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Assignment: 02

Ques-1) Linear Search Pseudocode:

```
bool linearSearch (int arr [], int key)
{
    for (i = 0; i < n; i++)
    {
        if (arr[i] == key)
            return true;
    }
    return false;
}
```

Ques-2) Pseudo code for iterative insertion sort:
ITERATIVE

```
for (int i = 1; i < n; i++)
{
    int t = arr[i];
    int j = i - 1;
    while (j >= 0 && arr[j] > t)
    {
        arr[j+1] = arr[j];
        j--;
    }
    arr[j+1] = t;
}
```


RECURSIVE :

```
void sort (arr[], int n)
{
    if (n <= 1)
        return;
    sort (arr, n-1);
    int last = arr [n-1];
    int j = n-2;
    while (j >= 0 & arr [j] > last)
    {
        arr [j+1] = arr [j];
        j = j+1;
    }
    arr [j+1] = last;
}
```

- It can sort elements while receiving new ones that's why it is called online sorting.
- Other sorting techniques like merge, Quick, selection can't do this.

Ques 3)

Sorting technique	COMPLEXITY		
	best	avg	worst
Bubble	$O(n)$	$O(n^2)$	$O(n^2)$
Selection	$O(n^2)$	$O(n^2)$	$O(n^2)$
Insertion	$O(n)$	$O(n^2)$	$O(n^2)$
Count	$O(n+k)$	$O(n+k)$	$O(n+k)$
Quick	$O(n \log n)$	$O(n \log n)$	$O(n^2)$
Merge	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
heap	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Radix	$O(d \cdot (n+k))$	$O(d \cdot (n+k))$	$O(d \cdot (n+k))$

Ques 4)	Sorting Techniques	Inplace	Stable	Online
	Bubble	Yes	Yes	No
	Selection	Yes	No	No
	Insertion	Yes	Yes	Yes
	Count	No	Yes	No
	Quick	Yes	No	No
	Merge	No	Yes	No
	Heap	Yes	No	No
	Radix	No	Yes	No

Ques 5) Recursive Binary Search:

```

int BinSearch ( int arr[], int target, int l, int h )
{
    if ( l > h ) {
        return -1; // element not found
    }
    mid = (l + h) / 2;
    if ( arr[mid] == target ) {
        return mid;
    }
    if ( target < arr[mid] ) {
        return binsearch ( arr, l, mid-1, target );
    }
    else {
        return binsearch ( arr, mid+1, h, target );
    }
}

```

Iterative binary Search:

```

int binSearch ( int arr[], int target )
{
    low = 0;
    high = length ( arr ) - 1;
    while ( low <= high )
    {
        mid = low + (high - low) / 2;
        if ( arr[mid] == target ) {
            return mid;
        }
        else if ( arr[mid] < target ) {
            low = mid + 1;
        }
        else {
            high = mid - 1;
        }
    }
}

```



```

        high = mid - 1;
    }
    return -1;
}

```

Ques-6 Dividing the array until target element is found or the array search is resulted in out of bound

1. Calling the fnc with parameter arr as sorted array target as element to search and low, high as starting and ending point of search search.
2. base case if $low > high$ that is target not found
3. Otherwise
 - mid will be ~~call~~ calculated.
 - and check if arr's mid == target
target found at mid which is returned.
 - and if arr's mid < target
high is set to mid - 1 ~~is return~~
 - and if arr's mid > target.
low = mid + 1

pseudo code

```

fnc binsearch (arr, low, high, target) {
    if (low > high)
        return -1
    mid = (low + high) / 2
    if (arr[mid] == target)
        return mid;
}

```



```

else if (arr[mid] > target);
    high = mid - 1;
    return binSearch(arr, low, mid - 1, target);
else
    return binSearch(arr, mid + 1, high, target);
}

```

Ques-7)

```

int findPairSumK (arr, k) {
    sort(arr);
    int left = 0;
    int right = length(arr) - 1;
    while (left < right) {
        if (arr[left] + arr[right] == k)
            return 1 // found
        else if (arr[left] + arr[right] < k)
            left = left + 1;
        else
            right = right - 1;
    }
    return -1 // not found.
}

```


Ques 8). Quick Sort - fastest sorting algo especially for large dataset.

- Merge sort / Heap sort for moderate dataset
- Insertion or Selection Sort for small dataset
- Insertion sort for nearly sorted data.

Ques 9)

Inversion: When smaller element is after larger element if the sorting is ~~not~~ ought to be in ascending order or vice versa for descending order.

{ 7, 21, 31, 8, 10, 1, 20, 6, 4, 5 }

$$n = 10 \gg \text{mid} = \frac{10}{2} = 5$$

{ 7, 21, 31, 8, 10, 1, 20, 6, 4, 5 }

{ 7, 21, 31, 8, 10 } { 1, 20, 6, 4, 5 }

{ 7, 21 } { 31, 8, 10 } { 1, 20 } { 6, 4, 5 }

{ 7 } { 21 } { 31 } { 8, 10 } { 1 } { 20 } { 6 } { 4, 5 }

{ 8 } { 10 }

{ 4 } { 5 }

$\{7\} \{21\} \{31\} \{8\} \{10\} \{1\} \{20\} \{6\} \{4\} \{5\}$
 $\{7, 21\} \{8, 31\} \{1, 10\} \{6, 20\} \{4, 5\}$
 $\{7, 8, 21, 31\} \{1, 6, 10, 20\}$
 $\{7, 21\} \{8, 31\} \{10\} \{1, 20\} \{4, 6\} \{5\}$
 $\{7, 8, 21, 31\} \{10\} \{1, 4, 6, 20\} \{5\}$
 $\{7, 8, 10, 21, 31\} \{1, 4, 5, 6, 20\}$
 $\{1, 4, 5, 6, 7, 8, 10, 20, 21, 31\}$

$$\begin{aligned}
 \text{No. of inversion: } & \underline{5+5+5+5} + 2 + 1 + 1 + 1 + 1 + 1 \\
 & + 1 + 1 + 1 + 1 \\
 & = 31
 \end{aligned}$$

Ques to) Best case: When pivot divides array in equal halves.

Worst case: When pivot divides array in highly imbalanced way.

Merge sort:

best case: $T(n) = 2T(n/2) + O(n)$

Worst case $T(n) = 2T(n/2) + O(n)$

Quick Sort

best case $T(n) = T(n/2) + T(n/2) + O(n)$

Worst case $T(n) = T(n-1) + O(n)$

Similarities:

both have divide and conquer
 $TC = O(n \log n)$

Difference In Quick Sort TC varies.

Ques-12) void selectionSort(arr, n) {
 for (i = 0; i < n; i++)
 {
 int min = i;
 for (j = i+1; j < n; j++) {
 if (arr[j] < arr[min])
 min = j;
 }
 minValue = arr[min];
 }


```

while (min > i)
{
    arr[min] = arr[min-1];
    min = min-1;
}
arr[i] = minvalue;
}
}

```

Ques-13)

```

void sort (arr, n) {
    bool swapped;
    for (int i = 0; i < n-1; i++) {
        swapped = false;
        for (int j = 0; j < n-1; j++) {
            if (arr[j] > arr[j+1])
            {
                swap (arr[j], arr[j+1]);
                swapped = true;
            }
        }
        if (!swapped)
            break;
    }
}

```


- Ques 14). Merge sort optimized for external sorting
- Divide and conquer approach.
 - Requires small portion of data to fit memory.

External Sorting

Internal Sorting

On virtual memory

On RAM.

Eg: Quick, merge
Sort

Eg: bubble, selection,
inserting sort.