Integrated Combinational Circuits As Building Blocks

In combinational logic design, there are several common structures (such as adders, multiplexers, decoders) that are used regularly as building blocks in larger systems.

Instead of designing every complex function with basic logic gates, using these common structures makes the design simpler.

Their level of functionality often matches a designer's level of thinking when partitioning the large problem into smaller chunks. (As functions in programming.)

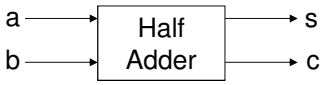
These structures are manufactured and sold as integrated circuits (ICs).

Generations of ICs according to integration scale factors:

- Small-Scale Integration (**SSI**): These digital circuits contain transistors numbering in the tens and provide a few logic gates.
- Medium-Scale Integration (**MSI**): They contain hundreds (up to 1000) of transistors. Adders, decoders.
- Large-Scale Integration (**LSI**): Tens of thousands of transistors per chip. First memory and microprocessor chips
- Very Large-Scale Integration (**VLSI**): Hundreds of thousands of transistors in the early 1980s, and continues beyond several billion transistors as of 2009.
- Ultra-large-scale integration (**ULSI**): More than 1 million transistors.

Half Adder:

It adds two 1-bit numbers (without carry input).



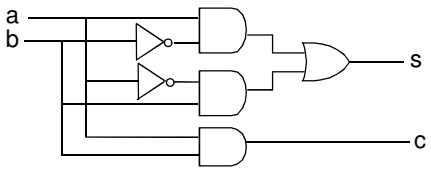
a: First number
b: Second number
s: Result
c: Carry output

Truth table:

a	b	c	s
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

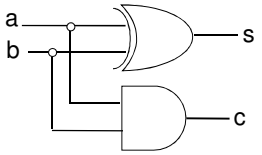
From the truth table the logical expression is obtained.

s= ab' + a'b
c= ab



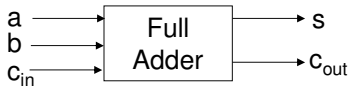
The circuit can also be implemented with XOR gates.

s= a ⊕ b
c= ab



Full Adder:

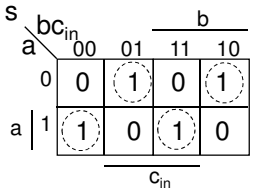
It adds two 1-bit numbers with a carry input.



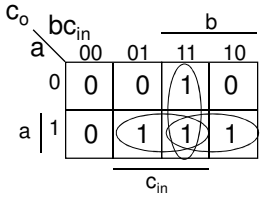
a : First number
b : Second number
c_{in}: Carry Input
s : Result
c_{out}: Carry Output

Truth table:

a	b	c_{in}	c_{out}	s
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1



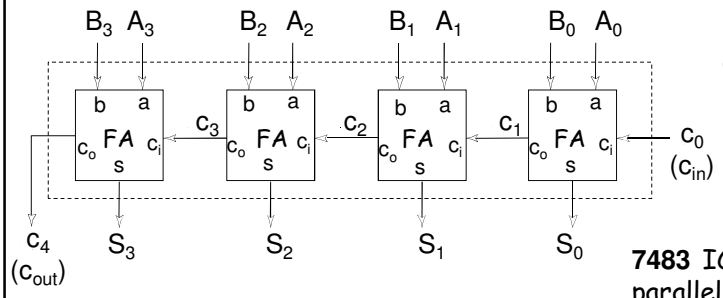
$s = a'b'c_{in} + a'bc_{in}' + ab'c_{in}' + abc_{in}$
$s = a \oplus (b \oplus c_{in})$
$s = a \oplus b \oplus c_{in}$

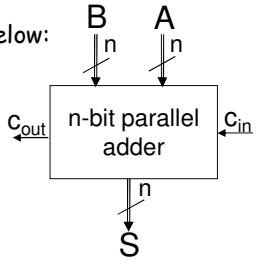


$c_{out} = ac_{in} + bc_{in} + ab$

n-Bit Binary Parallel Adder:

It adds two n-bit binary numbers.
Depending on the size of the numbers, 1-bit full adders (FA) can be connected to implement binary parallel adders.
Internal structure of a 4-bit binary parallel adder is shown below:

