

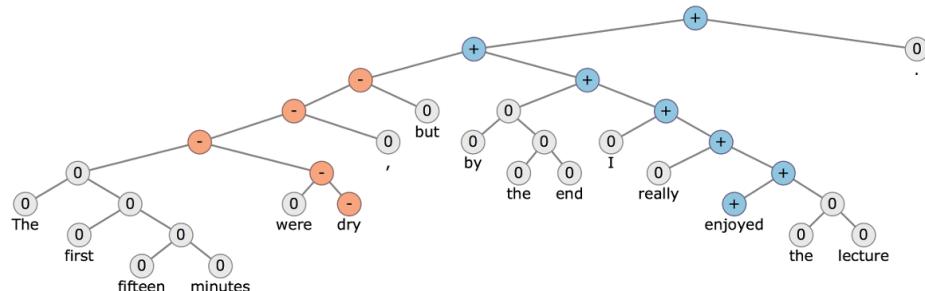
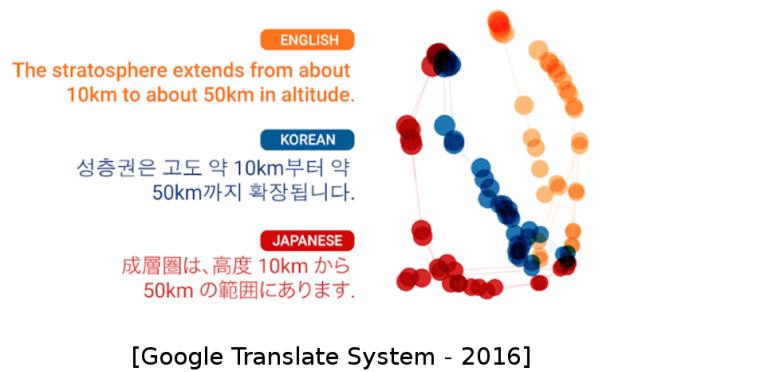
Natural Language Processing with Deep Learning

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DATASCIENCE
UNIVERSITÉ PARIS-SACLAY

Natural Language Processing



[Socher 2015]

Natural Language Processing

- Sentence/Document level Classification (topic, sentiment)
- Topic modeling (LDA, ...)

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- Sentence/Document level Classification (topic, sentiment)
- Topic modeling (LDA, ...)
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- Summarization

Recommended reading

A Primer on Neural Network Models for Natural Language Processing by Yoav Goldberg

<http://u.cs.biu.ac.il/~yogo/nlp.pdf>

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Useful open source projects

gensim spaCy



HUGGING FACE

Outline

Classification and word representation

Outline

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Word2Vec

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Language Modelling

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Recurrent neural networks

Word Representation and Word2Vec

Word representation

Words are indexed and represented as 1-hot vectors

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Large Vocabulary of possible words $|V|$

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Use of **Embeddings** as inputs in all Deep NLP tasks

Word representation

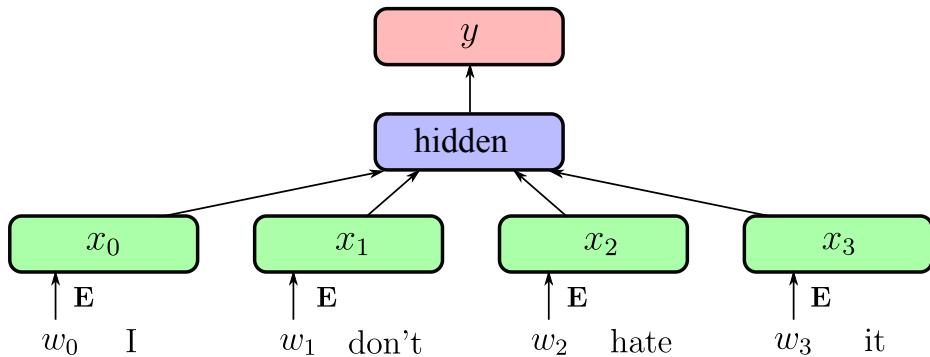
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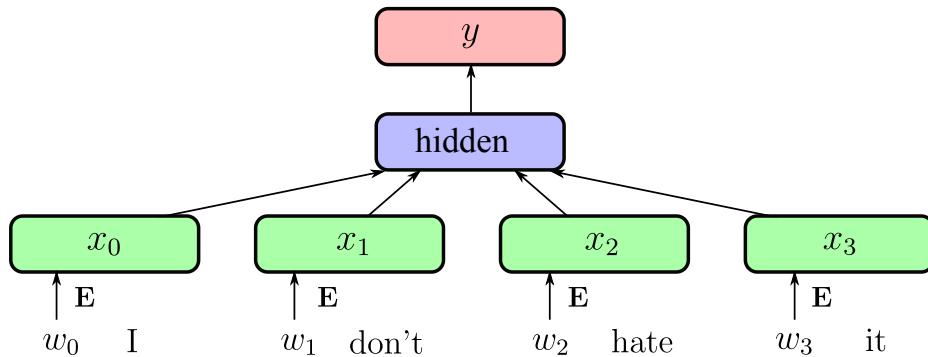
Use of **Embeddings** as inputs in all Deep NLP tasks

Word embeddings usually have dimensions 50, 100, 200, 300

Supervised Text Classification



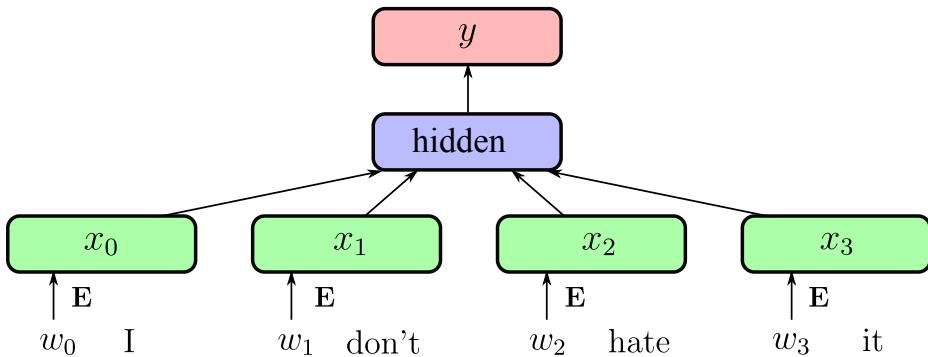
Supervised Text Classification



E embedding (linear projection)

$|V| \times H$

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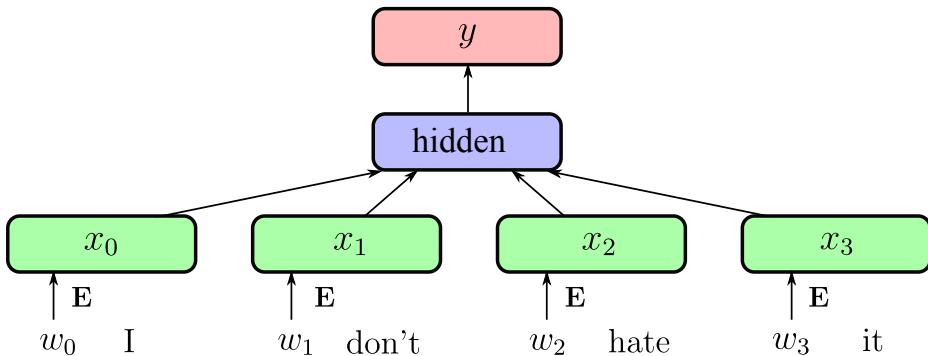
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hidden activation size: H

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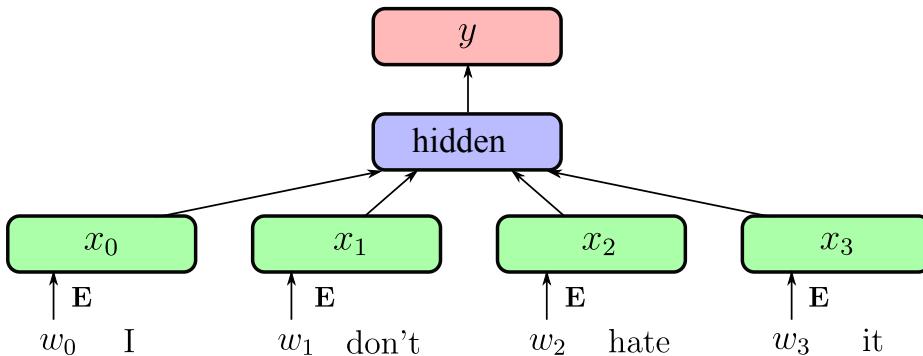
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Dense output connection W, b

