

Final project

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Introduction

The original idea on this project was using Sentence Transformers(SBERT, for reference view <https://sbert.net/>) embedding to classify, human and AI generated text. However this attempt was unsuccessful because features that were extracted from SBERT failed to capture any significant information as shown in t-SNE plot below. Seeing this, choose to fine tune pretrained LLM RoBERTa.

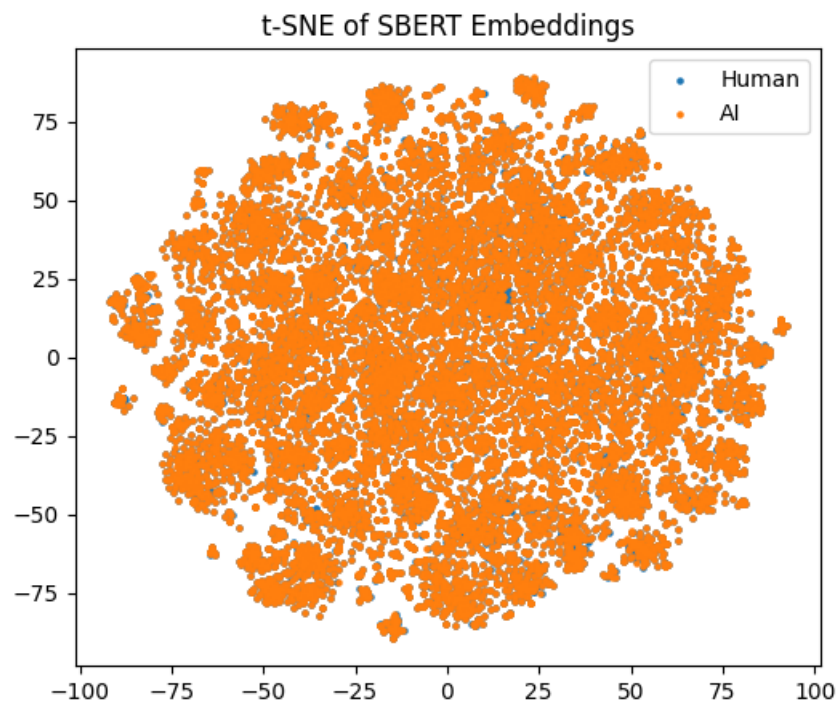


Figure 1: t-SNE plot of SBERT feature

Theoretical Background

Perceptrons and Deep Models

Back propagation and fine tuning

Transformers and attention mechanism

RoBERTa and LLM

Methods

Our approach combines sentence-level encoding with a multi-attention mechanism to classify paragraph-level text. This method is based on our assumption that GPT will have hard time

RoBERTector

RoBERTector is finetuned RoBerta that specify on AI detection on sentence level. it's predictive abilities were Accuracy: 0.8648 F1 Score: 0.8644 on validation set.

Architecture

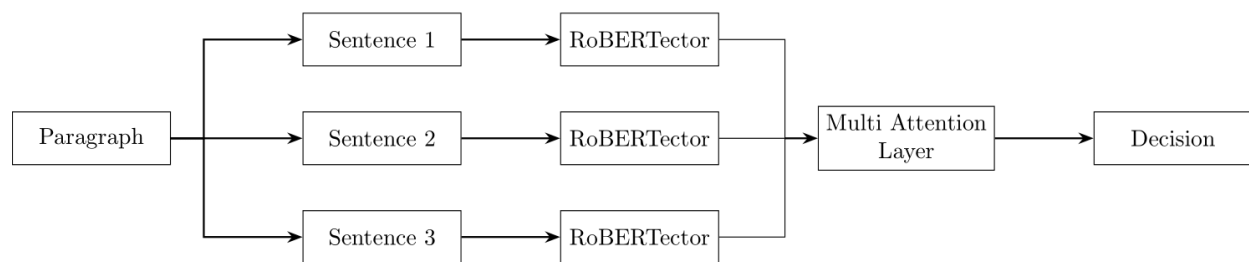


Figure 2: Architecture

A paragraph’s “main content” is concentrated in a small subset of its sentences, and by assigning higher attention weights to those key sentences (and down-weighting the rest), the model can accurately classify the paragraph as AI-generated vs. human-written. This main content is valid because of various point of view, psycholinguistics, cognitive science, deep-learning.

Perspective in Psycholinguistics

People tend to focus on main point of view instead of remembering all details. This is because gist information is more efficiently encoded, thereby being meaningful into memory. People prefer the most meaningful portion of the text, so people usually remember the main idea most. Also, according to Van Dijk and Kintsch’s discourse comprehension theory, people are reported to remember contents by compressing and generalizing to macro-level semantic structure (gist).

Perspective in Cognitive Science

It is proved in cognitive science fields that people get their attention on main ideas. Our cognitive system processes and emphasizes data selectively rather than catching full context at once. For example, when we write essays, people usually loads the most information, main idea, into the first sentence or paragraph instead of spreading contexts into paragraph or full text.

Application in Deep-Learning

Attention mechanism, which is utilized in this research, is a technology that aimed to weigh more on main factors. This is inspired by selective cognition mechanism of people, and led to optimization in model efficiency by lowering the burden to encode long text at once.

In special, Multi-Head Attention uses lots of attention heads, so it collects complex main information in parell. Through this mechanism, attention layer assigns high value in most informative sentences while considering sentence-sentence interactions. So, in summry, the model creates embedding that represents full meaning by focusing main sentences in the text.

Our model begins by **splitting each paragraph** into at most 16 sentences. We scan for sentence delimiters (., ?, !), trim whitespace, and discard empty fragments. If a paragraph produces fewer than 16 sentences, we pad the remainder with dummy tokens; if it exceeds 16, we simply truncate after the 16th. This approach guarantees every input tensor has a fixed shape (`batch_size` × 16 × `max_length`), which simplifies batching and avoids dynamic control-flow overhead.

