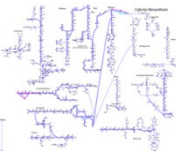


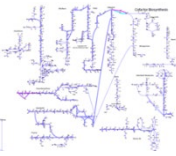
Matlab Tutorial



Lecture Learning Objectives

Each student should be able to:

- Describe the Matlab desktop
- Explain the basic use of Matlab variables
- Explain the basic use of Matlab scripts
- Explain the basic mathematical operations in Matlab
- Explain the simple Matlab visualization techniques
- Explain simple Matlab programming
- Explain the basic data structures available in Matlab



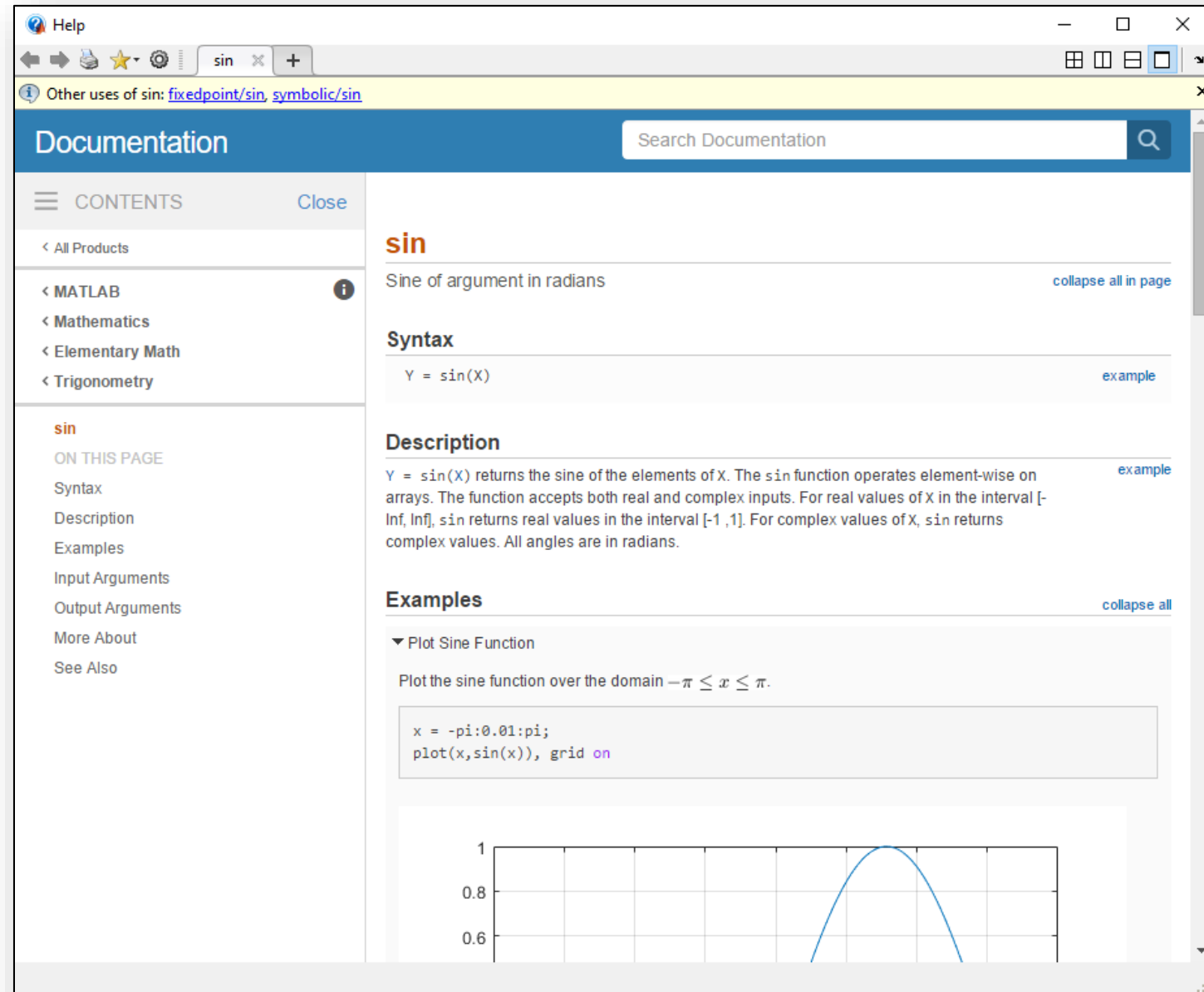
Course Introduction

- Desktop
- Variables
- Scripts
- Operations
- Visualization
- Programming
- Data Structures

Command History

Overview and Help

- MATLAB can be used as a super-powerful graphing calculator
- It is also a programming language
 - ✓ MATLAB is an interpreted language like Java
 - ✓ Commands are executed line by line
- Help/documentation can be found with the doc command
 - ✓ Example: doc sin
 - ✓ Same as "help"
- ✓ "clc" clears the command window
- ✓ "clear" clears the workspace

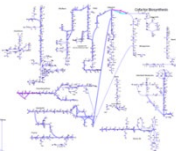


The screenshot shows the MATLAB documentation window for the `sin` function. The window has a title bar with "Help" and standard window controls. Below the title bar is a navigation bar with "sin" and a "+" button. A yellow banner at the top says "Other uses of sin: [fixedpoint/sin](#), [symbolic/sin](#)". The main content area is titled "Documentation" and includes a search bar. On the left, a "CONTENTS" sidebar lists navigation options: "All Products", "MATLAB", "Mathematics", "Elementary Math", and "Trigonometry". The "sin" function is selected under "Trigonometry". The main content area displays the following information:

- sin**: Sine of argument in radians. A link "collapse all in page" is on the right.
- Syntax**: `Y = sin(X)`. A link "example" is on the right.
- Description**: `Y = sin(X)` returns the sine of the elements of X. The `sin` function operates element-wise on arrays. The function accepts both real and complex inputs. For real values of X in the interval $[-\infty, \infty]$, `sin` returns real values in the interval $[-1, 1]$. For complex values of X, `sin` returns complex values. All angles are in radians. A link "example" is on the right.
- Examples**: A link "collapse all" is on the right.
 - Plot Sine Function**: Plot the sine function over the domain $-\pi \leq x \leq \pi$.

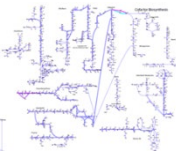

```
x = -pi:0.01:pi;
plot(x,sin(x)), grid on
```

Below the code, a plot shows the sine function $y = \sin(x)$ over the domain $-\pi \leq x \leq \pi$. The x-axis ranges from approximately -3.14 to 3.14, and the y-axis ranges from 0.6 to 1.0. The plot shows a blue curve representing the sine function, with a grid.



Course Introduction

- Desktop
- ➔ • Variables
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Variable Types

- MATLAB is a weakly typed language
 - ✓ No need to initialize variables!
- MATLAB supports various types, the most often used are
 - ✓ Numbers (42.42) are 64-bit double precision (default)
 - ✓ Alphanumeric characters ('b') are 16-bit precision (default)
- Most variables will be vectors or matrices of numbers or alphanumeric characters
- Other types are also supported, including: complex, symbolic, 16-bit and 8 bit integers, etc.

Naming Variables

- To create a variable, simply assign a value to a name:

✓ `>> x = 42.42`

✓ `>> string = 'name'`

- Variable names

- ✓ The first character must be a LETTER, after that, any combination of letters, numbers and _
- ✓ Matlab is CASE SENSITIVE! (x is different from X)

- Built-in variables. Don't use these names!

- ✓ "i" and "j" are used to indicate complex numbers
- ✓ "pi" has the value 3.1415926...
- ✓ "ans" stores the last unassigned value (like on a calculator)
- ✓ "Inf" and "-Inf" are positive and negative infinity
- ✓ "NaN" represents "Not a Number"

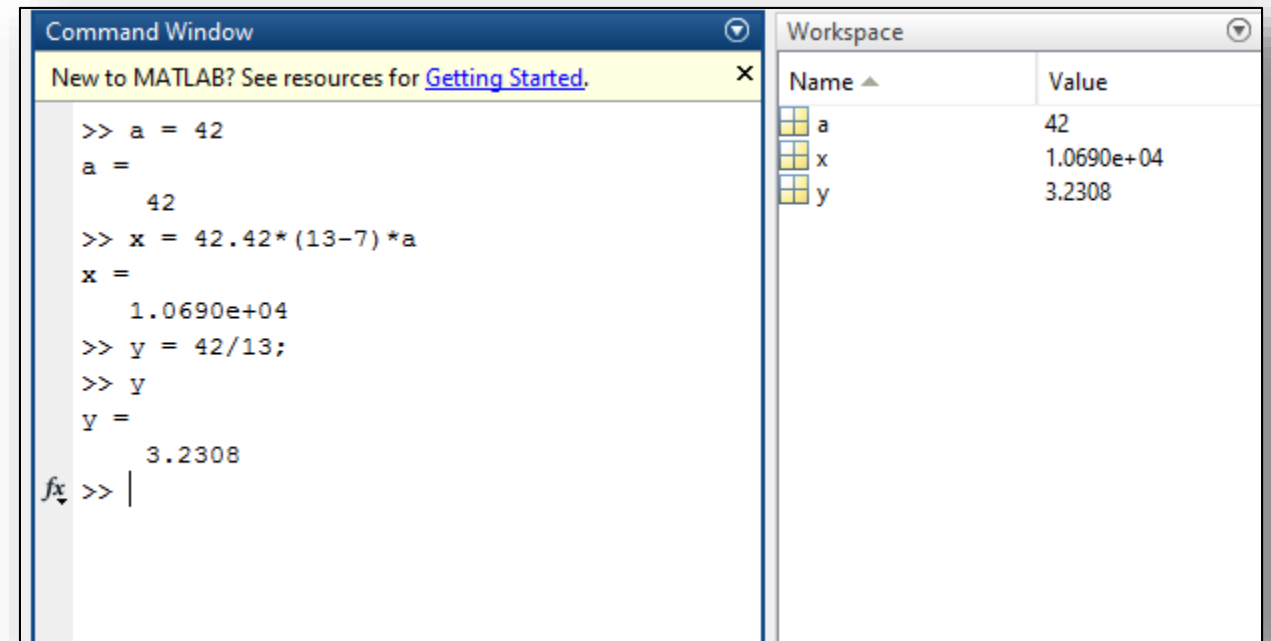
```
Command Window
New to MATLAB? See resources for Getting Started.

>> x=42.42
x =
    42.4200
>> x = 42.42
x =
    42.4200
>> string_name = 'Metabolic modeling'
string_name =
    Metabolic modeling
>> 4x = 42.42
    4x = 42.42
    ↑
Error: Unexpected MATLAB expression.

>> pi
ans =
    3.1416
>> ans
ans =
    3.1416
```


