

Schwarzschild Metric in spherical coordinates with a variable spherically symmetric matter density:

$$x^\mu$$

$$\begin{aligned}x^0 &= t. \\ x^1 &= r. \\ x^2 &= \theta. \\ x^3 &= \phi.\end{aligned}$$

$$g_{\mu\nu}$$

$$\begin{aligned}g_{00} &= 1 - \frac{8}{3}r^2\pi\epsilon(r). \\ g_{01} &= 0. \\ g_{02} &= 0. \\ g_{03} &= 0. \\ g_{10} &= 0. \\ g_{11} &= 3\frac{1}{-3 + 8\rho(r)r^2\pi}. \\ g_{12} &= 0. \\ g_{13} &= 0. \\ g_{20} &= 0. \\ g_{21} &= 0. \\ g_{22} &= -r^2. \\ g_{23} &= 0. \\ g_{30} &= 0. \\ g_{31} &= 0. \\ g_{32} &= 0. \\ g_{33} &= -r^2\sin(\theta)^2.\end{aligned}$$

$$\sqrt{\hspace{0.05cm}} = \sqrt{-\det(g_{\mu\nu})}$$

$$\sqrt{\hspace{0.05cm}} = \sqrt{-\frac{3r^4\sin(\theta)^2 - 8r^6\sin(\theta)^2\pi\epsilon(r)}{-3 + 8\rho(r)r^2\pi}}.$$

$$g^{\mu\nu}$$

$$\begin{aligned}g^{00} &= -3\frac{1}{-3 + 8r^2\pi\epsilon(r)}. \\ g^{01} &= 0. \\ g^{02} &= 0. \\ g^{03} &= 0. \\ g^{10} &= 0. \\ g^{11} &= -1 + \frac{8}{3}\rho(r)r^2\pi. \\ g^{12} &= 0. \\ g^{13} &= 0. \\ g^{20} &= 0. \\ g^{21} &= 0. \\ g^{22} &= -\frac{1}{r^2}. \\ g^{23} &= 0. \\ g^{30} &= 0. \\ g^{31} &= 0. \\ g^{32} &= 0. \\ g^{33} &= -\frac{1}{r^2\sin(\theta)^2}.\end{aligned}$$

$$\Gamma^\sigma_{\mu\nu}$$

$$\begin{aligned}\Gamma^0_{00} &= 0. \\ \Gamma^0_{01} &= 4\frac{c'(r)r^2\pi + 2r\pi\epsilon(r)}{-3 + 8r^2\pi\epsilon(r)}. \\ \Gamma^0_{02} &= 0. \\ \Gamma^0_{03} &= 0. \\ \Gamma^0_{10} &= 4\frac{c'(r)r^2\pi + 2r\pi\epsilon(r)}{-3 + 8r^2\pi\epsilon(r)}. \\ \Gamma^0_{11} &= 0. \\ \Gamma^0_{12} &= 0. \\ \Gamma^0_{13} &= 0. \\ \Gamma^0_{20} &= 0. \\ \Gamma^0_{21} &= 0. \\ \Gamma^0_{22} &= 0. \\ \Gamma^0_{23} &= 0. \\ \Gamma^0_{30} &= 0. \\ \Gamma^0_{31} &= 0. \\ \Gamma^0_{32} &= 0. \\ \Gamma^0_{33} &= 0.\end{aligned}$$

$$\begin{aligned}\Gamma^1_{00} &= \frac{4}{9}(-3 + 8\rho(r)r^2\pi)(c'(r)r^2\pi + 2r\pi\epsilon(r)). \\ \Gamma^1_{01} &= 0. \\ \Gamma^1_{02} &= 0. \\ \Gamma^1_{03} &= 0. \\ \Gamma^1_{10} &= 0. \\ \Gamma^1_{11} &= -4\frac{\rho'(r)r^2\pi + 2\rho(r)r\pi}{-3 + 8\rho(r)r^2\pi}. \\ \Gamma^1_{12} &= 0. \\ \Gamma^1_{13} &= 0. \\ \Gamma^1_{20} &= 0. \\ \Gamma^1_{21} &= 0. \\ \Gamma^1_{22} &= \frac{1}{3}r(-3 + 8\rho(r)r^2\pi). \\ \Gamma^1_{23} &= 0. \\ \Gamma^1_{30} &= 0. \\ \Gamma^1_{31} &= 0. \\ \Gamma^1_{32} &= 0. \\ \Gamma^1_{33} &= \frac{1}{3}r(-3 + 8\rho(r)r^2\pi)\sin(\theta)^2.\end{aligned}$$