Next, each of these up to 16 sentence slots is **encoded independently** by RoBERTector(a RoBERTa model that was previously fine-tuned on sentence-level AI vs. human text classification). By freezing all of RoBERTector’s parameters, we preserve its robust ability to capture subtle stylistic and lexical cues (word choice, phrasing patterns, function-word frequencies) without risking over-fitting on our comparatively small paragraph dataset. From each sentence’s transformer output we extract the CLS token embedding (a 768-dimensional vector), producing a tensor of shape (`batch_size`, 16, 768).

These 16 sentence embeddings are then fed into a **multi-head self-attention layer** (four heads, `embed_dim=768`). Because the Query, Key, and Value all derive from the same set of sentence embeddings, the attention mechanism learns to assign higher weights to the most informative sentences—thesis statements, topic transitions, or discourse markers—while down-weighting less relevant ones. The attended outputs are mean-pooled across the sentence axis, yielding a single 768-dimensional “paragraph embedding” that fuses both micro-level sentence cues and macro-level discourse structure.

Finally, a **lightweight classification head** (a two-layer MLP with ReLU and dropout) maps this paragraph embedding to a single logit. We apply `BCEWithLogitsLoss` during training—combining sigmoid activation and binary cross-entropy in a numerically stable way—and use a 0.5 threshold on the sigmoid probability to make the AI vs. human decision. We train only the attention and MLP head (leaving RoBERTector frozen), save model checkpoints after every epoch, and evaluate on an 80/10/10 train/val/test split of our ~20 000-paragraph dataset (with test performed just once at the end).

By **reusing** a specialized sentence encoder, **learning** which sentences truly matter via attention, and **regularizing** most of the model by freezing, this architecture achieves high accuracy and generalization while remaining interpretable: attention weights can be visualized to show exactly which sentences drove each classification.

Training

Set up python enviroment

Install packages

Fine tune RoBERTa

Load data and split paragraphs into sentences

```
import pandas as pd
df=pd.read_csv('/kaggle/input/ai-text/ai_press_releases.csv')
df=df.dropna()
human=df['non_chat_gpt_press_release']
ai=df['chat_gpt_generated_release']
hu=[]
a=[]
for i in human:
    l=list(i.split('. '))
    hu.extend(l)
for i in ai:
    l=list(i.split('. '))
    a.extend(l)

ap=a.copy()
a.extend(hu)
texts=a
labels=[0 if i<len(ap) else 1 for i in range(len(texts))]
from sklearn.model_selection import train_test_split

#split train, test and validation data.
texts_train_val, texts_test, labels_train_val, labels_test = train_test_split(
    texts,
    labels,
    test_size=0.2,          # 20% of the entire dataset
    random_state=42,
    stratify=labels        # Maintain label distribution
)

# 2) Split train_temp again into train (75% of temp + 60% of the total) and val (25% of temp + 20% of t
texts_train, texts_val, labels_train, labels_val = train_test_split(
    texts_train_val,
    labels_train_val,
    test_size=0.25,        #25% of train_temp + 0.2 of total
    random_state=42,
    stratify=labels_train_val
)

print(f"Train: {len(texts_train)} samples")
print(f"Valid: {len(texts_val)} samples")
print(f"Test : {len(texts_test)} samples")
```

Load Roberta and fine tune

```
import torch
from torch.utils.data import DataLoader
from transformers import AutoTokenizer, AutoModelForSequenceClassification
from torch.optim import AdamW
from datasets import Dataset
from tqdm.auto import tqdm
from sklearn.metrics import accuracy_score, f1_score

# Load pretrained tokenizer
tokenizer = AutoTokenizer.from_pretrained("roberta-base")

# Function to prepare batch inputs
def collate_fn(batch):
    enc = tokenizer(
        [x["text"] for x in batch], # Extract texts
        padding="longest", # Pad to the longest in batch
        truncation=True, # Truncate if too long
        max_length=256, # Limit to 256 tokens
        return_tensors="pt" # Return PyTorch tensors
    )
    enc["labels"] = torch.tensor([x["label"] for x in batch], dtype=torch.long)
    return enc

# Convert to HuggingFace Dataset format
train_ds = Dataset.from_dict({"text": texts_train, "label": labels_train})
val_ds = Dataset.from_dict({"text": texts_val, "label": labels_val})
test_ds = Dataset.from_dict({"text": texts_test, "label": labels_test})

# Create PyTorch DataLoaders
train_loader = DataLoader(train_ds, batch_size=16, shuffle=True, collate_fn=collate_fn)
val_loader = DataLoader(val_ds, batch_size=32, shuffle=False, collate_fn=collate_fn)
test_loader = DataLoader(test_ds, batch_size=32, shuffle=False, collate_fn=collate_fn)

# Model and optimizer configuration
device = torch.device("cuda" if torch.cuda.is_available() else "cpu") # Use GPU if available
model = AutoModelForSequenceClassification.from_pretrained("roberta-base", num_labels=2).to(device) #
optim = AdamW(model.parameters(), lr=2e-5) # Use AdamW optimizer

num_epochs = 8 # Train for 8 epochs

# Training loop
for epoch in range(1, num_epochs+1):
    # 1) Training phase
    model.train()
    train_loop = tqdm(train_loader, desc=f"Epoch {epoch}/{num_epochs} [TRAIN]") # Show progress
    for batch in train_loop:
        batch = {k: v.to(device) for k, v in batch.items()} # Move to GPU
        outputs = model(**batch) # Forward pass
        loss = outputs.loss
        optim.zero_grad() # Reset gradients
        loss.backward() # Backpropagation
```

```

optim.step() # Update weights
gpu_mem = torch.cuda.memory_allocated(device) // (1024**2) # Monitor GPU memory
train_loop.set_postfix(loss=f"{loss.item():.4f}", gpu_mem=f"{gpu_mem}MiB")

# 2) Validation phase
model.eval()
all_preds, all_labels = [], []
val_loop = tqdm(val_loader, desc=f"Epoch {epoch}/{num_epochs} [VAL] ")
with torch.no_grad(): # Disable gradient tracking
    for batch in val_loop:
        batch = {k: v.to(device) for k, v in batch.items()}
        logits = model(**batch).logits
        preds = torch.argmax(logits, dim=-1).cpu().tolist()
        labels = batch["labels"].cpu().tolist()
        all_preds += preds
        all_labels += labels
val_acc = accuracy_score(all_labels, all_preds) # Compute accuracy
val_f1 = f1_score(all_labels, all_preds, average="weighted") # Compute weighted F1
print(f"→ Validation | Acc: {val_acc:.4f}, F1: {val_f1:.4f}")

# 3) Test phase (for monitoring)
all_preds, all_labels = [], []
test_loop = tqdm(test_loader, desc=f"Epoch {epoch}/{num_epochs} [TEST] ")
with torch.no_grad():
    for batch in test_loop:
        batch = {k: v.to(device) for k, v in batch.items()}
        logits = model(**batch).logits
        preds = torch.argmax(logits, dim=-1).cpu().tolist()
        labels = batch["labels"].cpu().tolist()
        all_preds += preds
        all_labels += labels
test_acc = accuracy_score(all_labels, all_preds)
test_f1 = f1_score(all_labels, all_preds, average="weighted")
print(f"→ Test | Acc: {test_acc:.4f}, F1: {test_f1:.4f}")

# 4) Save model
save_dir = f"/kaggle/working/checkpoint-epoch{epoch}" # Output directory
model.save_pretrained(save_dir) # Save model weights
tokenizer.save_pretrained(save_dir) # Save tokenizer files
print(f"→ Model & Tokenizer saved to: {save_dir}\n")

