

Robertson-Walker Metric of a flat universe:

$$\boxed{x^\mu}$$

$$\begin{aligned}x^0 &= t. \\ x^1 &= r. \\ x^2 &= \theta. \\ x^3 &= \phi.\end{aligned}$$

$$\boxed{g_{\mu\nu}}$$

$$\begin{aligned}g_{00} &= 1. \\ g_{01} &= 0. \\ g_{02} &= 0. \\ g_{03} &= 0. \\ g_{10} &= 0. \\ g_{11} &= -a(t)^2. \\ g_{12} &= 0. \\ g_{13} &= 0. \\ g_{20} &= 0. \\ g_{21} &= 0. \\ g_{22} &= -r^2a(t)^2. \\ g_{23} &= 0. \\ g_{30} &= 0. \\ g_{31} &= 0. \\ g_{32} &= 0. \\ g_{33} &= -r^2a(t)^2\sin(\theta)^2.\end{aligned}$$

$$\boxed{\sqrt{-\det(g_{\mu\nu})}}$$

$$\sqrt{-\det(g_{\mu\nu})} = \sqrt{r^4a(t)^6\sin(\theta)^2}.$$

$$\boxed{g^{\mu\nu}}$$

$$\begin{aligned}g^{00} &= 1. \\ g^{01} &= 0. \\ g^{02} &= 0. \\ g^{03} &= 0. \\ g^{10} &= 0. \\ g^{11} &= -\frac{1}{a(t)^2}. \\ g^{12} &= 0. \\ g^{13} &= 0. \\ g^{20} &= 0. \\ g^{21} &= 0. \\ g^{22} &= -\frac{1}{r^2a(t)^2}. \\ g^{23} &= 0. \\ g^{30} &= 0. \\ g^{31} &= 0. \\ g^{32} &= 0. \\ g^{33} &= -\frac{1}{r^2a(t)^2\sin(\theta)^2}.\end{aligned}$$

$$\boxed{\Gamma^\sigma_{\mu\nu}}$$

$$\begin{aligned}\Gamma^0_{00} &= 0. \\ \Gamma^0_{01} &= 0. \\ \Gamma^0_{02} &= 0. \\ \Gamma^0_{03} &= 0. \\ \Gamma^0_{10} &= 0. \\ \Gamma^0_{11} &= \dot{a}(t)a(t). \\ \Gamma^0_{12} &= 0. \\ \Gamma^0_{13} &= 0. \\ \Gamma^0_{20} &= 0. \\ \Gamma^0_{21} &= 0. \\ \Gamma^0_{22} &= r^2\dot{a}(t)a(t). \\ \Gamma^0_{23} &= 0. \\ \Gamma^0_{30} &= 0. \\ \Gamma^0_{31} &= 0. \\ \Gamma^0_{32} &= 0. \\ \Gamma^0_{33} &= r^2\dot{a}(t)a(t)\sin(\theta)^2.\end{aligned}$$

$$\begin{aligned}\Gamma^1_{00} &= 0. \\ \Gamma^1_{01} &= \frac{\dot{a}(t)}{a(t)}. \\ \Gamma^1_{02} &= 0. \\ \Gamma^1_{03} &= 0. \\ \Gamma^1_{10} &= \frac{\dot{a}(t)}{a(t)}. \\ \Gamma^1_{11} &= 0. \\ \Gamma^1_{12} &= 0. \\ \Gamma^1_{13} &= 0. \\ \Gamma^1_{20} &= 0. \\ \Gamma^1_{21} &= 0. \\ \Gamma^1_{22} &= -r. \\ \Gamma^1_{23} &= 0. \\ \Gamma^1_{30} &= 0. \\ \Gamma^1_{31} &= 0. \\ \Gamma^1_{32} &= 0. \\ \Gamma^1_{33} &= -r\sin(\theta)^2.\end{aligned}$$

$$\begin{aligned}
\Gamma_{00}^2 &= 0, \\
\Gamma_{01}^2 &= 0, \\
\Gamma_{02}^2 &= \frac{\dot{a}(t)}{a(t)}, \\
\Gamma_{03}^2 &= 0, \\
\Gamma_{10}^2 &= 0, \\
\Gamma_{11}^2 &= 0, \\
\Gamma_{12}^2 &= \frac{1}{r}, \\
\Gamma_{13}^2 &= 0, \\
\Gamma_{20}^2 &= \frac{\dot{a}(t)}{a(t)}, \\
\Gamma_{21}^2 &= \frac{1}{r}, \\
\Gamma_{22}^2 &= 0, \\
\Gamma_{23}^2 &= 0, \\
\Gamma_{30}^2 &= 0, \\
\Gamma_{31}^2 &= 0, \\
\Gamma_{32}^2 &= 0, \\
\Gamma_{33}^2 &= -\cos(\theta)\sin(\theta).
\end{aligned}$$

