

## Spatial Concepts and Data Models

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### What is a Data Model?

- What is a model? (Dictionary meaning!)
  - A set of plans (blueprint drawing)
  - A miniature representation of a system to analyze properties of interest
- What is Data Model?
  - Specify structure or schema of a data set
  - Document description of data
  - Facilitates early analysis of some properties, e.g. querying ability, redundancy, consistency, storage space requirements, etc.
- Examples:
  - GIS organize spatial set as a set of layers
  - Databases organize dataset as a collection of tables
- Data models facilitate
  - Early analysis of properties, e.g. storage cost, querying ability, ...
  - Reuse of shared data among multiple applications
  - Exchange of data across organization
  - Conversion of data to new software / environment

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## Types of Data Models

- Two Types of data models
  - Generic data models
    - Developed for business data processing
    - Support simple abstract data types (ADTs), e.g. numbers, strings, date
    - Not convenient for spatial ADTs, e.g. polygons
    - Need to extend with spatial concepts, e.g. ADTs
  - Application Domain specific, e.g. spatial models
    - Set of concepts developed in Geographic Info. Science
    - Common spatial ADTs across different GIS applications

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## Models of Spatial Information

### State-Park Spatial dB

- Forests – collections of forest stands
- Accessed by road
- Has Manager
- Fire-stations within State-Park
- Facilities: Camping ground, Offices
- Rivers passes through the park and supply water at different facilities

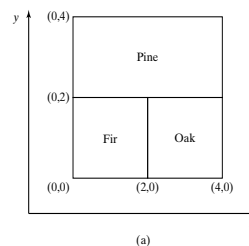
#### Two common models

- Field based
- Object based

#### Example: Forest stands

##### Fig.

- (a) forest stand map
- (b) Object view has 3 polygons
- (c) Field view has a function



Object Viewpoint of Forest Stands

Area-ID	Dominant Tree Species	Area/Boundary
FS1	Pine	[(0,2),(4,2),(4,4),(0,4)]
FS2	Fir	[(0,0),(2,0),(2,2),(0,2)]
FS3	Oak	[(2,0),(4,0),(4,2),(2,2)]

(b)

Field Viewpoint of Forest Stands

$$f(x,y) = \begin{cases} \text{"Pine,"} & 2 \leq x \leq 4; 2 \leq y \leq 4 \\ \text{"Fir,"} & 0 \leq x \leq 2; 0 \leq y \leq 2 \\ \text{"Oak,"} & 2 \leq x \leq 4; 0 \leq y \leq 2 \end{cases}$$

(c)

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## Field based Model

### ✦ Three main concepts:

- ▣ Spatial Framework is a partitioning of space
  - e.g., Grid imposed by Latitude and Longitude
- ▣ Field Functions:
  - f: Spatial Framework → Attribute Domain
- ▣ Field Operations
  - Examples, addition(+) and composition(o).

$$f + g : x \rightarrow f(x) + g(x)$$

$$f \circ g : x \rightarrow f(g(x))$$

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## Types of Field Operations

- ✦ **Local:** value of the new field at a given location in the spatial framework depends only on the value of the input field at that location(e.g., Thresholding)
- ✦ **Focal:** value of the resulting field at a given location depends on the values that the input field assumes in a small neighborhood of the location(e.g., Gradient)
- ✦ **Zonal:** Zonal operations are naturally associated with aggregate operators or the integration function. An operation that calculates the average height of the trees for each species is a zonal operation.
- ✦ Classify following operations on elevation field
  - ▣ Identify peaks (points higher than its neighbors)
  - ▣ Identify mountain ranges (elevation over 2000 feet)
  - ▣ Determine average elevation of a set of river basins

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## Object Model

### ✦ Object model concepts

- ▣ Objects: distinct identifiable things relevant to an application
- ▣ Objects have attributes and operations
- ▣ Attribute: a simple (e.g. numeric, string) property of an object
- ▣ Operations: function maps object attributes to other objects

### ✦ Example from a roadmap

- ▣ Objects: roads, landmarks, ...
- ▣ Attributes of road objects:
  - spatial: location, e.g. polygon boundary of land-parcel
  - non-spatial: name (e.g. Route 66), type (e.g. interstate, residential street), number of lanes, speed limit, ...
- ▣ Operations on road objects: determine center line, determine length, determine intersection with other roads, ...