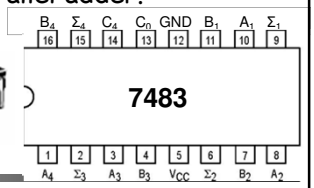




1. Number: $A_3A_2A_1A_0$
2.Number: $B_3B_2B_1B_0$
Result : $S_3S_2S_1S_0$
Carry In : c_0
Carry Out: c_4

Example:
1. Num.: 0110
2.Num.: 1100
Result : 0010
Carry : 1

7483 IC is a 4-bit binary parallel adder.



Subtraction Circuit

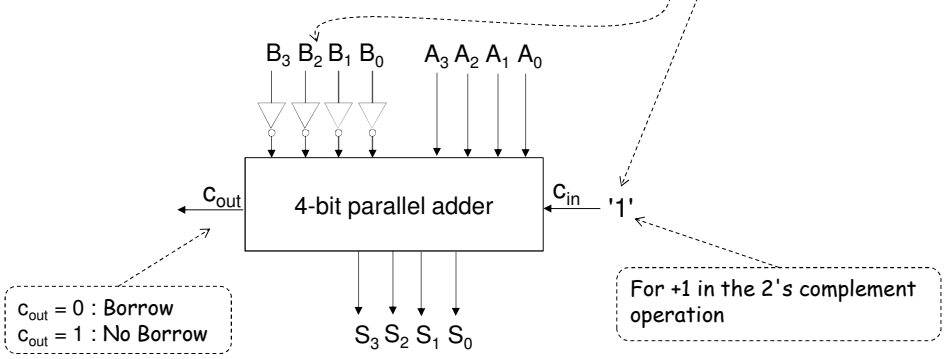
Subtraction is accomplished as "addition using 2's complement".
A subtraction circuit can be implemented with an n-bit adder and NOT gates.

Example: A 4-bit subtraction circuit

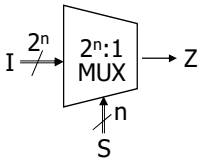
$S = A - B$

2's complement of B is added to A.

$S = A - B = A + \text{2's complement}(B) = A + (B'+1)$

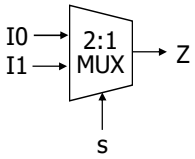


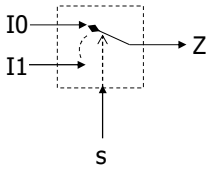
Multiplexer (MUX) (Data Selector):



- 2^n data inputs (I), n selector (control) inputs (S), 1 data output (Z).
- The control inputs are used to select one of the data inputs and connect it to the output terminal.
- Select lines are used to select which one of the 2^n input line is sent to the output.
- Multiplexers are named according to the number of data inputs as m:1. Here m is the number of data inputs.

Example: 2:1 Multiplexer (Read as "2 to 1 multiplexer".)





Function Table:

s	Z
0	I_0
1	I_1

Logical Expression:

$Z = s' I_0 + s I_1$

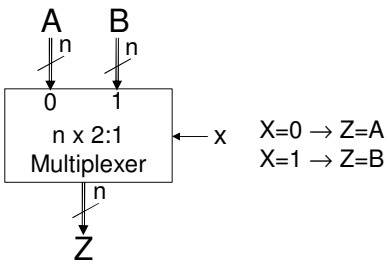
Truth Table:

I_1	I_0	s	Z
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

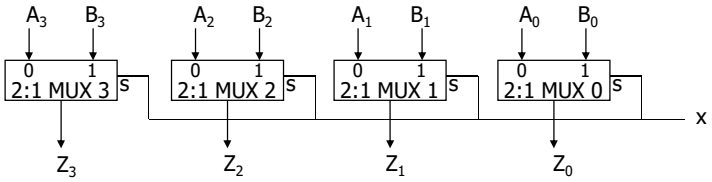
Parallel connection of multiplexers:

To select one of two n-bit data words, n units of 2:1 multiplexers have to be connected in parallel.

The circuit with the block diagram given on the right side, forwards one of the n-bit numbers (A or B) to the output Z according to the selector line x.



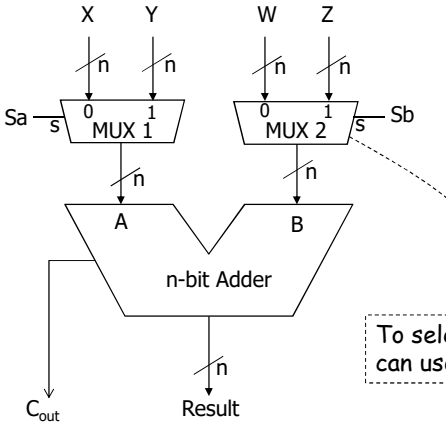
Example: A circuit that forwards one of the 4-bit numbers A or B to the output Z.



In this circuit, selector lines of all multiplexers are connected (short circuit).

Examples of Usage of Multiplexers:

Example 1:
The same adder circuit can be used to add different numbers from different sources.