$$\begin{aligned}\Gamma_{00}^2 &= 0. \\ \Gamma_{01}^2 &= 0. \\ \Gamma_{02}^2 &= 0. \\ \Gamma_{03}^2 &= 0. \\ \Gamma_{10}^2 &= 0. \\ \Gamma_{11}^2 &= 0. \\ \Gamma_{12}^2 &= \frac{1}{r}. \\ \Gamma_{13}^2 &= 0. \\ \Gamma_{20}^2 &= 0. \\ \Gamma_{21}^2 &= \frac{1}{r}. \\ \Gamma_{22}^2 &= 0. \\ \Gamma_{23}^2 &= 0. \\ \Gamma_{30}^2 &= 0. \\ \Gamma_{31}^2 &= 0. \\ \Gamma_{32}^2 &= 0. \\ \Gamma_{33}^2 &= -\cos(\theta)\sin(\theta).\end{aligned}$$

$$\begin{aligned}\Gamma_{00}^3 &= 0. \\ \Gamma_{01}^3 &= 0. \\ \Gamma_{02}^3 &= 0. \\ \Gamma_{03}^3 &= 0. \\ \Gamma_{10}^3 &= 0. \\ \Gamma_{11}^3 &= 0. \\ \Gamma_{12}^3 &= 0. \\ \Gamma_{13}^3 &= \frac{1}{r}. \\ \Gamma_{20}^3 &= 0. \\ \Gamma_{21}^3 &= 0. \\ \Gamma_{22}^3 &= 0. \\ \Gamma_{23}^3 &= \frac{\cos(\theta)}{\sin(\theta)}. \\ \Gamma_{30}^3 &= 0. \\ \Gamma_{31}^3 &= \frac{1}{r}. \\ \Gamma_{32}^3 &= \frac{\cos(\theta)}{\sin(\theta)}. \\ \Gamma_{33}^3 &= 0.\end{aligned}$$

$$\tilde{x}^\mu = (\Gamma^0_{\sigma\rho}\tilde{x}^\mu - \Gamma^\mu_{\sigma\rho})\,\tilde{x}^\sigma\tilde{x}^\rho$$

$$\begin{aligned}\tilde{x}^0 &= 0. \\ \tilde{x}^1 &= \frac{1}{9}\frac{216\epsilon'(r)\dot{x}^2r^2\pi+576\epsilon'(r)\rho(r)r^4\pi^2-288\dot{x}^2\rho'(r)r^4\pi^2\epsilon(r)-108\epsilon'(r)r^2\pi-1536\epsilon'(r)\rho(r)r^6\pi^3\epsilon(r)+1536\rho(r)^2r^7\sin(\theta)^2\pi^3\epsilon(r)\dot{z}^2+576r^3\pi^2\epsilon(r)^2+2048\epsilon'(r)\rho(r)^2r^8\pi^4\epsilon(r)+432\rho(r)r^3\sin(\theta)^2\pi\dot{z}^2+108\dot{x}^2\rho'(r)r^2\pi-1152\rho(r)r^5\sin(\theta)^2\pi^2\epsilon(r)\dot{z}^2-576\epsilon'(r)\dot{x}^2\rho(r)r^4\pi^2+288\epsilon'(r)r^4\pi^2\epsilon(r)-81r\sin(\theta)^2\dot{z}^2-3072\rho(r)r^5\pi^3\epsilon(r)^2-1536\rho(r)^2r^5\pi^3\epsilon(r)-576\rho(r)^2r^5\sin(\theta)^2\pi^2\dot{z}^2+216r^3\sin(\theta)^2\pi\epsilon(r)\dot{z}^2-768\epsilon'(r)\rho(r)^2r^6\pi^3+4096\rho(r)^2r^7\pi^4\epsilon(r)^2+216\dot{x}^2\rho(r)r\pi-216r\pi\epsilon(r)-1728\dot{x}^2\rho(r)r^3\pi^2\epsilon(r)+432\dot{x}^2r\pi\epsilon(r)+1152\rho(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))(-3+8\rho(r)r^2\pi)}. \\ \tilde{x}^2 &= \cos(\theta)\sin(\theta)\dot{z}^2. \\ \tilde{x}^3 &= 2\frac{3\dot{x}\dot{z}+4\epsilon'(r)\dot{x}r^3\pi\dot{z}}{(-3+8r^2\pi\epsilon(r))r}.\end{aligned}$$

