

Homework-02 CPM Exercise

Task-01 Construct a network diagram

Given tasks according to precedence

- ① No other task can start until preliminary design is completed

Preliminary design (A) — 5 — no task

- ② When preliminary design (A) is completed, final design (B) preparation of assembly & test requirements (C) and parts procurement (D) can start.

Final design (B) — 7 — A

Prepare Assembly and test requirements (C) — 5 — A

Procure parts (D) — 10 — A

- ③ Assembly (E) cannot start until parts are procured (D), final design (B) is complete and assembly and test requirements (C) are completed

Assembly (E) — 8 — B, C, D

i.e. B, C, D starts only after E is completed.

- ④ Procurement of test equipment (F) and preparation of test procedures (G) cannot start until requirements for assembly and test (C) are available

Procure test equipment (F) — 12 — C

Prepare test procedures (G) — 7 — C

ie Task F, G starts only after completion of task C

⑤ Preparation of test fixtures (H) cannot start until test procedures (G) are available

Prepare of test fixtures (H) —————— 3 —————— G

ie Task H starts only after completion of task G

⑥ Testing (I) cannot start until assembly (E) is complete, test equipment (F) has been procured, and test fixtures(H) are available

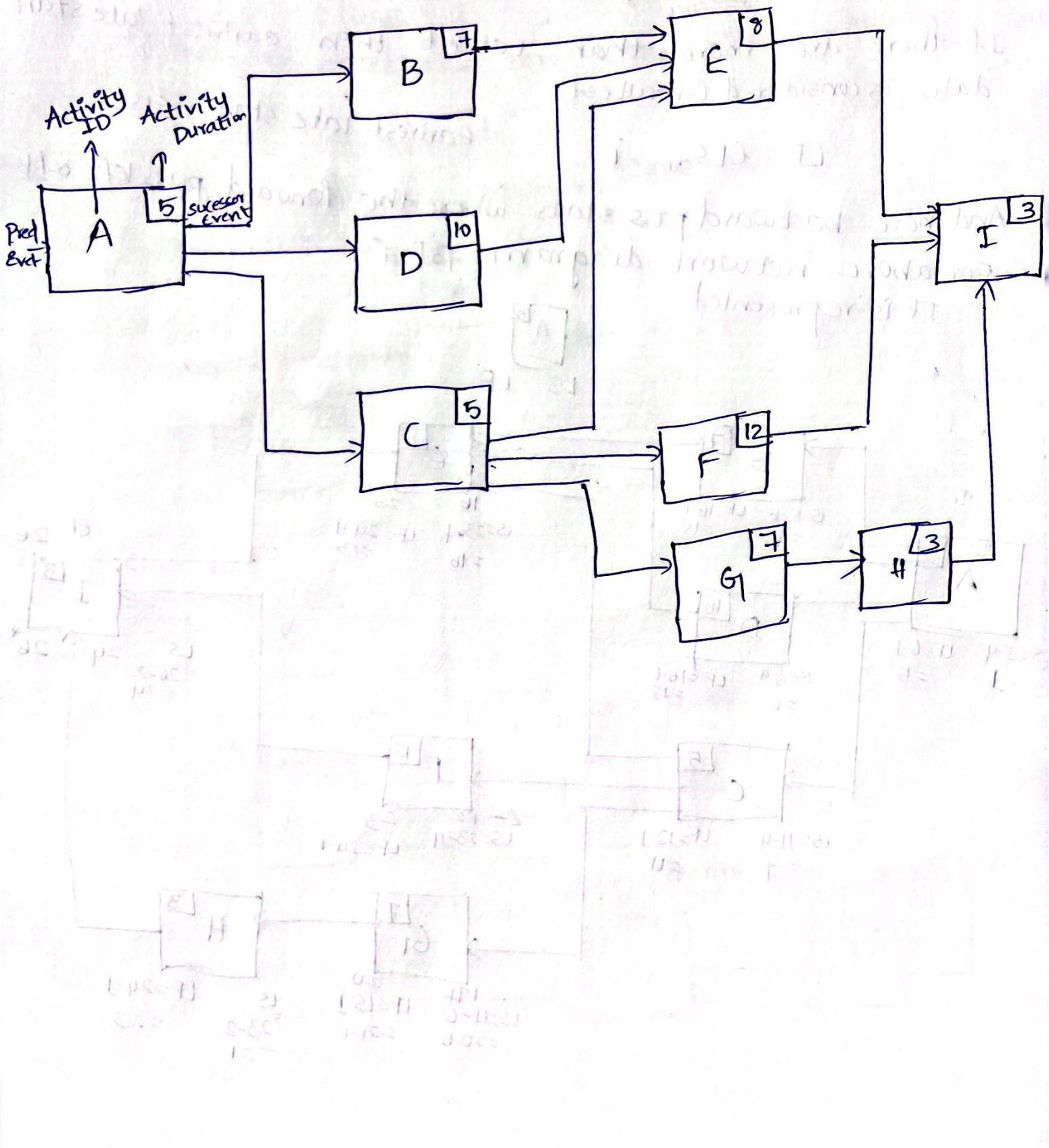
Test (I) —————— 3 —————— E, F, H

ie Task I starts only after completion of task E, F, H

so from above we can construct the given table

Symbolic (successor) representation	Project Task	Duration in Weeks	Predessor Event
A	Preliminary Design	5	-
B	Final Design	7	A
C	Prepare assembly and test requirement	5	A
D	Procure parts	10	A
E	Assembly	8	B, C, D
F	Procure test equipment	12	C
G	Procure test procedures	7	C
H	Prepare test fixtures	3	G
I	test	3	E, F, H

From the above table using the Activity ID and Activity Duration construct the linked nodes



* Conduct forward pass

In this

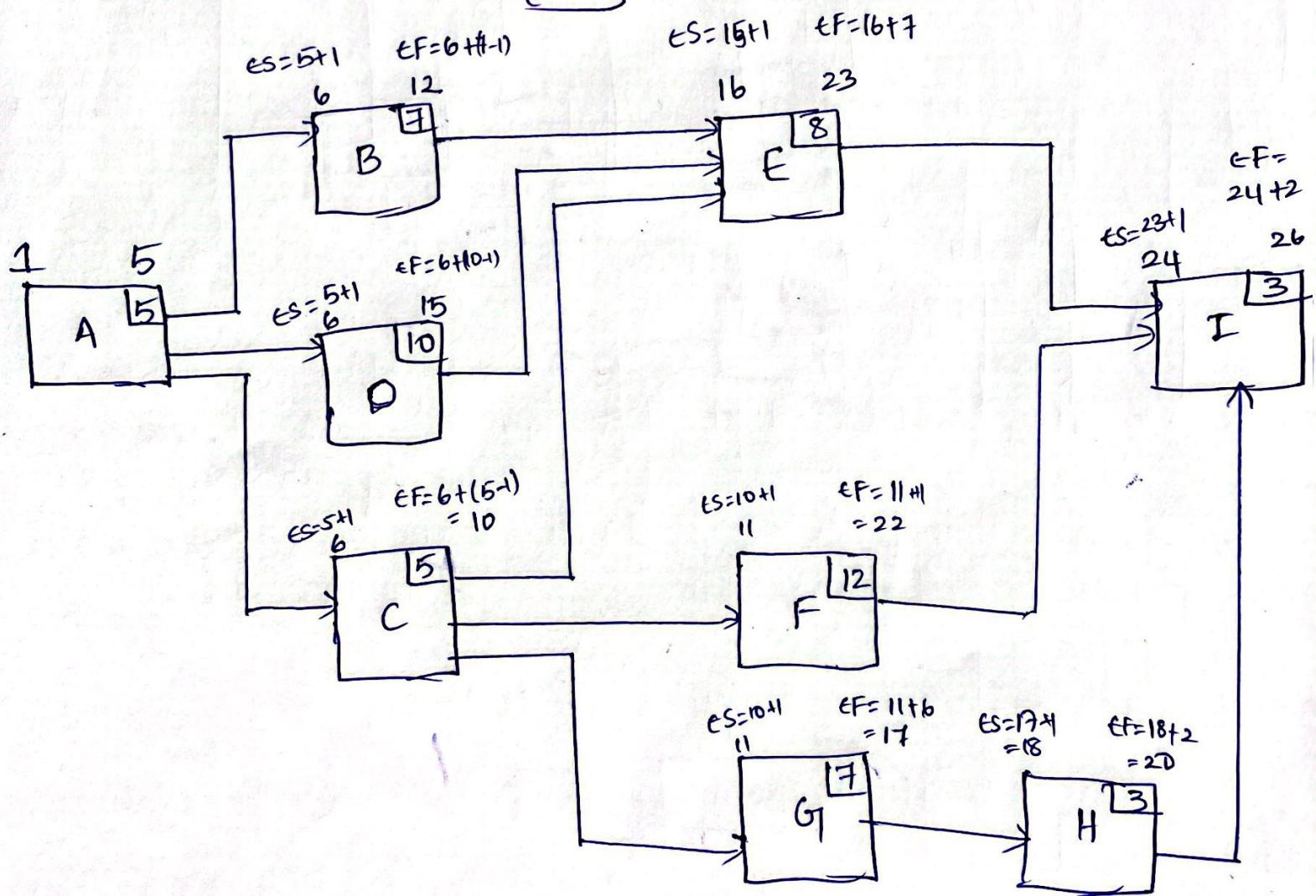
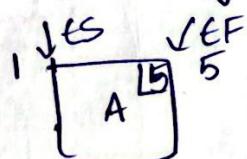
$$EF = ES + (Dur - 1)$$

$$ES = EF_{pred} + 1$$

If there are more than 1 event then latest early finish (high) + 1

$$ES = LEF_{pred} + 1$$

For above network diagram the FP is
It is represented



* Conduct backward pass

In this

$$LS = LF - (Dur - 1)$$

$$\begin{aligned} \text{late state} &= LS \\ \text{late finish} &- LF \end{aligned}$$

