

# Day 81/180 Time and Space Complexity in Recursion

**Calculate the time and space complexity of each program**

1:

```
int fact(int n)
{
    if(n<=1)
        return 1;

    return n*fact(n-1);
}
```

**Recursive calls** : fact(n) -> fact(n-1) -> ... ..... -> fact(1).

**Time Complexity** :  $O(n)$

**Space Complexity** :  $O(n)$

2:

```
int power(int base, int exponent) {
    if (exponent == 0)
        return 1;
    return base * power(base, exponent - 1);
}
```

**Recursive calls** : power(base, exponent ) -> power(base, exponent -1 )-> ... ..... -> power(base, 0 ).

So, no of recursive calls are dependent on exponent variable.

**Time Complexity** :  $O(\text{exponent})$   
**Space Complexity** :  $O(\text{exponent})$

3:

```
bool isPalindrome(string str, int start, int end) {  
    if (start >= end)  
        return true;  
    return (str[start] == str[end]) && isPalindrome(str, start + 1, end - 1);  
}
```

**Assume** : size of str = n

**Recursive calls** : isPalindrome( str, 0, n -1) -> isPalindrome( str, 1 ,  
n-2) -> isPalindrome( str, start+2, n-3) -> ..... ->  
isPalindrome( str, mid, mid)

So, no of recursive call will be ther (start to mid) or (mid to end)  
that is  $n/2$  i.e size of str.

But Here **str is passed by value**, so for each of the recursive call  
new string created for that call. So, copying str will take  **$O(n)$**  time  
complexity for each calls and there are nearly  **$n/2$**  calls.

Here **str is passed by value**, so for each of the recursive call  
new string created for that call. So, each calls space complexity is  
 **$O(n)$** , and there are nearly  **$n/2$**  calls.

**Time Complexity** :  $O(n^2)$   
**Space Complexity** :  $O(n^2)$

4:

```
void reverseString(string& str, int start, int end) {  
    if (start < end) {
```

```

        swap(str[start], str[end]);
        reverseString(str, start + 1, end - 1);
    }
}

```

**Assume** : size of str = n

**Recursive calls** : reverseString( str, 0, n - 1) -> reverseString( str, 1 , n-2) -> reverseString( str, start+2, n-3) -> ..... -> reverseString( str, mid, mid)

So, no of recursive call will be ther (start to mid) or (mid to end) that is  $n/2$ .

Here **str is passed by reference**, so it the same str in every call, so, no extra space.

**Time Complexity** :  $O(n)$

**Space Complexity** :  $O(n)$

5:

```

bool isEven(int n) {
    if (n == 0)
        return true;
    return !isEven(n - 1);
}

```

**Recursive calls** : isEven(n) -> isEven(n-1) -> ... -> isEven(0)

**Time Complexity** :  $O(n)$

**Space Complexity** :  $O(n)$