}1 = \frac{1}{2} (\underline{u}_A - \underline{u}_B)$$

$$u2 = 0$$

For 2-phase elements (120°):

$$\underline{u}0 = \frac{1}{\sqrt{3}} (\underline{u}_A + \underline{u}_B)$$

$$\underline{u}1 = \frac{1}{\sqrt{3}} (\underline{u}_A - \underline{u}_B)$$

$$\underline{u}2 = 0$$

For 1-phase elements:

$$\underline{u}0 = 0$$

$$\underline{u}1 = \underline{u}_A$$

$$\underline{u}2 = 0$$

Table 3.11: 0,1,2 sequence voltage related variables for elements

Name	Unit	Description
u0	p.u	Zero-Sequence-Voltage, Magnitude
phiu0	deg	Zero-Sequence-Voltage, Angle
u1r	p.u	Positive-Sequence-Voltage, Real Part
u1i	p.u	Positive-Sequence-Voltage, Imaginary Part
u1	p.u	Positive-Sequence-Voltage, Magnitude
U1	kV	Line-Ground Positive-Sequence-Voltage, Magnitude
U1l	kV	Line-Line Positive-Sequence-Voltage, Magnitude
phiu1	deg	Positive-Sequence-Voltage, Angle
u2	p.u	Negative-Sequence-Voltage, Magnitude
phiu2	deg	Negative-Sequence-Voltage, Angle

The variables from Table 3.11 are calculated as follows:

• u0 is obtained from the zero sequence complex voltage as:

$$u0 = \sqrt{\underline{u}_0 \cdot r^2 + \underline{u}_0 \cdot i^2} \cdot \frac{uknom}{U_{nom\ el}}$$

where uknom is the nominal voltage of the connected terminal and U_{nom_el} is the nominal voltage of the element.

• phiu0 is obtained as:

$$phiu0 = \arctan\left(\frac{\underline{u}_0.i}{\underline{u}_0.r}\right) \cdot \frac{180}{\pi}$$

• u1r is obtained from the positive sequence complex voltage as:

$$u1r = \underline{u}_1.r \cdot \frac{uknom}{U_{nom_el}}$$

• u1i is obtained from the positive sequence complex voltage as:

$$u1i = \underline{u}_1.i \cdot \frac{uknom}{U_{nom-el}}$$

• *u*1 is obtained from the positive sequence complex voltage as:

$$u1 = \sqrt{\underline{u}_1.r^2 + \underline{u}_1.i^2} \cdot \frac{uknom}{U_{nom.el}}$$

• *U*1 is obtained as: for AC elements:

$$U1 = u1 \cdot U_{nom_el} / \sqrt{3}$$

for AC/BI elements:

$$U1 = u1 \cdot U_{nom_el}/2$$

 U1l is obtained as: for 2-phase and 3-phase terminals:

$$U1l = u1 \cdot U_{nom_el}$$

for 1-phase terminals:

$$U1l = U1$$

• phiu1 is obtained as:

$$phiu1 = \arctan\left(\frac{\underline{u}_1.i}{\underline{u}_1.r}\right) \cdot \frac{180}{\pi}$$

• u2 is obtained from the negative sequence complex voltage as:

$$u2 = \sqrt{\underline{u}_2.r^2 + \underline{u}_2.i^2} \cdot \frac{uknom}{U_{nom.el}}$$

phiu2 is obtained as:

$$phiu2 = \arctan\left(\frac{\underline{u}_2.i}{\underline{u}_2.r}\right) \cdot \frac{180}{\pi}$$

3.2.5 0,1,2 sequence current related variables for elements

In addition to the phase quantities, also quantities in the positive, negative and zero sequence are available. \underline{I}_1 , \underline{I}_2 and \underline{I}_0 are obtained when the phase values are transformed to symmetrical components.

For 3-phase elements:

$$\underline{i}0 = \frac{1}{3} (\underline{i}_A + \underline{i}_B + \underline{i}_C)
\underline{i}1 = \frac{1}{3} (\underline{i}_A + a \cdot \underline{i}_B + a^2 \cdot \underline{i}_C)
\underline{i}2 = \frac{1}{3} (\underline{i}_A + a^2 \cdot \underline{i}_B + a \cdot \underline{i}_C)$$

where $a = \angle 120^{\circ}$

For BI-phase elements (180°):

$$\begin{split} \underline{i}0 &= \frac{1}{2} \left(\underline{i}_A + \underline{i}_B \right) \\ \underline{i}1 &= \frac{1}{2} \left(\underline{i}_A - \underline{i}_B \right) \\ \underline{i}2 &= 0 \end{split}$$