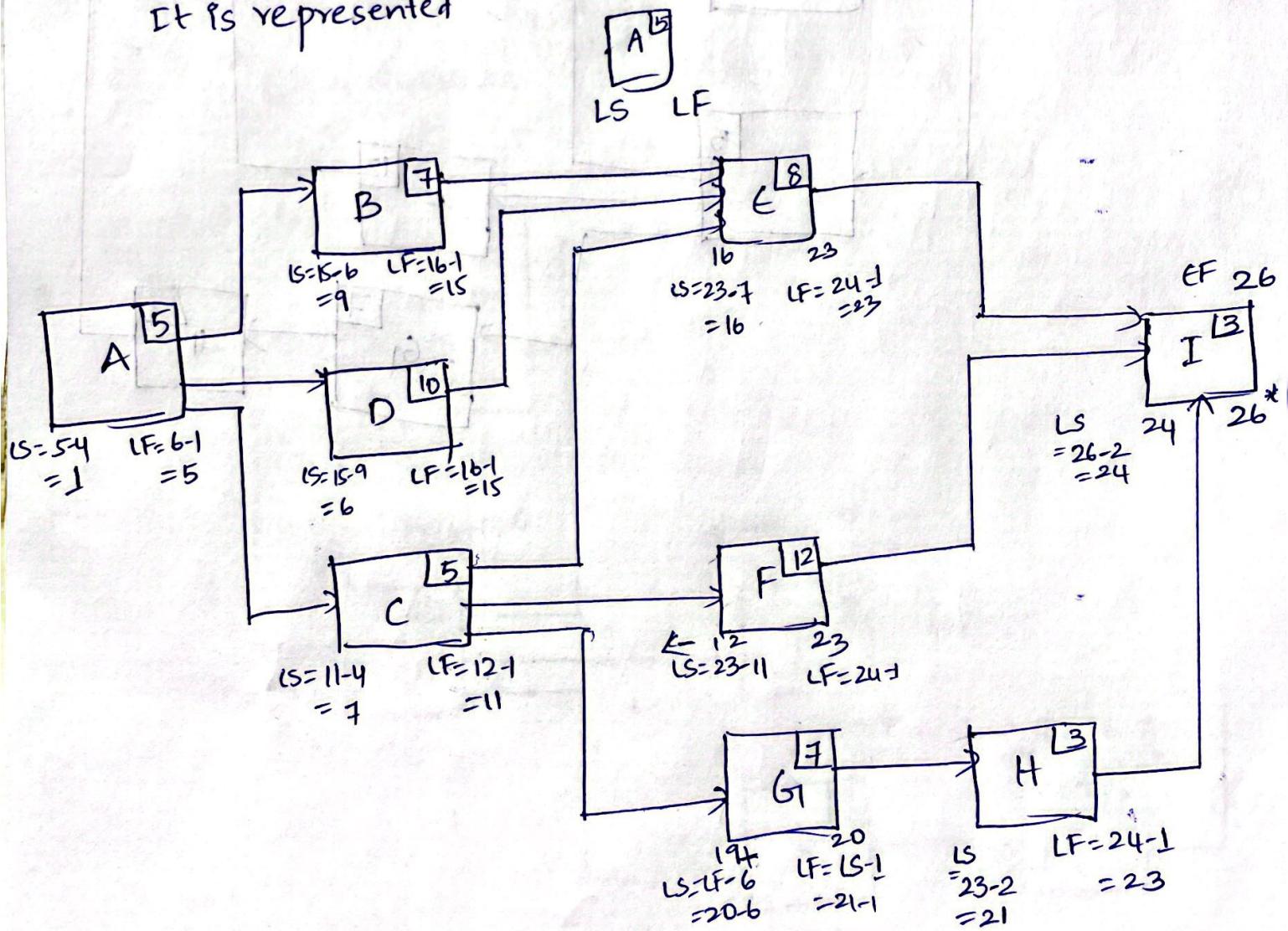
$$LF = LS_{\text{succ}} - 1$$

If there are more than 1 event then earliest late start date is considered (smallest)

