

BLG 335E – Analysis of Algorithms I Fall 2017, Recitation 4 14.11.2017

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- A 'd-ary' heap is like a binary heap, but non-leaf nodes have d children instead of 2 children.
- How would you represent a d-ary heap in an array?
- Verify that:

d-ary-parent(d-ary-child(i, j)) = i



binary-parent(i) return [i / 2]

binary-child(i,j) return 2i – 1 + j

d-ary-child(i,j)
return d(i-1)+1+j

- Root's d children are kept in A[2]~A[d+1]
- Their children are kept in $A[d+2]\sim A[d^2+d+1]$ and so on.



- Banks often record transactions on an account in order of the times of the transactions.
- But many people like to receive their bank statements with checks listed in order by check number.
- Banks need to convert time-of-transaction ordering to check-number ordering.
- Insertion Sort vs. Quick Sort



- People usually write checks in order by check number, and merchants usually cash them with reasonable dispatch.
- The problem is therefore the problem of sorting almost-sorted input.
- For **Quick Sort**, best and average case time complexity are the same $(O(n \log n))$.
- For **Insertion Sort**, the best case is O(n) and the average case is O(n+d).



• Illustrate the operation of **Counting-Sort** on the array below.

$$A = [6, 0, 2, 0, 1, 3, 4, 6, 1, 3, 2]$$

- 1. $Max{A[i]}=6$
- 2. 0 0 0 0 0 0 0
- 3. 2 2 2 2 1 0 2
- 4. 2 4 6 8 9 9 11

6 0 2 0 1 3 4 6 1 3 2



5.

1	2	3	4	5	6	7	8	9	10	11
					2					
					2		3			
			1		2		3			
			1		2		3			6
			1		2		3	4		6
			1		2	3	3	4		6
		1	1		2	3	3	4		6
	0	1	1		2	3	3	4		6
	0	1	1	2	2	3	3	4		6
0	0	1	1	2	2	3	3	4		6
0	0	1	1	2	2	3	3	4	6	6

0	1	2	3	4	5	6
2	4	6	8	9	9	11
2	4	5	8	9	9	11
2	4	5	7	9	9	11
2	3	5	7	9	9	11
2	3	5	7	9	9	10
2	3	5	7	8	9	10
2	3	5	6	8	9	10
2	2	5	6	8	9	10
1	2	5	6	8	9	10
1	2	4	6	8	9	10
0	2	4	6	8	9	10
0	2	4	6	8	9	9



• Illustrate the operation of **Radix-Sort** on the following list of English words:

COW, DOG, SEA, RUG, ROW, MOB, BOX, TAB, BAR, EAR, TAR, DIG, BIG, TEA, NOW, FOX.



COW

DOG

SEA

RUG

ROW

MOB

BOX

TAB

BAR

EAR

TAR

DIG

BIG

TEA

NOW

FOX



SEA

TEA

MOB

TAB

DOG

RUG

DIG

BIG

BAR

EAR

TAR

FOX

BOX

COW

ROW

NOW



TAB

BAR

EAR

TAR

SEA

TEA

DIG

BIG

MOB

DOG

FOX

BOX

COW

ROW

NOW

RUG



BAR

BIG

BOX

COW

DIG

DOG

EAR

FOX

MOB

NOW

ROW

RUG

SEA

TAB

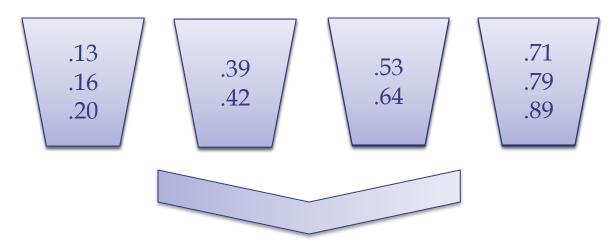
TAR

TEA



• Illustrate the operation of **Bucket-Sort** on the array below.

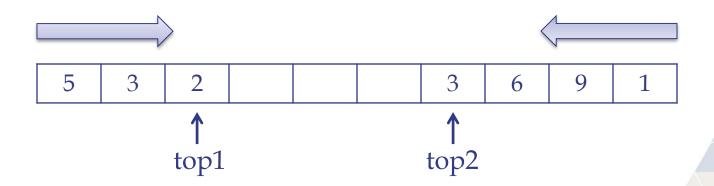
A = [.79, .13, .16, .64, .39, .20, .89, .53, .71, .42]



A = [.13, .16, .20, .39, .42, .53, .64, .71, .79, .89]



- Explain how to implement **two stacks** in **one array** A[1...n] in such a way that
 - neither stack overflows unless the total number of elements in both stacks is n.
 - the PUSH and POP operations should run in O(1) time.



Extra Exercises



• Implement a queue by a singly linked list L. The operations Enqueue and Dequeue should still take O(1) time.

- Write an **O(n)-time** procedure that, given an n-node **binary tree**, prints out the key of each node in the tree.
 - a) Recursively
 - b) Non-recursively using a **stack**