

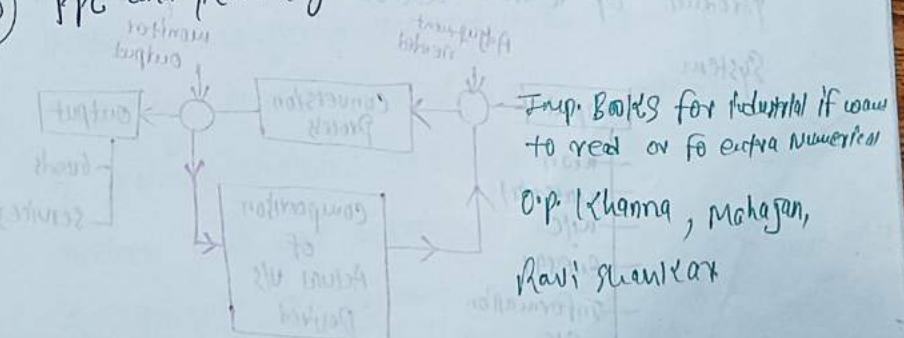
① Sequence of the Subject (weightage 6 to 7 marks) 14-03-21

- ① Introduction and BEA
- ② Inventory ~~**~~ Inventory
- ③ Sequencing.
- ④ PERT, CPM ~~**~~
- ⑤ Forecasting ~~**~~
- ⑥ Line balancing
- ⑦ Queuing

⑧ Linear Programming ~~**~~
 { - Graphical, Simplex
 - Transportation, Assignment }

⑨ MRP

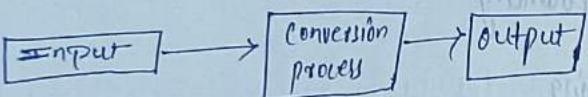
⑩ PPC and plant layout



Production

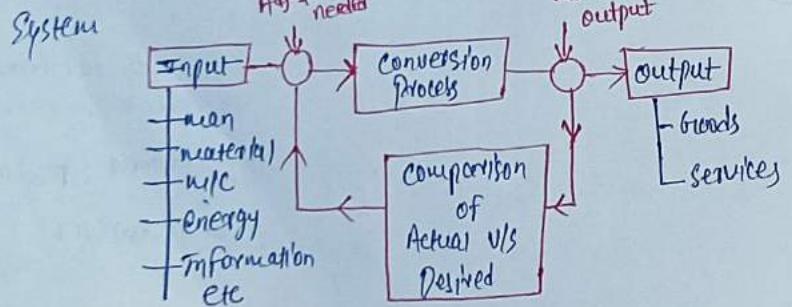
It is a step by step value addition process of converting one form of material into another form to increase the utility of the product for the user.

The product produced should be the need or necessity of some-one and should've economic value.



Production System:

It is an organized process of converting Raw material into finished product with a feed-back loop which compare the difference b/w the actual product produced and the desired product of which we've planned.



Productivity :-

It is a quantitative term to know what we produce and what we use as resources to produce them. Every organization always want to increase productivity by applying new technique and method.

$$\text{Productivity} = \frac{\text{output}(\uparrow)}{\text{Input}(\downarrow)}$$

Industrial engineer:

It is concerned with design, installation and improvement of production system. Its objective is to eliminate unproductive operations in order to increase productivity.

Production manager:

Production manager is concerned with planning, controlling, directing the day to day working of production system. Its objective is to produce goods and services of right quality and quantity at predetermined time and cost.

Cost in production:

(1) prime or Direct cost = Direct material + Direct labour
+ Direct expenses.

(2) factory overhead
or
factory expenses

= Indirect material + Indirect Labour
+ Indirect expenses.
↓
Cutting fluid
Grease, Lubricant
Cotton, Jute,
Stationary items etc.

watchman, supervisor,
Higher officers etc
etc.
↓
Rent, Facility development,
Telephone, electricity bills etc.

(3) Factory cost = Prime cost + factory overhead.

(4) Total cost = Factory cost + Marketing, Advertising, storage, transportation cost etc

(5) Selling cost = Total cost + profit

* BreakEven analysis :-
Total cost
Selling cost
Vol of products

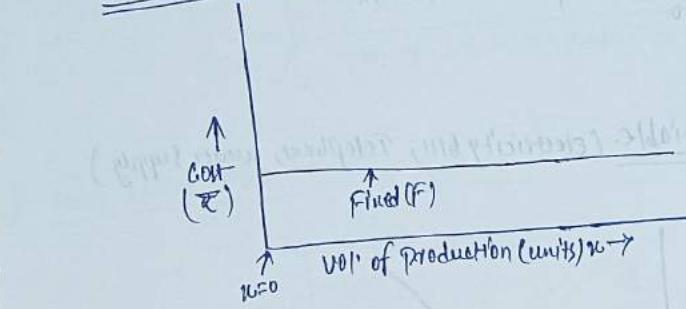
It is an imp. tool used by ~~producer~~ by producer

POCO M4 PRO 5G | SHIVANSHU ❤️🔥

① Total cost:

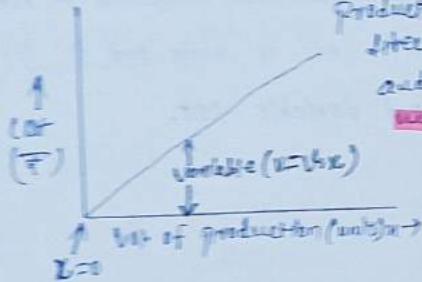
It indicates the expenditure required in order to produce certain no. of units and it is the sum of fixed and variable cost.

(a) Fixed cost (F)



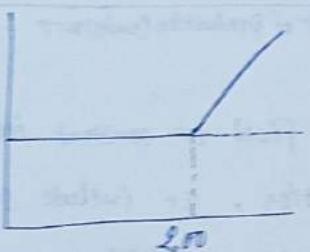
Fixed cost may fixed or constant irrespective of Vol. of production, it include salary of watchman, higher officers, rent of building cost of machine, advertisement cost, setup cost, insurance cost, interest etc

(b) Variable cost ($V=Vx$)



⇒ Fixed cost increases directly and proportionally with the vol. of production and it include directly and proportionally and it include direct material, direct labour and direct expenses.

(c) Semi-variable (electricity bill, Telephone, water supply)



Notations

F = fixed cost in Rupees.

x = No. of units produced or vol. of production.

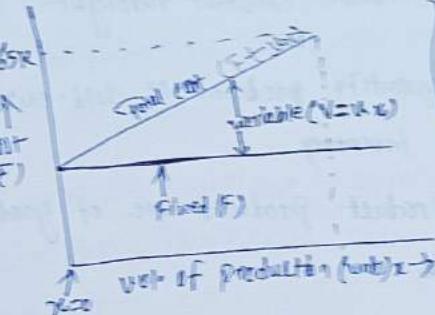
V = Variable cost per unit. (₹/unit)

$V = \text{Total variable cost in Rupees}$ $(\frac{₹}{x})$

S = Selling cost per unit. (Rupee/unit)

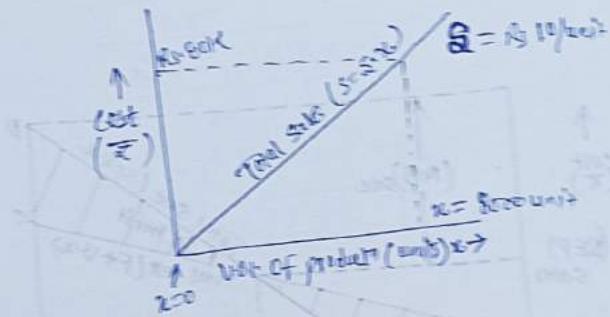
$S = \text{Total sales or revenue in Rupee}$ $(\$ \cdot x)$

Total cost ($F+Vx$)



$$\begin{aligned} F &= ₹ 25000 \\ V &= ₹ 5/\text{unit} \\ F+Vx &= 25000 + 5x \\ &= ₹ 65K \end{aligned}$$

Total Sale ($S=Sx$)



It is given the ~~written~~ statement obtained by selling out the quantity produced and it is directly proportional to vol. of production.

