

$$30 \cdot x \equiv_{18} 6$$

Schritt 1:

$$\text{ggT}(30, 18) = 6 \quad | \quad 6 \quad \checkmark$$

Schritt 2:

$$5 \cdot 5 + 4 \cdot 3 = 1$$

$$s_0 = 2$$

$$t_0 = -3$$

$$x_0 = 2 \cdot \frac{6}{6} \bmod \frac{18}{6}$$

$$= 2 \bmod 3$$

$$= 2$$

$$L = \{ 2 + (i-1) \cdot 3 \mid 0 < i \leq 6 \}$$

$$= \{ 2, 5, 8, 11, 14, 17 \}$$

$$x \equiv_3 2$$

$$x \equiv_5 1$$

$$x \equiv_7 6$$

Schritt 1:

$$M = 105$$

$$M_1 = 35$$

$$M_2 = 21$$

$$M_3 = 15$$

Schritt 2:

$$35 \cdot x \equiv_3 1$$

$$8s + 3t = 1$$

$$s = -1; t = 12$$

$$x_{01} = -1 \cdot 1 \bmod 3 \\ = 2$$

$$21 \cdot x \equiv_5 1$$

$$21s \cdot 5t = 1$$

$$s = 1 \quad t = -4$$

$$x_{02} = 1 \cdot 1 \bmod 5 \\ = 1$$

$$15x \equiv_7 1$$

$$15s \cdot 7t = 1$$

$$s = 1 \quad t = -2$$

$$x_{03} = 1 \cdot 1 \bmod 7 \\ = 1$$

Schritt 3:

$$\begin{aligned}x_0 &= (2 \cdot 35 \cdot 2 + 1 \cdot 21 \cdot 1 + 6 \cdot 15 \cdot 1) \bmod 105 \\&= 251 \bmod 105 = 61\end{aligned}$$