$$\begin{aligned}
\Gamma_{00}^3 &= 0, \\
\Gamma_{01}^3 &= 0, \\
\Gamma_{02}^3 &= 0, \\
\Gamma_{03}^3 &= \frac{\dot{a}(t)}{a(t)}, \\
\Gamma_{10}^3 &= 0, \\
\Gamma_{11}^3 &= 0, \\
\Gamma_{12}^3 &= 0, \\
\Gamma_{13}^3 &= \frac{1}{r}, \\
\Gamma_{20}^3 &= 0, \\
\Gamma_{21}^3 &= 0, \\
\Gamma_{22}^3 &= 0, \\
\Gamma_{23}^3 &= \frac{\cos(\theta)}{\sin(\theta)}, \\
\Gamma_{30}^3 &= \frac{\dot{a}(t)}{a(t)}, \\
\Gamma_{31}^3 &= \frac{1}{r}, \\
\Gamma_{32}^3 &= \frac{\cos(\theta)}{\sin(\theta)}, \\
\Gamma_{33}^3 &= 0.
\end{aligned}$$

$$R_{\mu\nu}$$

$$\begin{aligned}
R_{00} &= 3\frac{\ddot{a}(t)}{a(t)}, \\
R_{01} &= 0, \\
R_{02} &= 0, \\
R_{03} &= 0, \\
R_{10} &= 0, \\
R_{11} &= -\ddot{a}(t)a(t) - 2\dot{a}(t)^2, \\
R_{12} &= 0, \\
R_{13} &= 0, \\
R_{20} &= 0, \\
R_{21} &= 0, \\
R_{22} &= -2r^2\dot{a}(t)^2 - \ddot{a}(t)r^2a(t), \\
R_{23} &= 0, \\
R_{30} &= 0, \\
R_{31} &= 0, \\
R_{32} &= 0, \\
R_{33} &= -\ddot{a}(t)r^2a(t)\sin(\theta)^2 - 2r^2\dot{a}(t)^2\sin(\theta)^2.
\end{aligned}$$

$$R^{\mu}{}_{\nu}$$

$$\begin{aligned}
R^0{}_0 &= 3\frac{\ddot{a}(t)}{a(t)}, \\
R^0{}_1 &= 0, \\
R^0{}_2 &= 0, \\
R^0{}_3 &= 0, \\
R^1{}_0 &= 0, \\
R^1{}_1 &= 2\frac{\dot{a}(t)^2}{a(t)^2} + \frac{\ddot{a}(t)}{a(t)}, \\
R^1{}_2 &= 0, \\
R^1{}_3 &= 0, \\
R^2{}_0 &= 0, \\
R^2{}_1 &= 0, \\
R^2{}_2 &= 2\frac{\dot{a}(t)^2}{a(t)^2} + \frac{\ddot{a}(t)}{a(t)}, \\
R^2{}_3 &= 0, \\
R^3{}_0 &= 0, \\
R^3{}_1 &= 0, \\
R^3{}_2 &= 0, \\
R^3{}_3 &= 2\frac{\dot{a}(t)^2}{a(t)^2} + \frac{\ddot{a}(t)}{a(t)}.
\end{aligned}$$

$$R$$

$$R=6\frac{\dot{a}(t)^2}{a(t)^2}+6\frac{\ddot{a}(t)}{a(t)}.$$

$$\boxed{G^\mu{}_\nu}$$

$$G^0_0=-3\frac{\dot{a}(t)^2}{a(t)^2}.$$

$$G^0_1=0.$$

$$G^0_2=0.$$

$$G^0_3=0.$$

$$G^1_0=0.$$

$$G^1_1=-\frac{\dot{a}(t)^2}{a(t)^2}-2\frac{\ddot{a}(t)}{a(t)}.$$

$$G^1_2=0.$$

$$G^1_3=0.$$

$$G^2_0=0.$$

$$G^2_1=0.$$

$$G^2_2=-\frac{\dot{a}(t)^2}{a(t)^2}-2\frac{\ddot{a}(t)}{a(t)}.$$

$$G^2_3=0.$$

$$G^3_0=0.$$

$$G^3_1=0.$$

$$G^3_2=0.$$

$$G^3_3=-\frac{\dot{a}(t)^2}{a(t)^2}-2\frac{\ddot{a}(t)}{a(t)}.$$

$$\boxed{G}$$

$$G=-6\frac{\dot{a}(t)^2}{a(t)^2}-6\frac{\ddot{a}(t)}{a(t)}.$$

$$\boxed{G^\mu{}_{\nu;\mu}=0}$$

$$G^\mu{}_{6;\mu}=0.$$

$$G^\mu{}_{1;\mu}=0.$$

$$G^\mu{}_{2;\mu}=0.$$

$$G^\mu{}_{3;\mu}=0.$$

$$\boxed{g^{\mu\nu}\,\Gamma^\lambda_{\mu\nu}=0?}$$

$$g^{\mu\nu}\,\Gamma^0_{\mu\nu}=-r^4\dot{a}(t)a(t)^3-r^4\dot{a}(t)a(t)^3\sin(\theta)^4-\dot{a}(t)a(t)^3.$$

$$g^{\mu\nu}\,\Gamma^1_{\mu\nu}=r^3a(t)^2+r^3a(t)^2\sin(\theta)^4.$$

$$g^{\mu\nu}\,\Gamma^2_{\mu\nu}=r^2\cos(\theta)a(t)^2\sin(\theta)^3.$$

$$g^{\mu\nu}\,\Gamma^3_{\mu\nu}=0.$$