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Joulin, Armand, et al. "Bag of tricks for efficient text classification." FAIR 2016

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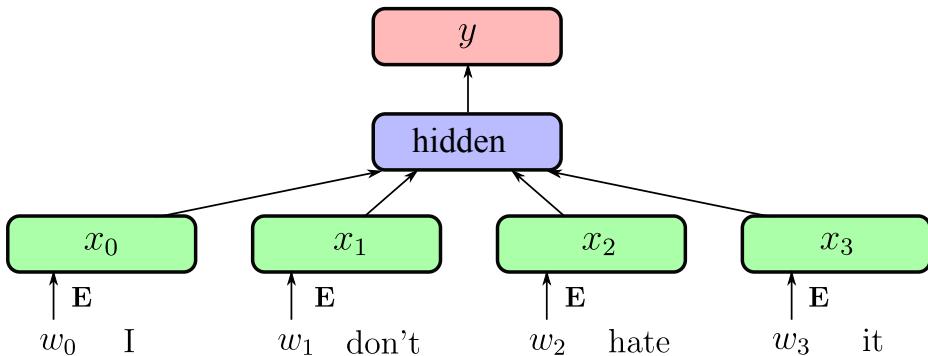
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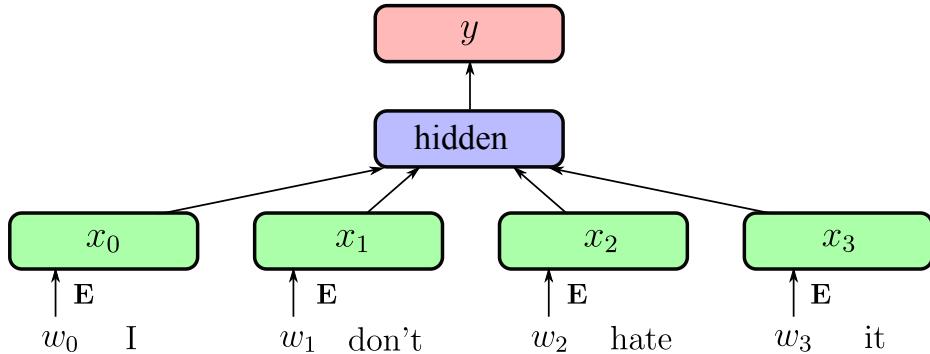
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Softmax and cross-entropy loss

Supervised Text Classification



- Very efficient (**speed** and **accuracy**) on large datasets

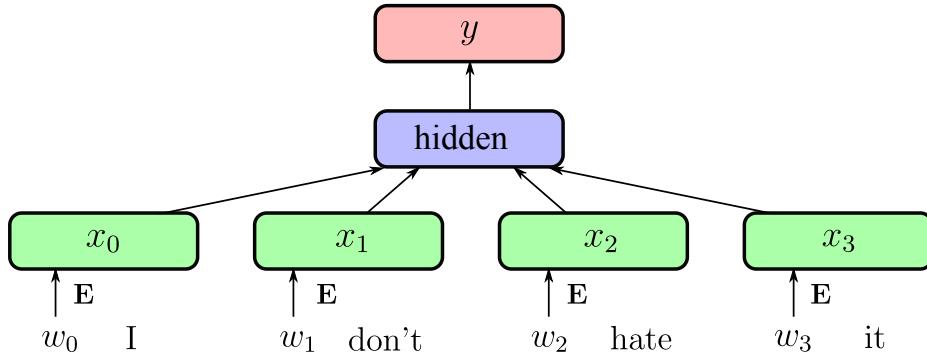
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- Little gains from depth

Transfer Learning for Text

Similar to image: can we have word representations that are generic enough to **transfer** from one task to another?

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Unsupervised / self-supervised learning of word representations

Transfer Learning for Text

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Unsupervised / self-supervised learning of word representations

Unlabelled text data is almost infinite:

- Wikipedia dumps
- Project Gutenberg
- Social Networks
- Common Crawl

Word Vectors

bilmark mary
 bob jack stephen elizabeth
 tony edward
 miss steve christian alexander
 chris andy charles
 joe tom harry robson
 tom harry joseph maria
 frank paul frances
 mrs. louis
 mr. sam pavlidis
 don arthur george jean
 ray martin thomas
 simon howard
 ben lee scott
 dr. al lewis bush
 x. a. taylor fox
 m. e. h. j. johnson
 s. w. smith williams
 c. b. d. p. jones davis ford grant
 von bell
 van

 s. et la michelles
 dad los los angeles
 el san san francisco
 santa santa monica
 des hong des
 core core

 june august
 february september
 january october
 april november
 december march

 cape

 super

 east
 western
 southeast
 northeast

 southern central
 central western
 western midwest

 usa philippines
 canada ireland britain
 australia sweden
 new zealand norway finland
 america europe
 asia africa russia
 africa korea japan rome
 asia pakistan egypt
 israel
 vietnam

 southam midwest
 central southeast
 western northeast

excerpt from work by J. Turian on a model trained by R. Collobert et al. 2008

Word2Vec

FRANCE	JESUS	XBOX	REDDISH	SCRATCHED	MEGABITS
AUSTRIA	GOD	AMIGA	GREENISH	NAILED	OCTETS
BELGIUM	SATI	PLAYSTATION	BLUISH	SMASHED	MB/S
GERMANY	CHRIST	MSX	PINKISH	PUNCHED	BIT/S
ITALY	SATAN	IPOD	PURPLISH	POPPED	BAUD
GREECE	KALI	SEGA	BROWNISH	CRIMPED	CARATS
SWEDEN	INDRA	PSNUMBER	GREYISH	SCRAPED	KBIT/S
NORWAY	VISHNU	HD	GRAYISH	SCREWED	MEGAHERTZ
EUROPE	ANANDA	DREAMCAST	WHITISH	SECTIONED	MEGAPIXELS
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Word2Vec

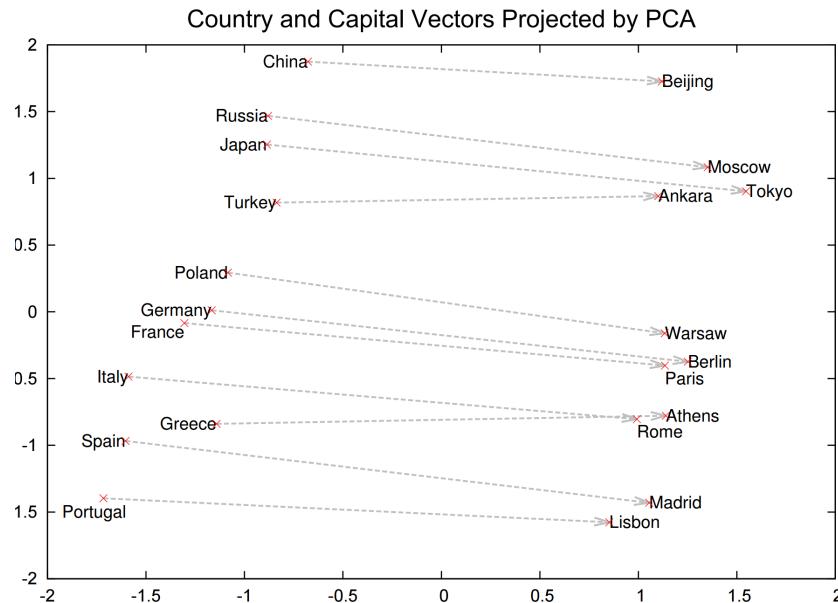
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Compositionality

Czech + currency	Vietnam + capital	German + airlines	Russian + river	French + actress
koruna	Hanoi	airline Lufthansa	Moscow	Juliette Binoche
Check crown	Ho Chi Minh City	carrier Lufthansa	Volga River	Vanessa Paradis
Polish zolty	Viet Nam	flag carrier Lufthansa	upriver	Charlotte Gainsbourg
CTK	Vietnamese	Lufthansa	Russia	Cecile De

