Localizing Ritz Values for Eigenvalue Computations

Russell Carden

Mark Embree Derek Hansen

Computational and Applied Mathematics

Rice University

Dissipative Spectral Theory Workshop Cardiff · January 2013

Outline

Introduction

- Computing eigenvalues of large matrices
- ▶ Ritz values, exact shifts, algorithm failure
- Ritz values and pseudospectra
- ► The inverse field of values (iFOV) problem

Normal Matrices [Carden and Hansen, to appear]

▶ Complete solution of iFOV for n = 3 via Ceva's Theorem

Nonnormal Matrices [Carden and E., 2012]

- A computational example: Jordan block
- ► Localization by real part and magnitude (toward 'interlacing')
- ► Examples

Convergence of Eigenvalue Algorithms

- ▶ Location of exact shifts
- ▶ Monotonic convergence to a desired eigenvector