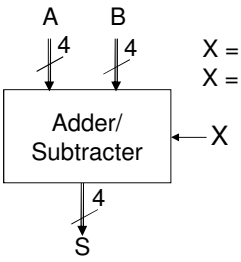


Sa	Sb	Result
0	0	X+W
0	1	X+Z
1	0	Y+W
1	1	Y+Z

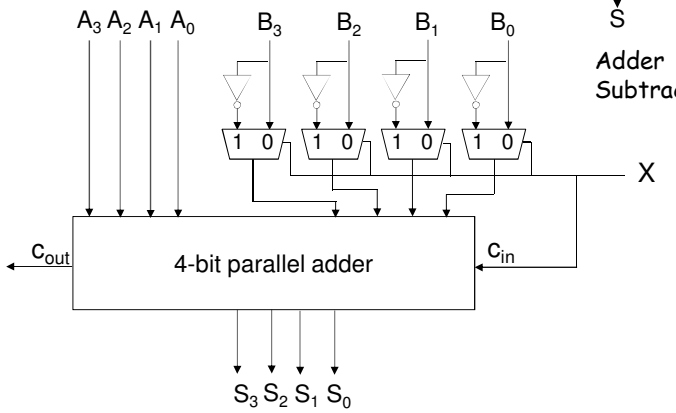
To select one of two n-bit numbers, we can use n x 2:1 multiplexers

Example 2:
4-bit Adder/Subtracter

Input X is used to control the function of the circuit.
If X is zero, it is an adder.
If X is one, it is an subtracter.



X = 0 → S = A +B
X = 1 → S = A - B



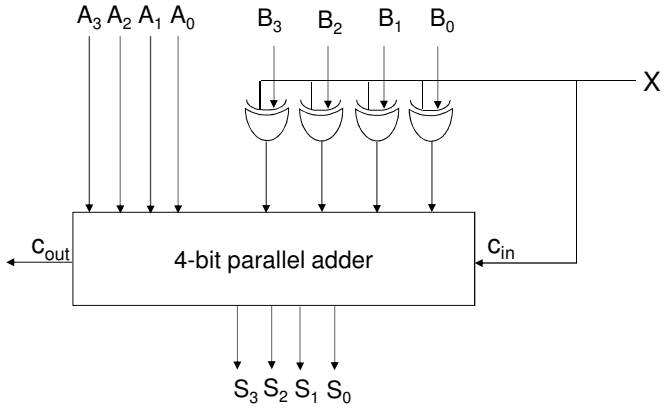
Adder : $S = A + B$
Subtracter: $S = A + (\bar{B} + 1)$

X = 0 → S = A + B
X = 1 → S = A - B

Example 2: (cont'd)
4-bit Adder/Subtracter

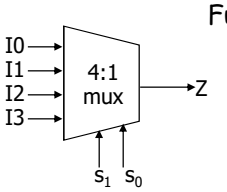
We can also design the adder/subtracter circuit using XOR gates instead of multiplexers and NOT gates.

Remember; if one input of an XOR gate is 0, it functions as a buffer. $0 \oplus x = x$
if one input of an XOR gate is 1, it functions as an inverter. $1 \oplus x = \bar{x}$



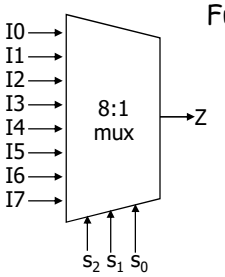
X=0 → S = A + B
X=1 → S = A - B

Multiplexers (MUX) of different sizes:



Function Table:

$s_1 s_0$	Z
0 0	I_0
0 1	I_1
1 0	I_2
1 1	I_3



Function Table:

$s_2 s_1 s_0$	Z
0 0 0	I_0
0 0 1	I_1
0 1 0	I_2
0 1 1	I_3
1 0 0	I_4
1 0 1	I_5
1 1 0	I_6
1 1 1	I_7

Logical Expressions:

2:1 mux: $Z = s' I0 + s I1$

4:1 mux: $Z = s_1' s_0' I0 + s_1' s_0 I1 + s_1 s_0' I2 + s_1 s_0 I3$

8:1 mux: $Z = s_2's_1's_0' I0 + s_2's_1's_0 I1 + s_2's_1s_0' I2 + s_2's_1s_0 I3 + s_2s_1's_0' I4 + s_2s_1's_0 I5 + s_2s_1s_0' I6 + s_2s_1s_0 I7$

General Expression (k:1 Mux): $Z = \sum_{j=0}^{k-1} (m_j I_j)$

k=2^n , m_j= j. minterm, n = number of control inputs

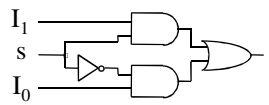
Exemplary Integrated Circuit:

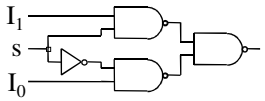
The IC 74151 contains an 8:1 multiplexer.