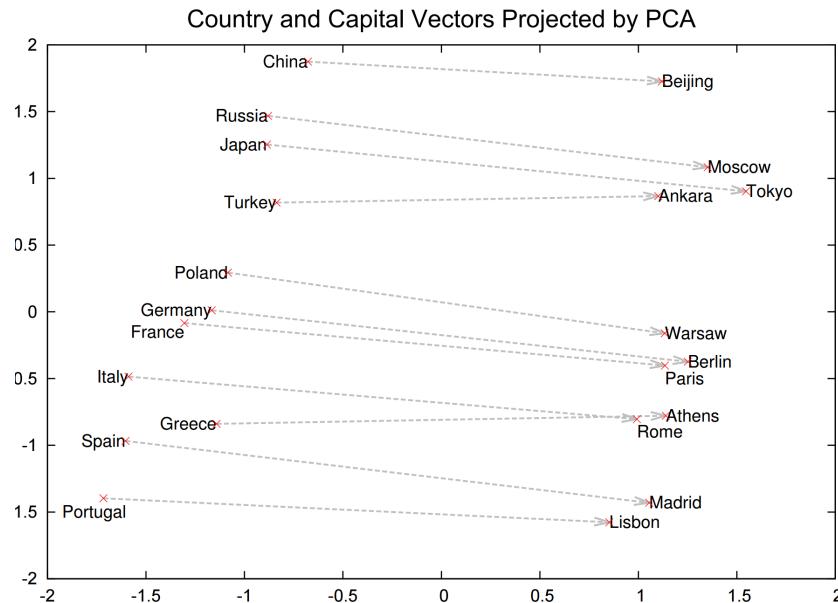
Colobert et al. 2011, Mikolov, et al. 2013

Word Analogies



Mikolov, Tomas, et al. "Distributed representations of words and phrases and their compositionality." NIPS 2013

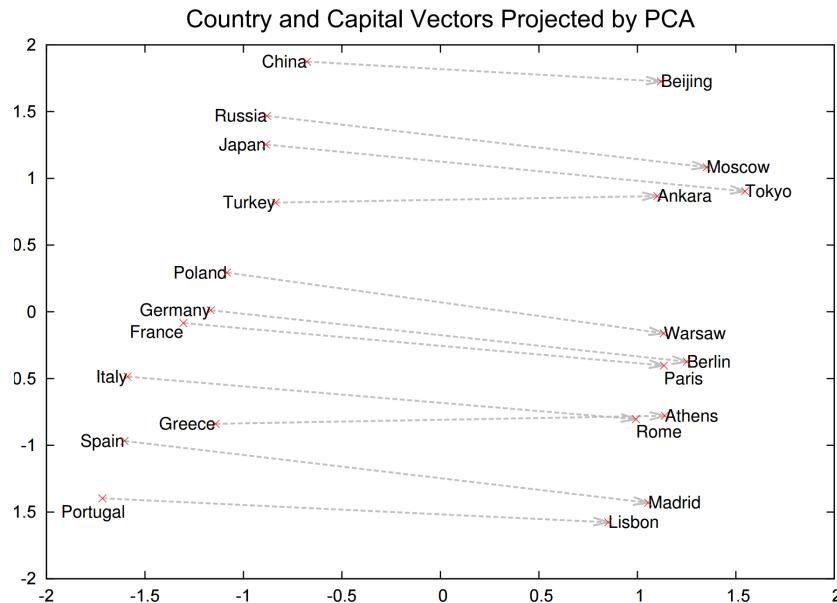
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- Linear relations in Word2Vec embeddings

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Self-supervised training

Distributional Hypothesis (Harris, 1954): “*words are characterised by the company that they keep*”

Main idea: learning word embeddings by **predicting word contexts**

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Given a word e.g. “carrot” and any other word $w \in V$ predict probability $P(w | \text{carrot})$ that w occurs in the context of “carrot”.

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Given a word e.g. “carrot” and any other word $w \in V$ predict probability $P(w | \text{carrot})$ that w occurs in the context of “carrot”.

- **Unsupervised / self-supervised:** no need for class labels.
- (Self-)supervision comes from **context**.
- Requires a lot of text data to cover rare words correctly.

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Word2Vec: CBoW

CBoW: representing the context as **Continuous Bag-of-Word**

Self-supervision from large unlabeled corpus of text: *slide* over an **anchor word** and its **context**:

the carrot is a root vegetable, usually orange

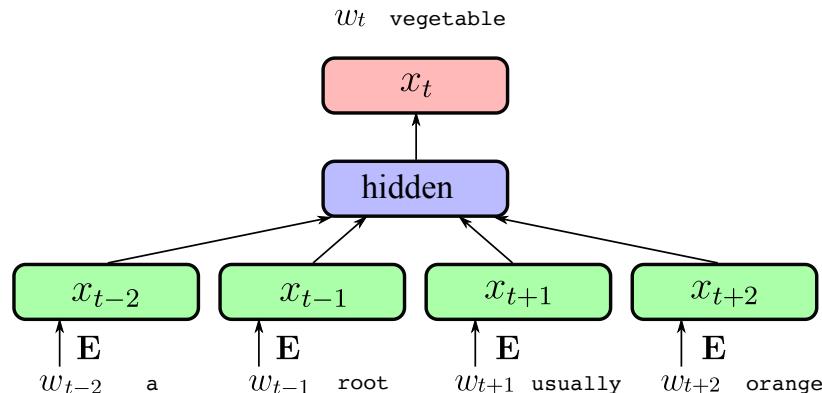
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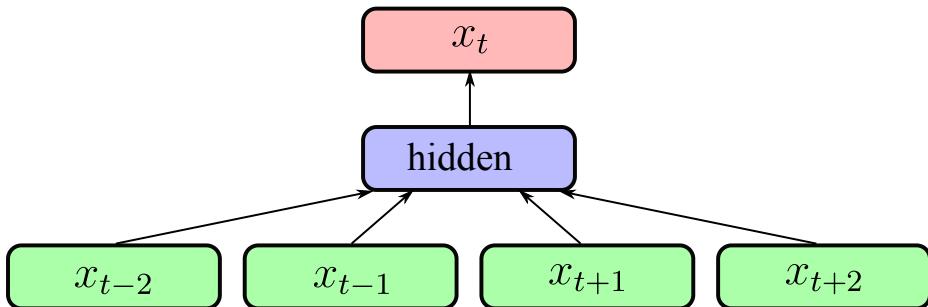
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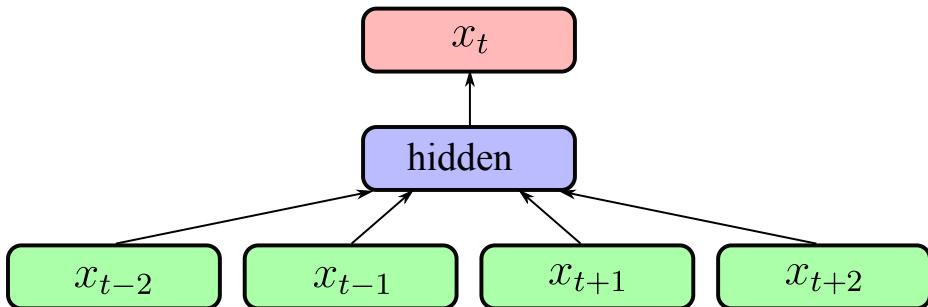
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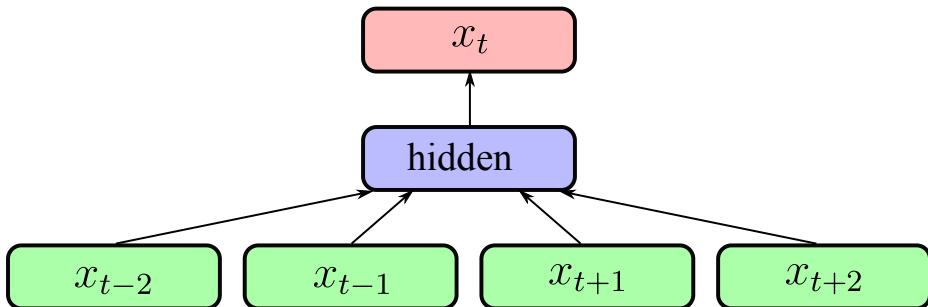


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- Use **Negative Sampling**: sample *negative* words at random instead of computing the full softmax. See:

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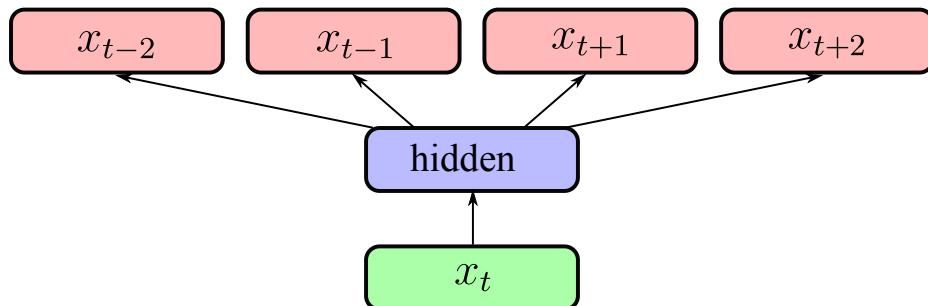
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Word2Vec: Skip Gram

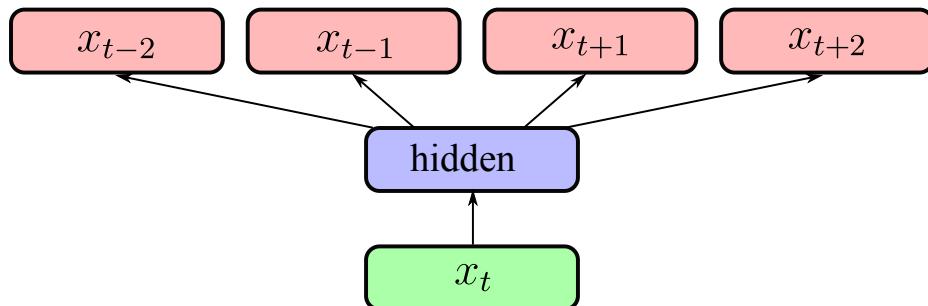
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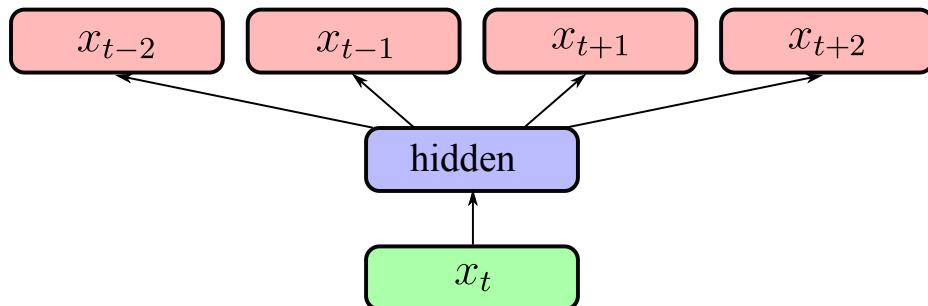
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- Widely used in practice

Word2Vec: Skip Gram

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- Widely used in practice
- Again **Negative Sampling** is used as a cheaper alternative to full softmax.

Evaluation and Related methods

Always difficult to evaluate unsupervised tasks

- WordSim (Finkelstein et al.)
- SimLex-999 (Hill et al.)
- Word Analogies (Mikolov et al.)

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Other popular method: **GloVe** (Socher et al.)

<http://nlp.stanford.edu/projects/glove/>

Pennington, Jeffrey, Richard Socher, and Christopher D. Manning. "Glove: Global Vectors for Word Representation." EMNLP. 2014

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Language Modelling and Recurrent Neural Networks

Language Models

Assign a probability to a sequence of words, such that plausible sequences have higher probabilities e.g:

- $p(\text{"I like cats"}) > p(\text{"I table cats"})$
- $p(\text{"I like cats"}) > p(\text{"like I cats"})$

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$$p_\theta(w_0)$$

p_θ is parametrized by a neural network.

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$$p_{\theta}(w_0) \cdot p_{\theta}(w_1 | w_0) \cdot \dots \cdot p_{\theta}(w_n | w_{n-1}, w_{n-2}, \dots, w_0)$$

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The internal representation of the model can better capture the meaning of a sequence than a simple Bag-of-Words.

Conditional Language Models

NLP problems expressed as **Conditional Language Models**:

Translation: $p(\text{Target} \mid \text{Source})$

- *Source*: "J'aime les chats"
- *Target*: "I like cats"

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Conditional Language Models

Question Answering / Dialogue:

$$p(\text{Answer} \mid \text{Question}, \text{Context})$$

- *Context:*
 - "John puts two glasses on the table."
 - "Bob adds two more glasses."
 - "Bob leaves the kitchen to play baseball in the garden."
- *Question:* "How many glasses are there?"
- *Answer:* "There are four glasses."

Conditional Language Models

Question Answering / Dialogue:

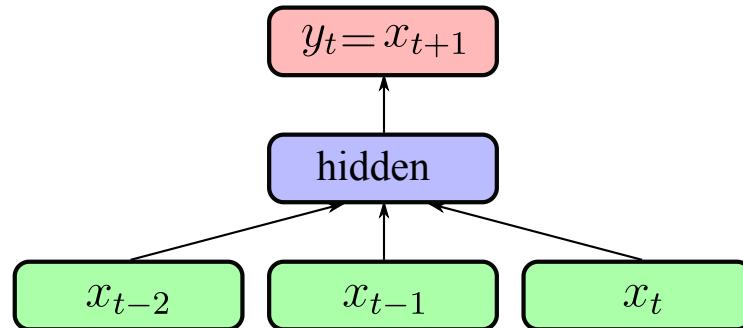
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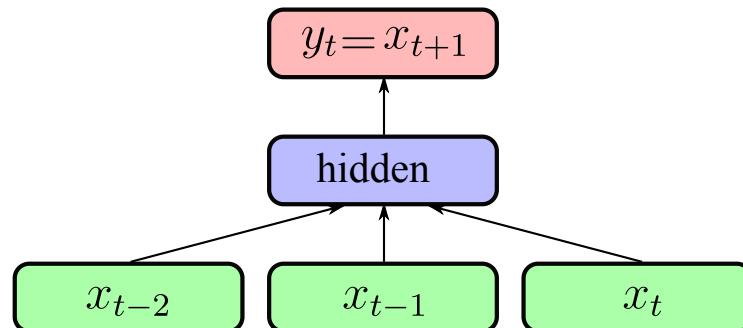
Image Captionning: $p(\text{Caption} \mid \text{Image})$

- Image is usually the 2048-d representation from a CNN

Simple Language Model



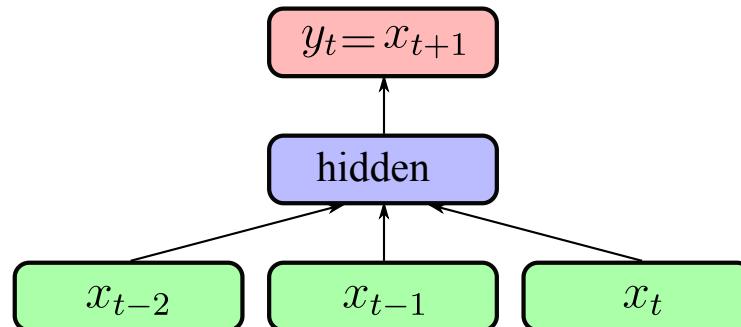
Simple Language Model



Fixed context size

- **Average embeddings:** (same as CBoW) no sequence information

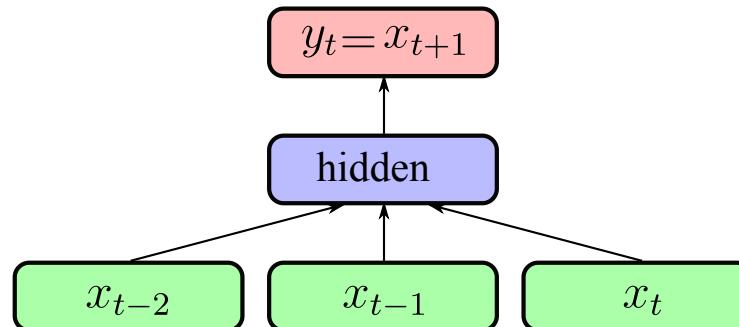
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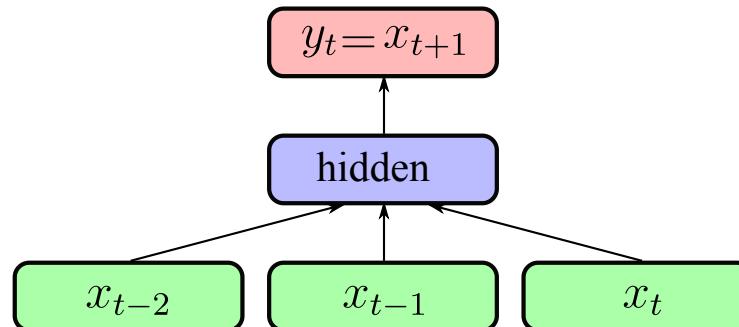
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- **1D convolution:** larger contexts and limit number of parameters

