

Robertson-Walker Metric:

$$\boxed{x^\mu}$$

$$\begin{aligned}x^0 &= t. \\ x^1 &= r. \\ x^2 &= \theta. \\ x^3 &= \phi.\end{aligned}$$

$$\boxed{g_{\mu\nu}}$$

$$\begin{aligned}g_{00} &= 1. \\ g_{01} &= 0. \\ g_{02} &= 0. \\ g_{03} &= 0. \\ g_{10} &= 0. \\ g_{11} &= \frac{R(t)^2}{-1+\kappa r^2}. \\ g_{12} &= 0. \\ g_{13} &= 0. \\ g_{20} &= 0. \\ g_{21} &= 0. \\ g_{22} &= -R(t)^2r^2. \\ g_{23} &= 0. \\ g_{30} &= 0. \\ g_{31} &= 0. \\ g_{32} &= 0. \\ g_{33} &= -R(t)^2\sin(\theta)^2r^2.\end{aligned}$$

$$\boxed{\sqrt{=\sqrt{-\det(g_{\mu\nu})}}}$$

$$\sqrt{=\sqrt{-\frac{R(t)^6\sin(\theta)^2r^4}{-1+\kappa r^2}}}.$$

$$\boxed{g^{\mu\nu}}$$

$$\begin{aligned}g^{00} &= 1. \\ g^{01} &= 0. \\ g^{02} &= 0. \\ g^{03} &= 0. \\ g^{10} &= 0. \\ g^{11} &= \frac{-1+\kappa r^2}{R(t)^2}. \\ g^{12} &= 0. \\ g^{13} &= 0. \\ g^{20} &= 0. \\ g^{21} &= 0. \\ g^{22} &= -\frac{1}{R(t)^2r^2}. \\ g^{23} &= 0. \\ g^{30} &= 0. \\ g^{31} &= 0. \\ g^{32} &= 0. \\ g^{33} &= -\frac{1}{R(t)^2\sin(\theta)^2r^2}.\end{aligned}$$

$$\boxed{\Gamma^\sigma_{\mu\nu}}$$

$$\begin{aligned}\Gamma^0_{00} &= 0. \\ \Gamma^0_{01} &= 0. \\ \Gamma^0_{02} &= 0. \\ \Gamma^0_{03} &= 0. \\ \Gamma^0_{10} &= 0. \\ \Gamma^0_{11} &= -\frac{R(t)\dot{R}(t)}{-1+\kappa r^2}. \\ \Gamma^0_{12} &= 0. \\ \Gamma^0_{13} &= 0. \\ \Gamma^0_{20} &= 0. \\ \Gamma^0_{21} &= 0. \\ \Gamma^0_{22} &= R(t)r^2\dot{R}(t). \\ \Gamma^0_{23} &= 0. \\ \Gamma^0_{30} &= 0. \\ \Gamma^0_{31} &= 0. \\ \Gamma^0_{32} &= 0. \\ \Gamma^0_{33} &= R(t)\sin(\theta)^2r^2\dot{R}(t).\end{aligned}$$

$$\begin{aligned}\Gamma^1_{00} &= 0. \\ \Gamma^1_{01} &= \frac{\dot{R}(t)}{R(t)}. \\ \Gamma^1_{02} &= 0. \\ \Gamma^1_{03} &= 0. \\ \Gamma^1_{10} &= \frac{\dot{R}(t)}{R(t)}. \\ \Gamma^1_{11} &= -\frac{\kappa r}{-1+\kappa r^2}. \\ \Gamma^1_{12} &= 0. \\ \Gamma^1_{13} &= 0. \\ \Gamma^1_{20} &= 0. \\ \Gamma^1_{21} &= 0. \\ \Gamma^1_{22} &= (-1+\kappa r^2)r. \\ \Gamma^1_{23} &= 0. \\ \Gamma^1_{30} &= 0. \\ \Gamma^1_{31} &= 0. \\ \Gamma^1_{32} &= 0. \\ \Gamma^1_{33} &= (-1+\kappa r^2)\sin(\theta)^2r.\end{aligned}$$