For 2-phase elements (120°):

$$\begin{split} \underline{i}0 &= \frac{1}{\sqrt{3}} \left(\underline{i}_A + \underline{i}_B \right) \\ \underline{i}1 &= \frac{1}{\sqrt{3}} \left(\underline{i}_A - \underline{i}_B \right) \\ i2 &= 0 \end{split}$$

For 1-phase elements:

$$\underline{i}0 = 0$$
 $\underline{i}1 = \underline{i}_A$
 $\underline{i}2 = 0$

Table 3.12: 0,1,2 sequence current related variables for elements

Name	Unit	Description
<i>I</i> 0	kA	Zero-Sequence Current, Magnitude
$I0\times3$	kA	3*10
phii0	deg	Zero-Sequence Current, Angle
i0	p.u	Zero-Sequence Current, Magnitude
i0r	p.u	Zero-Sequence Current, Real Part
i0i	p.u	Zero-Sequence Current, Imaginary Part
I1	kA	Positive-Sequence Current, Magnitude
phii1	deg	Positive-Sequence Current, Angle
i1	p.u	Positive-Sequence Current, Magnitude
i1r	p.u	Positive-Sequence Current, Real Part
i1i	p.u	Positive-Sequence Current, Imaginary Part
I2	kA	Negative-Sequence Current, Magnitude
phii2	deg	Negative-Sequence Current, Angle
i2	p.u	Negative-Sequence Current, Magnitude
i2r	p.u	Negative-Sequence Current, Real Part
i2i	p.u	Negative-Sequence Current, Imaginary Part
i1P	p.u.	Positive-Sequence Active Current
i1Q	p.u.	Positive-Sequence Reactive Current
I1P	kA	Positive-Sequence Active Current
I1Q	kA	Positive-Sequence Reactive Current
i2P	p.u.	Negative-Sequence Active Current
i2Q	p.u.	Negative-Sequence Reactive Current
I2P	kA	Negative-Sequence Active Current
I2Q	kA	Negative-Sequence Reactive Current
phiu0i0	deg	Angle between Voltage and Current in zero sequence system
phiu1i1	deg	Angle between Voltage and Current in positive sequence system
phiu2i2	deg	Angle between Voltage and Current in negative sequence system
ubfacI	%	Current Unbalance Factor

The result variables from Table 3.12 are calculated as follows:

• *I*0 is obtained as the magnitude of the zero sequence current:

$$I0 = \sqrt{\underline{I}_0.r^2 + \underline{I}_0.i^2}$$

- $I0 \times 3$ is obtained as $3 \cdot I0$ for three phase, as $2 \cdot I0$ for two phase and as I0 for single phase systems.
- phii0 is obtained as:

$$phii0 = \arctan\left(\frac{\underline{I}_0.i}{\underline{I}_0.r}\right) \cdot \frac{180}{\pi}$$

• i0 is obtained as:

$$i0 = \frac{I0}{I_{nom\ el}}$$

where I_{nom_el} is the nominal current of the element.

• i0r is obtained as:

$$i0r = \frac{\underline{I}_0.r}{I_{nom_el}}$$

• i0i is obtained as:

$$i0i = \frac{\underline{I}_0.i}{I_{nom_el}}$$

I1 is obtained as the magnitude of the positive sequence current:

$$I1 = \sqrt{\underline{I}_1.r^2 + \underline{I}_1.i^2}$$

• phii1 is obtained as:

$$phii1 = \arctan\left(\frac{\underline{I}_1.i}{I_1.r}\right) \cdot \frac{180}{\pi}$$

• i1 is obtained as:

$$i1 = \frac{I1}{I_{nom_el}}$$

where I_{nom_el} is the nominal current of the element.

• i1r is obtained as:

$$i1r = \frac{\underline{I}_1.r}{I_{nom_el}}$$

• *i*1*i* is obtained as:

$$i1i = \frac{\underline{I}_1.i}{I_{nom_el}}$$

I2 is obtained as the magnitude of the negative sequence current:

$$I2 = \sqrt{\underline{I}_2.r^2 + \underline{I}_2.i^2}$$

• phii2 is obtained as:

$$phii2 = \arctan\left(\frac{\underline{I}_2.i}{\underline{I}_2.r}\right) \cdot \frac{180}{\pi}$$

• i2 is obtained as:

$$i2 = \frac{I2}{I_{nom_el}}$$

where I_{nom_el} is the nominal current of the element.