Using Variables

- A variable can be given a value explicitly
 - ✓ `>> a = 42` (Note that a shows up in workspace!)
- A variable can be used as a function of explicit values and existing variables
 - ✓ `>> x = 42.42*(13-7)*a`
- To suppress the output, end the line with a semicolon
 - ✓ `>> y = 42/13;`



The screenshot shows the MATLAB Command Window and Workspace. The Command Window displays the following commands and their outputs:

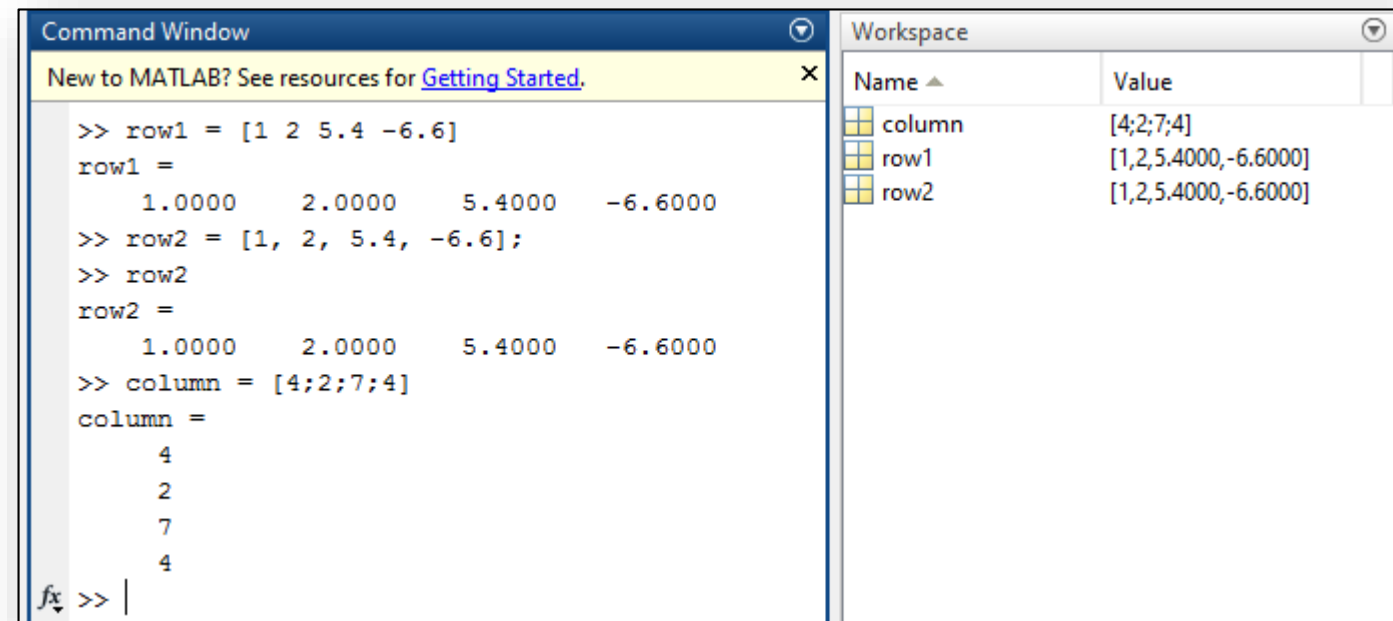
```
>> a = 42
a =
    42
>> x = 42.42*(13-7)*a
x =
    1.0690e+04
>> y = 42/13;
>> y
y =
    3.2308
fx >> |
```

The Workspace window shows the following variables and their values:

Name	Value
a	42
x	1.0690e+04
y	3.2308

Arrays

- Like other programming languages, arrays are an important part of MATLAB
- There are two types of arrays
 - ✓ Matrix of numbers (either double or complex)
 - ✓ Cell array of objects (advanced data structure)
- Row vectors: Use a comma or space to separate values between brackets
 - ✓ `>> row1 = [1 2 5.4 -6.6]`
 - ✓ `>> row2 = [1, 2, 5.4, -6.6];`
- Column vectors: Use a semicolon to separate values between brackets
 - ✓ `>> column = [4;2;7;4]`



The screenshot shows the MATLAB Command Window and Workspace. The Command Window displays the following commands and outputs:

```
>> row1 = [1 2 5.4 -6.6]
row1 =
    1.0000    2.0000    5.4000   -6.6000
>> row2 = [1, 2, 5.4, -6.6];
>> row2
row2 =
    1.0000    2.0000    5.4000   -6.6000
>> column = [4;2;7;4]
column =
     4
     2
     7
     4
```

The Workspace window shows the following variables and their values:

Name	Value
column	[4;2;7;4]
row1	[1,2,5.4000,-6.6000]
row2	[1,2,5.4000,-6.6000]

Size & Length

- The difference between a row and a column vector can be seen by:
 - ✓ Looking at the workspace
 - ✓ Displaying the variable in the command window
 - ✓ Using the size function
- Use the length function to get a vector's length

The screenshot shows the MATLAB Command Window and Workspace. The Command Window displays the following commands and outputs:

```
>> size(row1)
ans =
     1     4
>> size(row2)
ans =
     1     4
>> size(column)
ans =
     4     1
>> length(row1)
ans =
     4
>> length(row2)
ans =
     4
>> length(column)
ans =
     4
```

The Workspace window shows the following variables and their values:

Name	Value
ans	4
column	[4;2;7;4]
row1	[1,2,5.4000,-6.6000]
row2	[1,2,5.4000,-6.6000]

Matrices

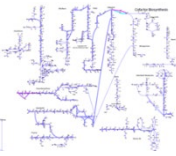
- Make matrices like vectors
- Construct matrix element by element
 - ✓ » `a = [1 2;3 4]`
 - ✓ » `b = [1,2,3;4,5,6;7,8,9]`
- Strings are character vectors
 - ✓ » `str1 = 'metabolic ';`
 - ✓ » `str2 = 'modeling ';`
 - ✓ » `str3 = 'course';`
 - ✓ » `c = [str1, str2, str3]`
 - ✓ » `d = ['metabolic ', 'modeling ', 'course']`

The screenshot shows the MATLAB Command Window and Workspace. The Command Window displays the following code and output:

```
>> a = [1 2;3 4]
a =
     1     2
     3     4
>> b = [1,2,3;4,5,6;7,8,9]
b =
     1     2     3
     4     5     6
     7     8     9
>> str1 = 'metabolic ';
>> str2 = 'modeling ';
>> str3 = 'course';
>> c = [str1, str2, str3]
c =
metabolic modeling course
>> d = ['metabolic ', 'modeling ', 'course']
d =
metabolic modeling course
fx >> |
```

The Workspace window shows the following variables and their values:

Name	Value
a	[1,2;3,4]
b	[1,2,3;4,5,6;7,8,9]
c	'metabolic modeling ...'
d	'metabolic modeling ...'
str1	'metabolic '
str2	'modeling '
str3	'course'