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## Classifying Spatial objects

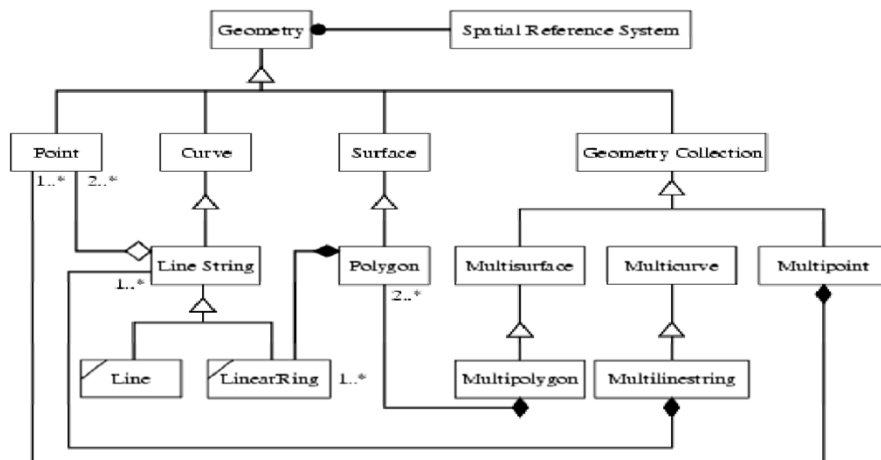
- Spatial objects are spatial attributes of general objects
- Spatial objects are of many types
  - Simple
    - 0- dimensional (points), 1 dimensional (curves), 2 dimensional (surfaces)
    - Example given at the bottom of this slide
  - Collections
    - Polygon collection (e.g. boundary of Japan or Hawaii), ...

Spatial Object Types	Example Object	Dimension
Point	City	0
Curve	River	1
Surface	Country	2

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## Spatial Object Types in OGIS Data Model

Fig: Each rectangle shows a distinct spatial object type



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## Classifying Operations on spatial objects in Object Model

- Classifying operations
  - Set theory based: 2-dimensional spatial objects (e.g. polygons) are sets of points
    - a set operation (e.g. intersection) of 2 polygons produce another polygon
  - Topological operations: Boundary of USA touches boundary of Canada
  - Directional: New York city is to east of Chicago
  - Metric: Chicago is about 700 miles from New York city.

Set theory based	Union, Intersection, Containment,
Topological	Touches, Disjoint, Overlap, etc.
Directional	East,North-West, etc.
Metric	Distance

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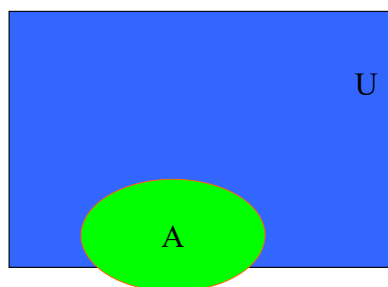
## Topological Relationships

- ✦ Topological Relationships
  - ▣ Invariant under elastic deformation (without tear, merge).
  - ▣ Two countries which touch each other in a planar paper map will continue to do so in spherical globe maps.
- ✦ Topology is the study of topological relationships
- ✦ Example queries with topological operations
  - ▣ What is the topological relationship between two objects A and B ?
  - ▣ Find all objects which have a given topological relationship to object A ?

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## Topological Concepts

- ✦ Interior, boundary, exterior
  - ▣ Let A be an object in a "Universe" U.



Green is A interior ( $A^\circ$ )

Red is boundary of A ( $\partial A$ )

Blue  $-($ Green  $+$  Red $)$  is  
A exterior ( $A^-$ )

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### Nine-Intersection Model of Topological Relationships

- Topological Relationship between A and B can be
  - specified using 9 intersection model
- Nine intersections
  - intersections between interior, boundary, exterior of A, B
  - A and B are spatial objects in a two dimensional plane.
  - Can be arranged as a 3 by 3 matrix
  - Matrix element take a value of 0 (false) or 1 (true).
- Q? Determine the number of many distinct 3 by 3 Boolean matrices

$$\Gamma_9(A, B) = \begin{pmatrix} A^\circ \cap B^\circ & A^\circ \cap \partial B & A^\circ \cap B^- \\ \partial A \cap B^\circ & \partial A \cap \partial B & \partial A \cap B^- \\ A^- \cap B^\circ & A^- \cap \partial B & A^- \cap B^- \end{pmatrix}$$

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### Specifying topological operation in 9-Intersection Model