Internal structure of the multiplexers:

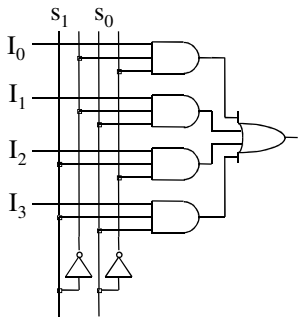
Multiplexers can be implemented using logic gates.

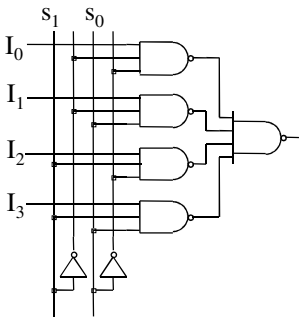
2:1 mux





4:1 mux

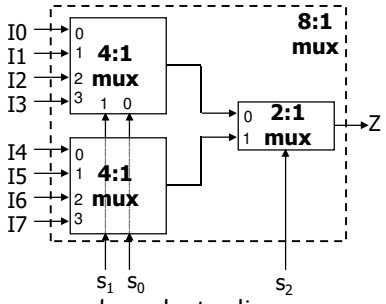




Implementing multiplexers of larger sizes using smaller multiplexers:

The following examples illustrate the implementation of an 8:1 multiplexer using other multiplexers in two different ways.

1. Method:

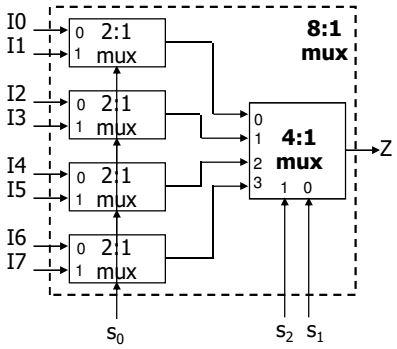


Here, s_0 and s_1 selector lines are common for 4:1 multiplexers.

Same inputs of both multiplexers are selected.

Selector s_2 determines which multiplexer's output is selected.

2. Method:



Design of Logic Circuits Using Multiplexers 1:

A logic circuit with n inputs and one output can be implemented by using only one 2^n:1 multiplexer and without any other logic gate.

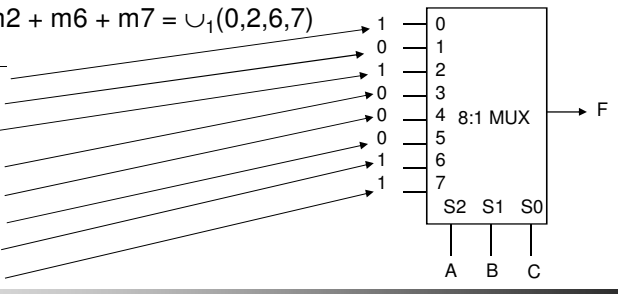
Method:

- The n inputs of the function (circuit) to be implemented are connected to the n selector lines of the multiplexer.
- Since each binary value of selector lines corresponds to an input combination , by considering the truth table of the function constant values ("0" or "1") are connected to the proper data inputs of the multiplexer.

Example:

$F(A,B,C) = m0 + m2 + m6 + m7 = \cup_1(0,2,6,7)$

No.	A	B	C	F
0	0	0	0	1
1	0	0	1	0
2	0	1	0	1
3	0	1	1	0
4	1	0	0	0
5	1	0	1	0
6	1	1	0	1
7	1	1	1	1



Design of Logic Circuits Using Multiplexers 2:

A logic circuit with n inputs and one output can be implemented by using only one 2^{n-1}:1 multiplexer and in addition with a NOT gate.

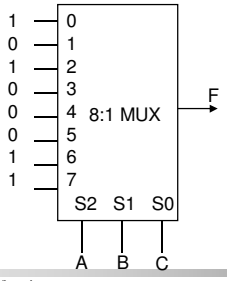
Method:

- n-1 inputs (variables) of the function are connected to the n-1 select lines of the multiplexer.
- The remaining variable or its complement is connected according to the truth table to the data inputs of the multiplexer.

