DESCRIPTION

BHS

$$unsteady - stocks - 3D$$

$$\mathbf{v}_{t} - \alpha \nabla^{2} \mathbf{v} + \nabla p = \mathbf{f}, \quad in \quad \Omega_{T}$$

$$\nabla \cdot \mathbf{v} = 0, \quad in \quad \Omega_{T}$$

$$\mathbf{v}|_{\partial \Omega} = 0, \quad on \quad \partial \Omega_{T}$$

$$\mathbf{v}|_{t=0} = \mathbf{v}_{0}, \quad on \quad \Omega$$

$$\alpha = 0.025$$

$$\mathbf{v} = [u_1(t, x), u_2(t, x), u_3(t, x)]$$

$$x_1 \in [0, 1], x_2 \in [0, 1], x_3 \in [0, 1], t \in [0, 1]$$

$$u_1(t, x) = \sin(t)\sin(\pi x_1)^2(\sin(2\pi x_2)\sin(\pi x_3)^2 - \sin(\pi x_2)^2\sin(2\pi x_3))$$

$$u_2(t, x) = \sin(t)\sin(\pi x_2)^2(\sin(2\pi x_3)\sin(\pi x_1)^2 - \sin(\pi x_3)^2\sin(2\pi x_1))$$

$$u_1(t, x) = \sin(t)\sin(\pi x_3)^2(\sin(2\pi x_1)\sin(\pi x_2)^2 - \sin(\pi x_1)^2\sin(2\pi x_2))$$

$$p(t, x) = \sin(t)\sin(\pi x_1)\sin(\pi x_2)\cos(\pi x_3)$$

References

[1] Jing Yue, Jian Li. The Physics Informed Neural Networks for the unsteady Stokes problems [J]. International Journal for Numerical Methods in Fluids.