```

Training Multi Attention Layer

Load packages

```

import torch
from torch.utils.data import DataLoader
from transformers import AutoTokenizer, AutoModelForSequenceClassification
from transformers import get_linear_schedule_with_warmup
from torch.optim import AdamW
from datasets import Dataset

```

```

from tqdm.auto import tqdm
from sklearn.metrics import accuracy_score, f1_score
import pandas as pd
from sklearn.model_selection import train_test_split
import torch.nn as nn
from torch.utils.data import Dataset, DataLoader, random_split
import random
import os
def set_seed(seed=42):
    random.seed(seed)
    torch.manual_seed(seed)
    torch.cuda.manual_seed_all(seed)

set_seed(42)

```

Load data

```

df=pd.read_csv('/kaggle/input/ai-text/ai_press_releases.csv')
df=df.dropna()
human=df['non_chat_gpt_press_release'].to_list()
ai=df['chat_gpt_generated_release'].to_list()
labels=[0 if i<len(ai) else 1 for i in range(len(ai)+len(human))]
ai.extend(human)
texts=ai
# 1) split train_temp(80%) and test(20%)
texts_train_val, texts_test, labels_train_val, labels_test = train_test_split(
    texts,
    labels,
    test_size=0.2,          # 20% of the total
    random_state=42,
    stratify=labels        # Maintain label distribution
)

# 2) Split train_temp again into train (75% of temp + 60% of the total) and val (25% of temp + 20% of t
texts_train, texts_val, labels_train, labels_val = train_test_split(
    texts_train_val,
    labels_train_val,
    test_size=0.25,        #25% of train_temp + 0.2 of total
    random_state=42,
    stratify=labels_train_val
)

print(f"Train: {len(texts_train)} samples")
print(f"Valid: {len(texts_val)} samples")
print(f"Test : {len(texts_test)} samples")

```

Define helper and Multiattention layer class

```

# 2. Sentence split
def split_sentences(paragraph: str):

```

```

    return [s.strip() for s in paragraph.split('. ') if s.strip()]

# 3. Dataset
class ParagraphDataset(Dataset):
    def __init__(self, texts, labels, tokenizer, max_sents=16, max_len=128):
        self.texts = texts
        self.labels = labels
        self.tokenizer = tokenizer
        self.max_sents = max_sents
        self.max_len = max_len

    def __len__(self):
        return len(self.texts)

    def __getitem__(self, i):
        para = self.texts[i]
        label = torch.tensor(self.labels[i], dtype=torch.float)
        sents = split_sentences(para)[:self.max_sents]
        encs = [self.tokenizer(s, truncation=True, padding='max_length',
                               max_length=self.max_len, return_tensors='pt')
                 for s in sents]
        # pad sentences
        pad_n = self.max_sents - len(encs)
        input_ids = torch.stack([e['input_ids'].squeeze(0) for e in encs] +
                                [torch.zeros(self.max_len, dtype=torch.long)]*pad_n)
        attn_mask = torch.stack([e['attention_mask'].squeeze(0) for e in encs] +
                                 [torch.zeros(self.max_len, dtype=torch.long)]*pad_n)
        return input_ids, attn_mask, label

# 4. Model: frozen encoder + attention + classifier
import torch
import torch.nn as nn
from transformers import AutoTokenizer, AutoModelForSequenceClassification

class HierAttnClassifier(nn.Module):
    def __init__(self,
                 base_model_name="/kaggle/input/robertector/transformers/sentences/1/checkpoint-epoch3",
                 max_sents=16,
                 hidden=768,
                 heads=4):
        super().__init__()
        # 1) Load your fine-tuned SequenceClassification model
        self.full_model = AutoModelForSequenceClassification.from_pretrained(
            base_model_name, output_hidden_states=True, return_dict=True
        )
        # 2) Freeze all its parameters
        for p in self.full_model.parameters():
            p.requires_grad = False

        # 3) Multi-Head Attention on the CLS embeddings
        self.attn = nn.MultiheadAttention(embed_dim=hidden,
                                           num_heads=heads,
                                           batch_first=True)