$$R_{\mu\nu}$$

$$\begin{aligned}R_{00} &= -\frac{4}{9}\frac{12\epsilon'(r)^2r^4\pi^2+9\epsilon''(r)r^2\pi-12\epsilon'(r)\rho'(r)r^4\pi^2-24\epsilon''(r)\rho(r)r^4\pi^2+384\rho(r)r^4\pi^3\epsilon(r)^2+32\epsilon'(r)\rho(r)r^6\pi^3\epsilon(r)-192\rho(r)r^2\pi^2\epsilon(r)+64\rho'(r)r^5\pi^3\epsilon(r)^2+64\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r)-24\epsilon''(r)r^4\pi^2\epsilon(r)-96r^2\pi^2\epsilon(r)^2-96\epsilon'(r)r^3\pi^2\epsilon(r)+54\pi\epsilon(r)+320\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r)-24\rho'(r)r^3\pi^2\epsilon(r)-168\epsilon'(r)\rho(r)r^3\pi^2-32\epsilon'(r)^2\rho(r)r^6\pi^3+54\epsilon'(r)r\pi}{-3+8r^2\pi\epsilon(r)}. \\ R_{01} &= 0. \\ R_{02} &= 0. \\ R_{03} &= 0. \\ R_{10} &= 0. \\ R_{11} &= 4\frac{12\epsilon'(r)^2r^4\pi^2+9\epsilon''(r)r^2\pi-12\epsilon'(r)\rho'(r)r^4\pi^2-24\epsilon''(r)\rho(r)r^4\pi^2+384\rho(r)r^4\pi^3\epsilon(r)^2+32\epsilon'(r)\rho'(r)r^6\pi^3\epsilon(r)-288\rho(r)r^2\pi^2\epsilon(r)+192\rho'(r)r^5\pi^3\epsilon(r)^2+64\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r)+36\rho(r)\pi-24\epsilon''(r)r^4\pi^2\epsilon(r)-48\epsilon'(r)r^3\pi^2\epsilon(r)+18\pi\epsilon(r)+18\rho'(r)r\pi+192\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r)-120\rho'(r)r^3\pi^2\epsilon(r)-120\epsilon'(r)\rho(r)r^3\pi^2-32\epsilon'(r)^2\rho(r)r^6\pi^3+36\epsilon'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2(-3+8\rho(r)r^2\pi)}. \\ R_{12} &= 0. \\ R_{13} &= 0. \\ R_{20} &= 0. \\ R_{21} &= 0. \\ R_{22} &= \frac{4}{3}\frac{6r^2\pi\epsilon(r)-48\rho(r)r^4\pi^2\epsilon(r)-8\epsilon'(r)\rho(r)r^5\pi^2+12\rho(r)r^2\pi+3\epsilon'(r)r^3\pi-8\rho'(r)r^5\pi^2\epsilon(r)+3\rho'(r)r^3\pi}{-3+8r^2\pi\epsilon(r)}. \\ R_{23} &= 0. \\ R_{30} &= 0. \\ R_{31} &= 0. \\ R_{32} &= 0. \\ R_{33} &= -\frac{4}{3}\frac{48\rho(r)r^4\sin(\theta)^2\pi^2\epsilon(r)-6r^2\sin(\theta)^2\pi\epsilon(r)-12\rho(r)r^2\sin(\theta)^2\pi-3\epsilon'(r)r^3\sin(\theta)^2\pi+8\rho'(r)r^5\sin(\theta)^2\pi^2\epsilon(r)+8\epsilon'(r)\rho(r)r^5\sin(\theta)^2\pi^2-3\rho'(r)r^3\sin(\theta)^2\pi}{-3+8r^2\pi\epsilon(r)}.\end{aligned}$$

