

Robertson-Walker Metric in proper distance:

$$\boxed{x^\mu}$$

$$\begin{aligned}x^0 &= t, \\ x^1 &= p, \\ x^2 &= \theta, \\ x^3 &= \phi.\end{aligned}$$

$$\boxed{g_{\mu\nu}}$$

$$\begin{aligned}g_{00} &= -\frac{\dot{H}(t)^2 p^2 - H(t)^2}{H(t)^2}, \\ g_{01} &= \frac{\dot{H}(t)p}{H(t)}, \\ g_{02} &= 0, \\ g_{03} &= 0, \\ g_{10} &= \frac{\dot{H}(t)p}{H(t)}, \\ g_{11} &= -1, \\ g_{12} &= 0, \\ g_{13} &= 0, \\ g_{20} &= 0, \\ g_{21} &= 0, \\ g_{22} &= -p^2, \\ g_{23} &= 0, \\ g_{30} &= 0, \\ g_{31} &= 0, \\ g_{32} &= 0, \\ g_{33} &= -p^2 \sin(\theta)^2.\end{aligned}$$

$$\boxed{\sqrt{\hspace{-.1cm}} = \sqrt{-\det(g_{\mu\nu})}}$$

$$\sqrt{\hspace{-.1cm}} = \sqrt{p^4 \sin(\theta)^2}.$$

$$\boxed{g^{\mu\nu}}$$

$$\begin{aligned}g^{00} &= 1, \\ g^{01} &= \frac{\dot{H}(t)p}{H(t)}, \\ g^{02} &= 0, \\ g^{03} &= 0, \\ g^{10} &= \frac{\dot{H}(t)p}{H(t)}, \\ g^{11} &= \frac{\dot{H}(t)^2 p^2 - H(t)^2}{H(t)^2}, \\ g^{12} &= 0, \\ g^{13} &= 0, \\ g^{20} &= 0, \\ g^{21} &= 0, \\ g^{22} &= -\frac{1}{p^2}, \\ g^{23} &= 0, \\ g^{30} &= 0, \\ g^{31} &= 0, \\ g^{32} &= 0, \\ g^{33} &= -\frac{1}{p^2 \sin(\theta)^2}.\end{aligned}$$

$$\boxed{\Gamma^\sigma_{\mu\nu}}$$

$$\begin{aligned}\Gamma^0_{00} &= \frac{\dot{H}(t)^3 p^2}{H(t)^3}, \\ \Gamma^0_{01} &= -\frac{\dot{H}(t)^2 p}{H(t)^2}, \\ \Gamma^0_{02} &= 0, \\ \Gamma^0_{03} &= 0, \\ \Gamma^0_{10} &= -\frac{\dot{H}(t)^2 p}{H(t)^2}, \\ \Gamma^0_{11} &= \frac{\dot{H}(t)}{H(t)}, \\ \Gamma^0_{12} &= 0, \\ \Gamma^0_{13} &= 0, \\ \Gamma^0_{20} &= 0, \\ \Gamma^0_{21} &= 0, \\ \Gamma^0_{22} &= \frac{\dot{H}(t)p^2}{H(t)}, \\ \Gamma^0_{23} &= 0, \\ \Gamma^0_{30} &= 0, \\ \Gamma^0_{31} &= 0, \\ \Gamma^0_{32} &= 0, \\ \Gamma^0_{33} &= \frac{\dot{H}(t)p^2 \sin(\theta)^2}{H(t)},\end{aligned}$$

$$\begin{aligned}\Gamma^1_{00} &= -\frac{pH(t)^3 \dot{H}(t) - \dot{H}(t)^4 p^3}{H(t)^4}, \\ \Gamma^1_{01} &= -\frac{\dot{H}(t)^3 p^2}{H(t)^3}, \\ \Gamma^1_{02} &= 0, \\ \Gamma^1_{03} &= 0, \\ \Gamma^1_{10} &= -\frac{\dot{H}(t)^3 p^2}{H(t)^3}, \\ \Gamma^1_{11} &= \frac{\dot{H}(t)^2 p}{H(t)^2}, \\ \Gamma^1_{12} &= 0, \\ \Gamma^1_{13} &= 0, \\ \Gamma^1_{20} &= 0, \\ \Gamma^1_{21} &= 0, \\ \Gamma^1_{22} &= \frac{p(\dot{H}(t)^2 p^2 - H(t)^2)}{H(t)^2}, \\ \Gamma^1_{23} &= 0, \\ \Gamma^1_{30} &= 0, \\ \Gamma^1_{31} &= 0, \\ \Gamma^1_{32} &= 0, \\ \Gamma^1_{33} &= \frac{p(\dot{H}(t)^2 p^2 - H(t)^2) \sin(\theta)^2}{H(t)^2}.\end{aligned}$$

