```
In [1]:
         import matplotlib.pyplot as plt
         import numpy as np
         from qiskit import IBMQ, QuantumCircuit, Aer, transpile, assemble
         from qiskit.visualization import plot_histogram
         from math import gcd
         from numpy.random import randint
         import pandas as pd
         from qiskit.providers.ibmq import least_busy
         from fractions import Fraction
In [2]:
         def qft_inv(n):
             qc = QuantumCircuit(n)
             for qubit in range(n//2):
                  qc.swap(qubit, n-qubit-1)
             for j in range(n):
                 for m in range(j):
                      qc.cp(-np.pi/float(2**(j-m)), m, j)
                  qc.h(j)
             qc.name = "QFT_INV"
             return qc
In [3]:
         n count = 3
         n = 5
         qc = QuantumCircuit(n_count+2, n_count)
         for q in range(n_count):
             qc.h(q)
         qc.cx(2,4)
         qc.cx(1,4)
         qc.cx(4,3)
         qc.ccx(1,3,4)
         qc.cx(4,3)
         qc.x(4)
         qc.cswap(3,0,4)
         qc.x(4)
         qc.cx(4,3)
         qc.ccx(0,3,4)
         qc.cx(4,3)
         qc.barrier()
         qc.append(qft_inv(n_count), range(n_count))
         qc.measure(range(n_count), range(n_count))
         qc.draw()
Out[3]: q_0:
                Η
                                                                                        0
                Н
        q 1:
                                                                                        1 Q1
        q 2:
                Η
                                                                                        2
                                  Χ
                                              Χ
                                                                    Χ
        q 3:
                                                                                Χ
                            Χ
                                        Χ
                                                    Χ
        q 4:
        c: 3/=
        «q 0: - M
```

```
aer_sim = Aer.get_backend('aer_simulator')
t_qc = transpile(qc, aer_sim)
qobj = assemble(t_qc)
results = aer_sim.run(qobj).result()
counts = results.get_counts()
plot_histogram(counts)
```

```
Out[4]:
                 0.4
                          0.357
                 0.3
             Probabilities
                                     0.191
                 0.2
                                                                                                0.176
                 0.1
                                                                            0.074
                                                                                      0.062
                                              0.057
                                                        0.057
                                                                   0.026
                 0.0
                                               070
                                     907
                                                                    200
                                                                             707
```

least busy backend: ibmq_manila
<ipython-input-5-5f8f17d7194d>:13: DeprecationWarning: Passing a Qobj to Backend.run
is deprecated and will be removed in a future release. Please pass in circuits or pu
lse schedules instead.
 job = backend.run(qobj)

Job Status: job has successfully run

```
In [6]: # Get results and plot counts
    device_counts = job.result().get_counts()
    plot_histogram(device_counts)
```

```
Out[6]:
                           0.197
                0.20
                                                                                             0.150
            Probabilities
                0.15
                                              0.129
                                    0.128
                                                                                   0.120
                                                       0.105
                0.10
                                                                 0.087
                                                                          0.083
                0.05
                0.00
                                                                 700
                                     907
                                                        077
                                                                           707
```

```
Register Output
                              Phase
  101(bin) =
                5(dec)
                        5/8 = 0.62
1
  111(bin) =
                7(dec)
                        7/8 = 0.88
  000(bin) =
                0(dec)
                        0/8 = 0.00
3
  011(bin) =
                3(dec)
                        3/8 = 0.38
  001(bin) =
                1(dec)
                        1/8 = 0.12
                        6/8 = 0.75
  110(bin) =
                6(dec)
                        2/8 = 0.25
  010(bin) =
                2(dec)
  100(bin) =
                4(dec)
                        4/8 = 0.50
```

```
rows = []
for phase in measured_phases:
    frac = Fraction(phase).limit_denominator(15)
    rows.append([phase, f"{frac.numerator}/{frac.denominator}", frac.denominator])
# Print as a table
headers=["Phase", "Fraction", "Guess for r"]
df = pd.DataFrame(rows, columns=headers)
print(df)
```

```
Phase Fraction Guess for r
a
  0.625
              5/8
                              8
1 0.875
              7/8
                              8
  0.000
2
              0/1
                              1
3
  0.375
              3/8
                              8
4
  0.125
                              8
              1/8
5
  0.750
                              4
              3/4
```

```
7 0.500
                       1/2
 In [9]:
          rows, measured_phases = [], []
          for output in device_counts:
              decimal = int(output, 2) # Convert (base 2) string to decimal
              phase = decimal/(2**n_count) # Find corresponding eigenvalue
              measured_phases.append(phase)
              # Add these values to the rows in our table:
              rows.append([f"{output}(bin) = {decimal:>3}(dec)",
                           f"{decimal}/{2**n count} = {phase:.2f}"])
          # Print the rows in a table
          headers=["Register Output", "Phase"]
          df = pd.DataFrame(rows, columns=headers)
          print(df)
                Register Output
                                      Phase
         0 000(bin) =
                         0(dec) 0/8 = 0.00
         1 \ 001(bin) =
                         1(dec) 1/8 = 0.12
         2 010(bin) =
                         2(dec) 2/8 = 0.25
         3 011(bin) =
                         3(dec) 3/8 = 0.38
         4 100(bin) =
                         4(dec)
                                4/8 = 0.50
         5 101(bin) =
                         5(dec) 5/8 = 0.62
                         6(dec) 6/8 = 0.75
         6 110(bin) =
         7 111(bin) =
                         7(dec) 7/8 = 0.88
In [10]:
          rows = []
          for phase in measured_phases:
              frac = Fraction(phase).limit_denominator(15)
              rows.append([phase, f"{frac.numerator}/{frac.denominator}", frac.denominator])
          # Print as a table
          headers=["Phase", "Fraction", "Guess for r"]
          df = pd.DataFrame(rows, columns=headers)
          print(df)
            Phase Fraction Guess for r
           0.000
                       0/1
                                      1
         1 0.125
                       1/8
                                      8
         2 0.250
                       1/4
                                      4
         3 0.375
                       3/8
                                      8
         4 0.500
                       1/2
                                      2
         5 0.625
                       5/8
                                      8
         6 0.750
                       3/4
                                      4
         7 0.875
                       7/8
                                      8
In [ ]:
```

1/4

6 0.250