Nine (9) intersection matrices for a few topological operations

$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 1 \end{pmatrix}$ disjoint	$\begin{pmatrix} 1 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix}$ contains	$\begin{pmatrix} 1 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 1 \end{pmatrix}$ inside	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$ equal
$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$ meet	$\begin{pmatrix} 1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix}$ covers	$\begin{pmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{pmatrix}$ coveredBy	$\begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$ overlap

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## **Using Object Model of Spatial Data**

### Object model of spatial data

- OGIS/OGC standard set of spatial data types and operations
- Similar to the object model in computer software
- Easily used with many computer software systems
- Programming languages like Java, C++, Visual basic
- Post-relational databases, e.g. OODBMS, ORDBMS

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## **Three-Step Database Design**

### Database applications are modeled using a three-step design process

- Conceptual - datatypes, relationships and constraints(ER model)
- Logical - mapping to a Relational model and associated query language(Relational Algebra)
- Physical - file structures, indexing

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### **Example Application Domain**

- ✚ Database design is for a specific application domain
  - ✚ Often a requirements document is available
  - ✚ Designers discuss requirements with end-users as needed
  - ✚ We will use a simple spatial application domain
    - to illustrate concepts in conceptual and logical data models
    - to illustrate translation of conceptual DM to logical DM
- ✚ Spatial application domain
  - ✚ A *state-park* consists of *forests*.
  - ✚ A forest is a collection of *forest-stands* of different species
  - ✚ State-Park is accessed by *roads* and has a *manager*
  - ✚ State-Park has *facilities*
  - ✚ *River* runs through state-park and supplies water to the facilities

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### **Conceptual DM: The ER Model**

- ✚ Three basic concepts
  - ✚ Entities have an independent conceptual or physical existence.
    - Examples: Forest, Road, Manager, ...
  - ✚ Entities are characterized by Attributes
    - Example: Forest has attributes of name, elevation, etc.
  - ✚ An Entity interacts with another Entity through relationships.
    - Road allow access to Forest interiors.
    - This relationship may be name "Accesses"
- ✚ Comparison with Object model of spatial information
  - ✚ Entities are collections of attributes are like objects
  - ✚ However ER model does not permit general user defined operations
  - ✚ Relationships are not directly supported in Object model
    - but may be simulated via operations

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
## Relationship Types

- ✚ Relationships can be categorized by
  - ▣ cardinality constraints
  - ▣ other properties, e.g. number of participating entities
    - Binary relationship: two entities participate
- ✚ Types of Cardinality constraints for binary relationships
  - ▣ One-One: An instance of an entity relates to a unique instance of other entity.
  - ▣ Many-One: Many instances of an entity relate to an instance of an other.
  - ▣ Many-Many: Many instances of one entity relate to multiple instances of another.
- ✚ Identify type of cardinality constraint for following:
  - ▣ Many facilities belong to a forest. Each facility belong to one forest.
  - ▣ A manager manages 1 forest. Each forest has 1 manager.
  - ▣ A river supplies water to many facilities. A facility gets water from many rivers.

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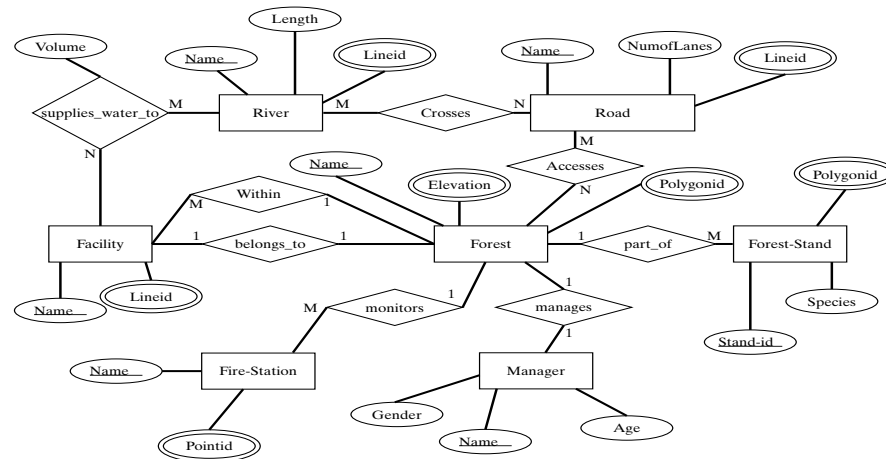
## ER Diagrams Graphical Notation

- ER Diagrams are graphic representation of ER models
  - Several different graphic notation are used
- Q? Compare and contrast “Attributes” and “Multi-valued attributes”