$$R_{\nu}^{\mu}$$

$$\begin{aligned}R_0^0 &= 72\frac{\epsilon'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2}+\frac{256}{3}\frac{\rho'(r)r^5\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+512\frac{\rho(r)r^4\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+\frac{128}{3}\frac{\epsilon'(r)\rho'(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-224\frac{\epsilon'(r)\rho(r)r^3\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-128\frac{\epsilon'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-128\frac{r^2\pi^2\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+72\frac{\pi\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-256\frac{\rho(r)r^2\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-16\frac{\epsilon'(r)\rho'(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-32\frac{\rho'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+16\frac{\epsilon'(r)^2r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}+\frac{1280}{3}\frac{\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+12\frac{\epsilon''(r)r^2\pi}{(-3+8r^2\pi\epsilon(r))^2}-\frac{128}{3}\frac{\epsilon'(r)^2\rho(r)r^6\pi^3}{(-3+8r^2\pi\epsilon(r))^2}+\frac{256}{3}\frac{\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-32\frac{\epsilon''(r)\rho(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-32\frac{\epsilon''(r)r^4\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}. \\ R_1^0 &= 0. \\ R_2^0 &= 0. \\ R_3^0 &= 0. \\ R_0^1 &= 0. \\ R_1^1 &= 48\frac{\epsilon'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2}+256\frac{\rho'(r)r^5\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+512\frac{\rho(r)r^4\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+48\frac{\rho(r)\pi}{(-3+8r^2\pi\epsilon(r))^2}+\frac{128}{3}\frac{\epsilon'(r)\rho'(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-160\frac{\epsilon'(r)\rho(r)r^3\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-64\frac{\epsilon'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+24\frac{\pi\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+24\frac{\rho'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2}-384\frac{\rho(r)r^2\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-16\frac{\epsilon'(r)\rho'(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-160\frac{\rho'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+16\frac{\epsilon'(r)^2r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}+256\frac{\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+12\frac{\epsilon''(r)r^2\pi}{(-3+8r^2\pi\epsilon(r))^2}-\frac{128}{3}\frac{\epsilon'(r)^2\rho(r)r^6\pi^3}{(-3+8r^2\pi\epsilon(r))^2}+\frac{256}{3}\frac{\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-32\frac{\epsilon''(r)\rho(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-32\frac{\epsilon''(r)r^4\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}. \\ R_2^1 &= 0. \\ R_3^1 &= 0. \\ R_0^2 &= 0. \\ R_1^2 &= 0. \\ R_2^2 &= \frac{32}{3}\frac{\rho'(r)r^3\pi^2\epsilon(r)}{-3+8r^2\pi\epsilon(r)}+\frac{32}{3}\frac{\epsilon'(r)\rho(r)r^3\pi^2}{-3+8r^2\pi\epsilon(r)}-8\frac{\pi\epsilon(r)}{-3+8r^2\pi\epsilon(r)}-4\frac{\rho'(r)r\pi}{-3+8r^2\pi\epsilon(r)}-4\frac{\epsilon'(r)r\pi}{-3+8r^2\pi\epsilon(r)}+64\frac{\rho(r)r^2\pi^2\epsilon(r)}{-3+8r^2\pi\epsilon(r)}-16\frac{\rho(r)\pi}{-3+8r^2\pi\epsilon(r)}. \\ R_3^2 &= 0. \\ R_0^3 &= 0. \\ R_1^3 &= 0. \\ R_2^3 &= 0. \\ R_3^3 &= \frac{32}{3}\frac{\rho'(r)r^3\pi^2\epsilon(r)}{-3+8r^2\pi\epsilon(r)}+\frac{32}{3}\frac{\epsilon'(r)\rho(r)r^3\pi^2}{-3+8r^2\pi\epsilon(r)}-8\frac{\pi\epsilon(r)}{-3+8r^2\pi\epsilon(r)}-4\frac{\rho'(r)r\pi}{-3+8r^2\pi\epsilon(r)}-4\frac{\epsilon'(r)r\pi}{-3+8r^2\pi\epsilon(r)}+64\frac{\rho(r)r^2\pi^2\epsilon(r)}{-3+8r^2\pi\epsilon(r)}-16\frac{\rho(r)\pi}{-3+8r^2\pi\epsilon(r)}.\end{aligned}$$

$$[R]$$

$$R=144\frac{\epsilon'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2}+512\frac{\rho'(r)r^5\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+2048\frac{\rho(r)r^4\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+144\frac{\rho(r)\pi}{(-3+8r^2\pi\epsilon(r))^2}+\frac{256}{3}\frac{\epsilon'(r)\rho'(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-448\frac{\epsilon'(r)\rho(r)r^3\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-256\frac{\epsilon'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-256\frac{r^2\pi^2\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}+144\frac{\pi\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+48\frac{\rho'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2}-1280\frac{\rho(r)r^2\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-32\frac{\epsilon'(r)\rho'(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-320\frac{\rho'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+32\frac{\epsilon'(r)^2r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}+\frac{2560}{3}\frac{\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+24\frac{\epsilon''(r)r^2\pi}{(-3+8r^2\pi\epsilon(r))^2}-\frac{256}{3}\frac{\epsilon'(r)^2\rho(r)r^6\pi^3}{(-3+8r^2\pi\epsilon(r))^2}+\frac{512}{3}\frac{\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-64\frac{\epsilon''(r)\rho(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-64\frac{\epsilon''(r)r^4\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}.$$