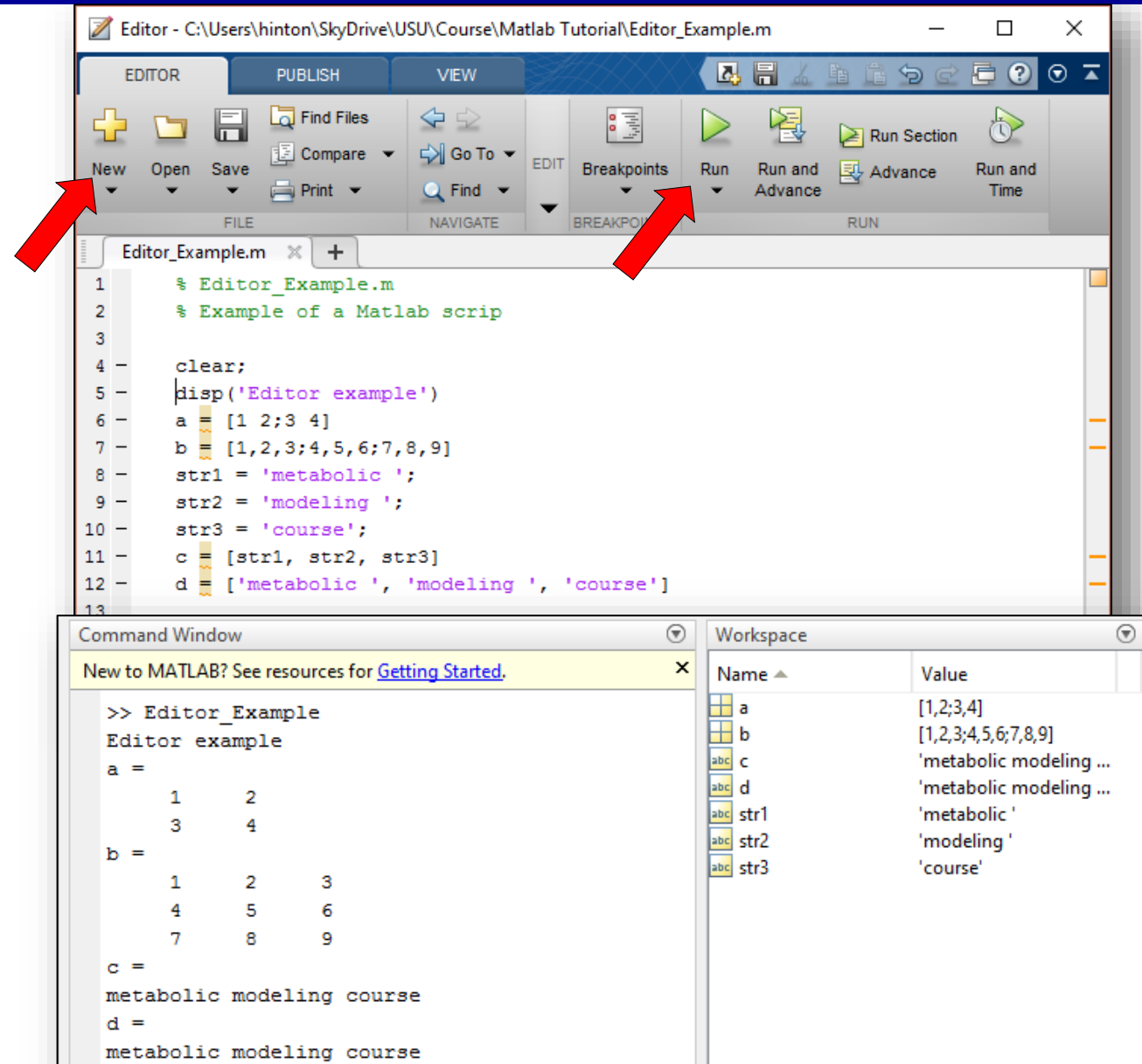


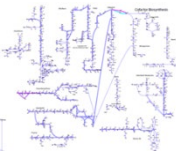
Course Introduction

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Editor & Scripts

- The Matlab desktop includes an editor that can be used to create scripts which are composed of Matlab commands stored in a Matlab ".m" file.
- "%" assigns whatever text that follows on that line as a comment
- "clear" clear's the workspace
- The "disp()" command can be used to display strings



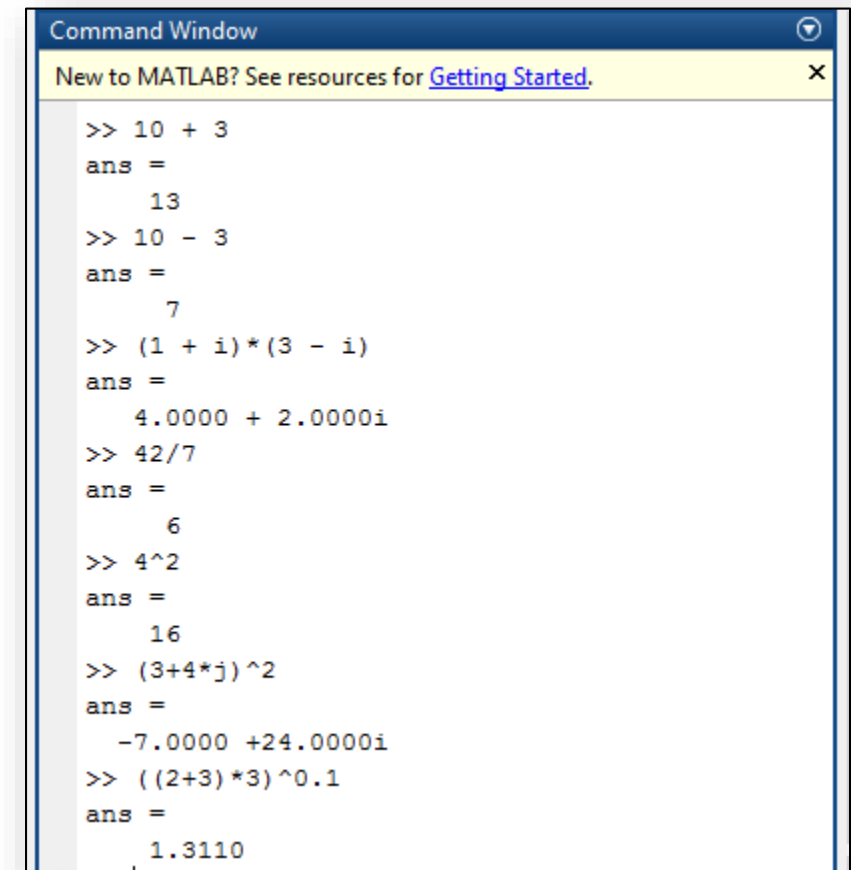


Course Introduction

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Scalar Operations

- Arithmetic operations (+,-,*,/)
 - ✓ » 10 + 3
 - ✓ » 10 - 3
 - ✓ » (1+i) * (3-i)
 - ✓ » 42/7
- Exponentiation (^)
 - ✓ » 4^2
 - ✓ » (3+4*j)^2
- Complicated expressions, use parentheses
 - ✓ » ((2+3)*3)^0.1



```

Command Window
New to MATLAB? See resources for Getting Started. x

>> 10 + 3
ans =
    13

>> 10 - 3
ans =
     7

>> (1 + i)*(3 - i)
ans =
    4.0000 + 2.0000i

>> 42/7
ans =
     6

>> 4^2
ans =
    16

>> (3+4*j)^2
ans =
   -7.0000 +24.0000i

>> ((2+3)*3)^0.1
ans =
    1.3110
    
```


Built-in Matlab Functions

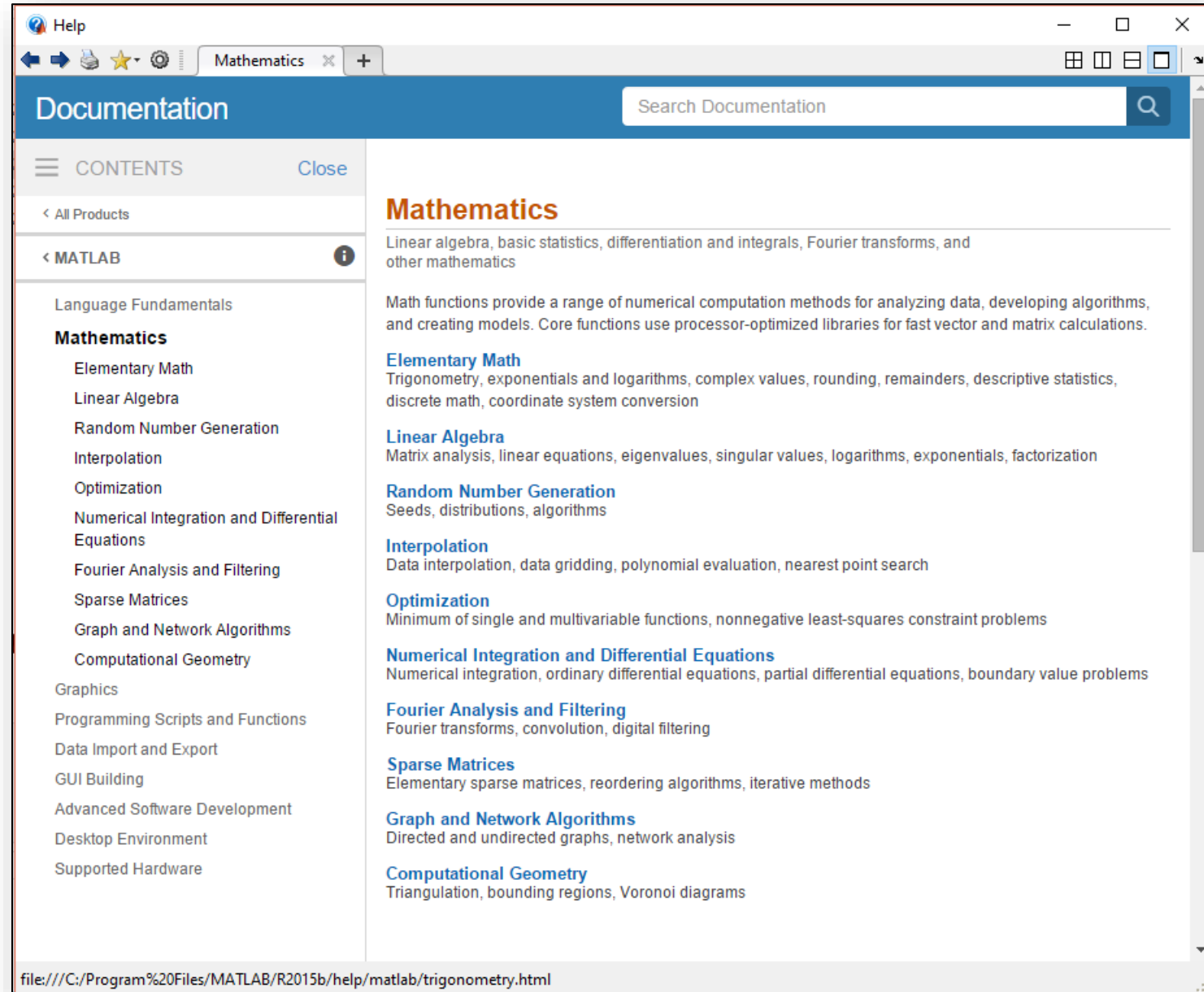
- MATLAB has a large library of built-in functions
 - ✓ https://www.mathworks.com/help/matlab/functionlist.html?s_cid=doc_ftr
- To use the functions, call using parentheses which passes the parameters to function
 - ✓ » `sqrt(5)`
 - ✓ » `log(4)` , `log10(0.33)`
 - ✓ » `cos(1.4)` , `atan(-.9)`
 - ✓ » `exp(1+5*i)`
 - ✓ » `round(2.4)` , `floor(3.6)` , `ceil(3.23)`
 - ✓ » `angle(i)` ; `abs(1+i)` ;

```
Command Window
New to MATLAB? See resources for Getting Started.

>> sqrt(5)
ans =
    2.2361
>> log(4)
ans =
    1.3863
>> log10(0.33)
ans =
   -0.4815
>> cos(1.4)
ans =
    0.1700
>> atan(-.9)
ans =
   -0.7328
>> exp(1+5*i)
ans =
    0.7711 - 2.6066i
>> round(2.4)
ans =
     2
>> floor(3.6)
ans =
     3
>> ceil(3.23)
ans =
     4
>> angle(i)
ans =
    1.5708
>> abs(1+i)
ans =
    1.4142
```