$$\begin{aligned}\Gamma_{00}^2 &= 0, \\ \Gamma_{01}^2 &= 0, \\ \Gamma_{02}^2 &= \frac{\dot{R}(t)}{R(t)}, \\ \Gamma_{03}^2 &= 0, \\ \Gamma_{10}^2 &= 0, \\ \Gamma_{11}^2 &= 0, \\ \Gamma_{12}^2 &= \frac{1}{r}, \\ \Gamma_{13}^2 &= 0, \\ \Gamma_{20}^2 &= \frac{\dot{R}(t)}{R(t)}, \\ \Gamma_{21}^2 &= \frac{1}{r}, \\ \Gamma_{22}^2 &= 0, \\ \Gamma_{23}^2 &= 0, \\ \Gamma_{30}^2 &= 0, \\ \Gamma_{31}^2 &= 0, \\ \Gamma_{32}^2 &= 0, \\ \Gamma_{33}^2 &= -\cos(\theta)\sin(\theta).\end{aligned}$$

$$\begin{aligned}\Gamma_{00}^3 &= 0, \\ \Gamma_{01}^3 &= 0, \\ \Gamma_{02}^3 &= 0,\end{aligned}$$

$$\begin{aligned}\Gamma_{03}^3 &= \frac{\dot{R}(t)}{R(t)}, \\ \Gamma_{10}^3 &= 0, \\ \Gamma_{11}^3 &= 0, \\ \Gamma_{12}^3 &= 0, \\ \Gamma_{13}^3 &= \frac{1}{r}, \\ \Gamma_{20}^3 &= 0, \\ \Gamma_{21}^3 &= 0, \\ \Gamma_{22}^3 &= 0,\end{aligned}$$

$$\Gamma_{23}^3 = \frac{\cos(\theta)}{\sin(\theta)},$$

$$\Gamma_{30}^3 = \frac{\dot{R}(t)}{R(t)}.$$

$$\Gamma_{31}^3 = \frac{1}{r}.$$

$$\Gamma_{32}^3 = \frac{\cos(\theta)}{\sin(\theta)}.$$

$$\Gamma_{33}^3 = 0.$$

$$\boxed{R_{\mu\nu}}$$

$$R_{00} = 3\frac{\ddot{R}(t)}{R(t)},$$

$$R_{01} = 0.$$

$$R_{02} = 0.$$

$$R_{03} = 0.$$

$$R_{10} = 0.$$

$$R_{11} = \frac{2\kappa + 2\dot{R}(t)^2 + R(t)\ddot{R}(t)}{-1 + \kappa r^2}.$$

$$R_{12} = 0.$$

$$R_{13} = 0.$$

$$R_{20} = 0.$$

$$R_{21} = 0.$$

$$R_{22} = -2\kappa r^2 - 2r^2\dot{R}(t)^2 - R(t)\ddot{R}(t)r^2.$$

$$R_{23} = 0.$$

$$R_{30} = 0.$$

$$R_{31} = 0.$$

$$R_{32} = 0.$$

$$R_{33} = -R(t)\dot{R}(t)\sin(\theta)^2r^2 - 2\kappa\sin(\theta)^2r^2 - 2\sin(\theta)^2r^2\dot{R}(t)^2.$$

$$\boxed{R^\mu{}_\nu}$$

$$R^0{}_0 = 3\frac{\ddot{R}(t)}{R(t)}.$$

$$R^0{}_1 = 0.$$

$$R^0{}_2 = 0.$$

$$R^0{}_3 = 0.$$

$$R^1{}_0 = 0.$$

$$R^1{}_1 = 2\frac{\kappa}{R(t)^2} + \frac{\ddot{R}(t)}{R(t)} + 2\frac{\dot{R}(t)^2}{R(t)^2}.$$

$$R^1{}_2 = 0.$$

$$R^1{}_3 = 0.$$

$$R^2{}_0 = 0.$$

$$R^2{}_1 = 0.$$

$$R^2{}_2 = 2\frac{\kappa}{R(t)^2} + \frac{\ddot{R}(t)}{R(t)} + 2\frac{\dot{R}(t)^2}{R(t)^2}.$$

$$R^2{}_3 = 0.$$

$$R^3{}_0 = 0.$$

$$R^3{}_1 = 0.$$

$$R^3{}_2 = 0.$$

$$R^3{}_3 = 2\frac{\kappa}{R(t)^2} + \frac{\ddot{R}(t)}{R(t)} + 2\frac{\dot{R}(t)^2}{R(t)^2}.$$