Example:

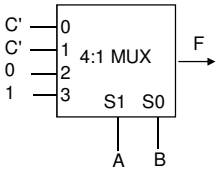
$F(A,B,C) = m0 + m2 + m6 + m7 = \cup_1(0,2,6,7)$

Reminder: Solution with a 8:1 MUX: (Previous method)



A	B	C	F	
0	0	0	1	C'
0	0	1	0	
0	1	0	1	C'
0	1	1	0	
1	0	0	0	0
1	0	1	0	
1	1	0	1	1
1	1	1	1	

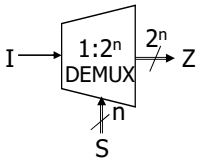
Solution with a 4:1 MUX:



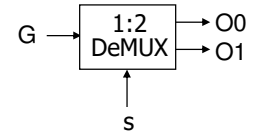
Here both c' values are obtained from the same NOT gate.

Demultiplexer:

- 1 data input, n selector (control) lines, 2^n data outputs.
- It selects one of the many data output lines, and connects it to the single input.
- The binary value on the select inputs determines the output line to which the data input is forwarded.
- The value on the not-selected output lines is "0".
- Demultiplexers are named according to the number of data outputs 1:m.



Example: 1:2 Demultiplexer

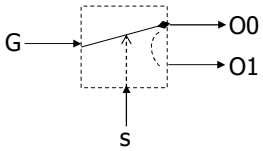


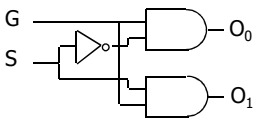
Function Table:

s	O_1	O_0
0	0	G
1	G	0

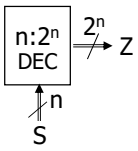
Truth Table:

s	G	O_1	O_0
0	0	0	0
0	1	0	1
1	0	0	0
1	1	1	0



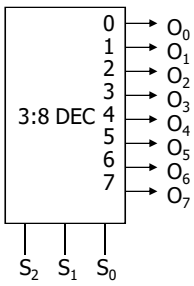


Decoder:



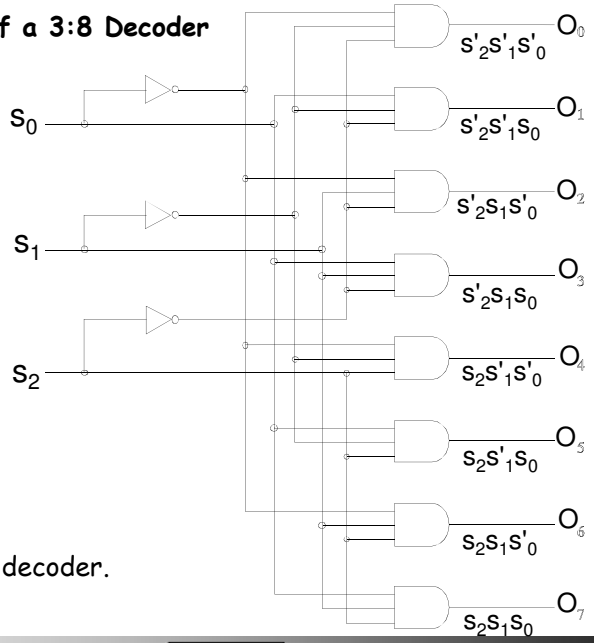
- n selector (control) inputs, 2^n outputs.
- According to the value on the select lines only one output gets the value "1" and other outputs are "0".
- Decoder can be considered as a demultiplexer that has a constant "1" on its input.
- Decoders are named as $n:2^n$ according to their lines. Here, n is the number of selector lines and 2^n is the number of outputs.

Example: 3:8 Decoder



S_2	S_1	S_0	O_7	O_6	O_5	O_4	O_3	O_2	O_1	O_0
0	0	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	0	1	0
0	1	0	0	0	0	0	0	1	0	0
0	1	1	0	0	0	0	1	0	0	0
1	0	0	0	0	0	1	0	0	0	0
1	0	1	0	0	1	0	0	0	0	0
1	1	0	0	1	0	0	0	0	0	0
1	1	1	1	0	0	0	0	0	0	0

Internal Structure of a 3:8 Decoder



An Exemplary IC:
74138 includes a 3:8 decoder.

Design of Logic Circuits Using Decoders:

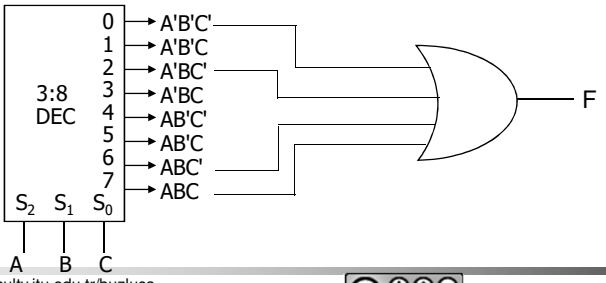
A general logic circuit with n inputs and m outputs can be implemented by using only one n:2^n decoder and in addition with OR gates.