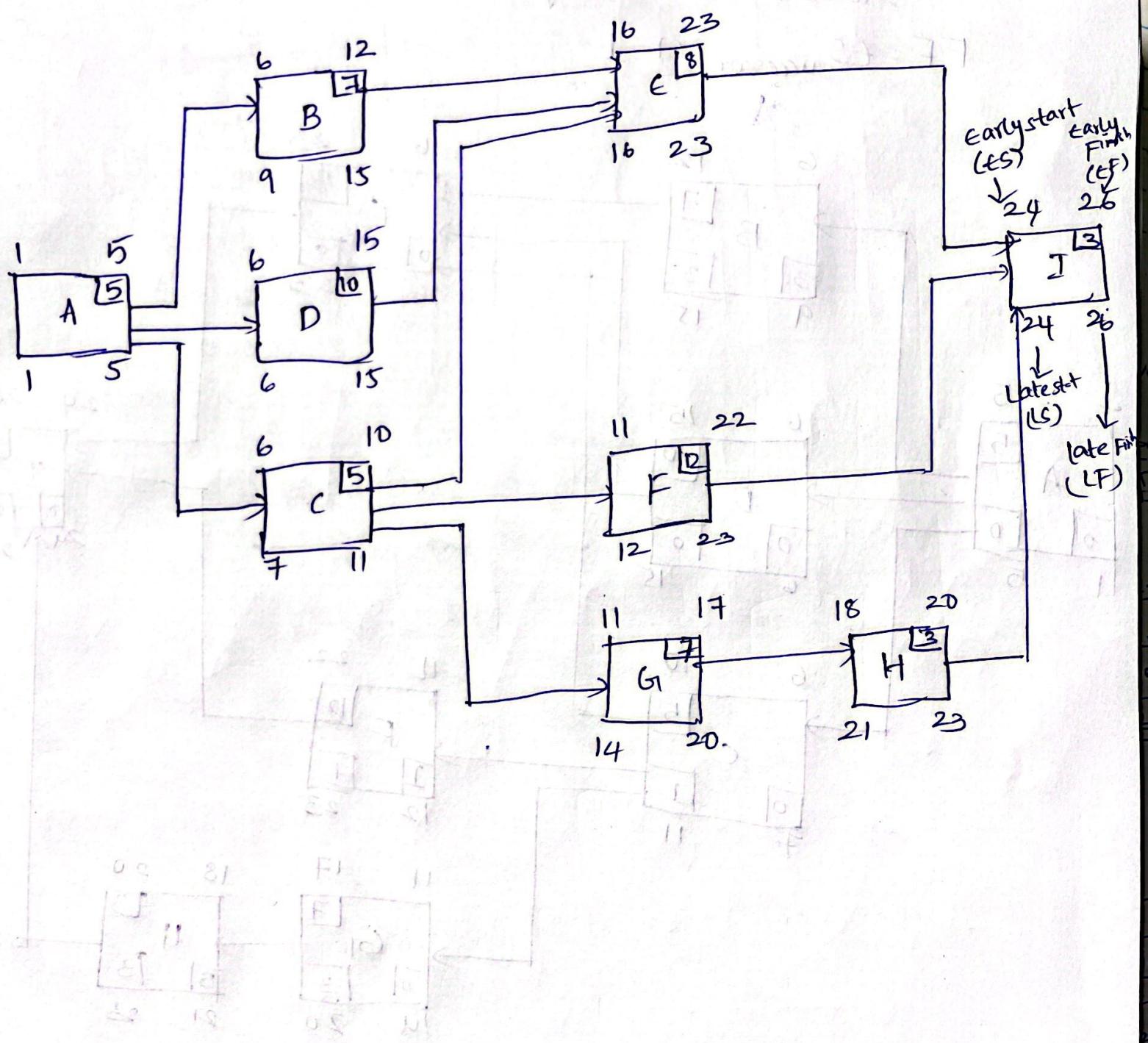
$$LF = ELS_{\text{succ}} - 1$$

$$\text{earliest late start} = ELS$$

And here backward pass starts where the forward pass left off
For above network diagram BP is
It is represented