$$\boxed{R}$$

$$R = 6\frac{\kappa}{R(t)^2} + 6\frac{\ddot{R}(t)}{R(t)} + 6\frac{\dot{R}(t)^2}{R(t)^2}.$$

$$\boxed{G_{\nu}^{\mu}}$$

$$G_0^0 = -3 \frac{\kappa}{R(t)^2} - 3 \frac{\dot{R}(t)^2}{R(t)^2}.$$

$$G_1^0 = 0.$$

$$G_2^0 = 0.$$

$$G_3^0 = 0.$$

$$G_0^1 = 0.$$

$$G_1^1 = -\frac{\kappa}{R(t)^2} - 2 \frac{\ddot{R}(t)}{R(t)} - \frac{\dot{R}(t)^2}{R(t)^2}.$$

$$G_2^1 = 0.$$

$$G_3^1 = 0.$$

$$G_0^2 = 0.$$

$$G_1^2 = 0.$$

$$G_2^2 = -\frac{\kappa}{R(t)^2} - 2 \frac{\ddot{R}(t)}{R(t)} - \frac{\dot{R}(t)^2}{R(t)^2}.$$

$$G_3^2 = 0.$$

$$G_0^3 = 0.$$

$$G_1^3 = 0.$$

$$G_2^3 = 0.$$

$$G_3^3 = -\frac{\kappa}{R(t)^2} - 2 \frac{\ddot{R}(t)}{R(t)} - \frac{\dot{R}(t)^2}{R(t)^2}.$$

$$\boxed{G}$$

$$G = -6 \frac{\kappa}{R(t)^2} - 6 \frac{\ddot{R}(t)}{R(t)} - 6 \frac{\dot{R}(t)^2}{R(t)^2}.$$

$$\boxed{G_{\nu;\mu}^{\mu} = 0}$$

$$G_{0,\mu}^{\mu} = 0.$$

$$G_{1,\mu}^{\mu} = 0.$$

$$G_{2,\mu}^{\mu} = 0.$$

$$G_{3,\mu}^{\mu} = 0.$$

$$\boxed{g^{\mu\nu}\,\Gamma_{\mu\nu}^{\lambda} = 0?}$$

$$g^{\mu\nu}\,\Gamma_{\mu\nu}^0 = -\frac{\kappa^2 R(t)^3 r^8 \dot{R}(t)}{(-1+\kappa r^2)^2} + 2 \frac{\kappa R(t)^3 \sin(\theta)^4 r^6 \dot{R}(t)}{(-1+\kappa r^2)^2} + 2 \frac{\kappa R(t)^3 r^6 \dot{R}(t)}{(-1+\kappa r^2)^2} - \frac{R(t)^3 \sin(\theta)^4 r^4 \dot{R}(t)}{(-1+\kappa r^2)^2} - \frac{R(t)^3 \dot{R}(t)}{(-1+\kappa r^2)^2} - \frac{\kappa^2 R(t)^3 \sin(\theta)^4 r^8 \dot{R}(t)}{(-1+\kappa r^2)^2} - \frac{R(t)^3 r^4 \dot{R}(t)}{(-1+\kappa r^2)^2}.$$

$$g^{\mu\nu}\,\Gamma_{\mu\nu}^1 = \frac{R(t)^2 \sin(\theta)^4 r^3}{(-1+\kappa r^2)^2} - \frac{\kappa^3 R(t)^2 r^9}{(-1+\kappa r^2)^2} - 3 \frac{\kappa R(t)^2 r^5}{(-1+\kappa r^2)^2} + \frac{R(t)^2 r^3}{(-1+\kappa r^2)^2} - \frac{\kappa^3 R(t)^2 \sin(\theta)^4 r^9}{(-1+\kappa r^2)^2} - 3 \frac{\kappa R(t)^2 \sin(\theta)^4 r^5}{(-1+\kappa r^2)^2} + 3 \frac{\kappa^2 R(t)^2 \sin(\theta)^4 r^7}{(-1+\kappa r^2)^2} + 3 \frac{\kappa^2 \dot{R}(t)^2 r^7}{(-1+\kappa r^2)^2} - \frac{\kappa R(t)^2 r}{(-1+\kappa r^2)^2}.$$

$$g^{\mu\nu}\,\Gamma_{\mu\nu}^2 = \cos(\theta) R(t)^2 \sin(\theta)^3 r^2.$$

$$g^{\mu\nu}\,\Gamma_{\mu\nu}^3 = 0.$$