<i>Concept</i>	<i>Symbol</i>
Entities	
Attributes	
Multi-valued Attributes	
Relationships	
Cardinality of Relationship	1:1, M:1, M:N

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### ER Diagram for “State-Park”



- Examples:
  - List the entities, attributes, relationships in this ER diagram
  - Identify cardinality constraint for each relationship.
  - How many roads “Accesses” a “Forest\_stand”? (one or many)

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### Logical Data Model: The Relational Model

- ✦ Relational model is based on set theory
- ✦ Main concepts
  - Domain: a set of values for a simple attribute
  - Relation: cross-product of a set of domains
    - Represents a table, i.e. homogeneous collection of rows (tuples)
    - Set of columns (i.e. attributes) are same for each row
- ✦ Comparison to concepts in conceptual data model
  - Relations are similar to but not identical to entities
  - Domains are similar to attributes
  - Translation rules establishing exact correspondence

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## Relational Schema

### ✧ Schema of a Relation

- ✧ Enumerates columns, identifies primary key and foreign keys.
- ✧ Primary Key :
  - one or more attributes uniquely identify each row within a table
- ✧ Foreign keys
  - R's attributes which form primary key of another relation S
  - Value of a foreign key in any tuple of R match values in some row of S

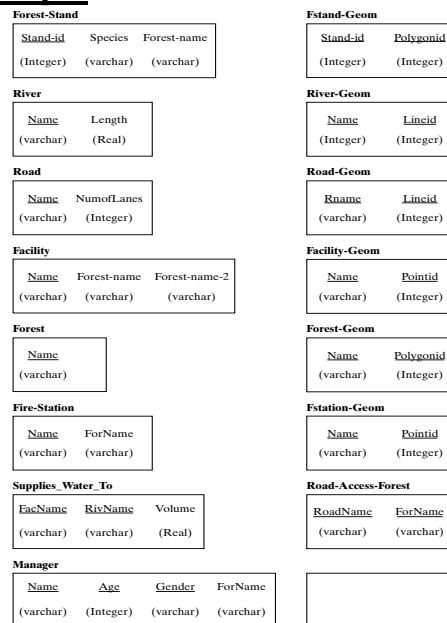
### ✧ Relational schema of a database

- ✧ Collection of schemas of all relations in the database
- ✧ A Blue print summary drawing of the database table structures
- ✧ Allows analysis of storage costs, data redundancy, querying capabilities
- ✧ Some databases were designed as relational schema in 1980s

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## Relational Schema Example

- Identify relations with
  - primary keys
  - foreign keys
  - other attributes
- Compare with ER diagram



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### Relational Schema for “Point”, “Line”, “Polygon” and “Elevation”

- Relational model restricts attribute domains
  - Simple atomic values, e.g. a number
  - Disallows complex values (e.g. polygons) for columns
  - Complex values need to be decomposed into simpler domains
  - A polygon may be decomposed into edges and vertices

**Polygon**

<u>Polygonid</u>	<u>Seq-no</u>	Pointid
(Integer)	(Integer)	(Integer)

**Line**

<u>Lineid</u>	<u>Seq-no</u>	Pointid
(Integer)	(Integer)	(Integer)

**Point**

<u>Pointid</u>	Latitude	Longitude
(Integer)	(Real)	(Real)

**Elevation**

<u>Forest-name</u>	Pointid (F.K.)	Elevation
(varchar)	(Integer)	(Real)

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### More on Relational Model

#### ✦ Integrity Constraints

- ✦ Key: Every relation has a primary key.
- ✦ Entity Integrity: Value of primary key in a row is never undefined
- ✦ Referential Integrity: Value of an attribute of a Foreign Key must appear as a value in the primary key of another relationship or must be null.

#### ✦ Normal Forms (NF) for Relational schema

- ✦ Reduce data redundancy and facilitate querying
- ✦ 1st NF: Each column in a relation contains an atomic value.
- ✦ 2nd and 3rd NF: Values of non-key attributes are fully determined by the values of the primary key, only the primary key, and nothing but the primary key.
- ✦ Other normal forms exists but are seldom used
- ✦ Translating a well-designed ER model yields a relational schema in 3rd NF
  - satisfying definition of 1st, 2nd and 3rd normal forms

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### **Mapping ER to Relational**

- Highlights of transactional rules
  - Entity becomes Relation
  - Attributes become columns in the relation
  - Multi-valued attributes become a new relation
    - includes foreign key to link to relation for the entity
  - Relationships (1:1, 1:N) become foreign keys
  - M:N Relationships become a relation
    - containing foreign keys or relations from participating entities