Method:

- n inputs (variables) of the function are connected to the n select lines of the decoder.
- Each output of a decoder corresponds to a minterm.
- The outputs of the decoder, which correspond to the minterms of the function are added by using an OR gate.

Example:

F(A,B,C) = $\cup_1$(0,2,6,7) = m0 + m2 + m6 + m7 = $\overline{A}\overline{B}\overline{C} + \overline{A}B\overline{C} + AB\overline{C} + ABC$

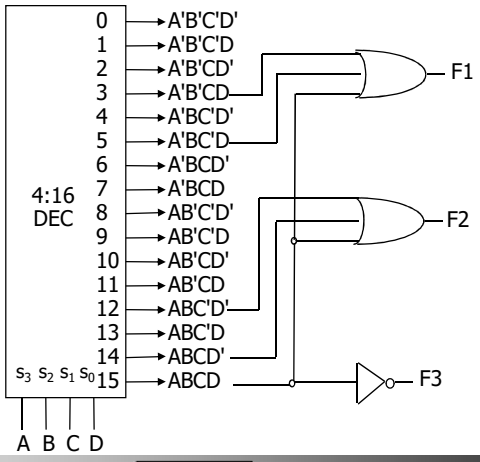


Example: Implementation of a function with 4 inputs and 3 outputs

F1(A,B,C,D) = A' B C' D + A' B' C D + A B C D

F2 (A,B,C,D) = A B C' D' + A B C

F3 (A,B,C,D) = (A' + B' + C' + D')



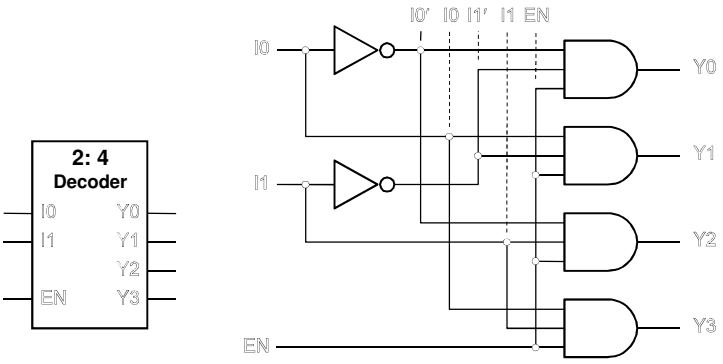
A decoder with an Enable (EN) input:

Decoders may also have an "enable" (EN) input.

If EN input is "1" decoder preforms normally.

If EN input is "0" all outputs of the decoder become "0".

Example: A 2:4 decoder with enable input is shown below:



An example of the usage of the decoders:

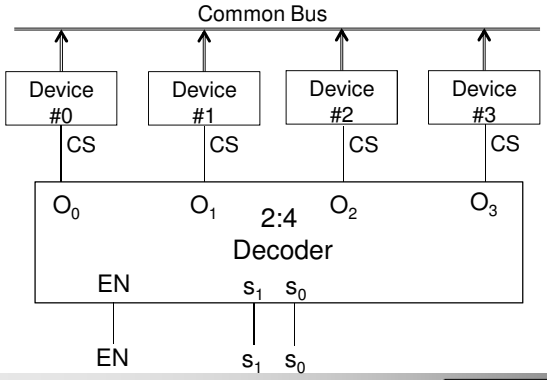
In some systems it is required that only one unit (device) in a group is active at a certain instant in time.

In other words, two devices can not be active at the same time.

These type of devices have «chip select» (CS) inputs, which are used to activate or deactivate them.

Decoders can be used to select the active unit.

Example: A decoder that controls 4 devices.



EN	s_1	s_0	#0	#1	#2	#3
1	0	0	+	-	-	-
1	0	1	-	+	-	-
1	1	0	-	-	+	-
1	1	1	-	-	-	+
0	X	X	-	-	-	-

Programmable Logic Device (PLD)

Today, complicated digital circuits are implemented using programmable logic devices.

These devices are integrated circuits that include many reconfigurable logic gates. (From several hundreds to several millions).

Some PLDs also include memory units (flip-flops).

The designer can reconfigure the connections between logical gates in the PLD by using a programming language and a programming device.

It is possible to implement complicated digital circuits with only one IC (PLD).