Assumptions in Breakeven chart

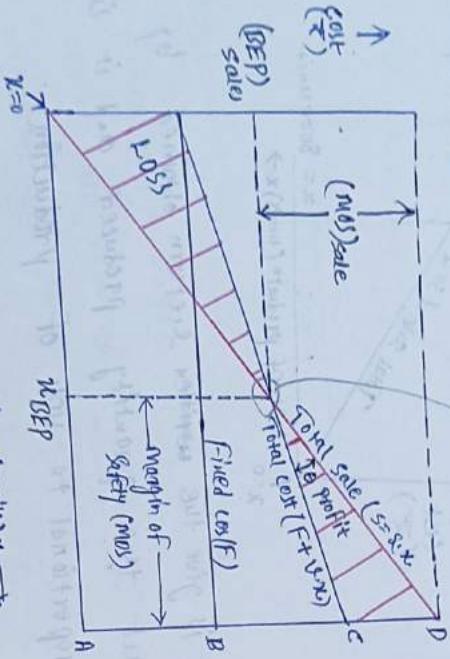
① F, v, S remain constant throughout

⇒ **Breakeven Point** is a volume of production between which total cost = total sales and organisation neither earn profit nor suffer from loss. Tr is also known as no profit and no loss point.

② All the quantity produced or sold out i.e. there is unsold inventory

③ All the product produced are of good standard dimensions.

④ Effectiveness and efficiency of production system remain constant throughout.



$$\text{Total sale} = \text{Total cost} + \text{Profit}$$

$$\text{Total sale} = S = Q \cdot x$$

$$\text{Total cost} = F + V = F + v \cdot x$$

$$\text{Profit} = P$$

$$S = F + V + P$$

$$Sx = F + Vx + P$$

$$Qx = F + Vx + P$$

$$Q = \frac{F + P}{(S - V)}$$

$$At BEP, P=0$$

$$Q_{BEP} = \frac{F}{(S - V)}$$

$$(BEP)_{\text{sale}} = Q_{BEP} \cdot S = \frac{F}{(S - V)} \cdot S \neq$$

Terms in Break even chart :-

(10)

① Angle of Incidence (θ) :- It is the angle at which total sales line cut the total cost line. Larger this angle better will be the working condition.

② contribution margin

$$CM = S - V = (S - V) \cdot x_c$$

$$\text{Contribution} = (S - V)$$

$$S = F + V + P$$

$$S - V = F + P$$

$$CM = F + P = (S - V) \cdot x_c$$

$$P = CM - F$$

→ marginal profit

or
gross margin

$$\left. \begin{array}{l} F = Rs\ 20,000 \\ V = Rs\ 6/\text{unit} \\ S = Rs\ 10/\text{unit} \\ S - V = Rs\ 4/\text{unit} \end{array} \right\}$$

(in page No. 4)
Book made by.

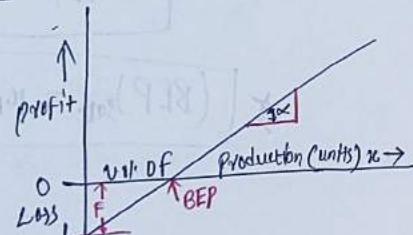
profit volume graph

$$S = F + V + P$$

$$S \cdot x = F + V \cdot x + P$$

$$P = (S - V) \cdot x - F$$

$$\textcircled{1} \text{ At } x = 0 \quad P = -F$$



(Profit → Volume) ratio

(11)

It is the term used to represent profitability related to sales. This ratio always remains constant for a particular product and it is ratio of contribution margin to the vol. of Sales. It is normally preferred when the organisation deal in multiproduct.

$$(P/V) \text{ Ratio} = \frac{CM}{S} = \frac{S - V}{S} = \frac{S - V}{S}$$

$$(P/V) \text{ Ratio} = \frac{F + P \uparrow}{S \uparrow} = \frac{S - V}{S}$$

Exact

$$\frac{F + P_1}{S_1} = \frac{F + P_2}{S_2} = \frac{F}{S_{BEP}} = \frac{S - V}{S}$$

Approximate

$$(P/V) \text{ Ratio} = \frac{\Delta P}{\Delta S}$$

NOTE :- If there is option of increasing the sale, highest (P/V) ratio should be preferred. And if there is option of decreasing the sales, lowest (P/V) ratio should be preferred.

margin of safety (MOS)

(12)

It is the difference of output at full capacity compare to output at break even point.

$$(MOS)_{Sale} = (Sale)_x - (Sales)_{BEP}$$

$$(MOS)_{Sale} = S_x - S_{BEP} \quad \text{₹}$$

or

$$(MOS)_{Sale} = S \cdot x - S \cdot (S_{BEP})$$

$$= S \cdot \left[x - \frac{F}{(S-V)} \right]$$

$$= S \cdot \left[\frac{(S-V)x - F}{(S-V)} \right]$$

$$= \frac{P}{\left(\frac{S-V}{S} \right)}$$

$$(MOS)_{Sale} = \frac{P}{(P/V) \text{ ratio}}$$

$$MOS \% = \left(\frac{S_x - S_{BEP}}{S_x} \right) \times 100$$

NOTE:- Changes in breakeven point when:-

① Fixed cost increases

$$F \uparrow \rightarrow S_{BEP} \uparrow \quad S_{BEP} = \frac{F}{(S-V)}$$

② V↑ → S_{BEP}↑

③ Q↑ → S_{BEP}↓

Q. A product can be produced by four process as given below:
In order to produce 100 unit which process should be preferred?

Medium you like
Channel 71
Explanation
Lecture 2, 25 min

Process	F (₹)	V (₹/unit)
I	20	3
II	40	1
III	30	2
IV	10	4

→ 320
→ 140 ^{Ans} minimum
least expenditure

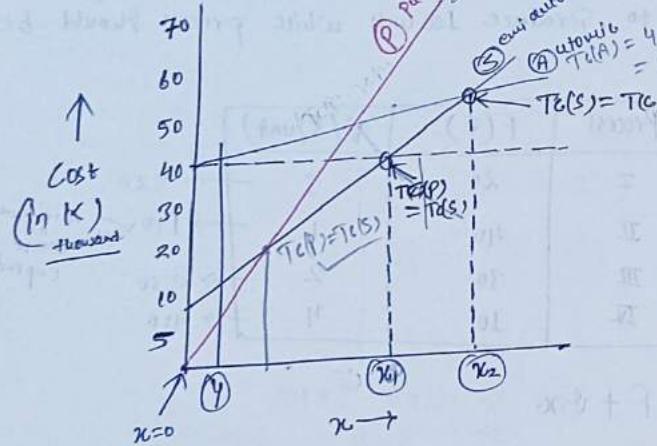
$$\Rightarrow TC = F + V \cdot x \Rightarrow 20 + 3 \times 100 \\ x=100 \Rightarrow 320 \quad \text{similarly}$$

Q. A company requires a product for which they've three options as given below. Draw the total cost graph for all the three process and find the economic feasibility. If 5 thousands units are to be produced, which process should be preferred and the corresponding cost



Options	$F(\text{₹})$	$V(\text{₹}/\text{unit})$
Purchase (P)	-	10
Semi-Automatic (S)	6800	6
Automatic (A)	40400	3

(14)



$$TC(P) = 10 \cdot x$$

$$TC(S) = 6800 + 6x$$

$$TC(A) = 40400 + 3x$$

$$x_1 = 1700, \quad x_2 = 11200 \text{ unit}$$

$$x = 5000 \text{ unit}$$

$$TC(P) = \text{Rs } 50000$$

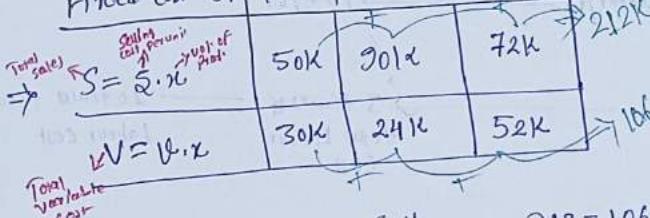
$$TC(S) = \text{Rs } 36800 \checkmark \text{ Any ATO}$$

$$TC(A) = \text{Rs } 55400$$

Q. Find out the Breakeven Sales in rupees for (15) the following product

Product	A	B	C
Sales (units)	5000	6000	4800
$S(\text{₹}/\text{unit})$	10	15	18
$V(\text{₹}/\text{unit})$	6	11	13

Fixed cost of the product is Rs 20,000



$$(P/V) \text{ Ratio} = \frac{S-V}{S} = \frac{212-106}{212}$$

$$(P/V) \text{ Ratio} = 0.5$$

$$(P/V) \text{ Ratio} = \frac{F+P}{S} = \frac{F}{S \cdot BEP}$$

$$0.5 = \frac{20,000}{S \cdot BEP}$$

$$S \cdot BEP = \text{Rs } 40,000 \checkmark$$

Operating w/c and
either of

Q. A component can be manufactured in either of two machines operating are given below. Determine Break even quantity for production of component