Matlab Functions

- See Matlab documentation



The screenshot shows the MATLAB Documentation web page in a browser window. The browser's address bar shows the file path: `file:///C:/Program%20Files/MATLAB/R2015b/help/matlab/trigonometry.html`. The page has a blue header with the word "Documentation" and a search bar. On the left, there is a "CONTENTS" sidebar with a "Close" button. The sidebar lists various categories, with "MATLAB" selected. Under "MATLAB", the "Mathematics" category is expanded, showing a list of sub-topics: Language Fundamentals, Mathematics, Graphics, Programming Scripts and Functions, Data Import and Export, GUI Building, Advanced Software Development, Desktop Environment, and Supported Hardware. The "Mathematics" sub-category is further expanded, showing a list of topics: Elementary Math, Linear Algebra, Random Number Generation, Interpolation, Optimization, Numerical Integration and Differential Equations, Fourier Analysis and Filtering, Sparse Matrices, Graph and Network Algorithms, and Computational Geometry. The main content area on the right displays the "Mathematics" section, which includes a brief description of math functions and a list of sub-topics with their descriptions.

Mathematics
Linear algebra, basic statistics, differentiation and integrals, Fourier transforms, and other mathematics

Math functions provide a range of numerical computation methods for analyzing data, developing algorithms, and creating models. Core functions use processor-optimized libraries for fast vector and matrix calculations.

Elementary Math
Trigonometry, exponentials and logarithms, complex values, rounding, remainders, descriptive statistics, discrete math, coordinate system conversion

Linear Algebra
Matrix analysis, linear equations, eigenvalues, singular values, logarithms, exponentials, factorization

Random Number Generation
Seeds, distributions, algorithms

Interpolation
Data interpolation, data gridding, polynomial evaluation, nearest point search

Optimization
Minimum of single and multivariable functions, nonnegative least-squares constraint problems

Numerical Integration and Differential Equations
Numerical integration, ordinary differential equations, partial differential equations, boundary value problems

Fourier Analysis and Filtering
Fourier transforms, convolution, digital filtering

Sparse Matrices
Elementary sparse matrices, reordering algorithms, iterative methods

Graph and Network Algorithms
Directed and undirected graphs, network analysis

Computational Geometry
Triangulation, bounding regions, Voronoi diagrams

Linear Algebra

- Transpose

- ✓ The transpose operators turns a column vector into a row vector and vice versa
 - `>> a = [1 2 3 4+i]`
 - `>> transpose(a)`
 - `>> a'`
 - `>> a.'`
- ✓ The `'` gives the Hermitian-transpose, i.e. transposes and conjugates all complex numbers
- ✓ For vectors of real numbers `.'` and `'` give same result

```

Command Window
New to MATLAB? See resources for Getting Started.
>> a = [1 2 3 4+i]
a =
    1.0000 + 0.0000i    2.0000 + 0.0000i    3.0000 + 0.0000i    4.0000 + 1.0000i
>> transpose(a)
ans =
    1.0000 + 0.0000i
    2.0000 + 0.0000i
    3.0000 + 0.0000i
    4.0000 + 1.0000i
>> a'
ans =
    1.0000 + 0.0000i
    2.0000 + 0.0000i
    3.0000 + 0.0000i
    4.0000 - 1.0000i
>> a.'
ans =
    1.0000 + 0.0000i
    2.0000 + 0.0000i
    3.0000 + 0.0000i
    4.0000 + 1.0000i
fx >>
    
```

Adding and Subtracting Arrays

- Addition and subtraction are element-wise; sizes must match (unless one is a scalar):
 - ✓ `>> row = [1 2 3]`
 - ✓ `>> column = [4;2;1]`
 - ✓ `>> c = row + column` % **Error**
- Use the transpose to make sizes compatible
 - ✓ `>> c = row' + column`
 - ✓ `>> c = row + column'`
- Can sum up or multiply elements of vector
 - ✓ `>> s = sum(row);`
 - ✓ `>> p = prod(row);`

```

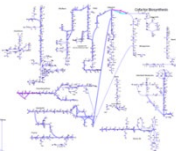
Command Window
New to MATLAB? See resources for Getting Started.
>> row = [1 2 3]
row =
     1     2     3
>> column = [4;2;1]
column =
     4
     2
     1
>> c = row + column
Error using +
Matrix dimensions must agree.
>> c = row' + column
c =
     5
     4
     4
>> c = row + column'
c =
     5     4     4
>> s = sum(row)
s =
     6
>> p = prod(row)
p =
     6
fx >> |
    
```

Standard and Element-Wise Operators

- Operators ($*$ / $^$) have two modes of operation
 - ✓ Standard ($*$ / $^$)
 - ✓ Element-wise ($.*$./ $.^$)
- All the functions that work on scalars also work on vectors
 - ✓ `t = [1 2 3];`
 - ✓ `f = exp(t)` is the same as
 - ✓ `f = [exp(1) exp(2) exp(3)];`
- For element-wise operations, use the dot: ($.*$, $./$, $.^$). Both dimensions must match (unless one is scalar)!
 - ✓ `a = [1 2 3]; b = [4;2;1];`
 - ✓ `a.*b`, `a./b`, `a.^b` are all errors
 - ✓ `a.*b'`, `a./b'`, `a.^(b')` are all valid

```
Command Window
New to MATLAB? See resources for Getting Started.

>> t = [1 2 3]
t =
     1     2     3
>> f = exp(t)
f =
     2.7183     7.3891    20.0855
>> f = [exp(1) exp(2) exp(3)]
f =
     2.7183     7.3891    20.0855
>> a = [1 2 3]; b = [4;2;1];
>> a.*b
Error using .*
Matrix dimensions must agree.
>> a./b
Error using ./
Matrix dimensions must agree.
>> a.^b
Error using .^
Matrix dimensions must agree.
>> a.*b'
ans =
     4     4     3
>> a./b'
ans =
     0.2500     1.0000     3.0000
>> a.^(b')
ans =
     1     4     3
fx >> |
```



Operator Guidelines

- Multiplication can be done in a standard way or element-wise
- Standard multiplication (*) is either a dot-product or an outer-product
 - ✓ Remember from linear algebra: inner dimensions must MATCH!!
- Standard exponentiation (^) can only be done on square matrices or scalars
- Left and right division (/ \) is same as multiplying by inverse
 - ✓ Recommendation: just multiply by inverse

Indexing Vectors

- MATLAB indexing of arrays starts with 1, not 0
- $x(n)$ returns the n^{th} element of the array

$x = [15 \ 4 \ 8 \ 12]$

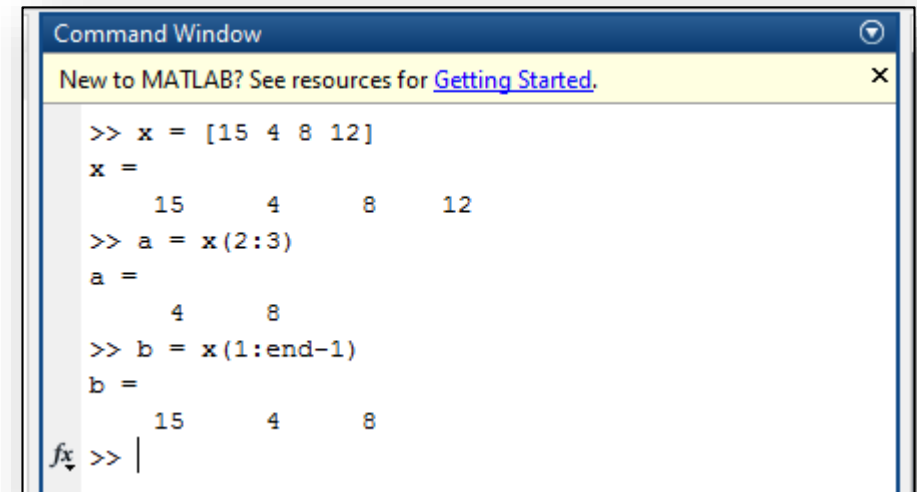
\swarrow \swarrow \swarrow \swarrow
 $x(1)$ $x(2)$ $x(3)$ $x(4)$

- The index argument can be a vector. In this case, each element is looked up individually, and returned as a vector of the same size as the index vector.