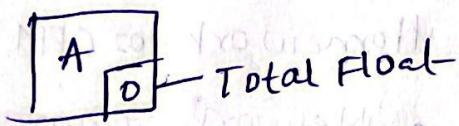


Representing Early and late Dates



During total stoppage after completion of all activities

Calculating total float for



$$`A' = LF - EF \\ = 5 - 5 = 0$$

$$`B' = \cancel{12} - 15 = 15 - 12 = 3$$

$$`C' = 11 - 10 = 1$$

$$`D' = 15 - 15 = 0$$

$$`E' = 23 - 23 = 0$$

$$`F' = 23 - 22 = 1$$

$$`G' = 20 - 17 = 3$$

$$`H' = 23 - 20 = 3$$

$$I = 26 - 26 = 0$$

calculating Free float for

$$`I' = 0 \quad \text{As it is the last one}$$

$$`E' = ESUC - EF - 1 = 24 - 23 - 1 = 0$$

$$`B' = 16 - 12 - 1 = 3$$

$$`H' = 24 - 20 - 1 = 3$$

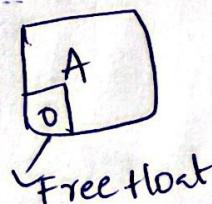
$$`G' = 18 - 17 - 1 = 0$$

$$`F' = 24 - 22 - 1 = 1$$

$$`C' = 11 - 10 - 1 = 0$$

$$`D' = 16 - 15 - 1 = 0$$