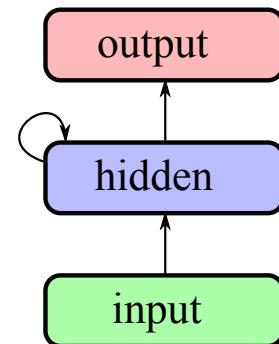
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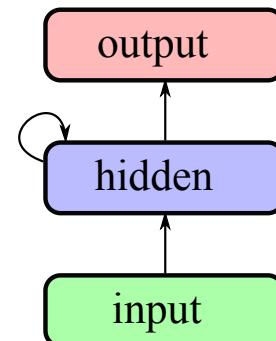
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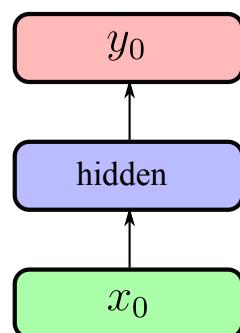
Recurrent Neural Network



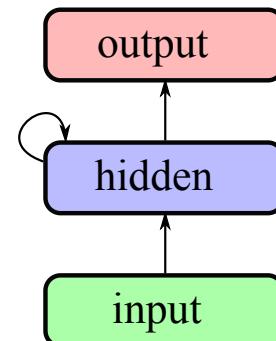
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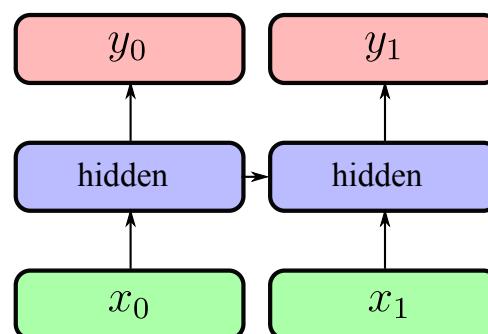
Unroll over a sequence (x_0, x_1, x_2) :



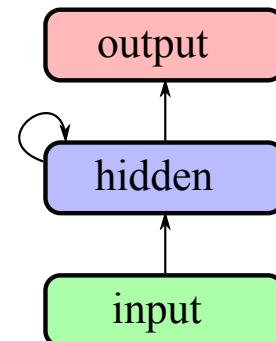
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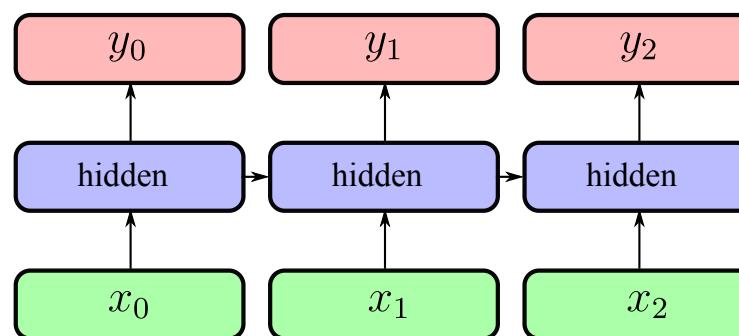
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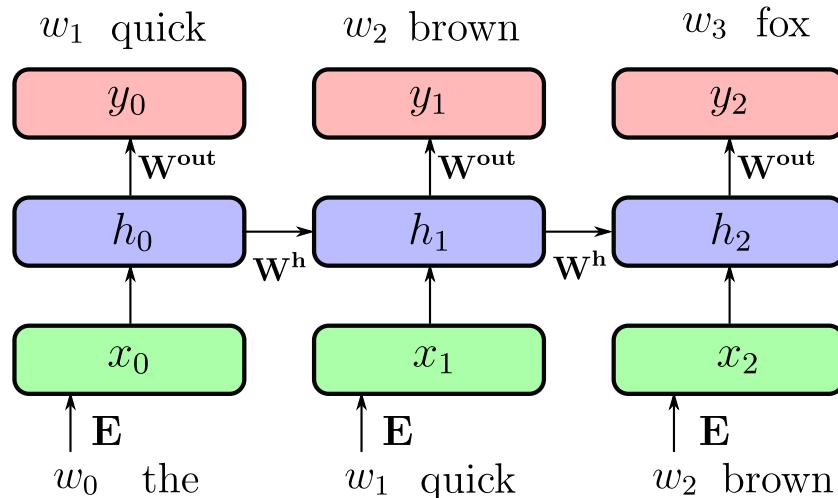
Recurrent Neural Network



Unroll over a sequence (x_0, x_1, x_2) :



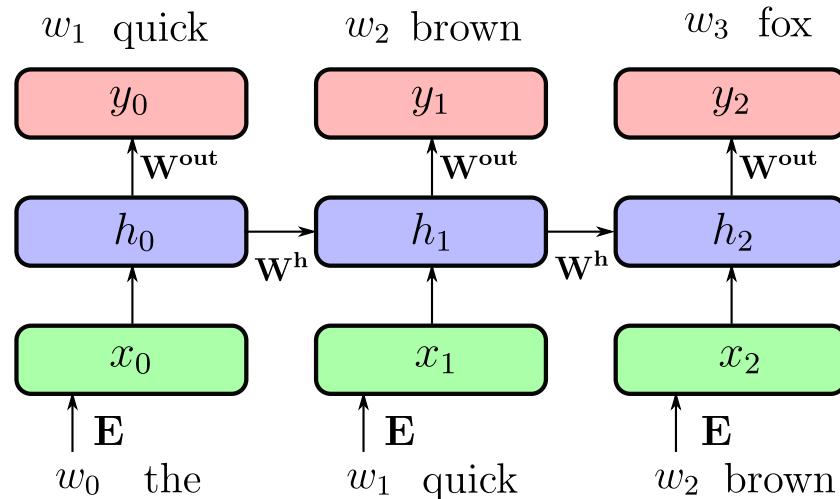
Language Modelling



input (w_0, w_1, \dots, w_t) sequence of words (1-hot encoded)

output (w_1, w_2, \dots, w_{t+1}) shifted sequence of words (1-hot encoded)