```



```

# 4) Final MLP head after attention
self.classifier = nn.Sequential(
    nn.Linear(hidden, hidden // 2),
    nn.ReLU(),
    nn.Dropout(0.1),
    nn.Linear(hidden // 2, 1),
)

def forward(self, input_ids, attention_mask):
    b, s, l = input_ids.size()
    # flatten to (b*s, l)
    flat_ids = input_ids.view(b * s, l)
    flat_mask = attention_mask.view(b * s, l)
    # 5) Run through RoBERTector; we asked for hidden_states
    outputs = self.full_model(
        input_ids=flat_ids,
        attention_mask=flat_mask,
    )
    # 6) Grab the last hidden layer states: outputs.hidden_states is a tuple
    # where hidden_states[-1] is (batch, seq_len, hidden)
    last_hid = outputs.hidden_states[-1]
    # CLS is token 0
    cls_embs = last_hid[:, 0, :].view(b, s, -1) # (b, s, hidden)

    # 7) Self-attention over the s sentence embeddings
    attn_out, _ = self.attn(cls_embs, cls_embs, cls_embs) # (b, s, hidden)

    # 8) Pool and classify
    doc_emb = attn_out.mean(dim=1) # (b, hidden)
    logits = self.classifier(doc_emb).squeeze(-1) # (b,)
    return logits

```

Load RoBERTector and set up hyperparameters

```

# 5. Prepare data, loaders, model, optimizer
model_path = "/kaggle/input/robertector/transformers/sentences/1/checkpoint-epoch3"
device = torch.device("cuda" if torch.cuda.is_available() else "cpu")

# Load the tokenizer from the directory
# This reads files like tokenizer.json and tokenizer_config.json
tokenizer = AutoTokenizer.from_pretrained(model_path)

# Load the model from the directory
model = AutoModelForSequenceClassification.from_pretrained(model_path).to(device)
dataset = ParagraphDataset(texts, labels, tokenizer)
n = len(dataset)
# Split the dataset into training (60%), validation (20%), and test (20%) sets
train_n = int(0.6*n); val_n = int(0.2*n); test_n = n - train_n - val_n
train_ds, val_ds, test_ds = random_split(dataset, [train_n, val_n, test_n])

# Wrap the datasets with PyTorch DataLoader for mini-batch training and parallel data loading
train_loader = DataLoader(train_ds, batch_size=64, shuffle=True, num_workers=2)

```

```

val_loader = DataLoader(val_ds, batch_size=64, num_workers=2)
test_loader = DataLoader(test_ds, batch_size=64, num_workers=2)

device = torch.device('cuda' if torch.cuda.is_available() else 'cpu') # Define the device again (potenti
model = HierAttnClassifier().to(device) # Initialize a custom hierarchical attention-based classifier mo
opt = torch.optim.AdamW(filter(lambda p: p.requires_grad, model.parameters()), lr=1e-4) # Use AdamW opti
criterion = nn.BCEWithLogitsLoss() # Use binary cross-entropy loss with logits for multi-label classific

```

Train Multi Attention Layer

```

from tqdm.auto import tqdm

num_epochs = 6
os.makedirs('/kaggle/working/ckpts', exist_ok=True) # Directory to save model checkpoints

for epoch in range(1, num_epochs + 1):
    # TRAIN
    model.train() # Set model to training mode
    train_loss_sum = 0.0
    train_steps = 0
    loop = tqdm(train_loader, desc=f"Train E{epoch}")
    for ids, mask, lbl in loop:
        ids, mask, lbl = ids.to(device), mask.to(device), lbl.to(device)
        # Move input IDs, attention masks, and labels to the correct device
        opt.zero_grad()
        logits = model(ids, mask)
        loss = criterion(logits, lbl)
        loss.backward()
        opt.step()

        train_loss_sum += loss.item()
        train_steps += 1
        # Display current batch loss on the tqdm progress bar
        loop.set_postfix(loss=f"{loss.item():.4f}") # Update progress bar with current batch loss

    avg_train_loss = train_loss_sum / train_steps
    print(f"Epoch {epoch} | Train Loss: {avg_train_loss:.4f}")

    # VALIDATION
    model.eval() # Set model to evaluation mode
    val_loss_sum = 0.0
    preds, trues = [], []
    with torch.no_grad(): # Disable gradient calculation for validation
        for ids, mask, lbl in val_loader:
            ids, mask, lbl = ids.to(device), mask.to(device), lbl.to(device)
            logits = model(ids, mask)
            loss = criterion(logits, lbl)
            val_loss_sum += loss.item()
            # Apply sigmoid and threshold at 0.5 to get binary predictions
            preds += (torch.sigmoid(logits) > 0.5).cpu().int().tolist()
            trues += lbl.cpu().int().tolist()