There are different kinds of PLDs:

- *Programmable Logic Array* – **PLA**
- *Programmable Array Logic* – **PAL®**
- *Generic Array Logic* – **GAL**
- *Complex PLD* – **CPLD**
- *Field-Programmable Gate Array* – **FPGA**

PAL is a registered trademark of Lattice Semiconductor Corp.

Programming of PLDs:

In early versions of PLDs (PLA, PAL) bipolar transistors were used (See Chapter 9).

They have fuses on the connection points between gates, which provide reconfiguration (programming) of devices.

In these devices fuses can be blown only once; therefore they are called one-time programmable (OTP).

Todays devices (GAL, CPLD, FPGA) are made of CMOS transistors and they consist memory units for programming.

They can be erased and reprogrammed many times.

To program PLDs various Hardware Description Languages (**HDL**) and programing devices are used.

Some examples of HDLs:

PALASM

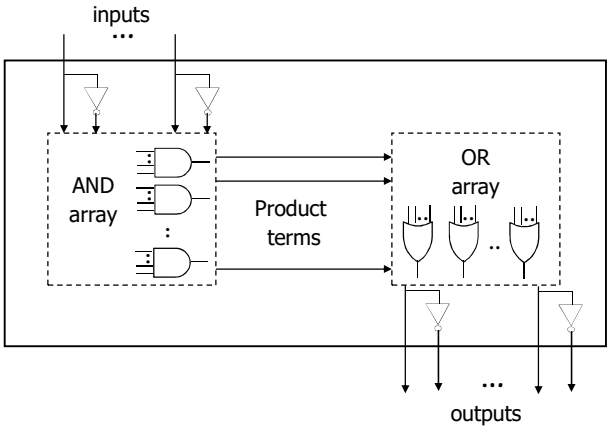
ABEL

Verilog

VHDL (*Very high speed integrated circuits* HDL)

Programmable Logic Array - PLA

It includes AND (product) units in the input layer and OR (sum) units in the output layer.



Both AND, OR arrays are flexible programmable.

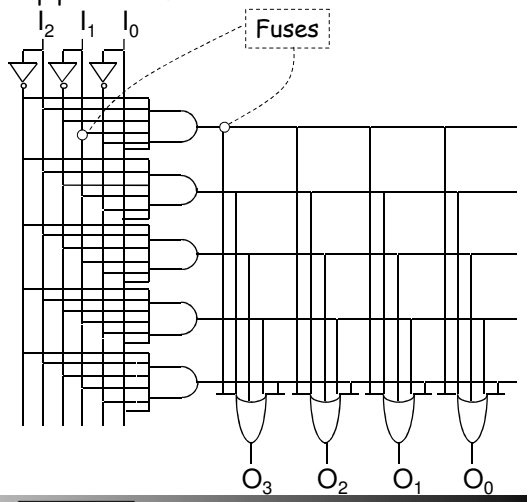
Parameters that determine the limits of a PLA:

Inputs: n
Outputs: m
AND gates (products):p
Such a device is called, "n x m PLA with p products".

On the right internal structure of a 3x4 PLA with 5 products is shown.

In real, PLAs include about 100 gates.

Example: 82S100
16 inputs, 8 outputs, 48 products

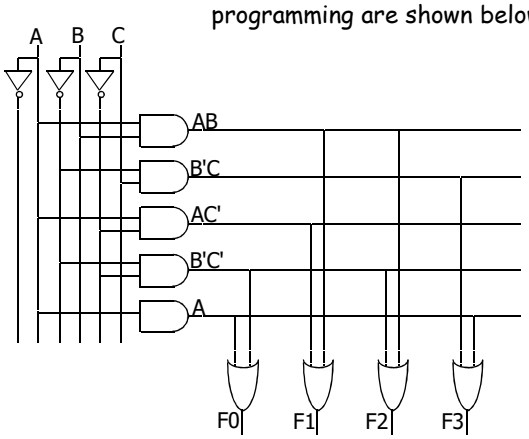


Example:

F0 = A + B' C'
F1 = A C' + A B
F2 = B' C' + A B
F3 = B' C + A

In the programming process unnecessary fuses are blown.

Internal connections of a 3x4 PLA with 5 products after programming are shown below.



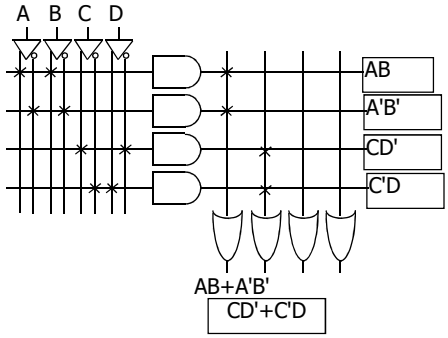
Simple Representation:

For the sake of simplicity all connections in a PLA are not shown.