$$\boxed{G^{\mu}_{\nu}}$$

$$\begin{aligned} G^0_0 &= -8\rho(r)\pi - \frac{8}{3}\rho'(r)r\pi. \\ G^1_1 &= 0. \\ G^0_2 &= 0. \\ G^0_3 &= 0. \\ G^1_0 &= 0. \\ G^1_1 &= -\frac{8}{3}\frac{24\rho(r)r^2\pi^2\epsilon(r) - 3\rho(r)\pi - 6\pi\epsilon(r) + 8\epsilon'(r)\rho(r)r^3\pi^2 - 3\epsilon'(r)r\pi}{-3 + 8r^2\pi\epsilon(r)}. \\ G^1_2 &= 0. \\ G^1_3 &= 0. \\ G^2_0 &= 0. \\ G^2_1 &= 0. \\ G^2_2 &= -\frac{4}{3}\frac{12\epsilon'(r)^2r^4\pi^2 + 9\epsilon''(r)r^2\pi - 12\epsilon'(r)\rho'(r)r^4\pi^2 - 24\epsilon''(r)\rho(r)r^4\pi^2 + 384\rho(r)r^4\pi^3\epsilon(r)^2 + 32\epsilon'(r)\rho'(r)r^6\pi^3\epsilon(r) - 240\rho(r)r^2\pi^2\epsilon(r) + 128\rho'(r)r^5\pi^3\epsilon(r)^2 + 64\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r) + 18\rho(r)\pi - 24\epsilon''(r)r^4\pi^2\epsilon(r) - 48r^2\pi^2\epsilon(r)^2 - 72\epsilon'(r)r^3\pi^2\epsilon(r) + 36\pi\epsilon(r) + 9\rho'(r)r\pi + 256\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r) - 72\rho'(r)r^3\pi^2\epsilon(r) - 144\epsilon'(r)\rho(r)r^3\pi^2 - 32\epsilon'(r)^2\rho(r)r^6\pi^3 + 45\epsilon'(r)r\pi}{(-3 + 8r^2\pi\epsilon(r))^2}. \\ G^2_3 &= 0. \\ G^3_0 &= 0. \\ G^3_1 &= 0. \\ G^3_2 &= 0. \\ G^3_3 &= -\frac{4}{3}\frac{12\epsilon'(r)^2r^4\pi^2 + 9\epsilon''(r)r^2\pi - 12\epsilon'(r)\rho'(r)r^4\pi^2 - 24\epsilon''(r)\rho(r)r^4\pi^2 + 384\rho(r)r^4\pi^3\epsilon(r)^2 + 32\epsilon'(r)\rho'(r)r^6\pi^3\epsilon(r) - 240\rho(r)r^2\pi^2\epsilon(r) + 128\rho'(r)r^5\pi^3\epsilon(r)^2 + 64\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r) + 18\rho(r)\pi - 24\epsilon''(r)r^4\pi^2\epsilon(r) - 48r^2\pi^2\epsilon(r)^2 - 72\epsilon'(r)r^3\pi^2\epsilon(r) + 36\pi\epsilon(r) + 9\rho'(r)r\pi + 256\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r) - 72\rho'(r)r^3\pi^2\epsilon(r) - 144\epsilon'(r)\rho(r)r^3\pi^2 - 32\epsilon'(r)^2\rho(r)r^6\pi^3 + 45\epsilon'(r)r\pi}{(-3 + 8r^2\pi\epsilon(r))^2}. \end{aligned}$$