```

```

avg_val_loss = val_loss_sum / len(val_loader) # Average validation loss
acc = accuracy_score(trues, preds)           # Accuracy metric
f1 = f1_score(trues, preds)                   # F1 score (macro or binary depending on usage)
print(f"Epoch {epoch} | Val Loss: {avg_val_loss:.4f} | Acc: {acc:.4f} | F1: {f1:.4f}")

# CHECKPOINT SAVE
checkpoint_path = f"/kaggle/working/ckpts/epoch{epoch}.pt"
torch.save(model.state_dict(), checkpoint_path)
print(f"Saved checkpoint: {checkpoint_path}")

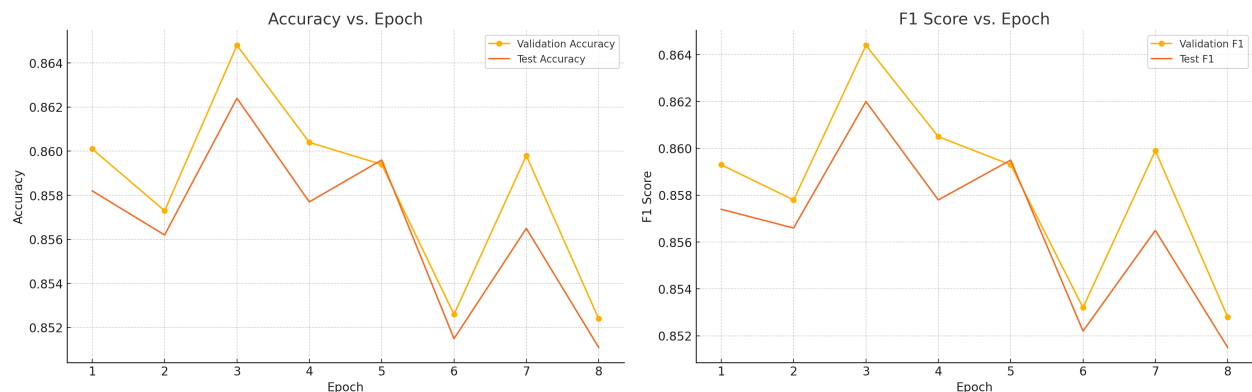
# FINAL TEST
model.load_state_dict(torch.load('/kaggle/working/ckpts/epoch6.pt'))
model.eval()
preds, trues = [], []
with torch.no_grad(): # No gradient calculation needed during evaluation
    for ids, mask, lbl in test_loader:
        ids, mask, lbl = ids.to(device), mask.to(device), lbl.to(device)
        logits = model(ids, mask)
        preds += (torch.sigmoid(logits) > 0.5).cpu().int().tolist()
        trues += lbl.cpu().int().tolist()

# Compute final test metrics
acc = accuracy_score(trues, preds)
f1 = f1_score(trues, preds)
print(f"Test Acc {acc:.4f} | F1 {f1:.4f}")

```

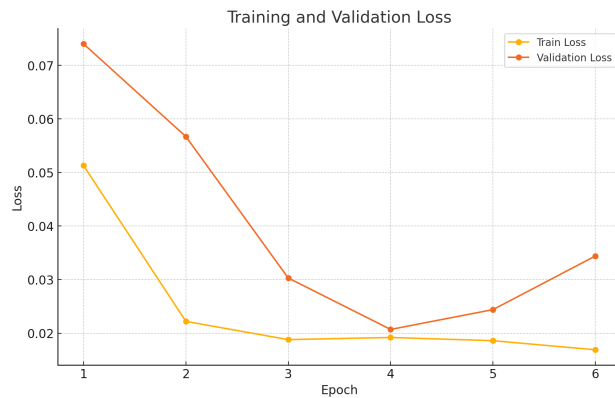
Results

FineTuning

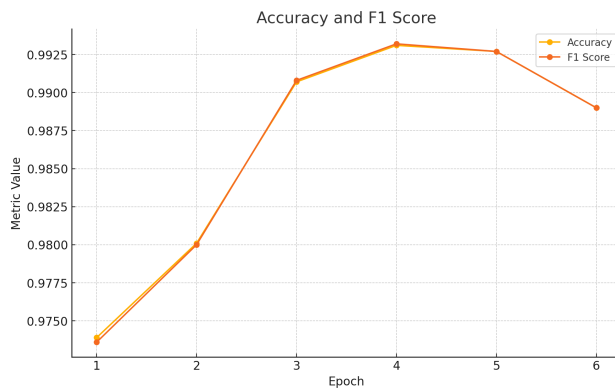


The above graphs show the relation with epoch, accuracy and f1 score of the model. From the diagram, model from epoch 3 recorded the highest accuracy and f1 score in both validation and test sets. As a result, we chose the model from epoch 3 for the following steps.

Training Multi Attention layer



Above plot shows the loss in train and validation sets as train proceeds. Both losses decreased until epoch 4, but validation loss increased after epoch 4 while train loss decreased.



The above graphs show the relation with epoch, accuracy and f1 score of the model. From the diagram, model from epoch 3 recorded the highest accuracy and f1 score in both validation and test sets. As a result, we chose the model from epoch 3 for the following steps. In order to avoid overfitting, we selected the model from epoch 4 because the validation loss recorded the lowest at that point.

model from epoch 4 was chosen.