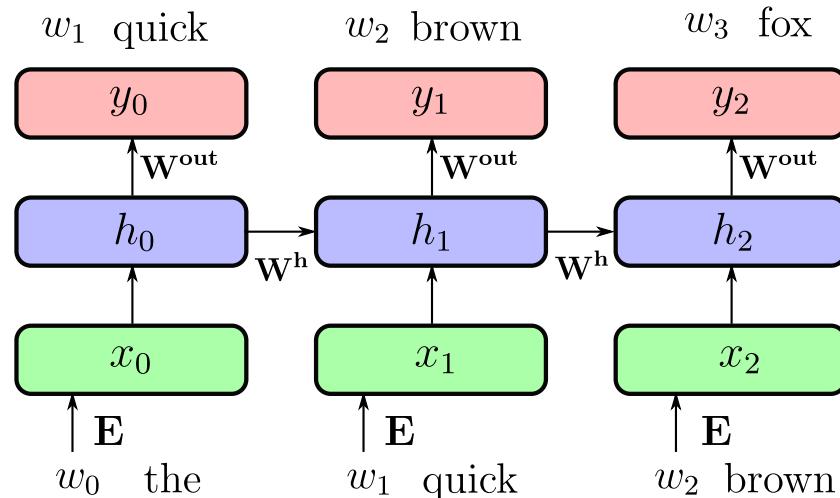
Language Modelling



$$x_t = \text{Emb}(w_t) = \mathbf{E} w_t$$

input projection \mathbf{H}

Language Modelling



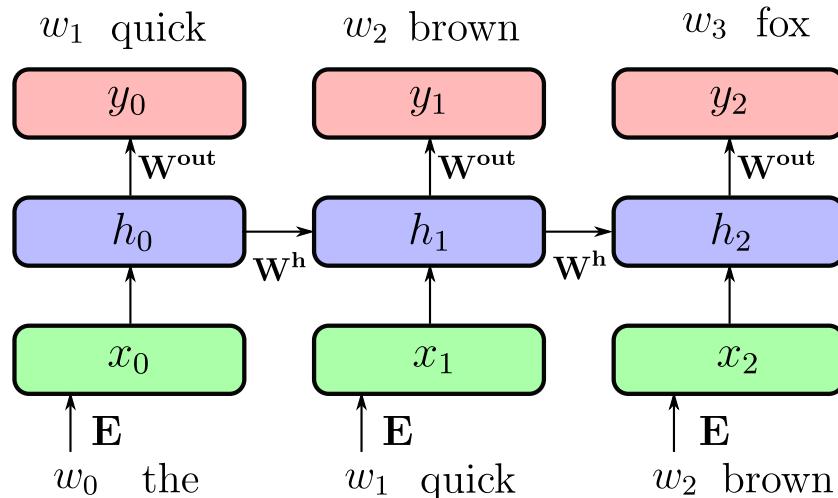
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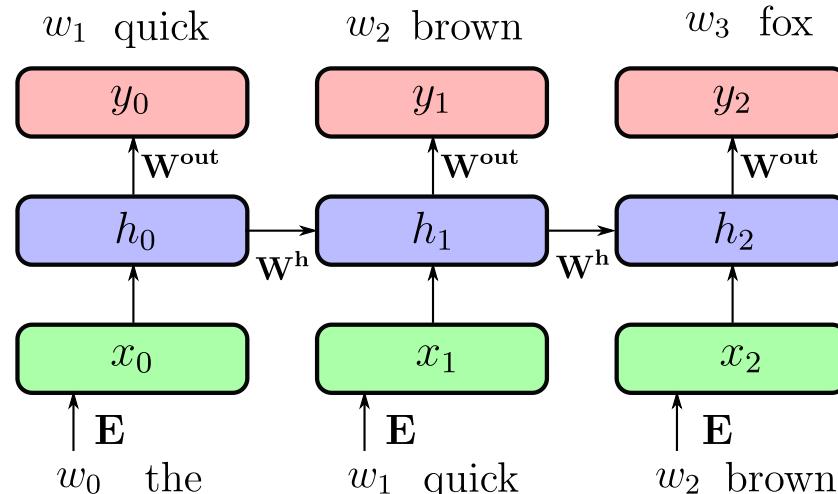
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output projection $\mathbf{K} = |\mathcal{V}|$

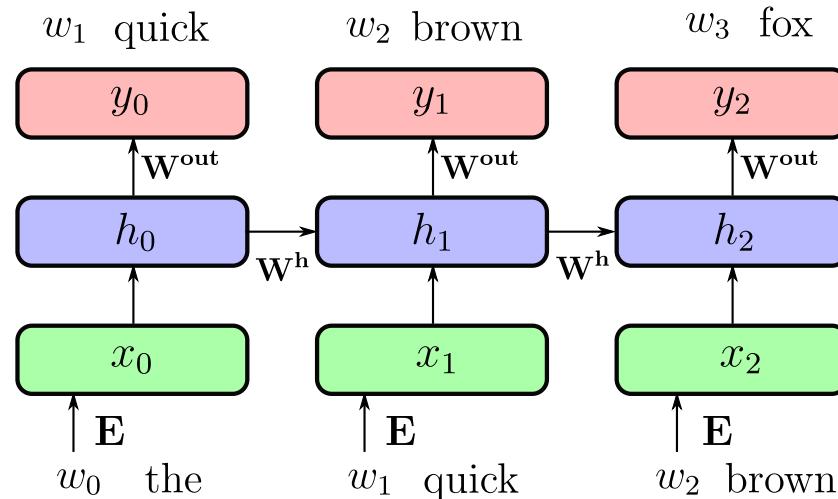
Recurrent Neural Network



Input embedding E

$|V| \times H$

Recurrent Neural Network



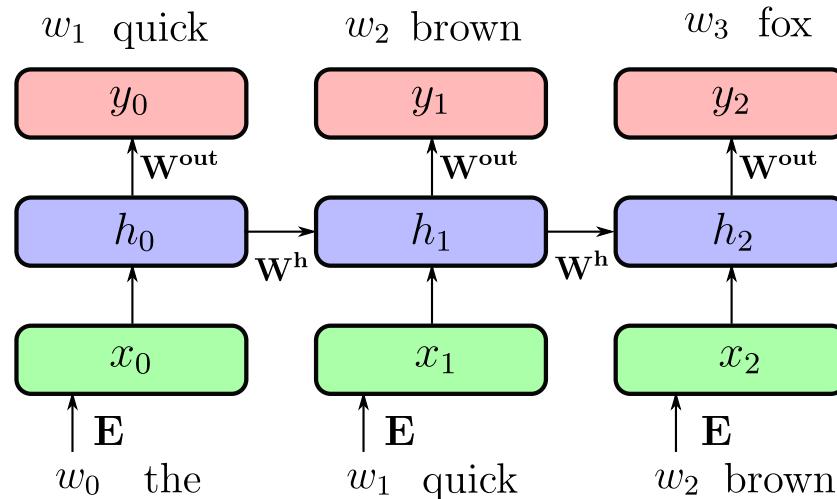
Input embedding \mathbf{E}

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Recurrent weights \mathbf{W}^h

$H \times H$

Recurrent Neural Network



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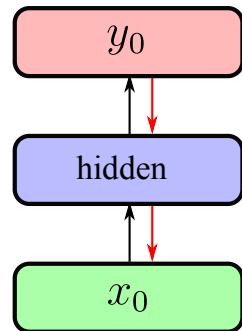
$H \times H$