✓ `>> x = [15 4 8 12]`

✓ `>> a = x(2:3)`

✓ `>> b = x(1:end-1)`



```

Command Window
New to MATLAB? See resources for Getting Started.
>> x = [15 4 8 12]
x =
    15     4     8    12
>> a = x(2:3)
a =
     4     8
>> b = x(1:end-1)
b =
    15     4     8
fx >> |
    
```

Indexing Matrices

- Matrices can be indexed in two ways
 - ✓ Using subscripts (row and column)
 - ✓ Using linear indices (as if matrix is a vector)
- Matrix indexing: subscripts or linear indices

$x(1,1) \rightarrow \begin{bmatrix} 22 & 34 \end{bmatrix} \leftarrow x(1,2)$
 $x(1) \rightarrow \begin{bmatrix} 22 & 34 \end{bmatrix} \leftarrow x(3)$
 $x(2,1) \rightarrow \begin{bmatrix} 4 & 5 \end{bmatrix} \leftarrow x(2,2)$
 $x(2) \rightarrow \begin{bmatrix} 4 & 5 \end{bmatrix} \leftarrow x(4)$

- Picking submatrices

- ✓ `>> x = rand(5)` % Uniformly distributed random numbers
- ✓ `>> x(1:3,1:2)` % Specify contiguous submatrix
- ✓ `>> x([1 5 3], [1 4])` % Specify rows and columns

```

Command Window
New to MATLAB? See resources for Getting Started.
>> x = rand(5)
x =
    0.8147    0.0975    0.1576    0.1419    0.6557
    0.9058    0.2785    0.9706    0.4218    0.0357
    0.1270    0.5469    0.9572    0.9157    0.8491
    0.9134    0.9575    0.4854    0.7922    0.9340
    0.6324    0.9649    0.8003    0.9595    0.6787

>> x(1:3,1:2)
ans =
    0.8147    0.0975
    0.9058    0.2785
    0.1270    0.5469

>> x([1 5 3], [1 4])
ans =
    0.8147    0.1419
    0.6324    0.9595
    0.1270    0.9157
fx >>
    
```


Advanced Indexing

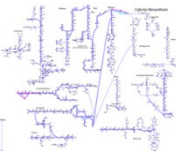
- To select rows or columns of a matrix, use ":"

$$x = \begin{bmatrix} 22 & 34 \\ 4 & 5 \end{bmatrix}$$

- ✓ `>> d = x(1,:)` % list elements of row 1
- ✓ `>> e = x(:,2)` % list elements of column 2
- ✓ `>> x(2,:) = [3 6];` % replaces second row of x
- Functions that can help you find desired values within a vector or matrix
 - ✓ `>> y = [5 3 1 9 7]`
- To get the minimum value and its index:
 - ✓ `>> [minVal, minInd] = min(y);`
 - ✓ `>> [maxVal, maxInd] = max(y);`
- To find any the indices of specific values or ranges
 - ✓ `>> ind = find(y == 9);`
 - ✓ `>> ind = find(y > 2 & y < 6);`

```

Command Window
New to MATLAB? See resources for Getting Started.
>> x = [22 34; 4 5]
x =
    22    34
     4     5
>> d = x(1,:)
d =
    22    34
>> e = x(:,2)
e =
    34
     5
>> x(2,:) = [3 6]
x =
    22    34
     3     6
>> y = [5 3 1 9 7]
y =
     5     3     1     9     7
>> [minVal, minInd] = min(y)
minVal =
     1
minInd =
     3
>> [maxVal, MaxInd] = max(y)
maxVal =
     9
MaxInd =
     4
>> ind = find(y == 9)
ind =
     4
>> ind = find(y > 2 & y < 6)
ind =
     1     2
    
```



Course Introduction

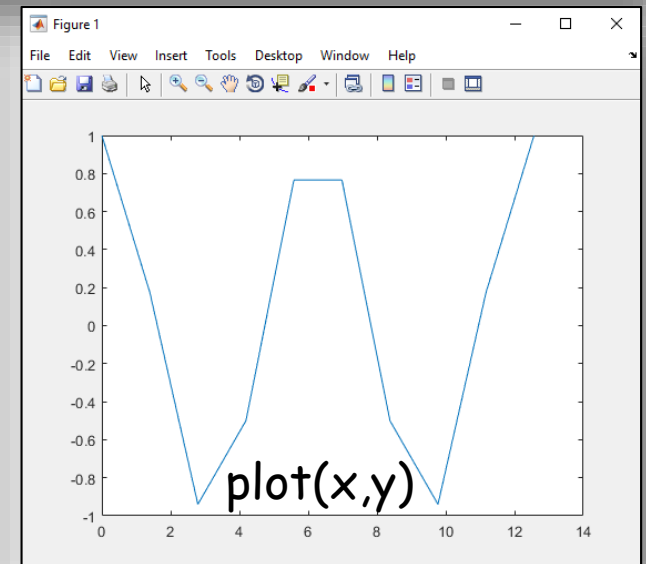
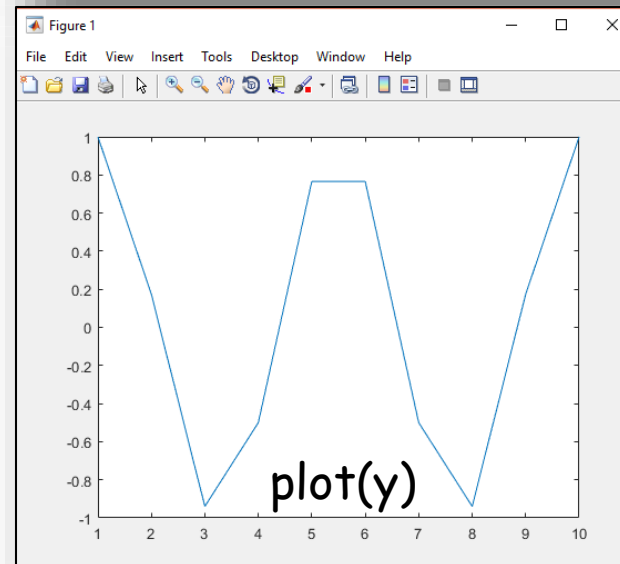
- Desktop
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- Scripts
- Operations
- ➔ • Visualization
- Programming
- Data Structures

Simple Plotting

- Simple example
 - ✓ `>> x = linspace(0,4*pi,10)`
 - ✓ `>> y = cos(x)`
- Plot values against their index
 - ✓ `>> plot(y);`
- Plotting y versus x
 - ✓ `>> plot(x,y);`
- “plot” generates dots at each (x,y) pair and then connects the dots with a line
- Default is plotting 10 points

```
Command Window
New to MATLAB? See resources for Getting Started.

>> x = linspace(0,4*pi,10)
x =
    Columns 1 through 7
         0    1.3963    2.7925    4.1888    5.5851    6.9813    8.3776
    Columns 8 through 10
    9.7738   11.1701   12.5664
>> y = cos(x)
y =
    Columns 1 through 7
    1.0000    0.1736   -0.9397   -0.5000    0.7660    0.7660   -0.5000
    Columns 8 through 10
   -0.9397    0.1736    1.0000
>> plot(y)
>> plot(x,y)
```



Simple Plotting: Increasing Resolution

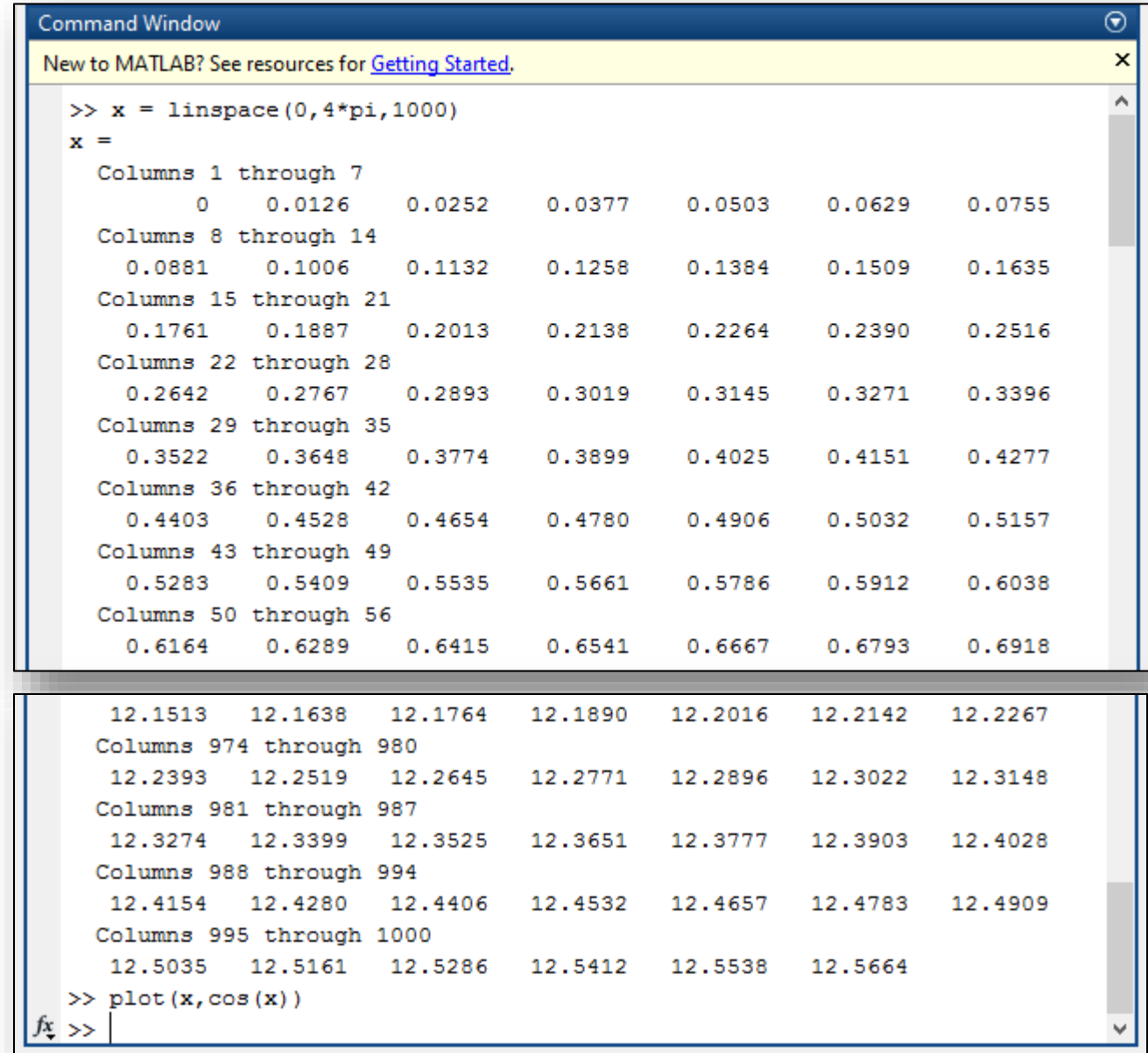
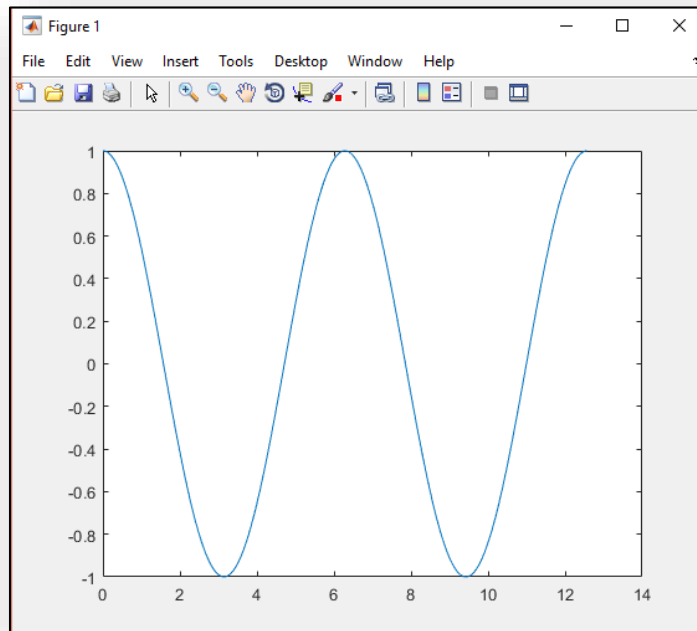
- Example