Graph Drawing Using R

Weekly Proportion and its Smooth Line

```
library(tidyverse)
library(lubridate)

# Load and Preprocess Data
df <- read_csv("data/prob.csv")

# Invert Probabilities (AI = 1, Human = 0)
df <- df %>%
  mutate(probability = 1 - probability,
         prediction = 1 - prediction,
         Week = floor_date(as.Date(Date), unit = "week"))
```

```

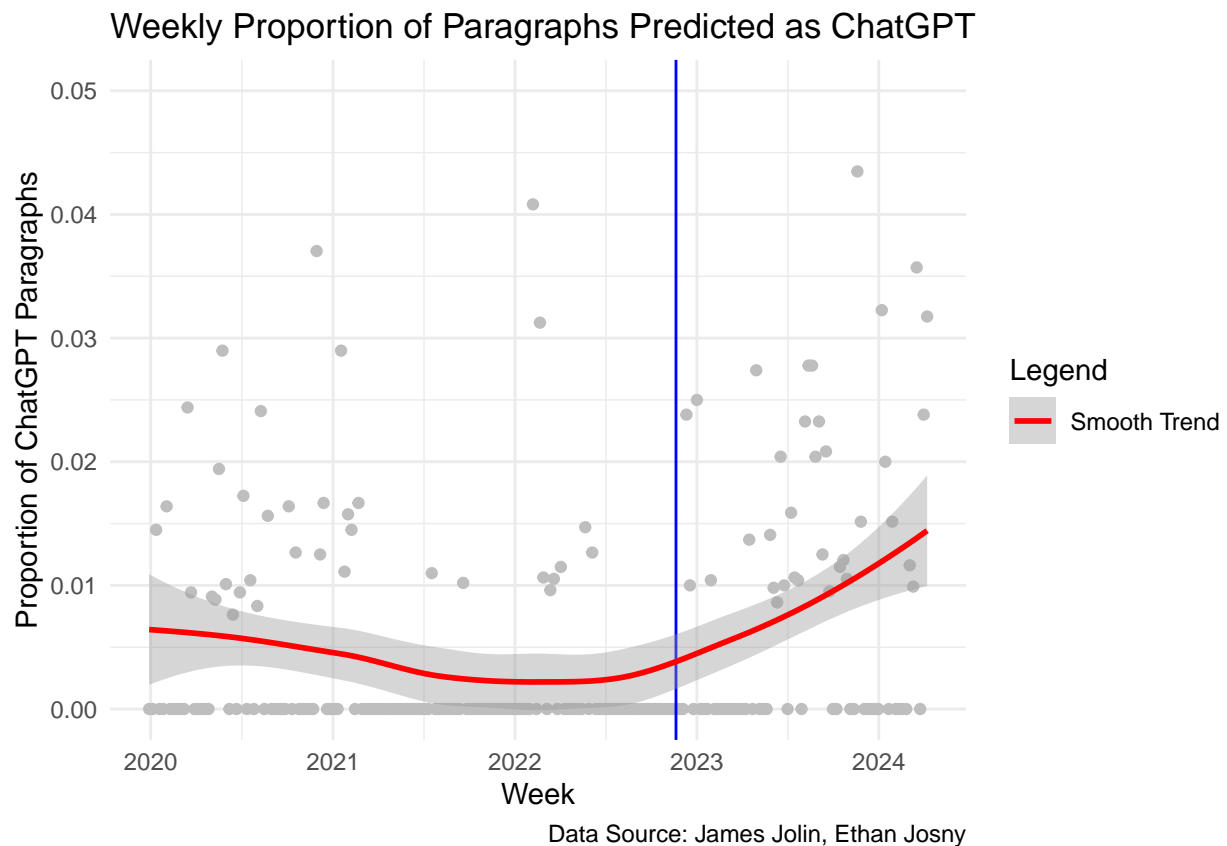
# Weekly Mean Calculation
df_mean <- df %>%
  group_by(Week) %>%
  summarise(mean_chatgpt = mean(prediction), .groups = "drop")

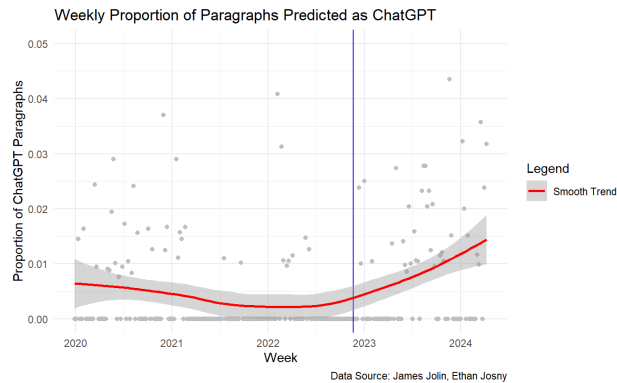
# GPT Release Date
gpt_date <- floor_date(as.Date("2022-11-21"), unit = "week")

# Subsets for Pre and Post-GPT
df_pre_gpt <- df %>% filter(Week <= gpt_date)
df_post_gpt <- df %>% filter(Week > gpt_date)

# Plot 1: Smoothed Trend Line with Points
ggplot(data = df_mean, aes(x = Week, y = mean_chatgpt)) +
  geom_point(color = "gray") +
  geom_vline(xintercept = gpt_date, color = "blue") +
  geom_smooth(aes(color = "Smooth Trend"), se = TRUE) +
  scale_color_manual(values = c("Smooth Trend" = "red")) +
  coord_cartesian(ylim = c(0, 0.05)) +
  theme_minimal() +
  labs(x = "Week",
       y = "Proportion of ChatGPT Paragraphs",
       title = "Weekly Proportion of Paragraphs Predicted as ChatGPT",
       caption = "Data Source: James Jolin, Ethan Josny",
       color = "Legend")