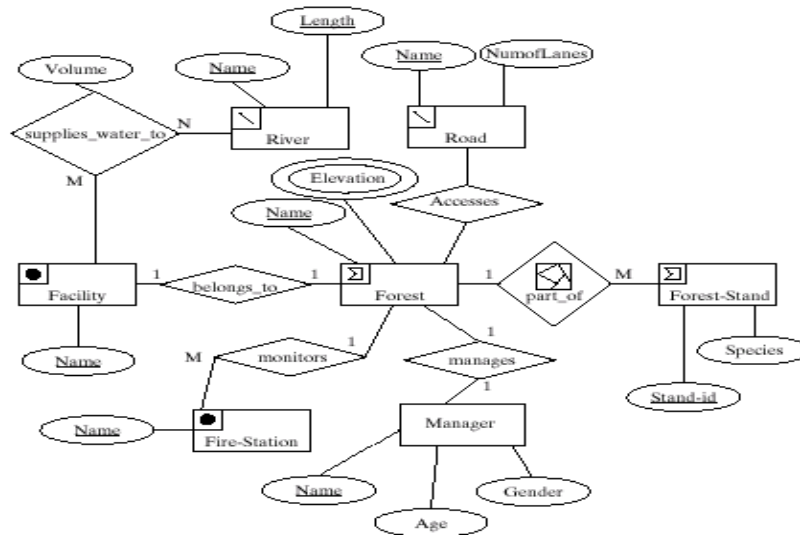
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### **Extending ER with Spatial Concepts**

- Motivation
  - ER Model is based on discrete sets with no implicit relationships
  - Spatial data comes from a continuous set with implicit relationships
  - Any pair of spatial entities has relationships like distance, direction, ...
- Explicitly drawing all spatial relationship
  - Clutters ER diagram
  - Generates additional tables in relational schema
  - Misses implicit constraints in spatial relationships (e.g. partition)
- Pictograms
  - Label spatial entities along with their spatial data types
  - Allows inference of spatial relationships and constraints
  - Reduces clutter in ER diagram and relational schema

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## ER Diagram with Pictograms: An Example



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## Specifying Pictograms

- Grammar based approach
  - Rewrite rule
  - like English syntax diagrams
- Classes of pictograms
  - Entity pictograms
    - basic: point, line, polygon
    - collection of basic
    - ...
  - Relationship pictograms
    - partition, network



Part\_of(Network)



Part\_of(Partition)

Pictograms for Relationships

⟨ Pictogram ⟩ → ⟨ Shape ⟩

→ \*

→ !