Instead, we put an 'X' on the connection points which are connected to the inputs of gates.

Example:

F0 = A B + A' B'
F1 = C D' + C' D



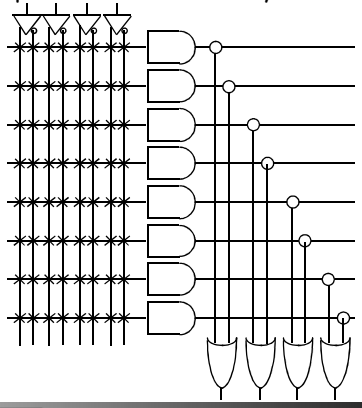
Programmable Array Logic - PAL

Inputs of AND gates can be flexible programed as in PLAs.

But inputs of OR gates are fixed. To each OR gate only outputs of certain AND gates can be connected.

For example to the inputs of the first OR gate only outputs of the first two AND gates can be connected.

PALs can be easily programmed, they are cheaper than PLAs and they can contain more gates.



PALs are introduced by the company Monolithic Memories, Inc. (MMI).

MMI obtained a registered trademark on the term PAL for use in "Programmable Semiconductor Logic Circuits".

The trademark is currently held by Lattice Semiconductor Corporation.

MMI, was acquired by Advanced Micro Devices (AMD).

Programmable logic division of AMD (Vantis) was then acquired by Lattice Semiconductor.

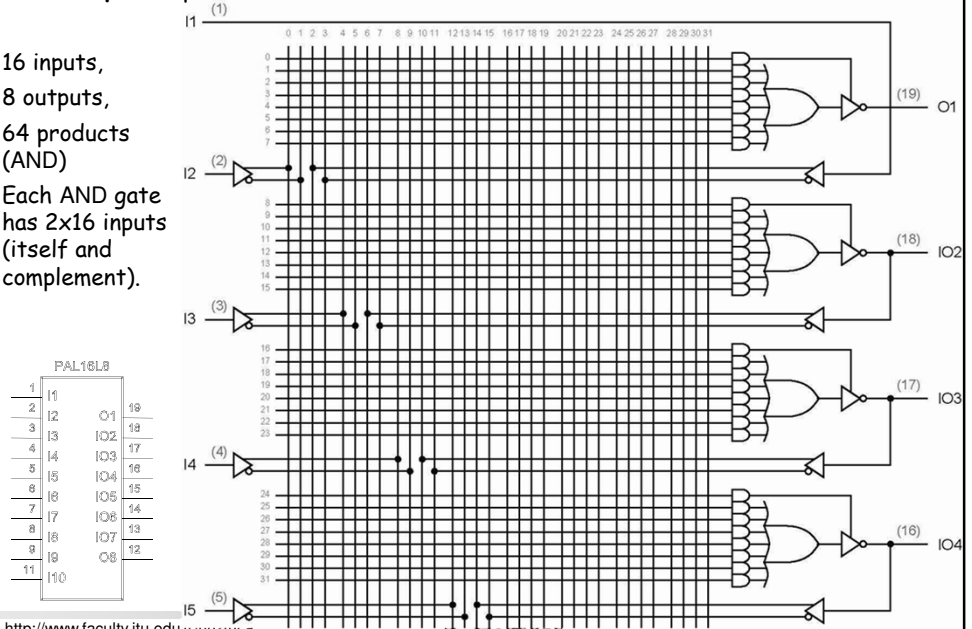
Example: A part of PAL 16L8 device is shown below:

16 inputs,

8 outputs,

64 products (AND)

Each AND gate has 2x16 inputs (itself and complement).



Generic Array Logic – GAL

Its logical properties are similar to PAL.

It is made of CMOS transistors. It can be many times erased and programmed.

It is introduced by Lattice Semiconductor.

Example: GAL16V8

Complex PLD – CPLD

It is an IC that contains several PLDs (*macro cell*).

Each internal PLD (macro cell) has GAL properties.

A typical CPLD may include from thousand to ten thousand gates.

Internal structures of macro cells and connections between them can be programmed.

Example: Atmel ATF1500

32 input/output + 4 inputs

32 PLDs (*macro cell*).

Field-Programmable Gate Array – FPGA

They contain many logical blocks and interconnections between these blocks.

Can be erased and programmed many times.

Number of logical gates is between several thousands and several millions.

Can be used to implement complex digital circuits (for example special purpose microprocessors).

Compared to CPLDs FPGAs are more flexible and they can implement more complicated circuits.

But their delay cost is higher.

Example: Atmel AT6010

204 input/output

30000 gates