```



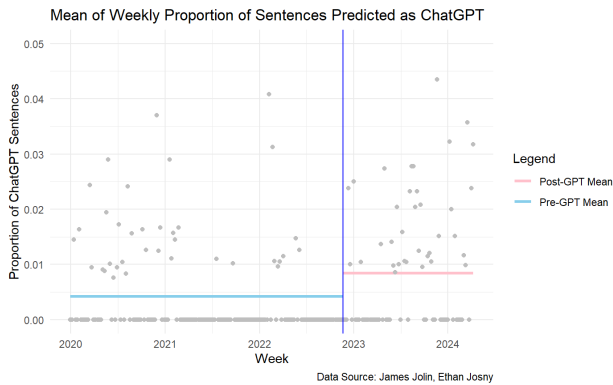
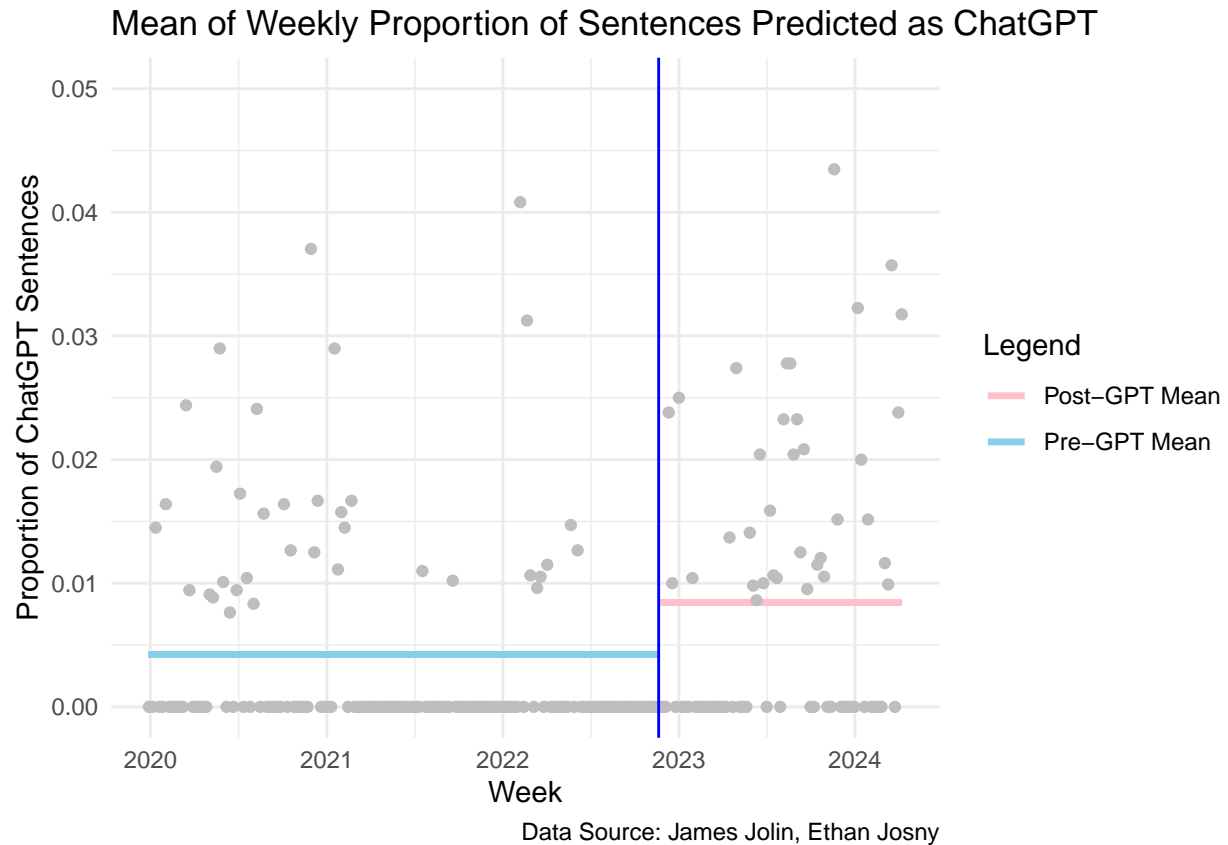


This graph shows the **distribution of the weekly proportion of paragraphs predicted as ChatGPT** by RoBERTector. In this graph, blue horizontal line indicates the time that ChatGPT was first released, and red line is the smooth trend line of distribution. As you can see from the graph, after ChatGPT, the trend of weekly proportion seems to increase.

Average of Pre-GPT, Post_GPT

```
# Calculate Pre/Post GPT Means
pre_mean <- mean(df_pre_gpt$prediction)
post_mean <- mean(df_post_gpt$prediction)

# Plot 2: Pre/Post GPT Mean Lines
ggplot(data = df_mean, aes(x = Week, y = mean_chatgpt)) +
  geom_segment(aes(x = min(Week), xend = gpt_date,
                  y = pre_mean, yend = pre_mean, color = "Pre-GPT Mean"),
              size = 1.2) +
  geom_segment(aes(x = gpt_date, xend = max(Week),
                  y = post_mean, yend = post_mean, color = "Post-GPT Mean"),
              size = 1.2) +
  scale_color_manual(values = c("Pre-GPT Mean" = "skyblue", "Post-GPT Mean" = "pink")) +
  geom_point(color = "gray") +
  geom_vline(xintercept = gpt_date, color = "blue") +
  coord_cartesian(ylim = c(0, 0.05)) +
  theme_minimal() +
  labs(x = "Week",
       y = "Proportion of ChatGPT Sentences",
       title = "Mean of Weekly Proportion of Sentences Predicted as ChatGPT",
       caption = "Data Source: James Jolin, Ethan Josny",
       color = "Legend")
```



This graph shows the **mean of ChatGPT-classified paragraph proportion** in post-GPT (pink line), pre-GPT period (skyblue line). The mean of paragraph proportion in pre-GPT period recorded 0.004231799, and 0.008446278 in post-GPT period. It shows that the proportion increased after official release of ChatGPT.