$$`A' = 6 - 5 - 1 = 0$$

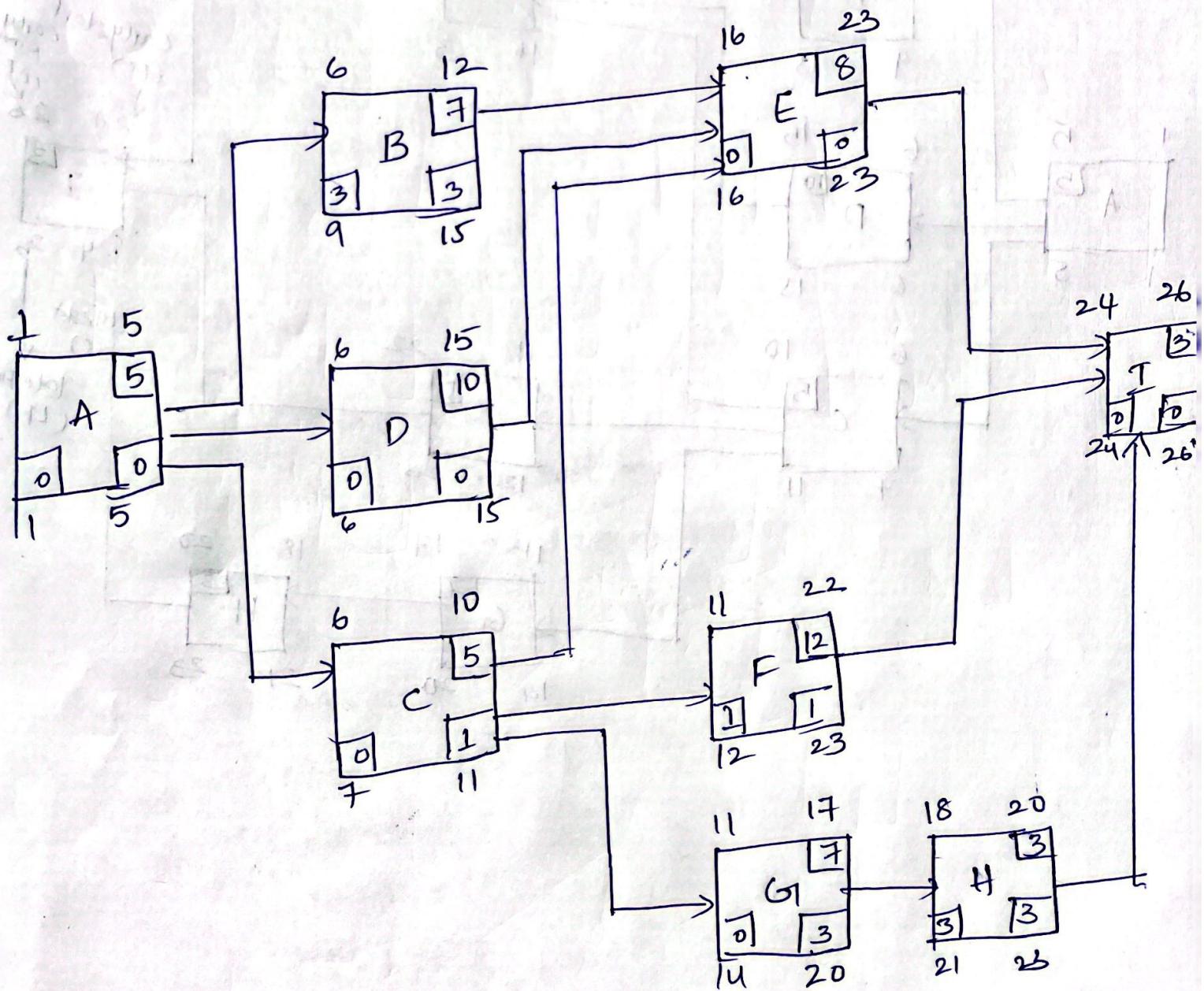


Total Float and Free Float

$$TF = LF - EF$$

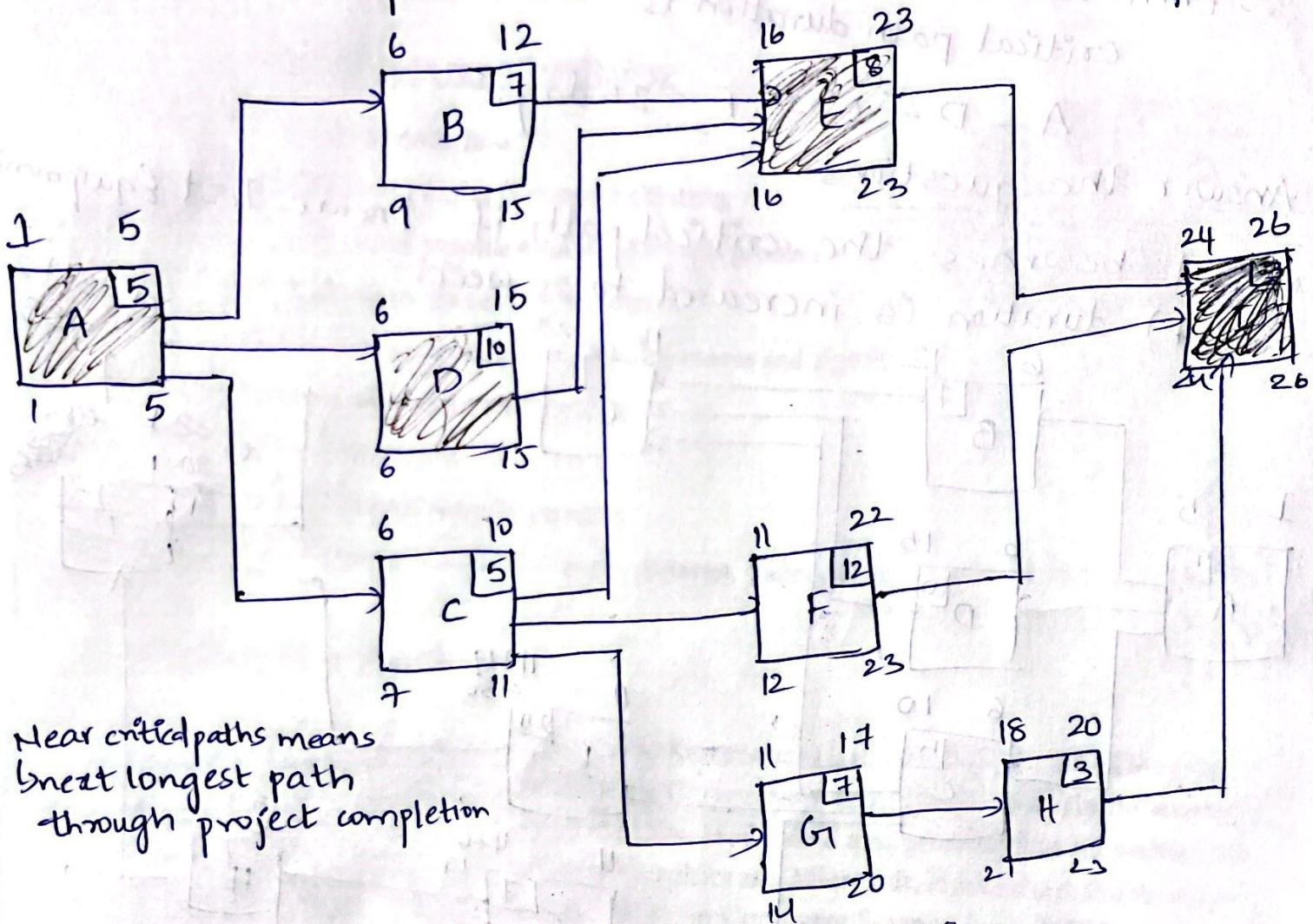
= late finish - Early Finish

$$FF = ES_{\text{successor}} - EF - 1$$



This is the new diagram with complete label on each node

Critical path - longest continuous sequence of tasks for project completion



To find critical path for above NW diagram
we should start at the end of the critical path and ask
"why". So here

Q1 Why does task "I" starts on day 24?

Ans "I" starts on day 24, because "E" finishes on day 23

Q2 Why does "E" starts on day 16?

Ans "E" starts on day 16, because "D" finishes on day 15.

Q3 Why does "D" starts on day 6?