PTO

Q10

Variable	No. of units produced/unit	15	60
Cost of tooling		Rs 200	Rs 420
Selling price		Rs 4/unit	Rs 4/unit
Machining Labour/unit		Rs 15/unit	Rs 20/unit
Setting Labour/unit		Rs 15/unit	Rs 20/unit
Overtime Charges		3 times of Labour cost	10 times total Labour cost

$\Rightarrow T_c = \text{Tooling cost} + \text{Machining cost}$
 + Overtime cost

$$\frac{T_c}{T_c - (I)^t} = 200 + \left(\frac{70}{60}\right) \times 15 + \left(\frac{15}{15}\right) \times 4 + 3 \left[\left(\frac{70}{60}\right) \times 15 + \frac{15}{15} \right] \quad (1)$$

$$\text{For } T_c - I^{\text{new}} = 420 + \left(\frac{230}{60}\right) \times 20 + \left(\frac{25}{60}\right) \times 4 + 10 \left[\left(\frac{230}{60}\right) \times 20 + \frac{25}{60} \right] \quad (2)$$

$$20 + \left(\frac{70}{60}\right) \times 15 + 3 \left[\left(\frac{70}{60}\right) \times 15 + \frac{15}{15} \right] = 420 + \left(\frac{230}{60}\right) \times 20 + \frac{40}{60} + 10 \left[\left(\frac{230}{60}\right) \times 20 + \frac{15}{60} \right]$$

$$x = 2980 \text{ units.}$$

Q. For a production system

$$\text{Fixed cost } (F) = \text{Rs 10 lakh}$$

$$V = \text{Rs } 60/\text{unit}$$

$$S = \text{Rs } 100/\text{unit}$$

$$\text{Due to inflation fixed cost increases by } 10\%. \text{ Find the } V.$$

Variable cost (V) increases by 10%. Find the V.
 Change required in selling price per unit then
 BEP unit wise increases by 5%.

$$BEP = \text{Rs } 10 \text{ lakh} \Rightarrow F = 10.5 \text{ lakh}$$

$$V = \text{Rs } 60/\text{unit}$$

$$S = \text{Rs } 100/\text{unit}$$

$$(BEP)_{\text{new}} = 1.5 \times (BEP)_{\text{old}}$$

$$\frac{F'}{S' - V} = 1.5 \times \frac{F}{S - V}$$

$$\frac{10.5}{S' - 66} = 1.5 \times \frac{10}{100 - 60}$$

$$S' = \text{Rs } 94/\text{unit}$$

$$\left(\frac{S' - S}{S} \right) \times 100 = -6\%$$

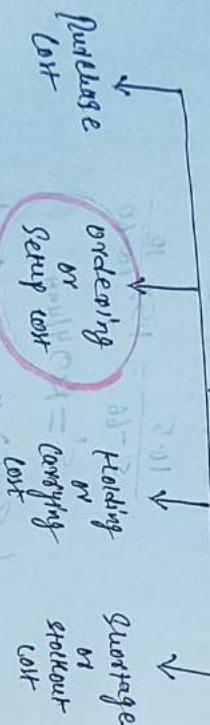
(18)

INVENTORY

INVENTORY can be defined as stocks on hand at a given point of time which may be helpful for the purpose of later use or sale. It is ideal resource having economic value and it may include raw material, working process inventory, semi-finished or sub-assembly inventory and final products.

In an inventory control over aim is to manage inventory in such a manner that day to day working will run smoothly without any delay. But at the minimum of cost.

Inventory Cost



Purchasing cost → It is a cost of purchasing inventory items and it depend upon the city or the bulk amount purchased.

$$P.C = \frac{\text{No. of units}}{\text{unit}} \times \text{Cost/unit}$$

Ordering cost → When inventories purchased from outside. The cost associated with bringing inventory within the production system is termed as ordering cost. It include cost of tender, Paper work cost, processing fee, communication cost, salary of purchasing department, transportation cost, inspection cost etc.

$$O.C = \frac{\text{No. of order}}{\text{order}} \times \text{cost/order}$$

Setup cost → When inventory is produced internally the cost associated with bringing the shutdown production system again into starting position is termed as setup cost. It include maintenance cost of machine, schedule plant preparation cost, cost of bringing raw material, arrangement of worker, tool, equipment etc.

$$S.C = \frac{\text{No. of setup}}{\text{setup}} \times \text{cost/setup}$$

Holding or Carrying cost → It is a cost associated with storing, keeping and maintaining inventory within the production system. It include storage cost, handling cost, damage and depreciation cost, insurance cost, interest etc.

(2) This cost depend upon the qty and period for which inventory is stored.

$$H.C = \text{Average Inventory} \times \text{Holding cost/unit/time}$$

Shortage Cost

- Shortage simply mean the absence of inventory and the loss associated with not serving the customer is termed as shortage or stockout cost. It include potential profit loss (PPL), breakdown cost, loss of product value, failure transportation cost, discount etc.

$$S.C = \text{Average no. of units short} \times \text{Shortage cost/unit/time}$$

Inventory classification

- 1) Transit or pipeline :- Inventory can not provide service while in transportation and such inventories called transit or pipeline inventory.

Decoupling inventory

- It is extra surplus semi finished inventory kept b/w interdependent work station which works as buffer stock during breakdown and maintenance.

(2) Buffer or Safety stock :- It is reserve stock kept throughout the year and it's held for protecting against future in the demand rate and lead time. It is never greater under normal working condition and used fully during adverse condition to prevent stockout.

Lead time

It is a time gap b/w placing an order and inventory on hand, so that it can be used or consumed.

Seasonal inventory

The demand for these inventory item changes with seasonal variation.

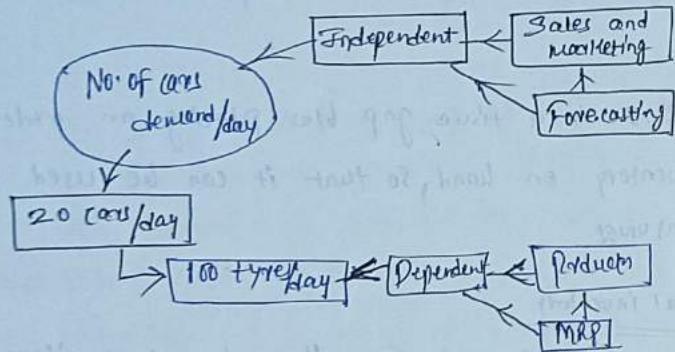
Anticipation inventory

These inventory are buildup to meet anticipated demand in future like big selling forecast, boom, policy change, price hike, strike, shutdown etc.

Q1 Inventory model characteristics:-

16-03-21

① Dependent and Independent demand item



Dependent

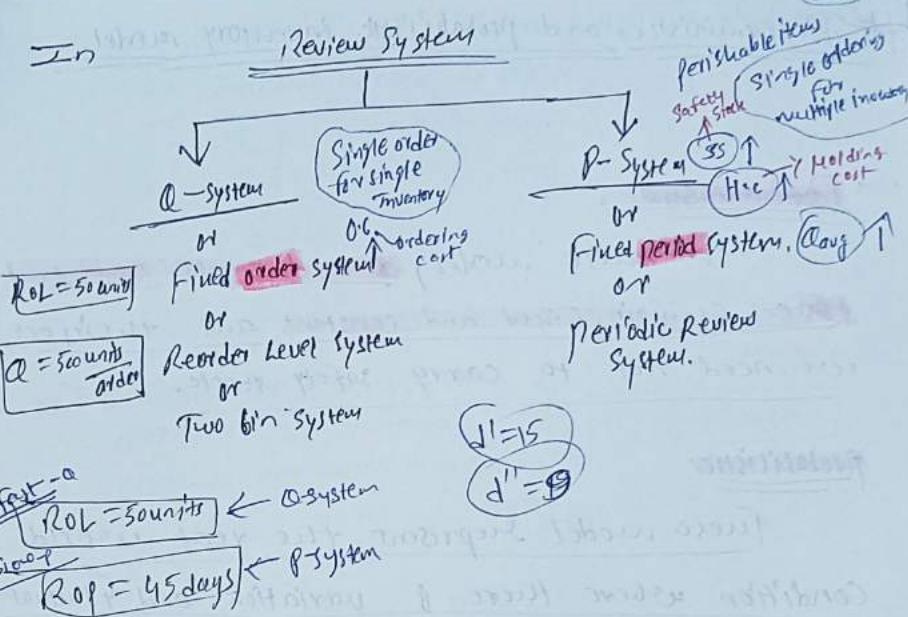
The demand for these items is directly related or linked to any other item, usually of a higher level of which it becomes a part.