Output weights \mathbf{W}^{out}

$H \times K = H \times |V|$

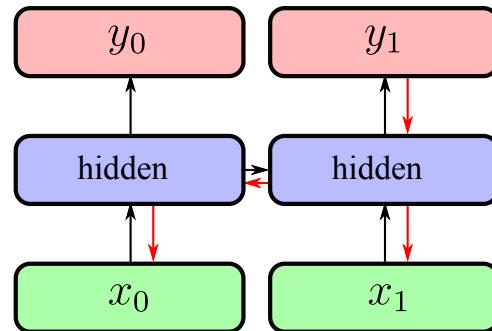
Backpropagation through time

Similar as standard backpropagation on unrolled network



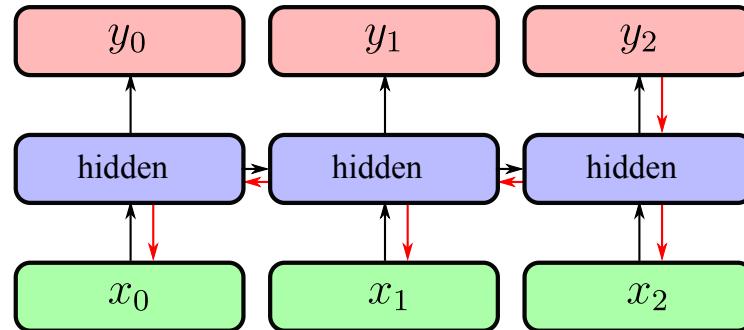
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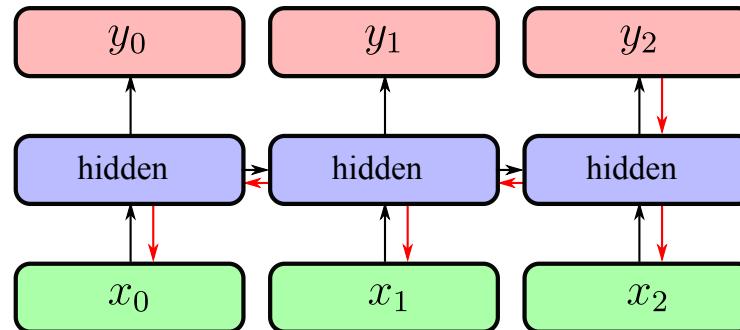
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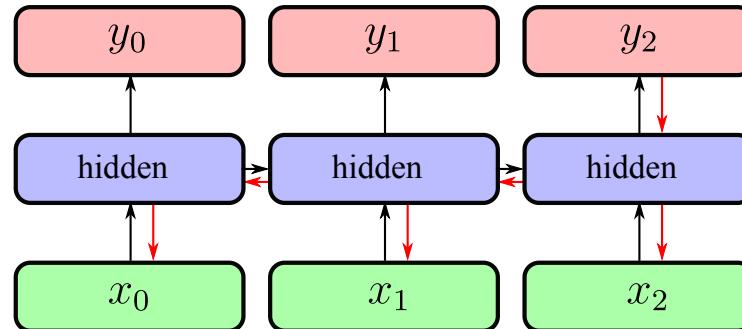
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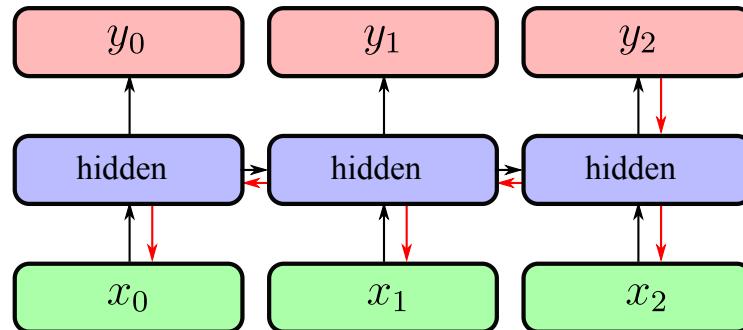
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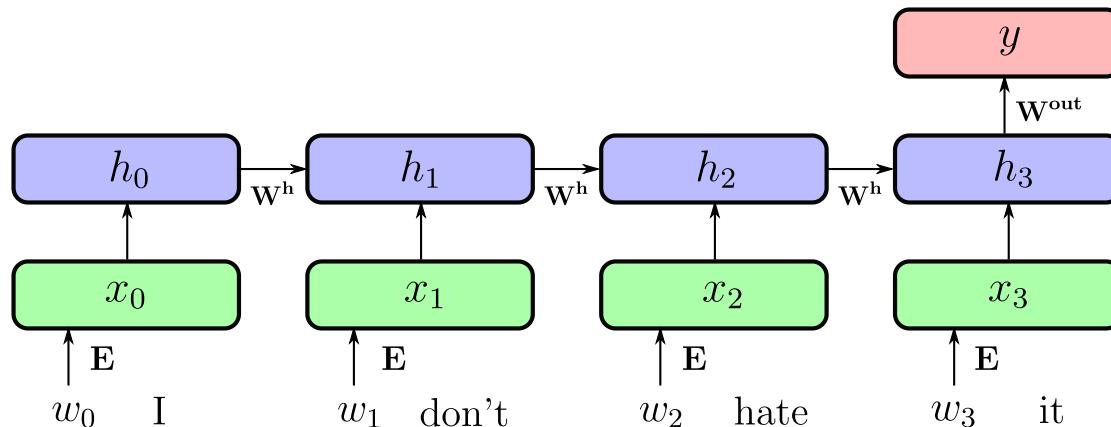
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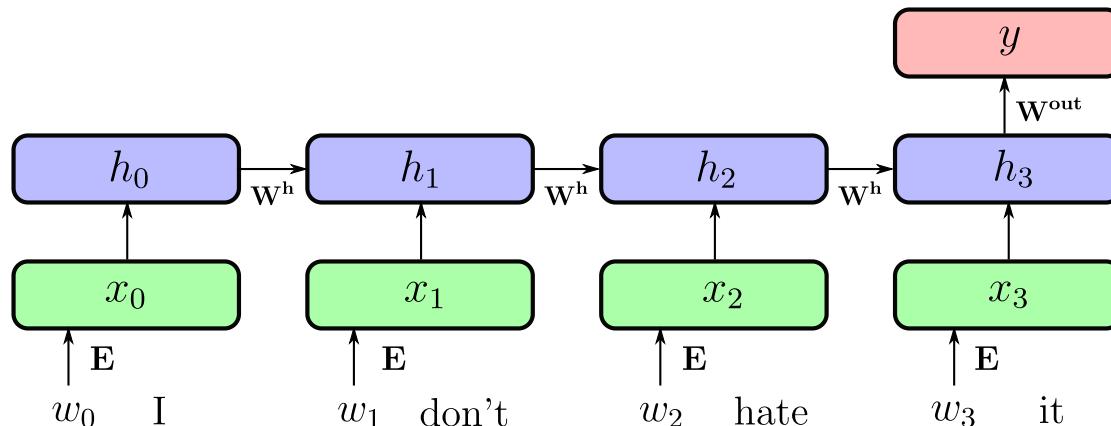
- Similar as training **very deep networks** with tied parameters
- Example between x_0 and y_2 : W^h is used twice
- Usually truncate the backprop after T timesteps
- Difficulties to train long-term dependencies

Other uses: Sentiment Analysis



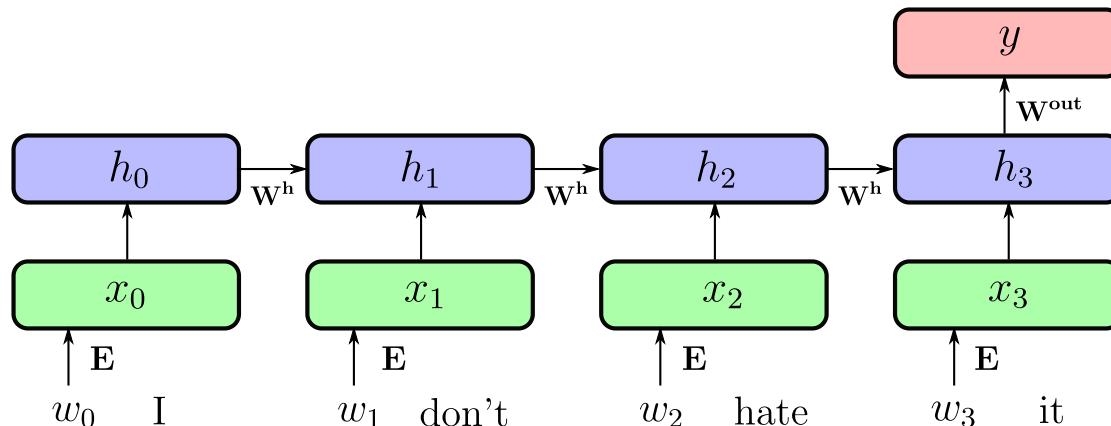
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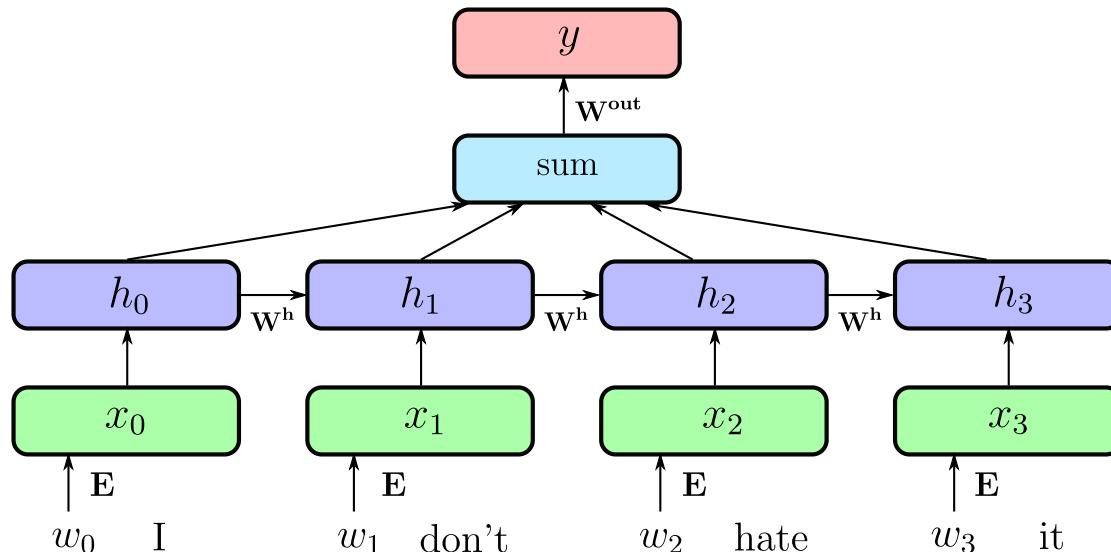
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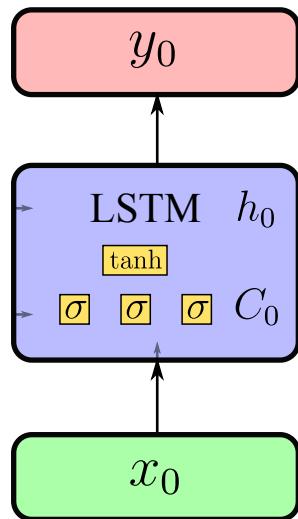
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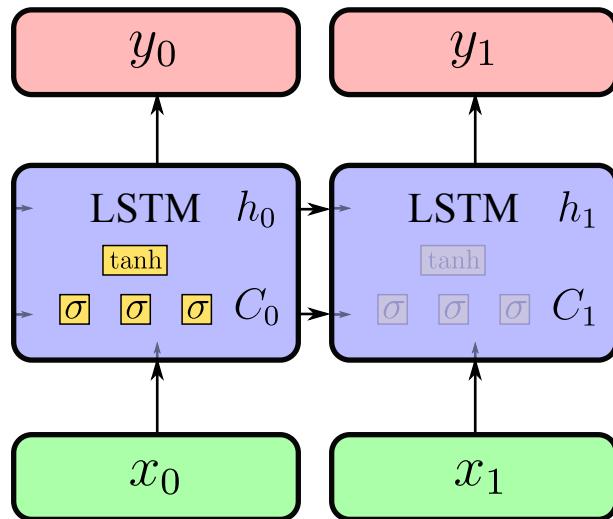
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LSTM