- ✓ `» x = linspace(0,4*pi,1000)`

- ✓ `» y = cos(x)`

- Plot values against their index

- ✓ `» plot(x, cos(x))`

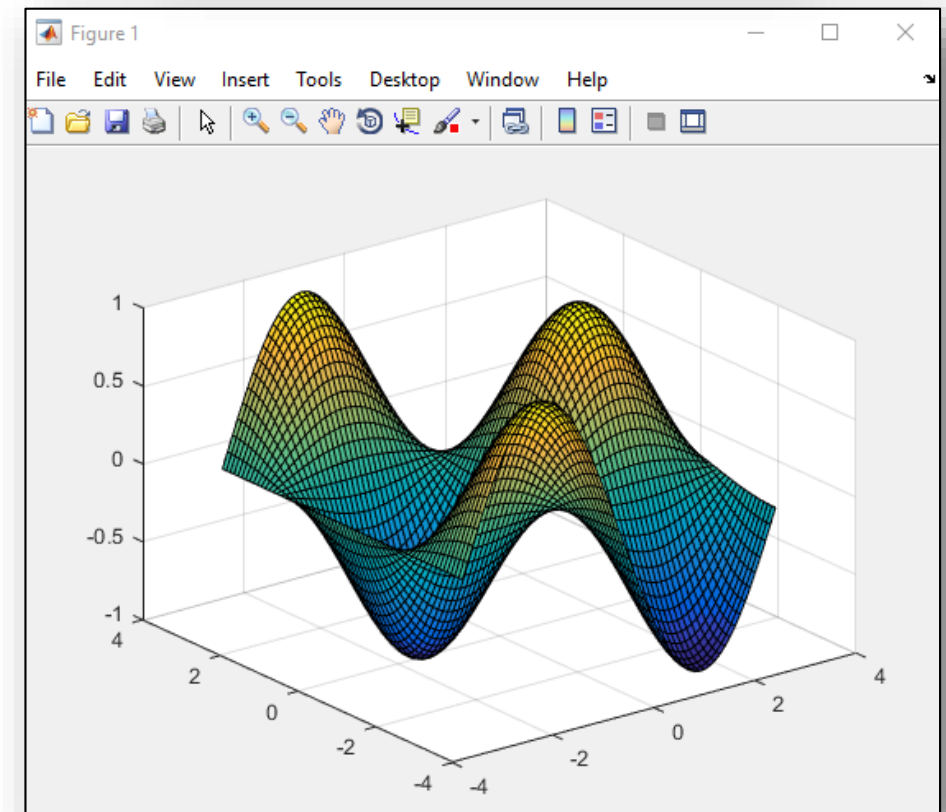


Surface Plots

- "surf" puts vertices at specified points in space x,y,z , and connects all the vertices to make a surface
- Example: make the x and y vectors
 - ✓ `>> x = -pi:0.1:pi;`
 - ✓ `>> y = -pi:0.1:pi;`
- Use meshgrid to make matrices (this is the same as loop)
 - ✓ `>> [X,Y] = meshgrid(x,y);`
- To get function values, evaluate the matrices
 - ✓ `>> Z = sin(X).*cos(Y);`
- Plot the surface
 - ✓ `>> surf(X,Y,Z) or surf(x,y,Z);`

```
Command Window
New to MATLAB? See resources for Getting Started. X

>> x = -pi:0.1:pi;
>> y = -pi:0.1:pi;
>> [X,Y]=meshgrid(x,y);
>> Z =sin(X).*cos(Y);
>> surf(X,Y,Z)
```

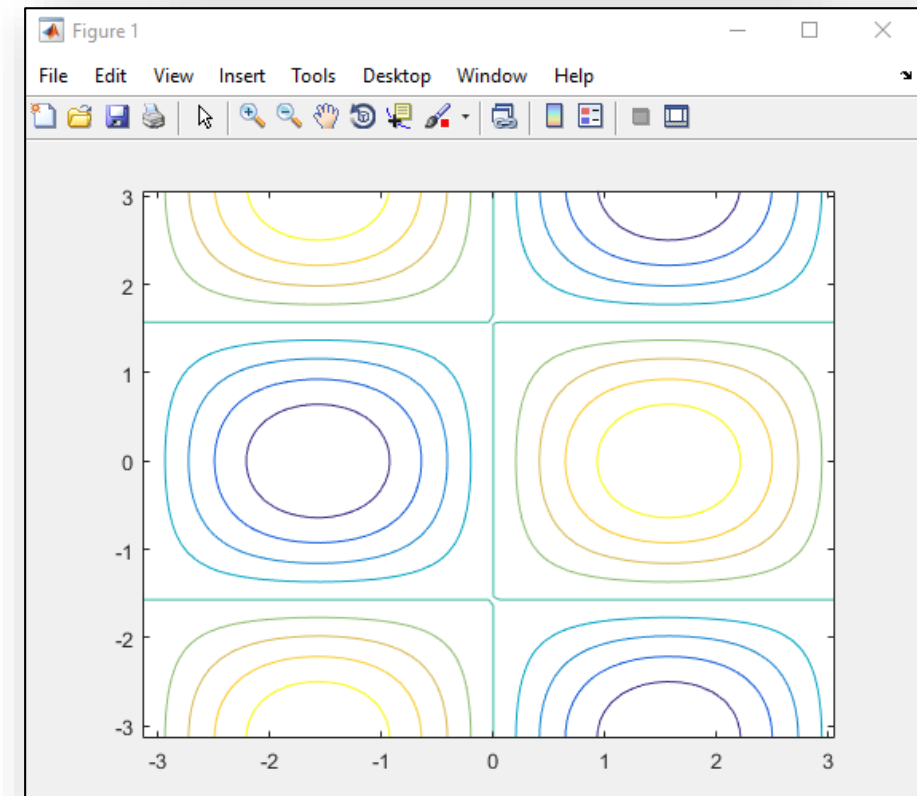


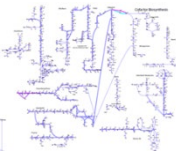
Contour Plots

- Contour plots make surfaces two-dimensional
 - ✓ `>> contour(X,Y,Z)`
 - ✓ Same arguments as surf
 - ✓ Color indicates height
- Example: make the x and y vectors
 - ✓ `>> x = -pi:0.1:pi;`
 - ✓ `>> y = -pi:0.1:pi;`
- Use meshgrid to make matrices (this is the same as loop)
 - ✓ `>> [X,Y] = meshgrid(x,y);`
- To get function values, evaluate the matrices
 - ✓ `>> Z = sin(X) .* cos(Y);`
- Plot the surface
 - ✓ `>> contour(X,Y,Z)`

```
Command Window
New to MATLAB? See resources for Getting Started. X

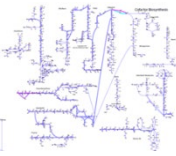
>> x = -pi:0.1:pi;
>> y = -pi:0.1:pi;
>> [X,Y] = meshgrid(x,y);
>> Z = sin(X) .* cos(Y);
>> contour(X,Y,Z)
fx >>
```





Course Introduction

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User-defined Functions

- The function declaration is given by

```
function[x, y, z] = funName(in1, in2)
```

Must use the
reserved word: function

If more than one output,
must be in brackets

Function name should match
Matlab file name

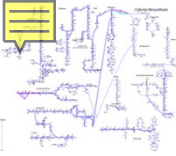
Inputs must be specified

- MATLAB 'returns' the variables whose names match those in the function declaration
- Any variables created within the function but not returned disappear after the function stops running