Independent

The demand for these items is not directly related or linked to any other item, it is difficult to compute and is projected with the help of forecasting.

In Review System

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Fixed order system

In this system as inventory decreases to re-order level, a fresh order for fixed qty is placed at that point. In this system size of order is fixed but, the time of order is variable.

Fixed period system: In this system inventory is reviewed after a fix period of time and a fresh order for variable qty is placed at that point. In this system size of order is variable but the time of order is fixed.



Deterministic and Probabilistic Inventory model

T = time length of one inventory cycle or time gap b/w two successive orders. (Yearly)

$$T = \frac{1}{N}$$

They should be in
Similar unit
 $N = 4$ order/yr

$$T = \frac{1}{4} \text{ yr/order}$$

- To these model, demand rate and lead time remain fixed and constant and therefore we need not to carry safety stock.

Probabilistic

These model represent the real world condition where there is variation and fluctuation in the demand rate and lead time in these

model we need to carry safety stock to prevent stock out during adverse condition

- If yearly demand $D = d$
- $C = \text{Cost of placing one unit of inventory } (\text{₹}/unit)$
- $c_o = \text{Cost of placing one order. } (\text{₹}/order)$
- $c_h = \text{Holding cost or cost of holding one unit in inventory for a complete year. } (\text{₹}/unit/yr)$

Notations

D = Annual or yearly demand of inventory
(units/year)

c_o = Cost to be ordered at each order
Polar (units/order) or (Current policy)

$N \rightarrow$ No. of orders placed in a year
(order/year) $N = \frac{D}{c_o} = \frac{4800 \text{ units}}{600 \text{ units/order}}$

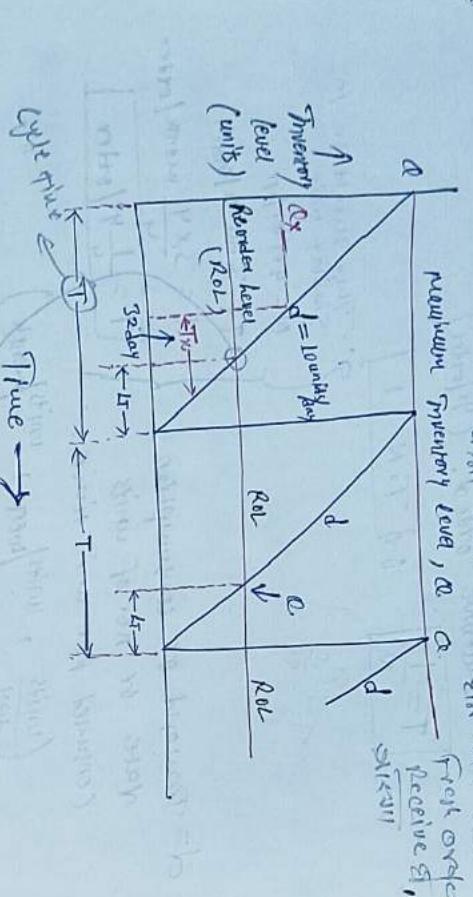
$$\boxed{N = \frac{D}{c_o}} \\ = 6 \text{ orders/yr}$$

Economic Order Qty (EOQ)

or
Farris Wilson model

1st Model

(26)



2 रोपन (Economic Order Quantity) पर लागत की तरफ लेने की दूसरी विधि द्वारा फ्रेक्चर ऑर्डर रिसेवर्स।

$$H_0, 30, 20, 10, 0$$

$$Q_{avg} = \frac{100}{5} = 20 \text{ units}$$

$$Q_{avg} = \frac{40+10}{2} = 20$$

$$H.C = 20 \times 5 \times 2$$

$$H.C = 200$$

$$H.C = \mu_1 200$$

$$H.C \text{ for period } T = \frac{Q}{2} \cdot H.C$$

$$\frac{Q}{2} = \frac{100}{2} = 50$$

$$Q_{avg} = 20 \text{ units}$$

$$Q_{avg} = \frac{40+10}{2} = 20$$

$$H.C = 20 \times 5 \times 2$$

$$H.C = \mu_1 200$$

$$H.C \text{ for period } T = \frac{Q}{2} \cdot H.C$$

$$\text{Annual H.C} = \frac{Q}{2} \cdot C_h \cdot (T.N) \rightarrow 1$$

$$H.C = \frac{Q}{2} \cdot C_h$$

$$TAC = P.C + \left(\frac{P}{C_o} \cdot C_o + \frac{Q}{2} \cdot C_h \right)$$

constant

$$\text{Total inventory cost} = \frac{P}{C_o} \cdot C_o = O.C$$

Total variable cost

$$T.V.C = \frac{P}{C_o} \cdot C_o + \frac{Q}{2} \cdot C_h$$

$$TAC \text{ or } T.C = T.V.C + O.C$$

$$\begin{aligned} \text{Total annual cost} &= \text{Purchase cost} + \text{Ordering cost} + \text{Holding cost} \\ (TAC \text{ or } T.C) & \\ P.C &= N \times C_o \\ O.C &= \frac{P}{C_o} \cdot C_o \\ O.C &= \frac{P}{C_o} \cdot C_o \end{aligned}$$

$$\begin{aligned} P.C &= P \times C_o \\ O.C &= N \times C_o \\ O.C &= \frac{P}{C_o} \cdot C_o \end{aligned}$$

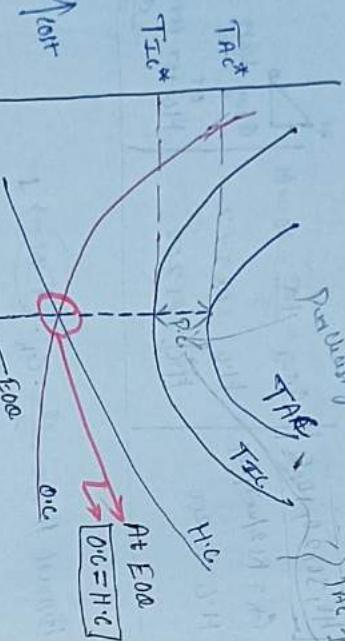
(27)

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$$\text{Total Cost} = P_C + Q_C$$

$$T_{IC}^* = \frac{Q^*}{2} \cdot C_h$$



order size (Q^*) \rightarrow

order holding cost

The ordering qty (Q^*) at which holding cost

become equals to ordering cost and total

inventory cost is known as

Economic order qty

(1) T_{IC} represents total cost
(2) $H.C$ represents holding cost

At EOQ

$Q^* = H.C$

$$\frac{P_c \cdot Q^*}{2} \cdot C_h$$

$$Q^* = \sqrt{\frac{2P_c \cdot C_h}{C_h}}$$

$$T_{IC}^* = \frac{P_c}{Q^*} \cdot Q^* + \frac{Q^*}{2} \cdot C_h$$

$$T_{IC}^* = 2 \times H.C = 2 \times Q^* C$$

$$T_{IC}^* = Q^* \cdot C_h$$

$$T_{IC}^* = \sqrt{2 D C_h}$$

$$\text{For } T_{IC} \text{ to be minimum } \frac{dT_{IC}}{dQ} = 0,$$

$$\frac{C_h}{2} - \frac{D \cdot C_o}{Q^*} = 0$$

2nd diff.

$$Q^* = \sqrt{\frac{2 D C_o}{C_h}}$$

$$+ \frac{2 \cdot D \cdot C_o}{Q^{*2}}$$

Note: When holding cost is given in terms of interest

on % It always correspond to unit price of

Inventory and interest rate should be always

year.

$$t_{sp} \cdot C_h = \% \text{ of } C$$

$$C = Rs \text{ / unit}$$

$$t_{sp} = 1 \text{ yr. / month}$$

$$t_{sp} = 12 \text{ yr. / year}$$

$$C_h = 0.12 \times 60 = Rs 7.2 \text{ / unit / yr.}$$

$$T_{IC}^* = 2 \frac{Q^*}{2} \cdot C_h \quad \text{--- from (1) and (2)}$$

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(Q) a. maximum inventory level is 3000 units and it is delivered with infinite rate of replenishment.