• i2r is obtained as:

$$i2r = \frac{\underline{I}_2.r}{I_{nom_el}}$$

• *i*2*i* is obtained as:

$$i2i = \frac{\underline{I}_2.i}{I_{nom_el}}$$

• i1P is obtained as:

$$i1P = i1 \cdot \cos(\phi_1)$$

where ϕ_1 is the angle between the active and reactive power in the positive sequence.

• i1Q is obtained as:

$$i1Q = i1 \cdot \sin(\phi_1)$$

• *I*1*P* is obtained as:

$$I1P = I1 \cdot \cos(\phi_1)$$

• *I*1*Q* is obtained as:

$$I1Q = I1 \cdot \sin(\phi_1)$$

• i2P is obtained as:

$$i2P = i2 \cdot \cos(\phi_2)$$

where ϕ_2 is the angle between the active and reactive power in the negative sequence.

• i2Q is obtained as:

$$i2Q = i2 \cdot \sin(\phi_2)$$

• I2P is obtained as:

$$I2P = I2 \cdot \cos(\phi_2)$$

• I2Q is obtained as:

$$I2Q = I2 \cdot \sin(\phi)$$

• phiu0i0 is obtained as:

$$phiu0i0 = phiu0 - phii0$$

• phiu1i1 is obtained as:

$$phiu1i1 = phiu1 - phii1$$

• phiu2i2 is obtained as:

$$phiu2i2 = phiu2 - phii2$$

• *ubfacI* is obtained as:

$$ubfacI = \frac{i2}{i1} \cdot 100$$

If number of phases (without neutral) is less then three, it is set to zero.

3.2.6 0,1,2 sequence power related variables for elements

The total complex apparent power is the sum of apparent powers of all phases:

$$\underline{S}_{sum} = \underline{S}_A + \underline{S}_B + \underline{S}_C + \underline{S}_N$$

where:

$$\underline{S}_A = \underline{U}_A \cdot \underline{I}_A^*$$

$$\underline{S}_B = \underline{U}_B \cdot \underline{I}_B^*$$

$$\underline{S}_C = \underline{U}_C \cdot \underline{I}_C^*$$

$$\underline{S}_N = \underline{U}_N \cdot \underline{I}_N^*$$

and the sequence powers:

For 3-phase elements:

$$\begin{split} \underline{S}_1 &= 3 \cdot \underline{U} \underline{1} \cdot \underline{I} \underline{1}^* \\ \underline{S}_2 &= 3 \cdot \underline{U} \underline{2} \cdot \underline{I} \underline{2}^* \\ \underline{S}_0 &= 3 \cdot \underline{U} \underline{0} \cdot \underline{I} \underline{0}^* \end{split}$$

For AC/BI elements (180°):

$$\begin{split} \underline{S}_1 &= 2 \cdot \underline{U1} \cdot \underline{I1}^* \\ \underline{S}_2 &= 0 \\ \underline{S}_0 &= 2 \cdot \underline{U0} \cdot \underline{I0}^* \end{split}$$

For 2-phase elements (120°):

$$\underline{S}_1 = 3/2 \cdot \underline{U1} \cdot \underline{I1}^*$$

$$\underline{S}_2 = 0$$

$$\underline{S}_0 = 3/2 \cdot \underline{U0} \cdot \underline{I0}^*$$

where

$$\underline{S}_{sum} = \underline{S}_1 + \underline{S}_2 + \underline{S}_0$$

Table 3.13: 0,1,2 sequence power related variables for elements

Name	Unit	Description
Psum	MW	Total Active Power
Qsum	Mvar	Total Reactive Power
Ssum	MVA	Total Apparent Power
cosphisum		Total Power Factor
tanphisum		Total tan(phi)
P1	MW	Positive Sequence Active Power
Q1	Mvar	Positive Sequence Reactive Power
P2	MW	Negative Sequence Active Power
Q2	Mvar	Negative Sequence Reactive Power
ubfacS	%	Power Unbalance Factor

The result variables from Table 3.13 are calculated as follows:

• Psum is obtained as:

$$Psum = \underline{S}_{sum}.r$$

• Qsum is obtained as:

$$Qsum = \underline{S}_{sum}.i$$

• Ssum is obtained as:

$$Ssum = \sqrt{\underline{S}_{sum}.r^2 + \underline{S}_{sum}.i^2}$$

• cosphisum is obtained as:

$$cosphisum = cos(\phi_s)$$

where the angle is defined as:

$$\phi_s = \arctan\left(\frac{\underline{S}_{sum}.i}{\underline{S}_{sum}.r}\right)$$