User-defined Function Example

```
function FBAsolution = optimizeCbModel(model,osenseStr, minNorm, allowLoops)
%optimizeCbModel Solve a flux balance analysis problem
%
% Solves LP problems of the form: max/min
%                               subject
%
% FBAsolution = optimizeCbModel(model,osenseStr, minNorm, allowLoops)
%
% INPUT
% model (the following fields are required)
%   S      Stoichiometric matrix
%   b      Right hand side = dx/dt
%   c      Objective coefficients
%   lb     Lower bounds
%   ub     Upper bounds
%
% OPTIONAL INPUTS
% osenseStr Maximize ('max')/minimize ('min')
% minNorm   {(0), 'one', > 0, n x 1}
%           0      Default, normal LP
%           'one'  Minimise the Taxicab norm
%           min |v|
%           s.t. S
%           C
%           l
%
% -----
% The remaining options work the same as in the
% -----
% > 0 Minimises the Euclidean norm
%     Typically 1e-6 works
%     min ||v||
%     s.t. S
%
% Markus Herrgard 8/21/06 Original code.
% Ronan Fleming 01/20/10 Take the extremal flux from the flux vector,
%                        not from the objective since this is invariant

function [minFlux,maxFlux,Vmin,Vmax] = fluxVariability(model,optPercentage,osenseStr,rxnNameList,verbFlag,
%fluxVariability Performs flux variability analysis
%
% [minFlux,maxFlux] = fluxVariability(model,optPercentage,osenseStr,rxnNameList,verbFlag, allowLoops)
%
% INPUT
% model COBRA model structure
%
% OPTIONAL INPUTS
% optPercentage Only consider solutions that give you at least a certain
%               percentage of the optimal solution (Default = 100
%               or optimal solutions only)
% osenseStr Objective sense ('min' or 'max') (Default = 'max')
% rxnNameList List of reactions for which FVA is performed
%             (Default = all reactions in the model)
% verbFlag Verbose output (opt, default false)
% allowLoops Whether loops are allowed in solution. (Default = true)
%           See optimizeCbModel for description
%
% OUTPUT
% minFlux Minimum flux for each reaction
% maxFlux Maximum flux for each reaction
%
% OPTIONAL OUTPUT
% Vmin Matrix of column flux vectors, where each column is a
%      separate minimization.
% Vmax Matrix of column flux vectors, where each column is a
%      separate maximization.
%
% Markus Herrgard 8/21/06 Original code.
% Ronan Fleming 01/20/10 Take the extremal flux from the flux vector,
%                        not from the objective since this is invariant
```



Relational & Logical Operators

- MATLAB uses mostly standard relational operators

✓ equal	==
✓ not equal	~=
✓ greater than	>
✓ less than	<
✓ greater or equal	>=
✓ less or equal	<=

- Logical operators (scalars)
- | | elementwise | short-circuit |
|------------|-------------|---------------|
| ✓ And | & | && |
| ✓ Or | | |
| ✓ Not | ~ | |
| ✓ Xor | xor | |
| ✓ All true | all | |
| ✓ Any true | any | |

- Boolean values: zero is false, nonzero is true

if/else/elseif

- Basic flow-control, common to all languages
- MATLAB syntax is somewhat unique
- No need for parentheses: since command blocks are between reserved words

IF

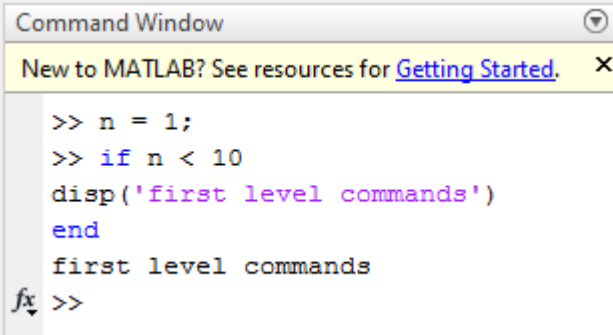
```
if cond
    commands
end
```

ELSE

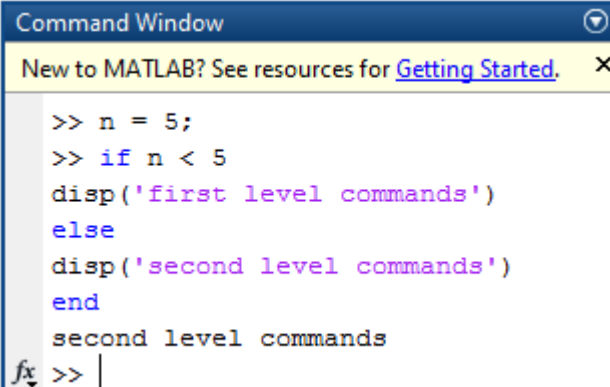
```
if cond
    commands1
else
    commands2
end
```

ELSEIF

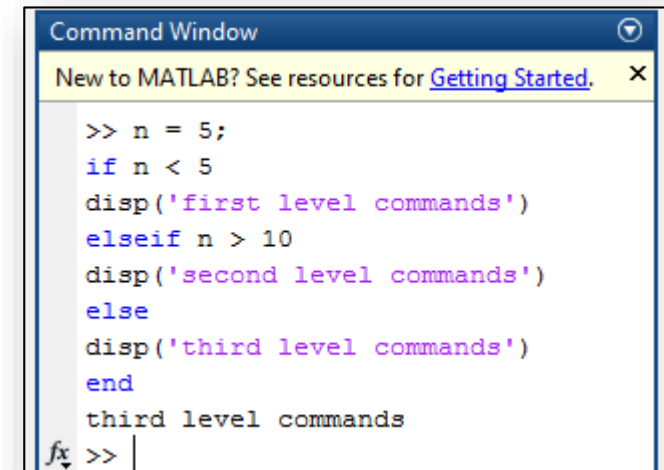
```
if cond1
    commands1
elseif cond2
    commands2
else
    commands3
end
```



```
Command Window
New to MATLAB? See resources for Getting Started. X
>> n = 1;
>> if n < 10
    disp('first level commands')
end
first level commands
fx >>
```



```
Command Window
New to MATLAB? See resources for Getting Started. X
>> n = 5;
>> if n < 5
    disp('first level commands')
else
    disp('second level commands')
end
second level commands
fx >> |
```



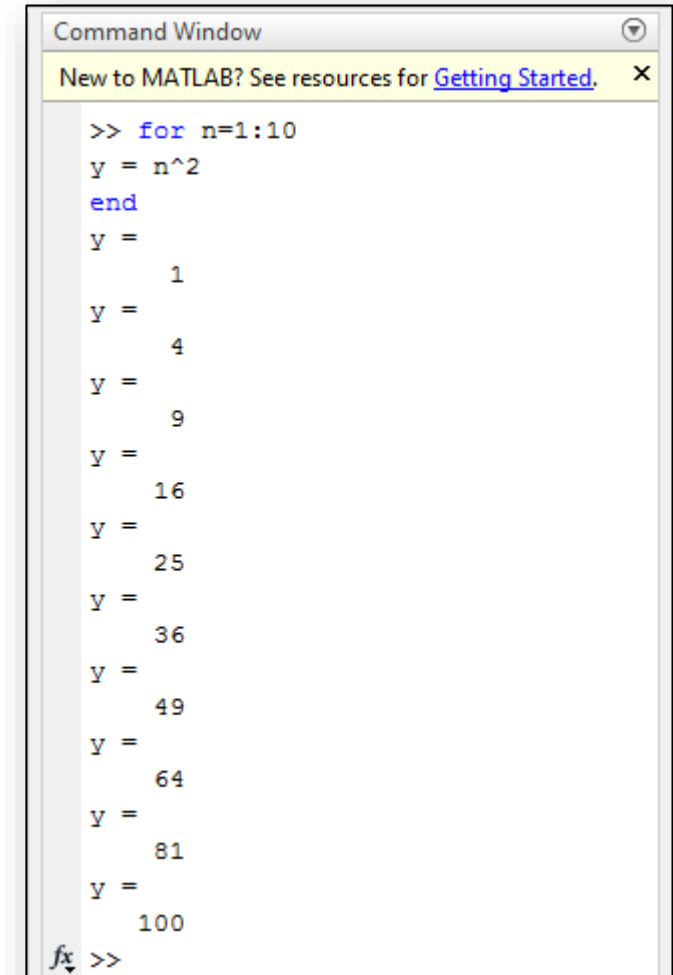
```
Command Window
New to MATLAB? See resources for Getting Started. X
>> n = 5;
if n < 5
    disp('first level commands')
elseif n > 10
    disp('second level commands')
else
    disp('third level commands')
end
third level commands
fx >> |
```

For Loops

- **for** loops: use for a known number of iterations
- MATLAB syntax:

```
for n=1:100
    commands
end
```

- The loop variable (**n**)
 - ✓ Is defined as a vector
 - ✓ Is a scalar within the command block
- The command block
 - ✓ Anything between the **for** line and the **end**



Command Window

New to MATLAB? See resources for [Getting Started.](#) X

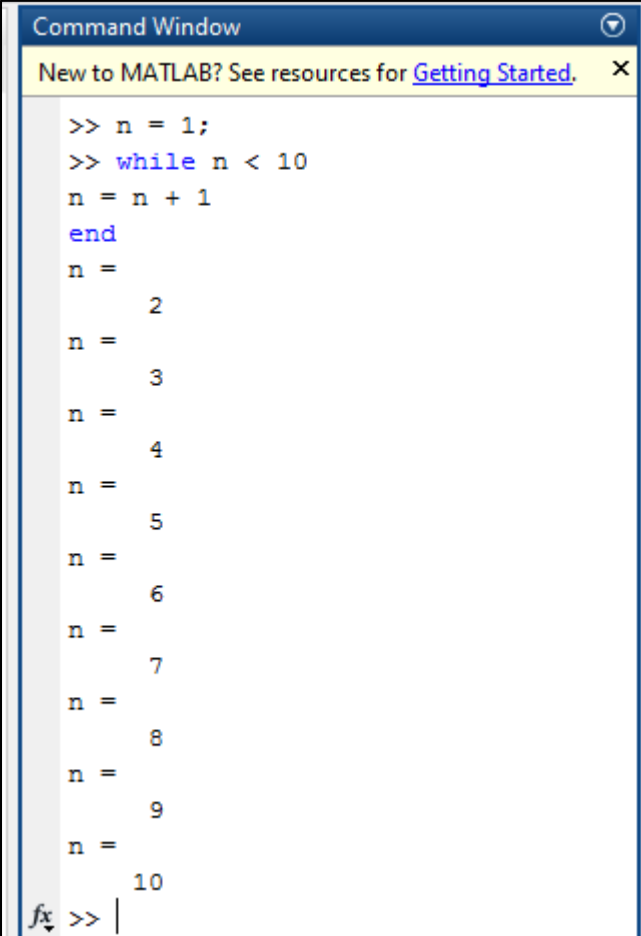
```
>> for n=1:10
y = n^2
end
y =
     1
     4
     9
    16
    25
    36
    49
    64
    81
   100
fx >>
```

While Statement

- The **while** is like a more general for loop that doesn't require the need to know the number of iterations

```
while cond
    commands
end
```

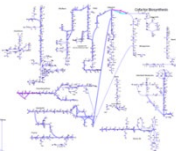
- The command block will execute while the conditional expression is true
- Beware of infinite loops!