Inventory become zero in 110 months, due to consumption at uniform rate $C_0 = Rs 160/\text{order}$ C_h is Rs. $\alpha^2/\text{unit/month}$ then determine,

- Total inventory cost neglecting holding cost

(ii) Design a better ordering plan and find out the saving possible

$$\alpha = 3000 \text{ units/order}$$

$$T = 1.5 \text{ months/order} \rightarrow \text{Order interval}$$

$$N = \frac{12}{T} = 8 \text{ orders/year}$$

$$N = \frac{D}{\alpha} = P = 2400 \text{ units}$$

$$C_h = \frac{P}{Q} \cdot C_h \cdot \left(\frac{1}{T} \right)$$

$$C_h = \frac{P}{Q} \cdot C_h$$

$$C_h = Rs 30/\text{unit}^2/\text{year}$$

$$Savings = 5760 - 48000$$

$$(1) T_{TC} = \frac{P}{Q} \cdot C_0 + \frac{\alpha}{2} \cdot C_h$$

$$= 8 \times 160 + \frac{3000 \times 30}{2}$$

$$= Rs. 57600$$

$$(2) \alpha^* = \sqrt{\frac{2P C_0}{C_h}} = \sqrt{\frac{2 \times 24000 \times 160}{30}}$$

$$\alpha^* = 1600 \text{ units/order}$$

Vinice Ques
Q. Total inventory cost at order size of 100 units and 1600 units are equal then determine C_0 that is at?

$$\Rightarrow \text{Total inventory cost } T_{TC}(100) = T_{TC}(\alpha^*) = \frac{P}{Q} \cdot C_0 + \frac{\alpha}{2} \cdot C_h$$

$$\frac{P}{100} \cdot C_0 + \frac{100}{2} \cdot C_h = \frac{P}{1600} \cdot C_0 + \frac{1600}{2} \cdot C_h$$

$$P \cdot C_0 \left[\frac{1}{100} - \frac{1}{1600} \right] = C_h (800 - 200)$$

$$\frac{P \cdot C_0 \cdot 1600}{1600} = C_h \times 800$$

$$2 \cdot P \cdot C_0 = 1600 \times 800$$

$$\alpha^* = \sqrt{\frac{2P C_0}{C_h}} = \sqrt{1600 \times 800}$$

$$\alpha^* = 800 \quad \text{Then } \alpha^* = \sqrt{\alpha_1 \cdot \alpha_2}$$

Vinice Ques
Q. The demand of sugar at a retailer is 40 kg/day. And he purchase it @Rs 50/kg. Retailer spend Rs 200 for each order and the holding cost is Rs. 0.1/kg/day.

Lead time is of 3 days. The retailer current ordering policy is to order 200 kg every 5 day. Then determine

- EOQ
- Amount of saving with EOQ compared to current policy in 30 days.

$$d = 40 \text{ kg/day}$$

$$C_o = ₹ 50/\text{kg}$$

$$C_h = ₹ 200/\text{order}$$

$$C_h = ₹ 0.1/\text{kg/day}$$

$$LT = 3 \text{ days}$$

$$\alpha = 200 \text{ kg/order}$$

$$\boxed{\alpha = 200 \text{ kg/order}}$$

$\sum D_A$ if year demand

$$(i) \quad \alpha^* = \sqrt{\frac{2DC}{C_h}}$$

should be in similar units always.

$$= \sqrt{\frac{2 \times 40 \times 200}{0.1}}$$

$$\alpha^* = 400 \text{ kg/order}$$

(2) 30 days

$$D = 30 \times 40 = 1200 \text{ kg/month}$$

$$C_h = 30 \times 0.1 = ₹ 3/\text{kg/month}$$

$$\alpha = 200 \text{ kg/order}$$

$$TIC = \frac{D}{\alpha} \cdot C_o + \frac{\alpha}{2} \cdot C_h$$

$$= \frac{1200}{200} \times 200 + \frac{200}{2} \times 3$$

$$= ₹ 1500$$

$$(b) \quad \alpha^* = 400 \text{ kg/order}$$

$$TIC^* = \frac{1200}{400} \times 200 + \frac{400}{2} \times 3$$

$$\boxed{TIC^* = ₹ 1200, \text{ Saving} = ₹ 300}$$

Q. Determine value of EOQ when annual demand is worth ₹ 50000, C_o is 4% of order value and C_h is 10%.

of avg. inventory value

$$\Rightarrow D.C = ₹ 50,000 \text{ per year}$$

$$C_o = 4\% (D.C)_{\text{per yr}}$$

$$C_h = 10\% \text{ of } C$$

can only apply in order quantity cost

$$\alpha^* = \sqrt{\frac{2D C_o}{C_h}}$$

$$\alpha^* = \sqrt{\frac{2 \times 50,000 \times 0.04 \times \alpha^* \cdot C_o}{C_h \times 0.1 \times C_h}}$$

why?

$$\alpha^* = \frac{40,000 \times C_o}{C_h}$$

$$\boxed{\alpha^* \cdot C_h = ₹ 40,000}$$

Q. In a production system

$$D = 10000 \text{ units/yr}$$

Best to
keep
level
lead
time

$$C_o = ₹ 8/\text{unit}$$

$$C_h = ₹ 0.01 \text{ per unit per day}$$

$$C_h = ₹ 0.01 \times 10000 \times 0.01$$

Op. & Int歇 = 5%
of
Damage = 2%

Transportation = 3%.

part of storage = 5%.

LT = 60 days

30 working days/yr

thus determine

Q) Given determine

Note:- ~~always will be equal to zero~~

(i) α^*

(ii) optimum no. of orders in a year

(iii) amount of saving with EOQ against the

earlier practice of 4 orders in a year.

(iv) increase in total cost associated with

ordering

(a) 25% more than EOQ

(b) 25% less than EOQ

\Rightarrow

$$(1) \alpha^* = 3000 \text{ units/order}$$

$$(2) N^* = \frac{D}{\alpha^*} = 6 \text{ orders/year}$$

$$(3) T^* = \frac{1}{N^*} = \frac{1}{6} \text{ yr/order} \Rightarrow T^* = 50 \text{ days/order}$$

$$(4) TIC^* = \sqrt{2 D C_o} \text{ days/year} \text{ So, } \frac{300}{6} = 50 \text{ days/order}$$

$$= \underline{\underline{Rs\ 2880}}$$

$$(5) ROL = L T C_d$$

$$d = \frac{18000}{300} \rightarrow d = \frac{Q}{T}$$

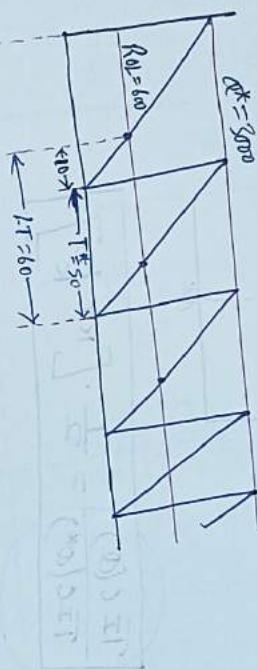
$$d = 60 \text{ units/day}$$

$$\text{ROL} = 60 \times 60 \\ \text{ROL} = 3600 \text{ unit}$$

This is wrong should
not write it
in year

$$\text{effective LT} = 60 - 50$$

$$\text{ROL} = 10 \times 60 = 600 \text{ units}$$



$$(6) 10 \text{ days}$$

$$N = \frac{D}{\alpha} = 1$$

$$T^* = 4 \times 240 + \frac{4500}{2} \times 0.96 = \underline{\underline{Rs.\ 3120}}$$

$$\text{Saving} = \underline{\underline{Rs.\ 3120}} - \underline{\underline{Rs.\ 2880}} = \underline{\underline{Rs.\ 240}}$$

$$\text{⑥ a) 25% more than } \alpha^*$$

$$\text{⑥ b) } \alpha = 105 \times 3000 = 3750 \text{ unit/order}$$

$$\text{TIC} = \frac{18000}{3750} \times 240 + \frac{3750}{2} \times 0.96$$

$$= \underline{\underline{Rs.\ 2952}}$$

$$\text{Increase} = 2952 - 2880 = \underline{\underline{Rs.\ 72}}$$

2nd model with EOQ with price break

or
Quantity discount

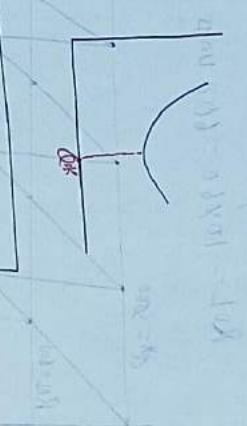
(b)