*Grammar (for Pictogram)*

⟨ Shape ⟩ → ⟨ Basic Shape ⟩

→ ⟨ Multi-Shape ⟩

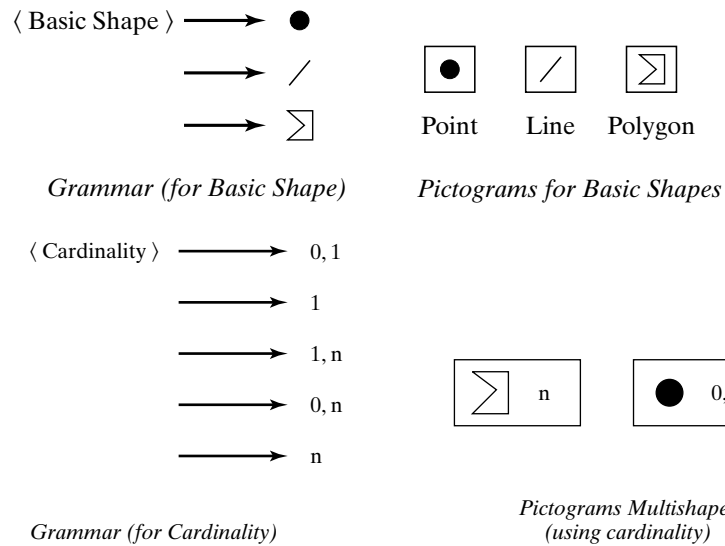
→ ⟨ Derived Shape ⟩

→ ⟨ Alternate Shape ⟩

*Grammar (for Shape)*

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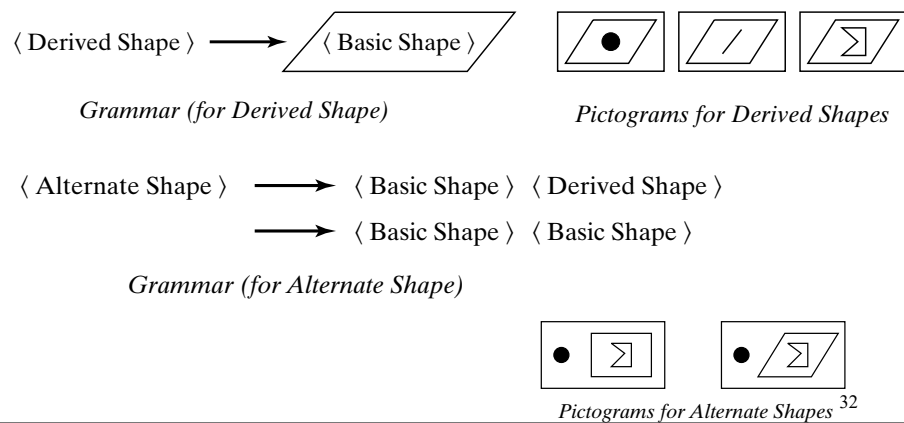
## Entity Pictograms: Basic shapes, Collections



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## Entity Pictograms: Derived and Alternate Shapes

- Derived shape example is city center point from boundary polygon
- Alternate shape example: A road is represented as a polygon for construction, or, as a line for navigation





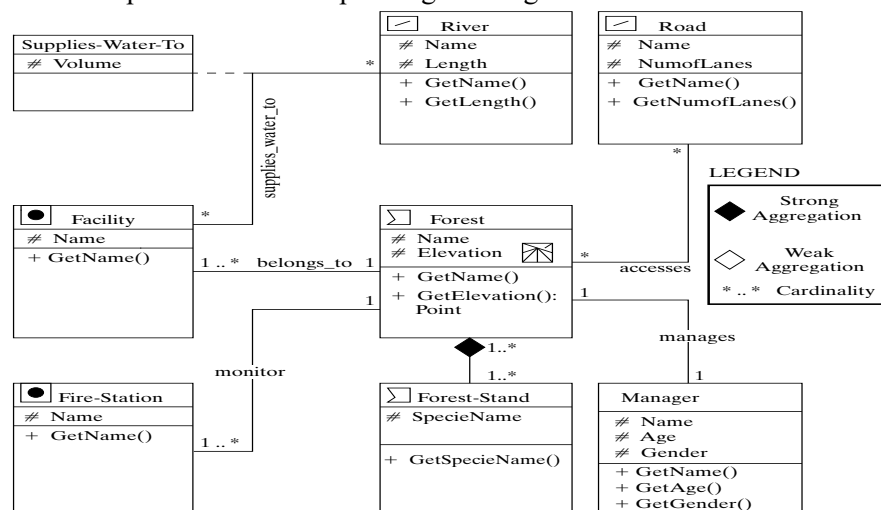
## Conceptual Data Modeling with UML

- Motivation
  - ER Model does not allow user defined operations
  - Object oriented software development uses UML
  - UML stands for Unified Modeling Language
  - It is a standard consisting of several diagrams
    - class diagrams are most relevant for data modeling
- UML class diagrams concepts
  - Attributes are simple or composite properties
  - Methods represent operations, functions and procedures
  - Class is a collection of attributes and methods
  - Relationship relate classes

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## UML Class Diagram with Pictograms: Example

- Exercise: Identify classes, attributes, methods, relationships in the Figure.
- Compare it with corresponding ER diagram



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### **Comparing UML Class Diagrams to ER Diagrams**

- Concepts in UML class diagram vs. those in ER diagrams
  - Class without methods is an Entity
  - Attributes are common in both models
  - UML does not have key attributes and integrity constraints
  - ERD does not have methods
  - Relationships properties are richer in ERDs
  - Entities in ER diagram relate to datasets, but UML class diagram can contain classes which have little to do with data

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### **Summary**

- ✦ Spatial Information modeling can be classed into Field based and Object based
- ✦ Field based for modeling smoothly varying entities, like rainfall
- ✦ Object based for modeling discrete entities, like country

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### Summary

- ✦ A data model is a high level description of the data
  - ▣ it can help in early analysis of storage cost, data quality
- ✦ There are two popular models of spatial information
  - ▣ Field based and Object based
- ✦ Database are designed in 3-steps
  - ▣ Conceptual, Logical and Physical
- ✦ Pictograms can simplify Conceptual data models