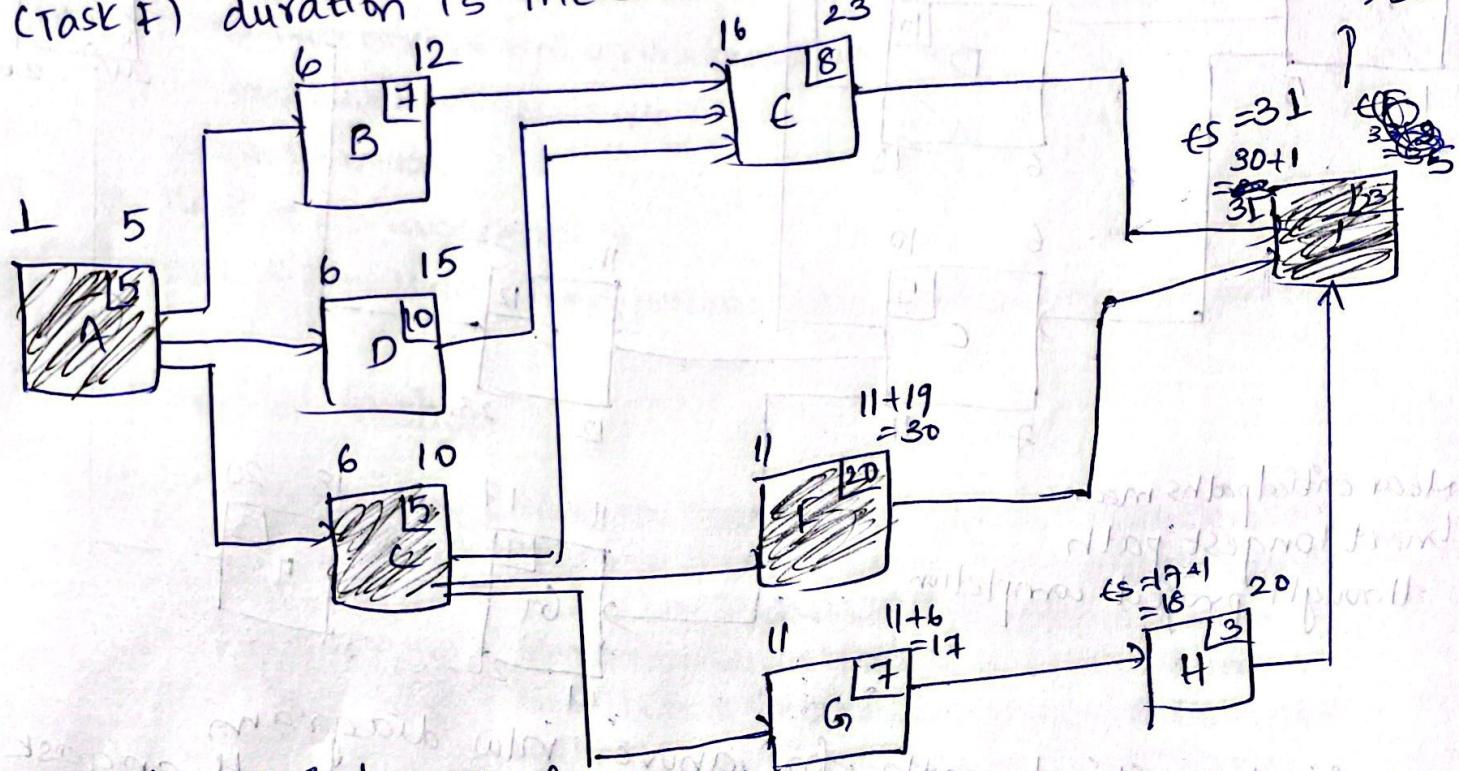
Ans "D" starts on day 6, because "A" finishes on day 5
we can stop when the project start ∴ A → D → E → I
critical path

∴ From above
critical path duration is

$$A - D - E - F = 26 \text{ days}$$

Answer the questions

* What becomes the critical path if 'Procure Test Equipment' (Task F) duration is increased to 20 weeks



To find critical path for above

Q1 Why does task 'I' starts on day 31?

A "I" starts on day 31, because 'F' finishes on day 30

Q2 Why does task 'F' starts on day 11?