$$\begin{aligned}\Gamma_{00}^2 &= 0, \\ \Gamma_{01}^2 &= 0, \\ \Gamma_{02}^2 &= 0, \\ \Gamma_{03}^2 &= 0, \\ \Gamma_{10}^2 &= 0, \\ \Gamma_{11}^2 &= 0, \\ \Gamma_{12}^2 &= \frac{1}{p}, \\ \Gamma_{13}^2 &= 0, \\ \Gamma_{20}^2 &= 0, \\ \Gamma_{21}^2 &= \frac{1}{p}, \\ \Gamma_{22}^2 &= 0, \\ \Gamma_{23}^2 &= 0, \\ \Gamma_{30}^2 &= 0, \\ \Gamma_{31}^2 &= 0, \\ \Gamma_{32}^2 &= 0, \\ \Gamma_{33}^2 &= -\cos(\theta)\sin(\theta).\end{aligned}$$

$$\begin{aligned}\Gamma_{00}^3 &= 0, \\ \Gamma_{01}^3 &= 0, \\ \Gamma_{02}^3 &= 0, \\ \Gamma_{03}^3 &= 0, \\ \Gamma_{10}^3 &= 0, \\ \Gamma_{11}^3 &= 0, \\ \Gamma_{12}^3 &= 0, \\ \Gamma_{13}^3 &= \frac{1}{p}, \\ \Gamma_{20}^3 &= 0, \\ \Gamma_{21}^3 &= 0, \\ \Gamma_{22}^3 &= 0, \\ \Gamma_{23}^3 &= \frac{\cos(\theta)}{\sin(\theta)}, \\ \Gamma_{30}^3 &= 0, \\ \Gamma_{31}^3 &= \frac{1}{p}, \\ \Gamma_{32}^3 &= \frac{\cos(\theta)}{\sin(\theta)}, \\ \Gamma_{33}^3 &= 0.\end{aligned}$$

$$\boxed{R_{\mu\nu}}$$

$$\begin{aligned}R_{00} &= -\frac{2\dot{H}(t)^4p^2-3H(t)^3\ddot{H}(t)+\dot{H}(t)^2p^2H(t)\ddot{H}(t)}{H(t)^4}, \\ R_{01} &= \frac{2\dot{H}(t)^3p+\dot{H}(t)pH(t)\ddot{H}(t)}{H(t)^3}, \\ R_{02} &= 0, \\ R_{03} &= 0, \\ R_{10} &= \frac{2\dot{H}(t)^3p+\dot{H}(t)pH(t)\ddot{H}(t)}{H(t)^3}, \\ R_{11} &= -\frac{H(t)\ddot{H}(t)+2\dot{H}(t)^2}{H(t)^2}, \\ R_{12} &= 0, \\ R_{13} &= 0, \\ R_{20} &= 0, \\ R_{21} &= 0, \\ R_{22} &= -\frac{2\dot{H}(t)^2p^2+p^2H(t)\ddot{H}(t)}{H(t)^2}, \\ R_{23} &= 0, \\ R_{30} &= 0, \\ R_{31} &= 0, \\ R_{32} &= 0, \\ R_{33} &= -\frac{p^2H(t)\ddot{H}(t)\sin(\theta)^2+2\dot{H}(t)^2p^2\sin(\theta)^2}{H(t)^2}.\end{aligned}$$