• tanphisum is obtained as:

$$tanphisum = tan(\phi_s)$$

• P1 is the positive sequence active power of the element.

$$P1 = S1.r$$

• *Q*1 is the positive sequence reactive power of the element.

$$Q1 = \underline{S1}.i$$

• P2 is the negative sequence active power of the element.

$$P2 = \underline{S2}.r$$

• Q2 is the negative sequence reactive power of the element.

$$Q2 = S2.i$$

• ubfacS is calculated as a ratio between Δ_{max_abs} and the average of absolute apparent powers. Δ_{max_abs} is the biggest absolute difference between the apparent power of a phase and the average apparent power. In this calculation the neutral connection is not taken into account.

3.2.7 Miscellaneous variables (min/max values) for elements

Table 3.14: Miscellaneous variables (min/max values) for elements

Name	Unit	Description
Tfct	S	Fault Clearing Time
Brkload	%	Breaker Loading
Imax	kA	Maximum Current
Smax	MVA	Maximum Power

The result variables from Table 3.14 are calculated as follows:

- Tfct is the minimum from the fault clearing times: TfctPh:A, TfctPh:B, TfctPh:C, TfctPh:N.
- Brkload is the maximum breaker loading from: BrkloadPh:A, BrkloadPh:B, BrkloadPh:C, BrkloadPh:N.
- *Imax* is the biggest value of the maximum currents per phase from low-voltage load flow analysis (coincidence of low-voltage loads is considered).
- *Smax* is obtained as:

$$Smax = \sqrt{3} \cdot uknom \cdot Imax$$

4 Linear DC Load Flow calculation

For the linear DC calculation all the terminal magnitudes are set to 1p.u. and the losses are neglected. The calculation delivers only active power and voltage angles as results.

4.1 Result variables for terminals

As described in Section 1.2.2, the result variables from the *Bus Results* set from the port elements are equivalent to the result variables from the *Currents, Voltages and Currents* set for the terminals.

The result variables available for terminals after a linear DC Load Flow calculation are presented in the following sub chapters.

4.1.1 Voltage related variables for terminals

Name Unit Description Voltage, Magnitude up.u.u1Positive-Sequence Voltage, Magnitude p.u.% Voltage, Magnitude upcLine-Ground Voltage, Magnitude U kVkVLine-Line Voltage, Magnitude UlVoltage, Angle phiudeqphiurel Voltage, Relative Angle deg

Table 4.1: Voltage related variables for terminals

The result variables from Table 4.1 are calculated as follows:

- u has a constant value of 1p.u.
- u1 has a constant value of 1p.u..
- upc has a constant value of 100%.
- U is obtained as:

$$U = 1 \cdot uknom/\sqrt{3}$$

where *uknom* is the nominal voltage of the terminal.

• *Ul* is obtained as:

$$Ul = 1 \cdot uknom$$

- phiu is a result from the calculation.
- phiurel is obtained using the Initial Angle of Bus Voltage phiini basic data parameter as:

$$phiurel = phiu - phiini \cdot \frac{180}{\pi}$$

4.1.2 Power related variables for terminals

Table 4.2: Power related variables for terminals

Name	Unit	Description
Pgen	MW	Generation, Active Power
Pmot	MW	Motor Load, Active Power
Pload	MW	General Load, Active Power
Pcomp	MW	Compensation (Losses)
Pnet	MW	External Networks, Active Power
Pflow	MW	Power Flow, Active Power

The result variables from Table 4.2 are calculated as follows:

- Pgen is the active power sum of all synchronous, asynchronous and static generators connected to the terminal. If generation is defined in the MV Load (ElmLodmv), the generated active power is added to this sum.
- *Pmot* is the active power sum of all synchronous and asynchronous motors connected to the terminal.
- Pload is the active power sum of all loads connected to the terminal.
- *Pcomp* is the active power sum of all shunts and filters connected to the terminal.
- · Pnet is the active power sum of all external network elements connected to the terminal.
- Pflow is the sum of all active power flowing out of the terminal.

4.2 Result variables for elements

The result variables available for for single- and multiple-port elements after a linear DC Load Flow calculation are presented in the following sub chapters.

4.2.1 Power related variables for elements

Table 4.3: Power related variables for elements

Name	Unit	Description
P	MW	Active Power
Q	Mvar	Reactive Power

The result variables from Table 4.3 are calculated as follows:

- P is a calculation result.
- Q is always 0Mvar.