

## Data Structure:

- Structure of Data
  - The organization of data in memory.
  - Operations performed on that data.
- Types of data structures:
  - Linear - Array, Stack, Queue, Linked List.
  - Non-Linear - Tree, Graph
  - Associative:- data is stored in key value pair e.g. HashTable
- Usually data structures are represented as "Abstract Data Types".
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- Example Data Structures:
  - Array, Stack, Queue, Linked List, Tree, Graph, Hashtable, etc.

## Time Complexity:

- Approximate measure of time required for completing any algo/operation.
- Example: Factorial:

```
res = 1;

for(i=1; i<= num; i++)
    res = res * i;

printf("factorial : %d\n", res);
```

- Time complexity of any algorithms depends on number of iterations in that algorithms .
- In above program, time is proportional to number whose factorial is to be calculated.
- $T \propto n$  . Hence time complexity is  $O(n)$  -> Order of  $n$ .
- If time required for any algo is constant (not dependent on any factor)  
i.e.  $T = k$ . Then time complexity is represented as  $O(1)$ .
- Time complexity is represented in "Big O" notation.

## Selection Sort:

```
for(i=0; i<n-1; i++)
{
    for(j=i+1; j<n; j++)
    {
        if(a[i] > a[j])
            SWAP(a[i], a[j]);    // macro
    }
}
```

- Number of iterations =  $1 + 2 + 3 + \dots + n-1 = n(n-1) / 2$
- $T \propto n(n-1) / 2$
- $T \propto n^2 - n$
- If  $n \gg 1$ , then  $n^2 \gg n \Rightarrow$  Hence all lower order terms can be ignored.
- $T \propto n^2$
- Time complexity =  $O(n^2)$

## Bubble Sort:

```
for(i=0; i<n-1; i++)
{
    for(j=0; j<n-1; j++)
    {
        if(a[j] > a[j+1])
            swap(a[j], a[j+1]);    // macro
    }
}
```

- Number of iterations =  $(n-1)(n-1)$
- $T \propto n^2 - 2n + 1$
- If  $n \gg 1$ , then  $n^2 \gg n \Rightarrow$  Hence all lower order terms can be ignored.
- $T \propto n^2$
- Time complexity =  $O(n^2)$

## Linear Search:

```
for(i=0; i<n; i++)
{
    if(key==a[i])
        return i; // element found at index i
}
return -1; // ele not found
```

- Best case : "key" is found at index 0.
  - o Number of iterations = 1
  - o  $T = k$
  - o  $O(1)$
- Worst case : "key" is found at last index (n-1).
  - o Number of iterations = n
  - o  $T \propto n$
  - o  $O(n)$
- Average case : "key" is found in middle.
  - o Number of iterations (average) =  $n / 2$
  - o  $T \propto n / 2$
  - o  $T \propto n$
  - o  $O(n)$

## Binary Search:

- 1 start
2. accept Arr (asc sorted) ,Accept Key(element to search)
3. assign size =10 left=0, right=size-1
4. check left<=right
  - if yes
    - mid=(left+right)/2
    - check(key==arr[mid])
      - if yes
        - return mid
      - check (key>arr[mid])
        - if yes
          - left=mid+1
        - check (key<arr[mid])
          - if yes
            - right=mid-1
      - go to 4
    - 5 if not
      - return -1
    - 6. stop

---

```

while(left <= right)
{
    mid = (left+right) / 2;
    if(key == arr[mid])
        return mid; // element found at index "mid"
    if(key < arr[mid])
        right = mid - 1;
    else
        left = mid + 1;
}
return -1;

```

- Array must be sorted to use binary search.
- $2^i = n$       -> where 'n' is number of elements, 'i' is number of iterations
- $i \log 2 = \log n$
- $i = \log n / \log 2$
- $T \propto \log n / \log 2$
- $T \propto \log n$
- Time complexity :  $O(\log n)$

### **Most common time complexities:**

- $O(1)$
- $O(\log n)$
- $O(n)$
- $O(n \log n)$
- $O(n^2)$

### **Recursion:**

- Function calling itself is called as "recursive function".
- From programming perspective two things are important:
  - o Explain process in terms of itself.
  - o Terminating condition.
- Advantages:
  - o Simplifies / reduce the code.
- Disadvantages:
  - o Increased space complexity (function activation records are created per call).
  - o Increased time (time required to create activation record and call the function).