$$\boxed{R^\mu{}_\nu}$$

$$\begin{aligned}R^0_0 &= 3\frac{\ddot{H}(t)}{H(t)}, \\ R^0_1 &= 0, \\ R^0_2 &= 0, \\ R^0_3 &= 0, \\ R^1_0 &= -2\frac{\dot{H}(t)^2p}{H(t)^3}+2\frac{\dot{H}(t)p\ddot{H}(t)}{H(t)^2}, \\ R^1_1 &= 2\frac{\dot{H}(t)^2}{H(t)^2}+\frac{\ddot{H}(t)}{H(t)}, \\ R^1_2 &= 0, \\ R^1_3 &= 0, \\ R^2_0 &= 0, \\ R^2_1 &= 0, \\ R^2_2 &= 2\frac{\dot{H}(t)^2}{H(t)^2}+\frac{\ddot{H}(t)}{H(t)}, \\ R^2_3 &= 0, \\ R^3_0 &= 0, \\ R^3_1 &= 0, \\ R^3_2 &= 0, \\ R^3_3 &= 2\frac{\dot{H}(t)^2}{H(t)^2}+\frac{\ddot{H}(t)}{H(t)}.\end{aligned}$$

$$\boxed{R}$$

$$R=6\frac{\dot{H}(t)^2}{H(t)^2}+6\frac{\ddot{H}(t)}{H(t)}.$$

$$\boxed{G^{\mu}_{\nu}}$$

$$G^0_0=-3\frac{\dot{H}(t)^2}{H(t)^2}.$$

$$G^0_1=0.$$

$$G^0_2=0.$$

$$G^0_3=0.$$

$$G^1_0=-2\frac{\dot{H}(t)^3p}{H(t)^3}+2\frac{\dot{H}(t)p\ddot{H}(t)}{H(t)^2}.$$

$$G^1_1=-\frac{\dot{H}(t)^2}{H(t)^2}-2\frac{\ddot{H}(t)}{H(t)}.$$

$$G^1_2=0.$$

$$G^1_3=0.$$

$$G^2_0=0.$$

$$G^2_1=0.$$

$$G^2_2=-\frac{\dot{H}(t)^2}{H(t)^2}-2\frac{\ddot{H}(t)}{H(t)}.$$

$$G^2_3=0.$$

$$G^3_0=0.$$

$$G^3_1=0.$$

$$G^3_2=0.$$

$$G^3_3=-\frac{\dot{H}(t)^2}{H(t)^2}-2\frac{\ddot{H}(t)}{H(t)}.$$

$$\boxed{G}$$

$$G=-6\frac{\dot{H}(t)^2}{H(t)^2}-6\frac{\ddot{H}(t)}{H(t)}.$$

$$\boxed{G^{\mu}_{\nu;\mu}=0}$$

$$G^{\mu}_{0;\mu}=0.$$

$$G^{\mu}_{1;\mu}=0.$$

$$G^{\mu}_{2;\mu}=0.$$

$$G^{\mu}_{3;\mu}=0.$$

$$\boxed{g^{\mu\nu}\,\Gamma^{\lambda}_{\mu\nu}=0?}$$

$$g^{\mu\nu}\,\Gamma^0_{\mu\nu}=-\frac{\dot{H}(t)^5p^4}{H(t)^5}-\frac{\dot{H}(t)p^4}{H(t)}-\frac{\dot{H}(t)^3p^2}{H(t)^3}-\frac{\dot{H}(t)}{H(t)}-\frac{\dot{H}(t)p^4\sin(\theta)^4}{H(t)}.$$

$$g^{\mu\nu}\,\Gamma^1_{\mu\nu}=-\frac{p\dot{H}(t)}{H(t)}-\frac{\dot{H}(t)^2p}{H(t)^2}-\frac{\dot{H}(t)^2p^5}{H(t)^2}+p^3\sin(\theta)^4+\frac{\dot{H}(t)^2p^3\dot{H}(t)}{H(t)^3}+p^4-\frac{\dot{H}(t)^2p^5\sin(\theta)^4}{H(t)^2}-\frac{\dot{H}(t)^4p^3}{H(t)^4}-\frac{\dot{H}(t)^6p^5}{H(t)^6}.$$

$$g^{\mu\nu}\,\Gamma^2_{\mu\nu}=p^2\cos(\theta)\sin(\theta)^3.$$

$$g^{\mu\nu}\,\Gamma^3_{\mu\nu}=0.$$