25% less than α^*

$$\alpha = 0.75 \times 3000 = 2250 \text{ units/order}$$

$$TTC = Rs 3000$$

$$\text{Increase} = Rs 120 \uparrow$$

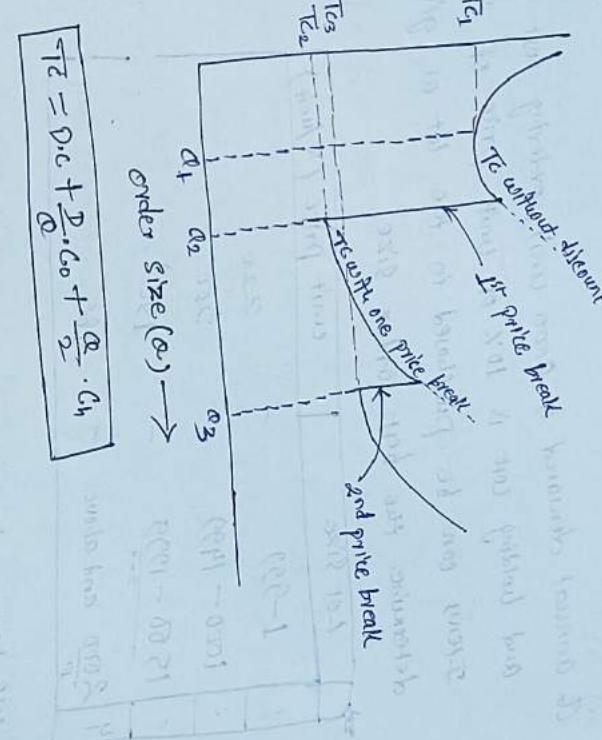


$$\frac{TTC(\alpha)}{TTC(\alpha^*)} = \frac{1}{2} \cdot \left[k + \frac{1}{k} \right] - 1$$

model sensitivity
or
model robustness

$$\alpha = k \cdot \alpha^*$$

prob. of
prob. of
prob. of



$$TTC = D \cdot C_0 + \frac{D}{Q} \cdot C_h + \frac{Q}{2} \cdot C_o$$

In some condition discount is offered on unit price of inventory for large qty purchase and these discount take the form of price break. As discount is always offered on unit price of inventory, in order to determine fix best order qty we need to

consider purchasing cost along with ordering and holding cost. In these problem first we compute

$$\frac{TTC}{2880} = \frac{1}{2} \left[1.25 + \frac{1}{1.25} \right] - 1$$

$$TTC = 2252$$

$$\text{order quantity} = 0.75 \times 3000 = 2250$$

$$25\% \text{ discount} = 0.75 \times 3000 = 2250$$

$$25\% \text{ discount} = 0.75 \times 3000 = 2250$$

(3) Feasible EOQ and then total cost is computed at EOQ and the next higher order size having price break, whenever the total cost comes out to be minimum give the best order size.

(3) $C = \text{Rs } 190/\text{unit}$
 $Q^* = \sqrt{\frac{2 \times 8000 \times 100}{(190 \times 0.1)}} = \frac{1231.17}{2^{nd}} \text{ units/order}$

$$(2) C = \text{Rs } 200/\text{unit}$$

$$Q^* = \sqrt{\frac{2 \times 8000 \times 100}{200 \times 0.1}} = 1200 \text{ units/order}$$

It is feasible as for $C = \text{Rs } 200/\text{unit}$, Q must be 600 less than 1999.

So we can determine the best order size.

Lot Size	Unit Price (₹/unit)
1-999	- 220
1000-1499	- 200
1500-1999	- 190 ^{1st price break point}
2000 and above	- 185 ^{2nd price break point}

We know that

$$\text{EOQ i.e. } Q^* = \sqrt{\frac{2D_C}{C_h}}$$

where $C_h = 10\% \text{ of } C$

Feasibility (1) $C_h = 10\% \text{ of } \text{Rs } 185/\text{unit} \Rightarrow$

$$Q^* = \sqrt{\frac{2 \times 8000 \times 100}{(185 \times 0.1)}} = \frac{1247.7}{1^{st}} \text{ units/order}$$

It is not feasible as for $C = \text{Rs } 185/\text{unit}$

$$Q^* \geq 2000 \Rightarrow \text{must be greater than}$$

So at 2000 lot is minimum when $EOP = 2000 \text{ lot}$

$$(3) C = \text{Rs } 190/\text{unit}$$

$$Q^* = \sqrt{\frac{2 \times 8000 \times 100}{(190 \times 0.1)}} = \frac{1231.17}{2^{nd}} \text{ units/order}$$

Again not feasible must be within range 1500-1999

(4)

$$1800 \rightarrow 1545/100$$

$$2400 \rightarrow 15082/100$$

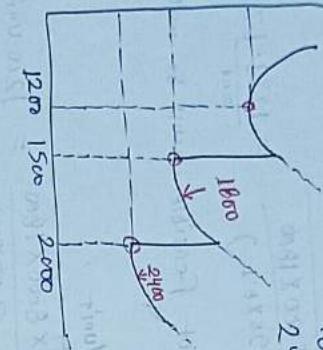
1624/100

1545/100

15082/100

15057/100

1200 1500 2000



~~$\alpha / D = 5000 \text{ units/yr}$~~

$c = \frac{1}{2} \cdot 5000$

$c_0 = \frac{1}{2} \cdot 80/\text{order}$

$C_h = 20.8 \cdot 0.04/100$

$\text{If } \alpha = 2500, 6\% \text{ discount on } c \rightarrow 4.7 \rightarrow R_s 24660$

$\alpha = 5000, 9\% \text{ discount on } c \rightarrow 4.7 \rightarrow R_s 24660$

Determine best order size?

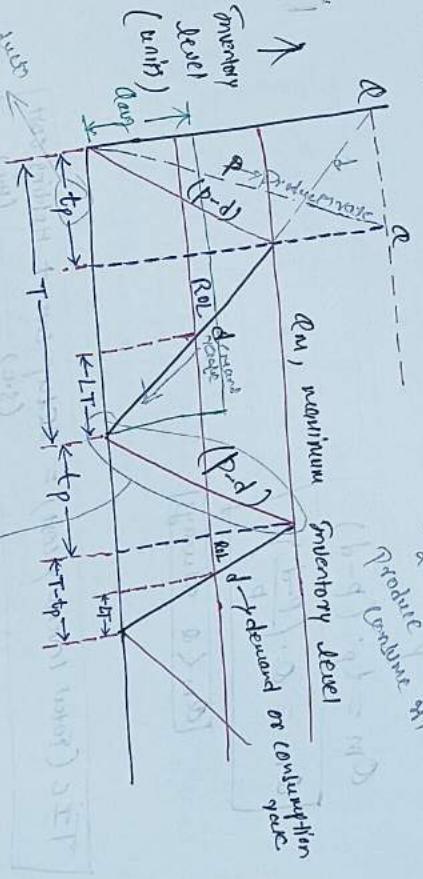
$$\Rightarrow \text{we know that } EOQ \quad \alpha^* = \sqrt{\frac{2Dc_0}{c_1}}$$

$$= \sqrt{\frac{2 \times 5000 \times 80}{0.8}}$$

instantaneous.

This model is similar to the EOQ model, the only difference is the inventory buildup is gradual (rather than instantaneous).

Total cost of the Product and buildup model



$$TC(5000) = 5000 \times 4.55 + \frac{5000}{2} \times 80 + \frac{5000}{2500} \times 0.8$$

$$TC(5000) = 24830$$

$\alpha \rightarrow \alpha^*$ to be produced or manufactured in every setup (units/setup)

$c_0 \rightarrow$ cost of one setup (\mathbb{Z}/setup)

$T_p \rightarrow$ production or manufacturing time.