Linear Regression of Post-GPT

```
# Dataframe Storing Post GPT's ChatGPT Proportion
df_post_mean <- df_mean %>% filter(Week > gpt_date)

# Linear Regression Model
model <- lm(mean_chatgpt ~ Week, data = df_post_mean)
co <- coef(model)
```

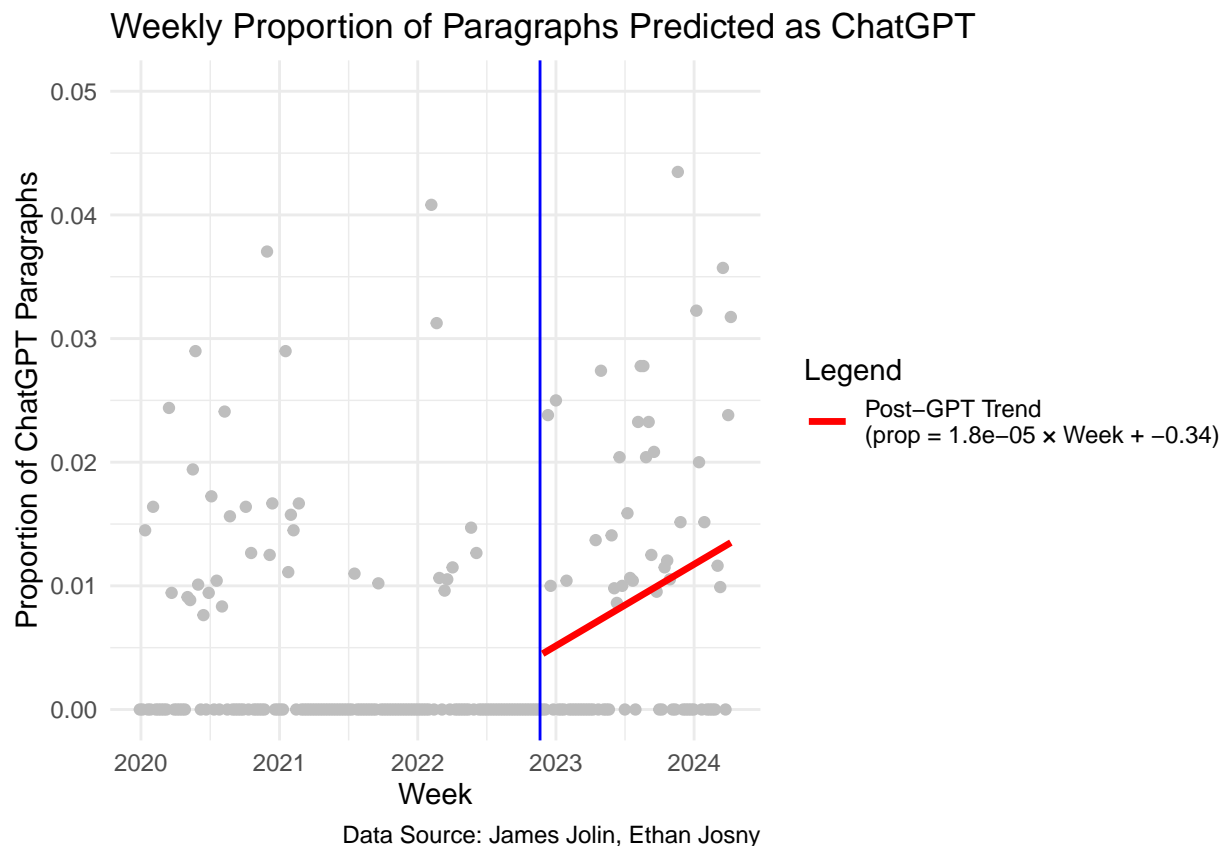
```

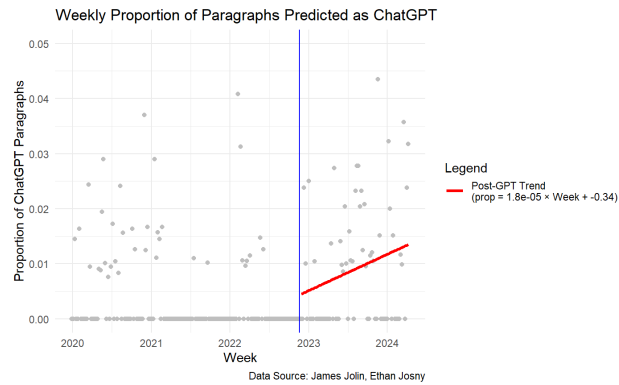
# Stores Linear Regression's Estimation Result
df_post_mean <- cbind(df_post_mean, predict(model, interval = 'confidence'))

# Get's Linear Model's Equation
equation <- paste("prop =", round(co[2], 6), "x Week +", round(co[1], 2))
legend_label <- paste("Post-GPT Trend\n(", equation, ")", sep = "")
df_post_mean$legend <- legend_label

# Plot 3: Linear Regression After GPT Release
ggplot(data = df_mean, aes(x = Week, y = mean_chatgpt)) +
  geom_point(color = "gray") +
  geom_vline(xintercept = gpt_date, color = "blue") +
  geom_line(data = df_post_mean, aes(x = Week, y = fit, color = legend), size = 1.2) +
  scale_color_manual(values = setNames("red", legend_label)) +
  coord_cartesian(ylim = c(0, 0.05)) +
  theme_minimal() +
  labs(x = "Week",
       y = "Proportion of ChatGPT Paragraphs",
       title = "Weekly Proportion of Paragraphs Predicted as ChatGPT",
       caption = "Data Source: James Jolin, Ethan Josny",
       color = "Legend")

```





This graph shows the distribution of weekly proportion of paragraphs which is predicted as ChatGPT, with its **linear regression model** fitted with post-GPT period data. Equation of linear regression model was approximately $\text{Proportion} = 1.808295 \times 10^{-5} \times \text{Week} - 3.449049 \times 10^{-1}$. The coefficient of “Week” variable was positive, so we can conclude that usage of ChatGPT in U. S. Senate press releases has been increasing since the release of ChatGPT.