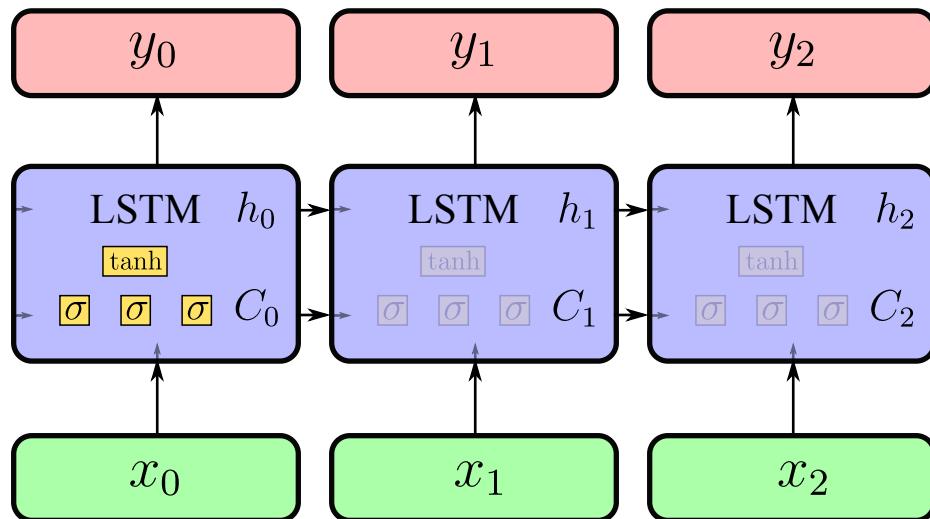
Hochreiter, Sepp, and Jürgen Schmidhuber. "Long short-term memory." Neural computation 1997

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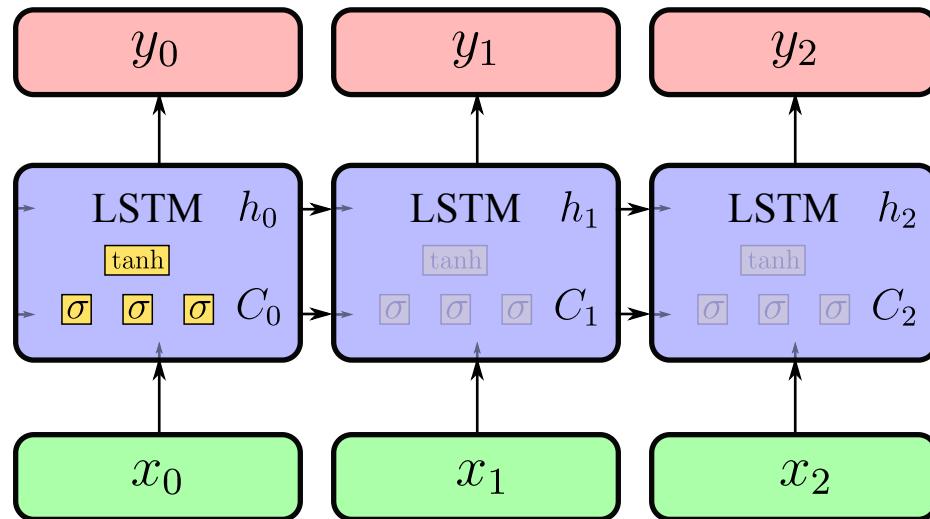
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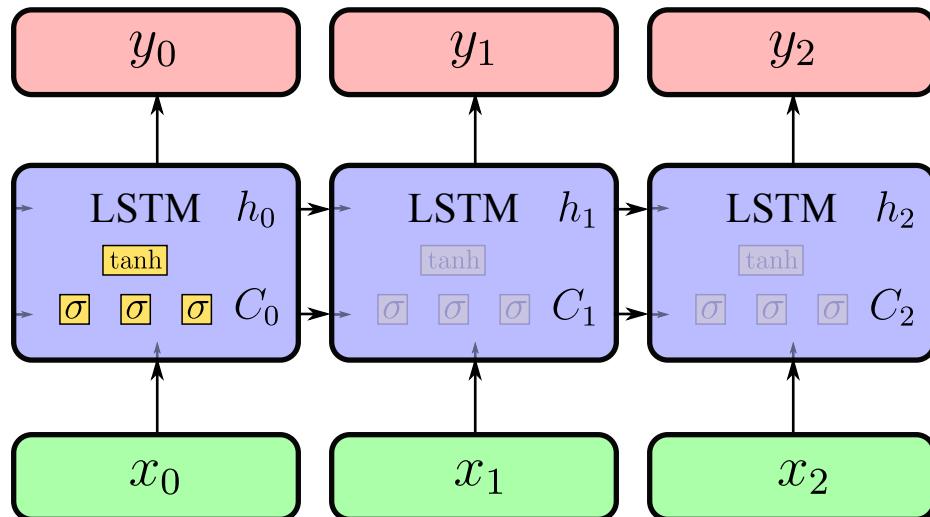
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- 4 times more parameters than RNN

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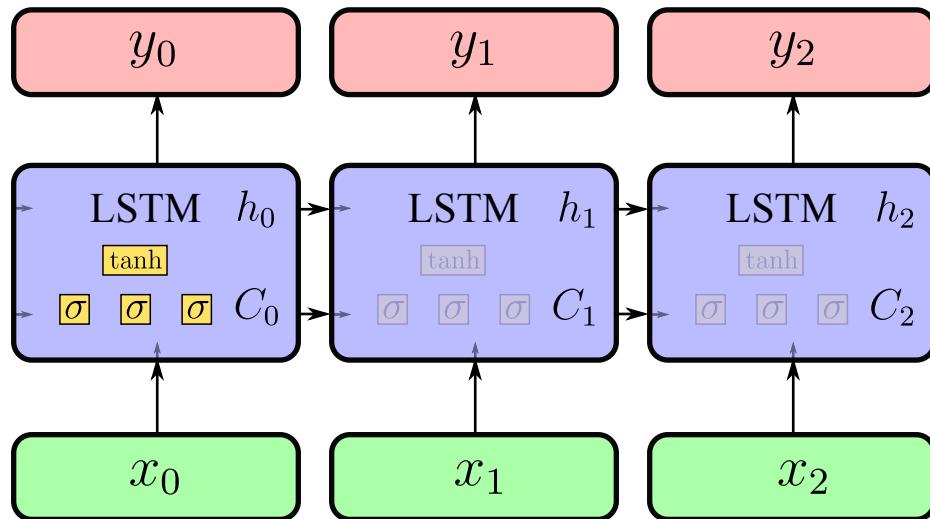
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- 4 times more parameters than RNN
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LSTM



- 4 times more parameters than RNN
- Mitigates vanishing gradient problem through gating
- Widely used and SOTA in many sequence learning problems

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Output \mathbf{K}

$$W^u, W^f, W^c, W^o$$

Recurrent weights $\mathbf{H} \times \mathbf{H}$

Hochreiter, Sepp, and Jürgen Schmidhuber. "Long short-term memory." Neural computation 1997

Input weights $\mathbf{N} \times \mathbf{H}$
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GRU

Gated Recurrent Unit: similar idea as LSTM

- less parameters, as there is one gate less
- no "cell", only hidden vector h_t is passed to next unit

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In practice

- more recent, people tend to use LSTM more
- no systematic difference between the two

Vanishing / Exploding Gradients

Passing through t time-steps, the resulting gradient is the **product** of many gradients and activations.

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Skip connections in ResNet also alleviate a similar optimization problem.

Lab 5: back here in 15 min!