$p \rightarrow$ Production or buildup rate
 $d \rightarrow$ Demand or consumption rate

$p > d$ \rightarrow should be

$$Q = T \cdot d$$

$$Q = t_p \cdot p$$

$$t_p = \frac{Q}{p}$$

$$Q_m = t_p \cdot (p-d)$$

$$Q_m = Q \cdot \left(\frac{p-d}{p} \right)$$

$Q_m < Q$ always

$$TIC \text{ (Total Inventory Cost)} = \text{Setup Cost} + \text{Holding Cost}$$

$$S.C = \text{No. of Setup} \times \text{Cost/Setup}$$

$$S.C = \frac{D}{Q} \cdot C_0$$

$$H.C = Q_m \cdot C_h$$

- a. A company requires 12000 units in a year and it is produced in 40 batches of 300 units each on a w/c that produces 8 units/hr. The company operates for 4000 hrs/yr costs \$500/setup and $C_h = \$15/\text{unit/hr}$. Find out whether the existing production plan is optimum and if not, design a better ordering plan and find the amount of saving possible. Also determine prod'ng quantity level.

$$\text{Area of trapezoid} = \text{Area of triangle}$$

$$Q_m = \frac{a}{2} \cdot \left(\frac{p-d}{p} \right)$$

$$\text{Avg } X_T = \frac{1}{2} \times TX_{dm}$$

$$\text{Avg } = \frac{Q_m}{2}$$

$$\frac{dTIC}{dQ} = 0,$$

$$\frac{C_h}{2} \left(\frac{p-d}{p} \right) - \frac{D}{Q^2} \cdot C_0 = 0$$

$$Q^* = \sqrt{\frac{2DC_0}{C_h} \cdot \left(\frac{p}{p-d} \right)}$$

$$Q^* = \frac{2DC_0}{C_h} \cdot \sqrt{\frac{p}{p-d}}$$

Production factor > 1

At $E \infty$

$$S.C = H.C$$

$$TIC^* = \sqrt{2DC_0C_h}$$

$$\sqrt{\frac{p-d}{p}}$$

(1)

Total inventory cost (TIC) = $\frac{Q}{2} \cdot C_h \cdot (p-d)^2$

For TIC to be minimum

(44) and total cycle time corresponding to optimum condition

$$\Rightarrow D = 12000 \text{ units/yr}$$

$$N = 40, \alpha = 300$$

$$P = 8 \text{ units/lot}$$

$$4000 \text{ lots/yr}$$

$$C_o = Rs. 500/\text{setup}$$

$$C_h = Rs. 15/\text{units/yr}$$

$$d = \frac{12000}{4000} = 3 \text{ units/lot}$$

$$(1) d^* = \sqrt{\frac{2C_o \cdot (\frac{P}{P-d})}{C_h}} = 1131.37 \text{ units/setup}$$

$$T_{IC}^* = \sqrt{\frac{2C_o \cdot C_h \cdot (\frac{P-d}{P})}{d}} \Rightarrow \sqrt{2 \times 12000 \times 500 \times 15 \left(\frac{8-3}{8}\right)}$$

= Rs 10606.6 \rightarrow Should not be in frame

a/b setup cost too

$$N^* = \frac{D}{d^*} = \frac{12000}{1131.37} = 10.6 \text{ setup/yr}$$

first
time above
10.6

$$N = 11, \alpha = \frac{12000}{11} = 1090.9 \times \text{Should be in}$$

$$(10N = 12), d = \frac{12000}{12} = 1000$$

Now below 10.6

$$(b) N = 10, \alpha = \frac{12000}{10} = 1200$$

PRO

$$\text{Now } T_{IC}(\alpha) = \frac{D}{\alpha} \cdot \cot \frac{\alpha}{2} \cdot C_h \cdot \left(\frac{P-d}{P} \right)$$

$$T_{IC}(1000) = \frac{12000}{1000} \text{ sec}$$

$$(2) N = 10, \alpha = 1200$$

$$T_{IC} = Rs. 10687.5$$

$$T_{IC} = \frac{1}{2} \times 12000 + \frac{300}{2} \times 15 \times \left(\frac{5}{8}\right)$$

Now current policy is

$$N = 40, \alpha = 300$$

$$T_{IC} = 40 \times 500 + \frac{300}{2} \times 15 \times \left(\frac{5}{8}\right)$$

$$\text{Saving} = 21406.25 - 10625 \Rightarrow 10781.25 \text{ Ans}$$

$$-10000 \text{ Production time}$$

$$t_p = \frac{\alpha}{P} = \frac{1200}{8} = 150 \text{ hrs/setup}$$

$$Q_u = t_p \cdot (P-d) = 150 \times 5 = 750 \text{ units/setup Ans} \frac{3}{2}$$

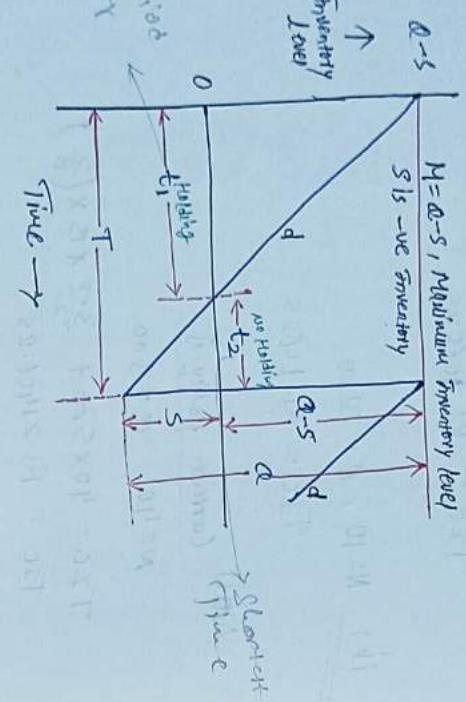
$$\boxed{T = \frac{\alpha}{d} = \frac{1200}{3} = 400 \text{ hrs/setup Ans}}$$

PRO

(46)

4th
Model

Shortage or Stockout Or Backorder model



$$C_h \rightarrow (\$/unit/year)$$

$$TIC = O.C + H.C + \text{Shortage cost (S.C)}$$

$$\text{Annual holding cost} = \frac{D}{Q} \cdot C_h$$

$$\text{Annual H.C} = \frac{(Q-S)^2}{2Q} \cdot C_h$$

$$S.C = \frac{s^2}{2a} \cdot C_s$$

$$H.C \text{ for Period } T$$

$$= \frac{1}{2} \left(\frac{Q-S}{2} \right) \cdot t_1 \cdot C_h$$

$$(Q-S) = t_1 \cdot d$$

$$Q = T \cdot d$$

On dividing

$$\frac{t_1}{T} = \frac{Q-S}{Q}$$

$$t_1 = \left(\frac{Q-S}{Q} \right) \cdot T$$

$$H.C \text{ for Period } T$$

$$= \left(\frac{Q-S}{2} \right) \cdot \left(\frac{Q-S}{Q} \right) T \cdot C_h$$

$$= \left(\frac{Q-S}{2Q} \right)^2 \cdot C_h \cdot T$$

$$\text{Annual H.C} = \left(\frac{Q-S}{2Q} \right)^2 \cdot C_h \cdot T \cdot N + 1$$

- $S \rightarrow$ no. of units short or back order
- $C_h \rightarrow$ backorder or shortage cost per unit balance ordered per year ($\$/unit/year$)

This model is similar to 1st model ~~for the only~~ difference shortages are allowed. Planned shortage or backorder is the condition when a customer places an order and finds that inventory is out of stock then he wait for the next shipment then to get his order fulfilled

S.C. for period T

$$= \frac{S}{2} \cdot t_2 \cdot c_b$$

$$S = t_2 \cdot d$$

$$Q = T \cdot d$$

On dividing

$$\frac{t_2}{T} = \frac{S}{d}$$

$$t_2 = \frac{S}{d} \cdot T$$

Shortage cost S.C. for period T

$$= \frac{S}{2} \cdot \frac{S}{d} \cdot T \cdot c_b$$

$$= \frac{S^2}{2d} \cdot c_b \cdot T$$

$$\text{Annual S.C.} = \frac{S^2}{2d} \cdot c_b \cdot T \cdot N$$

$$\bar{TIC} = \frac{D}{\alpha} \cdot c_o + \left(\frac{\alpha - S}{2\alpha} \right)^2 c_h + \frac{S^2}{2\alpha} \cdot c_b$$

$$Q^* = \sqrt{\frac{2Dc_o}{c_h}} \cdot \sqrt{\frac{c_b + c_h}{c_b}}$$

$$M^* = Q^* - S^*$$

$$N^* = Q^* \cdot \frac{c_b}{c_b + c_h}$$

Normal inventory level

$c_b \rightarrow \infty$

$$\sqrt{1 + \frac{c_o}{c_b}} \rightarrow \infty$$

$$c_o = 1000/\mu_{0.01}/41$$

$$c_h = 1000/\mu_{0.01}/41$$

Optimum no. of units backordered OR
Short (S*)

$$\frac{Q^* - S^*}{S^*} = \sqrt{\frac{c_b}{c_h}}$$

Holdup cost in right side of graph
Equivalent shortage cost

$$(Q^* - S^*) \times c_h = S^* \times c_b$$

Shortage cost

$$\frac{Q^* - S^*}{S^*} = \frac{c_b}{c_h}$$

Addition + 1 both side

$$\frac{Q^*}{S^*} = \frac{c_b + c_h}{c_h}$$

$$S^* = Q^* \cdot \frac{c_h}{c_b + c_h}$$

$$\boxed{AT EOQ \quad D.C. = H.C. + S.C.}$$

$$\boxed{T.I.C.^* = \sqrt{2Dc_o c_h} \cdot \sqrt{\frac{c_b}{c_b + c_h}}} < 1$$

(20)

Chowdhury and Sharmin Product and Shortage model (p, c_b)

$$Q^* = \frac{2Dc_o}{C_h} \cdot \sqrt{\frac{p}{p-d}} \cdot \sqrt{\frac{C_h + C_b}{C_b}}$$

$$\overline{TIC}^* = \sqrt{2Dc_o} \cdot \sqrt{\frac{p-d}{p}} \cdot \sqrt{\frac{C_b}{C_b + C_h}}$$

Case-II $\rightarrow p \rightarrow \infty$, shortage

Case-II $\rightarrow C_b \rightarrow \infty$, production

Case-III $\rightarrow p \rightarrow \infty$, $C_b \rightarrow \infty$, EOC.