$$\boxed{G}$$

$$G=-144\frac{\epsilon'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2}-512\frac{\rho'(r)r^5\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}-2048\frac{\rho(r)r^4\pi^3\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}-144\frac{\rho(r)\pi}{(-3+8r^2\pi\epsilon(r))^2}-\frac{256}{3}\frac{\epsilon'(r)\rho'(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+448\frac{\epsilon'(r)\rho(r)r^3\pi^2}{(-3+8r^2\pi\epsilon(r))^2}+256\frac{\epsilon'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+256\frac{r^2\pi^2\epsilon(r)^2}{(-3+8r^2\pi\epsilon(r))^2}-144\frac{\pi\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-48\frac{\rho'(r)r\pi}{(-3+8r^2\pi\epsilon(r))^2}+1280\frac{\rho(r)r^2\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+32\frac{\epsilon'(r)\rho'(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}+320\frac{\rho'(r)r^3\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-32\frac{\epsilon'(r)^2r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}-\frac{2560}{3}\frac{\epsilon'(r)\rho(r)r^5\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}-24\frac{\epsilon''(r)r^2\pi}{(-3+8r^2\pi\epsilon(r))^2}+\frac{256}{3}\frac{\epsilon'(r)^2\rho(r)r^6\pi^3}{(-3+8r^2\pi\epsilon(r))^2}-\frac{512}{3}\frac{\epsilon''(r)\rho(r)r^6\pi^3\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}+64\frac{\epsilon''(r)\rho(r)r^4\pi^2}{(-3+8r^2\pi\epsilon(r))^2}+64\frac{\epsilon''(r)r^4\pi^2\epsilon(r)}{(-3+8r^2\pi\epsilon(r))^2}.$$

$$\boxed{G^{\mu}_{\nu,\mu}=0}$$

$$\begin{aligned} G^e_{0,\mu} &= 0. \\ G^u_{1,\mu} &= 0. \\ G^\mu_{2,\mu} &= 0. \\ G^s_{3,\mu} &= 0. \end{aligned}$$

$$\boxed{g^{\mu\nu}\,\Gamma^{\lambda}_{\mu\nu}=0?}$$

$$\begin{aligned} g^{\mu\nu}\,\Gamma^0_{\mu\nu} &= 0. \\ g^{\mu\nu}\,\Gamma^1_{\mu\nu} &= \frac{2048}{9}\frac{\epsilon'(r)\rho(r)r^3r^8\pi^4}{(-3+8\rho(r)r^2\pi)^2}-72\frac{\rho(r)r^5\pi}{(-3+8\rho(r)r^2\pi)^2}+\frac{2048}{3}\frac{\epsilon'(r)\rho(r)r^2r^8\pi^4\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}-24\frac{r\pi\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}+\frac{4096}{9}\frac{\rho(r)^3r^7\pi^4\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}-512\frac{\rho(r)r^5\pi^3\epsilon(r)^2}{(-3+8\rho(r)r^2\pi)^2}-12\frac{\rho'(r)r^2\pi}{(-3+8\rho(r)r^2\pi)^2}+32\frac{\epsilon'(r)r^4\pi^2\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}-12\frac{\epsilon'(r)r^2\pi}{(-3+8\rho(r)r^2\pi)^2}-\frac{16384}{27}\frac{\epsilon'(r)\rho(r)^3r^{10}\pi^2\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}+192\frac{\rho(r)r^3\pi^2\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}+192\frac{\rho(r)^2r^7\pi^2}{(-3+8\rho(r)r^2\pi)^2}-512\frac{\rho(r)^2r^5\pi^3\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}-256\frac{\epsilon'(r)\rho(r)r^6\pi^3\epsilon(r)}{(-3+8\rho(r)r^2\pi)^2}+64\frac{r^3\pi^2\epsilon(r)^2}{(-3+8\rho(r)r^2\pi)^2}+192\frac{\rho(r)^2r^7\sin(\theta)^4\pi^2}{(-3+8\rho(r)r^2\pi)^2}-72\frac{\rho(r)r^5\sin(\theta)^4\pi}{(-3+8\rho(r)r^2\pi)^2}+\frac{4096}{3}\frac{\rho(r)^2r^7\pi^4\epsilon(r)^2}{(-3+8\rho(r)r^2\pi)^2}+0\frac{r^3\sin(\theta)^4}{(-3+8\rho(r)r^2\pi)^2}-256\frac{\epsilon'(r)\rho(r)^2r^6\pi^3}{(-3+8\rho(r)r^2\pi)^2}-\frac{512}{3}\frac{\rho(r)^3r^9\pi^3}{(-3+8\rho(r)r^2\pi)^2}-24\frac{\rho(r)r\pi}{(-3+8\rho(r)r^2\pi)^2}. \\ g^{\mu\nu}\,\Gamma^2_{\mu\nu} &= \cos(\theta)r^2\sin(\theta)^3. \\ g^{\mu\nu}\,\Gamma^3_{\mu\nu} &= 0. \end{aligned}$$