A 'F' starts on day 11, because 'C' finishes on day 10

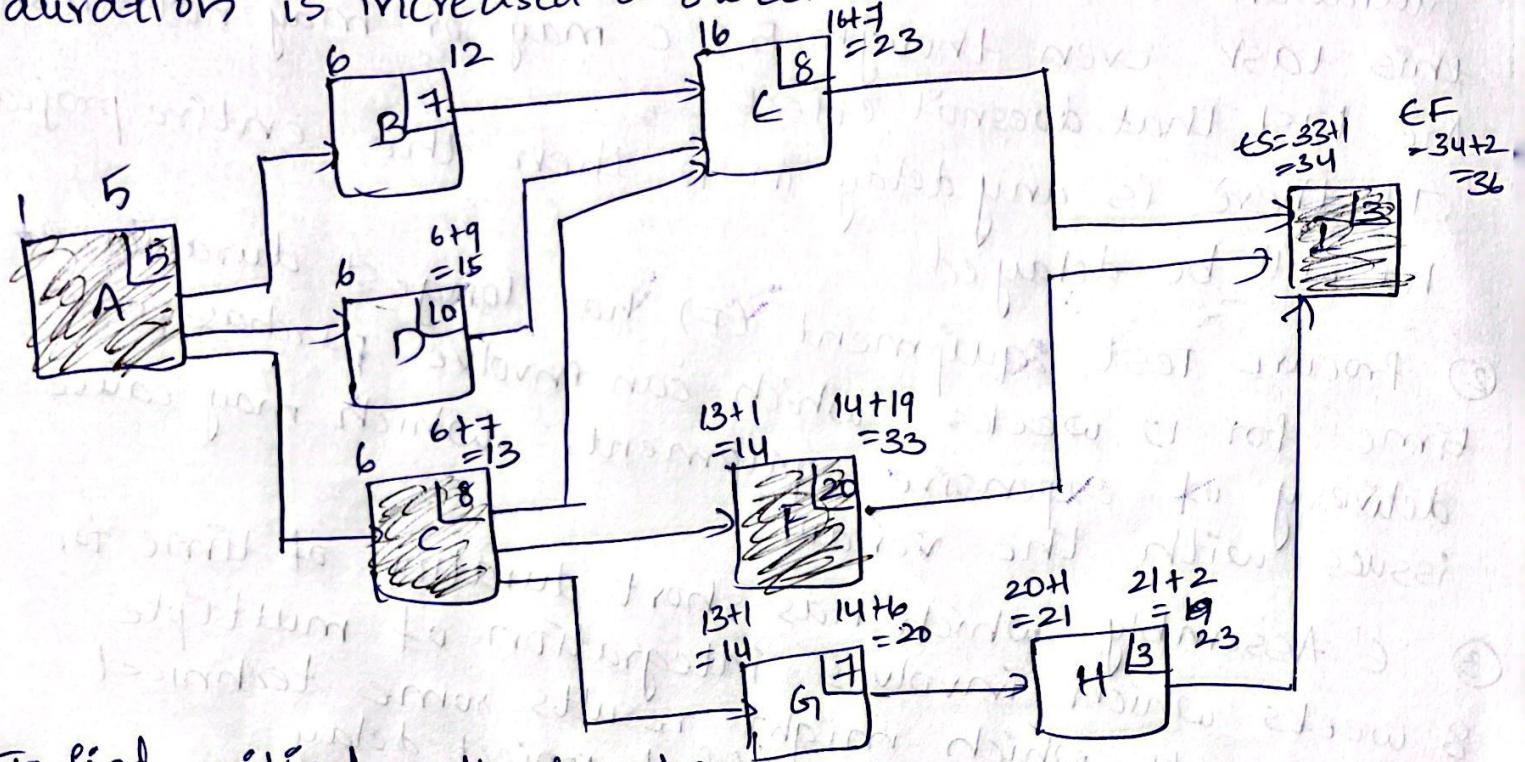
Q3 Why does task 'C' starts on day 6?

A 'C' starts on day 6, because 'A' finishes on day 5

∴ Total critical path is

$$A - C - F - I = 33 \text{ weeks.}$$

② Based on modified CPM nw from the first question (Task F is 20 weeks) what becomes the critical path if 'prepare assembly and test requirements task (c)' duration is increased to 8 weeks.



To find critical path for above

Q2 why does task 'I' starts on day 34?

A 'I' starts on day 34, because 'F' finishes on day 33.

Q2 why does task 'F' starts on day 14?

A 'F' starts on day 14, because C finishes on day 13.

Q2 why does task 'C' starts on day 6?

A 'C' starts on day 6, because A finishes on day 5.

∴ Total critical path is

$$A - C - F - I = 36 \text{ weeks.}$$

* What activities would you consider to be risky and why?

- ① If we look at the n/w diagram procure parts 'D' has duration of 10 weeks, where it is necessary to complete this task even though B & C may or may not finishes the task that doesn't effect 'E'.
If there is any delay in D then the entire project will be delayed.
- ② Procure Test equipment (F) has longest duration of time for 12 weeks which can involve purchase and delivery of expensive equipments which may cause issues with the vendors.
- ③ 'E' Assembly which has short duration of time for 8 weeks which involves integration of multiple components which might results some technical difficulties which may effect project delay.
- ④ even 'I' which is a testing phase has short duration of time for 3 weeks which involves testing the entire system which may not be sufficient