The image shows a MATLAB Command Window with a blue title bar. A yellow banner at the top says "New to MATLAB? See resources for [Getting Started.](#)". The command history shows the following code being executed:

```
>> n = 1;
>> while n < 10
n = n + 1
end
```

The output of the loop is displayed on the right side of the window, showing the value of `n` at each iteration from 2 to 10. At the bottom, the prompt `fx >> |` is visible.

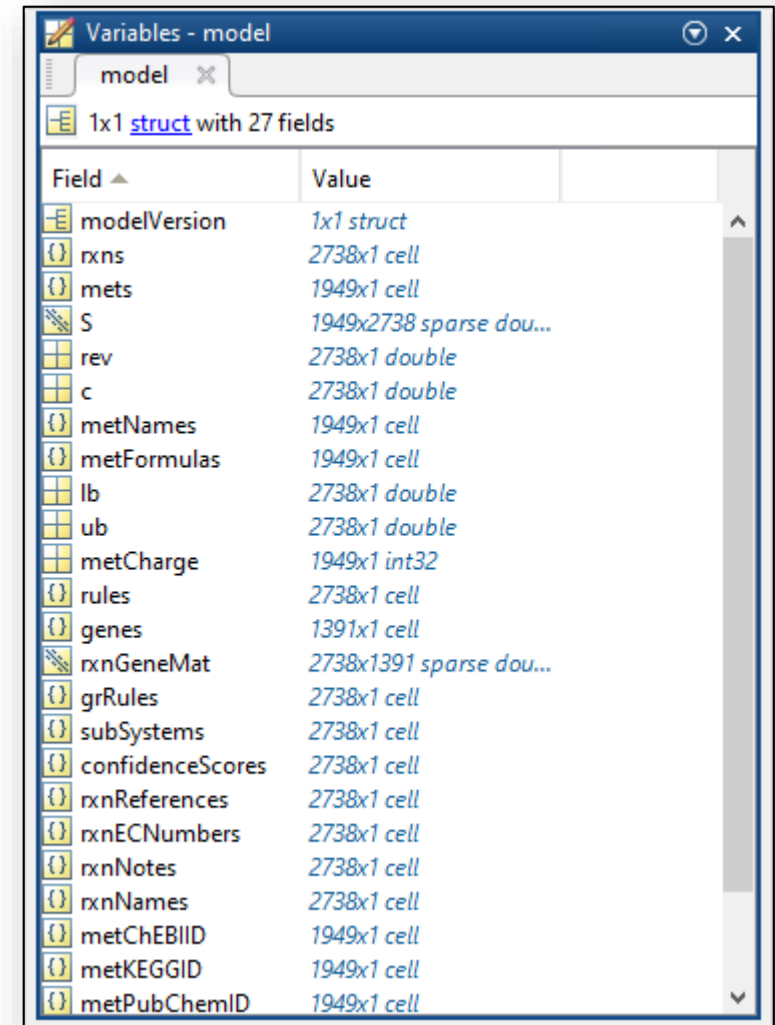


Course Introduction

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- ➔ • Data Structures

Data Structures

- Matrices
 - ✓ Can create n-dimensional matrices
 - ✓ All elements must be the same type (integers, double, character, ...)
 - ✓ Matrices are space-efficient and convenient for calculations
- More complex data structures are also possible in Matlab
 - ✓ Cell arrays - Like an array but the elements don't have to have to be the same type
 - ✓ Structs - Can be used to bundle variable names and values into one structure



Field	Value
modelVersion	1x1 struct
rxns	2738x1 cell
mets	1949x1 cell
S	1949x2738 sparse dou...
rev	2738x1 double
c	2738x1 double
metNames	1949x1 cell
metFormulas	1949x1 cell
lb	2738x1 double
ub	2738x1 double
metCharge	1949x1 int32
rules	2738x1 cell
genes	1391x1 cell
rxnGeneMat	2738x1391 sparse dou...
grRules	2738x1 cell
subSystems	2738x1 cell
confidenceScores	2738x1 cell
rxnReferences	2738x1 cell
rxnECNumbers	2738x1 cell
rxnNotes	2738x1 cell
rxnNames	2738x1 cell
metChEBIID	1949x1 cell
metKEGGID	1949x1 cell
metPubChemID	1949x1 cell

Cells

- A cell is just like a matrix, but each field can contain anything (even other matrices):
- To initialize a cell, specify the size
 - ✓ `>> a = cell(3,10);`
 - will create a cell with 3 rows and 10 columns
- Create a cell manually with curly braces {}
 - ✓ `>> c = {'metabolism',[1 5 6 2],rand(3,2)};`
 - c is a cell with 1 row and 3 columns
- Each element of a cell can be anything
- To access a cell element, use curly braces {}
 - ✓ `>> a{1,1} = [1 3 4 -10];`
 - ✓ `>> a{2,1} = 'hello world 2';`
 - ✓ `>> a{1,2} = c{3};`

Command Window

New to MATLAB? See resources for [Getting Started](#).

```
>> a = cell(3,10)

a =

    []    []    []    []    []    []    []    []    []    []
    []    []    []    []    []    []    []    []    []    []
    []    []    []    []    []    []    []    []    []    []

>> c = {'metabolism',[1 5 6 2],rand(3,2)}

c =

    'metabolism'    [1x4 double]    [3x2 double]

>> a{1,1} = [1 3 4 -10];
>> a{2,1} = 'hello world 2';
>> a{1,2} = c{3};
```

Variables - c

	1	2	3	4	5	6	7
1	'metabolism'	[1,5,6,2]	[0.9572,0.14...				
2							

Variables - a

	1	2	3	4	5	6	7
1	[1,3,4,-10]	[0.9572,0....	[]	[]	[]	[]	[]
2	'hello world...	[]	[]	[]	[]	[]	[]
3	[]	[]	[]	[]	[]	[]	[]
4							

Structs

- Structs allow you to name and bundle relevant variables
 - ✓ Like C-structs, which are objects with fields
- To add fields
 - ✓ Fields can be anything: matrix, cell, even struct
 - ✓ Useful for keeping variables together
 - ✓ » `model.reactions = {'Ex_glc(e)'; 'EX_o2(e)'}`
 - ✓ » `model.metabolites = {'glc[c]'; 'o2[c]'}`
 - ✓ » `model.flux = [1.45; 0.35]`
- Accessing values from the struct
 - ✓ » `model.reactions(2)`
 - ✓ » `model.metabolites(1)`
 - ✓ » `model.flux(2)`

```
Command Window

>> model.reactions = {'Ex_glc(e)'; 'EX_o2(e)'}

model =

    reactions: {2x1 cell}

>> model.metabolites = {'glc[c]'; 'o2[c]'}

model =

    reactions: {2x1 cell}
    metabolites: {2x1 cell}

>> model.flux = [1.45; 0.35]

model =

    reactions: {2x1 cell}
    metabolites: {2x1 cell}
    flux: [2x1 double]

>> model.reactions(2)

ans =

    'EX_o2(e)'

>> model.metabolites(1)

ans =

    'glc[c]'
```

Structs (2 of 2)

Variables - model

model

1x1 struct with 3 fields

Field	Value
reactions	2x1 cell
metabolites	2x1 cell
flux	[1.4500;0.3500]

Variables - model.reactions

model model.reactions

model.reactions

	1	2	3	4	5	6
1	Ex_glc(e)					
2	EX_o2(e)					
3						

Variables - model.metabolites

model model.reactions model.metabolites

model.metabolites

	1	2	3	4	5	6
1	glc[c]					
2	o2[c]					
3						

Command Window

```
>> model.reactions = {'Ex_glc(e)'; 'EX_o2(e)'}

model =

    reactions: {2x1 cell}

>> model.metabolites = {'glc[c]'; 'o2[c]'}

model =

    reactions: {2x1 cell}
    metabolites: {2x1 cell}

>> model.flux = [1.45; 0.35]

model =

    reactions: {2x1 cell}
    metabolites: {2x1 cell}
    flux: [2x1 double]

>> model.reactions(2)

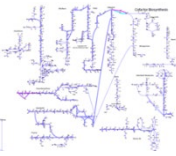
ans =

    'EX_o2(e) '

>> model.metabolites(1)

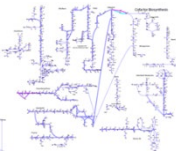
ans =

    'glc[c] '
```



Course Introduction

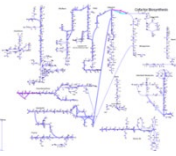
- Desktop
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- Scripts
- Operations
- Visualization
- Programming
- Data Structures



Lecture Learning Objectives

Each student should be able to:

- Describe the Matlab desktop
- Explain the basic use of Matlab variables
- Explain the basic use of Matlab scripts
- Explain the basic mathematical operations in Matlab
- Explain the simple Matlab visualization techniques
- Explain simple Matlab programming
- Explain the basic data structures available in Matlab



References

- [Matlab documentation](#)
- [MIT Opencourseware, introduction to Matlab by Danilo Šćepanović](#)
- Matlab Academy - https://matlabacademy.mathworks.com/?s_tid=srchtitle
- [Getting started with Matlab](#)