BOB/3/21

A Dealer supplies the following information: $D = 10000$ units/yr

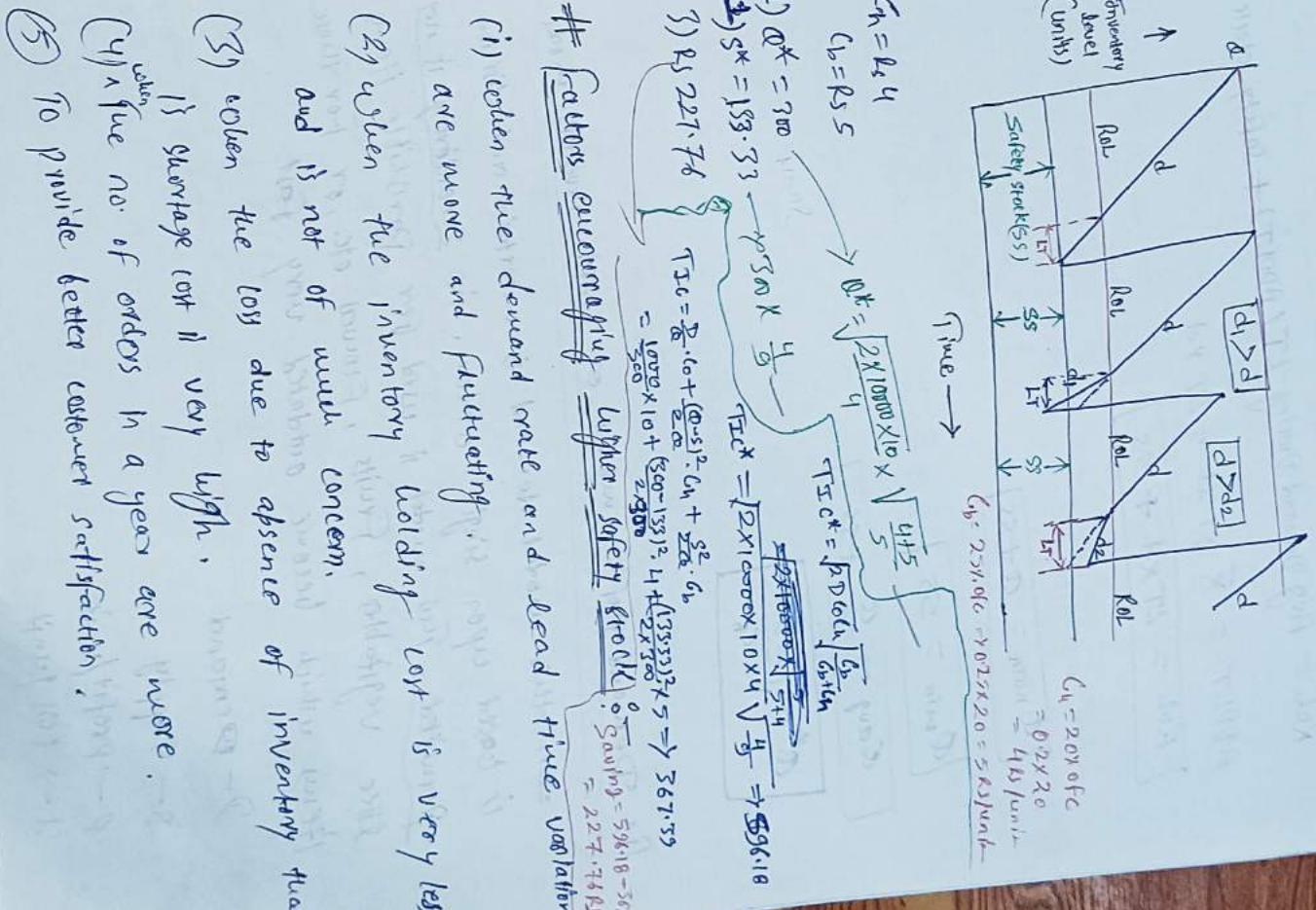
$C_h = \$200$ /unit, $c_o = \$10$ /order and $C_b = 20\%$ of unit price of inventory.

Dealer is considering the possibility of back ordering. Dealer is considering the possibility of back ordering and he has estimated that the annual cost of back ordering is 25% of unit price of inventory. Thus, determine:

(i) optimum no. of units back ordered

(ii) optimum order quantity

(iii) the amount of saving possible by adopting the policy of back ordering



$R_o = \text{Avg Demand During } LT (\text{ADLT}) + \text{Safety stock (SS)}$

$$\text{ADLT} = R \text{ or } d - LT \times d$$

$$R_o = LT \times d + SS$$

Planning Period

$$\sigma_{\text{plan}} = \sigma + SS$$

$$\sigma_{\text{min}} = SS$$

$$\text{Avg} \rightarrow \frac{\sigma}{2} + SS$$

$$\sigma^* = \sqrt{\frac{2Dc_o}{C_h}}$$

Planning Period
No. of days in planning period = 100
Demand expectation = 1000 units
Order quantity = 1000 units

1) Demand profit model or static inventory model

In this model demand is uncertain and discrete

is based upon single order, i.e. back ordering is not permitted. This model is used for Perishable items like vegetables, fruits, flowers etc. or for those items which become outdated very fast.

D - Demand

S - Supply

P - Profit/unit
 $d \rightarrow$ Loss/unit

$$(i) \text{ If } D_o > S_o \rightarrow [B - D] \cdot P$$



loss

$$\frac{1}{500}$$

$$\frac{1}{500}$$

$$\frac{1}{500}$$

$$\frac{1}{500}$$

P = Profit/unit for not meeting the demand

S_p = Selling price / unit

C = Purchasing cost / unit

C_b = Back order or shortage cost or goodwill loss / unit

L = Holding item cost / unit due to over supply

G = Salvage or scrap value / unit or segregate value

or holding cost / unit

For this model in order to maximize profit, we select ordering qty (S) such that

Cumulative probability of true demand for S units

$$P(S-1) < \frac{P}{P+1} \leq P(S)$$

Cumulative probability for
of the demand for
of the demand for
S-1 units

(56)

Service level model

(16) Model is preferred where the different cost factors involved with inventory are not known exactly, it is based upon probability theory and the amount of safety stock is kept according to the level of service management want to achieve.

$$\text{Service level} = \frac{\text{No. of units supplied without delay}}{\text{Total no. of units demanded}}$$

$$= 0.95 \rightarrow 90\% \text{ to } 100\%$$

$$= 0.99 \rightarrow 99\%$$

95% Service level is the standard value and it means that 95% of the customer order on an average are fulfilled during lead time and only 5% of the customers' order on an avg are rejected during lead time.

When the demand during lead time may be approximated by a normal distribution with certain avg (\bar{X}) or u and std deviation (σ) then the reorder level is given by

$$ROL = \bar{X} + Z \cdot \sigma$$

$$Z = 1.96$$

where \bar{X} = avg demand during lead time.

$$Z = ADDT = kT \cdot q$$

σ = Std deviation for the demand variation during lead time

$kT \cdot q$ = Std normal variate whose value depend upon the service level required.

$$0.84 - 80\%$$

$$1.28 - 90\%$$

$$1.645 - 95\% \text{ Min}$$

$$2.33 - 99\%$$

